

A COMPREHENSIVE UNCERTAINTY FRAMEWORK FOR HISTORICAL FLOOD FREQUENCY ANALYSIS: A 500-YEAR LONG CASE STUDY.

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Abstract

The value of historical data for flood frequency analysis has been acknowledged and studied for a long time. A specific statistical framework must be used to comply with the censored nature of historical data, for which only floods large enough to induce written records or to trigger flood marks are usually recorded. It is assumed that all floods having exceeded a given perception threshold were recorded as written testimonies or flood marks. Conversely, all years without a flood record in the historical period are assumed to have a maximum discharge below the perception threshold. This paper proposes a Binomial model which explicitly recognizes the uncertain nature of both the perception threshold and the starting date of the historical period. This model is applied to a case study for the Rhône River at Beaucaire, France, where a long (1816-2020) systematic series of annual maximum discharges is available along with a collection of 13 historical floods from documentary evidences over three centuries (1500-1815). Results indicate that the inclusion of historical floods reduces the uncertainty of 100- or 1000-year flood quantiles, even when only the number of perception threshold exceedances is known. However, ignoring the uncertainty around the perception threshold leads to a noticeable underestimation of flood quantiles uncertainty. A qualitatively similar conclusion is found when ignoring the uncertainty around the historical period length. However, its impact on flood quantiles uncertainty appears to be much smaller than that of the perception threshold.

Keywords

Flood frequency analysis

Historical data

Perception threshold

Historical period length

Uncertainty

Rhône River

1. Introduction

Flood Frequency Analysis (FFA) provides information on the magnitude and frequency of flood discharges. It is used to estimate the probability of flooding and manage the risk posed by floods to human health, the environment, the economy and cultural heritage (European Union, 2007). One of the main concerns in FFA is the difficulty to precisely estimate the parameters of the chosen distribution with discharge series of limited length (a few decades, generally). This is particularly problematic when low-probability (e.g. annual exceedance probability 10^{-3} or 10^{-4}) design floods are required to ensure the safety of people and hydraulic structures (Apel *et al.*, 2004; Kjeldsen *et al.*, 2014). Fortunately, sampling uncertainty can be reduced by providing additional information beyond the flood sample obtained from discharge

44 monitoring stations during a *systematic* period. Such information can be temporal (e.g.
45 historical data on ancient floods), regional (e.g. discharge data from similar catchments), causal
46 (e.g. rainfall data) (Merz and Blöschl, 2008), or a combination of these (Macdonald and
47 Sangster, 2017). This paper focuses on the first option and on the treatment of historical data in
48 FFA.

49 Historical data can take a variety of forms. Historical data may be issued from testimonials
50 (Pichard, 1995; Kjeldsen *et al.*, 2014), flood marks (Parkes and Demeritt, 2016; Piotte *et al.*,
51 2016; Engeland *et al.*, 2020; METS, 2023; Renard, 2023), or paleoflood reconstructions derived
52 from various proxies such as sedimentary deposits or riparian tree rings (Stedinger and Cohn,
53 1986; Benito *et al.*, 2004; Dezileau *et al.*, 2014; St. George *et al.*, 2020; Engeland *et al.*, 2020).
54 Using historical data in FFA has a long history and is now a well-established practice. Benson
55 (1950) and Hirsch (1987) first focused on plotting position formulas for historical floods.
56 Various types of historical data can be incorporated in FFA by selecting an adequate likelihood
57 function (Stedinger and Cohn, 1986; Kuczera, 1999). Parameter estimation is often performed
58 in a Bayesian way using Markov Chain Monte Carlo (MCMC) algorithms (Reis and Stedinger,
59 2005). Most recent studies emphasize the need to take full account of uncertainties (Neppel *et al.*,
60 2010; Kjeldsen *et al.* 2014; Parkes and Demeritt, 2016; Shang *et al.*, 2021; Sharma *et al.*,
61 2022). Although discharges from the systematic period are generally much better known than
62 those from the historical period, they are still affected by uncertainties. However, those
63 uncertainties are often neglected when using historical data. Only a few works propose to take
64 them into account: Reis and Stedinger (2005) or Parkes and Demeritt (2016) consider discharge
65 uncertainty during the systematic period via the use of a fixed percentage error, while Neppel
66 *et al.* (2010) use unknown multiplicative errors.

67 Historical flood data are not systematic: only floods large enough to induce written records or
68 to trigger flood marks are recorded. Such censored data can be analysed statistically thanks to
69 the perception threshold concept (Gerard and Karpuk, 1979; Stedinger and Cohn, 1986). The
70 assumption is that all floods exceeding this perception threshold were recorded, thus ensuring
71 the completeness of the historical flood record above the threshold. As a corollary, the annual
72 maximum flood can be assumed to be smaller than the perception threshold for all years in the
73 historical period with no recorded flood. It is possible, albeit not mandatory, to reconstruct the
74 discharge of historical floods above the perception threshold via the use of hydraulic models
75 (Lang *et al.*, 2004; Neppel *et al.*, 2010; Machado *et al.*, 2015). In cases where such
76 reconstruction is too complex, the sole knowledge of the number of floods having exceeded the
77 perception threshold during the historical period can be exploited by means of a Binomial
78 distribution, as described by Stedinger and Cohn (1986) or Payraastre *et al.* (2011). This
79 description highlights two key quantities in historical FFA that constitute the main focus of this
80 paper: the perception threshold and the length of the historical period.

81 The perception threshold is an empirical concept that only takes a physical meaning in specific
82 cases. The ideal situation corresponds to the availability of a cross-section that has not changed
83 over time, with overflows always occurring above the same discharge and systematically
84 leaving a trace in written records or on infrastructures (flood marks) as a result of the damage

85 caused. In such a situation, expressing the perception threshold as a precisely-estimated
86 discharge value is feasible. However, this ideal situation rarely holds, and the estimation of the
87 perception threshold can be undermined by many factors including the difficulty to precisely
88 estimate discharge, the temporally-varying perception of flood damages by populations living
89 adjacent to the river, etc. In spite of such uncertainties, the perception threshold is assumed to
90 be perfectly known in the vast majority of studies, although the sensitivity of results to the
91 perception threshold is often explored (Stedinger and Cohn, 1986, Viglione *et al.*, 2013;
92 Macdonald *et al.*, 2014; Payraastre *et al.*, 2011; Parkes and Demeritt, 2016).

93 The length of the historical period is generally considered to be perfectly known in the historical
94 FFA methods of the literature. In principle, the historical period (or surveying period) should
95 start at the date when the source of the historical information started to exist. However, it is
96 generally assumed to start with the first known flood and to finish with the starting date of the
97 systematic period. Prosdocimi (2018) showed that this leads to a systematic underestimation of
98 the length of the historical period and proposes an unbiased estimator of the starting date of the
99 historical period. However, this unbiased estimator is still treated as a known value in the
100 subsequent FFA procedure, whereas it is affected by considerable uncertainty.

101 This paper presents an FFA probabilistic model that uses the number of times a perception
102 threshold is exceeded over an historical period, and takes into account the uncertainty of
103 discharges during the systematic period. The key originality of this model is to recognize the
104 imperfectly-known nature of both the perception threshold and the length of the historical
105 period by making them parameters of the probabilistic model. The aim is to correctly assess the
106 uncertainties of flood quantiles, based on historical information.

107 This FFA model and several variants are applied to a case study based on the Rhône River at
108 Beaucaire, France, offering a very long systematic record (1816-2020, 205 years), with
109 discharge uncertainties carefully determined. An uncertainty propagation chain developed by
110 Lucas *et al.* (2023) accounts for errors on stage and gauging measurements, and rating curve
111 estimation. In a first step, the 205-year systematic record is artificially subsampled in order to
112 mimic a typical mixed dataset containing about 50 years of systematic data and about 150 years
113 of censored historical data. This allows testing of the FFA models on a real-world dataset, with
114 the full 205-year systematic dataset providing a precise baseline against which comparisons can
115 be made. The added value of precisely knowing the discharge of historical floods vs. only
116 knowing the number of perception threshold exceedances is also explored. In a second step, the
117 same FFA models are then applied to the 1816-2020 systematic record and a collection of
118 historical floods during the 1500-1815 period (Pichard and Roucaute, 2014). The impact of the
119 various sources of uncertainty on quantile estimates is discussed.

120 This paper is organized as follows. Methods for historical FFA are introduced in section 2.
121 Available data are presented in section 3 and their stationarity is verified. The FFA models are
122 then applied and compared using the artificially subsampled record on the 1816-2020 period
123 (section 4), and then to the entire dataset on the 1500-2020 period (section 5). Section 6
124 discusses some key results of this work and section 7 summarizes its main conclusions.

125 2. Probabilistic models

126 We first present how censored historical floods can be included into a probabilistic model
 127 (section 2.1) and then move towards more specific models accounting for uncertainties (section
 128 2.2).

129 2.1 Standard treatment of censored data

130 Likelihood function

131 We assume that the annual maximum (AMAX) discharge Q during systematic and historical
 132 periods is an *i.i.d.* (independent and identically distributed) random variable that follows a
 133 Generalized Extreme Value (GEV) distribution, with location, scale, shape parameters $\boldsymbol{\theta} = (\mu,$
 134 $\sigma, \zeta)$. When the shape parameter ζ is non-zero, the GEV cumulative distribution function (cdf)
 135 and the probability density function (pdf) are:

$$136 \quad F(q; \boldsymbol{\theta}) = \exp \left[- \left(1 - \xi \frac{q - \mu}{\sigma} \right)^{1/\xi} \right]$$

(1)

$$f(q; \boldsymbol{\theta}) = \frac{\partial F(q; \boldsymbol{\theta})}{\partial q} = \frac{1}{\sigma} \left(1 - \xi \frac{q - \mu}{\sigma} \right)^{1/\xi - 1} F(q; \boldsymbol{\theta}).$$

137 Under this parametrization, a positive shape parameter ($\zeta > 0$) corresponds to an upper-bounded
 138 distribution with quantiles lower than those of the corresponding Gumbel distribution. In the
 139 opposite case ($\zeta < 0$), the distribution is heavy-tailed with above-Gumbel quantiles. The Gumbel
 140 case is obtained by continuity when ζ tends to zero.

