



An ensemble-based approach for pumping optimization in an island aquifer considering parameter, observation and climate uncertainty

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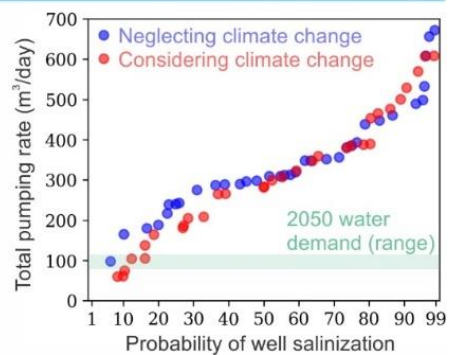
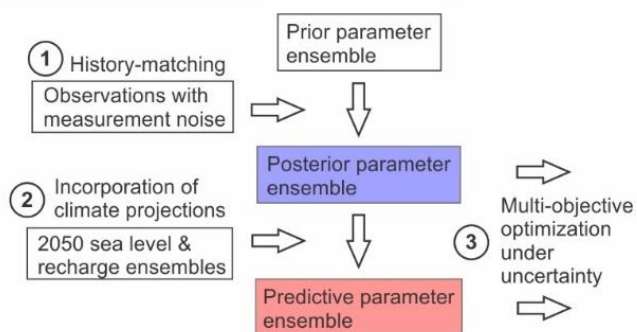
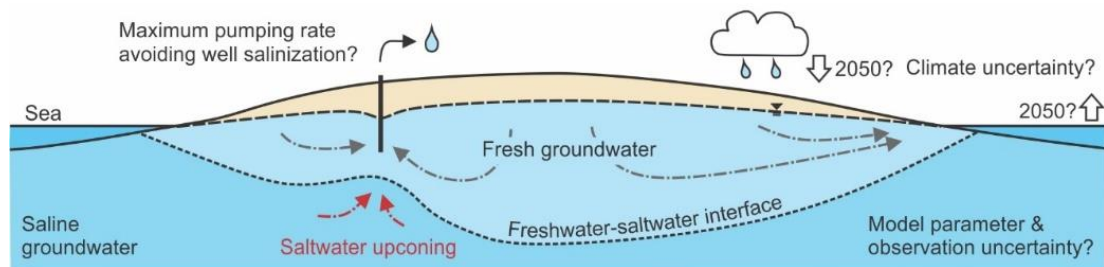
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Abstract. In coastal zones, a major objective of groundwater management is often to determine sustainable pumping rates avoiding well salinization. Understanding how model and climate uncertainties affect optimal management solutions is essential to provide groundwater managers information about salinization risk, and is facilitated by the use of optimization under uncertainty (OUU) methods. However, guidelines are missing for the widespread implementation of OUU in real-world coastal aquifers, and for the incorporation of climate uncertainty into OUU approaches. An ensemble-based OUU approach was developed, considering parameter, observation and climate uncertainty, and was implemented in a real-world island aquifer in the Magdalen Islands (Quebec, Canada). A sharp-interface seawater intrusion model was developed using MODFLOW-SWI2 and a prior parameter ensemble was generated, containing multiple equally plausible realizations. Ensemble-based history matching was conducted using an iterative ensemble smoother and yielded a posterior parameter ensemble conveying both parameter and observation uncertainty. 2050 sea level and recharge ensembles were generated and incorporated to generate a predictive parameter ensemble conveying parameter, observation and climate uncertainty. Multi-objective OUU was then conducted, aiming to both maximize pumping rates and minimize probability of well salinization. As a result, the optimal tradeoff between pumping and probability of salinization was quantified, considering parameter, historical observation and future climate uncertainty simultaneously. The multi-objective, ensemble-based OUU led to optimal pumping rates that were very different from a previous deterministic OUU, and close to the current and projected water demand for risk-averse stances. Incorporating climate uncertainty in the OUU was also critical since it reduced the maximum allowable pumping rates for users with a risk-averse stance. The workflow used tools adapted to very high-dimensional, nonlinear models and optimization problems, to facilitate its implementation in a wide range of real-world settings.





30 1 Introduction

Seawater intrusion is a major challenge for groundwater management in coastal zones, which are under pressure due to population growth, sea-level rise and changes in climate (Michael et al., 2017; Jiao and Post, 2019). Numerical models are often relied on to support groundwater management, using either advective-dispersive solute transport codes, which simulate mixing between freshwater and saltwater and are computationally demanding, or sharp-interface codes, which consider freshwater and saltwater
35 be immiscible but have significantly shorter simulation times. These numerical models can provide insight into freshwater availability under current and projected conditions, and they are frequently combined with optimization algorithms to determine sustainable pumping rates avoiding well salinization (Ketabchi and Ataie-Ashtiani, 2015). Optimizations in coastal zones should recognize the uncertainty in model predictions, to provide information to groundwater managers about salinization risk (Werner et al., 2013). However, optimization under uncertainty (OUU) approaches have mostly been implemented in synthetic or simplified
40 real-world cases (Rajabi and Ketabchi, 2017; Mostafaei-Avandari and Ketabchi, 2020), because of the high computational costs associated with both advective-dispersive solute transport models and stochastic uncertainty quantification. Guidance is missing for the implementation of OUU in real-world coastal settings (Ketabchi and Ataie-Ashtiani, 2015).

Real-world coastal OUU applications generally used advective-dispersive solute transport models in combination with surrogate models, evolutionary algorithms, and stochastic uncertainty quantification accounting for the uncertainty of a few models
45 parameters (e.g., between 2 and 11 parameters in Sreekanth and Datta, 2014; Rajabi and Ketabchi, 2017; Lal and Datta, 2019; Mostafaei-Avandari and Ketabchi, 2020; Han et al., 2021). They were also not systematically preceded by parameter estimation (i.e., automated calibration). However, accounting for model parameter uncertainty accurately and robustly can require very high numbers of parameters (White, 2018). Furthermore, conducting data assimilation prior to OUU is essential, since it allows to update parameter uncertainty estimates with observation uncertainty. In Coulon et al. (2022), the real-world OUU approach used
50 a sharp-interface model, sequential linear programming (SLP), and first-order-second-moment (FOSM) uncertainty analysis accounting for both parameter and observation uncertainty (including 60 parameters and 162 observations). It was preceded by parameter estimation (Coulon et al., 2021), conducted using the widely used Gauss-Levenberg-Marquardt (GLM) algorithm. However, the GLM and SLP algorithms can be computationally costly to apply in very highly parameterized and nonlinear models, which can limit the implementation of this workflow in other coastal settings. Furthermore, FOSM-based uncertainty analysis
55 relies on strong assumptions of model linearity and Gaussian distributions of uncertainty, and therefore can only provide approximations of model predictive uncertainty: stochastic, ensemble-based approaches are needed to provide more reliable uncertainty estimates. Developing an ensemble-based approach for coastal OUU adapted to highly-parameterized, nonlinear models would facilitate the implementation of OUU methods in real-world coastal settings.

Coupling climate uncertainty with model parameter uncertainty and understanding the consequences for groundwater management
60 was identified as a prospective topic of seawater intrusion research (Werner et al., 2013). However, current OUU approaches have considered parameter uncertainty only (e.g. in hydraulic conductivity, recharge, porosity, longitudinal dispersivity – Mostafaei-Avandari and Ketabchi, 2020), while climate change projections were incorporated into optimizations as discrete scenarios (e.g., optimization under a projected sea-level rise scenario or under four projected recharge scenarios in Roy and Datta (2018) and Zhao et al. (2021), respectively). The uncertainty associated with climate projections has therefore not been considered, although in the
65 field of hydrology, climate uncertainty is often evaluated using ensembles of climate projections (Mustafa et al., 2019; Al Atawneh et al., 2021). Generating ensembles of climate projections and combining them with model parameter ensembles, within an OUU framework, would enable the evaluation of the coupled impacts of climate and parameter uncertainty on groundwater management solutions, and lead to more robust decision-making.

