

1 **Supplemental Material S1**

2 **Title: Full prediction of unsaturated hydraulic conductivity - comparison of four different
3 capillary bundle models**

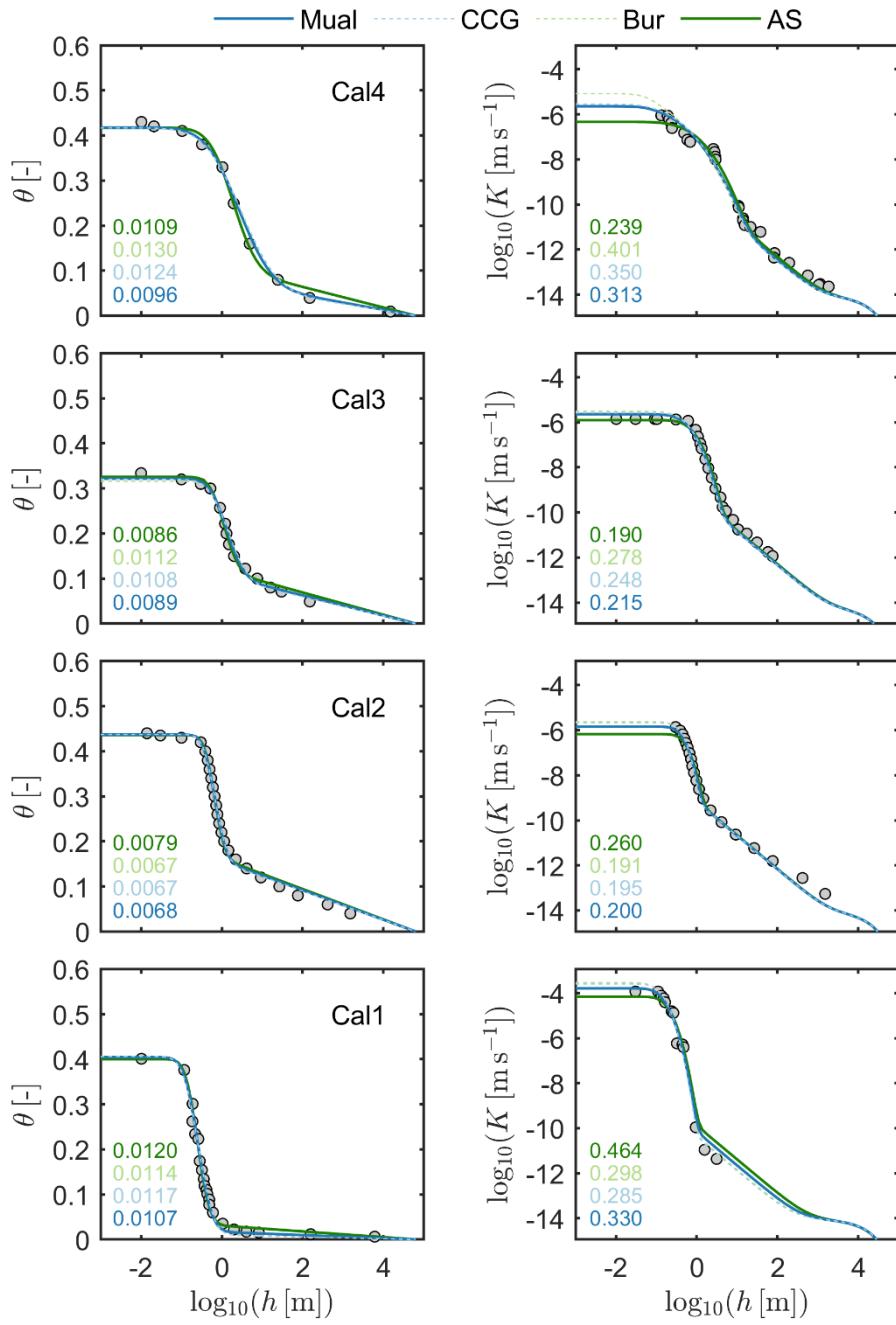
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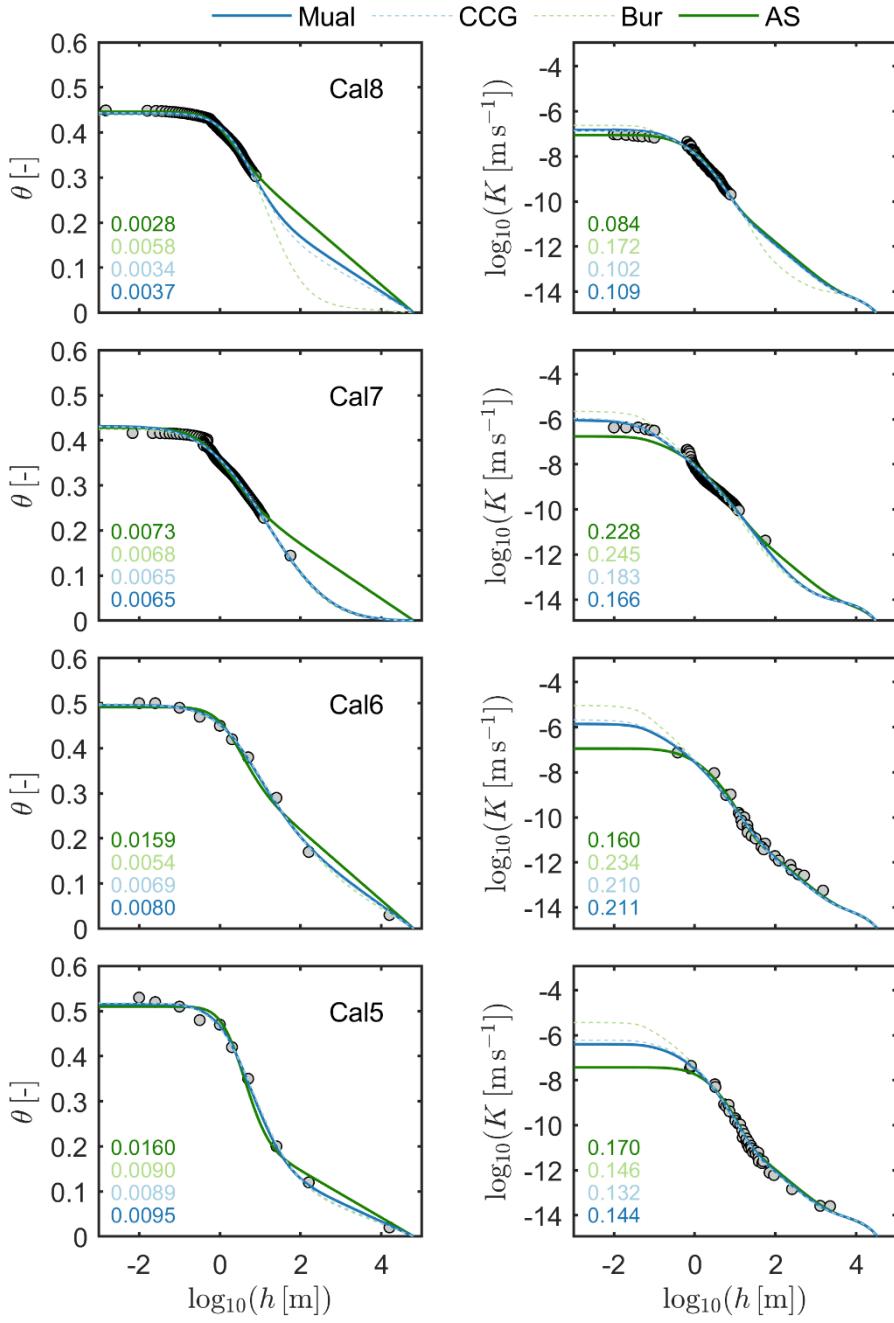
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10 **S 1.1: All calibration curves (pages 2 to 13)**



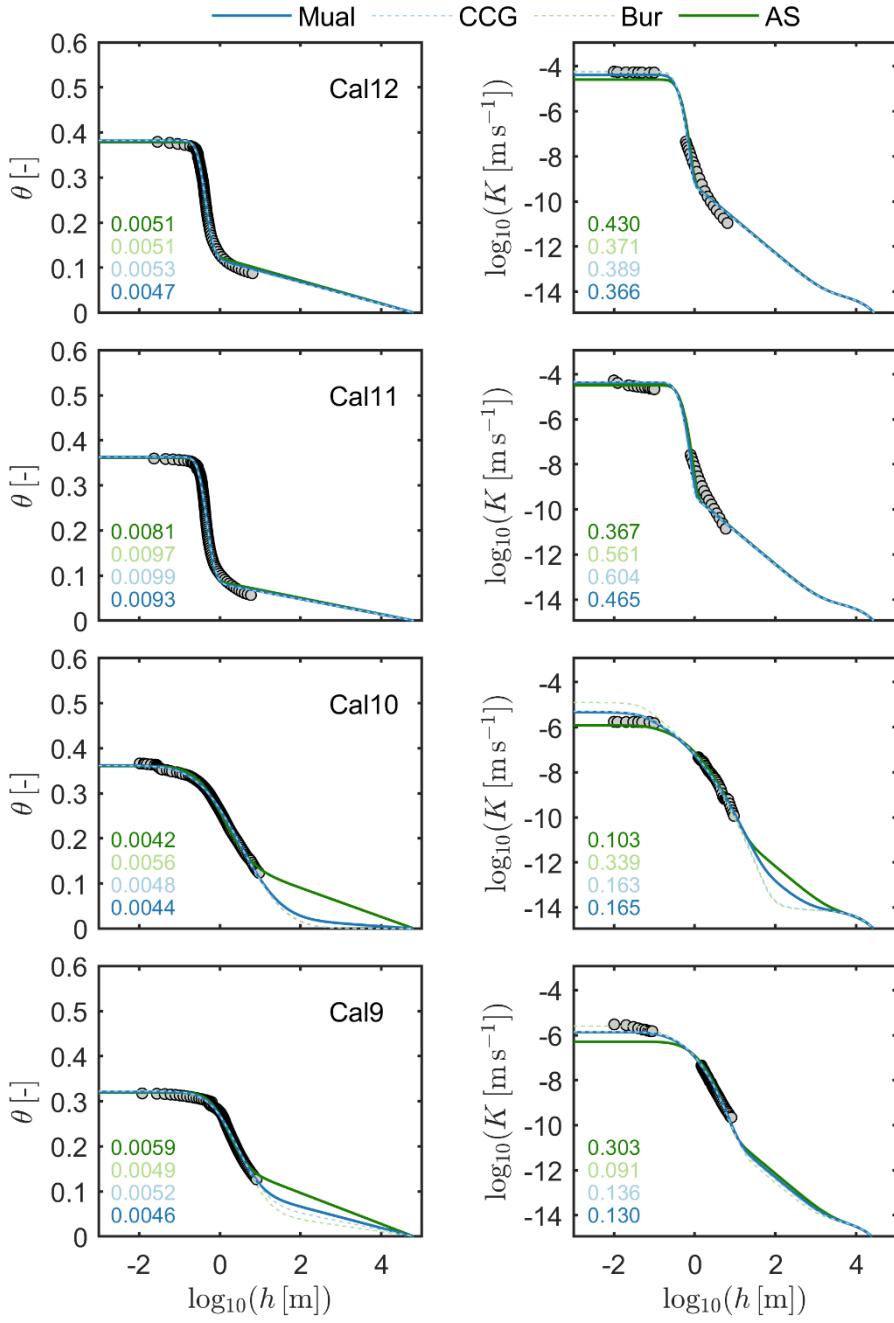
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12 Fig. S1: Calibration data sets and the fitted water retention and conductivity functions used to
 13 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 1 to 4 of the 12 calibration data
 14 sets and the **Kos-PDI** retention model combined with the 4 capillary bundle models. Parameter τ_s
 15 and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE $_{\theta}$ and
 16 RMSE $_{\log K}$ values for the various model combinations.



