



1 **Influence of bank slope on sinuosity-driven hyporheic exchange flow and**
2 **residence time distribution during a dynamic flood event**

3

4 **Manuscript submitted to Hydrology and Earth System Sciences**

5

6 Yiming Li^{1,2}, Uwe Schneidewind², Zhang Wen^{1*}, Stefan Krause², Hui Liu¹

7

8 ¹Hubei Key Laboratory of Yangtze River Catchment Environmental Aquatic Science,
9 School of Environmental Studies, China University of Geosciences, People's
10 Republic of China

11 ²School of Geography, Earth and Environmental Sciences, University of Birmingham,
12 UK

13

14 ***Correspondence:** Zhang Wen (wenz@cug.edu.cn)



15 **Abstract.** This study uses a reduced-order two-dimensional (2-D) horizontal model to
16 investigate the influence of riverbank slope on the bank storage and sinuosity-driven
17 hyporheic exchange flux (HEF) along sloping alluvial riverbanks during a transient
18 flood event. The Deformed Geometry Method (DGM) is applied to quantify the
19 displacement of the sediment-water interface (SWI) along the sloping riverbank
20 during river stage fluctuation. This new model approach serves as the initial step to
21 consider complicated floodplain morphologies in physics-based models for better
22 predictions of HEF. Several controlling factors, including sinuosity, alluvial valley
23 slope, and river flow advective forcing and duration of flow are incorporated in the
24 model to investigate the effects of bank slope in aquifers of variable hydraulic
25 transmissivity. Compared to simulations of a vertical riverbank, sloping riverbanks
26 were found to increase the HEF. For sloping riverbanks, the hyporheic zone (HZ)
27 encompassed a larger area and penetrated deeper into the alluvial aquifer, especially
28 in aquifers with smaller transmissivity (i.e., larger aquifer hydraulic conductivity or
29 smaller specific yield). Furthermore, consideration of sloping banks as compared to a
30 vertical river bank can lead to both underestimation or overestimation of the pore
31 water residence time. The impact of bank slope on residence time was more
32 pronounced during a flood event for high transmissivity aquifer conditions, while it
33 had a long-lasting influence after the flood event in lower transmissivity aquifers.
34 Consequently, this decreases the residence time of HEF relative to the base flow
35 condition. These findings highlight the need for (re)consideration of the importance of
36 more complex riverbank morphology as control of hyporheic exchange in alluvial
37 aquifers. The results have potential implications for river management and restoration
38 and the management of river and groundwater pollution.

39

40 **Key words:** hyporheic exchange, sloping riverbank, transient river stage, peak flow
41 event, residence time distribution

42



Nomenclature

ΔL	Nodal spacing [m]
∇	Laplace operator
α_L	Longitudinal dispersivity [L]
α_T	Transverse dispersivity [L]
\mathbf{D}	Dispersion-diffusion tensor [L^2T^{-1}]
D_L	Water diffusivity [L^2T^{-1}]
J_x	Base groundwater gradient [-]
K	Hydraulic conductivity [LT^{-1}]
n	Scaling number [-]
n_0	Intensity of flood event [-]
n_d	Skewness of flood event [-]
S_y	Specific yield [-]
t_d	Duration of flood event [T]
t_p	Time to peak river stage [T]
α	Amplitude of the river boundary [L]
Γ_d	Dimensionless aquifer transmissivity [-]
δ	Bank slope angle [$^\circ$]
δ_{ij}	Kronecker delta function [-]
ϵ	Tortuosity [-]
η	Degree of flood event asymmetry [T^{-1}]
θ	Effective porosity [-]
λ	River boundary wave length [L]
σ	River boundary sinuosity [-]
τ	Residence time [T]
ω	Flood event frequency [T^{-1}]
$h(\mathbf{x}, t)$	Transient groundwater head [L]
Δh^*	Dimensionless parameter of ambient groundwater flow [-]



$A^{**}(t)$	Dimensionless variation of HZ area relative to base flow conditions [-]
$C(\mathbf{x}, t)$	Solute concentrations in the aquifer [ML ⁻³]
$C_0(\mathbf{x})$	Solute concentrations in initial condition [ML ⁻³]
$C_s(\mathbf{x}, t)$	Solute concentrations in the river [ML ⁻³]
$d^{**}(t)$	Dimensionless variation of HZ penetration distance relative to base flow conditions [-]
$H(\mathbf{x}, t)$	Thickness of the saturated aquifer [L]
$H_0(\mathbf{x})$	Initial river stage [L]
H_p	Peak river stage during the flood event [L]
$H_r(t)$	River stage at the downstream end [L]
$h_r(x, t)$	Transient river stage [L]
$M(t)$	Displacement of the sediment-water interface [L]
P_e	Péclet number [-]
\mathbf{q}	Specific discharge or Darcy flux [LT ⁻¹]
\mathbf{Q}	Aquifer-integrated discharge [L ² T ⁻¹]
$Q_{in, HZ}^*(t)$	Dimensionless net flux along the river boundary [-]
$Q_{in, HZ}^*(t)$	Dimensionless exchange flux from the aquifer to the river [-]
$Q_{out, HZ}^*(t)$	Dimensionless exchange flux from the river to the aquifer [-]
$Y(x, t)$	Location of the sediment-water interface boundary [L]
$z_b(\mathbf{x})$	Elevation of the underlying impermeable layer [L]
Γ_d	Dimensionless parameter of aquifer transmissivity [-]
$\mu(\mathbf{x}, 0)$	Mean (first order of) residence time distribution [T]
$\mu_{out}^*(x, t)$	Flux-weighted ratio of mean RT to mean RT under baseflow conditions [-]
$\mu_n(\mathbf{x}, t)$	n -th moment of residence time distribution [T ^{n}]
$\mu_r^*(\mathbf{x}, t)$	Residence time distribution ratio between slope and vertical river bank model [-]
$\mu_{\tau 0-\max}$	Maximum RT in the domain [T]



$\mu_{\tau,s}(\mathbf{x}, t)$	Residence time distribution of slope river bank model [T]
$\mu_{\tau,v}(\mathbf{x}, 0)$	Residence time distribution of vertical river bank model [T]
$\rho(\mathbf{x}, t, \tau)$	Residence time distribution [T]

Abbreviations

HZ	Hyporheic zone
HEF	Hyporheic exchange flux
DGM	Deformed Geometry Method
SWI	Sediment-water interface
RTD	Residence time distribution
RT	Residence time
ALE	Arbitrary Lagrangian–Eulerian
2-D	Two-dimensional

43

44



45 1. Introduction

46 The hyporheic zone (HZ) can be described as the region that connects the river
47 channel and adjacent aquifer, and includes riverbed and riverbanks. Mixing of
48 different water types (groundwater, surface water) and ages in the HZ causes spatially
49 and temporally varying exchange of water, biogeochemical species, and energy
50 between river channel, riverbed and aquifer (Cardenas, 2009b; Hester and Gooseff,
51 2010; Krause et al., 2011, 2017, 2022; McClain et al., 2013; Boano et al., 2014).
52 Hyporheic exchange flow in vertical (e.g., bedform-driven) and horizontal (e.g.,
53 meander-driven) domains can add to general regional groundwater upwelling or
54 downwelling, with HEF representing those surface flow components that penetrate
55 and transport through the hyporheic sediment and back into the stream. The
56 distribution of hyporheic flow paths strongly determines the spatial and temporal
57 distribution of biochemical characteristics of water within the riverbed and the wider
58 river corridor as well as the formation of so-called hot zones and hot moments
59 (Krause et al., 2013, 2017; Cardenas, 2015; Pinay et al., 2015).

60 Hyporheic exchange flux (HEF) is controlled by parameters such as stream
61 discharge dynamics, recharge, riverbed and aquifer hydraulic properties, local
62 pressure head fluctuations, and river geometry and morphology including sinuosity
63 and riverbank slope (Larkin and Sharp, 1992; Gomez-Velez et al., 2012; 2017;
64 Schmadel et al., 2016). For example, Cardenas et al. (2004) demonstrate how riverbed
65 characteristics and especially heterogeneity could increase the hyporheic exchange
66 intensity by 17% to 32%. As such, to be able to better estimate the relative importance
67 of HEF on catchment water fluxes and biogeochemistry requires a good
68 understanding of the interactions of its different drivers and controls. This is
69 imperative as the spatiotemporal evolution of HEF paths, the resulting change in HZ
70 extent (area) and thus also the mean residence time (RT) of the exchanged water in
71 the HZ have significant impact on flow dynamics and transient storage along the river



72 continuum and in turn control attenuation capacity (Weatherill et al., 2018) and
73 biogeochemical functions of river corridors (Bertrand et al., 2012; Boulton et al., 2010;
74 Brunke and Gonser, 1997).

75 Both lateral exchange between river and flood-plain, as well as
76 bedform-induced vertical exchange at the streambed interface have been found to be
77 crucial with regards to HEF and the biogeochemical transformation potential along
78 the river corridor (Boano et al., 2010, 2014; Gomez-Velez and Harvey, 2014;
79 Gomez-Velez et al., 2015, 2017; Kiel and Cardenas, 2014; Stonedahl et al., 2013).
80 Considerable progress has been made in our understanding of how river platform
81 geometry (Boano et al., 2006, 2010; Cardenas 2006; 2008; 2009a, 2009b; Stonedahl
82 2013), dynamic flood events (Gomez-Velez et al., 2012; 2017) and evapotranspiration
83 (Kruegler et al., 2020) control HEF. Focusing on lateral exchange flow processes,
84 Cardenas (2008; 2009a, 2009b) developed numerical models to investigate HEF and
85 residence time distribution (RTD) for various river channel morphologies and regional
86 groundwater flow conditions. Their simulations indicate that channel morphology,
87 represented by sinuosity, is a dominant factor controlling HEF, the total HZ area, and
88 RTD. In addition, Boano et al. (2010) used a similar modeling framework to study the
89 relationship between RTD and biogeochemical transformation by introducing surface
90 water as a major source of dissolved organic matter that triggers a sequence of redox
91 reactions within the HZ. Reactive transport simulations showed a good relationship
92 between RTD and denitrification reaction potential. Based on these studies,
93 Gomez-Velez et al. (2012) conducted numerical simulations to investigate the impact
94 of aquifer parameters (water table gradient, hydraulic conductivity, dispersivity) and
95 channel sinuosity on HEF and RTD. By comparing RTD with the timescale of nitrate
96 forming or reducing reactions, a meander can be classified as a source or sink of
97 nitrate for (de)nitritification activities. More recent modeling studies have focused
98 predominantly on the effects of dynamic river/groundwater stage fluctuations on
99 lateral (e.g., Schmadel et al., 2016; Gomez-Velez et al., 2017) and vertical (e.g., Singh



100 et al., 2019, 2020; Wu et al., 2018, 2020, 2021) hyporheic exchange and RTD. For
101 example, Gomez-Velez et al. (2017) explored the HZ response to a dynamic river
102 stage under different parameter values for hydraulic conductivity, river stage during
103 flood events, groundwater gradient and river sinuosity conditions. Their results
104 indicate that the dynamic forcing greatly influences net HEF, the area of HZ and RTD
105 across different scenarios, whereby higher aquifer transmissivity will likely result in a
106 stronger but shorter response of HEF and RTD to a flood event.