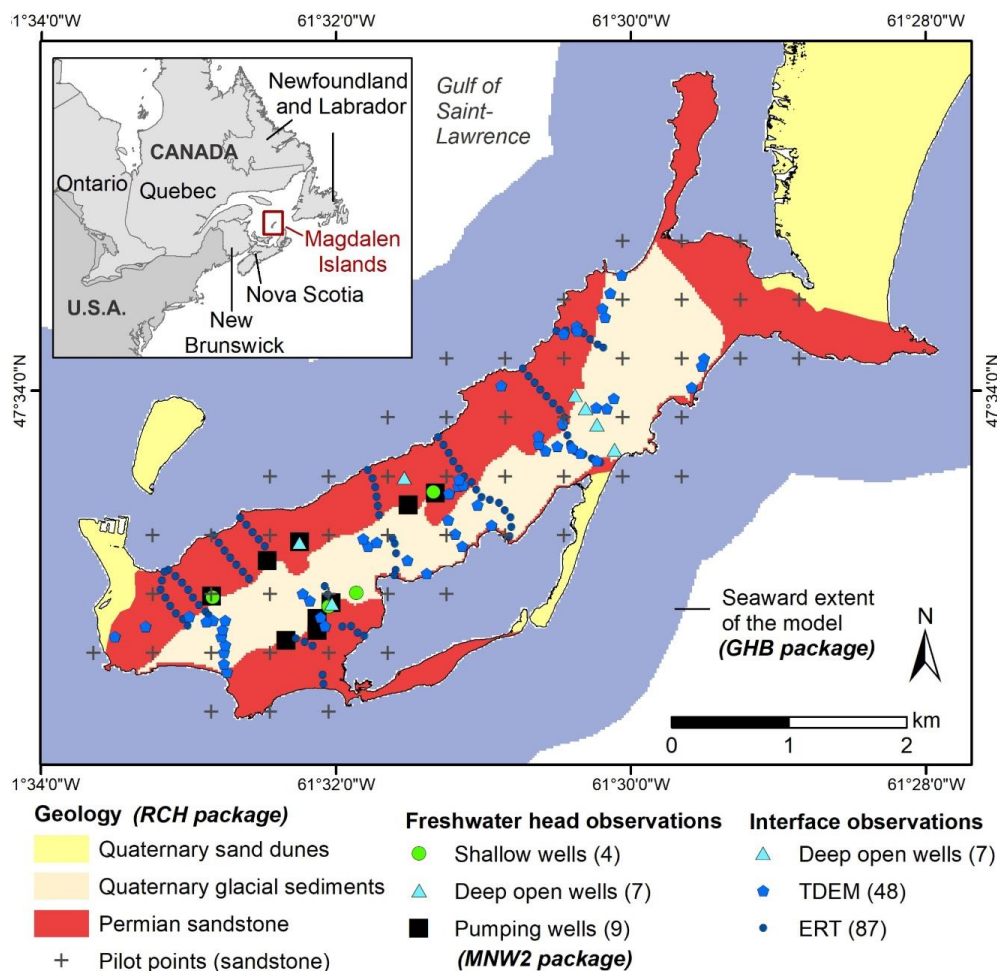


70 The objective of this study was to provide a framework for stochastic, ensemble-based pumping optimization under uncertainty in
an island aquifer considering parameter, historical observation and future climate uncertainty, and using methods adapted to very
high-dimensional, nonlinear models. An ensemble-based framework was implemented using a sharp-interface modeling approach.
A sharp-interface model was first built using MODFLOW-SWI2 (Bakker et al., 2013), after which ensemble-based history
75 matching was conducted using the iterative ensemble smoother PESTPP-IES (White, 2018). 2050 sea level and recharge climate
ensembles were generated and incorporated into the model parameter ensemble. Multi-objective optimization under uncertainty
was then conducted via PESTPP-MOU (White et al., 2022), using the ensemble to account for uncertainty in the simulated response
to groundwater extraction within the optimization process. Results were compared both to the current water demand and to 2050
water demand projections. This workflow was applied to a real-world island aquifer in the Magdalen Islands (Quebec, Canada)
and was entirely scripted in Python, to enhance the transparency and reproducibility of the analyses (e.g., White et al., 2020a;
Fienen and Bakker, 2016).

80 2 Study area

The Grande Entrée Island forms part of the Magdalen Islands archipelago, which is located in the middle of the Gulf of Saint-
Lawrence (Fig. 1). On this site, fresh groundwater is the only source of drinking water for the sparsely populated community, and
is contained in a lens overlying saline groundwater. The pumping wells in the water supply system are at risk of salinization, since
freshwater abstraction leads to the upward migration of saline groundwater towards the well, a process called saltwater upconing.
85 Deterministic parameter estimation and SLP, FOSM-based OUU were previously implemented on Grande Entrée Island to
determine maximum pumping rates avoiding well salinization, considering parameter and observation uncertainty and current
climate conditions (Coulon et al., 2021; Coulon et al., 2022). This study details the implementation of the ensemble-based approach
for history matching and multi-objective (MO) OUU, and the incorporation of climate uncertainty (specifically, sea level and
recharge uncertainty) into the pumping optimization. It compares the optimization results of the MO-ensemble approach to those
90 of the SLP-FOSM approach.

A detailed description of the study area is available in Coulon et al. (2021). The geology is comprised of a highly-permeable and
heterogeneous Permian sandstone (Fig. 1), along with Quaternary sand dunes and glacial sediments (mostly fine sand). A spatially
distributed recharge representative of the period 1989-2019 was generated for the Magdalen Islands archipelago by Lemieux et al.
(2022), using a SWB2 groundwater recharge model (Soil-Water-Balance-2, Westenbroek et al., 2018). A spatial average of 524
95 mm/year was determined for the whole archipelago, and of 559 mm/year for Grande-Entrée Island specifically. Using quadratic
regression and extrapolation of the Magdalen Islands' tide gage data, Barnett et al. (2017) projected a median relative sea-level
rise of 0.19 m for the archipelago between 2020 and 2050, assuming a normal probability distribution for the 2050 projected sea
level and a standard deviation of 0.11 m. Nine municipal pumping wells are drilled into the Permian sandstone formation, providing
freshwater to approximately 2,800 inhabitants and to the commercial, industrial and institutional sector since 2013. Between 2014
100 and 2020, the mean water demand in the network was approximately 93 m³/day. A median water demand projection of 94 m³/day
was estimated for 2050, with a range of possible values between 76 and 115 m³/day, showing no significant evolution in water
demand but uncertainty in the projections (Lemieux et al., 2022).



105 **Figure 1:** Map view of the Grande Entrée Island numerical model with seaward extent, geological formations and locations of pilot points, model observations and pumping wells (domestic wells not shown). The boundary conditions implemented in MODFLOW are shown: a uniform recharge rate on land cells (RCH package), general head boundary conditions for sea cells (GHB package), groundwater pumping at municipal wells (MNW2 package). Modified from Coulon et al. (2022).

3 Methods

3.1 Numerical model

110 A sharp-interface, 2D-horizontal model with a 20 m x 20 m grid was developed using the SWI2 package (Bakker et al., 2013) for MODFLOW-2005 (Harbaugh, 2005), which simulates vertically-integrated variable-density groundwater flow but does not account for hydrodynamic dispersion. Within the single model layer, the groundwater was divided into a freshwater zone and a saltwater zone, separated by an interface representing the 50% seawater salinity contour. The numerical model is described in detail by Coulon et al. (2021). A general head boundary condition was implemented in the offshore cells, to convert the sea level into equivalent freshwater heads at the ocean bottom (Bakker et al., 2013), and a uniform recharge rate was implemented on all land cells (Fig. 1). Municipal groundwater pumping was simulated using the MNW2 package (Konikow et al., 2009), to assimilate water levels (Coulon et al., 2021) and to calculate optimization constraints (Coulon et al., 2022). While domestic pumping was also simulated (Coulon et al., 2021), in the rest of the paper the term “pumping wells” will refer to the municipal pumping wells

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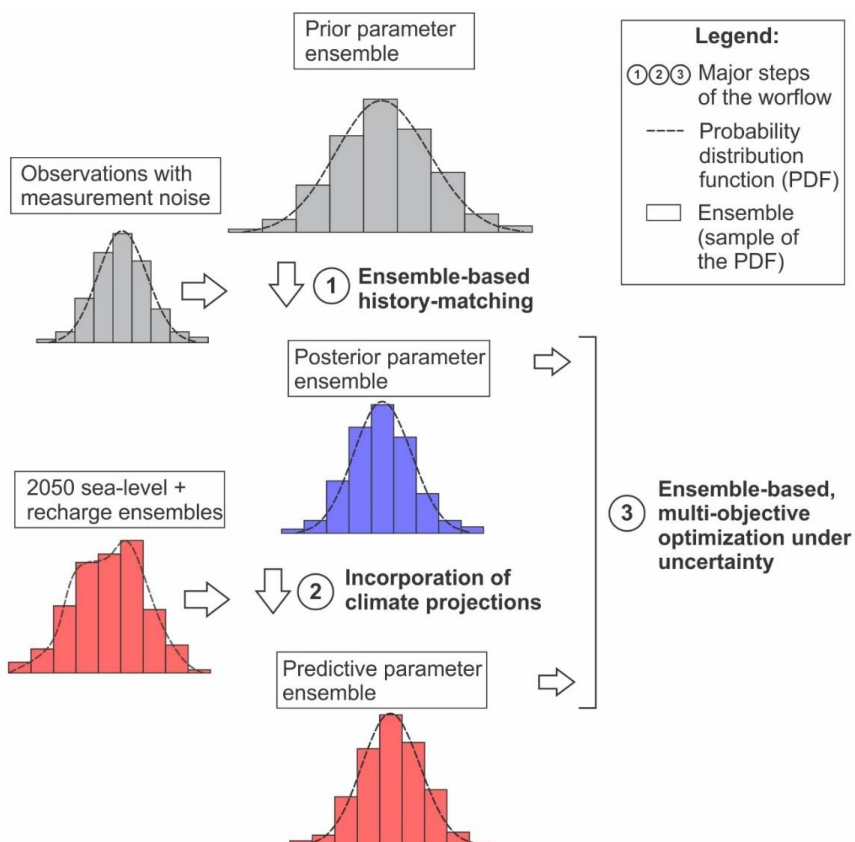
only. The hydraulic conductivity field was parameterized using a combination of pilot points and zones of piecewise constancy (Doherty, 2003). A homogeneous transverse dispersivity was implemented as a correction factor for the sharp interface (Coulon et al., 2021), while two additional parameters, longitudinal dispersivity and the initial transition zone width, intervened in the calculation of the optimization constraint (Coulon et al., 2022). Apart from recharge, whose prior value was updated with the Lemieux et al. (2022) estimates (Section 2), all model parameters were assigned prior values and ranges equal to those in Coulon et al. (2021) and Coulon et al. (2022), based on field measurements and existing literature, and assuming normal or lognormal probability distributions (Table 1). This allowed for the comparison between the previous SLP-FOSM approach and the current MO-ensemble approach.

Table 1: Prior parameter probability distributions of the uncertain model parameters, assumed to be normal or lognormal, described by the mean and the 95% confidence interval (i.e. the mean \pm 2 times the standard deviation).

	Mean	95% confidence interval
$K_{\text{sand dunes}}$ (m/s)	5×10^{-3}	$5 \times 10^{-5} - 5 \times 10^{-1}$
$K_{\text{sandstones}}$ (m/s) (offshore)	4×10^{-5}	$3 \times 10^{-6} - 6 \times 10^{-4}$
$K_{\text{sandstones}}$ (m/s) (52 pilot points)		
$K_{\text{glacial sediments}}$ (m/s)	1×10^{-5}	$1 \times 10^{-7} - 1 \times 10^{-3}$
K_{seabed} (m/s)	2×10^{-5}	$2 \times 10^{-7} - 2 \times 10^{-3}$
Transverse vertical dispersivity α_T (m)	1×10^{-1}	$1 \times 10^{-3} - 10$
Recharge (mm/yr)	560	360 – 760
Initial transition zone width M (m)	8	5 – 11
Longitudinal dispersivity α_L (m)	3	1 – 5

130 3.2 Ensemble-based history matching

Instead of adopting a deterministic approach, which seeks the minimum error variance parameter set resulting in the best fit to observations, an ensemble-based approach was selected: multiple, equally plausible realizations of parameter sets were generated (i.e., a parameter ensemble) and carried forward into the analyses (Anderson et al., 2015). The following definitions will be used throughout the paper. A realization is a parameter set; collectively, many realizations form a parameter ensemble. The prior parameter ensemble is the set of realizations that is generated prior to history matching, using only expert knowledge to define the statistical distributions of parameters. The posterior parameter ensemble is the set of realizations obtained after history matching (i.e., the prior parameter ensemble updated by observations). The predictive parameter ensemble is the set of realizations obtained after incorporating climate ensembles into the posterior parameter ensemble, all other aquifer parameters remaining constant (i.e., the posterior parameter ensemble updated by climate projections). The size of an ensemble corresponds to the number of realizations comprising the ensemble. The term “ensemble” is used in line with the PEST++ terminology (White et al., 2020b), and has the same meaning as the term “stack” commonly used in OUU literature (Bayer et al., 2008). Figure 2 summarizes the ensemble-based framework that was developed.