141 The sample of AMAX discharges during the systematic period covering j years is noted $\mathbf{q} =$
 142 $(q_t)_{t=1,j}$. For the time being discharges are supposed to be perfectly known and not affected
 143 by any uncertainty. The historical sample is made of k events having exceeded the perception
 144 threshold S over a period of n years. Therefore, the perception threshold was not exceeded over
 145 the remaining $(n - k)$ years. The probability π of exceeding the threshold S can be written as:

$$146 \quad \pi = (1 - F(S; \boldsymbol{\theta})) = 1 - \exp \left[- \left(1 - \xi \frac{S - \mu}{\sigma} \right)^{1/\xi} \right]$$

(2)

147 It is assumed that k , the number of exceedances of the perception threshold, follows a Binomial
 148 distribution $\mathcal{B}(n, \pi)$. The likelihood function of a mixed sample of AMAX discharges \mathbf{q} during
 149 the systematic period spanning j years and the number k of exceedances of the perception
 150 threshold S during the historical period spanning n years is:

$$151 \quad L(\boldsymbol{\theta}; \mathbf{q}, k) = \underbrace{\prod_{t=1}^j f(q_t; \boldsymbol{\theta})}_{(a)} \underbrace{\left[\binom{n}{k} (F(S; \boldsymbol{\theta}))^{n-k} (1 - F(S; \boldsymbol{\theta}))^k \right]}_{(b)}$$

(3)

152 Here, term (a) in Eq. (3) represents the likelihood for systematic data and term (b) in Eq. (3)
 153 represents the likelihood for historical data. By applying Bayes formula, the posterior
 154 distribution $p(\boldsymbol{\theta}|\mathbf{q}, k)$ of parameters $\boldsymbol{\theta}$ given systematic and historical data is:

$$155 \quad p(\boldsymbol{\theta}|\mathbf{q}, k) \propto L(\boldsymbol{\theta}; \mathbf{q}, k)p(\boldsymbol{\theta})$$

(4)

156 The term $p(\theta)$ represents the prior distribution of the parameters and needs to be elicited before
 157 inference. The posterior distribution $p(\theta|q, k)$ is explored via a MCMC method (Renard *et al.*,
 158 2006), leading to a representation of sampling uncertainty by means of r parameter vectors
 159 $\Theta = (\theta_1, \dots, \theta_r)$. The parameter vector $\hat{\theta}$ that maximizes the posterior distribution is called
 160 *maxpost*. Thereafter, the prior distribution $p(\theta)$ of the GEV parameters will be as follows: a
 161 positive Uniform distribution for μ and σ , and a Gaussian distribution with mean zero and
 162 standard deviation 0.2 for ξ , as proposed by Martins and Stedinger (2000).

163 **Starting date of the historical period**

164 The starting date t^* of the historical period can be assessed by two methods.

165 Let $NE = NE_H$ (historical period) + NE_C (continuous period) denote the total number of
 166 exceedances of the perception threshold S recorded during NY years, with $NY = NY_H$ (historical
 167 period) + NY_C (continuous period). Considering the date t_1 of the first known flood, which
 168 occurred $(NY - 1)$ years before the end of the systematic period, Prosdocimi (2018) proposed to
 169 choose the starting date as:

$$170 \quad t_{(\text{Prosdocimi})}^* = t_1 - (NY - 1)/NE \quad (5)$$

171 The idea behind this estimate is to start the historical period T_S years before the first known
 172 flood, where T_S is the return period of the perception threshold, estimated here as $(NY - 1) / NE$.

173 In some cases, the historical period (including flood and no-flood information) starts before the
 174 date t_1 of the first known flood (for instance, at the creation of the service in charge of surveying
 175 floods, or at the date of bridge construction where historical data is available). Let denote this
 176 date t_{start} , and consider the difference $(t_1 - t_{start})$ between these two dates. A second possible
 177 estimate, based on the Poisson process paradox (Feller, 1971), takes advantage that the expected
 178 duration between the last T -year event and current time is equal to the expected duration
 179 between current time and the next T -year event. Without any knowledge of the return period T_S
 180 of the threshold, but using the difference $(t_1 - t_{start})$, we have:

$$181 \quad t_{(\text{Poisson})}^* = t_{start} - (t_1 - t_{start}) = 2t_{start} - t_1 \quad (6)$$

182 **2.2 Models accounting for uncertainties**

183 We first present Binomial models for historical floods known to be larger than a perception
 184 threshold, with a propagation procedure for both stage and rating curve uncertainties (*model A*),
 185 or with parameters accounting for uncertainties on perception threshold (*model B*), length of
 186 the historical period (*model C*) or both (*model D*). Table 1 summarizes which Binomial model
 187 accounts for uncertainty, and/or historical period length. A fifth *model E* considers the case
 188 when historical discharges are known within an interval.

189

Table 1: Characteristics of the four Binomial models

Binomial model	Perception threshold S	Historical period length n
Model A	Fixed	Fixed
Model B	Uncertain	Fixed
Model C	Fixed	Uncertain
Model D	Uncertain	Uncertain

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192 **Model A: Binomial model for historical floods and propagation of systematic discharges** 193 **uncertainties**

194 In equation (3), the uncertainty in the AMAX discharges for the systematic period is assumed
195 to be negligible. As this uncertainty can reach 30% at Beaucaire during the XIXth century (see
196 following section 3.1), it seems necessary to consider it. We use the propagation procedure
197 accounting for both stage and rating curve uncertainties described by Lucas *et al.* (2023), that
198 leads to $s = 500$ realisations of AMAX discharges: $(q_t^{(i)})_{t=1,j;i=1,s}$. Each realization can be
199 used to compute a posterior distribution with equation (4), and each posterior distribution can
200 be explored with the MCMC sampler. This leads to a total of $r \times s$ parameter vectors
201 $(\theta_p^{(i)})_{p=1,r;i=1,s}$ representing the combined effect of sampling uncertainty and hydrometric
202 uncertainty for systematic data. The *maxpost* parameter vector is calculated using the *maxpost*
203 sample of AMAX discharges. The model described above will be referred to as *model A*. The
204 propagation of hydrometric uncertainties from the systematic period described here will be
205 carried out identically for all models defined in the following sections.

206 **Model B: Binomial model for historical floods, accounting for perception threshold** 207 **uncertainty**

208 A single perception threshold S for the entire sample is considered here. In order to take into
209 account the imperfect knowledge of S , it is possible to consider it as an unknown parameter of
210 the model, and to represent this imperfect knowledge through a prior distribution. In the
211 previous section, the perception threshold was already part of the model, but its value was
212 assumed to be known, which is no longer the case here. Therefore, the left-hand side of equation
213 (3) becomes $L(\theta, S; \mathbf{q}, k)$ instead of $L(\theta; \mathbf{q}, k)$, while its right-hand side remains unchanged.
214 The *posterior* distribution of the parameters θ and S given the data is:

$$215 \quad p(\theta, S | \mathbf{q}, k) \propto L(\theta, S; \mathbf{q}, k) p(\theta, S) \quad (7)$$

216 This posterior distribution takes into account the hydrometric uncertainty of the systematic
217 period, the sampling uncertainty and the uncertainty of the perception threshold. This model
218 will be referred to as *model B* in the following sections. Note that it is necessary to specify a
219 prior distribution for the perception threshold S which reflects the knowledge on this parameter,
220 which is highly case-specific and can range from very imprecise to nearly-known.

221 **Model C: Binomial model for historical floods, accounting for the uncertainty of the**
 222 **historical period length**

223 The uncertainty in the number n of years constituting the historical period can be treated in the
 224 same way as described in the previous section for the threshold S . Generally, the ending date of
 225 the historical period is perfectly known, as it also corresponds to the start of the systematic
 226 recordings. However, the starting date t^* of the historical sample, from which all floods above
 227 the perception threshold are supposed to be recorded, is generally poorly known. The number
 228 n of years constituting the historical period can hence be treated as an unknown parameter of
 229 the probabilistic model. The perception threshold S is assumed to be perfectly known in this
 230 case. Therefore, the left-hand side of equation (3) becomes $L(\boldsymbol{\theta}, n; \mathbf{q}, k)$. The posterior
 231 distribution of the parameters $\boldsymbol{\theta}$ and n given the data is:

$$232 \quad p(\boldsymbol{\theta}, n | \mathbf{q}, k) \propto L(\boldsymbol{\theta}, n; \mathbf{q}, k) p(\boldsymbol{\theta}, n) \quad (8)$$

233 As previously, a prior distribution reflecting the partial knowledge of the length of the historical
 234 period has to be specified. The lack of knowledge of the length of the historical period is
 235 therefore taken into account in the model and has an impact on the uncertainty of the results.
 236 This model will be referred to as *model C* in the following sections.

237 **Model D: Binomial model for historical floods, accounting for both perception threshold**
 238 **and historical period length uncertainties**

239 Since the perception threshold S and the number n of years of the historical period are linked
 240 by definition (a perception threshold being valid over a given duration), we finally consider a
 241 model which represents the lack of knowledge about both parameters. The left part of equation
 242 (3) becomes $L(\boldsymbol{\theta}, S; n; \mathbf{q}, k)$. The posterior distribution of the parameters $\boldsymbol{\theta}$, S and n given the
 243 data is:

$$244 \quad p(\boldsymbol{\theta}, S, n | \mathbf{q}, k) \propto L(\boldsymbol{\theta}, S, n; \mathbf{q}, k) p(\boldsymbol{\theta}, S, n) \quad (9)$$

245 This model for which S and n are uncertain will be called *model D* in the following sections.

246 **Model E: Considering historical flood discharges within intervals**

247 In some cases, the discharge of historical floods above the perception threshold can be
 248 reconstructed and taken into account in the probabilistic model (e.g. Stedinger and Cohn, 1986).
 249 Since such reconstructions are typically obtained by means of hydraulic models affected by
 250 large uncertainties, it is also useful to consider that the reconstructed discharges are not
 251 perfectly known but lie within intervals. Several examples of such models exist in the literature
 252 (e.g. Payraastre *et al.*, 2011 or Parkes and Demeritt, 2016). The corresponding likelihood can be
 253 written as:

$$254 \quad L(\boldsymbol{\theta}; \mathbf{q}, \mathbf{y}, k) = \prod_{t=1}^j f(q_t; \boldsymbol{\theta}) \prod_{i=1}^k [F(y_i^{sup}; \boldsymbol{\theta}) - F(y_i^{inf}; \boldsymbol{\theta})] (F(S; \boldsymbol{\theta}))^{n-k} \quad (10)$$

255 where q_t corresponds to the j floods of the systematic period and y_i to the k floods of the
 256 historical period whose discharge lies within the interval $[y_i^{inf}; y_i^{sup}]$. The posterior distribution
 257 of the model is:

$$258 \quad p(\boldsymbol{\theta} | \mathbf{q}, \mathbf{y}, k) \propto L(\boldsymbol{\theta}; \mathbf{q}, \mathbf{y}, k) p(\boldsymbol{\theta}) \quad (11)$$

259 Here, the perception threshold and the length of the historical period are assumed to be perfectly
260 known. This model will be referred to as *model E* in the following sections. The quantiles can
261 be compared with the results of the Binomial models, for which only the number k of perception
262 threshold exceedance S is known.

