

Operationalizing equity in multipurpose water systems

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5 **Abstract** Participatory decision-making is a well-established approach to address the increasing pressure on water systems induced by growing multi-sectoral demands and increased competition among different water users. Yet, most existing approaches search for system-wise efficient solutions and do not quantify their distributional effect among the stakeholders. In this work, we investigate how to operationalize equity principles to design improved water systems operations that better balance efficiency and justice. More specifically, we explore to which extent the inclusion of equity principles reshapes the space of efficient solutions. Numerical experiments are conducted on the Lake Como system, Italy, operated primarily for flood control and irrigation water supply while also providing recreation and river ecosystem services. Our results show how incorporating equity considerations into the design of water system operations enriches the solution space by generating more compromise solutions than those obtained using a traditional multi-objective optimization. Moreover, we find that including equity in the operating policy design can indirectly improve the performance of marginalized sectors, such as recreation and ecosystem, which are not explicitly considered by the current lake operation. Lastly, we illustrate how the aggregation of multi-sectoral interests into an equity index strongly shapes our results. Eliciting the preference structure of stakeholders and policymakers thus becomes paramount for the identification of a fair balance across competing interests. This work bridges the gap between multi-objective optimization approaches and equity-informed decision-making for real-world water resources planning and management, providing an effective tool to promote efficient and equitable policies.

20 1. Introduction

Proper operation of existing water systems is widely recognized as one of the most important and cost-effective ways to improve water use efficiency and reduce stresses caused by rapid population growth and socio-economic development (Ehsani et al., 2017; Giuliani et al., 2016a; Olsson, 2015). Water reservoirs generally serve multiple and competing purposes, including flood control, irrigation, power generation, navigation, and river ecosystem maintenance, but limited water resources make it impossible to fully and simultaneously satisfy all these water users (Billington and Jackson, 2006; Groenfeldt, 2019). At the same time, growing energy and food demands are putting additional pressure on these systems and are exacerbating conflicts (Ehsani et al., 2017; Giuliani et al., 2016a; Olsson, 2015), which are often related to emerging adverse social and environmental consequences caused by water infrastructure (Graham et al., 2020; Poff et al., 2016; Poff and Schmidt, 2016; Sabo et al., 2017; Schmitt et al., 2018) and to water security (D'Odorico et al., 2018; Liu et al., 2018; Scanlon et al., 2017). These challenges represent a well-established topic in the water systems analysis community since the Harvard Water Program (Maass et al., 2013), promoting the idea of adopting an a-posteriori decision making based on trade-off analysis between competing objectives (Cohon and Marks, 1975; Maier et al., 2014; Nicklow et al., 2010; Reed et al., 2013).

Traditionally, water system operations are formulated as multi-objective decision-making problems and the underlying conflicts among objectives capturing the interests of different stakeholders yield a set of Pareto optimal (or efficient) solutions rather than a single optimal solution (Loucks and Van Beek, 2017). A solution is defined as being Pareto optimal (or nondominated) if no other solution gives a better value for one objective without degrading the performance in at least one other objective. In this context, most existing approaches search for the Pareto optimal set to explore trade-offs between operating objectives (Geressu and Harou, 2019; Giuliani et al., 2014; Kasprzyk et al., 2009; Schmitt et al., 2018). Yet, Pareto

optimality pursues system-wise efficiency and ignores the distributional effects of the optimal solutions among the different stakeholders, potentially resulting in inequitable outcomes. Equity here is defined as “the provision of a consistent minimum quality and quantity, determined at the local level, of water services to all end-users” (Osman and Faust, 2021). The potential inconsistency between efficiency and equity might inadvertently bias the analysis on efficient but unfair solutions that the stakeholders will hardly accept (Cai et al., 2002; Cai et al., 2003; Cai, 2008; Loucks, 1997), while including equity among the objectives can be useful to ensure that the negotiations on the solution to be implemented succeed smoothly (Jafino et al., 2021).