145 **Figure 2:** Summary of the ensemble-based workflow. An ensemble represents a sample of the probability distribution function (PDF). After
generating a prior parameter ensemble by drawing from prior parameter PDFs, 1) ensemble-based history matching yielded a posterior parameter
150 ensemble; 2) a predictive parameter ensemble was obtained by updating the posterior parameter ensemble with 2050 sea level and recharge
projections; and 3) optimization under uncertainty was conducted using both the posterior and the predictive parameter ensembles, to obtain
maximum allowable pumping rates considering parameter and observation uncertainty and either neglecting or accounting for climate projections,
respectively.

Fifty-eight model parameters were considered to be adjustable, including 56 hydraulic conductivity values, a uniform recharge rate
and a homogeneous transverse dispersivity (Section 3.1). N_{prior} realizations were drawn from the prior probability distribution
functions (PDFs) of these parameters (assumed to be normal or lognormal, Table 1), accounting for prior spatial correlations
between the pilot points parameters using an exponential variogram with a range equal to 3 times the pilot point spacing. The prior
155 parameter ensemble therefore represented a sample of the prior parameter PDF (Fig. 2). Several constant model parameters were
included in this ensemble and remained fixed during history matching, including the sea level, longitudinal dispersivity and the
initial width of the transition zone (Table 2).

Ensemble-based history matching was then conducted using PESTPP-IES (White, 2018), which implements an iterative ensemble
smoother form of the GLM algorithm (Chen and Oliver, 2013). PESTPP-IES was selected because it enables history matching of
160 highly-parameterized models at a significantly lower computational burden than sampling methodologies such as Markov Chain
Monte Carlo. Over successive iterations, PESTPP-IES adjusted the prior parameter ensemble against 20 freshwater head
observations (extracted from shallow wells, deep open wells and pumping wells) and 142 freshwater-seawater interface elevation
observations (derived from deep open wells, TDEM and ERT geophysical surveys, Fig. 1) paired with random realizations of
measurement noise (PEST++ Development Team, 2022). PESTPP-IES was limited to two iterations as an optimal tradeoff between



165 parameter posterior variance and fit to observations (Fienen et al., 2022). Details on the observation dataset and the measurement
 noise are provided by Coulon et al. (2021). History matching was conducted under steady-state conditions, using 500-year
 simulations with constant boundary conditions (i.e., sea level, recharge and pumping rates) representative of the average conditions
 during the 2014–2019 calibration period. The model simulation times were approximately 8 minutes on a laptop computer (1.9
 GHz Intel Core i7®). History matching yielded a posterior parameter ensemble of size N_{post} , representing a sample of the posterior
 170 parameter PDF (Fig. 2). N_{post} is usually less than or equal to N_{prior} , since the parameter realizations resulting in model run failures
 and/or excessive simulation times are removed from the parameter ensemble during history matching. Running model simulations
 through the posterior parameter ensemble yielded posterior prediction ensembles, representing samples of the posterior prediction
 PDFs (Fig. 2) and conveying parameter and observation uncertainty for current conditions.

175 **Table 2:** Prior, posterior and predictive parameter ensembles, described by the ensemble size, the mean and the 5–95 percentile range. Statistics
 of the prior parameter ensemble are not identical to those of the prior parameter PDFs, because ensembles represent a sample of probability
 distributions. During history matching, the sea level, M and α_L were fixed to a constant value. The recharge and sea level ensembles were updated
 in the predictive parameter ensemble. For the OUU, M and α_L were considered uncertain in both the posterior and the predictive parameter
 ensembles. The percentile range of the pilot point hydraulic conductivities is not reported since it is different for each pilot point.

Parameter	Prior parameter ensemble (size N_{prior})		Posterior parameter ensemble (size N_{post})		Predictive parameter ensemble (size N_{post})	
	Mean	5 th – 95 th percentiles	Mean	5 th – 95 th percentiles	Mean	5 th –95 th percentiles
$K_{\text{sand dunes}}$ (m/s)	4×10^{-2}	1×10^{-4} – 3×10^{-1}	7×10^{-3}	9×10^{-5} – 4×10^{-2}		
$K_{\text{sandstones}}$ (m/s) (offshore)	7×10^{-5}	4×10^{-6} – 2×10^{-4}	1×10^{-4}	2×10^{-5} – 5×10^{-4}		
$K_{\text{sandstones}}$ (m/s) (52 pilot points)	8×10^{-5}	–	2×10^{-4}	–	Identical to the posterior ensemble	
$K_{\text{glacial sediments}}$ (m/s)	8×10^{-5}	1×10^{-7} – 4×10^{-4}	5×10^{-5}	5×10^{-7} – 2×10^{-4}		
K_{seabed} (m/s)	2×10^{-4}	4×10^{-7} – 1×10^{-3}	1×10^{-5}	4×10^{-6} – 3×10^{-5}		
Transverse vertical dispersivity α_T (m)	9×10^{-1}	2×10^{-3} – 5	2×10^{-2}	2×10^{-3} – 5×10^{-2}		
Recharge (mm/yr)	547	371 – 696	572	444 – 695	574	344 – 826
Sea level (masl)	0.014	– (fixed)	0.014	– (fixed)	0.21	0.052 – 0.39
Initial transition zone width M (m)	8	– (fixed)	Identical to the prior ensemble for history matching, to the predictive ensemble for OUU		8	6 – 10
Longitudinal dispersivity α_L (m)	3	– (fixed)			3	1 – 5

180 3.3 Incorporating climate projections

The sea level and the recharge ensemble contained in the posterior parameter ensemble were representative of the 2014–2019 calibration period (Table 2). To make model predictions for 2050 accounting for climate projections, they were replaced with 2050 sea level and recharge ensembles (Fig. 2). Running model simulations through the predictive parameter ensemble yielded 2050 prediction ensembles conveying parameter, observation and climate uncertainty.



185 3.3.1 Sea level ensemble

The reference elevation used for the numerical model was the local mean sea level of the Magdalen Islands (Lemieux et al., 2022), therefore the term “meters above sea level” (or “masl”) is used in reference to this elevation. Using the relative sea-level rise projections for the study area (Section 2) and the current sea level (0.014 masl), a 0.204 masl mean sea level was expected for 2050, with a normal distribution and a standard deviation of 0.11 m. N_{post} realizations were drawn from this probability distribution, from which values above 0 masl were truncated, to generate a 2050 sea level ensemble. The current sea level value used in the posterior parameter ensemble was replaced by the 2050 sea level ensemble in the predictive parameter ensemble (Table 2).

3.3.2 Recharge ensemble

Seventy-two projections of daily precipitation, minimum and maximum air temperature were provided by the OURANOS consortium for the Magdalen Islands, for the period 2021–2050 (Charron, 2016). These resulted from three emission scenarios (the Representative Concentration Pathways RCP2.6, RCP4.5 and RCP8.5) being run through an ensemble of 24 Global Climate Models (GCMs) of the Coupled Model Intercomparison Project – Phase 5 (CMIP5). These 72 climate projections were run through the SWB2 groundwater recharge model developed by Lemieux et al. (2022) for the Magdalen Islands (Section 2), assuming a constant land use, which generated 72 daily recharge projections for the period 2021–2050 (Fig. 3a).

A 2050 recharge ensemble was extracted ($R_{2050, \text{SWB2}}$), containing 72 plausible recharge projections for 2050 generated by a physically-based groundwater recharge model (Section 2), and conveying climate uncertainty (specifically, the uncertainty in future emission scenarios and the inter-model uncertainty of GCMs) (Fig. 3b). History matching yielded a current recharge ensemble ($R_{\text{current}, \text{MODFLOW}}$), containing N_{post} plausible recharge inputs for the groundwater model (both informed by the observation dataset and incorporating possible correlations with the hydraulic conductivity parameters), and conveying parameter and observation uncertainty. The information contained in both ensembles needed to be merged, to obtain a 2050 recharge ensemble ($R_{2050, \text{MODFLOW}}$) containing N_{post} plausible recharge inputs for the groundwater model, preserving the information acquired through history matching (i.e., fit to observations, parameter correlations) but also accounting for future climate projections, and therefore conveying parameter, observation and climate uncertainty.

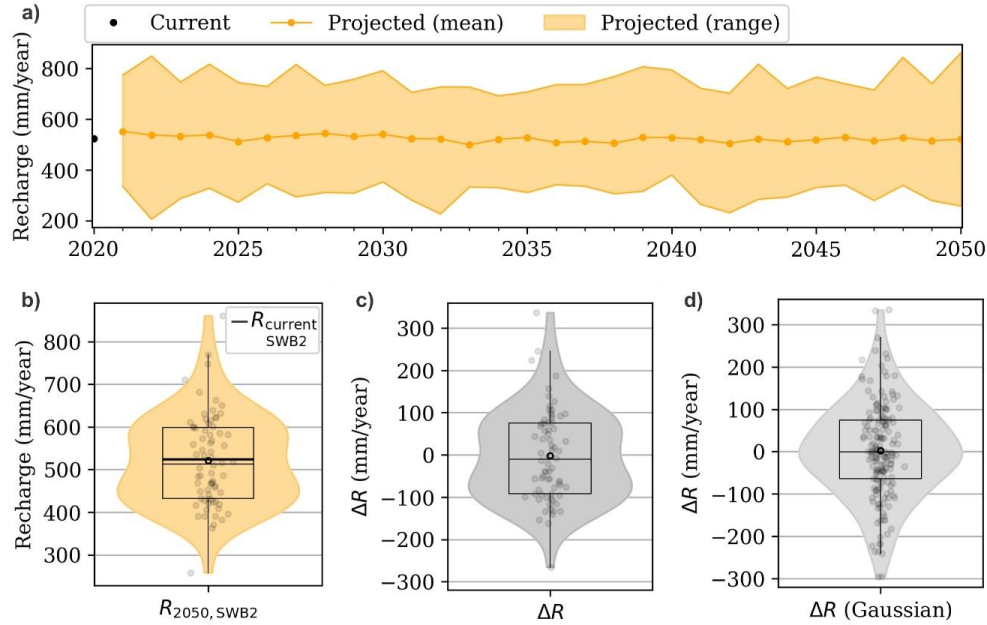
A ΔR ensemble was first generated, containing 72 possible recharge variations between current conditions and 2050, i.e., 72 possible perturbations to current recharge conditions (Fig. 3c), by subtracting the average current recharge value estimated by SWB2, $R_{\text{current}, \text{SWB2}}$, (Section 2) to all the projections in the $R_{2050, \text{SWB2}}$ ensemble:

$$\Delta R = R_{2050, \text{SWB2}} - R_{\text{current}, \text{SWB2}} \quad (1)$$

The ΔR ensemble was resampled to N_{post} realizations assuming a normal distribution (Fig. 3d). The $R_{2050, \text{MODFLOW}}$ ensemble, of size N_{post} , was then obtained by performing an element-wise sum between the ΔR and $R_{\text{current}, \text{MODFLOW}}$ ensembles:

$$R_{2050, \text{MODFLOW}} = R_{\text{current}, \text{MODFLOW}} + \Delta R \quad (2)$$

