

A Robust Calibration and Evaluation Framework for Dynamic Catchment Characteristics in Hydrological Modeling

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Abstract

Hydrological models often face challenges in accurately simulating hydrological processes within dynamic catchments due to simplifications of model structure. In a dynamic catchment where hydrological processes exhibit significant intra-annual or inter-annual variability, accurately capturing dynamic behaviours across different flow regimes is still challenging for models. To address these challenges, this study investigates calibration issues in dynamic catchments with a focus on two key aspects: the influence of objective function design on flow-phase-specific performance, and the limitations of sub-period calibration with dynamic parameters. Seven calibration experiments were designed to explore issues related to time-invariant parameters, objective function configurations, parameter correlations, dimensionality in global optimization, and abrupt parameter shifts. The experiments were conducted using the MOPEX dataset, which includes 219 basins across the United States, and were evaluated based on performance metrics, as well as state variables and fluxes. Among all calibration schemes, sub-period calibration with dynamic parameters exhibited the most reliable performance. Static parameter approaches often averaged catchment responses and poorly represented extreme flows, whereas enabling temporal variability to only a subset of parameters yielded limited improvement. In contrast, multi-parameter dynamic schemes significantly improved NSE and LNSE values and enhanced parameter transferability across flow phases, where the high-dimensional calibration strategy balanced dynamic adaptability with physical consistency, while the parallel calibration maintained accuracy through gradual parameter transitions despite higher variability in some catchments. This study demonstrates that sub-period calibration with dynamic catchment characteristics outperforms traditional static parameters by effectively capturing flow-regime variability and sustaining robust performance under changing catchment conditions, offering a generalizable solution for simulating hydrological processes in dynamic catchments.

1 Introduction

Hydrological models serve as essential tools in water management, supporting tasks such as runoff projection, disaster warning, and water-resource planning (Shao et al., 2023; Shrestha et al., 2021; Razavi et al., 2025). These models conceptualize hydrological processes with physically based parameters and state variables, enabling transparent simulations and process-informed diagnostic analysis of the catchment. However, limited understanding of the mechanisms underlying seasonal climate patterns, vegetation dynamics, and water storage variability has led existing model structures to rely on simplified representations of hydrological processes and steady-state assumptions (i.e., time-invariant parameters). Such assumptions only partially capture the dynamic catchment characteristics (Pathiraja et al., 2016; Deng et al., 2016; Wang et al., 2022b; Wen et al., 2021). A dynamic catchment is defined as one in which hydrological processes exhibit significant intra-annual or inter-annual variability, making their simulation particularly challenging. Dynamic catchment characteristics denote the time-varying states of a catchment that describe the temporal evolution of hydrological processes, such as precipitation seasonality and changes in vegetation cover under significant human disturbances. As a result, models tend to capture only the “average” behaviour of catchments, often at the cost of reduced accuracy in high- or low-flow phases (Longyang and Zeng, 2023; Yoshida et al., 2022). Understanding, modelling, and predicting dynamic hydrological processes with greater realism remain significant challenges in hydrological sciences (Bouaziz et al., 2022).

A key challenge in modelling catchments with dynamic variability lies in how to adapt the model to accurately reflect time-varying hydrological responses. Calibration aims to adjust model parameters using local observations, thereby tailoring a general model structure to the hydrological responses of a specific catchment. This process typically involves the definition of objective functions and the systematic exploration of parameter space. The mathematical form of the objective function determines which aspects of model performance are emphasized, such as the accuracy of peak flows or the representation of overall water balance (Gupta et

al., 2009; Fauer et al., 2021). In catchments with strong dynamics, however, the calibrated parameter sets may reflect not only the actual catchment behaviour but also implicit structural limitations and assumptions about boundary conditions. Consequently, the calibrated parameters often reflect trade-offs shaped by the objective function and model structure, leading to an averaged performance across flow phases (such as extreme high flow, high flow, middle flow, low flow, and extreme low flow).

One common strategy to improve model performance under structural limitations is to refine the configuration of the objective function to better emphasize key hydrological processes. Traditional calibration of hydrological models typically employs global evaluation metrics and time-constant parameters, focusing on the model's overall performance. However, this approach might average hydrological responses and fail to ensure accurate simulations across various flow phases and observational periods. In critical runoff events like floods and droughts, this static approach may fail to capture the dynamic catchment characteristic of hydrological processes, underscoring the need for more flexible calibration methods (Martel et al., 2025; Clark et al., 2021). Hence, various calibration techniques have been developed to incorporate dynamic catchment characteristics. One method involves revising the objective function based on selected evaluation criteria to improve model performance (Araya et al., 2023; Ji et al., 2023). Calibrations using multi-objective optimization algorithms better highlight different flow phases, but face potential challenges such as increased computational complexity, sensitivity to parameter settings, and slower convergence with more objective functions (Song et al., 2023; Carletti et al., 2022). Alternative approaches, like multi-weighted objective functions, can improve the simulation accuracy of specific time and flow phases. While these methods enhanced different flow phases and water balance, they may not effectively address structural deficiencies and cannot fundamentally enhance the model's overall performance (Lin et al., 2024; Fowler et al., 2018; Anderson and Radić, 2022).

Another strategy involves the use of dynamic parameters in hydrological models. A dynamic parameter is defined as a model parameter that varies across sub-periods rather than remaining fixed over the entire simulation period. Sub-periods are segments of the simulation period characterized by relatively homogeneous hydrological conditions, which are typically identified through clustering of the time series. The implementation of dynamic parameters addresses structural limitations of models and improves predictive performance across the full range of hydrological processes, rather than being restricted to specific flow regimes or periods (Zhang and Liu, 2021; Krapu and Borsuk, 2022). Recent studies have significantly advanced hydrological simulations by integrating the dynamic catchment characteristics. Clustering based on catchment characteristics, such as precipitation, evapotranspiration, and soil moisture, facilitates the clustering of dynamic hydrological processes into distinct sub-periods (Acuña Espinoza et al., 2024; Lakshmi and Sudheer, 2021). Wei et al. (2021) further broadened this perspective by highlighting the hydrological processes that arise from the interplay of various factors, including meteorological conditions, surface characteristics, and anthropogenic interference. This interaction among water balance components, such as soil, vegetation, and topography, exhibits temporal variability, which ideally should be captured by process-driven hydrologic simulation models. These changes need to be taken into account through model parameters (Wi and Steinschneider, 2022; Reichert et al., 2021). Zhang and Liu (2021) suggested that temporal variations in parameters reflect the evolving environment. However, some fundamental problems still need to be addressed before applying the dynamic parameters. Sub-period calibration with dynamic parameters involves the hydrological model structure, global optimization, physical mechanisms of dynamic catchment characteristics, as well as complex relationships between the parameters, state variables, and fluxes.

To address the model deficiencies and improve simulation across all flow regimes, it is imperative to re-examine the time-varying information in historical hydrological and meteorological data, extract dynamic catchment characteristics, and address the variation in calibration. This study investigates calibration challenges in dynamic catchments and proposes a structured framework to address

two major issues: the influence of objective function design on flow-phase-specific performance, and the limitations of sub-period calibration with dynamic parameters. Seven experiments are developed to systematically evaluate these aspects. Experiments 1–3 focus on the effects of time-invariant parameters and various objective function configurations. Experiments 4–7 explore issues in dynamic parameter calibration, such as parameter correlation, dimensionality, and state transitions. Model performance is assessed through multiple metrics and internal diagnostics across 219 MOPEX catchments.

2 Study area

The Model Parameter Estimation Experiment (MOPEX) is an international project aimed at developing enhanced techniques for a priori estimation of parameters in hydrologic models and land surface parameterization schemes of weather and climate models (Duan et al., 2006). A comprehensive MOPEX database has been developed that contains historical hydrometeorological data and land-surface characteristics data for numerous hydrological catchments in the United States (US) and other countries. This study utilizes the dataset from 219 catchments spatially distributed across the contiguous US (Fig. 1a). Rigorous screening criteria were applied to ensure the acquisition of high-quality data. The screening process involved three key considerations: (1) no missing or non-physical data throughout the study period; (2) minimal interference from anthropogenic influences in both temporal and spatial dimensions; and (3) a large spatial distribution scale of the selected catchments, including diverse meteorological and underlying surface conditions. The dataset for selected catchments includes the hydrometeorological forcing data, land-surface data, and streamflow data, covering the period from 1983 to 2000. Hydrometeorological data includes daily precipitation data (P), temperature data (T), and streamflow (Q) provided by the MOPEX dataset, as well as potential evaporation data (PE) calculated by the Hamon model (McCabe et al., 2015). The Normalized Difference Vegetation Index (NDVI) was used as one of the land-surface indicators to represent the vegetation coverage of the catchments, which had a spatial resolution of 8 km and a temporal resolution of half-monthly intervals (Tucker et al., 2010). Based on these criteria, a total of 219 catchments were selected (Fig. 1a), spanning a wide range of hydrological and meteorological characteristics, making them ideal for testing various model structures under diverse conditions (Duan et al., 2006).

In addition to the large-sample analysis of the MOPEX dataset, five representative catchments, Case A (12027500), Case B (6192500), Case C (7211500), Case D (1643000), Case E (1531000), are analyzed in more detail as case studies. These catchments encompass a variety of Köppen climate classifications and different dominant dynamic catchment characteristics, facilitating comparison of calibration strategies and evaluation of their robustness under diverse hydroclimatic conditions. Their locations and characteristics are listed in Table 1 and will be analyzed in depth in the subsequent sections.

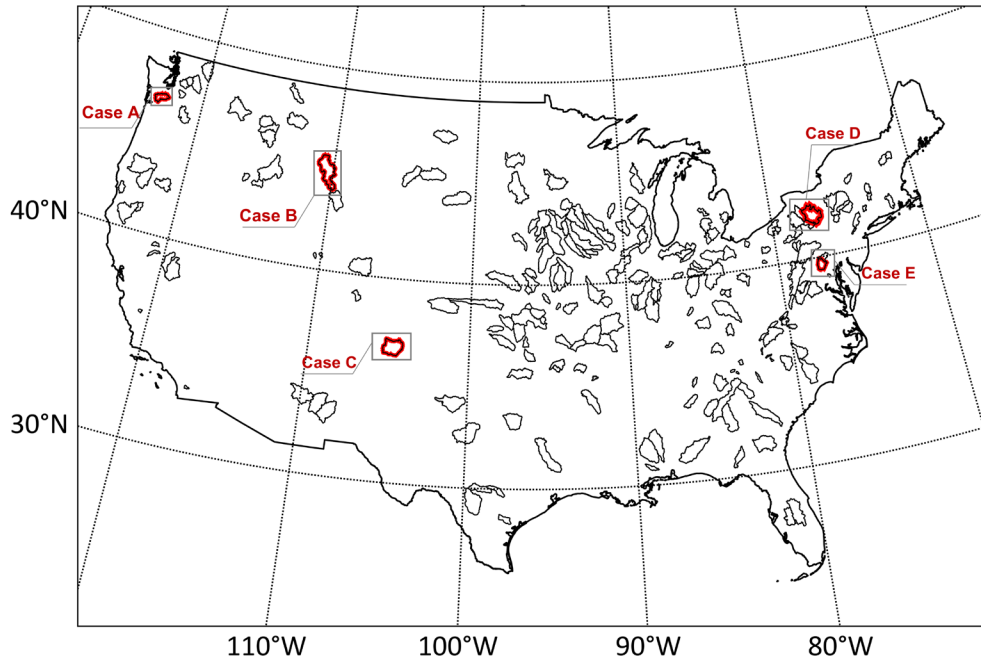


Figure 1. Location map of the catchment area used in this study, where cases A, B, C, D, and E correspond to catchments 12027500, 6192500, 7211500, 1643000, and 1531000 (from west to east) are highlighted with red outlines for reference.

Table 1. Summary of catchment characteristics for study cases.

ID	12027500	6192500	7211500	1643000	1531000
Location	122.99°W	110.40°W	104.76°W	77.25°W	77.24°W
Area (km ²)	895	3551	2850	817	2056
Climate	Csb	Dfc	Bsk	Cfa	Dfb
Mean <i>P</i> (mm)	1548.78	735.71	491.70	1068.49	870.53
Mean <i>PE</i> (mm)	596.53	731.59	1279.88	897.63	711.06
Mean <i>Q</i> (mm)	1110.19	369.79	10.08	430.15	366.76
Mean elevation (m)	253.06	2441.28	2262.91	191.80	492.25
Mean slope (°)	12.16	15.26	9.44	4.99	8.25
Runoff ratio	0.72	0.50	0.02	0.40	0.42
Aridity index	2.60	1.01	0.38	1.19	1.23
Forest cover (%)	71.96	36.95	16.76	31.31	57.36
Land use	Evergreen Forest, Pasture/Hay	Evergreen Forest, Shrub/Scrub	Evergreen Forest, Grassland/Herbaceous	Deciduous Forest, Cultivated Crops	Deciduous Forest, Pasture/Hay

3 Methods

Hydrological processes within catchments commonly exhibit significant annual and inter-annual variability. However, conventional hydrological models often fail to capture these temporal dynamics due to structural simplifications, resulting in averaged responses and reduced simulation accuracy. To address these limitations and improve model performance across different flow phases, this study investigates two strategies: (1) refining the configuration of objective functions during calibration to enhance sensitivity to temporal variations; and (2) integrating dynamic catchment characteristics into the modelling framework through dynamic parameterization, while systematically investigating the associated calibration challenges. This study aims to

evaluate the effectiveness and limitations of various calibration strategies under dynamic catchment conditions and to develop a robust calibration framework for catchments with temporal dynamics.

3.1 Hydrological model

The two investigated strategies involve only parameter configuration and calibration procedures, without necessitating structural changes to the hydrological model. Such strategies are compatible with lumped, semi-distributed, and fully distributed models, encompassing both conceptual and physically based types. To evaluate and compare the applicability of different calibration strategies under dynamic catchment conditions, the simple conceptual hydrological model, HYMOD (Hydrological MODEL) (Moore, 1985), is employed for verification. The HYMOD model is a conceptual rainfall-runoff model with a simple structure (five parameters), low input requirements, and empirical physical interpretations. It has been successfully used in streamflow prediction across America and many other regions (Vrugt et al., 2003; Wagener et al., 2001). In addition, to enhance model performance in snowy areas, the Degree-day model is applied to account for the snow melt (Supporting Information S1.6) (Wang et al., 2022a).