107 Although there is a considerable body of numerical research on the lateral
108 hyporheic response to the various geometrical (e.g., geometry of river channel, river
109 slope, etc) and dynamic drivers (e.g., fluctuation of river/groundwater, gaining and
110 losing conditions of groundwater, etc), many HZ studies do not specifically consider
111 floodplain-driven processes or they apply vertical riverbanks with straight river
112 planimetry in an attempt to reduce model complexity in line with the analytical or
113 numerical solutions used (Cooper and Rorabaugh, 1963; Hunt, 1990; Schmadel et al.,
114 2016; Gomez-Velez et al., 2017;). However, riverbanks are usually tilted rather than
115 vertical (Liang et al., 2018) as they undergo erosion (Osma and Thorne, 1988).
116 Previous research has proven that bank erosion and bank collapse are globally
117 spreading processes controlled by various factors, such as initial bank slope angle
118 (Zingg, 1940; Lindow et al., 2009), surface flow forces (Hagerty et al., 1995; Fox and
119 Wilson, 2010), vegetation cover (Mayor et al., 2008; Gao et al., 2009; Puttock et al.,
120 2013) and sediment properties (Millar and Quich, 1993). Neglecting bank slope in
121 analytical and numerical model solutions may therefore have a significant influence
122 on the prediction accuracy of HEF (Doble et al. 2012a, 2012b) and RTD (Derx et al.,
123 2014; Siergieiev et al., 2015). Thus, a detailed analysis of the floodplain drivers of
124 HEF should require a more detailed consideration of the floodplain geometry
125 including riverbank slope in bank storage conceptual models (Sharp, 1977).

126 Few previous studies have used numerical modeling where the model is
127 bounded by a sloping riverbank to assess the influence of bank slope on HEF for a



128 vertical section of an alluvial aquifer. In such cases, the aquifer was considered
129 variably saturated, homogenous, and isotropic, while flow in the unsaturated zone was
130 calculated using the Richards equation (Li et al., 2008; McCallum et al., 2010; Doble
131 2012a; b). These studies have confirmed that neglecting bank slope can lead to an
132 underestimation of the bank storage volume as well as the temporal HEF in vertical
133 cross-sectional profiles, especially under relatively small bank angles.

134 In turn, river sinuosity and ambient groundwater gradient (along the river
135 channel) have not been studied as potential drivers of sinuosity-driven lateral HEF
136 and RTD and their biogeochemical implications under complex riverbank
137 morphological conditions and it needs to be determined whether considering both
138 drivers can lead to significantly different findings as compared to previous
139 cross-sectional profile models (Doble et al., 2012; Siergieiev et al., 2015; Derx et al.,
140 2014). In this study, we therefore quantify the effect of bank slope on the simulated
141 spatial extent (area) of the HZ in sinuosity-driven river meanders and how it impacts
142 the evolution of HEF and RTD under varying aquifer transmissivity conditions to
143 better understand lateral HEF through the alluvial plain. We build on the numerical
144 model introduced by Gomez-Velez et al. (2017) and consider lateral bank slope by
145 using a deformed geometry method (DGM) approach. For this, we couple DGM with
146 the Boussinesq equation, the vertically integrated solute transport equation and
147 residence time distribution equation to study HEF. Our results will help to reveal the
148 importance of bank slope for the prediction of HEF and RTD in sinuosity-driven
149 meandering rivers.

150



151 **2. Methodology**

152 **2.1 Model setup with deformed geometry method**

153 Our modeling approach builds on the work of Gomez-Velez et al. (2017), who
154 developed a comprehensive simulation tool in dimensionless form that can represent
155 most riverbank-aquifer situations and dynamic flood conditions. In our study, we use
156 their model as a baseline with the same equations and metrics. Additional information
157 regarding implementation of this baseline model can be found in the SI and
158 Gomez-Velez et al. (2017). However, where Gomez-Velez et al. (2017) assume a
159 vertical riverbank, we consider a sloping riverbank and use the DGM approach to
160 capture the dynamic evolution of the SWI along the river course. A constant sloping
161 angle (δ [°]) along the alluvial riverbank of a sinusoidal river was implemented in our
162 model (see blue lines of conceptual model in Figure S1 and the corresponding
163 mathematical model in Figure S2a) while the SWI was assumed to be always vertical
164 (vertical solid red and green lines in Figure S2c). As such, the contraction or
165 expansion of the simulated domain, i.e., displacement of the SWI can be characterized
166 by the sloping angle (there is no movement of the SWI for the vertical riverbank case)
167 and river stage. As the river stage changes, so does the location of the SWI.

168 When the river stage changes in our model, the sinusoidal boundary will
169 migrate towards or away from the floodplain meaning that the submerged part of the
170 riverbank is considered contracted and our model only considers the alluvial aquifer
171 that is not submerged. The evolution of the SWI during a flood event can be
172 calculated by considering river stage and bank slope via:

173
$$Y(x, t) = Y_0(x) + M(t) \tag{1}$$

174 where $Y(x, t)$ [L] is the location of the SWI boundary; $Y_0(x)$ [L] is the initial location
175 of the SWI. In contrast to Gomez-Velez et al. (2017), the displacement of the SWI



176 caused by the deformation of the model domain ($M(t) = [h(t) - h(0)]/\tan(\delta)$, where $h(t)$
177 [L] is transient hydraulic head) is added in Eq. (1), which represents the displacement
178 of the river boundary in y -direction due to river stage fluctuation and bank slope angle
179 (see the horizontal distance between the vertical red and green solid line in Figure
180 S2c).

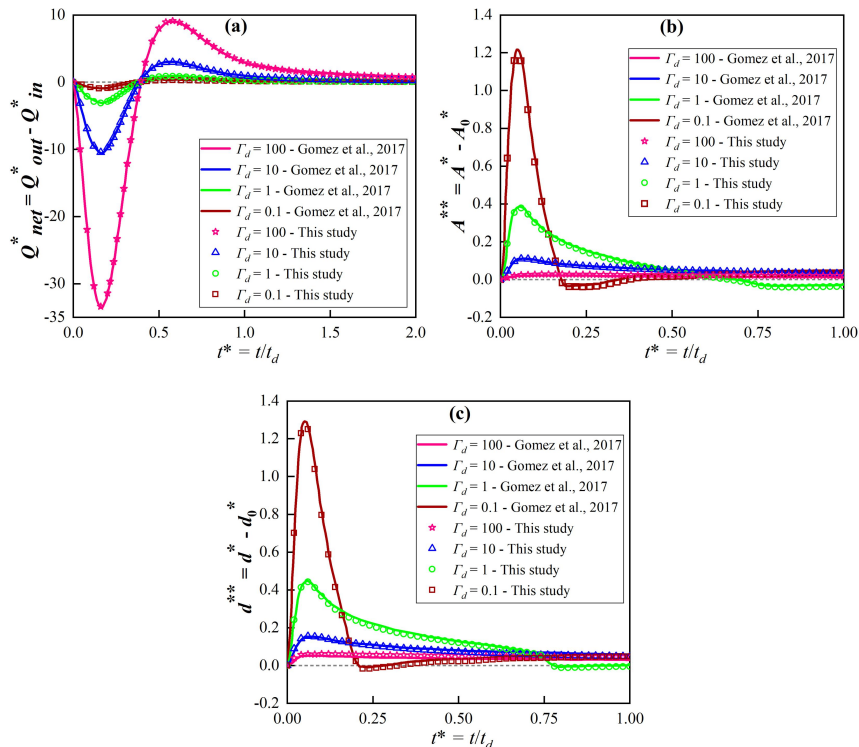
181 To simulate the model domain deformation and mesh displacement, we use the
182 DGM interface in COMSOL. In this interface, the deforming feature of a specified
183 domain can be defined as a boundary condition with a given moving velocity or
184 displacement. DGM is based on the arbitrary Lagrangian–Eulerian (ALE) method,
185 which is a hybrid method that allows both the model domain and mesh to move or
186 deform simultaneously in a predefined manner. More details on ALE can be found in
187 Donea et al. (2014). While it has previously been used for simulating general
188 free-surface problems (e.g., Duarte et al., 2004; Maury, 1996; Pohjoranta and Tenno,
189 2011), to our knowledge, DGM has not yet been implemented to solve moving
190 boundary problems in hyporheic exchange studies. Here we used Eq. (1) as an input
191 to the DGM interface to simulate the displacement of the SWI (water flow) during a
192 dynamic flood event. Infiltration and seepage face before and after the peak time of
193 the flood event, respectively, were neglected. Additionally, solute transport and RTD
194 were simulated based on the extent of the flow field according to Gomez-Velez et al.
195 (2017), as shown in the SI.

196 2.2 Model parameterization, testing and scenarios

197 Model hydraulic conditions used in our numerical modeling study are based on
198 values from Gomez-Velez et al. (2017), who conducted a Monte Carlo analysis. They
199 found that the dynamic variations of HEF and RTD are mainly determined by ambient
200 groundwater flow (referred to as dimensionless parameter $\Delta h^* = \frac{J\lambda^2}{0.5(1+n_0)H_0}$, see Table 1)
201 and the ratio of aquifer hydraulic conductivity to the duration of the flood event



(referred to as dimensionless constant $\Gamma_d = \frac{S_y \lambda_z}{0.5K(1+n_0)H_0 t_d}$, see Table 1). After setting up the original model of Gomez-Velez et al. (2017) as a baseline case ($\delta = 90^\circ$), we compared our model results for that case with those obtained by Gomez-Velez et al. (2017) for (a) net HEF represented by $Q_{net, HZ}^*(t)$; (b) area of HZ, $A^{**}(t)$; (c) penetration of the HZ, $d^*(t)$ in $\Gamma_d = 0.1, 1, 10$ and 100 , and found that our model simulated those cases with high accuracy (Fig. 1). Parameters $A^{**}(t)$ and $d^*(t)$ are based on modeling the transport of a conservative solute while $Q_{net, HZ}^*(t)$ is based on modeling water flow. Slight differences between our model and that of Gomez-Velez et al. (2017) might be due to the use of a much more refined mesh in this study and different length scales.



213

214

215 **Figure 1.** Comparison of results obtained in this study with those of Gomez et al.
 216 (2017) for the baseline case with a vertical river bank and variable Γ_d : (a) net



217 hyporheic exchange flux represented by $Q_{net, HZ}^*(t)$; (b) extent of the hyporheic zone
218 $A^{**}(t)$ and (c) penetration distance $d^*(t)$ of the hyporheic zone into the alluvial valley.
219 A more refined mesh and different length scales used in this study, can explain
220 occasional slight differences between our model and that of Gomez et al. (2017)
221 might occur. Information regarding model fits can be found in the SI.

222

223 We then considered a series of riverbank scenarios where the bank slope angle
224 ranged from $\delta = 90^\circ$ (vertical riverbank) to 10° (nearly horizontal case) and Γ_d values
225 ranged from 0.1 to 100, (corresponding to aquifer hydraulic conductivity ranging
226 from 480 to 0.048 m/d, indicating high to low transmissivity. Table 1 presents the
227 parameters used in our numerical modeling study. The finite-element models
228 proposed in this study were developed using the COMSOL Multiphysics (COMSOL)
229 software. Eq. (S1), Eq. (S3) and Eq. (S6) were implemented by customizing a PDE
230 interface to include the Boussinesq, vertical integrated solute transport and RTD
231 equation, respectively. The model domain was discretized into about 0.5 million
232 variably-sized triangular elements, with refinement imposed near the river boundary.
233 Mesh-independent numerical solutions are achieved by limiting grid size (ΔL) to less
234 than 0.2 m. Thus, the transverse and longitudinal Peclet numbers (calculated by $P_e =$
235 $\Delta L/\alpha_L$ and $P_e = \Delta L/\alpha_T$, respectively) in both advection and diffusion dominated zones
236 are less than 1, which is smaller than the upper limit of $P_e = 4$ to effectively avoid
237 numerical oscillations and instabilities.