The $R_{\text{current}, \text{MODFLOW}}$ ensemble contained in the posterior parameter ensemble was replaced by $R_{2050, \text{MODFLOW}}$ in the predictive parameter ensemble (Table 2). The relative changes in projected recharge (ΔR) were therefore used rather than absolute recharge projections ($R_{2050, \text{SWB2}}$), and one of the major assumptions of this approach was that the recharge perturbations ΔR are uncorrelated with the current recharge value. The 2050 sea level and recharge projections were also assumed to be independent.



220 **Figure 3:** Processing of the climate ensembles generated by the SWB2 groundwater recharge model: (a) SWB2 recharge projections for 2021–2050; (b) $R_{2050, SWB2}$ ensemble extracted in 2050 (72 realizations); (c) ΔR ensemble obtained by subtracting $R_{current, SWB2}$ from $R_{2050, SWB2}$ (72 realizations); (d) ΔR ensemble resampled to N_{post} realizations (i.e., the size of the posterior parameter ensemble) assuming a normal distribution. In panels (b), (c) and (d) data points, mean values (bold black circles) and box plots are superimposed to the violin plots.

3.4 Optimization using ensemble-based uncertainty

225 The primary objective of the optimization was to maximize pumping rates in the well field while avoiding well salinization due to upconing. Salinization occurred if the 1% seawater salinity contour simulated under the well ($\zeta_{1\%}$), referred to as the optimization constraint, reached the well bottom elevation (z_{botm}). $\zeta_{1\%}$ was obtained by postprocessing the 50% seawater salinity contour simulated by the groundwater model ($\zeta_{50\%}$), which introduced two new uncertain parameters, namely longitudinal dispersivity (α_L) and the initial width of the transition zone (M) (see Coulon et al., 2022 for more details). An additional objective was introduced to the optimization problem, i.e., maximization of reliability, effectively converting the single-objective optimization into a reliability-based, two-objective optimization (Deb et al., 2007). In an ensemble-based framework, running a single pumping scenario through a parameter ensemble generates a constraint ensemble, in which the constraints can be satisfied (i.e., well salinization is avoided) for a fraction of the realizations, while constraints are violated (i.e., well salinization has occurred) in the others. The reliability Re is the probability of the constraints being satisfied in all of the realizations in the ensemble (Bayer et al., 2008), i.e., the probability of avoiding well salinization simultaneously for all wells. $100 - Re$ represents the probability of well salinization. Multiple optimal pumping scenarios can be determined for different reliability values, depending on the degree of tolerance towards risk (Fig. 4). The OUU was mathematically formulated as a constrained two-objective optimization:

$$\text{Maximize } Q_{total} = \sum_i^n Q_i, \quad (i = 1, \dots, n) \quad (3)$$

$$\text{Maximize } Re = P(\zeta_{1\% i} \leq z_{botm i}) \quad (i = 1, \dots, n) \quad (4)$$

$$\text{Subject to } \zeta_{1\% i} \leq z_{botm i} \quad (i = 1, \dots, n) \quad (5)$$

$$\text{and } Q_{min i} \leq Q_i \leq Q_{max i} \quad (i = 1, \dots, n) \quad (6)$$

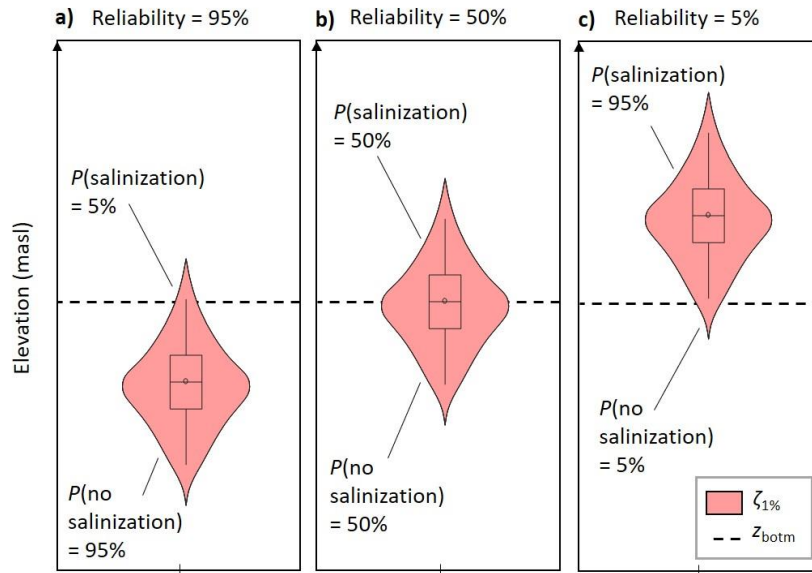
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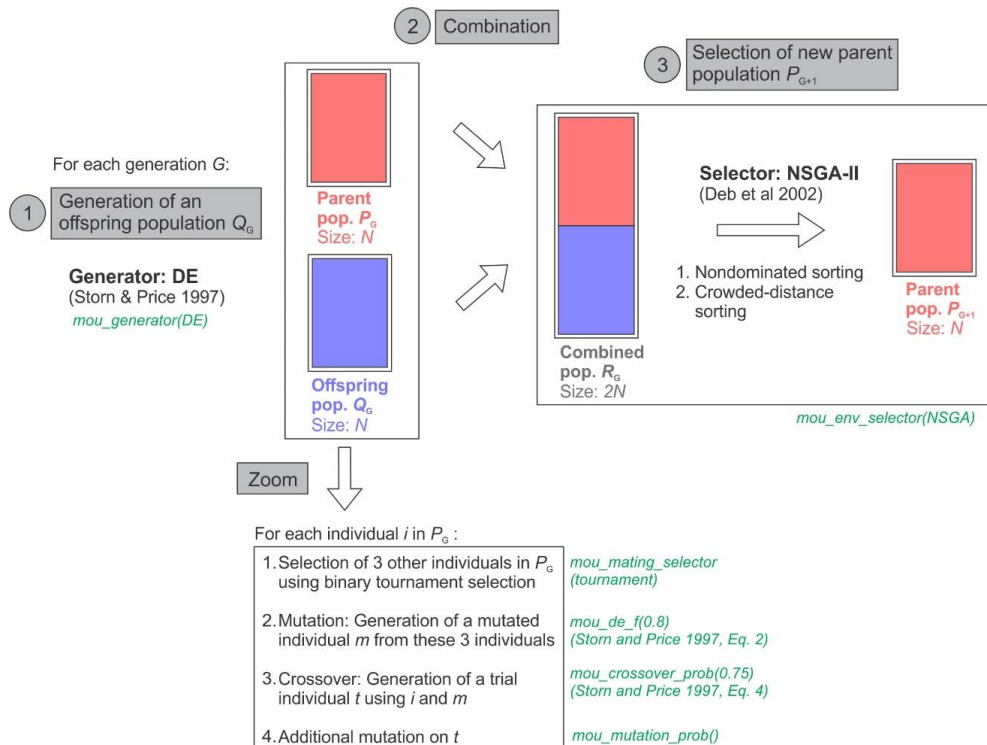
where Q_{total} is the total pumping rate in the well field (m^3/day), n is the number of pumping wells (nine in total), Q_i variables are the pumping rates at each well i (m^3/day), i.e., the decision variables of the optimization, $Q_{\text{min},i}$ and $Q_{\text{max},i}$ are the minimum and maximum pumping rates at each well i , respectively (m^3/day), Re is the reliability, $\zeta_{1\% i}$ values are the elevations of the 1% seawater salinity contour under each well i (masl), i.e., the optimization constraints, and $z_{\text{botm},i}$ is the bottom elevation of well i (masl). Wide $Q_{\text{min},i}$ and $Q_{\text{max},i}$ values were set, which effectively removed the constraint presented in Eq. (6).

Parameters M and α_L , which had remained fixed during history matching (Section 3.2), were considered to be uncertain in the optimization (Coulon et al., 2022). N_{post} realizations were drawn from the prior PDFs of M and α_L (Table 1) and were spliced into the posterior and predictive parameter ensembles (Table 2). 500-year initial simulations with zero pumping were run though both parameter ensembles to obtain equilibrium initial conditions for each realization. The pumping optimization under uncertainty was then conducted under steady-state conditions using 200-year simulations, and the occurrence of well salinization was examined at the end of the 200-year simulation period. Model simulation times were approximately 5 minutes on a laptop computer (1.9 GHz Intel Core i7®).