The structure of the HYMOD model is shown in Fig. 2. Precipitation (P) and potential evapotranspiration (PET) drive a probability-distributed soil-moisture store characterized by a maximum capacity (H_{uz}) and a shape parameter (B). Actual evaporation (AE) is limited by potential evapotranspiration and soil water availability. The remaining rainfall infiltrates to recharge the soil-moisture storage (XH_{uz}). When XH_{uz} reaches its maximum capacity (H_{uz}), the surplus is released as excess rainfall (saturation-excess runoff, OV). This excess rainfall is then partitioned by α into inputs to the quick-flow and the slow-flow pathways. Quick flow is routed through a cascade of three linear reservoirs (states X_{q1} – X_{q3}) governed by K_q , producing outflow Q_q , while the slow flow is routed through a single linear reservoir governed by K_s , producing outflow Q_s . The simulated discharge (Q_{sim}) is computed as the sum of Q_q and Q_s (Wang et al., 2022a). Detailed information on the HYMOD model parameters, state variables, and fluxes is provided in Table 2.

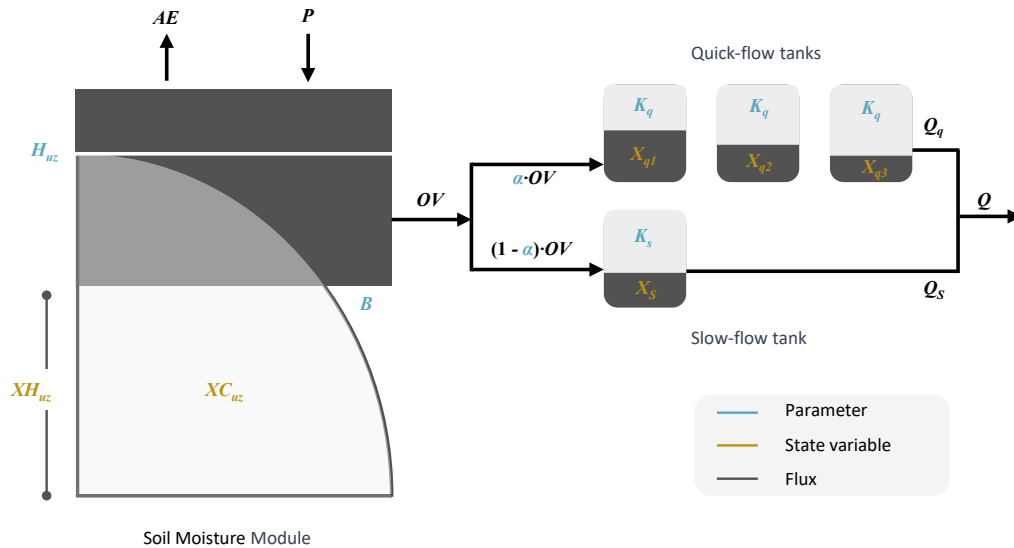


Figure 2. Schematic diagram of the HYMOD structure and principles (Vrugt et al., 2003; Wagener et al., 2001).

Table 2. HYMOD model parameters, state variables, and fluxes (Vrugt et al., 2003; Wagener et al., 2001).

Label	Property	Range	Description
H_{uz}	Parameter	10–1500 mm	Maximum height of the soil moisture accounting tank
B	Parameter	0–1.99	Scaled distribution function shape
α	Parameter	0–0.99	Quick or slow split
K_q	Parameter	0.5–0.99	Quick-flow routing tanks' rate
K_s	Parameter	0–0.5	Slow-flow routing tank's rate
XH_{uz}	State variable	mm	Upper-zone soil moisture tank state height
XC_{uz}	State variable	mm	Upper-zone soil moisture tank state contents
X_q	State variable	mm	Quick-flow tank state contents
X_s	State variable	mm	Slow-flow tank state contents
AE	Flux	mm d ⁻¹	Actual evapotranspiration flux
OV	Flux	mm d ⁻¹	Excess rainfall flux
Q_q	Flux	mm d ⁻¹	Quick-flow flux
Q_s	Flux	mm d ⁻¹	Slow-flow flux
Q_{sim}	Flux	mm d ⁻¹	Total simulated streamflow flux

3.2 Clustering hydrological processes

Sub-period calibration provides a practical means of linking dynamic catchment characteristics with hydrological models. In sub-period calibration, the simulation period is clustered into multiple sub-periods characterized by relatively homogeneous hydrological conditions, allowing dynamic parameters to better reflect temporal variations in catchment behaviour across different streamflow regimes (Zhang and Liu, 2021). In this study, the clustering of sub-periods is guided by temporal variations in key hydrometeorological and land-surface variables. The methodological framework consists of three key steps: (1) constructing a dynamic catchment characteristic index system to describe catchment states; (2) extracting dynamic catchment characteristics through screening and dimensionality reduction; and (3) applying unsupervised clustering to cluster the time series into sub-periods with similar hydrological processes for subsequent sub-period calibration.

Describing dynamic catchment characteristics: To characterize the temporal dynamics of catchment behaviour, a dynamic catchment characteristic index system comprising a climatic subsystem and a land-surface subsystem is constructed to represent the time-varying states of the catchment. The climatic subsystem includes core hydrometeorological variables such as precipitation (P), temperature (T), and potential evapotranspiration (PE), along with corresponding extreme climatic indicators. The land-surface subsystem reflects evolving surface conditions through indicators such as antecedent runoff, runoff coefficient, and the normalized difference vegetation index (NDVI). All indicators are sampled using a moving window approach, with the optimal window length determined through a time-windowed Bayesian inference framework based on predictive log-score (PLS) performance (Hsueh et al., 2024). The framework is designed to preserve long-term trend signals, suppress short-term high-frequency noise, and improve the stability and robustness of dynamic catchment characteristic extraction.

Extracting dynamic catchment characteristics: Not all indicators exhibit significant dynamic catchment variability; therefore, filtering irrelevant or redundant variables is essential to retain meaningful catchment dynamics. A threshold-based screening is applied to identify variables exhibiting significant seasonality, retaining only relevant subsystems and forming an initial pool of candidate indicators (see Supporting Information S2.1 for detailed criteria). The Maximal Information Coefficient (MIC) is then employed to quantify linear and nonlinear associations between candidate indicators and streamflow, ensuring hydrological relevance. To mitigate multicollinearity and reduce dimensionality, Principal Component Analysis (PCA) is performed, with the

first two principal components retained for clustering. This multi-step filtering and reduction procedure ensures robust extraction of dynamic catchment characteristics and provides a solid basis for sub-period clustering according to hydrological similarity.

Clustering hydrological processes: Based on the extracted dynamic catchment characteristics, the time series is clustered into distinct sub-periods using the unsupervised Fuzzy C-Means (FCM) clustering algorithm. The optimal number of clusters is determined through a combination of clustering validity indicators, including the Partition Coefficient (SC), Separation Index (S), and Xie–Beni (XB) index, which collectively assess clustering compactness and separation. In addition, the elbow method is employed as a supplementary diagnostic to identify the inflection point beyond which further increases in cluster number yield diminishing returns. Clustering is performed in the principal component space, enabling effective capture of structural patterns in catchment dynamics. The resulting sub-periods provide a robust foundation for integrating dynamic parameters into hydrological models.

In addition, the sub-period clustering is developed exclusively using data from the calibration period. To independently evaluate the generalization capability and robustness of the model under unseen conditions, no model training or parameter adjustment is performed during the evaluation period.

3.3 Calibration experiments

To systematically evaluate how calibration strategies capture catchment dynamics and improve the simulation of diverse flow regimes, a diagnostic framework comprising seven calibration strategies is developed. These experiments sequentially address key challenges in representing time-varying hydrological behaviour, with a focus on objective function design and time-varying parameterization (Fig. 3).

Experiments 1–3 use time-invariant parameters and focus on the design and weighting of objective functions. Experiment 1 establishes a baseline with standard global calibration. Experiment 2 applies a multi-objective approach to explore trade-offs between high and low flows. Experiment 3 designs a composite objective function to enhance simulation performance across a range of flow conditions. Experiments 4–7 incorporate time-varying parameters to better represent temporal catchment variability and examine related calibration challenges. Experiment 4 allows only the most sensitive parameter to vary, assessing partial dynamization and parameter compensation. Experiment 5 makes all parameters dynamic, raising issues of parameter dimensionality. Experiment 6 investigates the effects of abrupt parameter shifts on model continuity. Experiment 7 introduces smooth parameter transitions to reduce instability while preserving responsiveness to catchment dynamics.

Throughout the experiments, the Shuffled Complex Evolution algorithm (SCE-UA) is employed to search for the globally optimal parameter set (Duan et al., 1993). The HYMOD model is configured for catchments over 19 years from 1982 to 2000, with 1982 as the warm-up year, 1983–1995 for calibration, and 1996–2000 for evaluation. All other model parameters are held at their default values. Unless specified otherwise, model calibration is guided by the following objective function:

$$OF = 0.5 \cdot NSE + 0.5 \cdot LNSE \quad (1)$$

Experiment 1 uses time-invariant parameters calibrated over the entire period without sub-period clustering. It serves as a baseline for assessing standard global calibration.

Experiment 2 approximates a multi-objective calibration by combining NSE and LNSE into a weighted objective: $w \times NSE + (1-w) \times LNSE$. The weight w varies from 0 to 1 (step = 0.05), forming a series of single-objective optimizations using SCE-UA with time-invariant parameters. This setup explores trade-offs between flow regimes without changing the optimization algorithm.

Experiment 3 adopts a composite objective function to improve simulation across flow regimes. It integrates RMSE with flow duration curve (FDC)-based metrics (RMSE_Q95, Q70, Qmid, Q20, Q5, as listed in Table 3), representing different flow phases. Weights are derived from Experiment 1 using AHP, PP, and CRITIC methods (refer to Supporting Information S1.7).

215 Experiment 4 introduces time-varying parameters by allowing only the most sensitive parameter to vary across sub-periods, while all others remain fixed. State variables and fluxes are passed between sub-periods through an inheritance approach.

Experiment 5 extends the dynamic calibration to all parameters, with distinct values assigned to each sub-period. As a result, the number of parameters increases in proportion to the number of sub-periods, generating a high-dimensional calibration space. State and flux continuity between sub-periods is maintained through the same inheritance mechanism used in Experiment 4.

220 Experiment 6 investigates the impact of abrupt parameter transitions across sub-periods. Parameters are optimized independently for each sub-period. During model runs, parameter sets switch discretely between sub-periods, while state variables and fluxes are inherited to maintain continuity.

Experiment 7 adopts the same calibration structure as Experiment 6 but incorporates smooth parameter transitions during evaluation. The parallel calibration strategy is designed to preserve continuity in parameter evolution while maintaining water balance within each sub-period.

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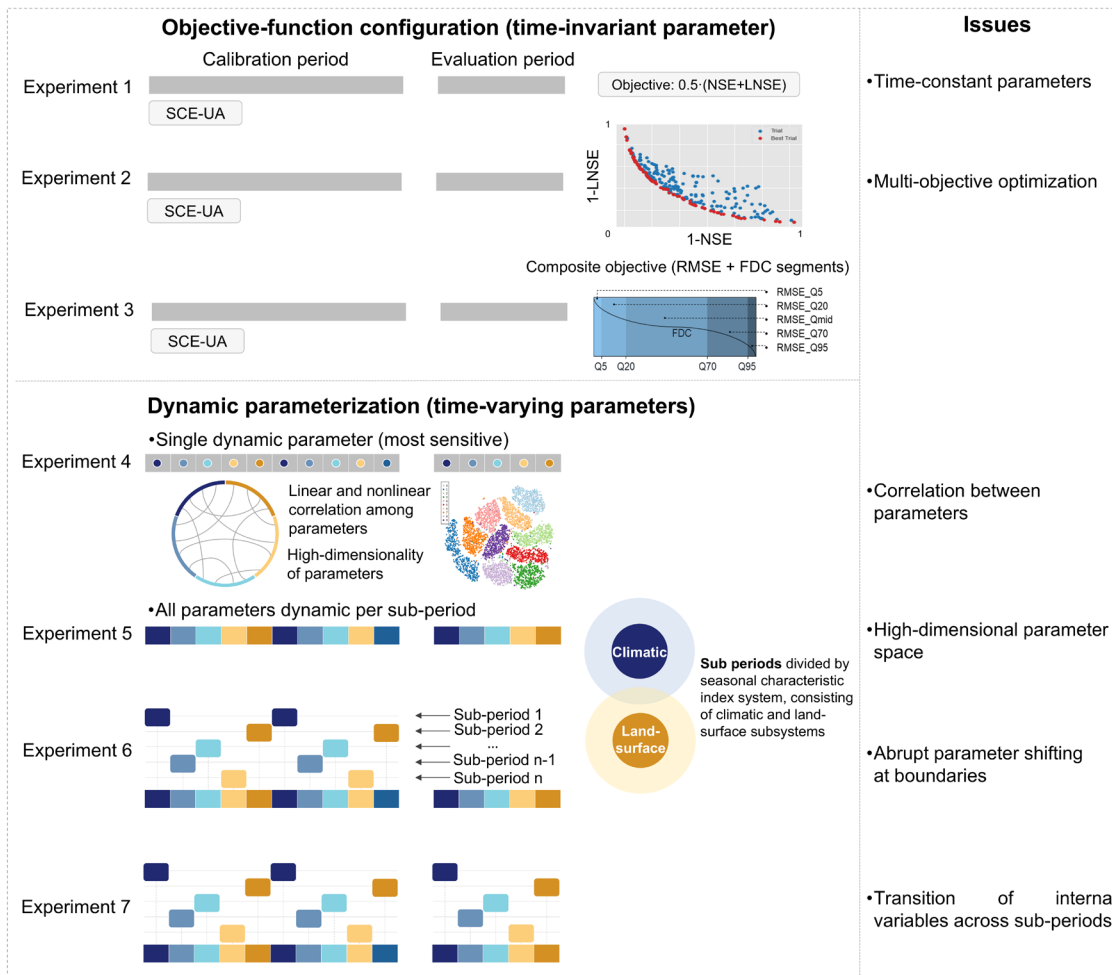


Figure 3. Schematic illustration of the seven calibration experiments. The colour bands represent state variables and fluxes, which are continuously transferred within the same period. In Experiments 1, 2, and 3, the parameters are time-invariant, but the experiments differ in their objective function configurations. Conversely, experiments 4, 5, and 6 maintain a consistent objective function, but vary the parameters across

230 different experiments. In Experiment 4, the dynamic of only the specific parameter is operated, and the other fixed parameters are optimized
simultaneously. In Experiment 5, the parameter set is dynamized. The parameter sets in different sub-periods are optimized simultaneously. In
Experiment 6, the data from the individual sub-periods are used for minimizing the objective function, while the model is run for the whole
period. In the evaluation period, the parameter set between two consecutive sub-periods is updated accordingly. In Experiment 7, the calibration
235 is the same as in Experiment 6. In the evaluation period, the simulated flow data from each separate sub-period are combined and compared with
the observed flow.