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18 Fig. S2: Calibration data sets and the fitted water retention and conductivity functions used to
 19 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 5 to 8 of the 12 calibration data
 20 sets and the **Kos-PDI** retention model combined with the 4 capillary bundle models. Parameter τ_s
 21 and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE_θ and
 22 $\text{RMSE}_{\log K}$ values for the various model combinations.

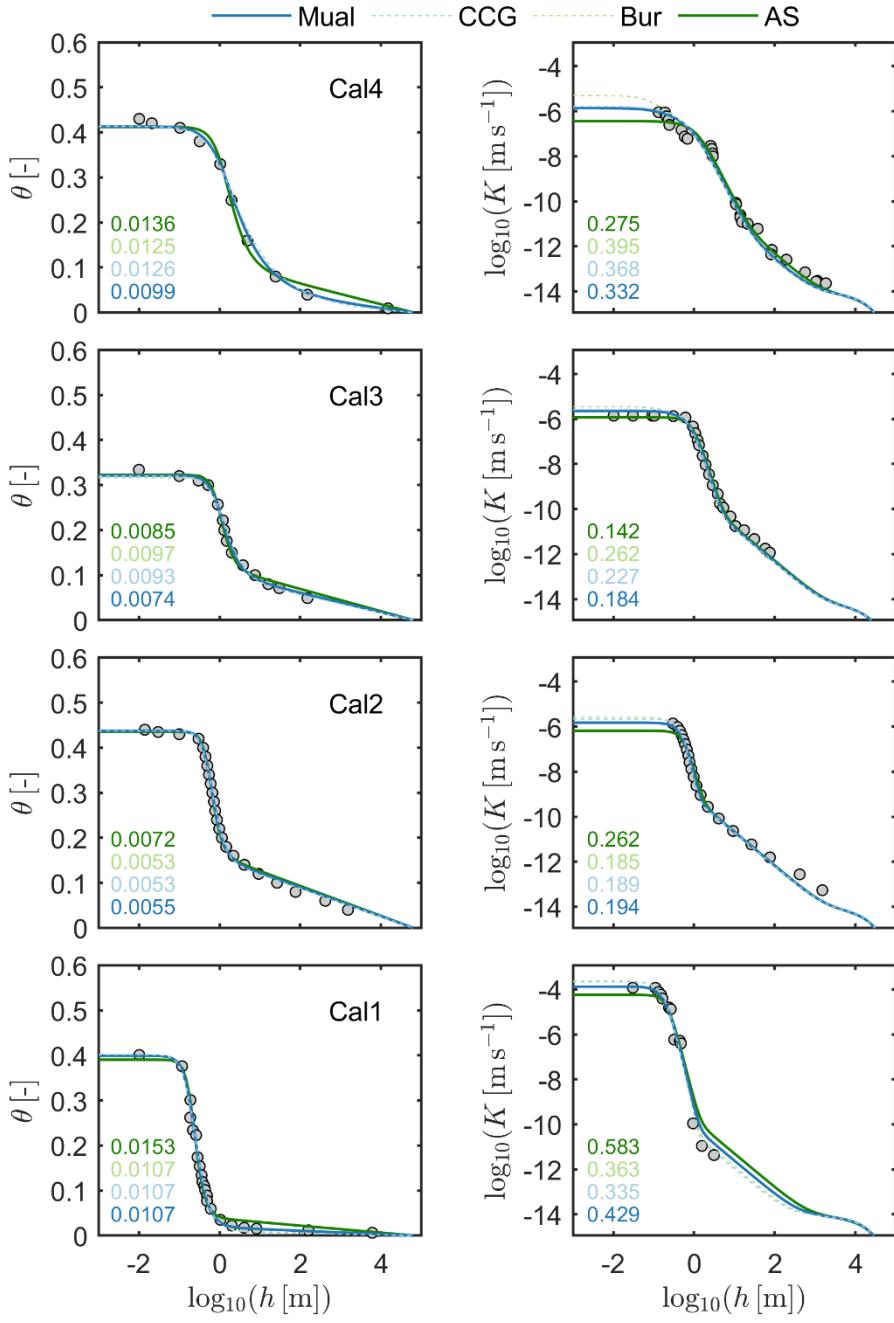


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24 Fig. S3: Calibration data sets and the fitted water retention and conductivity functions used to
 25 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 9 to 12 of the 12 calibration data
 26 sets and the **Kos-PDI** retention model combined with the 4 capillary bundle models. Parameter τ_s
 27 and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE_θ and
 28 $\text{RMSE}_{\log K}$ values for the various model combinations.

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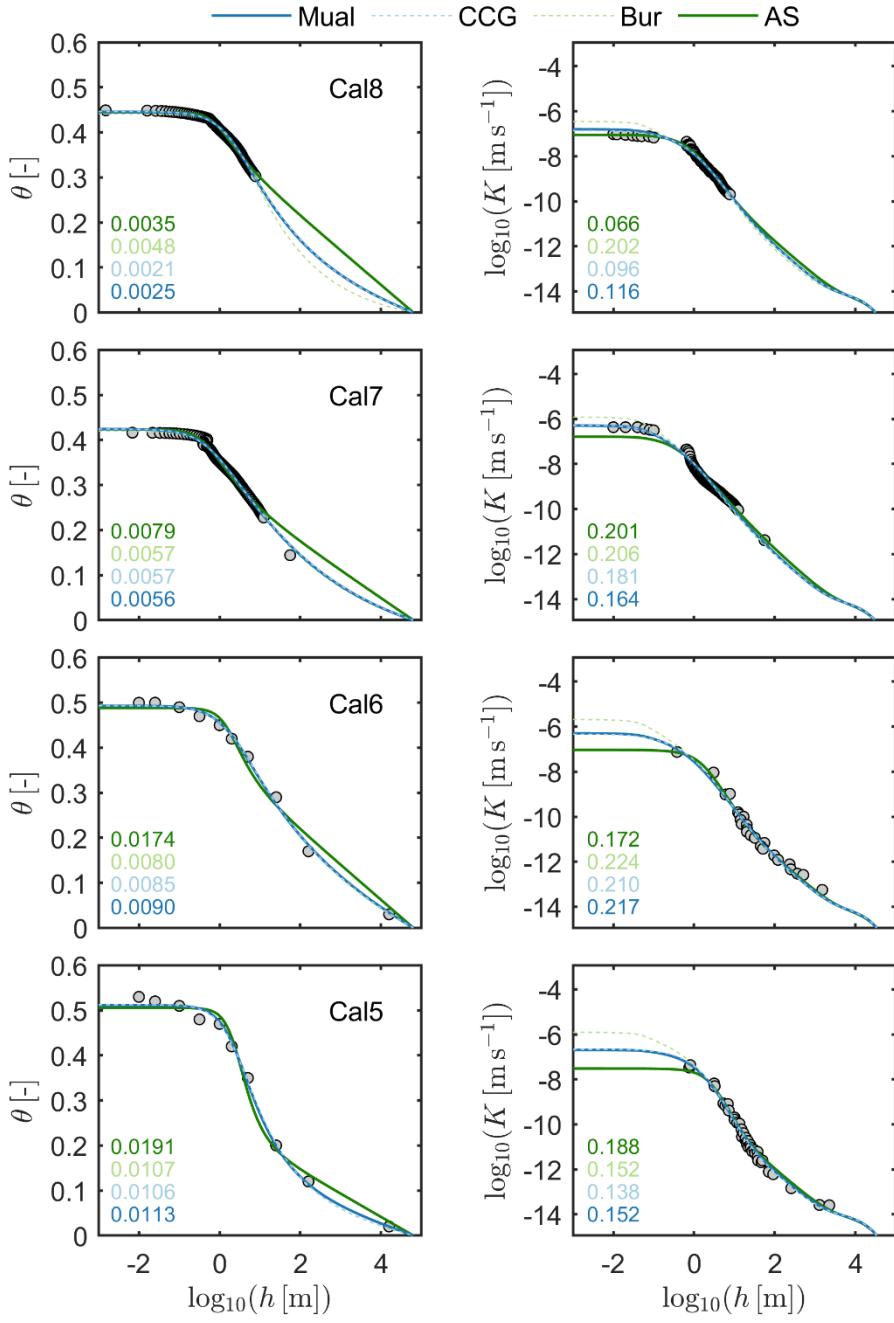
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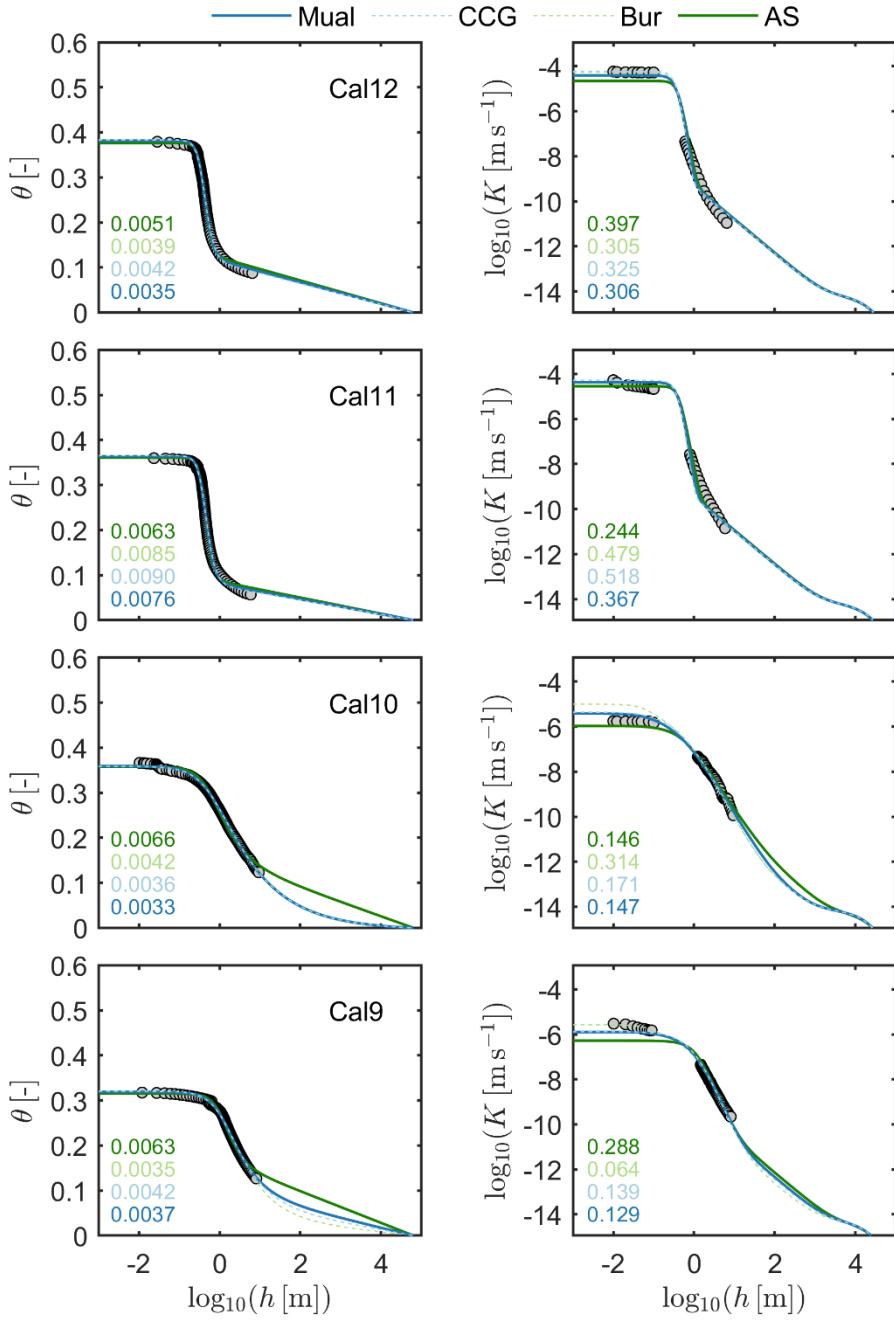
32 Fig. S4: Calibration data sets and the fitted water retention and conductivity functions used to
 33 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 1 to 4 of the 12 calibration data
 34 sets and the vGc-PDI retention model combined with the 4 capillary bundle models. Parameter τ_s
 35 and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE_{θ} and
 36 $\text{RMSE}_{\log K}$ values for the various model combinations.