238

239 **Table 1.** Parameters and values used in our numerical model simulations (adopted
240 from Gomez-Velez et al. (2017)).

Parameters	Value	Description
Constant model parameters		
S_y	0.3	Specific yield [-]
λ	40	River boundary wave length [L]



α	5	River boundary amplitude [L]
θ	0.3	Efficient porosity [-]
J_x	0.0025	Base groundwater gradient [-]
σ	1.14	River boundary sinuosity [-]
t_d	10	Duration of flood event [T]
n_d	0.25	Skewness of flood event [-]
t_p	$n_d t_d$	Time to peak river stage [T]
H_0	1	Base river stage [L]
n_0	1	Intensity of flood event [-]
α_L	2	Longitudinal dispersivity [L]
α_T	$0.1 \alpha_L$	Transverse dispersivity [L]
Varied model parameters		
Γ_d	0.1 1 10 100	Dimensionless aquifer transmissivity [-]
δ	90 70 50 20 10	Bank slope angle [°]

241

242



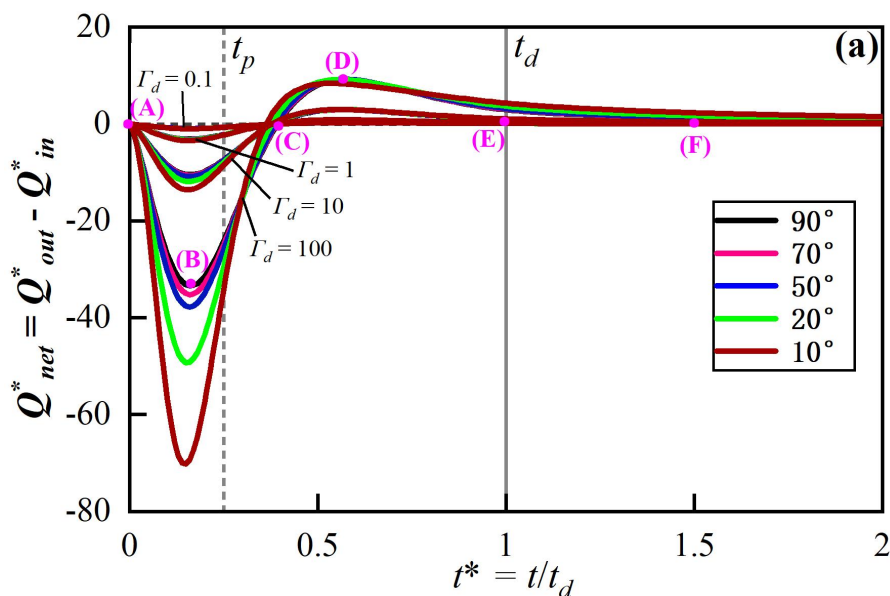
243 **3. Results**

244 **3.1 Effect of bank slope on hyporheic exchange flow and HZ patterns**

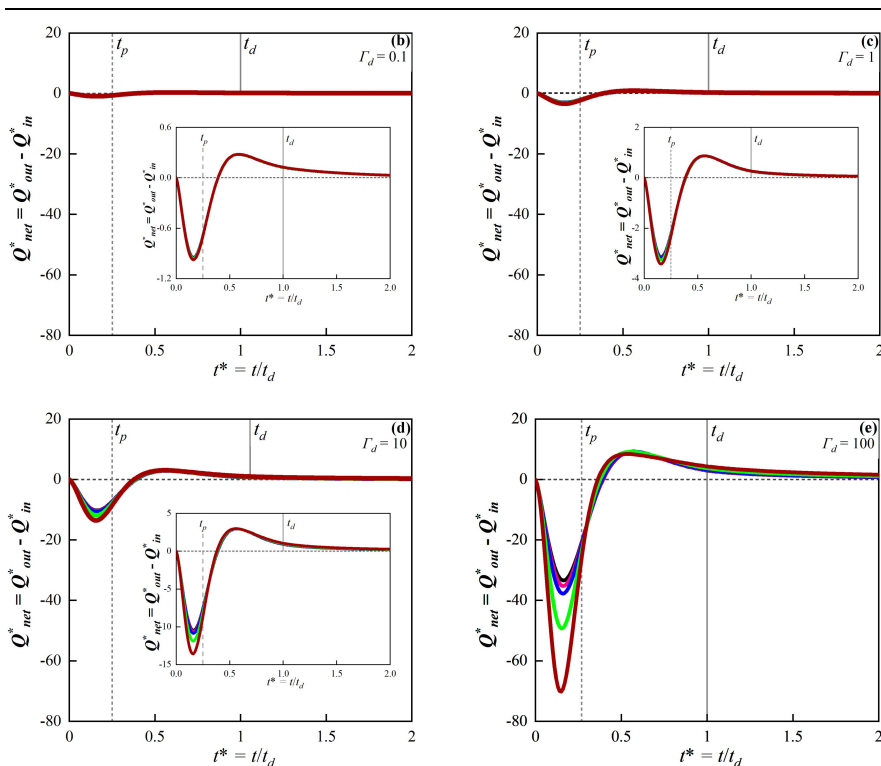
245 **3.1.1 Hyporheic exchange flow**

246 The flow field (velocity magnitude and direction) and net HEF ($Q_{net, HZ}^*(t)$)
247 changed dynamically during and after the simulated flood event. Fig. 2a shows a
248 comparison of $Q_{net, HZ}^*(t)$ values for different values of δ and Γ_d . In order to illustrate
249 the influence of δ on $Q_{net, HZ}^*(t)$ under different Γ_d conditions more clearly, Fig. 2b -
250 2e highlight the $Q_{net, HZ}^*(t)$ evolution for a given Γ_d at smaller scale. Snapshots of the
251 flow field and the boundary of the HZ area (isolines of $C(\mathbf{x}, t) = 0.5$ as concentration
252 of a conservative solute) for different δ conditions at different times (pink dots in Fig.
253 2a) for $\Gamma_d = 1$ are shown in Fig. 3a - 3f.

254



255

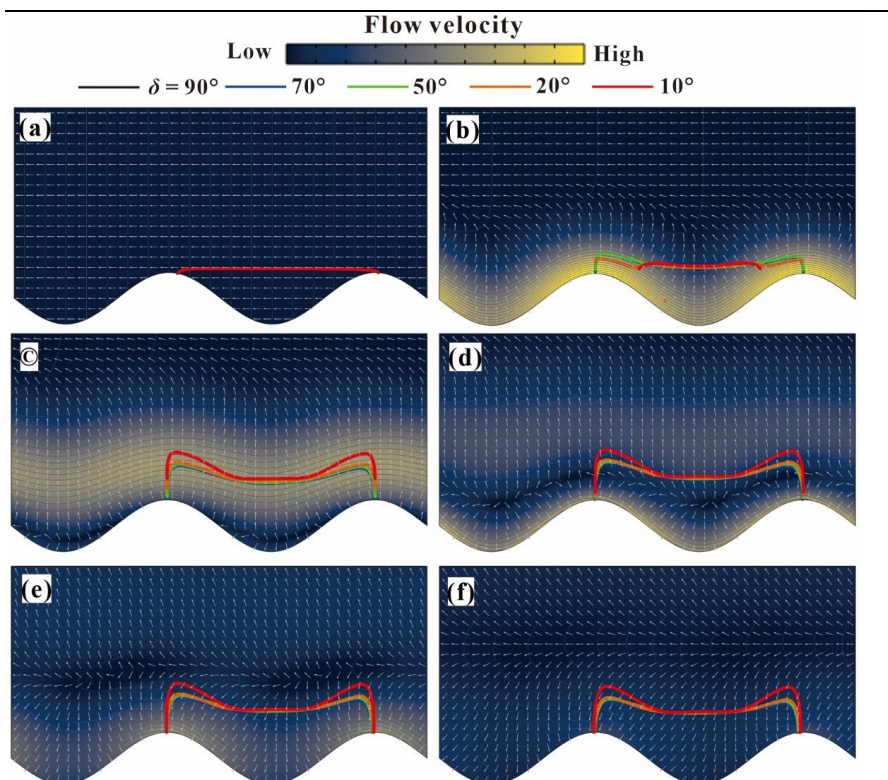


256

257

258 **Figure 2.** (a) Temporal evolution of dimensionless net flux for alternative values of Γ_d
 259 and δ (colored lines). The results for each Γ_d condition from 0.1 to 100 and different
 260 slopes are shown again in Fig. 2b - 2e separately, to represent smaller-scales. In each
 261 figure, time-to-peak (t_p) and flood duration (t_d) are marked by vertical dashed lines.
 262 Pink dots in (a) marked by (A) - (F) correspond to the snapshots of the flow field
 263 shown in Fig. 3. A negative flux value here represents water flow from river to
 264 aquifer.

265



266
267 **Figure 3.** Temporal evolution of the alluvial flow field and spatial extent of the HZ.
268 Snapshots of the flow field at different time steps during the simulated event (pink
269 dots in Fig. 2a). Colored surfaces represent the magnitude of the Darcy flux vector
270 (blue is low and yellow is high) and white isolines the dimensionless hydraulic head.
271 Bold colored lines correspond to the HZ extent for different bank slope conditions.

272

273 Before the flood event ($t = 0$), steady state base flow conditions are assumed, as
274 shown in Fig. 3a. The inflow and outflow (along the upstream and downstream
275 meander bend, respectively) are in balance. The HZ boundaries for different δ
276 conditions in Fig. 3a are the same before the flood event because the bank slope has
277 no influence on the flow field and HZ extent. The onset of the flood event is indicated
278 by the rising river stage and forces the river to infiltrate into the aquifer along the SWI
279 (negative values of $Q_{net, HZ}^*(t)$ in Fig. 2), resulting in the expanded HZ as shown in

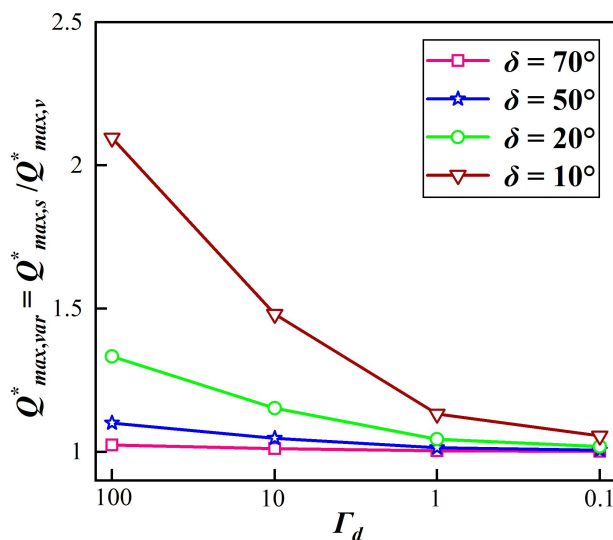


280 Fig. 3b. The influx of river water into the HZ ($-Q_{net, HZ}^*(t)$) reaches its maximum
281 before the time-to-peak river stage ($t = 0.25t_d$) because the pressure wave propagates
282 into the aquifer and decreases the head gradient between the river and the connected
283 aquifer. An aquifer with larger Γ_d limits the propagation of the pressure wave due to
284 the low transmissivity, which leads to a larger head gradient near the SWI. This,
285 consequently, leads to larger dimensionless net fluxes under increasing Γ_d conditions.