263 **3. Case study: The Rhône River at Beaucaire**

264 **3.1 Discharge data over five centuries**

265 We first consider the 205-year long daily discharge series of the Rhône River at Beaucaire,
266 France, from 1816 to 2020 (catchment area: 95 590 km²). Daily stage measurements started in
267 1816. The gauging station has been used until the construction of the Vallabrègues hydroelectric
268 scheme in 1967, which led to the derivation of a part of the discharge. Consequently, a new
269 gauging station was installed 2 km downstream from the restitution of the diverted discharges.
270 This new station has been used ever since. The Vallabrègues Dam has no impact on the
271 discharge at the station because it has a very limited storage capacity and it is opened during
272 floods to cancel the backwater effect it creates for low flows. A set of 500 realisations of AMAX
273 floods from 1816 to 2020 is available from Lucas *et al.* (2023), accounting for several sources
274 of hydrometric uncertainty. The estimated 95% discharge uncertainty varies from 30% (XIXth
275 century) to 5% (1967-2020). Secondly, a collection of historical flood testimonies from 1500
276 to 1815 is available from the HISTRHÔNE database (<https://histrhone.cerege.fr/>) (Pichard and
277 Roucaute, 2014). We focus on the 13 extreme floods (in 1529, 1548, 1570, 1573, 1674, 1694,
278 1705, 1706, 1711, 1745, 1755, 1801 and 1810), referenced as the *C4* class: “*extreme flood and*
279 *inundation*”. This ensemble is considered to be a comprehensive survey of the most damaging
280 floods of the historical period. The perception threshold S is about 9000 m³/s according to
281 Pichard *et al.* (2017). Figure 1a shows the available flood discharge sample with the
282 corresponding uncertainties. Note that we used a very uncertain prior for the perception
283 threshold in order to highlight its impact more clearly.

284 **3.2 Stationarity tests**

285 As the probabilistic models described in section 2 assume that AMAX values are independent
286 and identically distributed (*i.i.d.*), statistical tests should be applied to check the stationarity of
287 both systematic and historical periods.

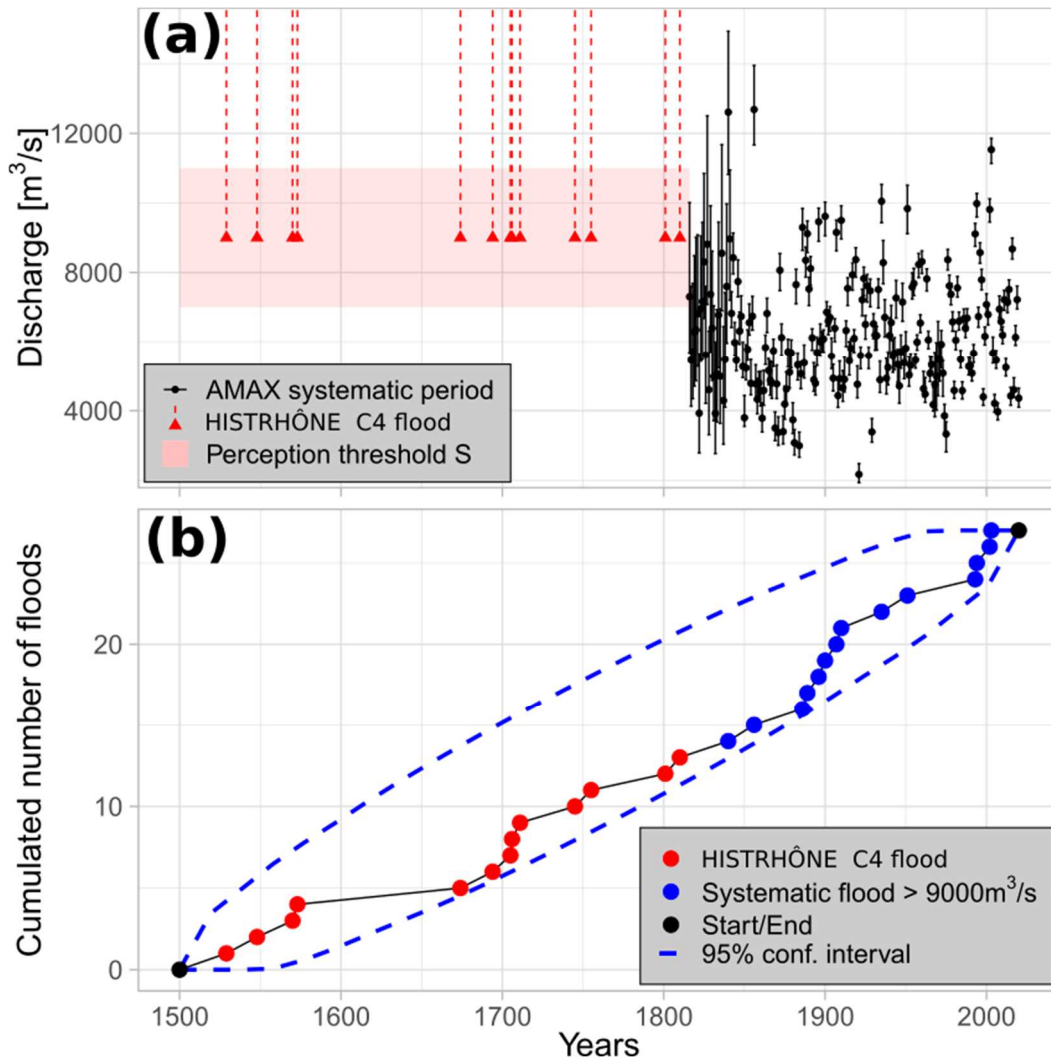
288 **Systematic data**

289 The Pettitt step-change test (Pettitt, 1979) and Mann-Kendall trend test (Mann, 1945; Kendall,
290 1948) were applied to the *maxpost* series of AMAX discharges during the 1816-2010 period.
291 The p-values of 0.15 and 0.4, respectively, indicate no significant change. The segmentation
292 procedure proposed by Darienzo *et al.* (2021) was also applied since it allows accounting for
293 the uncertainty around AMAX discharges. This procedure indicates that the optimum number
294 of segments is equal to one, confirming the absence of significant change.

295 **Historical data**

296 The historical data used here (13 extremes floods of $C4$ class) can be interpreted as peak-over-
 297 threshold (POT) values, since they correspond to all floods having exceeded the perception
 298 threshold S and that no year has more than one $C4$ flood during the 1500-1815 period. AMAX
 299 values from the continuous period larger than $9000 \text{ m}^3/\text{s}$ can also be viewed as POT values as
 300 the 14 largest values (in 1840, 1856, 1886, 1889, 1896, 1900, 1907, 1910, 1935, 1951, 1993,
 301 1994, 2002 and 2003) are from different years. Assuming that the number of occurrences of
 302 POT discharges follows a Poisson process, it is possible to compute a confidence interval for
 303 the cumulative number N_t of POT values during a period $[0; t]$ (Lang *et al.*, 1999) and to verify
 304 that the experimental curve is inside the limits of the interval. The Poisson test is applied on the
 305 whole period 1500-2020, using POT values from both historical and systematic periods (1500-
 306 1815 and 1816-2020). Figure 1b shows that the experimental curve is within the 95%
 307 confidence interval. The whole sample can hence be considered as stationary.

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 310 **Figure 1:** (a) The Rhône River at Beaucaire, AMAX flood discharges with 95% uncertainty intervals (1816-
 311 2020, systematic period, (Lucas *et al.*, 2023) and $C4$ class floods from 1500 to 1815 (HISTRHÔNE database);
 312 (b) Cumulated number of $C4$ class floods and POT floods (systematic period) with 95% Poisson process
 313 confidence interval

314 4. Flood Frequency Analysis on the 1816-2020 period

315 4.1 Subsampled data sets

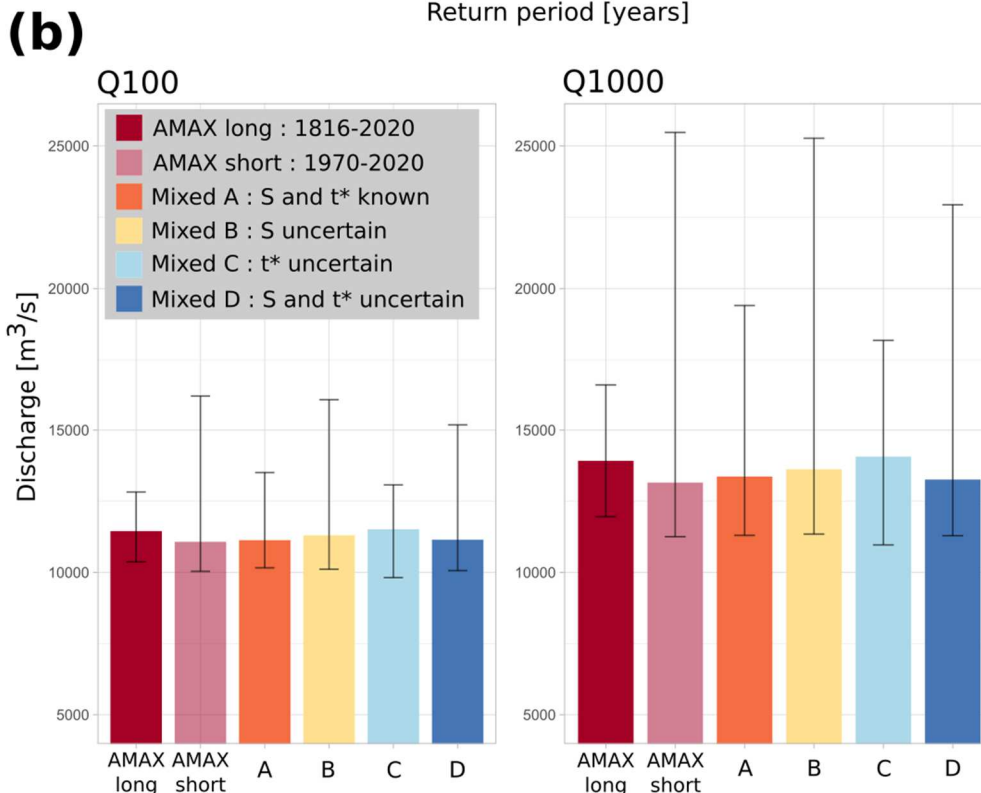
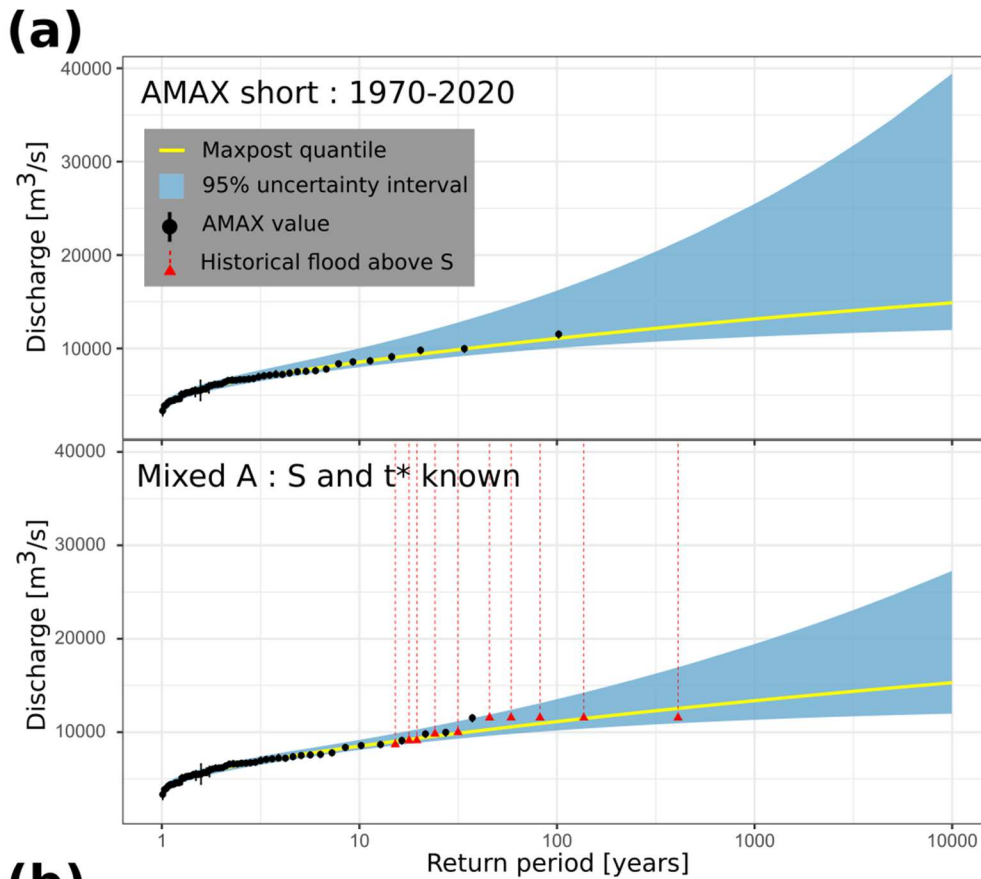
316 In this section, the GEV distribution fitted with AMAX discharges from the 1816-2020 period
 317 (including the propagation of hydrometric uncertainty described in section 2.2, *model A*) is used
 318 as a reference and is noted *AMAX long*. It can be compared with GEV distributions estimated
 319 with subsampled data, where only part of the available information is used:

- 320 • Short sample containing AMAX discharges during the 1970-2020 period, noted *AMAX*
 321 *short*. It corresponds to the typical length of hydrometric series in France, about 50 years of
 322 record, leading to a large extrapolation of the estimated distribution towards large quantiles
 323 (100-year or 1000-year return period).
- 324 • Mixed sample, with AMAX discharges on the 1970-2020 period and a collection of
 325 *historical* values on the 1816-1969 period, noted *Mixed A*, ..., *Mixed E*, according to the model
 326 used. A perception threshold $S = 9000 \text{ m}^3/\text{s}$ leads to a collection of 10 *historical* floods. When
 327 using *model B* (or *D*), we consider a vague Normal prior distribution on the perception
 328 threshold: $N(9000; 2000)$, 2000 being the standard deviation. When using *model C* (or *D*), we
 329 consider a Uniform prior distribution on the starting date of the historical period:
 330 $U[1316; 1816]$, corresponding to a large uncertainty (500 years).

331 Results with systematic data only (*AMAX long* and *AMAX short*) or with a mixed sample
 332 (*AMAX short* + 10 historical floods) are presented for the estimation of Q_{100} and Q_{1000} floods
 333 (Figure 2b), parameters (ξ, S, t^*) (Table 2) and GEV distributions (Figure 2a). The plotting
 334 position formula proposed by Hirsch (1987) in case of a mixed sample with AMAX values
 335 from a continuous period and historical discharges larger than a perception threshold is applied.
 336 The appendix gives a procedure in case where historical flood discharges are unknown, using
 337 only exceedances of the threshold.

338 **Table 2:** *Maxpost estimation \pm posterior standard deviation expressed in percentage for Q_{100} and Q_{1000}*
 339 *floods, and (ξ, S, t^*) parameters (1816-2020 period)*

Data set		AMAX values		AMAX short + historical data (1816-1969)				
		AMAX long (1816-2020)	AMAX short (1970-2020)	Mixed A	Mixed B	Mixed C	Mixed D	Mixed E
Quantiles (m^3/s)	Q_{100}	11451 $\pm 6\%$	11076 $\pm 23\%$	11132 $\pm 11\%$	11302 $\pm 21\%$	11517 $\pm 7\%$	11147 $\pm 18\%$	11286 $\pm 8\%$
	Q_{1000}	13919 $\pm 10\%$	13154 $\pm 50\%$	13367 $\pm 23\%$	13622 $\pm 43\%$	14069 $\pm 15\%$	13262 $\pm 36\%$	13827 $\pm 16\%$
Parameters	ξ	0.058 $\pm 76\%$	0.077 $\pm 132\%$	0.062 $\pm 142\%$	0.058 $\pm 176\%$	0.041 $\pm 202\%$	0.074 $\pm 130\%$	0.035 $\pm 191\%$
	S (m^3/s)	/	/	/	9163 $\pm 8\%$	/	9332 $\pm 9\%$	/
	t^*	/	/	/	/	1833 $\pm 4\%$	1785 $\pm 6\%$	/



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Figure 2: (a) GEV quantiles with 95% credibility intervals, example of two different models and datasets: GEV model on AMAX values (*AMAX short* 1970-2020) and binomial *Model A* on mixed sample (1816-2020); (b) *Q100* and *Q1000* floods with 95% credibility intervals displayed as error bars. *AMAX long* refers to the sample on the 1816-2020 period; *AMAX short* refers to the sample on the 1970-2020 period; *Mixed A-B-C-D* refers to a mixed sample (“historical” floods on the 1816-1969 period and AMAX 1970-2020) for various statistical models.

347 **4.2 Value of adding historical information from the 1816-1969 period**

348 Unsurprisingly, when the length of the systematic record (~50 years) is too short compared with
349 the target return period (~100 or 1000 years), the results are highly uncertain (*AMAX short* in
350 Figure 2). A Binomial model exploiting historical flood events notably reduces uncertainty
351 when the perception threshold S is known (Figure 2b, *Mixed A* and *Mixed C*), although not
352 achieving the precision obtained with 205 years of systematic records (Figure 2b, *AMAX long*).
353 Accounting for the uncertainty on threshold S (Figure 2b, *Mixed B* and *Mixed D*) increases the
354 uncertainty of flood quantiles and nearly annihilates the interest of historical flood occurrences.

355 The main part of the uncertainty comes from the estimation of the shape parameter ζ , which
356 governs the behaviour of the tail of the distribution. Note that all the estimates are close to zero
357 and slightly positive (Table 2), which corresponds to an upper-bounded distribution. As might
358 be expected, the estimate of parameter ζ is much more precise with a long series (*AMAX long*)
359 of two centuries than with a short series (*AMAX short*) of 5 decades. The use of historical data
360 through a Binomial model is not very efficient in reducing uncertainty on the shape parameter
361 ζ (Table 2). Overall, the *maxpost* estimate of $Q100$ and $Q1000$ quantiles are very close for all
362 models (Figure 2b). In the next sections, the interest of accounting for the uncertainties in the
363 perception threshold S and the starting date t^* of the historical period is assessed in more detail.

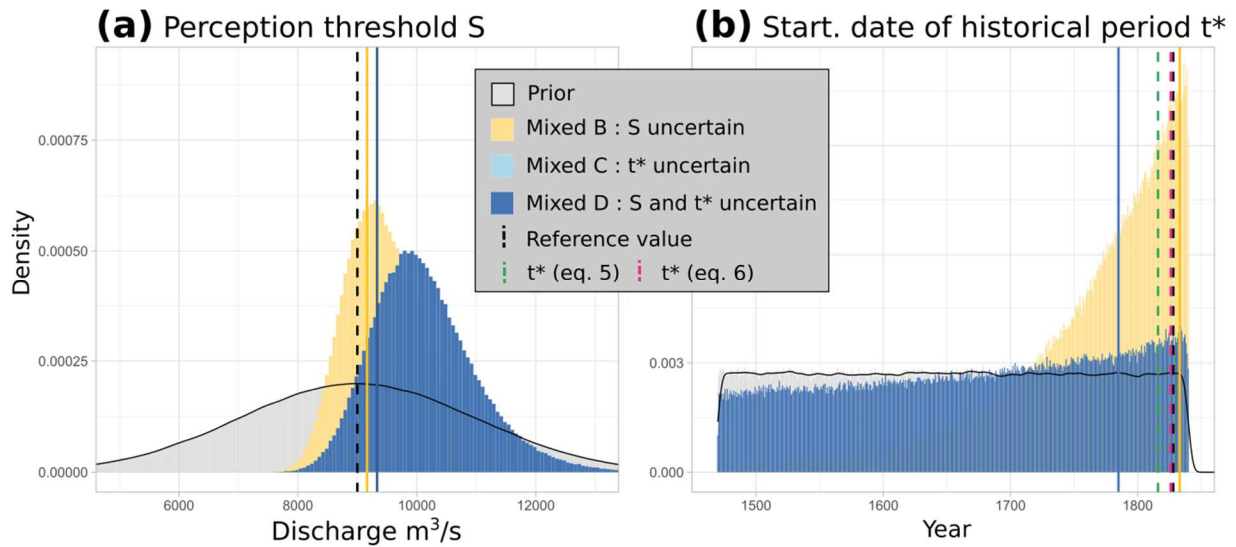
364 **4.3 Impact of considering the perception threshold uncertain**

365 The use of *model B* reflects a lack of knowledge of the perception threshold, which becomes a
366 parameter of the model. Figure 2b shows that the quantile uncertainty estimated with *model B*
367 is much greater than with *model A*, and is close to the one obtained with systematic data only
368 (*AMAX short*). Poor knowledge of the perception threshold therefore has major consequences
369 for the quantile estimates, since it greatly reduces the value of using historical occurrences. The
370 true value of the perception threshold is $S = 9000 \text{ m}^3/\text{s}$. The prior and posterior distributions of
371 the threshold S are shown in Figure 3a. It can be seen that the posterior estimate for *model B*
372 ($9163 \text{ m}^3/\text{s}$) is close to the true value ($9000 \text{ m}^3/\text{s}$), and that the model has effectively improved
373 the knowledge of the threshold compared with the prior distribution $N(9000; 2000)$. The
374 posterior uncertainty of the shape parameter ζ for *model B* is greater than that of *model A* and
375 thus becomes almost identical to that of *AMAX short* (Table 2). In real-world case studies,
376 specifying a more precise prior should limit this impact and should hence be considered as a
377 priority objective for historical FFA.