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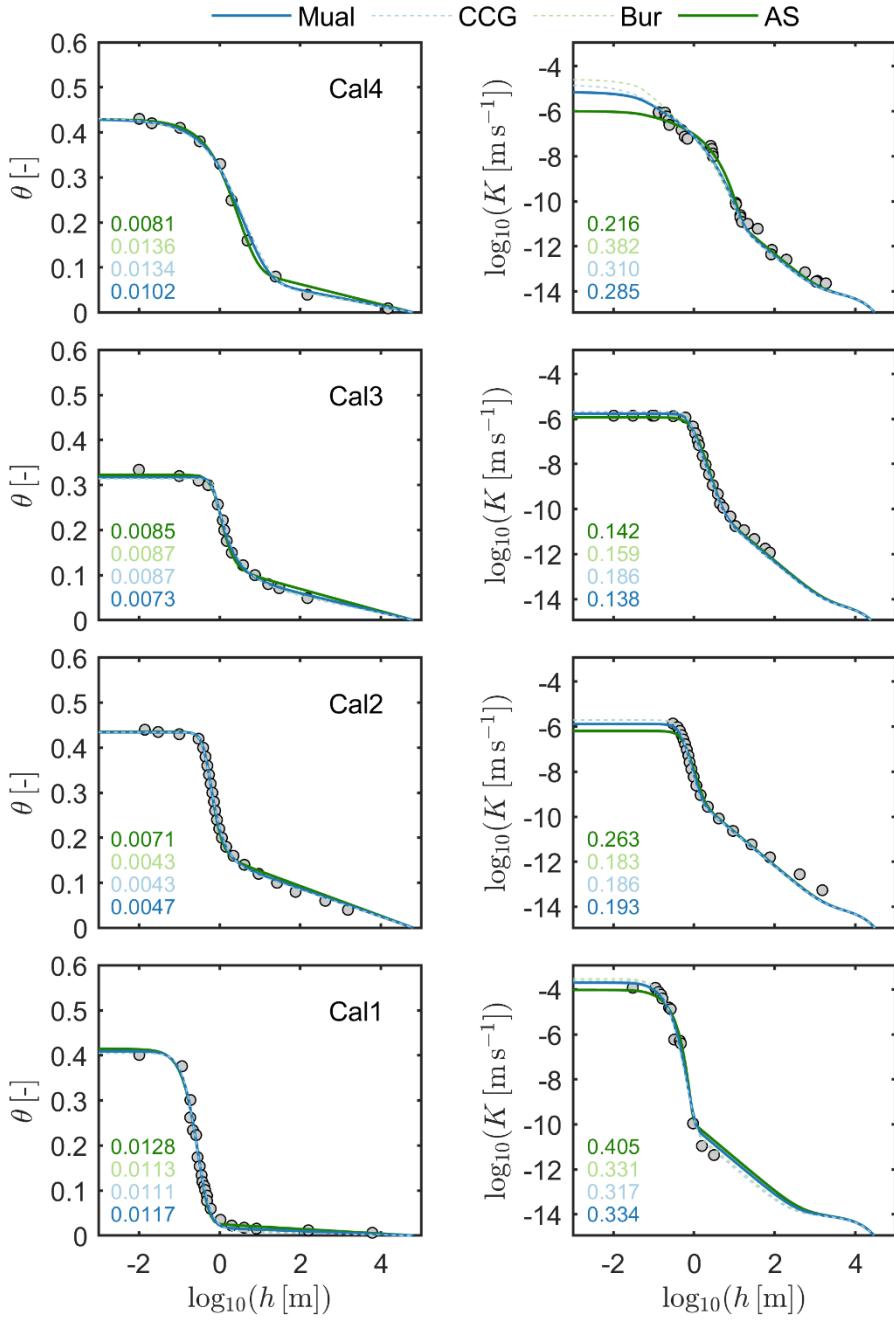
39 Fig. S5: Calibration data sets and the fitted water retention and conductivity functions used to
 40 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 5 to 8 of the 12 calibration data
 41 sets and the vGc-PDI retention model combined with the 4 capillary bundle models. Parameter τ_s
 42 and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE_{θ} and
 43 $\text{RMSE}_{\log K}$ values for the various model combinations.



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45 Fig. S6 Calibration data sets and the fitted water retention and conductivity functions used to
 46 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 9 to 12 of the 12 calibration data
 47 sets and the vGc-PDI retention model combined with the 4 capillary bundle models. Parameter τ_s
 48 and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE_θ and
 49 $\text{RMSE}_{\log K}$ values for the various model combinations.