The optimization was solved using the NSGA-II nondominated-sorting genetic algorithm (Deb et al., 2002) implemented in PESTPP-MOU (White et al., 2022), using ensemble-based constraint uncertainty. PESTPP-MOU was selected because it implements a wide range of evolutionary algorithms, which are more effective than traditional optimization methods when solving highly nonlinear optimization problems typical of coastal environments (Ketabchi and Ataie-Ashtiani, 2015), its use required very little modification to input files after having previously used PEST++ software, and the reliability-based optimization could be implemented using PESTPP-MOU's "risk as an objective" option (White et al., 2022). The NSGA-II algorithm has been applied in many past coastal OUU studies (Mostafaei-Avandari and Ketabchi, 2020). It uses a population-based approach to identify the Pareto front, which is the optimal tradeoff surface between competing objectives (on which any further improvement to one of the objectives results in the reduction of another). The NSGA-II algorithm was implemented using a population size of 30 and 150 generations. At each generation, PESTPP-MOU generated new individuals from the parent population using differential evolution (Storn and Price, 1997), ranked all individuals according to their fitness using the NSGA-II algorithm (Deb et al., 2002) and selected the most fit individuals to be the new parent population for the next generation (details in Fig. 5). The prediction ensemble was evaluated for all the individuals of the initial population, reevaluated every 10 generations (which required a total of $30 \times N_{\text{post}}$ model simulations each) and reused in the intermediate generations, as a tradeoff between uncertainty quantification and computational constraints (White et al., 2022; PEST++ Development Team, 2022).



270 **Figure 4:** Schematic 1% seawater salinity contour ($\zeta_{1\%}$) constraint ensembles, represented by violin plots and box plots, resulting from optimizations with reliabilities of (a) 95%, (b) 50% and (c) 5%. Panels (a), (b) and (c) correspond to probabilities of well salinization of 5% (risk-averse stance), 50% (risk-neutral stance) and 95% (risk-tolerant stance), respectively. Modified from Coulon et al. (2022).



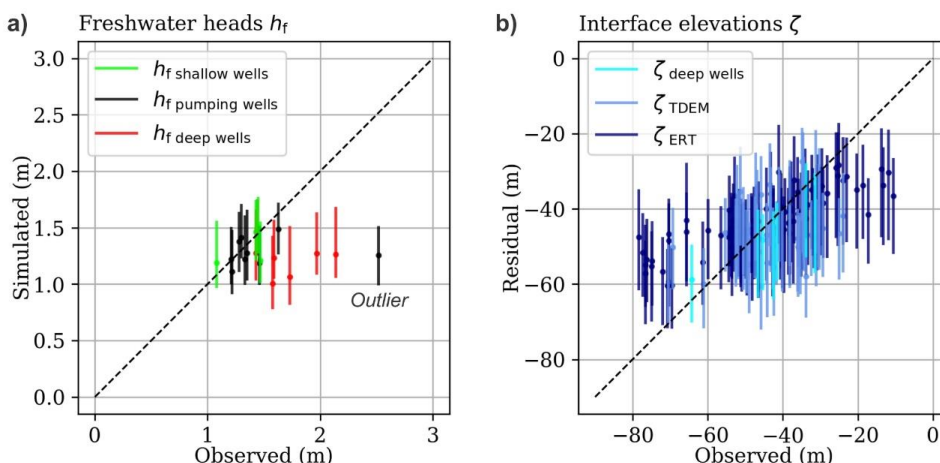
275 **Figure 5:** Summary of the main steps undertaken in each generation of the optimization, as a result of all PESTPP-MOU parameters (in green) being set to their default values (modified from Deb et al., 2002). The handling of chance constraints is not shown. More information on differential evolution (DE), the nondominated sorting genetic algorithm NSGA-II and PESTPP-MOU can be found in Storn and Price (1997), Deb et al. (2002) and PEST++ Development Team (2022), respectively.



4 Results

4.1 History matching

280 As the number of realizations increases, the ensembles become more representative of the PDFs that they sample, but
computational times increase. Analyzing the convergence of posterior $\zeta_{50\%}$ ensemble mean and standard deviation values as a
function of prior ensemble size led to the selection of a prior parameter ensemble containing 200 realizations. History matching
required 977 model runs, which took 2 hours using 50 cores at 2.3 GHz. 27 realizations were abandoned during history matching
(Section 3.2), resulting in a posterior parameter ensemble containing 173 realizations. The final objective function was in the range
285 of 1000–3200, with a mean value of 1250. An acceptable model-to-measurement misfit was obtained both for freshwater heads
(Fig. 6a) and freshwater-seawater interface elevations (Fig. 6b), and no prior-data conflicts were observed. These results were
similar to those of the deterministic parameter estimation conducted by Coulon et al. (2021), which had yielded a final objective
function of 1175 and similar patterns in the simulated-to-observed scatterplots (e.g., an outlier in the municipal well dataset and
biased freshwater head observations in deep wells). Hydrogeologically reasonable values were obtained in the posterior parameter
290 ensemble, with the sand dunes generally more permeable than the sandstones, in turn more permeable than the glacial sediments
(Table 2). Figure 7 presents a random sample of the 173 hydraulic conductivity fields obtained through history matching, and the
associated recharge values.



295 **Figure 6:** Scatter plots of simulated to observed data, for (a) freshwater heads and (b) freshwater-seawater interface elevations. To each observation corresponds an ensemble of simulated values: the line extends from the minimum to the maximum value and the point represents the mean. The 1:1 diagonal line represents equal simulated and observed data.

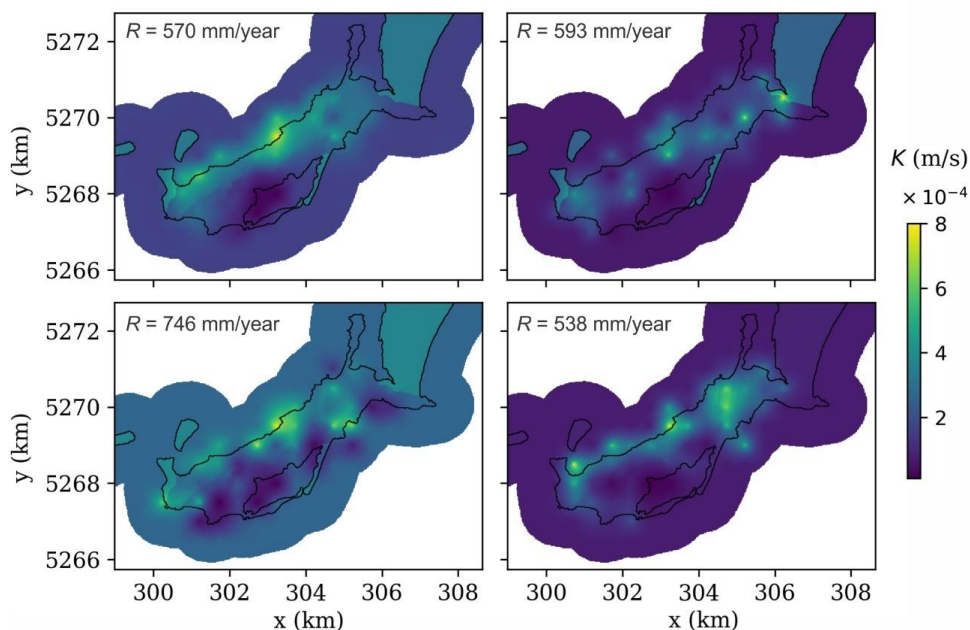


Figure 7: Example of four realizations extracted from the posterior parameter ensemble. Posterior hydraulic conductivity (K) fields and the associated recharge values (R) are shown.

300 4.2 Incorporating climate projections

All the projections in the 2050 sea level ensemble were greater than the current sea level value (Fig. 8a), with a mean projected sea-level rise of 0.2 m and an uncertainty (represented by the standard deviation) of 0.1 m. The ΔR ensemble, i.e., the ensemble containing possible recharge variations between current conditions and 2050 (Section 3.3.2), showed little-to-no evolution in the mean recharge (mean value close to zero, Fig. 3c), but a climate-related uncertainty of 108 mm/year. As a consequence, the current and 2050 recharge ensembles had very similar median values (less than 1% variation, Fig. 8b), but the uncertainty of the 2050 recharge ensemble increased by 86% (from 78 to 145 mm/year). The $\zeta_{50\%}$ ensembles obtained using the posterior and predictive parameter ensembles, i.e., when neglecting or accounting for climate projections, respectively, were compared at steady-state conditions with zero pumping (i.e., the pumping optimization initial conditions, Section 3.4). Both ensembles had very similar median values (less than 0.5% variation on average, Fig. 9). However, the uncertainty of the posterior $\zeta_{50\%}$ ensembles increased significantly (on average by 114%, from 4 to 8 m). When accounting for climate projections, some realizations in the predictive parameter ensemble led to $\zeta_{50\%}$ values reaching well bottom elevations, even with zero pumping (e.g. at wells no. 7 and 8, Fig. 9).

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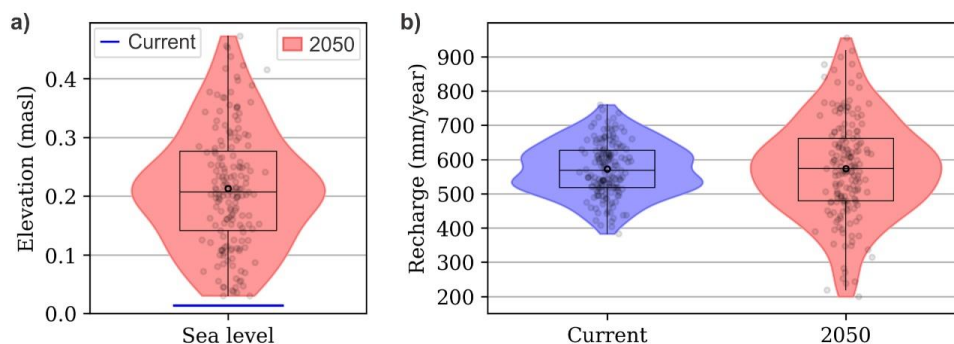
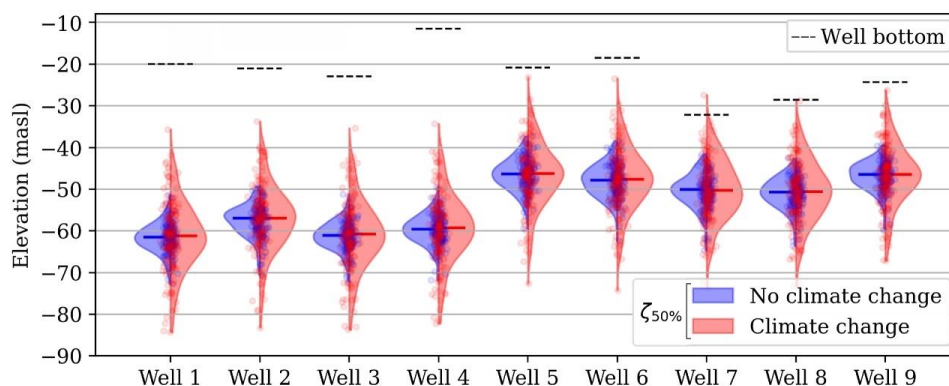


Figure 8: Current vs 2050 projected (a) sea level and (b) recharge ensembles, as implemented in either the posterior (blue) or the predictive (red) parameter ensembles. Data points, mean values (bold black circle) and box plots are superimposed to the violin plots.