378 **4.4 Impact of considering the historical period length uncertain**

379 *Model C* is used to represent the lack of knowledge on the length of the historical period. In
380 Figure 2b, the *maxpost* quantile estimates for *model C* have slightly higher values than the
381 estimates for *model A*. This may be due to the underestimation of the length of the historical
382 period, as can be seen in Figure 3b. The *maxpost* date is 1833, whereas the series actually
383 begins in 1816. This underestimation by 17 years can be explained by a greater frequency of
384 floods above the threshold S during the systematic period (4 floods during 50 years, i.e one
385 exceedance every 12.5 years) than during the historical period (10 floods during 153 years, i.e

386 one exceedance every 15 years). This imbalance is probably due to sampling variability as no
 387 break or trend was detected by the stationarity tests in section 3.2. The posterior distribution of
 388 the starting date t^* for *model C* (Figure 3b) is much more precise than the prior distribution,
 389 and is strongly asymmetric. The uncertainty around the quantiles estimated by *model C* is very
 390 similar to that estimated by *model A* (Figure 2b), as is the distribution of the shape parameter
 391 (Table 2). Overall, these results indicate that a poor knowledge of the length of the historical
 392 period has less impact on the precision of quantile estimates than poor knowledge of the
 393 perception threshold.



394

395 **Figure 3:** Prior and posterior distributions of: (a) the perception threshold S ; (b) the starting date t^* of the
 396 historical period (1816-2020 period). The solid vertical lines represent the maxpost estimate of the parameter for
 397 each of the models, and the black dashed lines represent the reference values ($S = 9000 \text{ m}^3/\text{s}$ and $t^* = 1816$). The
 398 green and pink dashed vertical lines (b) represent the estimates of t^* from equations (5) and (6).

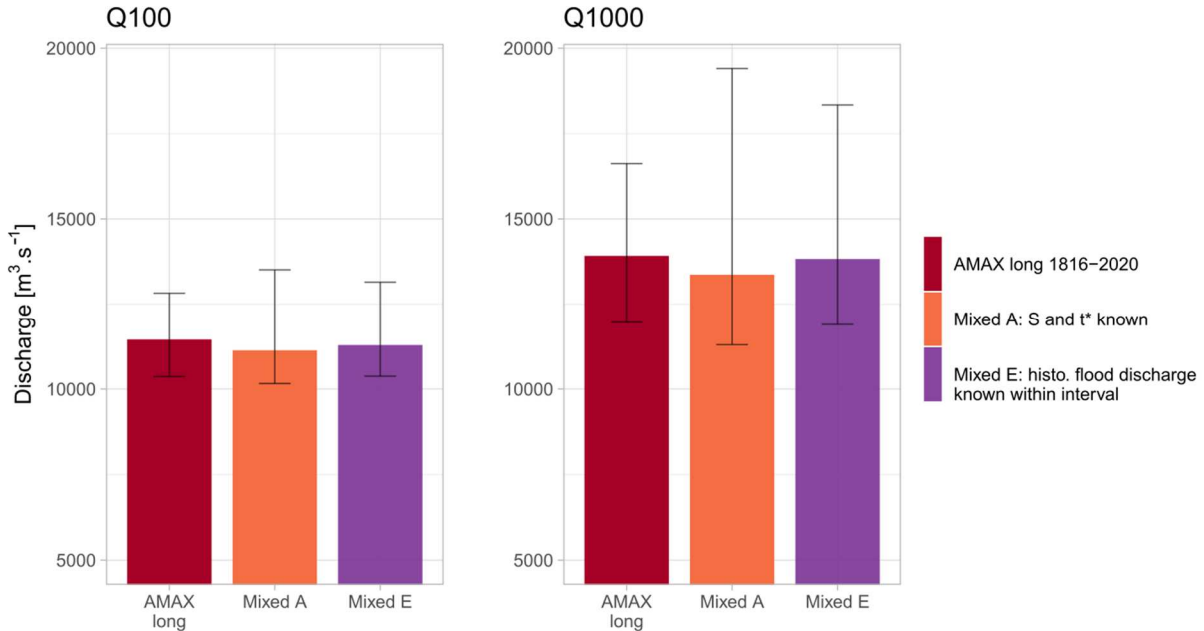
399 4.5 Impact of considering both the perception threshold and the historical 400 period length uncertain

401 *Model D* assumes that both S and n are uncertain in the probabilistic model. The *maxpost*
 402 quantiles estimated in Figure 2b are close to the reference values. In contrast, the width of the
 403 credibility interval is large and lies between that of *models B* and *C*. Although the estimate is
 404 more accurate than with a short series (*AMAX short*), it remains very imprecise for the 1000-
 405 year flood. Figure 3 helps understanding the origin of this large uncertainty. The posterior
 406 distribution of the perception threshold S , although with a *maxpost* value ($9332 \text{ m}^3/\text{s}$) close to
 407 the true value ($9000 \text{ m}^3/\text{s}$), is very imprecise with a large standard deviation ($883 \text{ m}^3/\text{s}$). The
 408 perception threshold S appears to be slightly less precisely estimated than with *model B* (Table
 409 2), with respectively posterior standard deviation of 9% and 8%. The starting date of the
 410 historical period is even more difficult to estimate, particularly in comparison with the estimate
 411 from *model C*. It can be seen that the posterior distribution t^* of *model D* is very similar to the
 412 prior Uniform distribution (Figure 3b), although it is slightly asymmetrical and shows a
 413 maximum not far from the true value (the year 1816). However, the flood discharge quantiles
 414 are less uncertain for *model D* than for *model B*. The precise reasons for this are unclear at this
 415 stage but this might be due to some correlations between parameters. In particular, the Pearson

416 correlation coefficient ρ is respectively equal to 0.44 and 0.42 between the length of the
 417 historical period n and the perception threshold S , as well as between the perception threshold
 418 S and the shape parameter ζ .

419 4.6 Value of estimating the peak discharge of historical flood

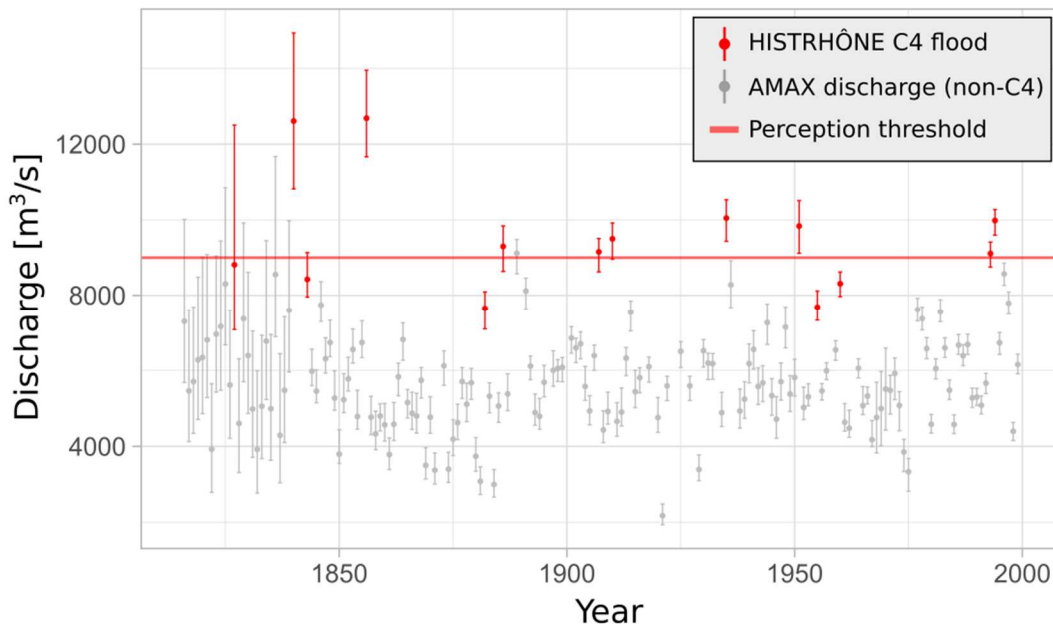
420 Binomial *models A, B, C* and *D* only use information on the number of times k a perception
 421 threshold S is exceeded over a period of n years. The discharge of historical floods that have
 422 exceeded the threshold is therefore ignored. *Model E* allows peak discharge estimates (with
 423 uncertainty) to be taken into account. The results are shown in Figure 4. There is a reduction in
 424 uncertainty of around 25% for $Q1000$ with *model E* compared to Binomial *model A* (posterior
 425 standard deviations of 2255 and 3019 m^3/s , respectively). However, the uncertainty of *model E*
 426 remains around 65% greater than that of the *GEV 1816-2020* model for $Q1000$. Although it is
 427 not a necessary condition for using historical data, knowledge of the discharge of historical
 428 floods does reduce the uncertainty around extreme quantiles. However, these results are only
 429 valid for the perception threshold S used here, which has a return period of about 15 years (with
 430 14 exceedances during 205 years). Stedinger and Cohn (1986) and Payraastre *et al.* (2011)
 431 showed that the difference in uncertainty between the results of these two types of models tends
 432 to reduce as the return period of the perception threshold increases towards 50 years or so, until
 433 it becomes negligible above this magnitude. This encourages the use of the number of
 434 exceedances of a perception threshold when it is not possible to have better information on
 435 historical floods.



436
 437 **Figure 4:** $Q100$ and $Q1000$ floods with 95% credibility intervals displayed as error bars. *AMAX long* refers to an
 438 annual maximum sample on the 1816-2020 period; *Mixed* refers to a mixed sample (“historical” floods on the
 439 1816-1969 period and *AMAX* 1970-2020). *Model A* uses only the number of times the perception threshold has
 440 been exceeded, while *Model E* considers the peak discharge (and its uncertainty) of each historical flood that
 441 exceeded threshold S . Perception threshold S and start date of historical period t^* are considered perfectly known
 442 (*models A* and *E*).

443 5. Flood Frequency Analysis on the 1500-2020 period

444 In the previous section, we used a synthetic case study from a 205-year systematic record (1816-
445 2020), which gives a baseline to compare the performance of five proposed models (A, B, C,
446 D, E) with known parameters (S and n). The systematic record has been artificially subsampled
447 into a mixed data set, containing 51 years of systematic data (1970-2020) and 154 years of
448 censored historical data larger than a known perception threshold (1816-1969). In this section,
449 Binomial models (A, B, C, D) are applied to a 500-year long case study, using the 205-year
450 systematic record (1816-2020) and a collection of historical floods from HISTRHÔNE database
451 (1500-1815). This time, S and n are not perfectly known.