286 The maximum dimensionless flux ratios $Q_{max, var}^* = Q_{max, s}^* / Q_{max, v}^*$ of sloping (δ
287 $< 90^\circ$, $Q_{max, s}^*$) and vertical ($\delta = 90^\circ$, $Q_{max, v}^*$) riverbank cases are shown in Fig. 4. The
288 bank slope is found to increase the infiltration flux by up to 120% ($Q_{max, var}^* \approx 2.2$) for
289 $\Gamma_d = 100$ with $\delta = 10^\circ$ while for larger slope angles or smaller Γ_d the dimensionless
290 infiltration flux gradually decreases. This is because aquifers with smaller Γ_d (higher
291 hydraulic transmissivity) are more sensitive to river stage variation and have a strong
292 ability to transmit the pressure wave into the aquifer. In such cases, the influence of δ
293 on the net flux becomes less important. On the other hand, a smaller δ induces a
294 longer displacement of the SWI ($M(t)$) away from the river, where the groundwater
295 head adjacent to the SWI is always relatively low (i.e., the head in base flow
296 condition).

297

298



299

300 **Figure 4.** Ratio of maximum negative net flux of slope to no-slope (vertical river
 301 bank) conditions $Q^*_{max,var} = Q^*_{max,s} / Q^*_{max,v}$, and aquifer transmissivities. The ratios of
 302 alternative slope condition are marked by different symbols and colors.

303

304 As the river stage decreases after t_p , the head gradient near the SWI gradually
 305 reverses and the net outflux starts increasing (the river is gaining water). This is
 306 associated with the river stage declining below the groundwater level (see Fig. 3c - 3f).
 307 Fig. 2 shows that the bank slope has little impact on the net outflux. Where $\Gamma_d = 100$,
 308 bank slope can slightly extend the time required for the system to recover to initial
 309 condition after t_p but in general, the response of the net outflux to bank slope is
 310 negligible when compared to that of the influx. Eventually, the net flux converges to
 311 zero, which indicates the flow field within the aquifer recovers to the initial
 312 conditions.

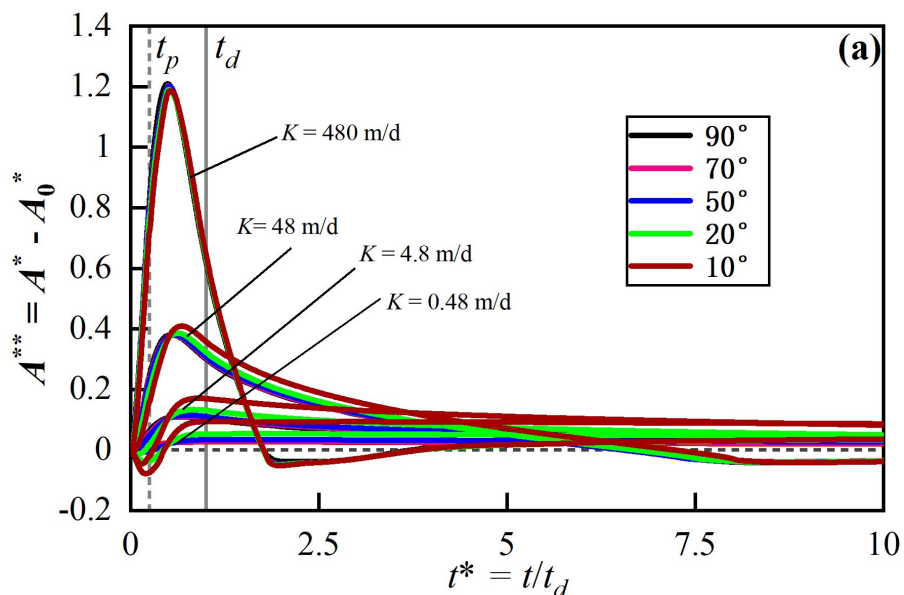
313 3.1.2 Patterns of hyporheic area and penetration distance

314 Fig. 5a and Fig. 6a show the temporal evolution of the HZ area ($A^{**}(t)$) and
 315 penetration distance ($d^{**}(t)$) into the alluvial valley relative to the initial condition for

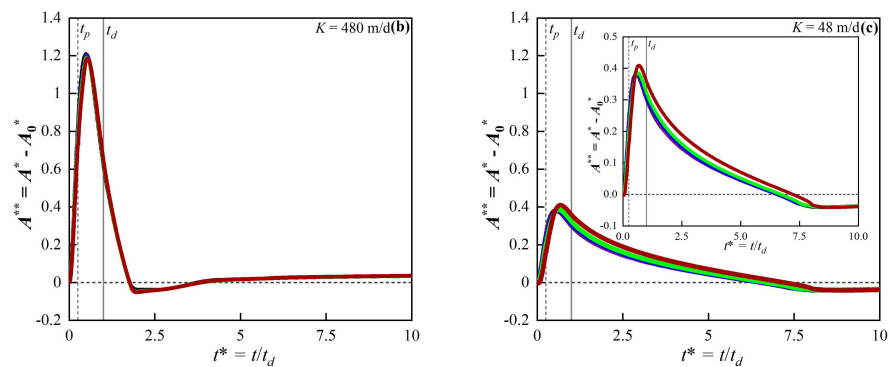


316 varying Γ_d and slope angles, while Fig. 5b – 5e and Fig. 6b – 6e illustrate the impact
 317 of δ on $A^{**}(t)$ and $d^{**}(t)$ for different values of Γ_d in a close-up.

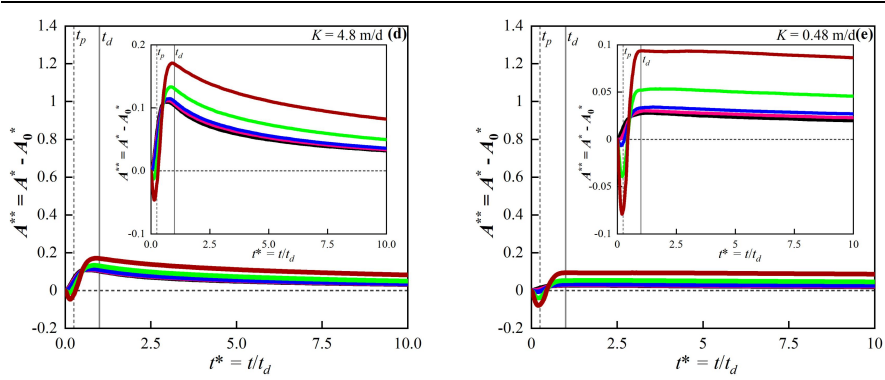
318



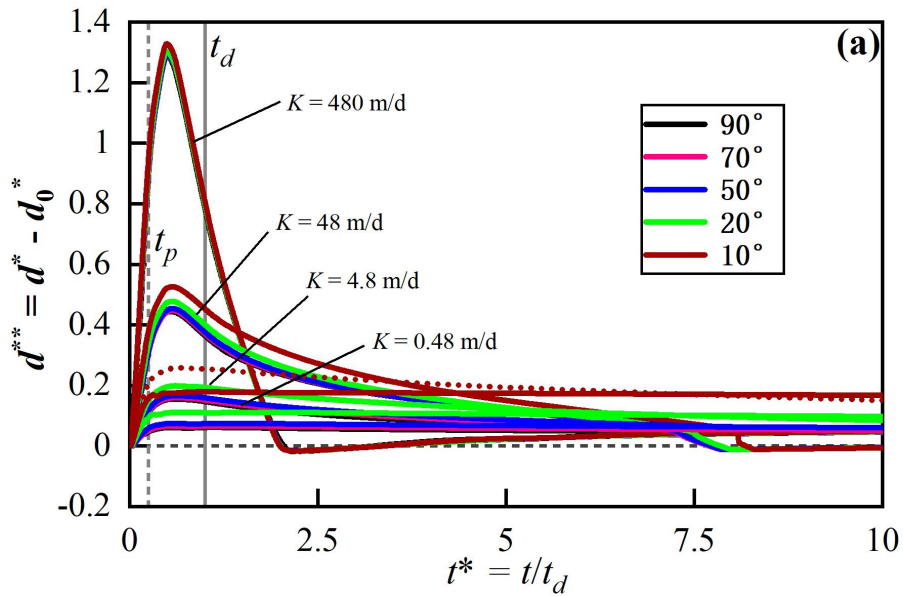
319



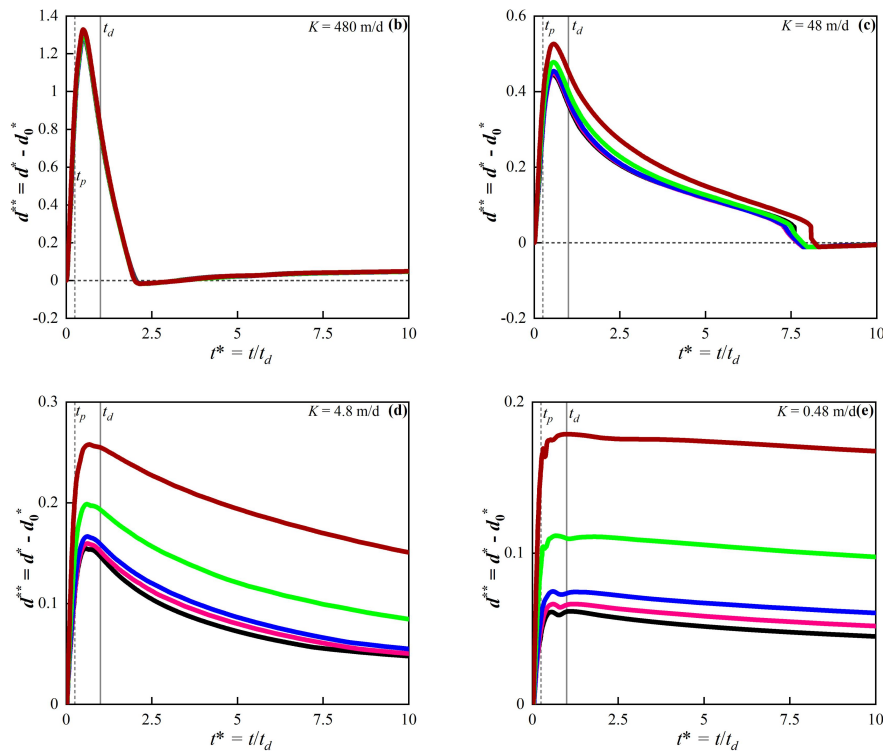
320



321
 322 **Figure 5.** (a) Temporal evolution of HZ area for different values of Γ_d and δ (colored
 323 lines). For clarity, the results for each Γ_d condition from 0.1 to 100 are shown again
 324 separately in (b) to (e), with inserts representing smaller scales.
 325



326



327

328

329 **Figure 6.** (a) Temporal evolution of HZ penetration distance into the alluvial valley
 330 for alternative values of Γ_d and δ (color lines). For clarity, the results for each Γ_d
 331 condition from 0.1 to 100 are shown again in (b) to (e), with inserts representing
 332 smaller scales.