3.4 Model evaluation

3.4.1 Multi-criteria evaluation

Model simulations are typically evaluated using performance metrics, which can be divided into statistical and signature metrics
(Pfannerstill et al., 2014; Yilmaz et al., 2008; Clark et al., 2021). However, a limitation exists with many common performance
240 metrics: They only focus on overall or specific segments of the streamflow series, neglecting other parts that may have the greatest
practical impact. Hence, for diagnostic analysis, streamflow segments of the flow duration curve (FDC) are used to identify flow
phases where model performance is poor (Pfannerstill et al., 2014; Schwemmler et al., 2021). Performance across multiple
streamflow segments is assessed through the criteria defined in Table 3, providing a comprehensive evaluation of model
performance.

245 **Table 3.** Description of performance metrics.

Metric	Formula	Description
NSE	$NSE = 1 - \frac{\sum_{i=1}^n (Q_{obs,i} - Q_{sim,i})^2}{\sum_{i=1}^n (Q_{obs,i} - \bar{Q}_{obs})^2}$	Sensitive to peaks and discharge dynamics
LNSE	$LNSE = 1 - \frac{\sum_{i=1}^n (\log Q_{obs,i} - \log Q_{sim,i})^2}{\sum_{i=1}^n (\log Q_{obs,i} - \overline{\log Q_{obs}})^2}$	Emphasizing low flows with the log of discharge
RMSE_Q5	$RMSE_{Q5} = \sqrt{\frac{1}{n_{Q5}} \sum_{i \in I_{Q>Q5}} (Q_{obs,i} - Q_{sim,i})^2}$	RMSE in FDC Q5 very-high-segment volume
RMSE_Q20	$RMSE_{Q20} = \sqrt{\frac{1}{n_{Q20}} \sum_{i \in I_{Q5 < Q < Q20}} (Q_{obs,i} - Q_{sim,i})^2}$	RMSE in FDC between Q5 and Q20 high-segment volume
RMSE_Qmid	$RMSE_{Qmid} = \sqrt{\frac{1}{n_{Qmid}} \sum_{i \in I_{Q20 < Q < Q70}} (Q_{obs,i} - Q_{sim,i})^2}$	RMSE in FDC between Q20 and Q70 mid-segment volume
RMSE_Q70	$RMSE_{Q70} = \sqrt{\frac{1}{n_{Q70}} \sum_{i \in I_{Q70 < Q < Q95}} (Q_{obs,i} - Q_{sim,i})^2}$	RMSE in FDC between Q70 and Q95 low-segment volume
RMSE_Q95	$RMSE_{Q95} = \sqrt{\frac{1}{n_{Q95}} \sum_{i \in I_{Q < Q95}} (Q_{obs,i} - Q_{sim,i})^2}$	RMSE in FDC Q95 very-low-segment volume
RMSE	$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (Q_{obs,i} - Q_{sim,i})^2}$	RMSE sensitive to flood peaks
MSE	$MSE = \frac{1}{n} \sum_{i=1}^n (Q_{obs,i} - Q_{sim,i})^2$	MSE is sensitive to high flow
MSEL	$MSEL = \frac{1}{n} \sum_{i=1}^n (\log Q_{obs,i} - \log Q_{sim,i})^2$	MSEL is sensitive to low flow
MAE	$MAE = \frac{1}{n} \sum_{i=1}^n Q_{obs,i} - Q_{sim,i} $	MAE is measuring the overall discharge

Notes: Where $Q_{obs,i}$ and $Q_{sim,i}$ represent the observed and simulated streamflow at time step i , and \bar{Q}_{obs} is the mean observed flow. n is the total number of time steps. For log-transformed metrics (e.g., LNSE and MSEL), log denotes the natural logarithm. Note that the FDC is usually split into various segments to describe different flow characteristics of a catchment (Gupta et al., 2009; Cheng et al., 2012; Pfannerstill et al., 2014). The RMSE with quadratic character is usually used to evaluate poor model performance due to the strong sensitivity to extreme positive and negative error values.

3.4.2 State variables and fluxes

The evaluation of state variables and fluxes links sub-period calibration and dynamic parameterization to internal model continuity and responsiveness, helping to diagnose performance differences across experiments. The internal behaviour of the hydrological model, involving the time series of state variables and fluxes that constitute subspaces within the model state space, is visualized in graphs and categorized by the operation of different sub-periods. Such visualization facilitates the identification of issues in calibration experiments. For instance, unreasonable values exceeding operational boundaries often signal errors in model operation triggered by abrupt parameter shifts. Similarly, unresponsive values may indicate either operational errors or unique catchment characteristics. Furthermore, a flux map is developed and applied to evaluate the equifinality or uncertainty of internal model behaviour by plotting different components of model fluxes (Khatami et al., 2019). The flux map is a ternary or binary plot where each dimension represents a model runoff flux, and each model run is projected as a single point based on the proportions of its equifinal runoff fluxes to the total simulated Q . To HYMOD model, the components with Q_{q1} , Q_{q2} , and Q_s are defined, which represents the runoff component of the output of quick-release reservoirs of linear routing component (OV_1), the output of quick-release reservoirs of nonlinear routing component (OV_2) and the output of slow-release reservoir (Q_s). The point cloud pattern from ternary or binary plots can vary from very constrained to filling the entire feasible flux space, which represents the different dominant components of runoff. Thus, the point cloud on the flux maps is an expression of the model uncertainty; filling a larger space on the flux map indicates higher degrees of model uncertainty.

4 Results

4.1 Defined sub-periods based on catchment dynamics

To support the implementation of sub-period calibration, periods were identified for all 219 catchments based on variations in dynamic catchment characteristics. The results indicate that dynamic catchment patterns are widespread across the study area, with 219 catchments exhibiting significant variation in at least one hydrometeorological variable (precipitation, temperature, potential evapotranspiration, NDVI, or runoff). Spatially, precipitation seasonality is more significant in the central and western regions; potential evapotranspiration seasonality is widespread, especially in northern areas; runoff seasonality is most evident in the central and northeastern regions; and vegetation seasonality is also common, with only a few high-latitude catchments lacking significant dynamic variation.

A data-driven method was applied to extract relevant information and cluster the time series into distinct periods. The optimal sampling window for each catchment was identified using a Bayesian inference approach, with values ranging from 5 to 150 days (mean = 59.45 days). The MIC was then applied to filter out indicators with weak correlation to runoff. PCA was performed for dimensionality reduction, and the first two components explained, on average, 83.5% of the total variance. Based on the reduced feature space, FCM clustering was used to group time steps, with an average of 4.2 periods identified per catchment.

To illustrate the applicability of the method under diverse hydro-climatic conditions, five representative catchments were selected, covering a range of climate zones and dominant hydrological drivers. These catchments were also used in the subsequent modelling experiments. As shown in Fig. 4a and Fig. 4b, their optimal window lengths ranged from 30 to 150 days, with 12 to 31 indicators retained after screening. In all five cases, the number of identified periods ranged from 3 to 5. When compared with hydrographs, the identified periods aligned well with key hydrological processes, such as rising and recession limbs (Fig. 4c). In catchments with strong dynamic signals (e.g., Case A and Case B), the identified periods showed stable interannual patterns, while in catchments with greater variability (e.g., Case D and Case E), the clusterings still captured major dynamic catchment characteristics. These period clusterings provide a physically interpretable structure that supports the dynamic parameterization and modelling experiments introduced in the following sections. Considering the performance of the seven modelling experiments across both calibration and evaluation periods, Experiments 5 and 7 are considered the recommended experiments for capturing dynamic catchment characteristics. Experiment 5, with multi-parameter dynamic calibration, achieves high predictive accuracy across diverse flow regimes, although it may slightly compromise physical consistency in runoff generation. Experiment 7, incorporating smooth parameter transitions, maintains comparable accuracy while promoting more consistent and physically reasonable runoff strategies across sub-periods, thus offering a balanced approach between model performance and hydrological interpretability. Detailed analysis of the results will be presented in the following sections.

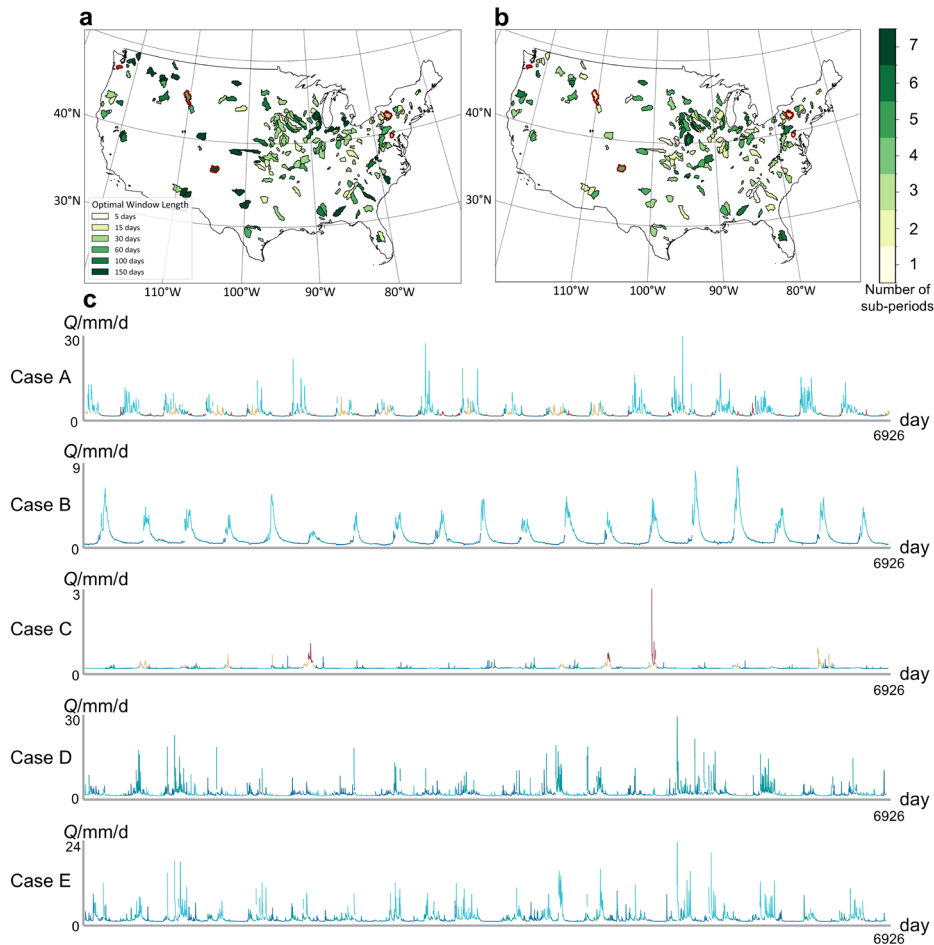


Figure 4. **a**, Optimal window lengths of catchment area used in this study for the sub-period clustering. **b**, Number of subperiods reflecting results from Section 3.2. **c**, Visualization of clustering results on the hydrograph for the respective study cases.

4.2 Model performance

300 To compare seven experiments in dynamic catchments and to identify potential limitations in model calibration, the evaluation is conducted across 219 catchments characterized by hydrological variability. As shown in Fig. 5, the NSE and LNSE values during both calibration and evaluation periods reveal differences in the ability of diverse calibration schemes to capture high- and low-flow conditions. The median NSE reached only 0.4–0.5 in Experiments 1 and 2, and although the LNSE approached 0.7, negative values are frequently observed. It is suggested that global optimization or simple weighted objective functions often lead to an

305 averaging of catchment responses, thereby limiting accuracy for both high- and low-flow conditions. Experiment 3 employed an objective function defined as: $OF = 0.27 \cdot RMSE_{Q5} + 0.16 \cdot RMSE_{Q20} + 0.08 \cdot RMSE_{Qmid} + 0.24 \cdot RMSE_{Q70} + 0.25 \cdot RMSE_{Q95}$, the weighting scheme explicitly accounted for extremely high (Q95), high (Q70), medium (Qmid), low (Q20), and extremely low (Q5) flows. Despite this design, both NSE and LNSE declined relative to Experiment 1. The decrease may be attributed to excessive parameter adjustments aimed at fitting a limited number of extreme events, which reduced the predictive

310 accuracy of the overall streamflow process. When single dynamic parameters are introduced in Experiment 4, median NSE and LNSE increased to approximately 0.55 and 0.8, respectively, with narrower interquartile ranges. These outcomes indicate that dynamic parameters enhanced the ability of the hydrological model to capture temporal variability, although structural errors persisted, as reflected in local outliers. More significant improvements emerged with multiple dynamic parameters. Experiment 5 achieved median NSE and LNSE values of approximately 0.7–0.8 in both calibration and evaluation periods. Although high-

315 dimensional optimization increased computational demand and LNSE variability in some basins, overall performance represented a balanced trade-off between dynamic adaptability and physical consistency. Experiment 6 also performed well during the calibration period; however, its abrupt parameter switching led to a particular decline of LNSE and increased dispersion in the evaluation period. Experiment 7 addressed these shortcomings by applying a gradual parameter-switching strategy during the evaluation period. As shown in Fig. 5, the boxplots are more compact and shifted toward higher values, indicating that stable and

320 consistent performance was achieved across most basins. However, compared with Experiment 5, Experiment 7 displayed a greater number of outliers, particularly in LNSE, where they tended to cluster at lower values, suggesting higher variability in model performance across catchments. The overall accuracy remained comparable to that of Experiment 5. In summary, compared with static calibration schemes (Experiments 1–3), single dynamic parameter calibration (Experiment 4) improved simulative accuracy, while multi dynamic parameter calibration produced further gains. Among all experiments, Experiments 5 and 7 demonstrated the

325 most robust and accurate performance.