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Figure 5: AMAX flood discharges (1816-2000) from Lucas *et al.* (2023) (in grey) cross-referenced with C4 floods from HISTRHÔNE database (in red). The horizontal line corresponds to the estimated perception threshold $S = 9000 \text{ m}^3/\text{s}$.

456 5.1 Prior on the perception threshold S and the starting t^* of the historical 457 period

458 Binomial *models A, B, C* and *D* are now applied on a mixed sample over the period 1500-2020,
459 with AMAX values for the systematic period 1816-2020 and occurrences of flood above the
460 perception threshold for the historical 1500-1815 period. The perception threshold and the
461 starting date of the historical period are not known precisely, and a first analysis is carried out
462 with vague priors, with $S \sim N(9000; 2000)$ and $t^* \sim U[1129; 1529]$. By definition, the
463 historical period begins, at the latest, on the date of the first known historical flood in 1529. The
464 lower limit of the Uniform distribution is arbitrarily set 400 years before the date of the first
465 historical flood in order to represent the lack of knowledge of t^* .

466 A second analysis will refine results of *model D*, with more accurate prior estimates of S and t^*
467 used for the historical 1500-1815 period, based on information of the systematic 1816-2020
468 period. The application of *model D* with these more informative priors will be referred to as
469 *model D**. Figure 5 cross-references *C4* (extreme) floods occurring between 1816 and 2000

470 according to the HISTRHÔNE database (Pichard *et al.*, 2017) and the estimated AMAX
471 discharge values on the same period (Lucas *et al.*, 2023). Five amongst fourteen *C4* floods are
472 below the threshold $S = 9000 \text{ m}^3/\text{s}$. Even accounting for discharge uncertainty, three *C4* floods
473 are still fully below the threshold S . As the flood ranking of the HISTRHÔNE database is based
474 on observed damages, it is therefore not possible to have a direct match between *C4* floods and
475 an exact discharge threshold. We refine the prior distribution $N(9000; 500)$, with a standard
476 deviation of $500 \text{ m}^3/\text{s}$ (instead of $2000 \text{ m}^3/\text{s}$ with *model D*). No *C4* flood is fully below the 95%
477 prior interval [8000; 10 000].

478 Considering the thirteen *C4* floods of the HISTRHÔNE database (1500-1815) and the fourteen
479 floods higher than a threshold $S = 9000 \text{ m}^3/\text{s}$ during the 1816-2020 period, we have two possible
480 estimates of the starting date t^* of the historical period:

- 481 • $t^*_{(\text{Prosdociami})} = 1511$ (from eq. 5), with the knowledge of the date of the first known flood (t_1
482 = 1529), the total number of threshold exceedances ($NE = 13$ (*C4* floods) + 14 ($AMAX > S$) =
483 27), and the total number of years ($NY = 2020 - 1529 = 491$ years);
- 484 • $t^*_{(\text{Poisson})} = 1471$ (from eq. 6), with the knowledge of the starting date of the surveying period
485 ($t_{start} = 1500$).

486 We refine the prior distribution of t^* as $U[1471; 1529]$, with a width of 58 years (instead of
487 400 years with *model D*).

488 5.2 Results with vague prior on the perception threshold and the historical 489 period length

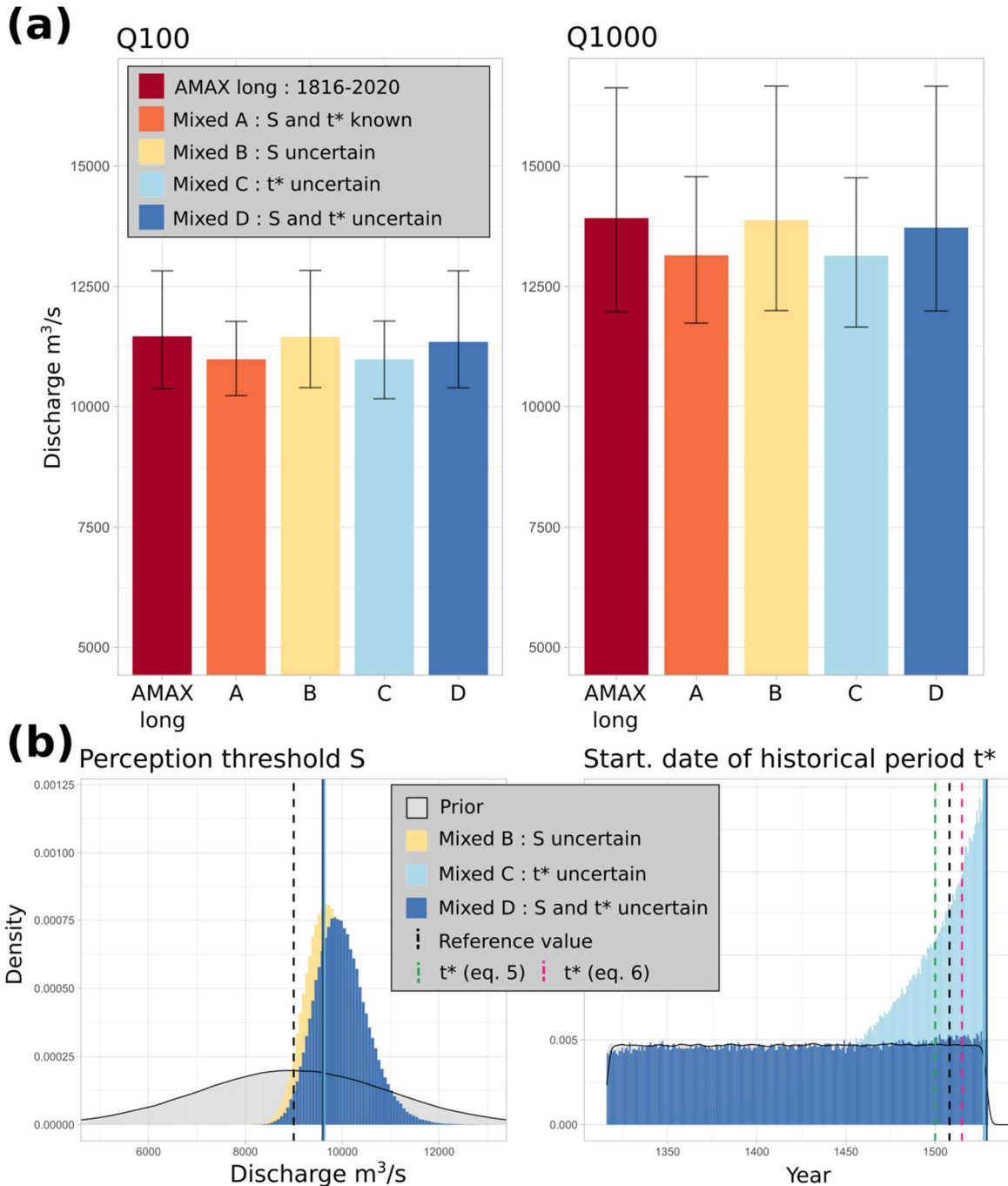
490 Results with systematic data only (*AMAX*) on the 1816-2020 period or with a mixed sample
491 (*AMAX* + 13 historical floods) on the 1500-2020 period are presented for the estimation of Q_{100}
492 and Q_{1000} floods (Figure 6) and parameters (ξ , S , t^*) (Table 3).

493 **Table 3:** Maxpost estimation \pm posterior standard deviation expressed in percentage for Q_{100} and Q_{1000} floods,
494 and (ξ , S , t^*) parameters (1816-2020 and 1500-2020 periods)

Data set		AMAX 1816-2020	AMAX + historical data (1500-1815)				
			Mixed A	Mixed B	Mixed C	Mixed D	Mixed D*
Quantiles (m^3/s)	Q_{100}	11451 $\pm 6\%$	10977 $\pm 4\%$	11438 $\pm 6\%$	10975 $\pm 4\%$	11336 $\pm 7\%$	11118 $\pm 5\%$
	Q_{1000}	13919 $\pm 10\%$	13149 $\pm 6\%$	13875 $\pm 10\%$	13139 $\pm 6\%$	13721 $\pm 11\%$	13421 $\pm 8\%$
Parameters	ξ	0.058 $\pm 76\%$	0.073 $\pm 52\%$	0.060 $\pm 73\%$	0.074 $\pm 51\%$	0.061 $\pm 72\%$	0.063 $\pm 63\%$
	S (m^3/s)	/	/	9628 $\pm 5\%$	/	9613 $\pm 6\%$	9386 $\pm 4\%$
	t^*	/	/	/	1527 $\pm 3\%$	1529 $\pm 4\%$	1526 $\pm 1\%$

495 The results with a mixed sample on the 1500-2020 period show that the uncertainty on Q_{100}
496 and Q_{1000} floods (Figure 6a) is lower than with AMAX values on the 1816-2020 period for
497 models assuming a known perception threshold (*models A* and *C*). For these two *models A* and
498 *C*, the *maxpost* quantiles are also slightly lower (by around 5%) than with AMAX values on the

499 1816-2020 period (Figure 6a). In the same way as with subsamples on section 4, this suggests
 500 that poor knowledge of the perception threshold (*models B and D*) is more detrimental to the
 501 precision of estimated quantiles than poor knowledge of the historical period length (*models C*
 502 and *D*). In particular, these differences can be explained by looking at the posterior distributions
 503 of the parameters S and t^* (Figure 6b).