333

334 For vertical banks ($\delta = 90^\circ$, grey lines in Fig. 5), $A^{**}(t)$ increases synchronously
 335 with the river stage ($t < t_p$). After the peak time of the flood event ($t > t_p$), $A^{**}(t)$
 336 continues to rise due to the water in the river still discharging into the aquifer.
 337 Furthermore, the groundwater mound continues to expand, migrating into the aquifer
 338 (see the more penetrated groundwater mound from in Fig. 3b vs Fig. 3c). After the
 339 flood event ($t > t_d$), the river water that was stored in the aquifer ($C(x, t) > 0$) slowly
 340 discharges back into the river channel. Thus, the HZ area and penetration distance
 341 gradually rebound to initial conditions.



342 Under sloping riverbank conditions, the riverbank will at times be submerged
343 by the rising river stage. Fig. 5b and 6b show that the effects of bank slope on $A^{**}(t)$
344 and $d^{**}(t)$ are almost counteracted by the high transmissivity of the aquifer and the
345 influence of bank slope on HZ area and penetration distance is negligible. At the
346 beginning of the flood event, Fig. 5c - 5e show that for conditions with smaller δ ,
347 $A^{**}(t)$ can be less than zero (HZ at these times are smaller than the initial condition).
348 This is due to the fact that the movement of the SWI during a rising river stage
349 towards the alluvial valley will submerge parts that were previously unsaturated as the
350 aquifer with low transmissivity will propagate water more slowly. As Γ_d increases
351 from Fig. 5d - 5e, smaller values of A^{**} were observed that stay negative for a longer
352 time for smaller bank slopes δ . This indicates that the bank slope has a more
353 significant effect on HZ area in cases where Γ_d is large as a low-transmissivity aquifer
354 takes more time to propagate infiltrating river water.

355 After about half of the flood duration ($t > 0.5t_d$), all of $A^{**}(t)$ becomes positive
356 due to the re-emergence of the model domain submerged during the flood event. As Γ_d
357 increases from Fig. 5b - 5e and from Fig. 6b - 6e, the impact of δ gradually emerges
358 especially in larger Γ_d condition, whereby smaller δ can increase the peak values of
359 $A^{**}(t)$ and $d^{**}(t)$, and delay the arrival time of the maximum value of $A^{**}(t)$. After the
360 flood event ($t > t_d$), the effect of bank slope is counteracted by the higher aquifer
361 transmissivity and only for large transmissivities has a significant impact on the HZ
362 resulting in larger $A^{**}(t)$ and $d^{**}(t)$ as shown in Fig. 5c - 5e and Fig. 6c - 6e.

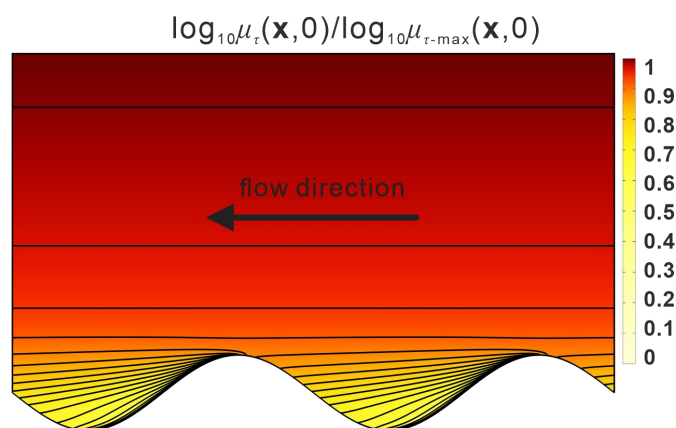
363 3.2 Spatiotemporal evolution of mean residence time distribution

364 The evolution of spatiotemporal patterns of mean RTD is a useful evaluation
365 method for identifying the dynamic variation of aging and rejuvenation of hyporheic
366 water. Here we use the mean RT ratio between a sloping model and a vertical model
367 $\mu_r^*(\mathbf{x}, t) = \log_{10}(\mu_{r-s}(\mathbf{x}, t)/\mu_{r-v}(\mathbf{x}, 0))$ to evaluate the influence of bank slope on the
368 predicted RTD for a given location and time. Fig. 7 presents RTDs for the initial



369 condition, where $\mu_{t_0-\max}$ is the maximum RT in the domain. It can be seen that the
370 isolines representing the RT are almost horizontal in the area extending from the river
371 but RT near the upstream river bend is smaller than downstream because the initial
372 flow direction is towards the negative direction of the x axis. Notably, $\mu(\mathbf{x}, 0)$ grows
373 almost exponentially as y increases, and a positive correlation to Γ_d at a given location
374 is observed.

375



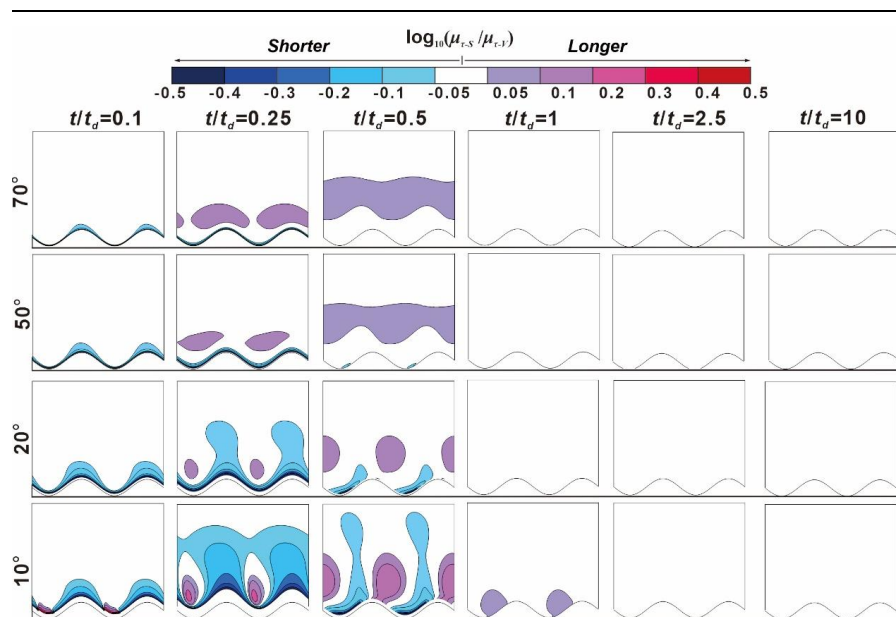
376

377 **Figure 7.** Relative mean residence time distributions [-] for baseline flow conditions
378 (no slope), which are represented by $\log_{10}\mu_t(\mathbf{x}, 0)/\log_{10}\mu_{t-\max}(\mathbf{x}, 0)$ to show the
379 distribution pattern. The value of the contour lines grows exponentially with the
380 distance from the river meander.

381

382 Fig. 8 - 11 present snapshots of μ_r^* for different bank slopes for $\Gamma_d = 0.1, 1, 10$
383 and 100, respectively, at the rising limb of the flood event ($t/t_d = 0.1$), the peak of
384 flood event ($t/t_d = 0.25$), the falling limb of flood ($t/t_d = 0.5$) and after the flood event
385 ($t/t_d = 1, 2.5$ and 10). The RT difference between sloping and vertical riverbank
386 models are within 12.2% in the white-colored areas ($-0.05 < \mu_r^* < 0.05$) of Fig. 8 - 11,
387 which indicates a minor effect of bank slope on RTD.

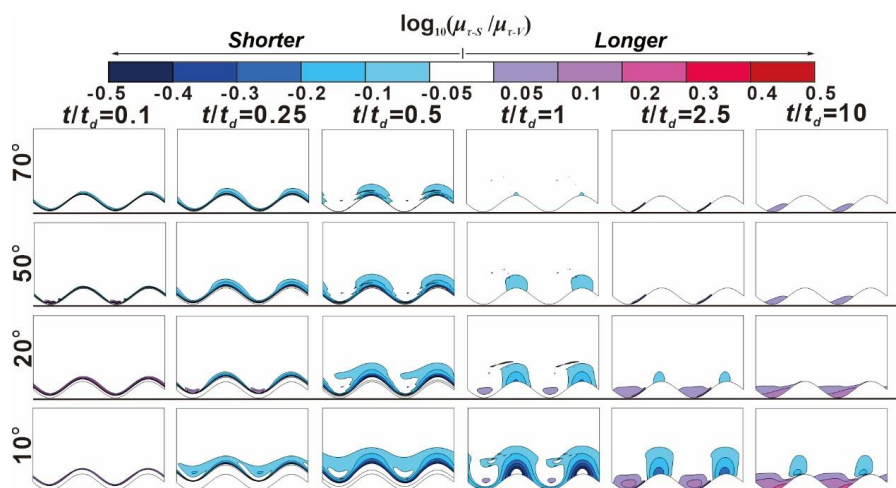
388



389

390 **Figure 8.** Snapshots for the RTD ratio $\mu_r^*(x, t)$ between sloping and vertical riverbank
 391 conditions at different times t/t_d as a function of δ for $\Gamma_d = 0.1$. The horizontal lines
 392 beneath each figure are the reference lines to show the initial location of SWI. The
 393 lower sinuous lines at the reference lines are the initial SWIs.

394



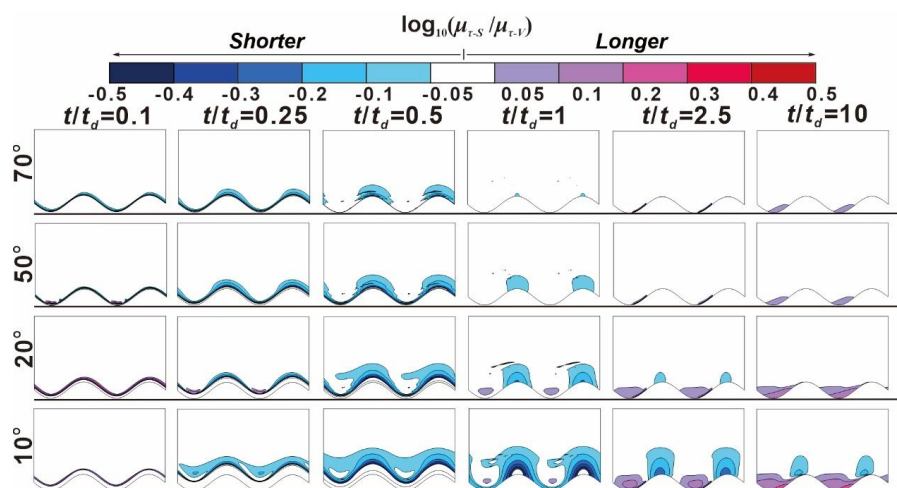
395

396 **Figure 9.** Snapshots for the RTD ratio $\mu_r^*(x, t)$ between sloping and vertical riverbank
 397 conditions at different times t/t_d as a function of δ for $\Gamma_d = 1$. The horizontal lines



398 beneath each figure are the reference lines to show the initial location of SWI. The
399 lower sinuous lines at the reference lines are the initial SWIs.

400



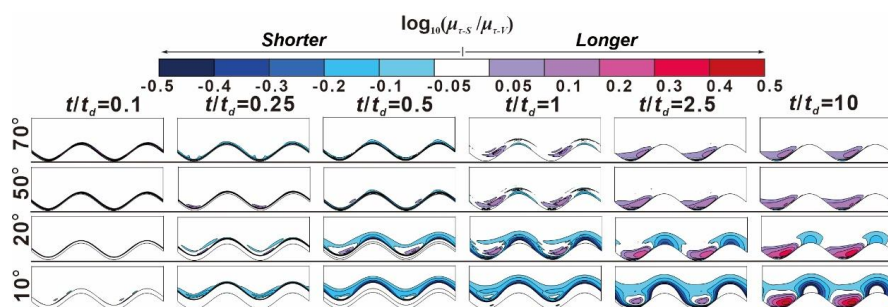
401

402 **Figure 10.** Snapshots for the RTD ratio $\mu_r^*(x, t)$ between sloping and vertical
403 riverbank conditions at different times t/t_d as a function of δ for $\Gamma_d = 10$. The
404 horizontal lines beneath each figure are the reference lines to show the initial location
405 of SWI. The lower sinuous lines at the reference lines are the initial SWIs.