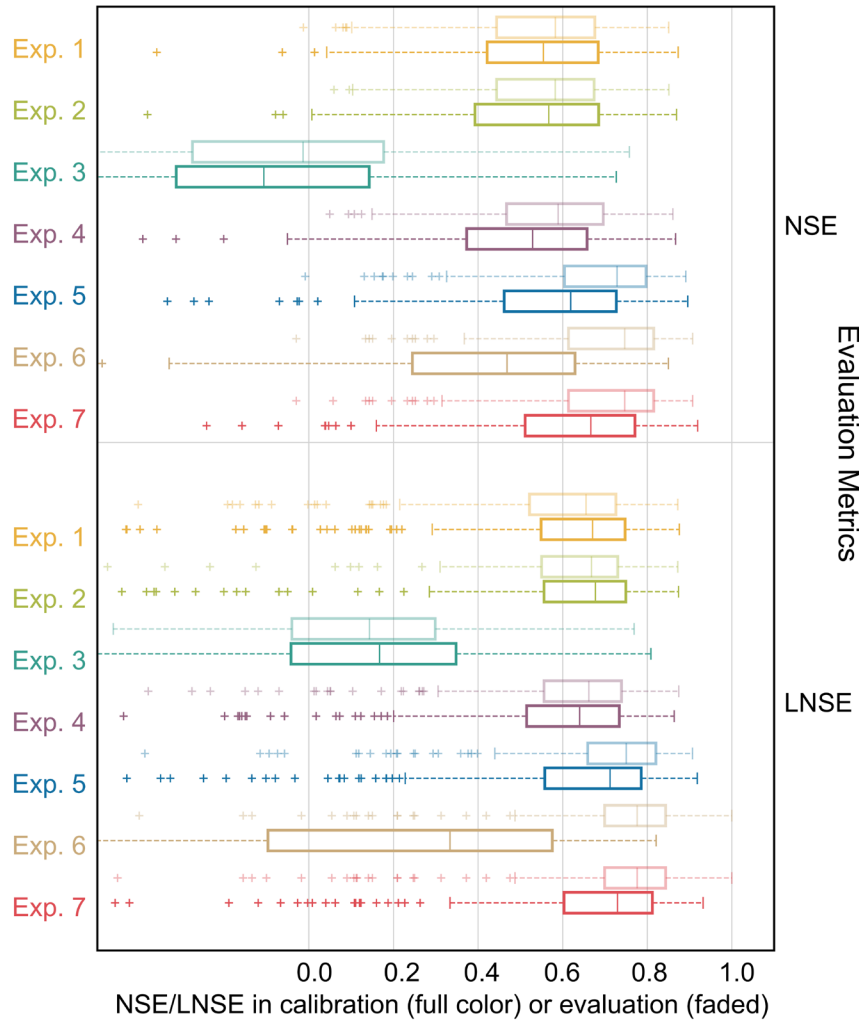


Figure 5. Performance of seven calibration experiments on the MOPEX dataset across 219 catchments. Boxplot colour denotes different experiments. The whiskers extend a maximum of 1.5 times the interquartile range. Values beyond the whiskers are marked as outliers and are denoted as +.

330 To further examine how the different experiments under various hydrological conditions, a detailed assessment of five representative catchments is conducted with diverse dynamic patterns and baseline model performance. Fig. 6 presents the model performance of the seven experiments in five study cases. In all study cases, Experiment 1 demonstrated low simulation accuracy and limited parameter transferability across different flow phases, particularly under extremely low-flow and high-flow conditions. The results in Experiments 2 and 3 show limitations on both objective functions compared to Experiments 5 and 7. Adjusting the

335 weights between NSE and LNSE improved accuracy for mid-phase flows but failed to account for other flow phases. For instance, in case A, considering NSE, the metric increased from 0.48 (Experiment 1) to 0.62 (Experiment 2) during the calibration period, and from 0.50 to 0.64 during the evaluation period. However, both RMSE_Q5 and RMSE_Q95 increased. Relative to Experiment 1, the RMSE_Q95 exhibited a diminished performance during both the calibration and evaluation periods in Experiment 2. Despite prioritizing high and low flows through a weighted objective function, Experiment 3 underperforms compared to Experiment 1.

340 While the objective function emphasizes these targeted phases, adjusting its weights unexpectedly failed to improve performance in the target flow phase and even worsened the model's performance in other evaluation metrics, indicating that this scheme exhibits instability in its performance across different flow phases. For instance, in case A, the NSE decreased from 0.48 to -0.74 in the calibration period, and from 0.50 to -0.27 in the evaluation period, compared with Experiment 1. In case C, the performance decline

was more significant, with NSE values during both the calibration and evaluation periods approaching zero. Experiment 4 exhibited only marginal improvements over Experiment 1 across most metrics. In contrast, Experiments 6 and 7, which employed the same calibration procedures, achieved strong overall performance during the calibration period, particularly in reproducing high flows and flood peaks. However, during the evaluation period, Experiment 6 showed inconsistent performance—while excelling in certain aspects such as high-flow simulation, it experienced significant degradation in others (e.g., NSE, MAE, and RMSE_Q95). The extent of performance decline in Experiment 6 varied among catchments: in case D, RMSE_Q95 increased by only 0.61 mm/d compared to the calibration period, whereas in case C, the deterioration was most severe, with RMSE_Q95 increasing by 17.64 mm/d. The decline can be attributed to extremely dry conditions, where runoff volumes approached zero (less than 0.01 mm), making small deviations translate into large relative errors. Notably, across all study cases, Experiments 5 and 7 consistently maintained excellent performance during the evaluation period, closely mirroring their calibration results and outperforming other experiments in nearly all metrics. Moreover, analysis of parameter transferability revealed minimal differences between calibration and evaluation periods for Experiments 5 and 7. Hence, Experiments 5 and 7 demonstrate the superior performance across all evaluation metrics, exhibiting improvements in simulations across various flow phases.

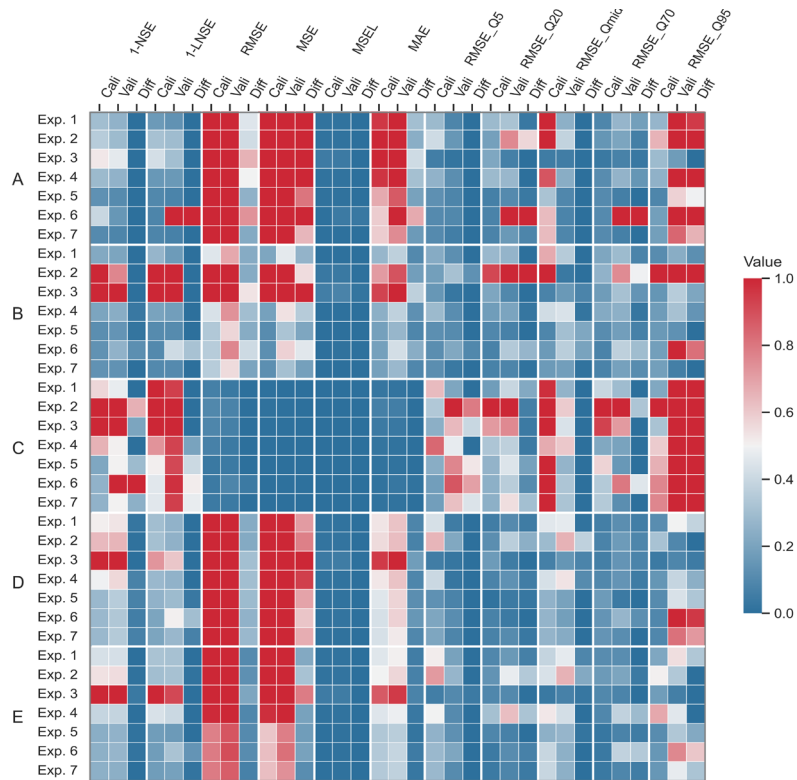


Figure 6. The model performance of seven experiments in five study cases was assessed using multiple evaluation metrics. Lower values reflect superior performance.

360 4.3 State variables and fluxes

The state variables and fluxes reflect the internal operation of the hydrological model. The assessment results of state variables and fluxes through seven calibration experiments for case study A are illustrated in Fig. 7 and Fig. 8 (results of cases B, C, D, and E are shown in S3 of Supporting Information). Experiments 1, 2, and 3 exhibited only minimal differences in both state variables and flux time series, with only the results of Experiments 1 and 3 shown for clarity. A slight improvement is shown in Experiment 4 compared with the time-invariant parameter schemes; however, small mismatches remain during flow recessions and peak timings. This indicates that the dynamic adjustment of a single parameter is insufficient to represent the full range of catchment

dynamics. Notably, the state variable X_q and flux Q_q in Experiment 4, the display is abnormally flat compared to Experiment 1, showing a wrong response of the rapid runoff module to input variations.

In Experiment 6, abrupt parameter switching is applied across sub-periods. The state variable X_q and flux Q_q in Experiment 6, exhibit step changes or even discontinuities at the switching boundaries, with large deviations during low-flow sub-periods. The phenomenon is particularly evident in cases B and D. These results indicate that abrupt switching disrupts water balance continuity, thereby reducing performance in low-flow simulations. Despite these setbacks, Experiments 5 and 7 introduced significant improvements across all study cases. In Experiment 5, multi-parameter dynamic calibration is applied while continuity of state variables and fluxes is maintained. As shown in Fig. 7 and Fig. 8, in case A, the flux variables Q_q and Q_s transition smoothly across sub-periods without visible discontinuities, the state variables $X_{H_{uz}}$ and $X_{C_{uz}}$ also connect consistently across sub-periods, indicating that multi-parameter dynamic calibration captures the catchment dynamics of soil moisture and storage processes. However, Experiment 5 shows limitations in maintaining the consistency of simulated discharge (Q_{sim}). For example, in case B, the baseline extent of Q_{sim} exhibited slight drift, reflected in systematic differences in response intensity to similar rainfall events across adjacent sub-periods. The fluxes and state variables in Experiment 7 exhibit results similar to those in Experiment 5. However, when sub-period simulations are concatenated, slight inconsistencies occasionally emerge at the sub-period boundaries, with flood peaks being slightly overestimated or baseflows being underestimated. Overall, Experiments 1, 2, and 3 exhibit negligible differences in state variables and flux series, although Experiment 3 produces a decline in low-flow accuracy. Experiment 4 shows marginal improvements compared with time-invariant parameterization; however, it indicates that a single dynamic parameter is insufficient to capture overall dynamic catchment characteristics. Experiment 6 applies abrupt parameter switching across sub-periods, which disrupts water continuity. In contrast, Experiments 5 and 7 display significant improvements in simulation performance, particularly by mitigating the underestimation of high flows and the overestimation of low flows, as evidenced by the behaviour of internal model variables.

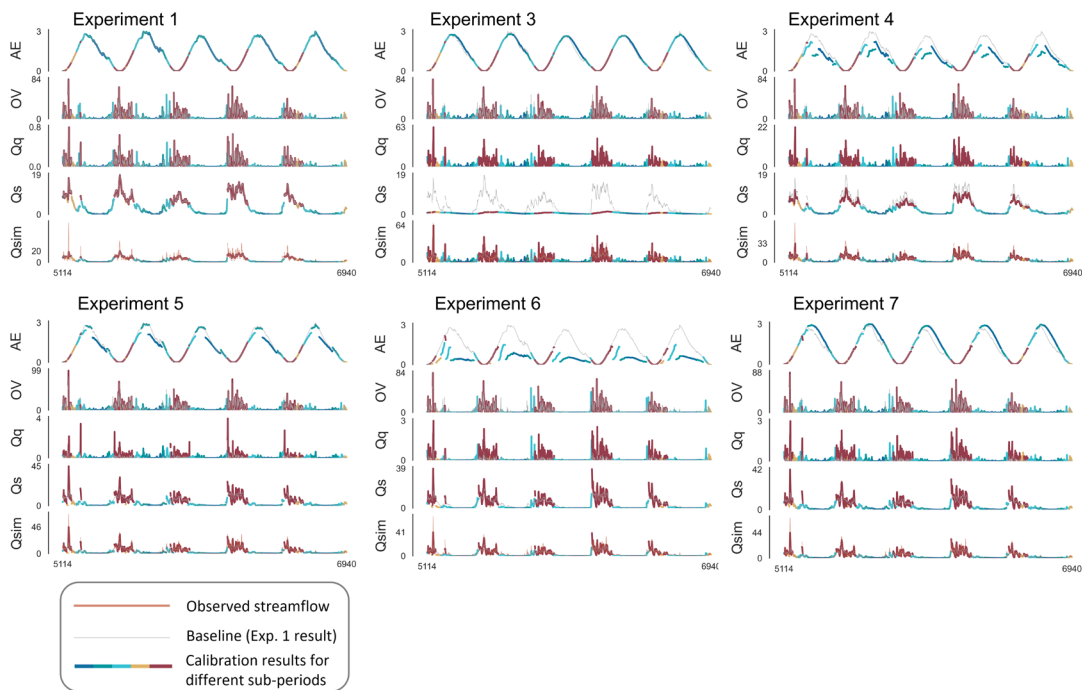


Figure 7. Fluxes simulation results of experiments during the representative evaluation period for case A. The figure shows the flux simulation results from Experiments 1 to 7, with different colours representing different sub-periods.