There is a growing interest in equity-related research in the water resources literature, with Fletcher et al. (2022) recently offering some actionable recommendations about the integration of equity into the water resources planning. For example, Wang et al. (2008) developed a cooperative water allocation model to achieve fair and efficient water allocation among competing stakeholders at the basin level. Girard et al. (2016) designed cost-effective and equitable portfolios for water resource adaptation to climate change in the Orb River basin by implementing cooperative game theory and social justice approaches. Siddiqi et al. (2018) developed a set of reliability and equity metrics to quantitatively evaluate the water security in a canal irrigation system in the Indus basin. Ciullo et al. (2020) proposed a decision criterion to account for the geographical distribution of flood risk in the transboundary area of the German-Dutch Lower Rhine River and investigate the impact of equity criteria on flood risk management. Gullotta et al. (2021) improved the equity among users of a water distribution network in northern Italy by optimizing the placement of control valves to maximize the uniformity coefficient (an equity index proposed in (Gottipati and Nanduri, 2014)). Kazemi et al. (2020) optimized the water allocation in the Sefidrud basin in Iran for the maximum water use revenue and minimum Gini index (which was introduced by Gini (1921) to measure income inequality). Although these works promote equity in water resource systems by fairly distributing benefits or risks, the impacts of equity on multi-objective decision-making and how equity affects the trade-offs between conflicting objectives have not yet been studied.

In this work, we investigate how to operationalize equity principles into the multi-objective design of improved water systems operations that better balance trade-offs among competing stakeholders’ interests. The approach is demonstrated on the Lake Como system, a regulated lake in Northern Italy historically operated for flood protection and irrigation supply. Over the last few years, the increasing frequency and intensity of severe droughts emphasized the importance of additional, so far marginalized services provided by the lake operations, such as preventing low lake levels for supporting recreational activities and ecosystem preservation downstream of the lake.

The paper provides two main contributions. First, we analyze alternative problem formulations to assess how the inclusion of equity principles reshapes the space of efficient solutions with respect to both a traditional optimization considering only primary objectives and an inclusive optimization that account for primary as well as historically marginalized objectives. Second, we explore the sensitivity of the resulting solutions with respect to the definition of the equity metric, which, in a multi-objective problem, requires the aggregation of multiple objective functions into a single index (e.g., coefficient of variation). Since aggregated objective functions might adversely bias the designed alternatives in unpredictable ways (Kasprzyk et al., 2016), this is an important aspect to explore for effectively operationalizing equity in multipurpose water systems. Moreover, the aggregation of primary and marginalized objectives into an equity index makes our approach a hybrid method that blends a-posteriori decision making with an aggregated objective formulated a-priori, which can become particularly promising to stretch our ability to solve multi-objective problems with high numbers of objectives.

The rest of the paper is organized as follows: in the next section, we introduce the Lake Como study site, while Sect. 3 describes the adopted methodology. Then, results and discussion are reported in Sect. 4, while conclusions and final remarks are presented in the last section.

80 2. Study Site

Lake Como, also known as Lario, is the third-largest lake in Italy and the fifth deepest lake in Europe; it has an active storage capacity of 254 million m³ and a depth of over 400 m. The catchment area of Lake Como is approximately 4,552 km², with the lake serving an irrigation-fed cultivated area of about 1,300 km² (Fig. 1). The major crops within the agricultural area include cereals, maize, and temporary grasslands for livestock. The climate of Lake Como is temperate around the lake and cold in the upper alpine catchment (Peel et al., 2007). The hydrologic regime is snow-rainfall dominated, with the dry seasons in winter and summer and wet seasons in late spring and autumn, respectively.

The lake's shape is close to an inverted letter “Y” and the city Como is located at its southwestern branch. Because of the dead-end and the lowest elevation on the lake shoreline at Como, this area is prone to flooding. Thus, the regulation of Lake Como has been historically studied mostly by looking at the conflict between irrigation water supply and flood control (Denaro et al., 2017; Giuliani et al., 2020; Guariso et al., 1986). Spring/summer snowmelt primarily creates the seasonal storage of Lake Como, which can be reallocated to satisfy the summer water demand peak for irrigation. Storing more water in spring will benefit the irrigation water supply in summer; however, this strategy could lead to high lake levels for longer periods and thus increase flood risk.

Lake Como is also a popular tourist destination because of its beautiful Alpine landscape and abundant wildlife, and it is a scenic spot for sailing, boating, and windsurfing. Interests related to ecosystems, tourism, navigation, and fishing are also attracting more and more attention in Lake Como water governance in recent years (Carvalho et al., 2019; Grizzetti et al., 2016). Accordingly, the Lake Como operation design can be formulated as a problem that involves up to four competing objectives, where recreation services (e.g., tourism and navigation) and river ecosystem maintenance downstream of the lake are added to irrigation water supply and flood control.