504
 505 **Figure 6:** (a) $Q100$ and $Q1000$ floods with 95% credibility intervals displayed as error bars. *AMAX long* refers to the annual maximum sample on the 1816-2020 period; *Mixed A-B-C-D* refer to a mixed sample (“historical”
 506 floods on the 1500-1815 period and *AMAX* for 1816-2020) for various statistical models. (b) Posterior
 507 distribution of: (left) the perception threshold S ; (right) the starting date t^* of the historical period (1500-2020
 508 period). The solid vertical lines represent the parameter maxpost estimates for each model and the black dashed
 509 lines represent the reference values ($S = 9000 m^3/s$ and $t^* = 1500$). The green and pink dashed vertical lines
 510 (right) represent the estimates of t^* by equations (5) and (6).
 511

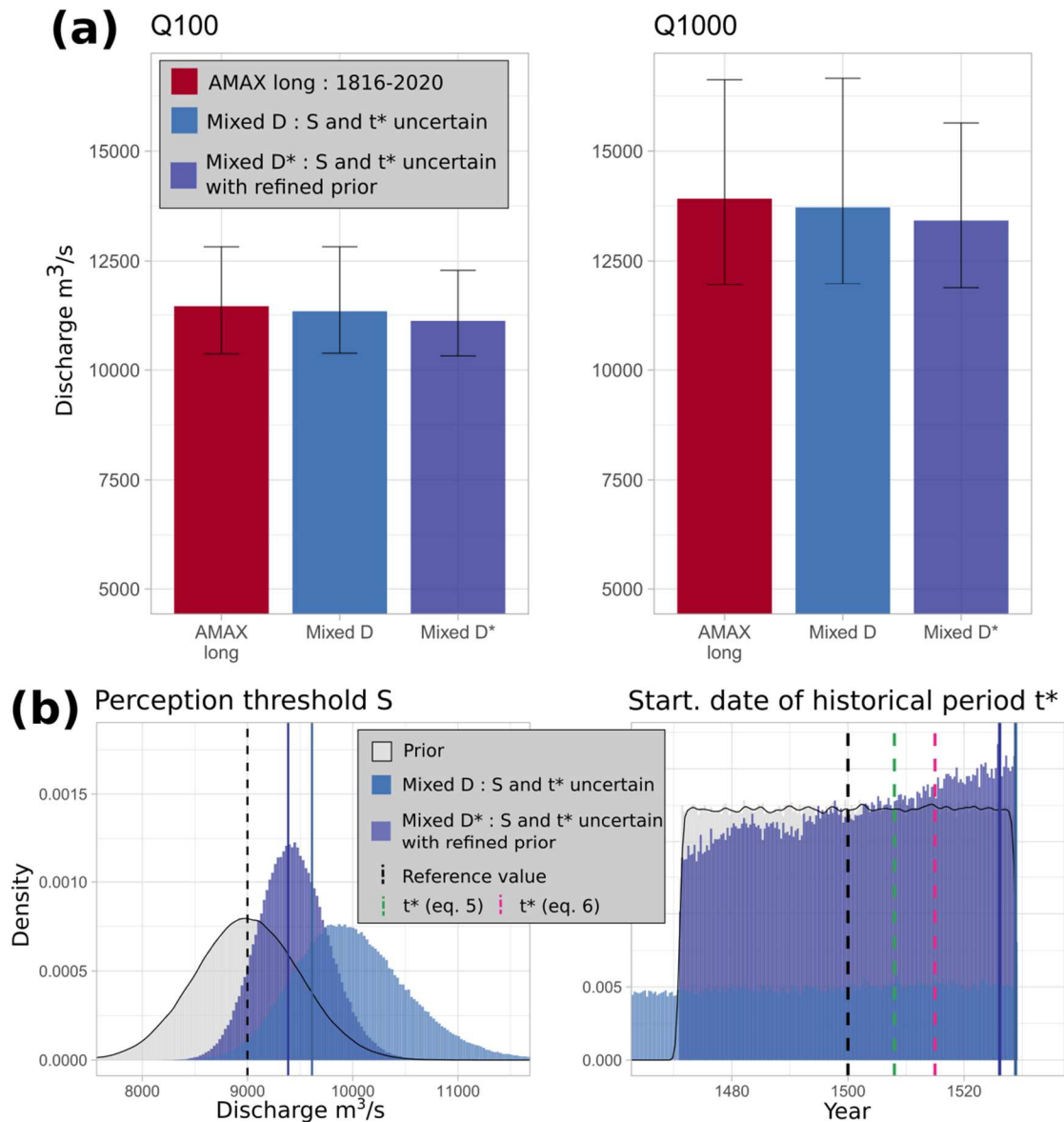
512 The posterior standard deviations for the perception threshold (*models B and D*) are relatively
513 small (around 500 m³/s for both models) and the distributions are lying mostly above the prior
514 value of 9000 m³/s (*maxpost* values around 9600 m³/s, Table 3). The starting date t^* of the
515 historical period is more precisely estimated with *model C* than with *model D*, whose posterior
516 distribution is very close to the prior distribution. For both models, the *maxpost* estimates of t^*
517 are almost 30 years higher than the assumed value of 1500. In particular, the posterior
518 distribution for *model C* shows a maximum for the year 1529, which corresponds to the date of
519 the first flood in the sample.

520 This trend towards a higher threshold and a shorter historical period could be a symptom of the
521 non-exhaustiveness of the extreme floods (C4 category) of the HISTRHÔNE database, despite
522 the fact that the stationarity hypothesis of the Poisson test over the 1500-2020 period was not
523 rejected (Figure 1b). Once again, we can compare the rate of occurrence of floods above the
524 threshold $S = 9000$ m³/s for each of the two samples. For the historical sample, 13 floods were
525 observed over 316 years, i.e. one exceedance every 24 years. For the systematic sample, there
526 were 14 floods over a period of 205 years, i.e. one exceedance every 15 years. This larger
527 frequency of S exceedances of the systematic period, whether due to sampling variability,
528 climatic variability or the non-exhaustiveness of the historical data, leads to the estimation of a
529 higher perception threshold and/or a shorter historical period length.

530 **5.3 Refining prior distributions of the perception threshold and the** 531 **historical period length**

532 The previous analysis is refined using narrower prior distributions of the perception threshold
533 S and the starting date t^* of the historical period. A comparison of the Binomial *models D and*
534 *D** and the AMAX GEV 1816-2020 model is presented in Figure 7a. It can be seen that the
535 uncertainty of the quantiles is smaller by about 15% compared to the reference for $Q100$ and
536 $Q1000$. *Maxpost* estimates are also reduced by approximately 3% for both return periods. The
537 use of historical floods therefore appears relevant to reduce the uncertainty of the quantiles,
538 even in the case where S and n are uncertain. It can also be noted that the elicitation of more
539 informative priors (see Falconer *et al.*, 2022 for a methodological review) reduced the standard
540 deviation of the posterior distribution for $Q1000$ by about 25% (comparison of model *D* with
541 vague priors on S and t^* , and model *D** with refined priors).

542 The posterior distributions of S and t^* are shown in Figure 7b. Once again, the posterior
543 distribution of the perception threshold is shifted towards values higher than the assumed value
544 of 9000 m³/s, with a *maxpost* threshold at 9386 m³/s. The posterior distribution of t^* is again
545 very close to the prior distribution, with a slightly higher density for the years close to the date
546 of the first flood. The *maxpost* estimate of t^* is here 1526, i.e. a length of the historical period
547 26 years shorter than expected. Therefore, a doubt remains as to the completeness of the
548 historical sample or the inter-sample stationarity as described in the previous section.



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Figure 7: (a) $Q100$ and $Q1000$ floods with 95% credibility intervals displayed as error bars. *AMAX long* refers to an annual maximum sample on the 1816-2020 period; *Mixed D** refers to a mixed sample (“historical” floods on the 1500-1815 period and AMAX for 1816-2020), with refined priors on S and t^* . (b) Posterior distributions of (left) the perception threshold S ; (right) the starting date t^* of the historical period for the two mixed models D and D^* . The solid vertical lines represent the *maxpost* estimate of the parameter for each of the models and the black dashed lines represent the reference values (threshold $S = 9000 m^3/s$; starting date $t^* = 1500$).

556

6. Discussion

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6.1 Main findings on the 1816-2020 period

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By using the probabilistic models described in section 2 on an artificially degraded sample whose characteristics are well known, it is possible to assess the impact of limited knowledge of the perception threshold S and the length n of the historical period on the estimation of extreme quantiles. The results show that poor knowledge of the perception threshold has a greater impact than poor knowledge of the historical period length. Even if the *maxpost* estimates of the perception threshold for models B and D are close to the true value ($9000 m^3/s$), the uncertainty resulting from determining the threshold has a strong impact on quantiles

565 uncertainty. Furthermore, the estimation of the historical period length in the case of *model C*
566 is also quite imprecise, but this has little impact on the uncertainty of the results when compared
567 with those of *model A*. The comparison of *model A*, for which only the number of exceedances
568 of the perception threshold is known, with *model E*, for which the discharge of historical floods
569 is known within an uncertainty interval, demonstrated the value of reconstructing the discharge
570 of each historical flood.

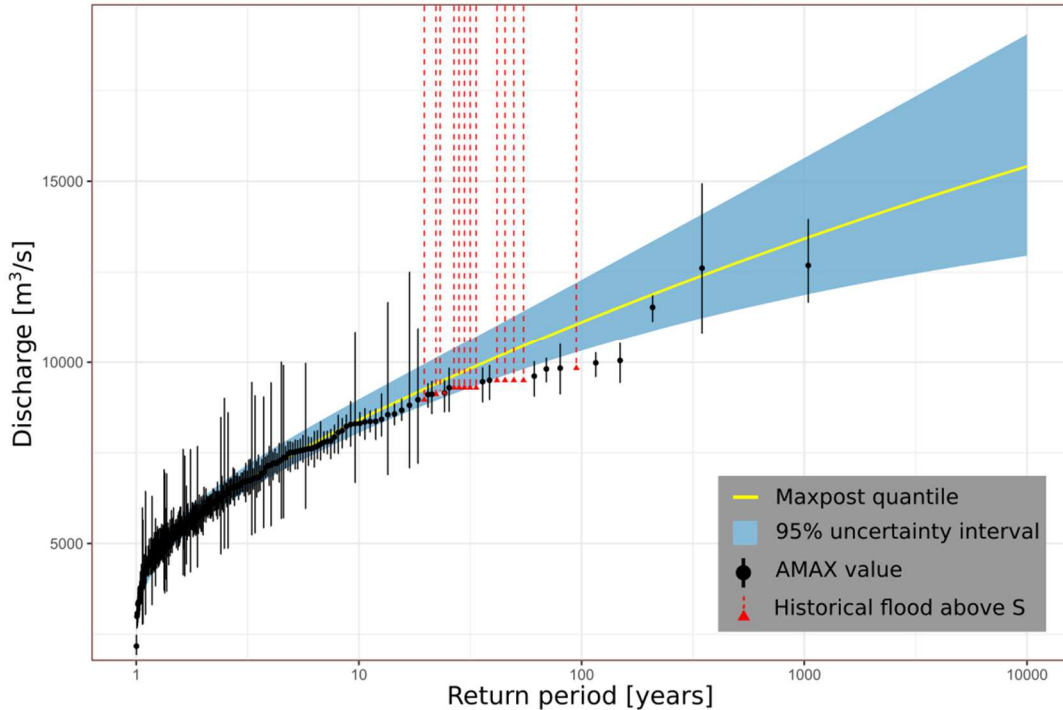
571 Finally, the results on the 1816-2020 period suggest that the quantiles uncertainty may be
572 underestimated when the perception threshold and the historical period length are unduly
573 considered to be perfectly known. The models proposed in this paper allow us to account for
574 imperfect knowledge when estimating extreme quantiles.