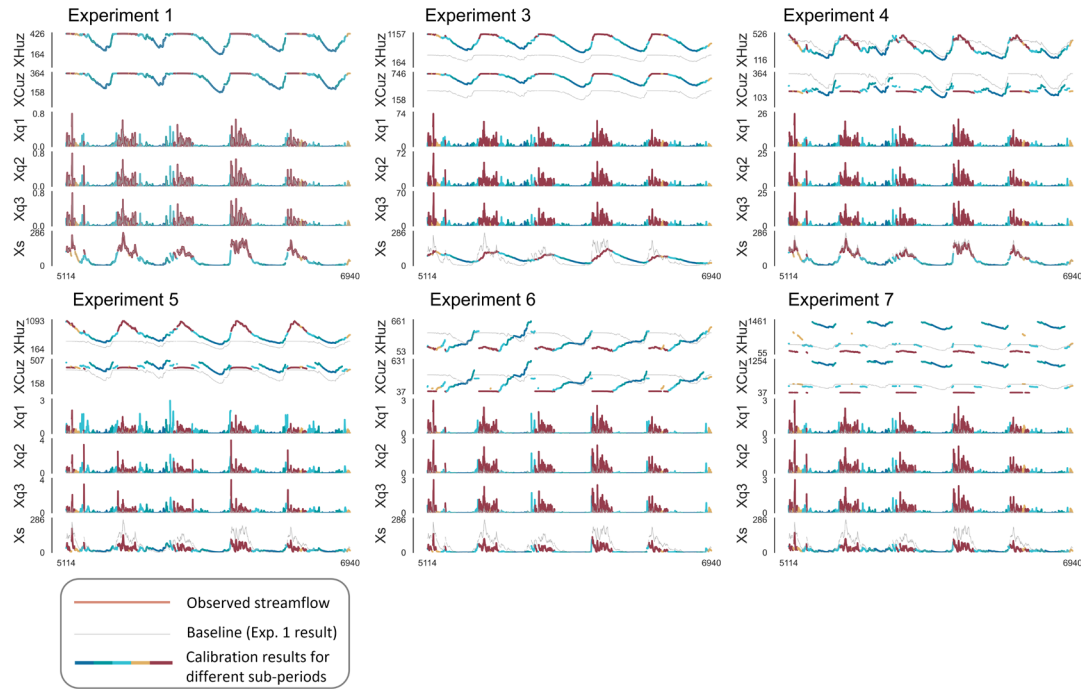


Figure 8. State variables simulation results of experiments during the representative evaluation period for case A. The figure shows the state variable simulation results from Experiments 1 to 7, with different colours representing different sub-periods.

The comparative analysis of Experiments 1, 5, and 7 further illustrates the performance improvements introduced by Experiments 5 and 7. Fig. 9 illustrates the flux mapping of various sub-periods in the study case A, comparing Experiments 1, 5, and 7. Flux-mapping figures for the other study cases are detailed in the *Supporting Information* (Fig. S13-S16). Each scatter point in the figures represents a parameter set generated during the SCE-UA algorithm optimization process. The colour and relative position of each scatter point on the axes illustrate the variation in runoff components for sub-periods under specific parameter sets, as well as the corresponding objective function value. To facilitate comparison, the results of Experiment 1 are also presented by the same sub-periods as Experiments 5 and 7. Notably, the differences in optimization performance between Experiments 1 and 7 reveal key insights into model behaviour. Across all study cases, both Experiments 1 and 7 show the poorest results in sub-periods 1 and 2, with the largest (worst) objective function values. In the remaining three sub-periods, the objective function values are significantly better. Compared to Experiment 1, Experiment 7 consistently identified more optimal parameter sets with smaller objective function values within the same period. For example, in Fig. 9b (Experiment 7), most of the dark blue scatter points for sub-period 5 cluster around a vertical axis value of approximately 0.25, whereas in Experiment 1, scatter points for the same sub-period are more widely distributed near 0.5. Shifting the focus to flux components, the spatial distribution of scatter points in the flux maps reveals varied runoff components and internal model behaviour for each sub-period. In Experiment 7, clusters of scatter points of the same colour appear more compact, while in the traditional scheme, they are more dispersed along both vertical and horizontal axes. This pattern indicates that, despite similar objective function values, Experiment 7 possesses a narrower range of optimal equifinality parameters during the parameter evolution process, reducing the model's internal fluxes equifinality and uncertainty. Furthermore, Fig. 9b shows that in Experiment 7, the colour bars along the vertical axis are shorter and more evenly distributed, demonstrating that from sub-periods 1 to 5, the SCE-UA algorithm more rapidly converges to near-optimal solutions, showing a narrower range of variability in the optimization process.

Further comparison with Experiment 5 (Fig. 9c) shows that parameter sets within each sub-period were tightly clustered in the vertical direction, indicating consistently high performance within individual sub-periods. However, these clusters were widely

dispersed along the horizontal axis. For instance, the cluster for Sub-period 2 (dark red) is concentrated at higher Q_s values (approximately 0.9), whereas the cluster for Sub-period 4 (orange) is concentrated at much lower values (approximately 0.5). Such horizontal separation suggests that different runoff generation mechanisms (fluxes) are adopted across sub-periods to achieve high performance, which may compromise the physical consistency of the overall simulated discharge (Q_{sim}). This inconsistency is particularly evident in case E, where runoff generation mechanisms across sub-periods appeared nearly independent, while the separation is less significant in case B. In contrast, scatter clusters in Experiment 7 (Fig. 9b) are more tightly aligned along the horizontal axis, indicating the adoption of more consistent and physically reasonable runoff strategies across sub-periods. Nevertheless, Experiment 7 poses a potential risk of discontinuities in internal state variables at sub-period boundaries, a phenomenon that was particularly evident in case D (Fig. S15). In summary, the improvements observed in Experiments 5 and 7 underscore both the importance of refining dynamic parameters and the model's ability to simulate complex hydrological processes across sub-periods. However, Experiment 5 may compromise physical consistency in runoff generation processes, while Experiment 7 faces the challenge of ensuring smooth transitions of state variables across boundaries.

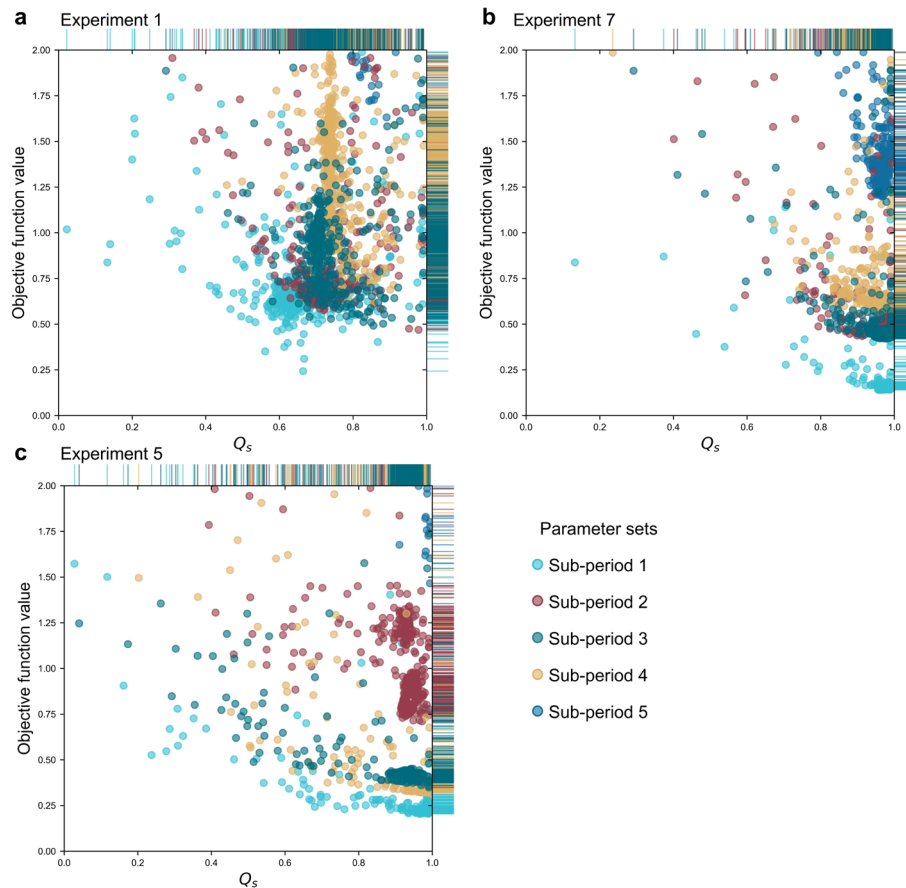


Figure 9. a, Flux mapping for case A in the conventional scheme, b, Experiment 7, and c, Experiment 5, where the horizontal axis represents the proportion of Q_s in the runoff.

4.4 Parameters

The dynamic parameter sets, optimized by various calibration experiments across five case studies, are depicted in Fig. 10. Experiments 1, 2, and 3 utilized a time-invariant parameter set, adjusted through the objective function to reflect the catchment's average characteristics. Experiment 4 allowed the parameter H_{uz} , which exhibits the highest sensitivity, to vary across different

435 sub-periods while maintaining other parameters constant. However, the dynamics of H_{uz} in response to catchment characteristic changes across sub-periods did not significantly improve the model's performance within the five case studies. In Experiment 5, all parameters vary across sub-periods, as illustrated in Fig. 10. The greater colour variation of parameters compared with Experiment 4 indicates a stronger response to catchment dynamics; however, no consistent variation pattern emerged in response to catchment characteristics. In Experiments 6 and 7, certain parameters, such as K_s , exhibited minimal correlation with sub-period characteristics within catchments. As indicated in Fig. 10, the colour variation of bubbles in the K_s column is limited. In some cases, however, deeper bubble colours appear during sub-periods with concentrated precipitation or higher antecedent soil moisture, indicating the K_s value is highest during sub-periods with abundant and concentrated precipitation, higher temperatures, and higher antecedent runoff (soil moisture), and lowest during relatively cold and dry sub-periods. However, this correlation is not significant. Furthermore, K_q does not exhibit a clear pattern of variation due to the poor response of α , which indirectly changed the model structure and bypassed the quick flow module. The phenomenon reflects the uncertainty inherent in model parameters and structure. In sum, compared to time-invariant schemes, Experiments 5 and 7 exhibit superior performance in identifying key parameters and their responses to catchment dynamics. The dynamic characteristic of parameters emphasizes the importance of calibration across sub-periods. Although the dynamic parameter set enhanced the model's response capability to catchment dynamics, the overall response of the entire dynamic parameter set to catchment dynamics remains relatively poor. The reasons for the improved simulation performance of the dynamic parameter set will be explored in the discussion section.

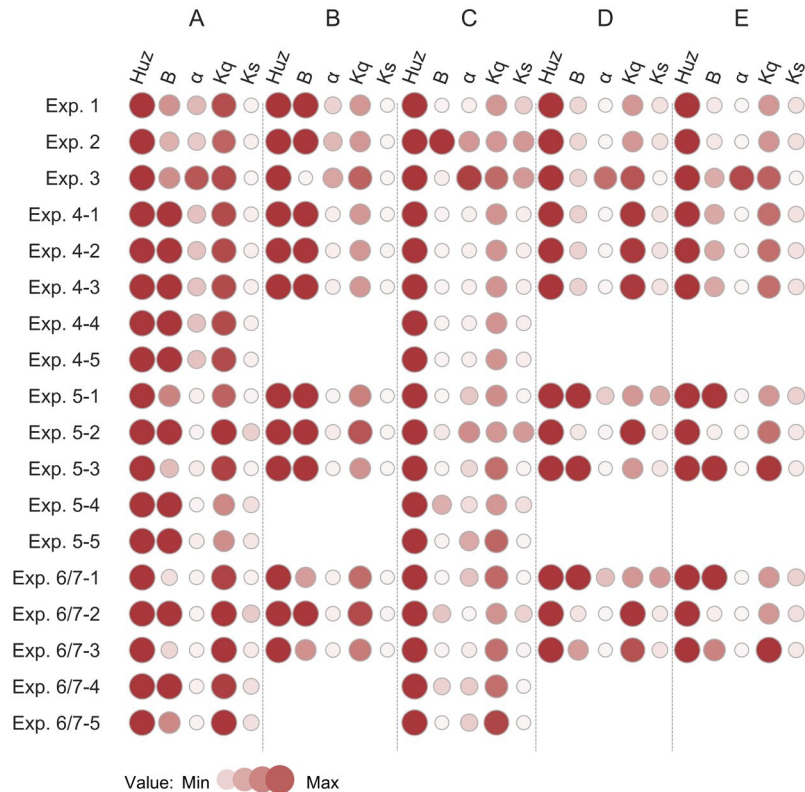


Figure 10. Assessment of dynamic parameter sets across various calibration experiments. The parameter boundaries shown in the figure are H_{uz} (0-1500), B (0-2), α (0-1), K_q (0.5-1), and K_s (0-0.5).

5 Discussion

455 5.1 Why dynamic parameter sets improve simulation performance

Despite the significant improvement in the simulation performance of hydrological models based on catchment dynamics, the response of discretized dynamic parameters (even highly sensitive ones) to these catchment dynamics is not satisfactory. However, a dynamic parameter set can collectively carry the extracted information of dynamic catchment characteristics, compensating for model structural deficiencies and improving model performance. Therefore, this study further explores the potential reasons from
460 three aspects: the correlations between parameters, equifinality in the hydrological model, and the evolution process of parameters.

5.1.1 Complex correlation between parameters

Fig. 11a and Fig. 11c demonstrate that there are both significantly linear and nonlinear correlations among the parameters of the hydrological model in the study case A (results of other cases are shown in supporting information). MIC values above 0.35 among most parameters suggest that the dynamics of individual parameters may be affected by others (Gillespie et al. 2021). This explains
465 the unimproved model performance when altering individual parameters during different sub-periods in Experiment 4. The analysis results of parameter sensitivity based on the scatter plot method also confirmed the influence of the correlation between parameters. In the recommended scheme (Experiment 7), parameters like K_s (the slow-flow routing tank's rate) exhibit a weak responsive relationship to the dynamic catchment, validating the significance of clustering sub-periods based on catchment dynamics. Due to the complex linear or nonlinear correlations between parameters, the variation of individual parameters can be compensated for by
470 changes or adjustments in other parameters, leading to no significant changes in the simulation performance of the model (Xiong et al., 2019; Gou et al., 2020; Zhou et al., 2022). Bárdossy (2007) suggested that parameters within a hydrological model parameter group should not be considered individually but rather treated as a whole.