315

Figure 9: 50% seawater salinity contour ($\zeta_{50\%}$) ensembles under each pumping well, under steady-state conditions without pumping, when neglecting (blue) or accounting for (red) climate projections. Data points, median values (horizontal lines) and well bottom elevations are superimposed to the violin plots.

4.3 Optimization under uncertainty

320 The OUU procedure for the posterior and predictive parameter ensembles required approximately 89,000 and 86,000 model simulations, respectively, which took a total of 320 hours, using 130 cores at 2.3 GHz. 34 and 35 Pareto-optimal pumping scenarios were identified. The Pareto front, or optimal tradeoff between pumping and probability of well salinization, was identified (Fig. 10), and the optimal allocation of pumping in the well field was determined for a range of probabilities of well salinization (Fig. 11). As the maximum pumping rate in the well field (Fig. 10) and at individual wells (Fig. 11) increased, the probability of well salinization increased as well.

330 The results of the MO-ensemble approach (when neglecting climate projections) were first compared to those of the SLP-FOSM approach described in Coulon et al. (2022). The maximum allowable pumping rates determined by the MO-ensemble approach were lower for all but highly risk-tolerant stances (Fig. 10), and the difference between both approaches was largest at highly risk-averse stances. For example, for a 6% probability of well salinization, the MO-ensemble approach found a maximum allowable pumping rate of 98 m³/day, versus 260 m³/day for the SLP-FOSM approach. For risk-averse stances, the pumping rates at individual wells were generally lower (e.g., wells 1 and 5, Fig. 11). The MO-ensemble approach determined higher probabilities of well salinization than the SLP-FOSM approach, for equal values of total pumping in the well field. For example, a 230 m³/day pumping rate corresponded to a 25% probability of salinization using the former approach, versus 2% using the latter approach. In



fact, the MO-ensemble approach did not identify any pumping scenarios with probabilities of salinization under 6% (Fig. 10). Most importantly, the most risk-averse pumping scenario found by the MO-ensemble approach (98 m³/day) was of the same order of magnitude as both the current and projected water demand, whereas the SLP-FOSM approach systematically found pumping scenarios far greater than the water demand.

The consequences of neglecting or accounting for climate projections within the MO-ensemble approach were then examined. When climate projections were considered, the maximum allowable pumping rates were lower for risk-averse stances (Fig. 10). Therefore, when considering climate projections, pumping rates needed to be lowered to conserve identical probabilities of well salinization; for example, selecting a 10% probability of salinization required reducing the total pumping in the well field from 165 to 60 m³/day (Fig. 10), and the pumping rate at well no. 8 from 19 to 4 m³/day (Fig. 11). On the other hand, neglecting climate projections resulted in underestimating probabilities of salinization, since a 98 m³/day total pumping rate in the well field represented a 6% probability of salinization when neglecting climate projections, but a 12% probability of salinization when considering climate projections (Fig. 10). The dispersion and non-unicity of the individual pumping rates identified by the ensemble-based method (Fig. 11) made a fine comparison of individual pumping rates challenging. Overall, when considering climate projections, no pumping scenarios were found with probabilities of well salinization lower than 8%. The most risk-averse pumping scenarios (with probabilities of salinization between 8–10%) were smaller than both the current and projected water demand, and less risk-averse scenarios (with probabilities of salinization between 10–15%) were of the same order of magnitude as the water demand.

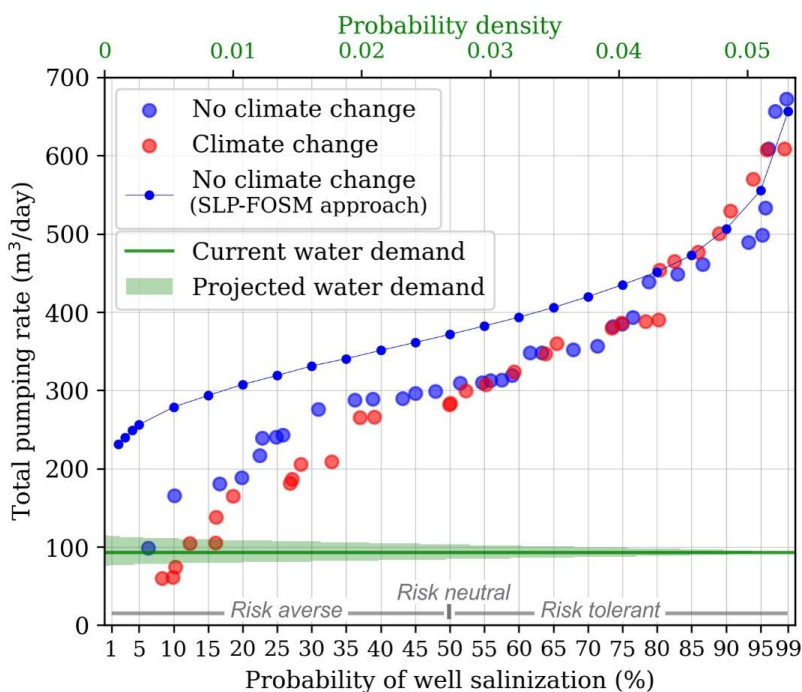


Figure 10: Optimal tradeoff between the total pumping rate in the well field and the probability of well salinization, when neglecting (blue) or accounting for (red) climate projections (ensemble-based approach). The results obtained using the SLP-FOSM approach (neglecting climate change effects) are also shown. The current water demand and the PDF of the 2050 projected water demand are superimposed. The y-axis was cut off at 700 m³/day.

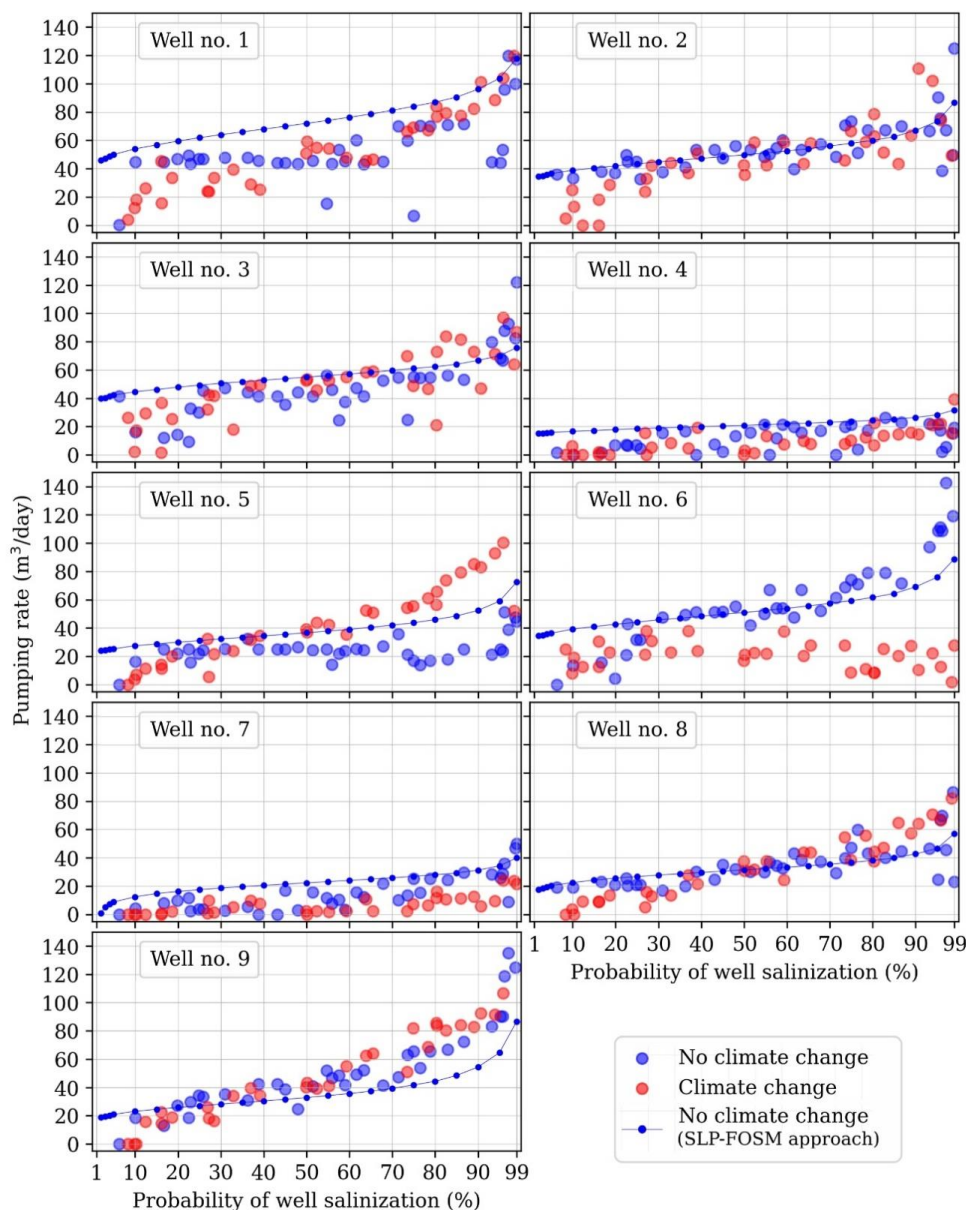


Figure 11: Optimal allocation of pumping in the well field as a function of probability of well salinization, when neglecting (blue) or accounting for (red) climate projections (ensemble-based approach). The results obtained using the SLP-FOSM approach (neglecting climate change effects) are also shown. The y-axis was cut off at 150 m³/day.

360 5 Discussion

5.1 Optimization under uncertainty

The OUs identified sets of maximum allowable pumping scenarios corresponding to different probabilities of salinization, from which the groundwater managers can choose depending on their attitude towards risk (Coulon et al., 2022). The limitations associated with using a sharp-interface model to simulate saltwater upconing are discussed in detail in Coulon et al. (2022).