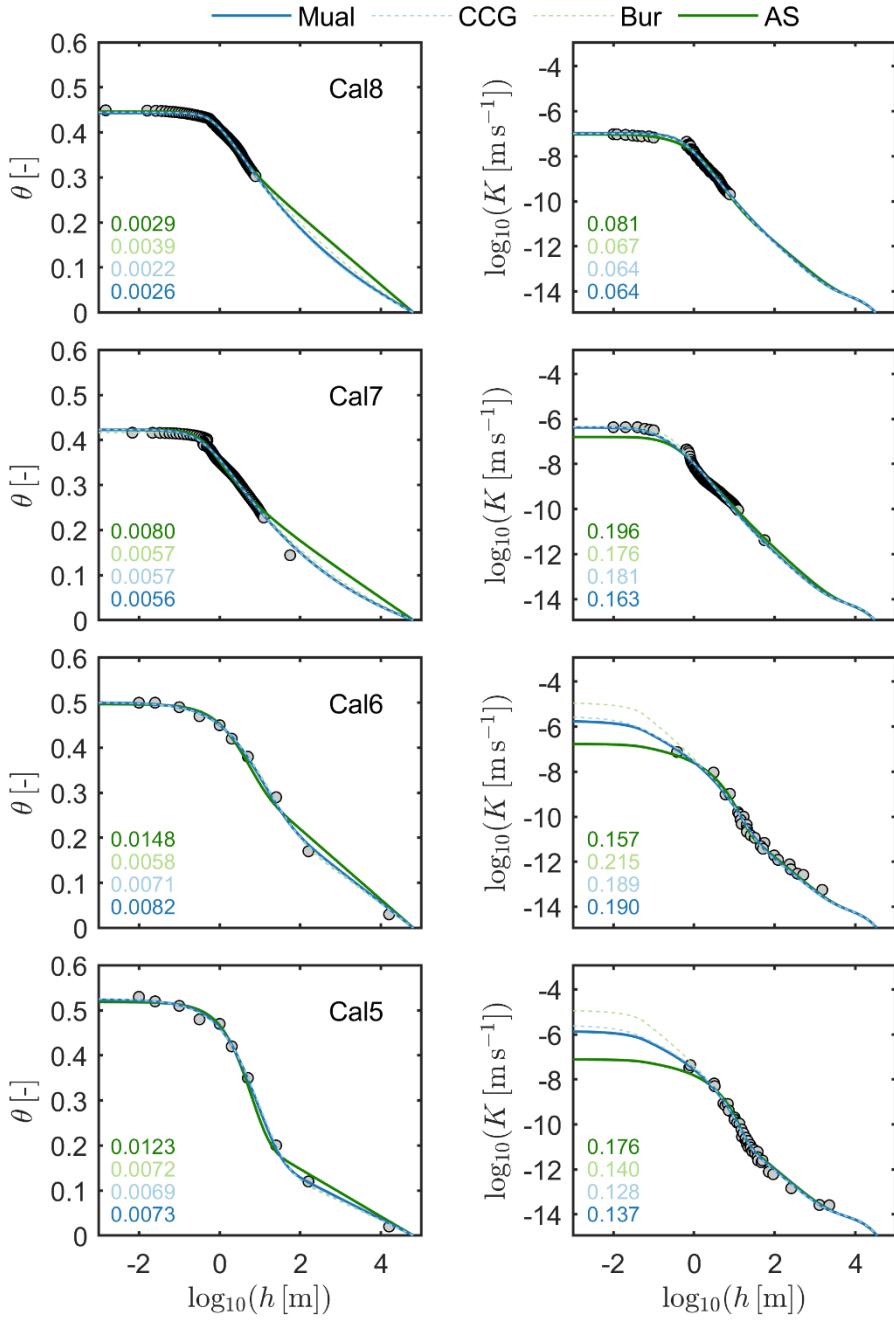
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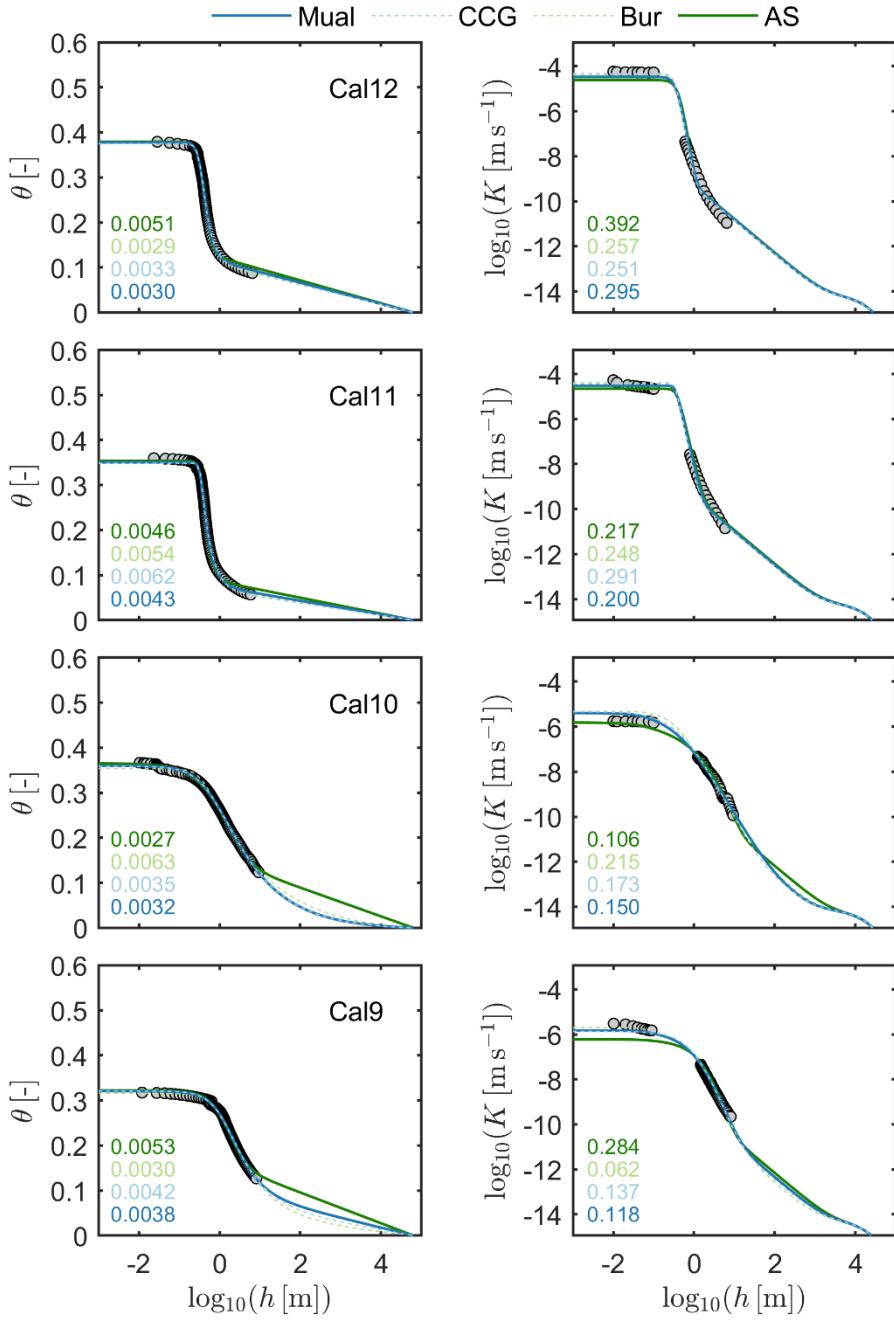
52 Fig. S7: Calibration data sets and the fitted water retention and conductivity functions used to
 53 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 1 to 4 of the 12 calibration data
 54 sets and the **vGmn-PDI** retention model combined with the 4 capillary bundle models. Parameter τ_s
 55 and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE $_{\theta}$ and
 56 RMSE $_{\log K}$ values for the various model combinations.

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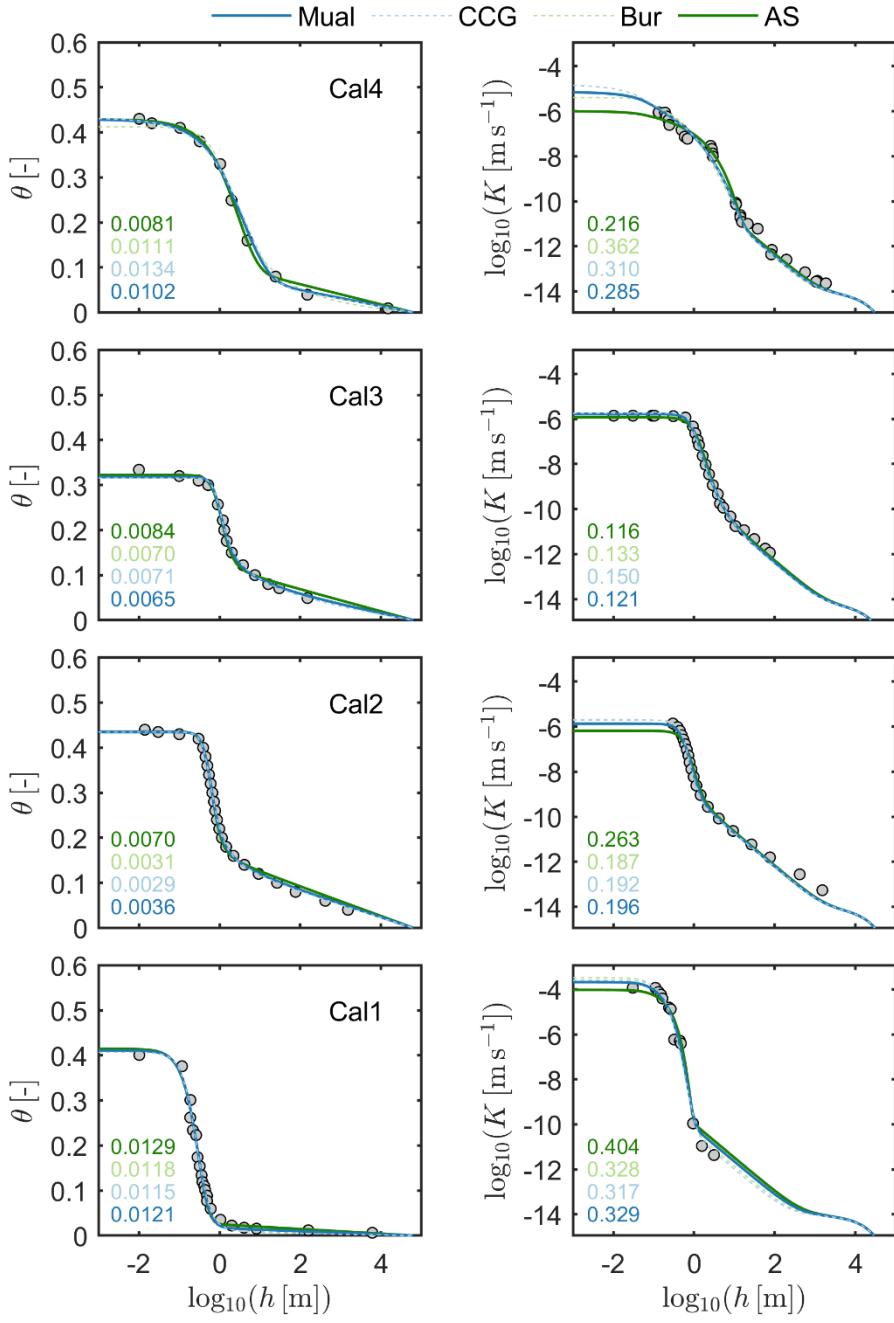
59 Fig. S8: Calibration data sets and the fitted water retention and conductivity functions used to
60 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 5 to 8 of the 12 calibration data
61 sets and the vGmn-PDI retention model combined with the 4 capillary bundle models. Parameter τ_s
62 and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE_{θ} and
63 $\text{RMSE}_{\log K}$ values for the various model combinations.



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65 Fig. S9: Calibration data sets and the fitted water retention and conductivity functions used to
 66 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 9 to 12 of the 12 calibration data
 67 sets and the **vGmn-PDI** retention model combined with the 4 capillary bundle models. Parameter τ_s
 68 and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE_θ and
 69 $\text{RMSE}_{\log K}$ values for the various model combinations.