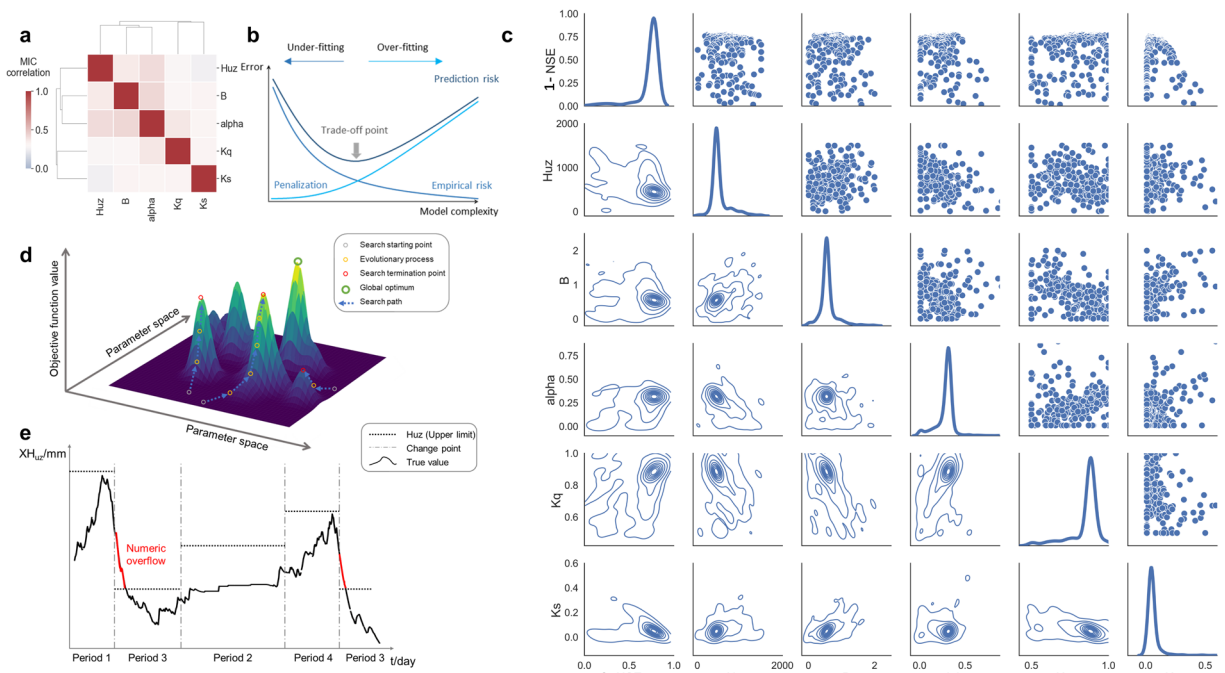
5.1.2 Equifinality in the hydrological model

The parameter sets derived by the SCE-UA algorithm for flux mapping encounter inherent limitations (Beven, 1993; Padiyedath
475 Gopalan et al., 2018). This arises due to the algorithm's inherent directionality in the optimization process, which potentially overlooks certain parameter sets capable of producing equifinality results. Analysis of parameter sensitivity through flux mapping and scatterplot methodology reveals a distinctive feature towards the end of the search path: A tail-like pattern in the scatterplot in Fig. 7a and Fig. 7b, indicating a series of parameter sets with equifinality identified by the optimization algorithm. These scatter points represent parameter sets producing similar results, though originating from distinctly different physical processes. Hence, it
480 may fail to infer that model runs exhibiting higher performance values consistently correspond to more realistic scenarios. The evaluation of model performance, particularly when quantified in a scalar manner, emerges as a weak, unreliable, and unrealistic approach for model assessment. The representation of model processes cannot be sufficiently measured by a solitary performance metric or a limited range of values (Khatami et al., 2019; Knoben et al., 2020; Santos et al., 2018). A rigid interpretation of objective functions can lead to misinterpretations; for instance, in Fig. 11b, model runs with marginally lower NSE values might offer more
485 realistic underlying processes compared to those with better NSE values (Gomez, 2019). It is vital to acknowledge that high model performance does not inherently equal realism and may be influenced by numerical artifacts arising from various sources of uncertainty. Moreover, our constrained understanding of catchment processes, involving runoff generation mechanisms and complex runoff events, makes it challenging to determine the likelihood of specific parameter sets occurring in reality (Troin et al., 2021).

While the causes of non-physical dynamic parameter values are complex, they might be partially attributed to the failure of global optimization algorithms to converge and find approximated global optimal solutions during the evolutionary process. Hydrological model parameter response surfaces exhibit a range of complex characteristics, including high non-linearity, multi-modality, non-convexity, irregularity, discontinuity, noise, roughness, and non-differentiability (Bian et al., 2024; Maier et al., 2014; Herrera et al., 2021). To better describe the evolutionary process of the parameters, a fitness landscape is used, where the vertical axis represents the objective function values and the horizontal axis represents the parameter space (Fig. 11 d). The evolutionary process is the process of searching for a global optimum. During this process, deceptive gradients of the objective function values can mislead the optimizer away from the global optimum; the increase in the number of local optima also makes the search path for the global optimum more complex and challenging (Bian et al., 2024). Terminating at a local optimum can prevent the optimized parameters from accurately responding to environmental changes.

5.2 Problems caused by parameter abrupt shifts

Abrupt parameter shifts disrupt the assumption of long-term water balance in traditional hydrological models, potentially leading to invalid values for state variables in adjacent sub-periods (Kim and Han, 2016; Myers et al., 2021; Fowler et al., 2022). For instance, during the transition of soil maximum storage height (H_{uz}), the H_{uz} value for the next sub-period might be lower than the former actual state variable value (XH_{uz}). Similarly, numerical overflow errors might lead to model crashes and the generation of invalid results (Fig. 11 e). These errors could also propagate through various modules of the model, such as the high-speed runoff module and slow-speed runoff module, disrupting the proper functioning of other parts of the model and making the optimization algorithm incapable of producing valid results.



510 **Figure 11.** a, Linear or nonlinear correlations between parameters based on MICs in case A, with red indicating the strongest correlation among parameters. b, Conceptual diagram illustrating the trade-off between empirical fitting to data and the penalization of model complexity, and its impact on prediction error (Schoups et al., 2008). c, Parameter sensitivity analysis for case A through scatter plots. d, Three-dimensional fitness

landscape showing the objective function values on the vertical axis, parameter space on the horizontal axis, and various evolutionary paths that elements can follow within the parameter space, indicated by arrows. e, Conceptual diagram of errors resulting from abrupt parameter shifts.

515 **5.3 Parameter response to catchment dynamics**

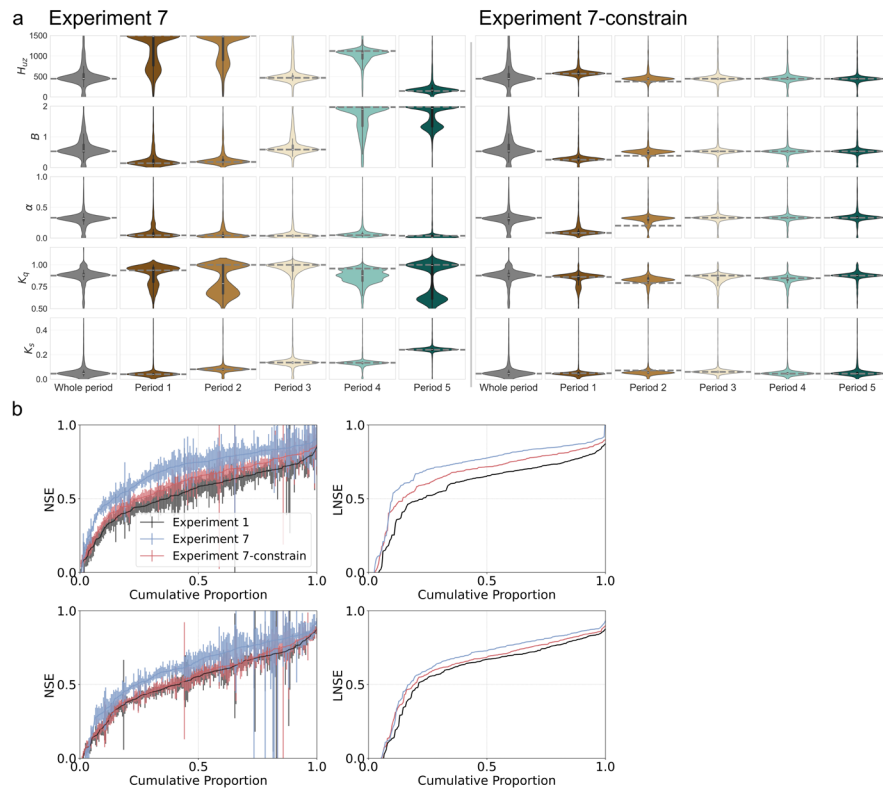
In this study, the sub-period clustering method (Section 3.3) is employed to extract the dynamic catchment characteristics of hydrological processes, enabling model parameters to adjust across hydrological periods. This approach improved simulation accuracy and robustness in dynamic catchments, demonstrating the necessity and effectiveness of incorporating dynamic parameters into conceptual hydrological models (Refsgaard et al., 2021). However, a critical question arises: To what extent do dynamic parameter variations represent the true dynamic variability of catchment properties, and to what extent do they compensate for structural deficiencies of the model itself (Thornton et al., 2022)? To address this problem, a diagnostic experiment is designed. Building on the sub-period calibration framework (Experiment 7), a soft constraint based on globally optimal parameters is introduced, integrating prior information on overall catchment behaviour into sub-period parameter estimation. This design balances the flexibility of dynamic parameter adjustment with the need to preserve physical consistency. The diagnostic objective function is defined as:

$$\text{OF}=1-(0.5*\text{NSE}+0.5*\text{LNSE}) + \text{Penalty} \quad (2)$$

where the penalty term quantifies the deviation of the sub-period parameter set $\hat{\theta}_i$ from the globally optimal parameter set θ_i . The penalty is formulated as the mean of the absolute relative errors: $\text{Penalty} = \frac{1}{N} \times \sum \left| \frac{\hat{\theta}_i - \theta_i}{\theta_i} \right|$, where i denotes the parameter index, and N is the total number of parameters (five in the HYMOD model). This setting allows assessment of how model responses change when parameter variability is constrained within a more stable and physically consistent range.

As shown in Fig. 12a, imposing the constraint leads to posterior distributions that are more concentrated within each sub-period, with reduced dispersion, reflecting greater stability. Parameter transferability between calibration and evaluation periods also improved, as illustrated in Fig. 12b, with smaller declines in model performance across periods. However, these gains in parameter stability are accompanied by significant reductions in NSE and LNSE, rendering performance inferior to unconstrained sub-period calibration. This trade-off highlights the compensatory role of dynamic parameters in addressing structural limitations of fixed model formulations. When the capacity of parameters to compensate is constrained, the observed performance decline reflects underlying structural inadequacies in representing key hydrological processes.

The demand for dynamic parameters is often symptomatic of structural insufficiency. A structurally adequate model should maintain stable parameters that represent physical catchment properties. When the model formulation fails to capture essential processes, the “optimal” parameters must vary dynamically to compensate for these omissions (Beven, 2019). Evidence from the GLUE framework has shown that posterior parameter distributions can diverge almost completely between wet and dry seasons, implying that sub-period calibration with distinct parameter sets effectively corrects structural errors and improves accuracy (Blasone et al., 2008). Moreover, concepts from Data-Based Mechanistic (DBM) modelling and state-dependent parameter (SDP) approaches suggest that time- or state-dependent gains—such as nonlinear filters linked to soil moisture or runoff—can be identified from data. These gains compensate for missing nonlinearities in effective rainfall, often exhibiting dynamic catchment patterns over longer periods. On this basis, the proposed sub-period calibration framework is positioned as a practical means of using parameters as proxy variables to alleviate structural deficiencies, thereby enhancing streamflow simulation accuracy in dynamic catchments (Bouaziz et al., 2022; Terrier et al., 2021).



550 **Figure 12. a**, Distributions of the optimal parameter spaces across sub-periods under different climatic and land-surface conditions for case A. Each violin depicts one parameter space, with parameter values on the y-axis; the violin width reflects the probability density of the parameter values. Parameter bounds are: H_{uz} (0-1500), B (0-2), α (0-1), K_q (0.5-1), and K_s (0-0.5). Results for all study cases are provided in S5 of the Supporting Information. **b**, Cumulative distribution functions (CDFs) of NSE and LNSE comparing the experiment built on Experiment 7 with added parameter constraints (blue), Experiment 7 (red), and Experiment 1 (black); higher values indicate better performance. Upper panels show calibration; lower panels show verification. Shaded bands denote 90% bootstrap confidence limits to indicate sampling uncertainty.

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6 Conclusions

Due to limitations in observational data and an incomplete understanding of catchment hydrological processes, traditional conceptual hydrological models often fail to represent catchment dynamic characteristics, leading to generalized simulation of different flow regimes. To address model deficiencies and improve simulation in dynamic catchment characteristics, it is essential to re-examine the time-varying information in historical hydrological and meteorological data and consider the variation in calibration. The study investigates calibration challenges in dynamic catchments and proposes a structured framework to address two major issues: The influence of objective function design on flow-phase-specific performance and the limitations of sub-period calibration with dynamic parameters. Seven experiments were conducted to systematically evaluate these aspects. Experiments 1–3 focused on the effects of time-invariant parameters and different objective function configurations, while Experiments 4–7 explored challenges in dynamic parameter calibration, including parameter correlation, high dimensionality, and state transitions. Model performance was comprehensively assessed using multiple metrics and internal diagnostics across 219 MOPEX catchments. The following specific conclusions could be drawn from this study:

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- Adjusting the configuration of the objective function can enhance the simulation of emphasized flow phases, but at the cost of sacrificing simulation performance for other flow phases, making it difficult to improve overall model performance.

- 570 • Due to issues of model structural deficiencies, correlation among parameters, dimensional disaster in optimization, and the transition of dynamic parameters between adjacent sub-periods, improving model performance through individual parameters alone is not feasible. Model parameters should be considered as a group of parameters.
- 575 • Among all calibration experiments, Experiments 5 and 7 effectively addressed the challenges associated with dynamic parameter operations and flow-phase-specific performance, balancing dynamic adaptability and physical consistency. These calibration strategies are thus recommended for application in dynamic catchments, where capturing temporal variability and maintaining model reliability are critical.