406



407



408

409 **Figure 11.** Snapshots for the RTD ratio $\mu_r^*(\mathbf{x}, t)$ between sloping and vertical
 410 riverbank conditions at different times t/t_d as a function of δ for $\Gamma_d = 100$. The
 411 horizontal lines beneath each figure are the reference lines to show the initial location
 412 of SWI. The lower sinuous lines at the reference lines are the initial SWIs.

413

414 At $t/t_d = 0.1$, a smaller bank slope can lead to shorter RT (negative values of μ_r^*)
 415 near the SWI. The area of shorter RT caused by bank slope was positively related to
 416 aquifer transmissivity. The effect of δ is small for $\Gamma_d = 10$ and 100 because the
 417 groundwater mound piles up around the river boundary, but that small area extended
 418 deeper into the alluvial valley for smaller δ . Due to the scattered and nested flow
 419 paths near the inner bend (cut bank) and outer bend (point bar), respectively, the
 420 penetration distance of the negative value of μ_r^* area at the cut bank of SWI is larger
 421 than that at the point bar. The change of flow direction near the point bar leads to a
 422 prolonged flow path for the water in the river as well as to forced groundwater mixing
 423 with the slightly older water. This effect was amplified with decreasing bank slope,
 424 but it is only statistically significant ($\mu_r^* < -0.05$ or $\mu_r^* > 0.05$) when $\delta = 10^\circ$ at $t/t_d =$
 425 0.1.

426 At the time of peak flood ($t/t_d = 0.25$), the river still infiltrates into the aquifer.
 427 For $\Gamma_d = 0.1$, bank slope can lead to both younger and older water, i.e., water
 428 undergoing shorter and longer RT. Both magnitude of μ_r^* and associated RT area
 429 increase with decreasing slope due to the longer penetration distance of river water



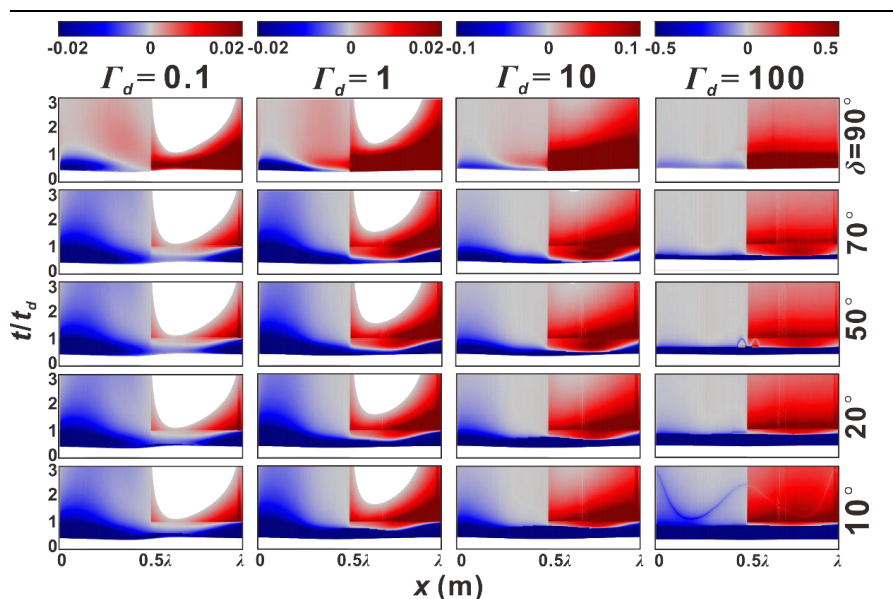
430 into the aquifer. As δ decreases, the positive values of μ_r^* are located closer to the
431 downstream point bar. The impact of bank slope on RTD for $\Gamma_d = 1$ is rather similar in
432 its pattern compared to $\Gamma_d = 0.1$, but μ_r^* was significant only for $\delta = 10^\circ$. For $\Gamma_d = 10$
433 and 100, the effect of bank slope can lead to larger and deeper penetration of the river
434 water into the alluvial valley (Fig. 8 - 11) but this effect is smaller than when looking
435 at smaller Γ_d because of the lower hydraulic transmissivity.

436 At $t/t_d = 0.5$, part of the submerged aquifer at $t/t_d = 0.25$ reemerges due to the
437 decline in river stage. In most cases, smaller bank slopes can lead to wider
438 reemergence of the aquifer, and therefore result in smaller μ_r^* near the river boundary;
439 however, this is not the case for $\Gamma_d = 0.1$ where bank slope can both increase and
440 decrease the RT of pore water. Furthermore, compared to when $t/t_d = 0.25$, the impact
441 of bank slope becomes weaker for $\Gamma_d = 0.1$, but more relevant for the larger Γ_d values.

442 After the flood event ($t/t_d > 1$), the influence of bank slope on RT is nearly
443 eliminated for $\Gamma_d = 0.1$ and 1 due to the high aquifer transmissivity. However, for
444 aquifers with lower transmissivity ($\Gamma_d = 10$ and 100), bank slope still has a significant
445 effect on RT at $t/t_d = 10$ and leads to older water near the point bar, which indicates
446 the bank slope has a more lasting influence on aquifer RT, as more time is required to
447 recover to initial condition.

448 3.3 Relative flux-weighted residence time

449 Fig. 12 shows the evolution of the flux-weighted relative RT $\mu_{out}^*(x, t) = \mathbf{n} \cdot \mathbf{Q}_{out}^*(x,$
450 $t) \log_{10}(\mu_r(x, t) / \mu_r(x, 0))$ for different slopes and aquifer transmissivities. $\mu_{out}^*(x, t)$
451 represents the difference in flux-weighted RT of the water discharged into the river
452 compared to the initial condition. At the start of the flood event, there is no μ_{out}^* as
453 river water infiltrates the aquifer. Following the decline in river stage, the aquifer
454 begins to discharge the mixed water with different RT back into the river (see Fig. 3c).
455



456

457 **Figure 12.** Temporal evolution of flux-weighted ratios of RT to the RT for base flow
 458 condition ($\mu^*_{out}(x, t) = \mathbf{n} \cdot \mathbf{Q}^*_{out}(x, t) \log_{10}(\mu_0(x, t)/\mu_0(x, 0))$) along the river meander as a
 459 function of δ and Γ_d .

460

461 For vertical riverbank conditions ($\delta = 90^\circ$, top row in Fig. 12), upstream ($0.5\lambda <$
 462 $x < \lambda$) and downstream ($0 < x < 0.5\lambda$) boundaries of the meander bend discharge older
 463 and younger water, respectively. The waters with relatively younger or older RT are
 464 mostly discharged before the flood event ($t/t_d < 1$) due to the greater outflux as shown
 465 in Fig. 2a. It also can be seen that water is older along the upstream bend compared to
 466 the more rejuvenated water along the downstream bend. After the flood event, μ^*_{out}
 467 gradually disappears along the upstream meander (blank areas) for $\Gamma_d = 0.1$ and 1,
 468 because the flow fields are recovering to base flow conditions. Therefore, the
 469 upstream meander gradually becomes the inflow boundary.

470 For cases with lower values of Γ_d (left columns in Fig. 12), μ^*_{out} reaches
 471 equilibrium earlier compared to cases with higher Γ_d . As δ decreases from the top
 472 row to the bottom row in Fig. 12, the increased impact of bank slope causes μ^*_{out} to
 473 gradually decrease the RT of the outflux during the flood event. For larger Γ_d , μ^*_{out} is



474 totally dominated by younger water during the flood event. Furthermore, the stronger
475 impact of smaller bank slope angles can both extend the time over which and increase
476 the magnitude with which younger water is discharging along the downstream
477 meander.

478 **4. Discussion**

479 **4.1. Why we should account for bank slope**

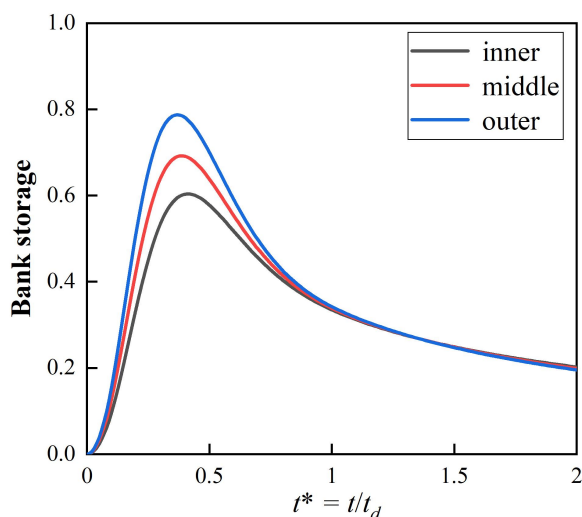
480 Tilted riverbanks are common in nature and caused by erosion and bank collapse,
481 as has been observed at multiple scales (Zingg, 1940). Previous studies have shown
482 that bank erosion is stronger where the river planimetry is more sinuous, river stage
483 varies more frequently, or where the riverbank has larger sloping angles, ultimately
484 leading to a flatter bank (Zingg, 1940; Hagorty et al., 1995; Mayor et al., 2008;
485 Puttock et al., 2013). Hence, recent studies have recognized the need for a
486 comprehensive analysis of how riverbank topography affects lateral hyporheic
487 exchange along meandering streams (Boano et al., 2014) and the specific importance
488 of bank slope on hyporheic exchange has been highlighted by Doble et al. (2012) and
489 Liang et al. (2018). Yet, in most previous studies, the impact of riverbank geometry
490 and in particular bank slope on sinuosity-driven lateral hyporheic exchange was
491 ignored. Flow was usually only considered perpendicular to the river axis, i.e., HEF in
492 river flow direction caused by the alluvial valley slope and river sinuosity was not
493 considered. However, as river planimetry can vary significantly along river corridors
494 (Hooke, 2013; Seminara, 2006), and the alluvial valley slope has a potentially
495 non-negligible impact on hyporheic exchange (Gomez-Velez et al., 2017), we
496 considered it important to close this knowledge gap by specifically focusing on the
497 impact of bank slope and the ambient groundwater gradient for various groundwater
498 flow conditions (as manifested through aquifer transmissivity) on HEF. Our results



499 clearly indicate that HZ characteristics (flow field, area and penetration distance of
500 HZ into alluvial valley) can significantly vary along a meandering river depending on
501 bank slope conditions.

502 Not accounting for bank slope and river sinuosity can lead to an
503 underestimation of infiltration from the river to the alluvial aquifer. This effect is
504 more pronounced for smaller bank slope angles and losing conditions can be
505 significantly underestimated. Doble et al. (2012), Siergieiev et al. (2015) and Liang et
506 al. (2018), assessed the influence of bank slope on HEF using a vertical
507 cross-sectional profile. Siergieiev et al. (2015) found that the impact of bank slope on
508 HEF was proportional to the hydraulic conductivity of the aquifer. However, we argue
509 here that bank slope is more relevant in rivers connected to aquifers with low
510 hydraulic transmissivity. Furthermore, we show (Fig. 13) that using only one
511 cross-sectional river profile perpendicular to the river axis does not capture the effect
512 of river sinuosity on HEF as bank storage decreases from point bar to cut bank. That
513 means the previous vertical cross-sectional profile models could not calculate the
514 bank storage evolution accurately when neglecting the sinuosity of river. In a
515 meandering river with variable bank slope, river geometry thus has a sizable effect on
516 bank storage evolution and HEF, and should be included into the future analytical/
517 numerical models.