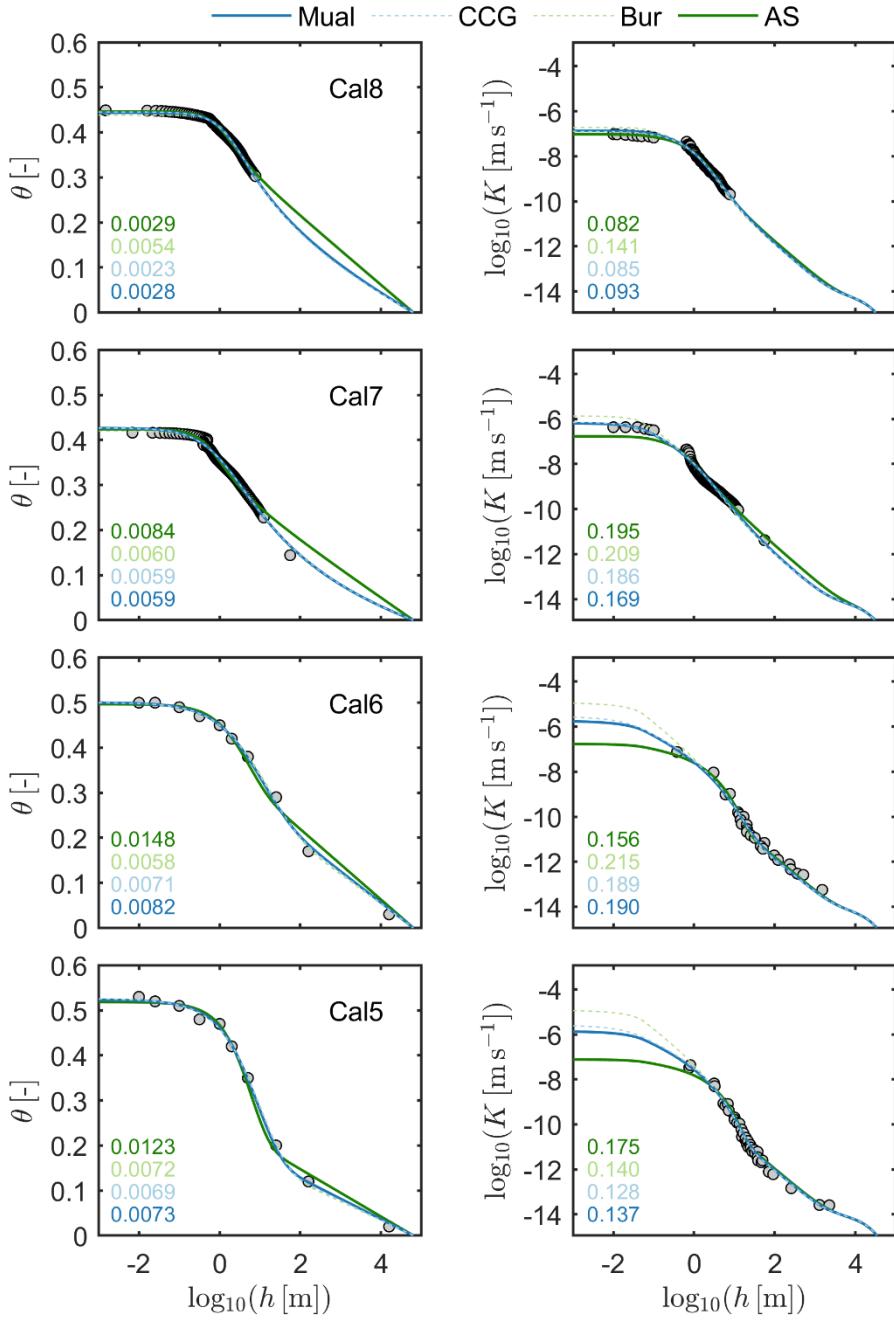
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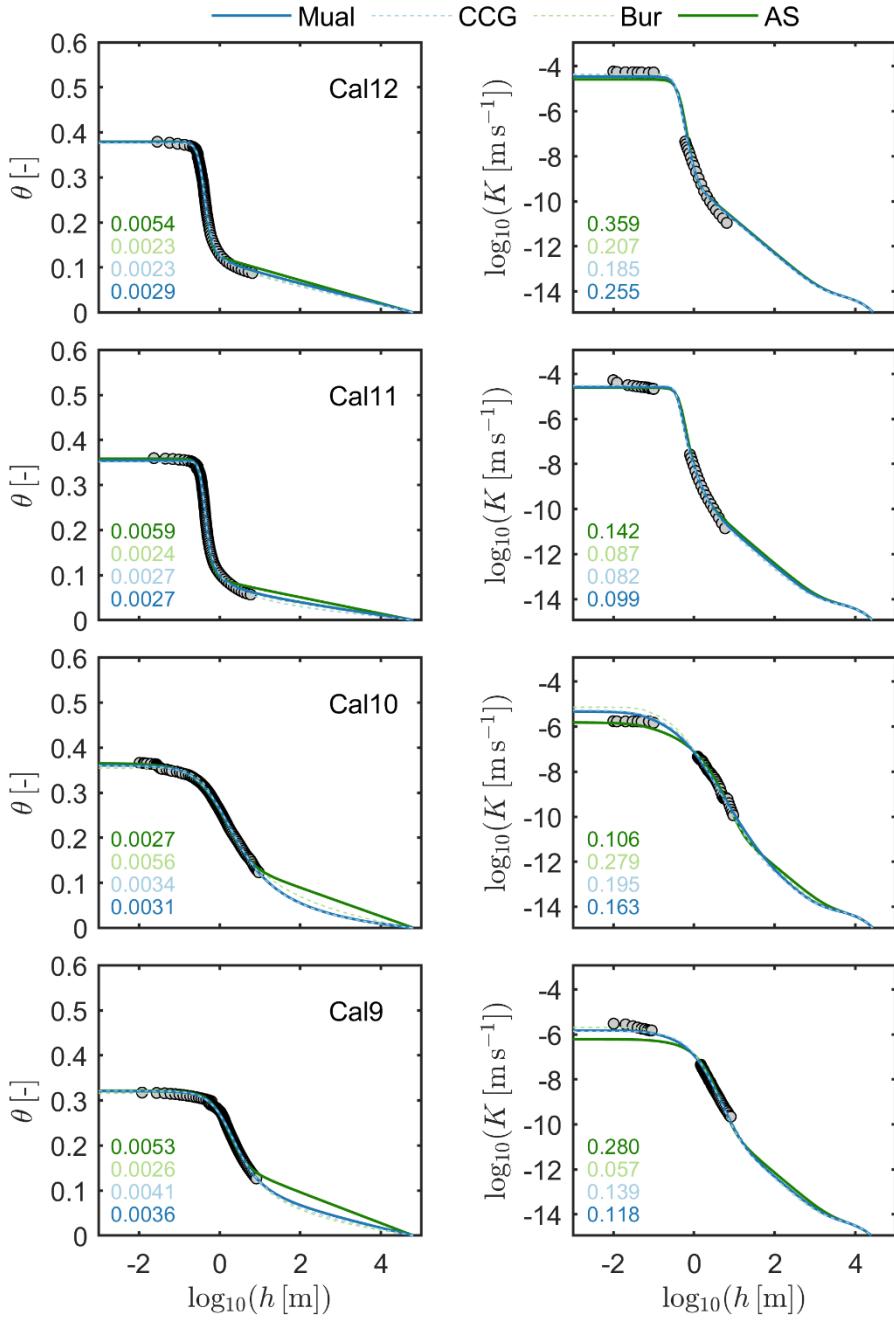
72 Fig. S10: Calibration data sets and the fitted water retention and conductivity functions used to
 73 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 1 to 4 of the 12 calibration data
 74 sets and the **FX-PDI** retention model combined with the 4 capillary bundle models. Parameter τ_s and
 75 the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE_{θ} and
 76 $\text{RMSE}_{\log K}$ values for the various model combinations.

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79 Fig. S11: Calibration data sets and the fitted water retention and conductivity functions used to
80 calibrate the saturated tortuosity coefficient τ_s . Shown are data set 5 to 8 of the 12 calibration data
81 sets and the **FX-PDI** retention model combined with the 4 capillary bundle models. Parameter τ_s and
82 the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE_{θ} and
83 $\text{RMSE}_{\log K}$ values for the various model combinations.



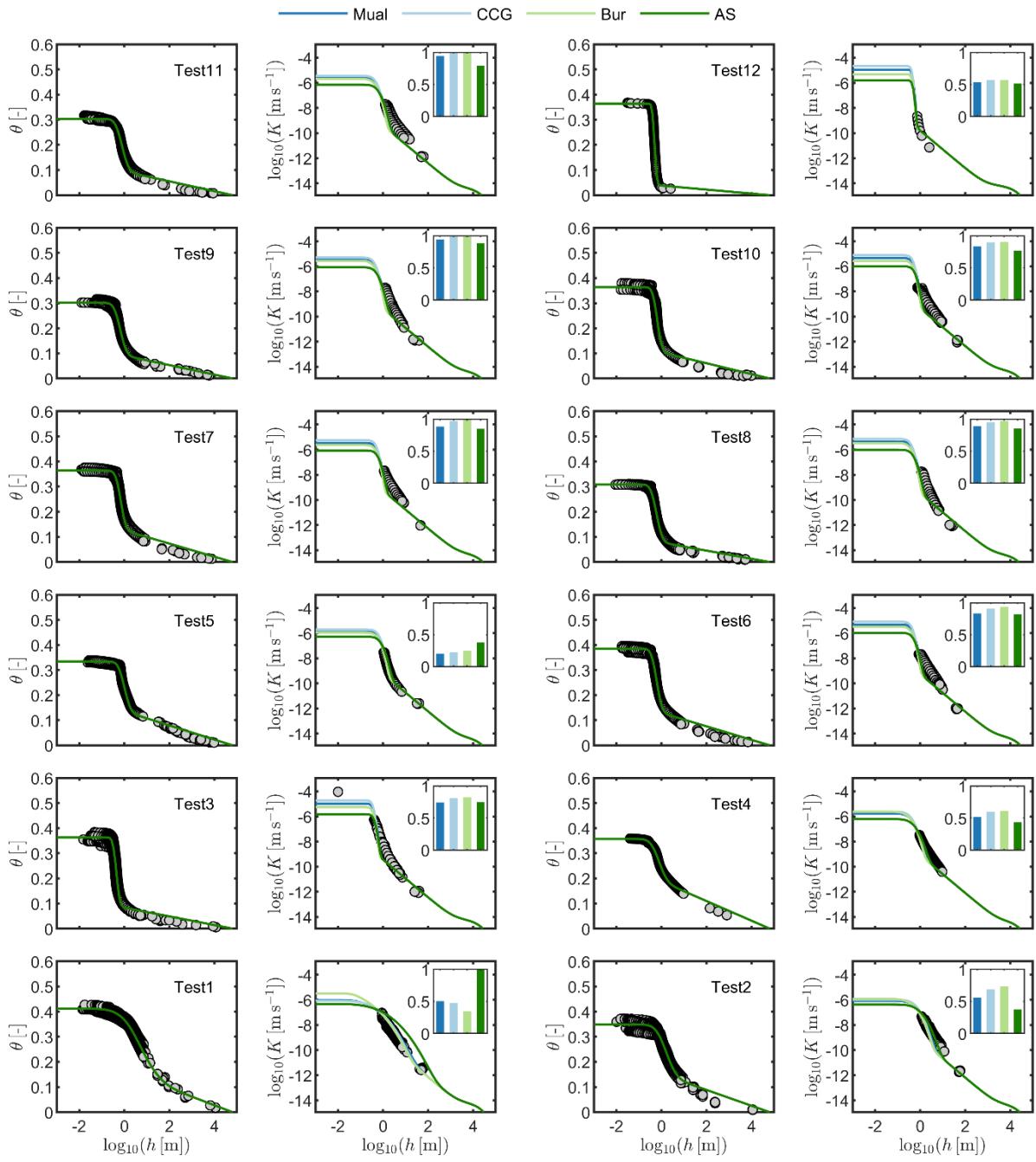
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Fig. S12: Calibration data sets and the fitted water retention and conductivity functions used to calibrate the saturated tortuosity coefficient τ_s . Shown are data set 9 to 12 of the 12 calibration data sets and the **FX-PDI** retention model combined with the 4 capillary bundle models. Parameter τ_s and the retention parameters were allowed to vary. Numbers in the subplots indicate RMSE _{θ} and RMSE _{$\log K$} values for the various model combinations.

