

Supplementary Information for

Machine learning-constrained projection of bivariate hydrological drought magnitudes and socioeconomic risks

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Table S1. Classification of drought and threshold values of the drought events.

Drought Classes	Drought Index (DI)
No Drought	DI > -0.5
Mild Drought	-1.0 < DI ≤ -0.5
Moderate Drought	-1.5 < DI ≤ -1.0
Severe Drought	-2.0 < DI ≤ -1.5
Extreme Drought	DI ≤ -2.0

Table S2. Seven candidate distributions to the marginal distributions of drought duration and severity.

Candidate distributions	Probability density functions
Gamma	$f(x) = \frac{x^{\alpha-1}}{\beta^\alpha \Gamma(\alpha)} e^{-\frac{x}{\beta}}$
Generalized Extreme Value	$f(x) = \exp \left\{ - \left[1 + \gamma \left(\frac{x - \mu}{\sigma} \right) \right]^{-\frac{1}{\gamma}} \right\}$
Inverse Gaussian	$f(x) = \frac{\sqrt{\lambda}}{\sqrt{2\pi x^3}} \exp \left\{ - \frac{\lambda(x - \mu)^2}{2\mu^2 x} \right\}$
Log-normal	$f(x) = \frac{1}{x\sigma\sqrt{2\pi}} \exp \left\{ - \frac{(\ln x - \mu)^2}{2\sigma^2} \right\}$
Normal	$f(x) = \frac{1}{\sigma\sqrt{2\pi}} \exp \left\{ - \frac{(x - \mu)^2}{2\sigma^2} \right\}$
Pearson type-III	$f(x) = \frac{\beta^\alpha}{\Gamma(\alpha)} (x - a_0)^{\alpha-1} e^{-\beta(x-a_0)}$
Weibull	$f(x) = \frac{k}{\lambda} \left(\frac{x}{\lambda} \right)^{k-1} e^{-\left(\frac{x}{\lambda} \right)^k}$