100 3. Methods and Tools

3.1. Model description

The model of the system reproduces the dynamics of Lake Como by using a mass-balance equation of the lake storage s_t (m³) assuming a modeling and decision-making time step $\Delta t = 24$ hours, where the lake releases are determined by the lake operating policy:

$$105 \quad s_{t+1} = s_t + (q_{t+1} - r_{t+1}) \cdot \Delta t \quad (1)$$

where q_{t+1} (m³/s) and r_{t+1} (m³/s) are the net inflow (i.e., inflow minus evaporation losses) to the lake and the actual lake release in the time period $[t, t+1)$, respectively. Specifically, the release volume r_{t+1} is determined by a non-linear, stochastic function that depends on the release decision u_t (Soncini-Sessa et al., 2007) and accounts for the effect of the uncertain inflows between the time t (at which the decision is taken) and the time $t+1$ (at which the release is completed). The release r_{t+1} does not necessarily equal the decision u_t due to existing legal and physical constraints on the lake level and release (e.g., spills, dead storage). According to the daily time step, the Adda River can be described by a plug-flow model to simulate the transfer of the lake releases from the lake outlet to the intake of the irrigation canals. The water diversions from the Adda River into the irrigation canals are regulated by the water rights of the agricultural districts.

The lake operating policies that determine the release decision u_t are defined as Gaussian radial basis functions (RBFs; Buşoniu et al. (2011)) as follows:

$$u_t = \alpha + \sum_{k=1}^K \omega_k \varphi_k(X_t) \quad t = 1, \dots, H \quad 0 \leq \varphi_k \leq 1 \quad (2)$$

$$\varphi_k(X_t) = \exp \left[-\sum_{j=1}^M \frac{((X_t)_j - c_{j,k})^2}{b_{j,k}^2} \right] \quad c_{j,k} \in [-1,1], b_{j,k} \in (0,1] \quad (3)$$

where K is the number of RBFs, ω_k is the weight of the k^{th} RBF, M is the number of input variables X_t , and \mathbf{c}_k and \mathbf{b}_k are the M -dimensional center and radius vectors of the k^{th} RBF, respectively. Lake level h_t , previous day inflow q_t , and the day of the year τ_t are used as input variables (i.e., $X_t = (s_t, q_t, \tau_t)$), and the number of RBFs is set to four ($K=4$) which proves effective in our previous works (Giuliani et al., 2016b; Giuliani et al., 2020). The final parameters vector can be summarized as: $\theta = [\alpha, \omega_k, c_{j,k}, b_{j,k}]$, and it thus contains 29 parameters (decision variables) to determine the release decision u_t . The operating policies are then optimized using the Evolutionary Multi-Objective Direct Policy Search (EMODPS) method (Giuliani et al., 2016b), a Reinforcement Learning approach that combines direct policy search, non-linear approximating networks, and multi-objective evolutionary algorithms.

3.2. Operating objectives

Building on previous works (Galelli and Soncini-Sessa, 2010; Giuliani and Castelletti, 2016; Giuliani et al., 2016c; Zaniolo et al., 2021), we formulate four objectives capturing the competing interests introduced in the previous section as follows

(a) Flood control: the high-level reliability (to be maximized) defined as

$$J^F = 1 - \frac{n_F}{H} \quad (4)$$

where n_F is the number of days in the evaluation horizon H during which the lake level is above a flood level threshold.

(b) Irrigation water supply: the daily average volumetric reliability (to be maximized) defined as

$$J^I = \frac{1}{H} \sum_{t=1}^H \left(\min \left(\frac{Y_{t+1}}{w_t}, 1 \right) \right) \quad (5)$$

where Y_{t+1} (m^3) is the daily volume of water available for irrigation, subject to the minimum environmental flow constraint to ensure adequate environmental conditions in the Adda River downstream of the abstraction point, and w_t (m^3) is the corresponding irrigation demand.

(c) Recreation services: the low-level reliability (to be maximized) defined as

$$J^R = 1 - \frac{n_R}{H} \quad (6)$$

where n_R is the number of days in the evaluation horizon H during which the lake level is below a time-varying, low-level threshold equal to the 10th percentile of the historical lake level.

(d) River ecosystem: the reliability of environmental flow (to be maximized) defined as

$$J^E = \frac{n_E}{H} \quad (7)$$

where n_E is the number of days in the evaluation horizon H during which $q_t^n - \sigma_t^n \leq r_{t+1} \leq q_t^n + \sigma_t^n$, with q_t^n and σ_t^n representing the mean and standard deviation, respectively, of the Adda river flow in natural conditions. It is worth noting that the ecosystem in the case study is sensitive to both high and low flows, thus the target of maintaining the lake release within a range approximating the natural variability instead of considering only a minimum flow threshold as traditionally done in the literature.