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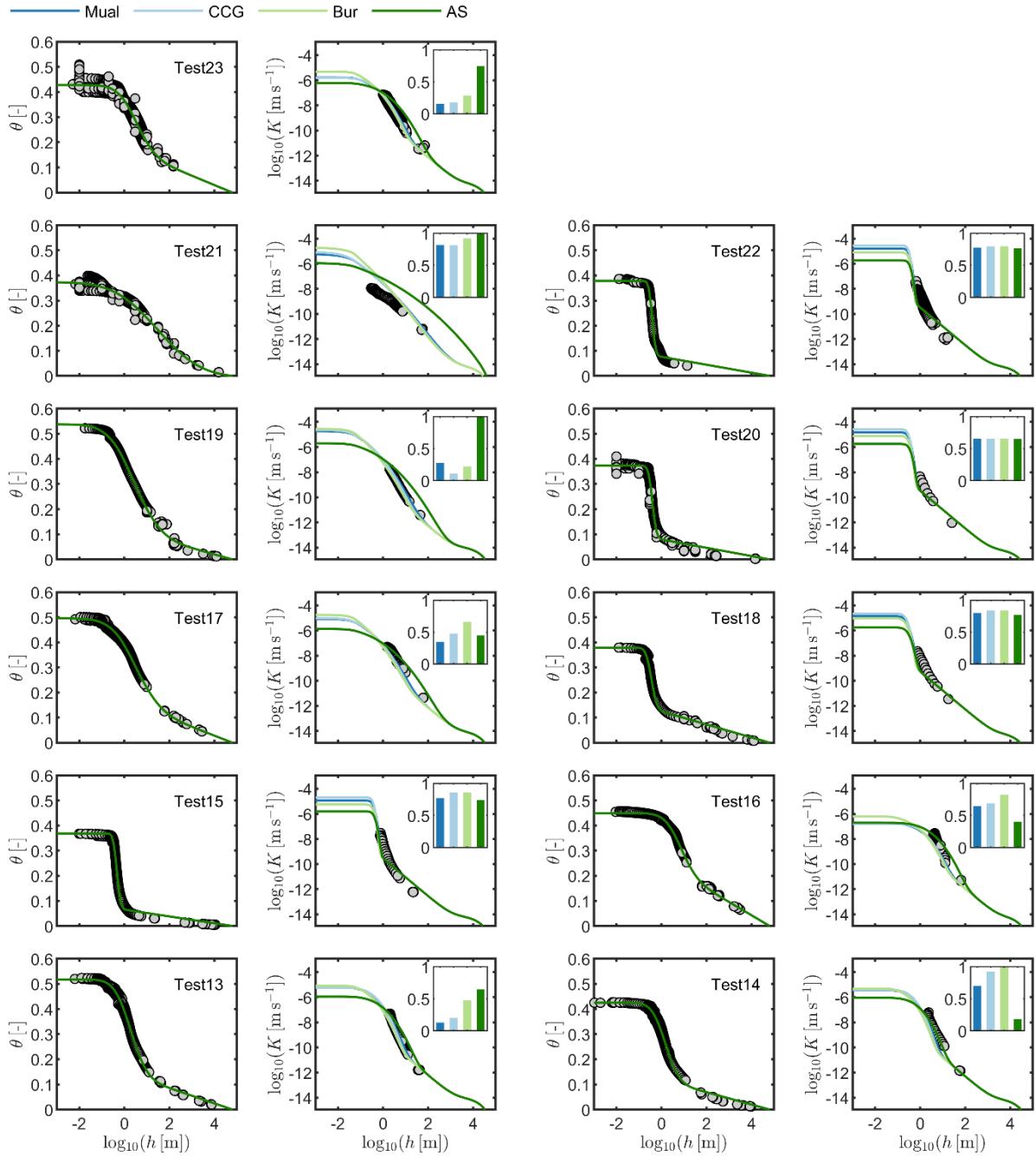
92 **S 1.2: All validation curves (pages 14 to 21)**



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94 Fig. S13: Measured data (dots), fitted retention functions (left) and fully predicted conductivity
 95 functions (right). Shown are the first 12 out of the 23 test data sets and the **Kos-PDI** retention model
 96 combined with the 4 capillary bundle models. Bars show the $\text{RMSE}_{\log K}$ values for the different used
 97 capillary bundle models. Note that the conductivity curves are not fits to the data but pure
 98 predictions.

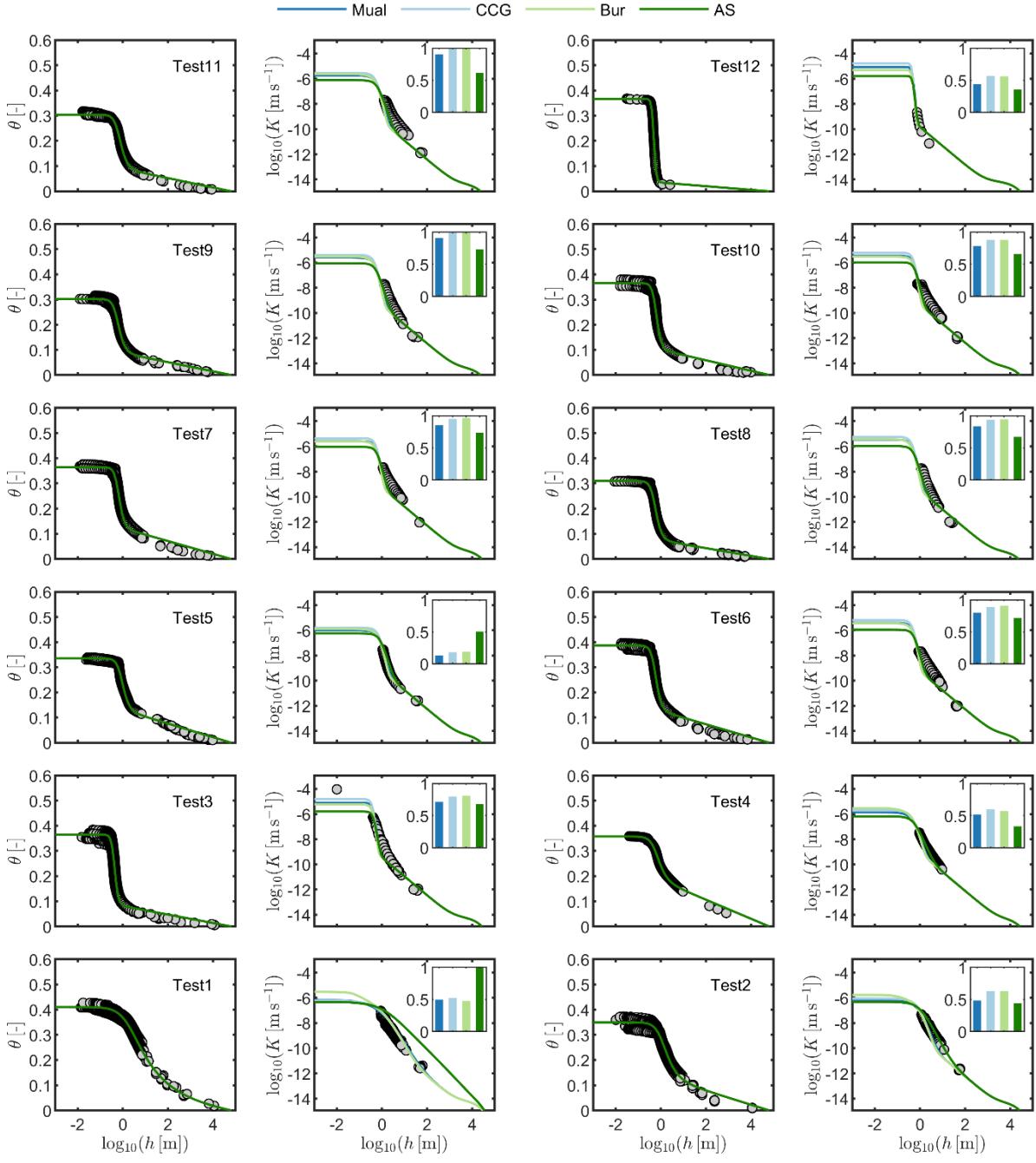
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101 Fig. S14: Measured data (dots), fitted retention functions (left) and fully predicted conductivity
 102 functions (right). Shown are data set 13 to 23 of the test data sets and the **Kos-PDI** retention model
 103 combined with the 4 capillary bundle models. Bars show the RMSE_{logK} values for the different used
 104 capillary bundle models. Note that the conductivity curves are not fits to the data but pure
 105 predictions.