365 Different results were obtained when using a MO-ensemble approach or a SLP-FOSM approach to OUU. Since ensemble-based
uncertainty quantification is more reliable than FOSM-based uncertainty estimates, the probabilities of well salinization determined
by the MO-ensemble approach are more reliable. In the study area, the SLP-FOSM approach may have overestimated the maximum
allowable pumping rates compared to the MO-ensemble approach and underestimated the probability of well salinization
associated with pumping scenarios, especially for risk-averse stances. The SLP-FOSM approach would have led to the conclusion
370 that the well field is able to supply both the current water demand and the highest water demand projections, with a large margin,
while maintaining a very low probability of salinization of 2%. In comparison, the MO-ensemble approach found much smaller
maximum allowable pumping rates, and if the highest risk-averse stance was adopted (i.e., a 6% probability of well salinization),
the well field would scarcely be able to meet the current water demand, and could only meet the higher water demand projections
with an increased probability of well salinization. However, in the MO-ensemble approach, the complete convergence to the Pareto
375 front requires many generations of the NSGA-II algorithm, which in practice is limited by computational constraints. Therefore,
the maximum allowable pumping rates found by the MO-ensemble approach for the study area may also be suboptimal, and overly
conservative.

Incorporating climate projections into the parameter ensembles, instead of moving directly from history matching to OUU, was
essential, since neglecting climate projections resulted in underestimating predictive uncertainties (Fig. 9) and therefore
380 underestimating probabilities of well salinization for risk-averse pumping scenarios (Fig. 10). This was the case even though the
climate projections hardly affected the median model predictions (Fig. 9): the simple increase in model predictive uncertainty due
to additional consideration of climate uncertainty, which can be expected in other areas, was enough to impact the results of the
OUU. Accounting for climate projections in the OUU decreased the maximum allowable pumping rates for users with a risk-averse
stance, and therefore led to more conservative pumping scenarios. When accounting for climate projections, if the highest risk-
385 averse stance was adopted (i.e., an 8% probability of well salinization), the well field would be unable to meet neither the current
water demand nor the lowest water demand projections. Therefore, groundwater managers could either decide to meet the water
demand but at higher probabilities of salinization (greater than 10–15%), or to find supplementary sources of water. Multiplying
the probability of well salinization by its consequences would allow to characterize the risk of salinization, and therefore assist
decision-makers in their evaluation of different management options.

390 **5.2 Incorporating climate projections**

Although the sea level and recharge projections were considered to be independent (Section 3.3), sea-level rise projections linked
to GCMs and RCPs can sometimes be found (e.g., James et al., 2021) and linked sea level-recharge ensembles could be used in
future OUUs. However, climate uncertainty is always dependent on the size and the nature of the projections contained in the
climate ensemble (for example the number and nature of GCMs and RCPs used), and the uncertainty is expected to increase with
395 the ensemble size. Even if all available GCMs were used, these would still represent a subset of possible future climates (Ray and
Brown, 2015). Therefore, the optimal pumping scenarios should regularly be updated with the latest climate projections. Another
approach could be to integrate robustness to climate uncertainty into the optimization, aiming to find pumping scenarios that are
less sensitive to climate uncertainty and that perform well under a wide range of climate projections (Borgomeo et al., 2018).

This study considered climate change effects under steady-state conditions, and explored the management options that would result
400 from the groundwater system (i.e., the freshwater lens) equilibrating with the 2050 climate projections. In reality, since climate
change effects are a transient process and this steady state may never be reached, this approach can therefore be viewed as being
conservative. When considering transient conditions, climate uncertainties might increase with time and interannual climate
variability (e.g. variations in the frequency and intensity of extreme weather events) may also impact the optimization results.



405 Few examples were found in the existing literature as to how to merge the parameter and climate recharge ensembles (Section 3.3.2). These were obtained independently, through different types of models: a calibrated groundwater flow model with a simplified representation of recharge (MODFLOW-SWI2) and a more complex, uncalibrated groundwater recharge model able to convert weather projections into recharge projections (SWB2). The groundwater recharge model could have been coupled to the groundwater flow model, with its uncertain parameters added to the history matching procedure, and the weather projections would then be run directly through the coupled models. However, the coupling of numerical models is often computationally demanding.

410 In the approach that was selected, the ΔR ensemble was resampled assuming a normal distribution, as a first approximation, which did not conserve the exact shape of the ΔR distribution (Fig. 3c, 3d). However, the ensemble-based approach allows for the incorporation of climate projections that do not necessarily follow Gaussian distributions. Rejection sampling or Markov Chain Monte Carlo methods could also be employed to resample the ΔR ensemble while conserving its shape. Further investigations on this subject would be of interest.

415 **5.3 Use of an ensemble-based approach**

Using an ensemble-based approach in combination with a population-based evolutionary algorithm such as NSGA-II required a significant number of model simulations. The use of parallel processing was critical to implement the framework within reasonable computational times and was greatly facilitated by the use of PEST++ software, which contain a fault-tolerant, parallel run manager (White et al., 2020b). The Pareto front is sensitive to the ensemble size, and Sreekanth et al. (2016) analyzed the convergence to the Pareto front using different amounts of realizations. In particular, the solutions at the extremities of the Pareto front are expected to be sensitive to the tails of the constraint PDFs, but the convergence of the extreme percentiles (e.g. 95th, 99th) of constraint ensembles could require a prohibitive amount of realizations. In our case, while the extremities of the Pareto front were found to be sensitive to the ensemble size, using 173 realizations was the maximum that was computationally feasible. Therefore, the highly risk-averse region may not be fully explored. While it is educative, mapping the entire Pareto front is computationally expensive,

420 when it is only the high-reliability solutions that are generally of interest to groundwater managers. Stack-ordering methods have been developed to find highly-reliability solutions in ensemble-based OUs at a very low computational burden (e.g. Bayer et al., 2010; Paly et al., 2013), and implementing these would be very useful for managers wishing to adopt highly risk-averse stances. Finally, with the MO-ensemble approach, the dispersion and non-unicity of the individual pumping rates (i.e., of the decision variables) could make the presentation of the results to decision-makers and their implementation more challenging.

425

430 **6 Conclusion**

A fully scripted workflow was developed for ensemble-based history matching, incorporation of climate projections and pumping optimization under uncertainty considering parameter, historical observation and future climate uncertainty. The workflow was implemented in a real-world island aquifer. It allowed for the quantification of the optimal tradeoff between pumping and probability of well salinization considering parameter, observation and climate uncertainty simultaneously, letting groundwater managers choose the final pumping scenario depending on their attitude towards risk. Incorporating climate projections into the OU allows groundwater managers to account for multiple sources of uncertainty simultaneously, i.e., uncertainty arising from the model itself (e.g., parameter and observation uncertainty) and climate uncertainty (e.g., sea level and recharge uncertainty).

435 The workflow used easily accessible, model-independent tools for ensemble-based history matching and multi-objective optimization under uncertainty, that are applicable to high-dimensional, nonlinear models and to nonlinear optimization problems.

440 It could therefore be implemented in a large range of coastal settings, including high-dimensional and nonlinear models, provided



that model simulations are parallelized. The workflow could also be adapted to other management optimization under uncertainty problems. The multi-objective, ensemble-based approach led to much lower maximum allowable pumping rates than the previously applied sequential linear programming, FOSM-based approach (Coulon et al., 2022), for users with risk averse stances. This was the case even though the numerical model and optimization problem were relatively linear.

445 A method for merging parameter and climate recharge ensembles was suggested, and the effect of this coupling on management optimization was explored. Incorporating climate uncertainty into the workflow was critical, since it reduced the maximum allowable pumping rate for users with a risk-averse stance, and since neglecting climate uncertainty resulted in underestimating the probabilities of well salinization. In the study area, when considering 2050 sea level and recharge projections, the well field would be unable to meet the current water demand or any of the 2050 water demand projections while maintaining very low risks
450 of well salinization. Conceptual uncertainty was not considered in the analysis, but its evaluation and coupling with the other sources of uncertainty would be useful as it could also impact the results of the optimization.

Code availability

The Python scripts used to implement the workflow and produce figures are available on GitHub at <https://github.com/Cecile-A-C/swi2-ensembles> and are archived at <https://doi.org/10.5281/zenodo.7574457> (version 1.0.0, MIT license). MODFLOW-2005
455 (version 1.12.00) is available at <https://www.usgs.gov/software/modflow-2005-usgs-three-dimensional-finite-difference-ground-water-model>. PESTPP-IES, PESTPP-SWP and PESTPP-MOU are available at <https://www.usgs.gov/software/pest-software-suite-parameter-estimation-uncertainty-analysis-management-optimization-and> and the source code is available at <https://github.com/usgs/pestpp/releases> (version 5.1.13 was used for PESTPP-IES and PESTPP-SWP and version 5.1.24 was used for PESTPP-MOU).

460 Author contribution

Cécile Coulon: Conceptualization, Formal analysis, Methodology, Visualization, Writing. **Jeremy T. White:** Formal analysis, Methodology, Software, Writing. **Alexandre Pryet:** Conceptualization, Methodology, Resources, Writing. **Laura Gatel:** Formal analysis, Methodology. **Jean-Michel Lemieux:** Conceptualization, Resources, Supervision, Writing.

Competing interests

465 The authors declare that they have no conflict of interest. Jeremy White was funded by INTERA Incorporated.

Acknowledgments

This work was funded by the Ministère de l'Environnement et de la Lutte contre les changements climatiques of Quebec, as part of the project « Acquisition de connaissances sur les eaux souterraines dans la région des Îles-de-la-Madeleine » (Groundwater characterization project in the Magdalen Islands region). The authors would like to thank the OURANOS consortium and Marco
470 Braun for supplying the daily precipitation, minimum and maximum air temperature climate simulations for the Magdalen Islands for the period 1950-2100. A scholarship provided by the Canadian National Chapter of the IAH (IAH-CNC) to Cécile Coulon helped conduct this study. Jeremy White was funded by INTERA Incorporated.