580 The calibration and evaluation framework proposed in this study not only addresses defects caused by the simplification of model structure for hydrological models but also enhances model simulation accuracy across different flow phases and effectively reduces model uncertainty. The evaluation framework comprehensively assesses the performance of hydrological models through multi-criteria evaluation and reveals sources of uncertainty in model internal operation from the perspectives of state variables and fluxes. Despite the positive results of this study, developing more realistic models will aid in our understanding of hydrological processes and improve hydrological forecasting.

Supplement link

Supporting Information is provided.

585 Author contributions

Tian Lan devised the modelling concept. Tian Lan and Xiao Wang wrote the code and prepared the original draft manuscript. Hongbo Zhang, Xinghui Gong, Xue Xie, Yongqin David Chen, and Chong-Yu Xu provided supervision and reviewed/edited the manuscript. Jiajia Zhang and Wenqing Cheng contributed to supplementary calculations and textual revisions during the manuscript revision.

590 Code availability

The MOPEX dataset is available at Duan et al. (2006). The Sensitivity Analysis For Everyone (SAFE) toolbox is available at <https://safetoolbox.github.io/> (last access: 23 November 2024) (Pianosi et al., 2015). Model set-up configurations have been reported in <https://doi.org/10.5281/zenodo.16676391> (last access: 26 September 2025).

Competing interests

595 The authors declare that they have no conflict of interest.

Acknowledgments

Data Availability Statement: Data and code reported in this paper can be downloaded from Lan (2025) at <https://doi.org/10.5281/zenodo.16676391>. The MOPEX dataset is available from Duan et al. (2006). The Sensitivity Analysis For Everyone (SAFE) toolbox is available at <https://safetoolbox.github.io/> (Pianosi et al., 2015).

600 References

- Acuña Espinoza, E., Loritz, R., Álvarez Chaves, M., Bäuerle, N., and Ehret, U.: To bucket or not to bucket? Analyzing the performance and interpretability of hybrid hydrological models with dynamic parameterization, *Hydrology and Earth System Sciences*, 28, 2705-2719, <https://doi.org/10.5194/hess-28-2705-2024>, 2024.
- Anderson, S. and Radić, V.: Evaluation and interpretation of convolutional long short-term memory networks for regional hydrological modelling, *Hydrology and Earth System Sciences*, 26, 795-825, <https://doi.org/10.5194/hess-26-795-2022>, 2022.
- 605 Araya, D., Mendoza, P. A., Muñoz-Castro, E., and McPhee, J.: Towards robust seasonal streamflow forecasts in mountainous catchments: impact of calibration metric selection in hydrological modeling, *Hydrology and Earth System Sciences*, 27, 4385-4408, <https://doi.org/10.5194/hess-27-4385-2023>, 2023.
- Bárdossy, A.: Calibration of hydrological model parameters for ungauged catchments, *Hydrology and Earth System Sciences*, 11, 703-710, <https://doi.org/10.5194/hess-11-703-2007>, 2007.
- 610 Bárdossy, A. and Singh, S. K.: Robust estimation of hydrological model parameters, *Hydrology and Earth System Sciences*, 12, 1273-1283, <https://doi.org/10.5194/hess-12-1273-2008>, 2008.
- Beven, K.: How to make advances in hydrological modelling, *Hydrology Research*, 50(6), 1481-1494, <https://doi.org/10.2166/nh.2019.134>, 2019.
- 615 Beven, K.: Prophecy, reality and uncertainty in distributed hydrological modelling. *Advances in Water Resources*, 16(1), 41-51, [https://doi.org/10.1016/0309-1708\(93\)90028-E](https://doi.org/10.1016/0309-1708(93)90028-E), 1993.
- Bian, K., & Priyadarshi, R.: Machine learning optimization techniques: a survey, classification, challenges, and future research issues. *Archives of Computational Methods in Engineering*, 31(7), 4209-4233, <https://doi.org/10.1007/s11831-024-10110-w>, 2024.
- Blasone, R. S., Vrugt, J. A., Madsen, H., Rosbjerg, D., Robinson, B. A., & Zyvoloski, G. A.: Generalized likelihood uncertainty estimation (GLUE) using adaptive Markov Chain Monte Carlo sampling. *Advances in Water Resources*, 31(4), 630-648, <https://doi.org/10.1016/j.advwatres.2007.12.003>, 2008.
- 620 Bouaziz, L. J., Aalbers, E. E., Weerts, A. H., Hegnauer, M., Buiteveld, H., Lammersen, R., ... & Brachowitz, M.: Ecosystem adaptation to climate change: the sensitivity of hydrological predictions to time-dynamic model parameters. *Hydrology and Earth System Sciences*, 26(5), 1295-1318, <https://doi.org/10.5194/hess-26-1295-2022>, 2022.
- Carletti, F., Michel, A., Casale, F., Burri, A., Bocchiola, D., Bavay, M., & Lehning, M.: A comparison of hydrological models with different level of complexity in Alpine regions in the context of climate change. *Hydrology and Earth System Sciences*, 26(13), 3447-3475, <https://doi.org/10.5194/hess-26-3447-2022>, 2022.
- 625 Cheng, L., Yaeger, M., Viglione, A., Coopersmith, E., Ye, S., and Sivapalan, M.: Exploring the physical controls of regional patterns of flow duration curves – Part 1: Insights from statistical analyses, *Hydrology and Earth System Sciences*, 16, 4435-4446, <https://doi.org/10.5194/hess-16-4435-2012>, 2012.
- 630 Clark, M. P., Vogel, R. M., Lamontagne, J. R., Mizukami, N., Knoben, W. J. M., Tang, G., Gharari, S., Freer, J. E., Whitfield, P. H., Shook, K. R., and Papalexiou, S. M.: The Abuse of Popular Performance Metrics in Hydrologic Modeling, *Water Resources Research*, 57, e2020WR029001, <https://doi.org/10.1029/2020WR029001>, 2021.
- Clark, M. P., Fan, Y., Lawrence, D. M., Adam, J. C., Bolster, D., Gochis, D. J., Hooper, R. P., Kumar, M., Leung, L. R., Mackay, D. S., Maxwell, R. M., Shen, C., Swenson, S. C., and Zeng, X.: Improving the representation of hydrologic processes in Earth System Models, *Water Resources Research*, 51, 5929-5956, <https://doi.org/10.1002/2015WR017096>, 2015.
- 635 Daggupati, P., Yen, H., White, M. J., Srinivasan, R., Arnold, J. G., Keitzer, C. S., and Sowa, S. P.: Impact of model development, calibration and validation decisions on hydrological simulations in West Lake Erie Basin, *Hydrological Processes*, 29, 5307-5320, <https://doi.org/10.1002/hyp.10536>, 2015.
- Deng, C., Liu, P., Guo, S., Li, Z., and Wang, D.: Identification of hydrological model parameter variation using ensemble Kalman filter, *Hydrology and Earth System Sciences*, 20, 4949-4961, <https://doi.org/10.5194/hess-20-4949-2016>, 2016.
- 640 Duan, Q., Schaake, J., Andréassian, V., Franks, S., Goteti, G., Gupta, H. V., Gusev, Y. M., Habets, F., Hall, A., Hay, L., Hogue, T., Huang, M., Leavesley, G., Liang, X., Nasonova, O. N., Noilhan, J., Oudin, L., Sorooshian, S., Wagener, T., and Wood, E. F.: Model Parameter Estimation Experiment (MOPEX): An overview of science strategy and major results from the second and third workshops, *Journal of Hydrology*, 320, 3-17, <https://doi.org/10.1016/j.jhydrol.2005.07.031>, 2006.
- 645 Duan, Q. Y., Gupta, V. K., and Sorooshian, S.: Shuffled Complex Evolution Approach for Effective and Efficient Global Minimization, *Journal of Optimization Theory and Applications*, 76, 501-521, <https://doi.org/10.1007/BF00939380>, 1993.
- Fauer, F. S., Ulrich, J., Jurado, O. E., and Rust, H. W.: Flexible and consistent quantile estimation for intensity–duration–frequency curves, *Hydrology and Earth System Sciences*, 25, 6479-6494, <https://doi.org/10.5194/hess-25-6479-2021>, 2021.
- 650 Fowler, K., Coxon, G., Freer, J., Peel, M., Wagener, T., Western, A., Woods, R., and Zhang, L.: Simulating runoff under changing climatic conditions: A framework for model improvement, *Water Resources Research*, 54, 9812-9832, <https://doi.org/10.1029/2018WR023989>, 2018.
- Fowler, K., Peel, M., Saft, M., Nathan, R., Horne, A., Wilby, R., ... & Peterson, T.: Hydrological shifts threaten water resources. *Water Resources Research*, 58(8), e2021WR031210, <https://doi.org/10.1029/2021WR031210>, 2022.
- 655 Fowler, K., Peel, M., Saft, M., Peterson, T. J., Western, A., Band, L., Petheram, C., Dharmadi, S., Tan, K. S., Zhang, L., Lane, P., Kiem, A., Marshall, L., Griebel, A., Medlyn, B. E., Ryu, D., Bonotto, G., Wasko, C., Ukkola, A., Stephens, C., Frost, A., Weligamage, H. G., Saco,

- P., Zheng, H. X., Chiew, F., Daly, E., Walker, G., Vervoort, R. W., Hughes, J., Trotter, L., Neal, B., Cartwright, I., and Nathan, R.: Explaining changes in rainfall-runoff relationships during and after Australia's Millennium Drought: a community perspective, *Hydrology and Earth System Sciences*, 26, 6073-6120, <https://doi.org/10.5194/hess-26-6073-2022>, 2022.
- 660 Gillespie, L. M., Hättenschwiler, S., Milcu, A., Wambsganss, J., Shiha, A., & Fromin, N.: Tree species mixing affects soil microbial functioning indirectly via root and litter traits and soil parameters in European forests. *Functional Ecology*, 35(10), 2190-2204, <https://doi.org/10.1111/1365-2435.13877>, 2021.
- Gomez, J.: Stochastic global optimization algorithms: A systematic formal approach, *Inform Sciences*, 472, 53-76, <https://doi.org/10.1016/j.ins.2018.09.021>, 2019.
- 665 Gou, J., Miao, C., Duan, Q., Tang, Q., Di, Z., Liao, W., ... & Zhou, R.: Sensitivity analysis - based automatic parameter calibration of the VIC model for streamflow simulations over China. *Water Resources Research*, 56(1), e2019WR025968, <https://doi.org/10.1029/2019WR025968>, 2020.
- Guo, D., Johnson, F., and Marshall, L.: Assessing the potential robustness of conceptual rainfall-runoff models under a changing climate, *Water Resources Research*, 54, 5030-5049, <https://doi.org/10.1029/2018WR022636>, 2018.
- 670 Gupta, H. V., Kling, H., Yilmaz, K. K., and Martinez, G. F.: Decomposition of the mean squared error and NSE performance criteria: Implications for improving hydrological modelling, *Journal of Hydrology*, 377, 80-91, <https://doi.org/10.1016/j.jhydrol.2009.08.003>, 2009.
- Herrera, Paulo A., Miguel Angel Marazuela, and Thilo Hofmann.: Parameter estimation and uncertainty analysis in hydrological modeling. *Wiley Interdisciplinary Reviews: Water*, 9.1: e1569, <https://doi.org/10.1002/wat2.1569>, 2021.
- Höge, M., Wöhling, T., and Nowak, W.: A primer for model selection: The decisive role of model complexity, *Water Resources Research*, 54, 1688-1715, <https://doi.org/10.1002/2017WR021902>, 2018.
- 675 Hsueh, H. F., Guthke, A., Wöhling, T., & Nowak, W.: Optimized predictive coverage by averaging time - windowed Bayesian distributions. *Water Resources Research*, 60(5), e2022WR033280, <https://doi.org/10.1029/2022WR033280>, 2024.
- Ji, H. K., Mirzaei, M., Lai, S. H., Dehghani, A., and Dehghani, A.: The robustness of conceptual rainfall-runoff modelling under climate variability – A review, *Journal of Hydrology*, 621, 129666, <https://doi.org/10.1016/j.jhydrol.2023.129666>, 2023.
- 680 Karpatne, A., Atluri, G., Faghmous, J. H., Steinbach, M., Banerjee, A., Ganguly, A., Shekhar, S., Samatova, N., and Kumar, V.: Theory-guided data science: A new paradigm for scientific discovery from data, *IEEE Transactions on Knowledge and Data Engineering*, 29, 2318-2331, <https://doi.org/10.1109/TKDE.2017.2720168>, 2017.
- Khatami, S., Peel, M. C., Peterson, T. J., and Western, A. W.: Equifinality and flux mapping: A new approach to model evaluation and process Representation Under Uncertainty, *Water Resources Research*, 55, 8922-8941, <https://doi.org/10.1029/2018WR023750>, 2019.
- 685 Kim, K. B. and Han, D.: Exploration of sub-annual calibration schemes of hydrological models, *Hydrology Research*, 48, 1014-1031, <https://doi.org/10.2166/nh.2016.296>, 2017.
- Knoben, W. J., Freer, J. E., Peel, M. C., Fowler, K. J. A., & Woods, R. A.: A brief analysis of conceptual model structure uncertainty using 36 models and 559 catchments. *Water Resources Research*, 56(9), e2019WR025975, <https://doi.org/10.1029/2019WR025975>, 2020.
- Krapu, C. and Borsuk, M.: A differentiable hydrology approach for modeling with time-varying parameters, *Water Resources Research*, 58, e2021WR031377, <https://doi.org/10.1029/2021WR031377>, 2022.
- 690 Kratzert, F., Klotz, D., Brenner, C., Schulz, K., and Herrnegger, M.: Rainfall-runoff modelling using Long Short-Term Memory (LSTM) networks, *Hydrology and Earth System Sciences*, 22, 6005-6022, <https://doi.org/10.5194/hess-22-6005-2018>, 2018.
- Kratzert, F., Klotz, D., Herrnegger, M., Sampson, A. K., Hochreiter, S., and Nearing, G. S.: Toward improved predictions in ungauged basins: Exploiting the power of machine learning, *Water Resources Research*, 55, 11344-11354, <https://doi.org/10.1029/2019WR026065>, 2019a.
- 695 Kratzert, F., Klotz, D., Shalev, G., Klambauer, G., Hochreiter, S., and Nearing, G.: Towards learning universal, regional, and local hydrological behaviors via machine learning applied to large-sample datasets, *Hydrology and Earth System Sciences*, 23, 5089-5110, <https://doi.org/10.5194/hess-23-5089-2019>, 2019b.
- Lakshmi, G. and Sudheer, K. P.: Parameterization in hydrological models through clustering of the simulation time period and multi-objective optimization based calibration, *Environ Modell Softw*, 138, <https://doi.org/10.1016/j.envsoft.2021.104981>, 2021.
- 700 Lin, Y., Wang, D., Zhu, J., Sun, W., Shen, C., & Shangguan, W.: Development of objective function-based ensemble model for streamflow forecasts. *Journal of Hydrology*, 632, 130861, <https://doi.org/10.1016/j.jhydrol.2024.130861>, 2024.
- Longyang, Q. and Zeng, R.: A hierarchical temporal scale framework for data - driven reservoir release modeling, *Water Resources Research*, 59, <https://doi.org/10.1029/2022WR033922>, 2023.
- 705 Maier, H. R., Kapelan, Z., Kasprzyk, J., Kollat, J., Matott, L. S., Cunha, M. C., Dandy, G. C., Gibbs, M. S., Keedwell, E., Marchi, A., Ostfeld, A., Savic, D., Solomatine, D. P., Vrugt, J. A., Zecchin, A. C., Minsker, B. S., Barbour, E. J., Kuczera, G., Pasha, F., Castelletti, A., Giuliani, M., and Reed, P. M.: Evolutionary algorithms and other metaheuristics in water resources: Current status, research challenges and future directions, *Environmental Modelling & Software*, 62, 271-299, <https://doi.org/10.1016/j.envsoft.2014.09.013>, 2014.
- Martel, J.-L., Brissette, F., Arsenaault, R., Turcotte, R., Castañeda-Gonzalez, M., Armstrong, W., Mailhot, E., Pelletier-Dumont, J., Rondeau-Genesse, G., and Caron, L.-P.: Assessing the adequacy of traditional hydrological models for climate change impact studies: a case for long short-term memory (LSTM) neural networks, *Hydrology and Earth System Sciences*, 29, 2811-2836, <https://doi.org/10.5194/hess-29-2811-2025>, 2025.
- 710 McCabe, G. J., Hay, L. E., Bock, A., Markstrom, S. L., and Atkinson, R. D.: Inter-annual and spatial variability of Hamon potential evapotranspiration model coefficients, *Journal of Hydrology*, 521, 389-394, <https://doi.org/10.1016/j.jhydrol.2014.12.006>, 2015.
- Myers, D. T., Ficklin, D. L., Robeson, S. M., Neupane, R. P., Botero - Acosta, A., & Avellaneda, P. M.: Choosing an arbitrary calibration period for hydrologic models: How much does it influence water balance simulations?. *Hydrological Processes*, 35(2), e14045, <https://doi.org/10.1002/hyp.14045>, 2021.
- 715 Moore, R. J.: The probability-distributed principle and runoff production at point and basin scales, *Hydrological Sciences Journal*, 30, 273-297, <https://doi.org/10.1080/02626668509490989>, 2009.
- Nash, J. E. and Sutcliffe, J. V.: River flow forecasting through conceptual models part I — A discussion of principles, *Journal of Hydrology*, 10, 282-290, [https://doi.org/10.1016/0022-1694\(70\)90255-6](https://doi.org/10.1016/0022-1694(70)90255-6), 1970.