518



519

520 **Figure 13.** Bank storage versus time for $\Gamma_d = 1$ and $\delta = 90^\circ$ condition at: inner bend
521 ($x = 0$); middle bend ($x = 0.25\lambda$); outer bend ($x = 0.25\lambda$). Dimensionless bank storage

522 was calculated by $\frac{\int_{y(x,t)}^{y(x,t)+4\lambda} [h-z_b-H_0] dy}{\lambda H_p}$.

523

524 The impact of bank slope on RT is basically controlled by aquifer transmissivity.
525 When aquifer transmissivity increases, the impact of bank slope appears to be more
526 pronounced when river stage rises during a flood event. For decreasing aquifer
527 transmissivity, bank slope seems more relevant for RTD after the flood event and its
528 impact is more long-lasting. Bank slope could result in longer (near the point bar) or
529 shorter (near the cut bank) pore water RT at various times of a flood event. This
530 means that point bars with bank slopes are more conducive for river restoration (e.g.,
531 removal of dissolved organic carbon) while cut banks with bank slope may have
532 adverse effects on the groundwater quality near rivers. This is important to keep in
533 mind when assessing the influence of bank slope on biogeochemical efficiency. For
534 example, previous research indicates that the residence time of river water in the HZ
535 can control, and is often proportional to nutrient cycling (McCallum and Shanfield,
536 2016; Wondzell and Swanson, 1999; Zarnetske et al., 2011, 2012). As such, an



537 analysis of RTD can provide valuable information on whether and where riverbank
538 slope can induce biogeochemical hotspots and hot moments and help guide choices to
539 be made in biogeochemical field surveys regarding location and sampling time under
540 dynamic river stage conditions, especially when the connected aquifers have low
541 hydraulic transmissivity.

542 **4.2. Advantages and limitations of using a reduced 2-D model**

543 In this study, we propose a parsimonious reduced-order, idealized horizontal
544 2-D model that simplifies the variation of the river-aquifer interface by using the
545 moving boundary method to depict the displacement of SWI along a sloping
546 riverbank. An advantage of this approach is reduced model complexity as compared
547 to a three-dimensional model, which greatly reduces time and data requirements
548 during model building and computational demand during simulation of HEF and
549 especially residence time distributions. Thus, our reduced-order model acts as a first
550 step to gain insight into the patterns of hyporheic exchange, riverbank storage and
551 RTD in settings with more complex riverbank morphology and dynamic forcing.
552 Future efforts should be focused on optimizing the computational method applied
553 here and on including more detailed morphology and hydrodynamic characteristics.

554 It is important to note that in our simulations we assume a constant angle of
555 bank slope along the meandering river while natural riverbanks often have
556 non-uniform slopes which could lead to a different behavior. Thus, new
557 conceptualizations that account for the contribution of bank slope on time-varying
558 RTD and HZ extent can be applied to gain better understanding of a hyporheic zone,
559 especially in cases where bank slope is small, or where the system is relatively
560 insensitive to changes during peak flow.

561 In our simulations we tested the model using a range of aquifer hydraulic
562 conductivities. Although hydraulic conductivity (or transmissivity) is a critical
563 parameter in the quantification of exchange fluxes and RTD between the two systems



564 under varying slope conditions, other parameters such as valley water head fluctuation,
565 peak flood event characteristics or larger scale groundwater head fluctuation, e.g., due
566 to changing groundwater recharge patterns have not been considered here but might
567 also impact HZ extent, RTD and river-aquifer exchange flux.

568

569 **5. Conclusions**

570 The deformed geometry method was applied to characterize the expansion and
571 contraction of hyporheic zones along sloping riverbanks, and to evaluate the impact of
572 bank slope on hyporheic exchange flux, evolution of the HZ area and RTD. To
573 achieve this, various alluvial aquifers with varying slope angles and aquifer
574 transmissivity values were simulated. Our results show that bank slope in a
575 sinuosity-driven river can have significant impact on the evolution of the hyporheic
576 zone during and after a flood event (transient flood forcing).

577 The overall findings of our work underline the need for a detailed analysis of
578 lateral hyporheic exchange flow responses to dynamic forcings (including the
579 assumption of more realistic riverbank morphology conditions). Furthermore, our
580 results show that more detailed information on bank slope (e.g., through more
581 measurements) can lead to a better understanding of hyporheic flow patterns and
582 potentially result in improved biogeochemical process understanding for real-world
583 conditions in more complex morphology and depositional environments. Several
584 conclusions can be drawn from our study:

- 585 1. Sloping riverbanks can increase HEF, especially when the river is connected to a
586 low-transmissivity alluvial aquifer and bank slope angles are small. However,
587 bank slope has only a minor impact on the hyporheic outflow flux.
- 588 2. During a flood event, the bank slope can increase the area and penetration distance
589 of the HZ into the alluvial aquifer. This effect is more pronounced and



-
- 590 long-lasting for low-transmissivity aquifers.
- 591 3. During a flood event, the impact of bank slope on RTD is more pronounced for
592 high transmissivity aquifers. On the contrary, the impact of bank slope on RTD for
593 lower transmissivity aquifers is minor during the flood event, but can have a
594 significant and long-lasting effect under post-flood conditions.
- 595 4. River sinuosity should be considered when assessing the impact of bank slope on
596 RTD. Variable bank slope can lead to both longer and shorter RT compared to
597 vertical riverbank conditions.
- 598 5. Bank slope has a greater impact on the residence time of hyporheic water in
599 lower-transmissivity aquifers, thereby delaying the time of younger water
600 discharge downstream of a meander bend, which also delays the outflow of older
601 water upstream of that bend.



602 **Code and data availability**

603 Additional information regarding methodology and results is provided in the
604 supporting information (SI).

605 **Author contributions**

606 YL: Conceptualization, Formal analysis, Investigation

607 US: Conceptualization, Methodology, Writing

608 ZW: Funding acquisition, Software, Supervision

609 SK: Validation, Writing, Supervision

610 HL: Project administration, Supervision

611 **Acknowledgements**

612 This research was partially supported by the National Natural Science Foundation of
613 China (Grant Numbers: 42272290, 41830862, and 42022018), and China Scholarship
614 Council (CSC, 202106410042).

615

616 **Competing interests**

617 The authors declare that they have no conflict of interest.



618 **References**

- 619 Bear, J., and Cheng, A. H. D.: Modeling groundwater flow and contaminant transport,
620 Vol. 23, pp. 83, Dordrecht: Springer, 2010.
- 621 Bertrand, G., Goldscheider, N., Gobat, J.-M., and Hunkeler, D.: Review: From
622 multi-scale conceptualization to a classification system for inland
623 groundwater-dependent ecosystems, *Hydrogeology Journal*, 20, 5-25, 2012.
- 624 Boano, F., Camporeale, C., Revelli, R., and Ridolfi, L.: Sinuosity-driven hyporheic
625 exchange in meandering rivers, *Geophysical Research Letters*, 33, L18406, 2006.
- 626 Boano, F., Harvey, J. W., Marion, A., and Packman, A. I., Revelli, R., Ridolfi, L., and
627 Wörman, A.: Hyporheic flow and transport processes: Mechanisms, models, and
628 biogeochemical implications, *Reviews of Geophysics*, 52, 603-679, 2014.
- 629 Boano, F., Demaria, A., Revelli, R., and Ridolfi, L.: Biogeochemical zonation due to
630 intrameander hyporheic flow, *Water Resource. Research*. 46, W02511, 2010.
- 631 Boulton, A. J., Datry, T., Kasahara, T., Mutz, M., and Stanford, J. A.: Ecology and
632 management of the hyporheic zone: Stream-groundwater interactions of running
633 waters and their floodplains, *Journal of the North American Benthological*
634 *Society*, 29 (1), 26-40, 2010.
- 635 Brunke, M., and Gonser, T.: The ecological significance of exchange processes
636 between rivers and groundwater, *Freshwater Biology*, 37 (1), 1-33, 1997.
- 637 Cardenas, M. B.: The effect of river bend morphology on flow and timescales of
638 surface water-groundwater exchange across pointbars, *Journal of Hydrology*, 362,
639 134-141, 2008.
- 640 Cardenas, M. B.: A model for lateral hyporheic flow based on valley slope and
641 channel sinuosity, *Water Resources Research*, 45, W01501, 2009a.
- 642 Cardenas, M. B.: Stream-aquifer interactions and hyporheic exchange in gaining and
643 losing sinuous streams, *Water Resources Research*, 45, W06429, 2009b.
- 644 Cardenas, M. B.: Hyporheic zone hydrologic science: A historical account of its



-
- 645 emergence and a prospectus, *Water Resources Research*, 51, 3601-3616, 2015.
- 646 Cooper, H. H., and Rorabaugh, M. I.: Ground-water movements and bank storage due
647 to flood stages in surface streams, Report of Geological Survey Water-Supply, pp.
648 1536-J, US Government Printing Office, Washington, United States, 1963.
- 649 Derx, J., Farnleitner, A. H., Blöschl, G., Vierheilig, J., and Blaschke, A. P.: Effects of
650 riverbank restoration on the removal of dissolved organic carbon by soil passage
651 during floods—A scenario analysis, *Journal of Hydrology*, 512, 195-205, 2014.
- 652 Doble, R. C., Crosbie, R. S., Smerdon, B. D., Peeters, L., and Cook, F. J.:
653 Groundwater recharge from overbank floods, *Water Resources Research*, 48 (9),
654 W09522, 2012a.
- 655 Doble, R., Brunner, P., McCallum, J., and Cook, P. G.: An analysis of river bank slope
656 and unsaturated flow effects on bank storage, *Ground Water*, 50 (1), 77-86,
657 2012b.
- 658 Donea, J., A. Huerta, J.-P. Ponthot, and A. Rodriguez-Ferran.: Arbitrary
659 Lagrangian–Eulerian methods, In *Encyclopedia of Computational Mechanics*, ed.
660 E. Stein, R. de Borst, and T. J. R. Hughes, 413-434. New York: John Wiley &
661 Sons, 2004.
- 662 Duarte, F., Gormaz, R., and Natesan, S.: Arbitrary Lagrangian–Eulerian method for
663 Navier–Stokes equations with moving boundaries, *Computer Methods in
664 Applied Mechanics and Engineering*, 193 (45-47), 4819-4836, 2004.
- 665 Fox, G. A., and Wilson, G. V.: The role of subsurface flow in hillslope and stream
666 bank erosion: a review, *Soil Science Society of America Journal*, 74 (3), 717-733,
667 2010.
- 668 Gao, Y., Zhu, B., Zhou, P., Tang, J. L., Wang, T., and Miao, C. Y.: Effects of
669 vegetation cover on phosphorus loss from a hillslope cropland of purple soil
670 under simulated rainfall: a case study in China, *Nutrient Cycling in
671 Agroecosystems*, 85 (3), 263-273, 2009.
- 672 Gomez-Velez, J. D., and Harvey, J. W.: A hydrogeomorphic river network model