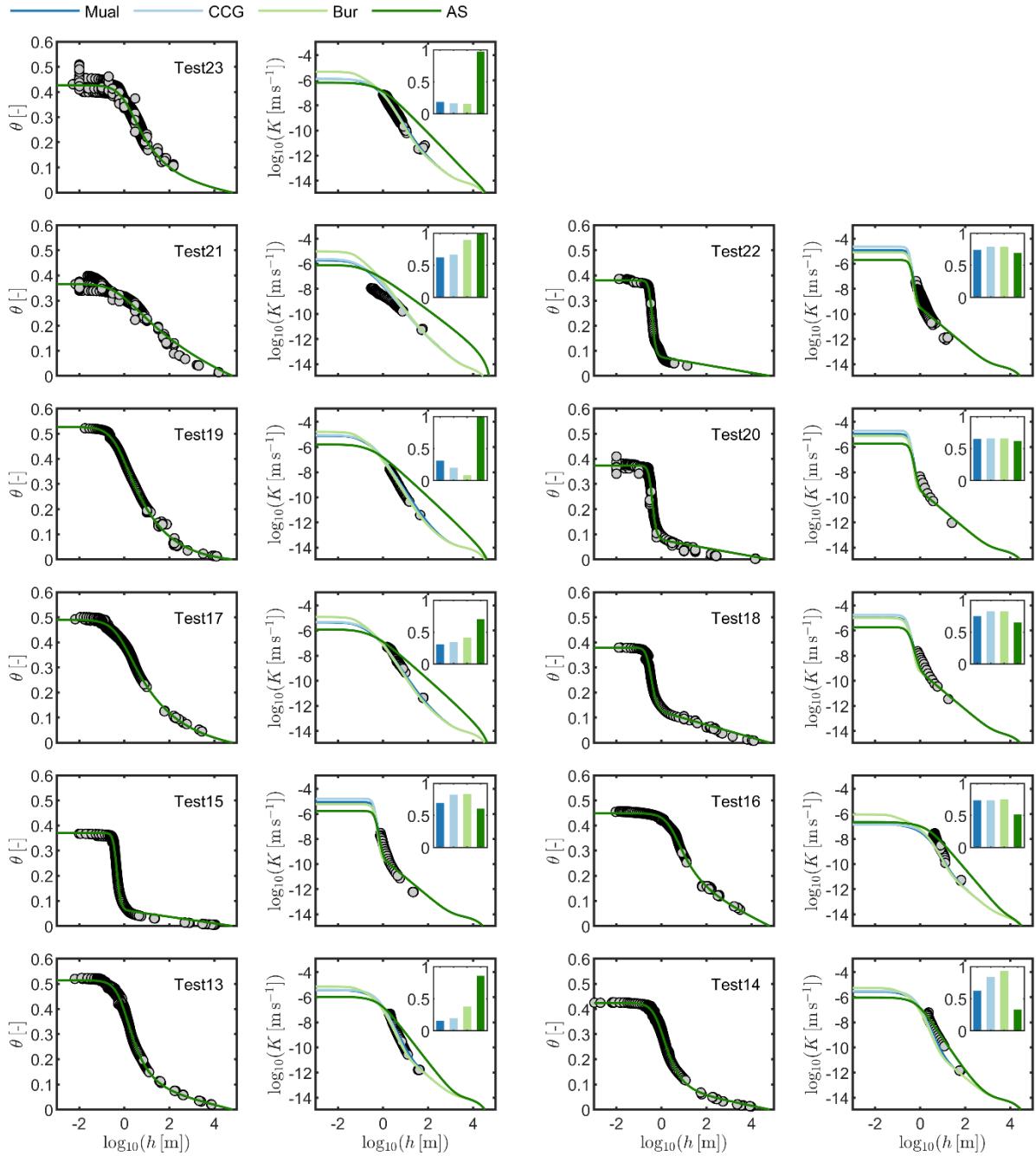
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108 Fig. S15: Measured data (dots), fitted retention functions (left) and fully predicted conductivity
 109 functions (right). Shown are the first 12 out of the 23 test data sets and the **vGc-PDI** retention model
 110 combined with the 4 capillary bundle models. Bars show the RMSE_{logK} values for the different used
 111 capillary bundle models. Note that the conductivity curves are not fits to the data but pure
 112 predictions.

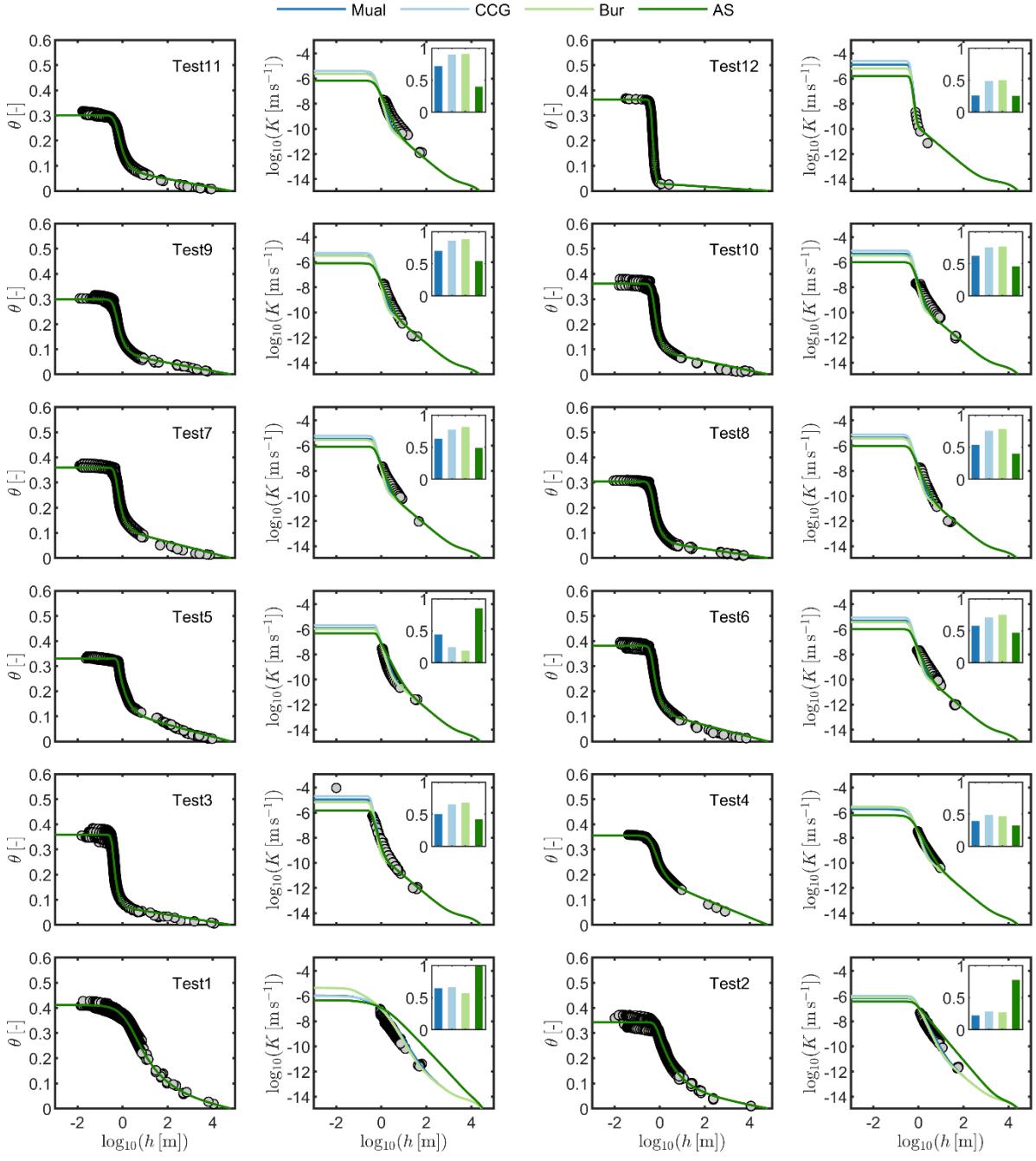
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115 Fig. S16: Measured data (dots), fitted retention functions (left) and fully predicted conductivity
 116 functions (right). Shown are data set 13 to 23 of the test data sets and the **vGc-PDI** retention model
 117 combined with the 4 capillary bundle models. Bars show the RMSE_{logK} values for the different used
 118 capillary bundle models. Note that the conductivity curves are not fits to the data but pure
 119 predictions.