575 **6.2 Main findings on the 1500-2020 period**

576 Application of the Binomial *model D* to a mixed sample with discharge estimate of AMAX
577 values on the systematic 1816-2020 period and a collection of 13 historical floods from 1500
578 to 1815 allows the uncertainty around the perception threshold S and the historical period length
579 to be considered. Priors of *model D* were refined, in order to have a more realistic assessment
580 of threshold S and the starting date t^* of the historical period. This refined model, called *model*
581 *D**, gives the following results:

- 582 • Despite the fact that the available AMAX flood series on the 1816-2020 period is really long
583 (205 years), it is possible to reduce the uncertainty of the flood quantiles (Figure 7a) by adding
584 information of 13 exceedances of a threshold $S = 9000 \text{ m}^3/\text{s}$ during three prior centuries (period
585 1500-1815) and prior knowledge about S and t^* ;
- 586 • The refinement of the prior distributions on the threshold S and the starting date t^* , with
587 *model D**, gives a more precise assessment of flood quantiles than with *model D* (Figure 7a).
588 Posterior standard deviation (expressed in %) of $Q1000$ quantile decreases from 11% to 8%
589 (Table 3). In both cases, considering the perception threshold S as being uncertain has much
590 more impact on the uncertainty of the results than considering a lack of knowledge about the
591 length of the historical period;
- 592 • The combination of an increased perception threshold ($S_{\text{maxpost}} = 9386 \text{ m}^3/\text{s}$ vs $S_{\text{prior}} = 9000$
593 m^3/s) and a reduced span of the historical period ($t^*_{\text{maxpost}} = 1526$ vs $t^*_{\text{prior}} = 1500$) may be the
594 symptom of the non-exhaustiveness of floods in the historical samples of the HISTRHÔNE
595 database, even though no non-stationarity of the frequency of floods was detected (Figure 1b).
596 As the historical flood inventory is based on damages, it may be sensitive to some changes in
597 damage perception.
- 598 • Flood distribution and 95% credibility interval of *model D** are represented in Figure 8.
599 AMAX values are reported with their uncertainty (from 5% to 30%) and historical floods as
600 exceedances. Information on floods during three prior centuries (1500-1815) reduces the level
601 of extrapolation towards extreme floods (flood of record has a plotting position around the
602 1000-year return period in Figure 8, instead of a 400-year return period in Figure 2a for the
603 1816-2020 period).

Mixed D* : S and t* uncertain with refined prior



604

605 **Figure 8:** Flood distribution and 95% confidence interval of *model D** (Mixed sample: systematic period 1816-
606 2020 + 13 historical exceedances on 1500-1815, refined prior on S and t^*). Experimental distribution in black
607 (AMAX values) or red (exceedances of the perception threshold).

608 7. Conclusion

609 This paper proposes Binomial models for the inclusion of historical data into FFA, which
610 explicitly recognize the uncertain nature of both the perception threshold and the starting date
611 of the historical period.

612 The models are first tested with a 205-year long series of AMAX values for the outlet of the
613 Rhône River at Beaucaire, France. ~~Lucas *et al.* (2023) produced a detailed analysis of the~~
614 ~~uncertainty of this flood discharge series.~~ It has been artificially subsampled in order to mimic
615 a historical context, considering AMAX values on a 50-year period (1970-2020) and a
616 collection of 10 “historical” floods during the 1816-1969 period. The estimated quantiles were
617 compared with estimates from a GEV model with AMAX values for the entire period (1816-
618 2020). Considering that the perception threshold is perfectly known when this is not the case
619 can lead to a significant underestimation of the uncertainty of flood quantiles. This also holds
620 for the length of the historical period but to a much lesser extent. In the case of this subsample,
621 the use of historical data makes it possible to reduce the uncertainty of the quantiles compared
622 to the sole use of the short systematic sample (1970-2020), considering uncertainties on the
623 threshold S and the starting date t^* of the historical period. The Binomial model estimate with
624 known S and t^* (*model A*) was then compared to an estimate for which historical flood
625 discharges are known within an interval (*model E*). In Beaucaire, the use of the historical flood
626 discharges turned out to be slightly more informative than the use of the sole number of
627 exceedances of the perception threshold. ~~According to Stedinger and Cohn (1986) and Payraastre~~
628 ~~*et al.* (2011), the magnitude of the perception threshold has a direct influence on the uncertainty~~

629 ~~of the results in the case of the Binomial model. The advantage of a model based on historical~~
630 ~~flood discharges instead of a Binomial model tends to be reduced when the perception threshold~~
631 ~~is large, especially with a return period greater than 50 years. In Beaucaire, the return period of~~
632 ~~the perception threshold S is about 15 years, which explains the advantage of *model E* over~~
633 ~~*model A* in this specific case.~~

634 ~~The shape parameter estimated at Beaucaire is positive, corresponding to an upper bounded~~
635 ~~GEV distribution (with the parametrization used in this paper). Therefore, the general~~
636 ~~conclusions discussed above may not apply to other series leading to negative shape parameters~~
637 ~~and hence heavy-tailed distributions. The methodology proposed in this paper should therefore~~
638 ~~be applied in future work to a diverse collection of real-life case studies, and possibly to~~
639 ~~synthetic data as well, in order to understand its properties in more depth.~~

640 The paper also presents the results of the Binomial model with a mixed sample of 205 AMAX
641 values (1816-2020 period) and 13 occurrences of historical floods (1500-1815 period). The
642 addition of historical information for three centuries reduces the uncertainty of $Q100$ and $Q1000$
643 flood quantiles (about 15%), despite only the number of exceedances being known. However,
644 some doubts remain about the completeness of the historical sample, as the posterior estimation
645 of S and t^* are larger than the prior. ~~Although the stationarity of the data has been checked, it is~~
646 ~~likely that the long series used in this paper is impacted by the imperfect completeness of the~~
647 ~~historical sample, which is based on damage perception. Indeed, the damage perception has~~
648 ~~probably evolved throughout the last five centuries at Beaucaire. Directly linking the~~
649 ~~consequences of a flood to its peak discharge is risky, as physical (levee failure, duration of~~
650 ~~flood...) or anthropic factors (population density, flood control policy, media coverage or~~
651 ~~politic context...) could impact the stationarity and the availability of the data. Therefore, it~~
652 ~~seems important to keep this in mind while using historical data, particularly during data~~
653 ~~collection. Using the whole set of available data doesn't always seem to be the best solution, as~~
654 ~~the exhaustiveness of the data must be the first criterion. Thus, as demonstrated in this article,~~
655 ~~it is essential to carry out a complete assessment of the various sources of uncertainty in order~~
656 ~~to decide to what extent the addition of historical information is useful to improve the estimation~~
657 ~~of flood risk.~~

658 Stationarity hypothesis may ~~also~~ be challenged by climatic variability at Beaucaire, as trends
659 in flood magnitudes have been identified in several regions of Europe (Hall *et al.*, 2014; Blöschl
660 *et al.*, 2020) and France (Giuntoli *et al.*, 2019). To date, there are no rules in France for taking
661 into account of the impact of climate change on flood risk estimates. However, it is still possible
662 to integrate temporal changes in climate processes or watershed characteristics within the
663 probabilistic model itself, as increasingly described in the literature (see Salas *et al.*, 2018, for
664 an overview). It is also important to note that out of the FFA scope, such long series remain
665 interesting for the study on the long-term variability of floods over several centuries, and their
666 value for risk awareness and memory.

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679 9. Appendix: Plotting position for unknown historical floods

680 The exceedance probability of the i^{th} value $q(i)$ of a sample ($q(1) \geq \dots \geq q(N)$) sorted by
 681 decreasing value is:

$$682 \quad p'_i = Prob[Q > q(i)] = \frac{i-a}{N+1-2a} \quad (\text{A1})$$

683 using for example $a = 0.44$, the optimum value for a Gumbel distribution (Cunnane, 1978).

684 Hirsch (1987) proposed to split a mixed sample, formed by (q_1, \dots, q_{NY_C}) AMAX values during
 685 NY_C years (continuous period) and NE_H historical values larger than a perception threshold S
 686 during NY_H years (historical period), into two sub-samples:

- 687 • NE exceedances of the threshold S on the whole period (divided into NE_H and NE_C
 688 exceedances on the historical and continuous periods), during NY years, with $NY = NY_H +$
 689 NY_C years:

$$690 \quad Prob[Q > q(i)] = \left(\frac{NE}{NY}\right) p'_i = \left(\frac{NE}{NY}\right) \frac{i-0.44}{NE+0.12} \quad i = 1, NE \quad (\text{A2})$$

- 691 • floods lower than S on the continuous period:

$$692 \quad Prob[Q > q(i)] = \left(\frac{NE}{NY}\right) + \left(1 - \frac{NE}{NY}\right) \frac{(i-NS)-0.44}{NY_C-NE_C+0.12} \quad i = NE + 1, NY_C + NE_H \quad (\text{A3})$$

693 In the current case study, as the discharge of historical floods is not known (only threshold
 694 exceedance), it is not possible to rank all values of the mixed sample. A way to circumvent this
 695 problem is to randomly rank the historical unknown floods amongst the NE_C floods larger than
 696 S during the continuous period:

- 697 • Step 1: randomly sample without replacement the rank of the NE_C floods of the continuous
 698 period within the whole period: `sample(x = 1:NE, size = NE_C, replace = FALSE)` (R code);
- 699 • Step 2: as we know the values of the NE_C floods larger than S during the continuous period,
 700 apply the ranks just sampled to them (i.e. the smallest sample rank is assigned to the largest
 701 flood, etc.);

702 • Step 3: assign the remaining ranks to the NE_H floods larger than S during the historical
703 period.

704 As we assigned ranks to all exceedances of the threshold S on the whole period, we are able to
705 compute their plotting position with equation (A2). Let denote $q_1 \geq \dots \geq q_{NE_C} \geq S$ the known
706 discharges of the continuous period larger than the threshold S , with their corresponding ranks
707 $r_1 < \dots < r_{NE_C}$. We now assign an interval to the unknown historical discharges (see Figure 8):

708 • If $r_l > 1$, we have $(r_l - 1)$ historical flood discharges larger than q_l . They will be plotted with
709 vertical dashed lines larger than q_l ;

710 • If $(r_{i+1} - r_i) > 1$, we have $(r_{i+1} - r_i)$ historical flood discharges within the interval $[q_{i+1}; q_i]$.
711 They will be plotted with vertical dashed lines larger $\frac{1}{2} (q_i + q_{i+1})$;

712 • If $r_{NE_C} < NE$, we have $(NE - r_{NE_C})$ historical flood discharges within the interval $[S; q_{NE_C}]$.
713 They will be plotted with vertical dashed lines larger $\frac{1}{2} (S + q_{NE_C})$.

714 This ordering is random, but it makes it possible to draw the empirical distribution of floods
715 and to compare it with the estimated GEV distributions.

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878 Data and codes availability: <https://github.com/MatLcs/HistoFloods>