-
- 673 predicts where and why hyporheic exchange is important in large basins,
674 Geophysical Research Letters, 41, 6403–6412, 2014.
- 675 Gomez, J. D., Wilson, J. L., and Cardenas, M. B.: Residence time distributions in
676 sinuosity - driven hyporheic zones and their biogeochemical effects, Water
677 Resources Research, 48 (9), 2012.
- 678 Gomez-Velez, J. D., Wilson, J. L., Cardenas, M. B., and Harvey, J. W.: Flow and
679 residence times of dynamic river bank storage and sinuosity-driven hyporheic
680 exchange, Water Resources Research, 53, 8572-8595, 2017.
- 681 Gomez-Velez, J. D., Harvey, J. W., Cardenas, M. B., and Kiel, B.: Denitrification in
682 the Mississippi River network controlled by flow through river bedforms, Nature
683 Geoscience, 8, 941-945, 2015.
- 684 Hagerty, D. J., Spoor, M. F., and Parola, A. C.: Near-bank impacts of river stage
685 control, Journal of Hydraulic Engineering, 121 (2), 196-207, 1995.
- 686 Hooke, J. M.: River meandering, In E. Wohl & J. Shroder (Eds.), Treatise on
687 geomorphology, Vol. 9, pp. 260-288, CA: Academic Press, San Diego, 2013.
- 688 Hester, E. T., and Gooseff, M. N.: Moving beyond the banks: Hyporheic restoration is
689 fundamental to restoring ecological services and functions of streams,
690 Environmental Science and Technology, 44 (5), 1521-1525, 2010.
- 691 Hunt, B.: An approximation for the bank storage effect, Water Resources Research, 26
692 (11), 2769–2775, 1990.
- 693 Kiel, B. A., Cardenas, M. B.: Lateral hyporheic exchange throughout the Mississippi
694 River network, Nature Geoscience, 7 (6), 413-417, 2014.
- 695 Krause, S., Abbott, B. W., Baranov, V., Bernal, S., Blaen, P., Datry, T., Drummond, J.,
696 Fleckenstein, J. H., Gomez-Velez, J., Hannah, D. M., Knapp, J. L. A., Kurz, M.,
697 Lewandowski, J., Marti, E., Mendoza-Lera C., Milner, A., Packman, A., Pinay,
698 G., Ward, A. S., Zarnetzke, J. P.: Organizational principles of hyporheic
699 exchange flow and biogeochemical cycling in river networks across scales,
700 Water Resources Research. 58, e2021WR029771, 2022.



-
- 701 Krause, S., Hannah, D. M., Fleckenstein, J. H., Heppell, C. M., Pickup, R., Pinay, G.,
702 Robertson, A. L., and Wood, P. J.: Inter-disciplinary perspectives on processes in
703 the hyporheic zone, *Ecohydrology Journal*. 4 (4), 481-499, 2011.
- 704 Krause, S., Lewandowski, J., Grimm, N., Hannah, D. M., Pinay, G., Turk, V., Argerich,
705 A., Sabater, F., Fleckenstein, J., Schmidt, C., Battin, T., Pfister, L., Martí, E.,
706 Sorolla, A., Larned, S., and Turk, V.: Ecohydrological interfaces as critical
707 hotspots for ecosystem functioning, *Water Resources Research*. 53, 6359-6376,
708 2017.
- 709 Krause, S., Tecklenburg, C., Munz, M., and Naden, E.: Streambed nitrogen cycling
710 beyond the hyporheic zone: Flow controls on horizontal patterns and depth
711 distribution of nitrate and dissolved oxygen in the upwelling groundwater of a
712 lowland river, *Journal of Geophysical Research: Biogeosciences*, 118 (1), 54-67,
713 2013.
- 714 Kruegler, J., Gomez-Velez, J. D., Lautz, L. K., and Endreny, T. A.: Dynamic
715 evapotranspiration alters hyporheic flow and residence times in the intrameander
716 zone, *Water*, 12 (2), 424, 2020.
- 717 Larkin, R. G., and Sharp, J. M.: On the relationship between river-basin
718 geomorphology, aquifer hydraulics, and groundwater flow direction in alluvial
719 aquifers, *Geological Society of America Bulletin*, 104, 1608-1620, 1992.
- 720 Li, H., Boufadel, M. C., and Weaver, J. W.: Quantifying bank storage of variably
721 saturated aquifers, *Ground Water*, 46 (6), 841-850, 2008.
- 722 Liang, X. Y., Zhan, H. B., and Schilling, K.: Spatiotemporal responses of groundwater
723 flow and aquifer-river exchanges to flood events, *Water Resources Research*, 54
724 (3), 1513-1532, 2018.
- 725 Lindow, N., Fox, G. A., and Evans, R. O.: Seepage erosion in layered stream bank
726 material, *Earth Surface Processes and Landforms*, 34 (12), 1693-1701, 2009.
- 727 Mayor, Á. G., Bautista, S., Small, E. E., Dixon, M., and Bellot, J.: Measurement of
728 the connectivity of runoff source areas as determined by vegetation pattern and



-
- 729 topography: A tool for assessing potential water and soil losses in drylands,
730 Water Resources Research, 44 (10), 2008.
- 731 Maury, B.: Characteristics ALE method for the unsteady 3D Navier-Stokes equations
732 with a free surface, International Journal of Computational Fluid Dynamics, 6 (3),
733 175-188, 1996.
- 734 McCallum, J.L., P.G. Cook, P. Brunner, and D. Berhane.: Solute dynamics during
735 bank storage flows and implications for chemical baseflow separation, Water
736 Resources Research, 46: W07541, 2010.
- 737 McClain, M. E., Boyer, E. W., Dent, C. L., Gergel, S. E., Grimm, N. B., Groffman, P.
738 M., Hart, S. C., Harvey, J. W., Johnston, C. A., Mayorga, E., McDowell, W and
739 Pinay, G.: Biogeochemical hot spots and hot moments at the interface of
740 terrestrial and aquatic ecosystems, Ecosystems, 6 (4), 301-312, 2003.
- 741 Millar, R. G., and Quick, M. C.: Effect of bank stability on geometry of gravel rivers,
742 Journal of Hydraulic Engineering, 119 (12), 1343-1363, 1993.
- 743 Millington, R. J., and Quirk, J. P.: Permeability of porous solids, Transactions of the
744 Faraday Society, 57, 1200-1207, 1961.
- 745 Osman, A. M., and Thorne, C. R.: Riverbank stability analysis. I: Theory, Journal of
746 Hydraulic Engineering, 114 (2), 134-150, 1988.
- 747 Pinay, G., Peiffer, S., De Dreuzy, J. R., Krause, S., Hannah, D. M., Fleckenstein, J. H.,
748 Sebilo, M., Bishop, K., and Hubert-M, L.: Upscaling nitrogen removal capacity
749 from local hotspots to low stream orders' drainage basins, Ecosystems, 18 (6),
750 1101-1120, 2015.
- 751 Pohjoranta, A., and Tenno, R.: Implementing surfactant mass balance in 2D
752 FEM-ALE models, Engineering with Computers, 27 (2), 165-175, 2011.
- 753 Puttock, A., Macleod, C. J., Bol, R., Sessford, P., Dungait, J., and Brazier, R. E.:
754 Changes in ecosystem structure, function and hydrological connectivity control
755 water, soil and carbon losses in semi-arid grass to woody vegetation transitions,
756 Earth Surface Processes and Landforms, 38 (13), 1602-1611, 2013.



-
- 757 Seminara, G.: Meanders, *Journal of Fluid Mechanics*, 554, 271-297, 2006.
- 758 Schmadel, N. M., A. S. Ward, C. S. Lowry, and J. M. Malzone.: Hyporheic exchange
759 controlled by dynamic hydrologic boundary conditions, *Geophysical Research*
760 *Letters*, 43, 4408-4417, 2016.
- 761 Sharp, J. M.: Limitations of bank-stopage model assumptions, *Journal of Hydrology*,
762 35 (1-2), 31-47, 1977.
- 763 Siergieiev, D., Ehlert, L., Reimann, T., Lundberg, A., and Liedl, R.: Modelling
764 hyporheic processes for regulated rivers under transient hydrological and
765 hydrogeological conditions, *Hydrology and Earth System Sciences*, 19 (1),
766 329-340, 2015.
- 767 Singh, T., Gomez-Velez, J. D., Wu, L., Wörman, A., Hannah, D. M., and Krause, S.:
768 Effects of successive peak flow events on hyporheic exchange and residence
769 times, *Water Resources Research*, 56 (8), e2020WR027113, 2020.
- 770 Singh, T., Wu, L., Gomez-Velez, J. D., Lewandowski, J., Hannah, D. M., Krause, S.:
771 Dynamic hyporheic zones: Exploring the role of peak flow events on bedform-
772 induced hyporheic exchange, *Water Resources Research*, 55, 218-235, 2019.
- 773 Stonedahl, S. H., Harvey, J. W., and Packman, A. I.: Interactions between hyporheic
774 flow produced by stream meanders, bars, and dunes, *Water Resources Research*,
775 49, 5450-5461, 2013.
- 776 Triska, F. J., Kennedy, V. C., Avanzino, R. J., Zellweger, G. W., and Bencala, K. E.:
777 Retention and transport of nutrients in a third - order stream in northwestern
778 California: Hyporheic processes, *Ecology*, 70 (6), 1893-1905, 1989.
- 779 Weatherill, J. J., Atashgahi, S., Schneidewind, U., Krause, S., Ullah, S., Cassidy, N.,
780 and Rivett, M. O.: Natural attenuation of chlorinated ethenes in hyporheic zones:
781 A review of key biogeochemical processes and in-situ transformation potential,
782 *Water research*, 128, 362-382, 2018.
- 783 Wondzell, S. M., and Swanson, F. J.: Floods, channel change, and the hyporheic zone,
784 *Water Resources Research*, 35 (2), 555-567, 1999.



-
- 785 Wu, L., Gomez-Velez, J. D., Krause, S., Singh, T., Wörman, A., and Lewandowski, J.:
786 Impact of flow alteration and temperature variability on hyporheic exchange,
787 Water Resources Research, 56 (3), e2019WR026225, 2020.
- 788 Wu, L., Gomez-Velez, J. D., Krause, S., Wörman, A., Singh, T., Nützmann, G., and
789 Lewandowski, J.: How daily groundwater table drawdown affects the diel
790 rhythm of hyporheic exchange, Hydrology and Earth System Sciences, 25 (4),
791 1905-1921, 2021.
- 792 Wu, L., Singh, T., Gomez-Velez, J. D., Nützmann, G., Wörman, A., Krause, S., and
793 Lewandowski, J.: Impact of dynamically changing discharge on hyporheic
794 exchange processes under gaining and losing groundwater conditions, Water
795 Resources Research, 54 (12), 10-076, 2018.
- 796 Zarnetske, J. P., Haggerty, R., Wondzell, S. M., and Baker, M. A.: Dynamics of nitrate
797 production and removal as a function of residence time in the hyporheic zone,
798 Journal of Geophysical Research, 116, G01025, 2021.
- 799 Zarnetske, J. P., Haggerty, R., Wondzell, S. M., Bokil, V. A., and González-Pinzón, R.:
800 Coupled transport and reaction kinetics control the nitrate source-sink function of
801 hyporheic zones, Water Resources Research, 48, W11508, 2012.
- 802 Zingg, A. W.: Degree and length of land slope as it affects soil loss in run-off,
803 Agricultural Engineering, 21, 59-64, 1940.
- 804