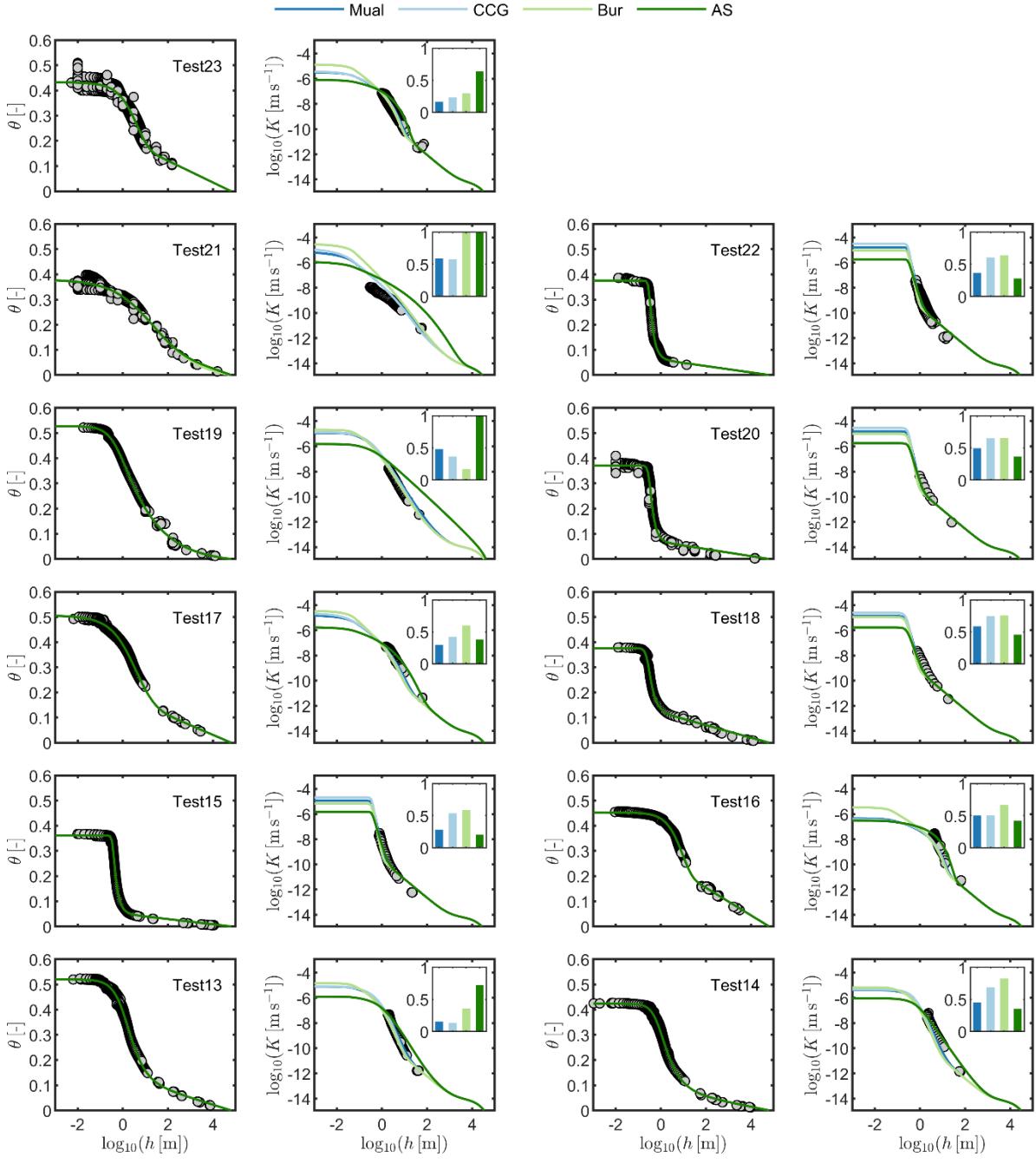
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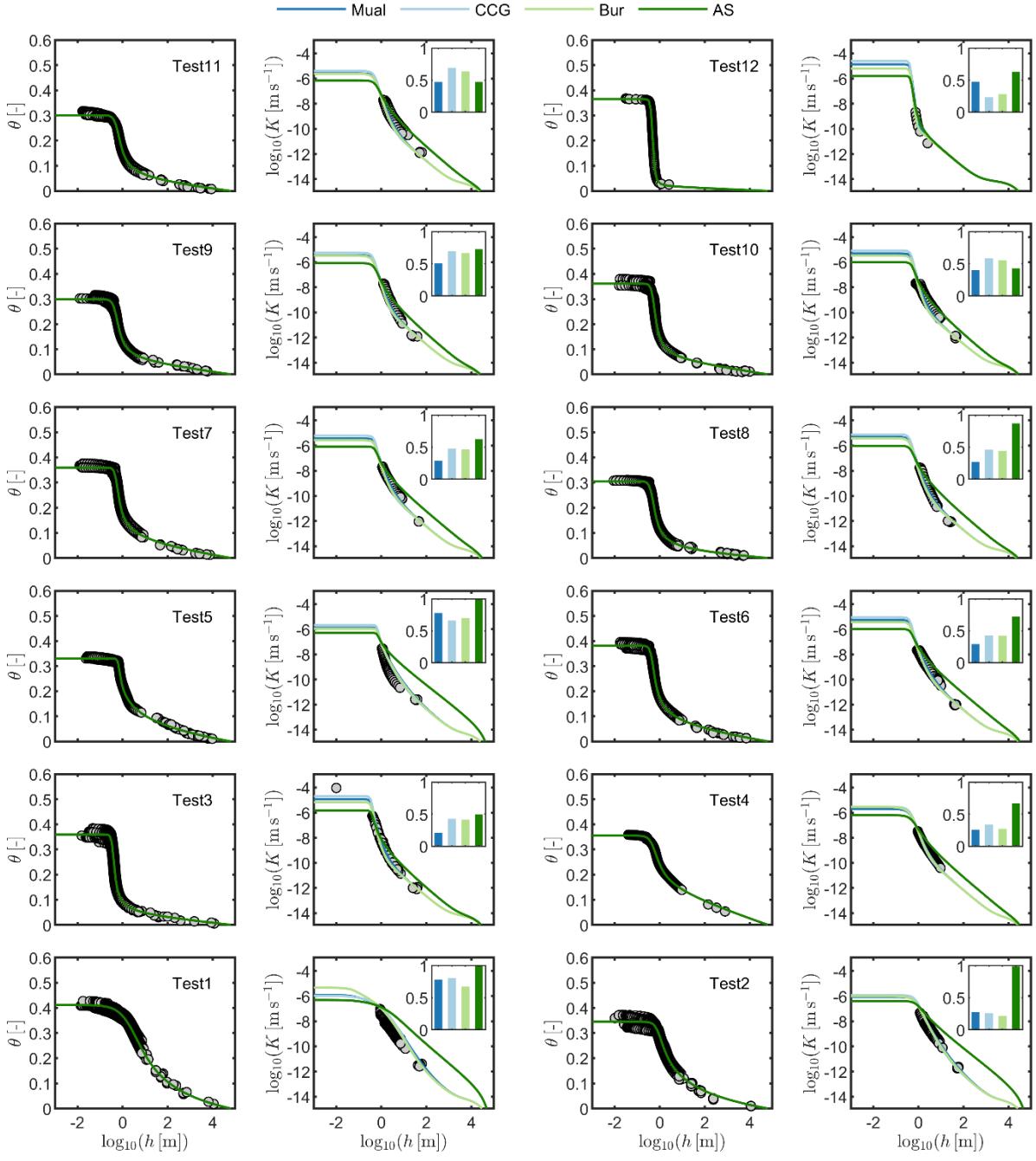
122 Fig. S17: Measured data (dots), fitted retention functions (left) and fully predicted conductivity
 123 functions (right). Shown are the first 12 out of the 23 test data sets and the **vGmn-PDI** retention
 124 model combined with the 4 capillary bundle models. Bars show the RMSE_{logK} values for the different
 125 used capillary bundle models. Note that the conductivity curves are not fits to the data but pure
 126 predictions.

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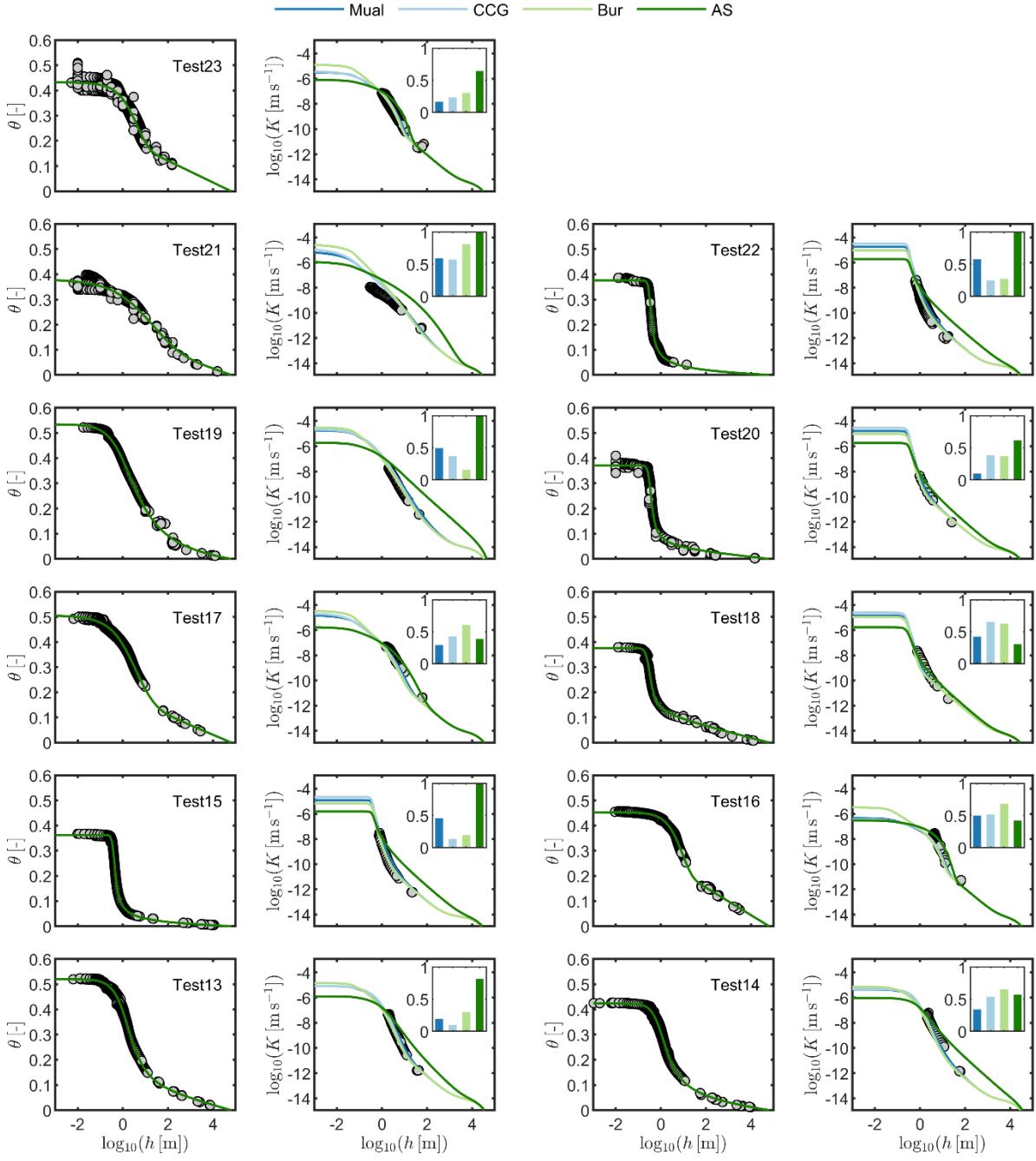
129 Fig. S18: Measured data (dots), fitted retention functions (left) and fully predicted conductivity
 130 functions (right). Shown are data set 13 to 23 of the test data sets and the **vGmn-PDI** retention
 131 model combined with the 4 capillary bundle models. Bars show the RMSE_{logK} values for the different
 132 used capillary bundle models. Note that the conductivity curves are not fits to the data but pure
 133 predictions.



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135 Fig. S19: Measured data (dots), fitted retention functions (left) and fully predicted conductivity
 136 functions (right). Shown are the first 12 out of the 23 test data sets and the **FX-PDI** retention model
 137 combined with the 4 capillary bundle models. Bars show the RMSE_{logK} values for the different used
 138 capillary bundle models. Note that the conductivity curves are not fits to the data but pure
 139 predictions.

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141

142 Fig. S20: Measured data (dots), fitted retention functions (left) and fully predicted conductivity
 143 functions (right). Shown are data set 13 to 23 of the test data sets and the **FX-PDI** retention model
 144 combined with the 4 capillary bundle models. Bars show the RMSE_{logK} values for the different used
 145 capillary bundle models. Note that the conductivity curves are not fits to the data but pure
 146 predictions.

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