References

- Al Atawneh, D., Cartwright, N., and Bertone, E.: Climate change and its impact on the projected values of groundwater recharge: A review, *Journal of Hydrology*, 601, 126602, 10.1016/j.jhydrol.2021.126602, 2021.
- Anderson, M. P., Woessner, W. W., and Hunt, R. J.: *Applied groundwater modeling: simulation of flow and advective transport*, Academic press, 2015.
- Bakker, M., Schaars, F., Hughes, J. D., Langevin, C. D., and Dausman, A. M.: Documentation of the seawater intrusion (SWI2) package for MODFLOW, *US Geological Survey Techniques and Methods*, Book, 6, 10.3133/tm6A46, 2013.
- Barnett, R. L., Bernatchez, P., Garneau, M., and Juneau, M. N.: Reconstructing late Holocene relative sea-level changes at the Magdalen Islands (Gulf of St. Lawrence, Canada) using multi-proxy analyses, *Journal of Quaternary Science*, 32, 380-395, 10.1002/jqs.2931, 2017.
- Bayer, P., Bürger, C. M., and Finkel, M.: Computationally efficient stochastic optimization using multiple realizations, *Advances in Water Resources*, 31, 399-417, 10.1016/j.advwatres.2007.09.004, 2008.
- Bayer, P., de Paly, M., and Bürger, C. M.: Optimization of high-reliability-based hydrological design problems by robust automatic sampling of critical model realizations, *Water Resources Research*, 46, 10.1029/2009wr008081, 2010.
- Borgomeo, E., Mortazavi-Naeini, M., Hall, J. W., and Guillod, B. P.: Risk, Robustness and Water Resources Planning Under Uncertainty, *Earth's Future*, 6, 468-487, 10.1002/2017ef000730, 2018.
- Charron, I.: *A Guidebook on Climate Scenarios: Using Climate Information to Guide Adaptation Research and Decisions*, 2016 Edition., Ouranos, 94, 2016.
- Chen, Y., and Oliver, D. S.: Levenberg–Marquardt forms of the iterative ensemble smoother for efficient history matching and uncertainty quantification, *Computational Geosciences*, 17, 689-703, 10.1007/s10596-013-9351-5, 2013.
- Coulon, C., Pryet, A., Lemieux, J.-M., Yrro, B. J. F., Bouchedda, A., Gloaguen, E., Comte, J.-C., Dupuis, J. C., and Banton, O.: A framework for parameter estimation using sharp-interface seawater intrusion models, *Journal of Hydrology*, 600, 10.1016/j.jhydrol.2021.126509, 2021.
- Coulon, C., Lemieux, J. M., Pryet, A., Bayer, P., Young, N. L., and Molson, J.: Pumping Optimization under Uncertainty in an Island Freshwater Lens using a Sharp-Interface Seawater Intrusion Model, *Water Resources Research*, 58, e2021WR031793, 10.1029/2021WR031793, 2022.
- Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T.: A fast and elitist multiobjective genetic algorithm: NSGA-II, *IEEE transactions on evolutionary computation*, 6, 182-197, 10.1109/4235.996017, 2002.
- Deb, K., Padmanabhan, D., Gupta, S., and Mall, A. K.: Reliability-based multi-objective optimization using evolutionary algorithms, *International Conference on Evolutionary Multi-Criterion Optimization*, 2007, 66-80,
- Doherty, J.: Ground water model calibration using pilot points and regularization, *Groundwater*, 41, 170-177, 10.1111/j.1745-6584.2003.tb02580.x, 2003.
- Fienen, M. N., and Bakker, M.: HESS Opinions: Repeatable research: what hydrologists can learn from the Duke cancer research scandal, *Hydrology and Earth System Sciences*, 20, 3739-3743, 10.5194/hess-20-3739-2016, 2016.
- Fienen, M. N., Corson-Dosch, N. T., White, J. T., Leaf, A. T., and Hunt, R. J.: Risk-Based Wellhead Protection Decision Support: A Repeatable Workflow Approach, *Ground Water*, 60, 71-86, 10.1111/gwat.13129, 2022.
- Han, Z., Lu, W., Fan, Y., Xu, J., and Lin, J.: Surrogate-Based Stochastic Multiobjective Optimization for Coastal Aquifer Management under Parameter Uncertainty, *Water Resources Management*, 35, 1479-1497, 10.1007/s11269-021-02796-5, 2021.
- Harbaugh, A. W.: MODFLOW-2005, the US Geological Survey modular ground-water model: the ground-water flow process, US Department of the Interior, US Geological Survey Reston, VA, 2005.
- James, T. S., Robin, C., Henton, J. A., and Craymer, M.: Relative sea-level projections for Canada based on the IPCC Fifth Assessment Report and the NAD83v70VG national crustal velocity model, *Geological Survey of Canada*, 2021.
- Jiao, J., and Post, V.: *Coastal hydrogeology*, Cambridge University Press, 2019.
- Ketabchi, H., and Ataie-Ashtiani, B.: Review: Coastal groundwater optimization—advances, challenges, and practical solutions, *Hydrogeology Journal*, 23, 1129-1154, 10.1007/s10040-015-1254-1, 2015.
- Konikow, L. F., Hornberger, G. Z., Halford, K. J., and Hanson, R. T.: Revised multi-node well (MNW2) package for MODFLOW ground-water flow model, *US Geological Survey Techniques and Methods*, 67, 10.3133/tm6A30, 2009.



- 520 Lal, A., and Datta, B.: Multi-objective groundwater management strategy under uncertainties for sustainable control of saltwater intrusion: Solution for an island country in the South Pacific, *Journal of Environmental Management*, 234, 115-130, 10.1016/j.jenvman.2018.12.054, 2019.
- Lemieux, J.-M., Germain, A., Tremblay, Y., Gatel, L., Arbour, G., Coulon, C., and Dupuis, C.: Portrait des ressources en eau souterraine des îles de la Madeleine [Overview of groundwater resources in the Magdalen Islands], *Département de géologie et de génie géologique, Université Laval*, , 2022.
- 525 Michael, H. A., Post, V. E. A., Wilson, A. M., and Werner, A. D.: Science, society, and the coastal groundwater squeeze, *Water Resources Research*, 53, 2610-2617, 10.1002/2017wr020851, 2017.
- Mostafaei-Avandari, M., and Ketabchi, H.: Coastal Groundwater Management by an Uncertainty-Based Parallel Decision Model, *Journal of Water Resources Planning and Management*, 146, 10.1061/(asce)wr.1943-5452.0001227, 2020.
- 530 Mustafa, S. M. T., Hasan, M. M., Saha, A. K., Rannu, R. P., Van Uytven, E., Willems, P., and Huysmans, M.: Multi-model approach to quantify groundwater-level prediction uncertainty using an ensemble of global climate models and multiple abstraction scenarios, *Hydrology and Earth System Sciences*, 23, 2279-2303, 10.5194/hess-23-2279-2019, 2019.
- Paly, M. d., Bürger, C. M., and Bayer, P.: Optimization under worst case constraints—a new global multimodel search procedure, *Structural and Multidisciplinary Optimization*, 48, 1153-1172, 10.1007/s00158-013-0950-5, 2013.
- 535 PEST++ Development Team: PEST++ Manual, Version 5.1.13, 2022.
- Rajabi, M. M., and Ketabchi, H.: Uncertainty-based simulation-optimization using Gaussian process emulation: Application to coastal groundwater management, *Journal of Hydrology*, 555, 518-534, 10.1016/j.jhydrol.2017.10.041, 2017.
- Ray, P. A., and Brown, C. M.: Confronting climate uncertainty in water resources planning and project design: The decision tree framework, *World Bank Publications*, 2015.
- 540 Roy, D. K., and Datta, B.: Influence of Sea Level Rise on Multiobjective Management of Saltwater Intrusion in Coastal Aquifers, *Journal of Hydrologic Engineering*, 23, 10.1061/(asce)he.1943-5584.0001680, 2018.
- Sreekanth, J., and Datta, B.: Stochastic and Robust Multi-Objective Optimal Management of Pumping from Coastal Aquifers Under Parameter Uncertainty, *Water Resources Management*, 28, 2005-2019, 10.1007/s11269-014-0591-5, 2014.
- 545 Sreekanth, J., Moore, C., and Wolf, L.: Pareto-based efficient stochastic simulation—optimization for robust and reliable groundwater management, *Journal of Hydrology*, 533, 180-190, 10.1016/j.jhydrol.2015.12.001, 2016.
- Storn, R., and Price, K.: Differential evolution—a simple and efficient heuristic for global optimization over continuous spaces, *Journal of global optimization*, 11, 341-359, 10.1023/A:1008202821328, 1997.
- Werner, A. D., Bakker, M., Post, V. E. A., Vandenbohede, A., Lu, C., Ataie-Ashtiani, B., Simmons, C. T., and Barry, D. A.: Seawater intrusion processes, investigation and management: Recent advances and future challenges, *Advances in Water Resources*, 51, 3-26, 10.1016/j.advwatres.2012.03.004, 2013.
- 550 Westenbroek, S. M., Engott, J. A., Kelson, V. A., and Hunt, R. J.: SWB Version 2.0—A soil-water-balance code for estimating net infiltration and other water-budget components, *US Geological Survey*2328-7055, 2018.
- White, J. T.: A model-independent iterative ensemble smoother for efficient history-matching and uncertainty quantification in very high dimensions, *Environmental Modelling & Software*, 109, 191-201, 10.1016/j.envsoft.2018.06.009, 2018.
- 555 White, J. T., Foster, L. K., Fienen, M. N., Knowling, M. J., Hemmings, B., and Winterle, J. R.: Toward Reproducible Environmental Modeling for Decision Support: A Worked Example, *Frontiers in Earth Science*, 8, 10.3389/feart.2020.00050, 2020a.
- White, J. T., Hunt, R. J., Fienen, M. N., and Doherty, J. E.: Approaches to highly parameterized inversion: PEST++ Version 5, a software suite for parameter estimation, uncertainty analysis, management optimization and sensitivity analysis, *US Geological Survey*2328-7055, 2020b.
- 560 White, J. T., Knowling, M. J., Fienen, M. N., Siade, A., Rea, O., and Martinez, G.: A model-independent tool for evolutionary constrained multi-objective optimization under uncertainty, *Environmental Modelling & Software*, 149, 10.1016/j.envsoft.2022.105316, 2022.
- 565 Zhao, J., Lin, J., Wu, J., and Wu, J.: Impact of climate change on multi-objective management of seawater intrusion in coastal karst aquifers in Zhoushuizi district of Dalian City, China, *Hydrogeology Journal*, 29, 2329-2346, 10.1007/s10040-021-02383-3, 2021.