- 720 Nearing, G. S., Kratzert, F., Sampson, A. K., Pelissier, C. S., Klotz, D., Frame, J. M., Prieto, C., and Gupta, H. V.: What Role Does Hydrological Science Play in the Age of Machine Learning?, *Water Resources Research*, 57, e2020WR028091, <https://doi.org/10.1029/2020WR028091>, 2021.
- Orth, R., Staudinger, M., Seneviratne, S. I., Seibert, J., and Zappa, M.: Does model performance improve with complexity? A case study with three hydrological models, *Journal of Hydrology*, 523, 147-159, <https://doi.org/10.1016/j.jhydrol.2015.01.044>, 2015.
- 725 Padiyedath Gopalan, S., Kawamura, A., Takasaki, T., Amaguchi, H., and Azhikodan, G.: An effective storage function model for an urban watershed in terms of hydrograph reproducibility and Akaike information criterion, *Journal of Hydrology*, 563, 657-668, <https://doi.org/10.1016/j.jhydrol.2018.06.035>, 2018.
- Pande, S. and Moayeri, M.: Hydrological interpretation of a statistical measure of basin complexity, *Water Resources Research*, 54, 7403-7416, <https://doi.org/10.1029/2018WR022675>, 2018.
- 730 Pathiraja, S., Marshall, L., Sharma, A., and Moradkhani, H.: Hydrologic modeling in dynamic catchments: A data assimilation approach, *Water Resources Research*, 52, 3350-3372, <https://doi.org/10.1002/2015WR017192>, 2016.
- Pianosi, F., Sarrazin, F., and Wagener, T.: A Matlab toolbox for global sensitivity analysis, *Environmental Modelling & Software*, 70, 80-85, <https://doi.org/10.1016/j.envsoft.2015.04.009>, 2015.
- 735 Razavi, S., Duffy, A., Eamen, L., Jakeman, A. J., Jardine, T. D., Wheeler, H., Hunt, R. J., Maier, H. R., Abdelhamed, M. S., and Ghoreishi, M.: Convergent and transdisciplinary integration: On the future of integrated modeling of human - water systems, *Water Resources Research*, 61, <https://doi.org/10.1029/2024WR038088>, 2025.
- Refsgaard, J. C., Stisen, S., & Koch, J.: Hydrological process knowledge in catchment modelling—Lessons and perspectives from 60 years development. *Hydrological Processes*, 36(1), e14463, <https://doi.org/10.1002/hyp.14463>, 2021.
- 740 Reichert, P., Ammann, L., & Fenicia, F.: Potential and challenges of investigating intrinsic uncertainty of hydrological models with stochastic, time - dependent parameters. *Water Resources Research*, 57(3), e2020WR028400, <https://doi.org/10.1029/2020WR028400>, 2021.
- Santos, L., Thirel, G., and Perrin, C.: Technical note: Pitfalls in using log-transformed flows within the KGE criterion, *Hydrology and Earth System Sciences*, 22, 4583-4591, <https://doi.org/10.5194/hess-22-4583-2018>, 2018.
- Schoups, G., van de Giesen, N. C., and Savenije, H. H. G.: Model complexity control for hydrologic prediction, *Water Resources Research*, 44, <https://doi.org/10.1029/2008WR006836>, 2008.
- 745 Schwemmler, R., Demand, D., & Weiler, M.: Diagnostic efficiency—specific evaluation of model performance. *Hydrology and Earth System Sciences*, 25(4), 2187-2198, <https://doi.org/10.5194/hess-25-2187-2021>, 2021.
- Shamir, E., Imam, B., Gupta, H. V., and Sorooshian, S.: Application of temporal streamflow descriptors in hydrologic model parameter estimation, *Water Resources Research*, 41, <https://doi.org/10.1029/2004WR003409>, 2005.
- 750 Shao, M., Fernando, N., Zhu, J., Zhao, G., Kao, S. C., Zhao, B., Roberts, E., and Gao, H.: Estimating future surface water availability through an integrated climate - hydrology - management modeling framework at a basin scale under CMIP6 scenarios, *Water Resources Research*, 59, <https://doi.org/10.1029/2022WR034099>, 2023.
- Shrestha, S., Bae, D.-H., Hok, P., Ghimire, S., and Pokhrel, Y.: Future hydrology and hydrological extremes under climate change in Asian river basins, *Scientific Reports*, 11, 17089, <https://doi.org/10.1038/s41598-021-96656-2>, 2021.
- 755 Song, Y., Knoben, W. J., Clark, M. P., Feng, D., Lawson, K. E., and Shen, C.: When ancient numerical demons meet physics-informed machine learning: adjoint-based gradients for implicit differentiable modeling, *Hydrology and Earth System Sciences Discussions*, 2023, 1-35, <https://doi.org/10.5194/hess-28-3051-2024>, 2023.
- Terrier, M., Perrin, C., De Lavenne, A., Andréassian, V., Lerat, J., & Vaze, J.: Streamflow naturalization methods: a review. *Hydrological Sciences Journal*, 66(1), 12-36, <https://doi.org/10.1080/02626667.2020.1839080>, 2021.
- 760 Thornton, J. M., Therrien, R., Mariéthoz, G., Linde, N., & Brunner, P.: Simulating fully - integrated hydrological dynamics in complex alpine headwaters: potential and challenges. *Water Resources Research*, 58(4), e2020WR029390, <https://doi.org/10.1029/2020WR029390>, 2022.
- Troin, M., Arsenault, R., Wood, A. W., Brissette, F., & Martel, J. L.: Generating ensemble streamflow forecasts: A review of methods and approaches over the past 40 years, *Water Resources Research*, 2020WR028392, <https://doi.org/10.1029/2020WR028392>, 2020.
- 765 Tucker, C. J., Pinzon, J. E., Brown, M. E., Slayback, D. A., Pak, E. W., Mahoney, R., Vermote, E. F., and El Saleous, N.: An extended AVHRR 8-km NDVI dataset compatible with MODIS and SPOT vegetation NDVI data, *International Journal of Remote Sensing*, 26, 4485-4498, <https://doi.org/10.1080/01431160500168686>, 2010.
- Vrugt, J. A., Gupta, H. V., Bastidas, L. A., Bouten, W., & Sorooshian, S.: Effective and efficient algorithm for multiobjective optimization of hydrologic models. *Water resources research*, 39(8), <https://doi.org/10.1029/2002WR001746>, 2003.
- 770 Wagener, T., Boyle, D. P., Lees, M. J., Wheeler, H. S., Gupta, H. V., & Sorooshian, S.: A framework for development and application of hydrological models. *Hydrology and Earth System Sciences*, 5(1), 13-26, <https://doi.org/10.5194/hess-5-13-2001>, 2001.
- Wagener, T. and Kollat, J.: Numerical and visual evaluation of hydrological and environmental models using the Monte Carlo analysis toolbox, *Environmental Modelling & Software*, 22, 1021-1033, <https://doi.org/10.1016/j.envsoft.2006.06.017>, 2007.
- 775 Wang, S., Ancell, B. C., Huang, G. H., and Baetz, B. W.: Improving robustness of hydrologic ensemble predictions through probabilistic pre- and post-processing in sequential data assimilation, *Water Resources Research*, 54, 2129-2151, <https://doi.org/10.1002/2018WR022546>, 2018.
- Wang, S., Huang, G. H., Baetz, B. W., and Ancell, B. C.: Towards robust quantification and reduction of uncertainty in hydrologic predictions: Integration of particle Markov chain Monte Carlo and factorial polynomial chaos expansion, *Journal of Hydrology*, 548, 484-497, <https://doi.org/10.1016/j.jhydrol.2017.03.027>, 2017.
- 780 Wang, Y., Wang, J., Xie, J., and Lu, H.: Improvements in the degree-day model, incorporating forest influence, and taking China's Tianshan Mountains as an example, *Journal of Hydrology: Regional Studies*, 44, <https://doi.org/10.1016/j.ejrh.2022.101215>, 2022a.
- Wang, Z., Yang, Y., Zhang, C., Guo, H., and Hou, Y.: Historical and future Palmer Drought Severity Index with improved hydrological modeling, *Journal of Hydrology*, 610, 127941, <https://doi.org/10.1016/j.jhydrol.2022.127941>, 2022b.
- Wei, X. T., Huang, S. Z., Huang, Q., Leng, G. Y., Wang, H., He, L., Zhao, J., and Liu, D.: Identification of the interactions and feedbacks among watershed water-energy balance dynamics, hydro-meteorological factors, and underlying surface characteristics, *Stochastic Environmental Research and Risk Assessment*, 35, 69-81, <https://doi.org/10.1007/s00477-020-01896-9>, 2021.

- 785 Wen, H., Brantley, S. L., Davis, K. J., Duncan, J. M., and Li, L.: The limits of homogenization: What hydrological dynamics can a simple model represent at the catchment scale?, *Water Resources Research*, 57, <https://doi.org/10.1029/2020WR029528>, 2021.
- Wi, S. and Steinschneider, S.: Assessing the physical realism of deep learning hydrologic model projections under climate change, *Water Resources Research*, 58, <https://doi.org/10.1029/2022WR032123>, 2022.
- 790 Xie, K., Liu, P., Zhang, J., Wang, G., Zhang, X., and Zhou, L.: Identification of spatially distributed parameters of hydrological models using the dimension-adaptive key grid calibration strategy, *Journal of Hydrology*, 598, 125772, <https://doi.org/10.1016/j.jhydrol.2020.125772>, 2021.
- Xiong, M., Liu, P., Cheng, L., Deng, C., Gui, Z., Zhang, X., and Liu, Y.: Identifying time-varying hydrological model parameters to improve simulation efficiency by the ensemble Kalman filter: A joint assimilation of streamflow and actual evapotranspiration, *Journal of Hydrology*, 568, 758-768, <https://doi.org/10.1016/j.jhydrol.2018.11.038>, 2019.
- 795 Yilmaz, K. K., Gupta, H. V., and Wagener, T.: A process-based diagnostic approach to model evaluation: Application to the NWS distributed hydrologic model, *Water Resources Research*, 44, <https://doi.org/10.1029/2007WR006716>, 2008.
- Yoshida, T., Hanasaki, N., Nishina, K., Boulange, J., Okada, M., and Troch, P.: Inference of parameters for a global hydrological model: Identifiability and predictive uncertainties of climate - based parameters, *Water Resources Research*, 58, <https://doi.org/10.1029/2021WR030660>, 2022.
- 800 Zhang, X. and Liu, P.: A time-varying parameter estimation approach using split-sample calibration based on dynamic programming, *Hydrology and Earth System Sciences*, 25, 711-733, <https://doi.org/10.5194/hess-25-711-2021>, 2021.
- Zhou, L., Liu, P., Gui, Z., Zhang, X., Liu, W., Cheng, L., and Xia, J.: Diagnosing structural deficiencies of a hydrological model by time-varying parameters, *Journal of Hydrology*, 605, <https://doi.org/10.1016/j.jhydrol.2021.127305>, 2022.