3.3. Operationalizing equity

The equity index considered in this study is formulated as in Siddiqi et al. (2018) as the ratio between the standard derivation (σ) and mean (μ) of the performance in the four objectives introduced in the previous section, i.e.

$$\zeta = \frac{\sigma(J^F, J^I, J^R, J^E)}{\mu(J^F, J^I, J^R, J^E)} \quad (8)$$

The lower the value of ζ , the more equitable the solution is, with low values of ζ obtained for high values of the original objectives with a limited performance dispersion across the four objective functions. When the objectives capturing diverse stakeholders' interests are expressed in different units of measure or explore different performance ranges, it could be necessary to map the original objectives into a satisfaction value by applying a value function. The latter allows re-scaling all the objectives into a dimensionless scale, e.g., from 0 to 1, by means of a linear or non-linear transformation. Assessing the equity index by computing the mean and standard deviation of satisfaction values rather than objectives is expected to improve the analysis by working on commensurable quantities.

Yet, the ranges of performance attained by the different sets of solutions across the four objectives could be not identical. Using the equity index directly computed by aggregating the reliability performance across the four objectives may lead to some bias in the equity assessment, especially when the minimum and maximum performance values are significantly different. For example, if the ranges of J^F and J^E are $[0.7, 1.0]$ and $[0.6, 0.9]$, a fair solution having 0.85 reliability in all objectives would imply that J^E would be highly satisfied as the 0.85 is close to the maximum value of 0.9; conversely, the performance in J^F would be only intermediate as the 0.85 is still much lower than the maximum value of 1.0. To mitigate this bias, a value function can be used to first transform each objective into a satisfaction value expressed in a dimensionless scale (e.g., from 0 to 1), with the equity index computed by aggregating the satisfaction values as follows:

$$\zeta' = \frac{\sigma[f^F(J^F), f^I(J^I), f^R(J^R), f^E(J^E)]}{\mu[f^F(J^F), f^I(J^I), f^R(J^R), f^E(J^E)]} \quad (9)$$

where $f^F(\cdot)$, $f^I(\cdot)$, $f^R(\cdot)$, and $f^E(\cdot)$ are the value functions of J^F , J^I , J^R , and J^E , respectively.

To explore the sensitivity of our results with respect to the use of different value functions, in this work, we examine the impacts of adopting both a linear and a non-linear value function (see Figure 2). The linear value function maps a performance value x to x' in the range $[0, 1]$ where these extremes correspond to the lowest and highest values of reliability across all the solutions, respectively. In the non-linear value function, we hypothesized a function that requires high values of J^F and J^I to get high values of satisfaction in these objectives as the historical operation of the Lake Como is primarily looking at flood control and irrigation water supply while accepting lower levels of reliabilities in terms of J^R and J^E . It should be noted that the purpose of this experiment is only testing the sensitivity of the equity index to the use of different values functions rather than capturing the preference structure of real stakeholders.

3.4. Experimental settings

As mentioned before, the Lake Como operator traditionally considers two primary objectives (irrigation water supply and flood control). More recently, other needs such as recreation services and river ecosystem maintenance are emerging due to increasingly frequent droughts, which motivates us to investigate how to fairly account for these previously marginalized objectives into the policy design. In this work, we contrast four rival formulations of the Lake Como EMODPS problem (Table 1) that can be summarized as follows:

- F1 – traditional formulation: $\theta^* = \arg \max_{\theta} \mathbf{J}(\theta) = |J^F, J^I|$
- F2 – traditional & fair formulation: $\theta^* = \arg \max_{\theta} \mathbf{J}(\theta) = |J^F, J^I, -\zeta|$
- F3 – inclusive formulation: $\theta^* = \arg \max_{\theta} \mathbf{J}(\theta) = |J^F, J^I, J^R, J^E|$
- F4 – inclusive & fair formulation: $\theta^* = \arg \max_{\theta} \mathbf{J}(\theta) = |J^F, J^I, J^R, J^E, -\zeta|$

F1 is a traditional multi-objective optimization problem that only searches for the maximum of the two primary objectives. F3 is an inclusive optimization that instead considers all four objectives. Finally, F2 and F4 add the equity index from equation (8) to the traditional and inclusive formulations, respectively. While the comparison between the traditional and inclusive formulations will provide the benefit of including all objectives into the policy design, the comparison between F1 vs. F2 and F3 vs. F4 will focus on assessing the value of including an equity-related objective function in either the traditional multi-objective optimization and the inclusive optimization problems. Finally, the comparison between F2 and F3 allows investigating the differences between using the equity index as a means for indirectly including in the problem formulation the traditionally marginalized objectives or formulating an inclusive optimization that directly includes all stakeholders' interests as separated objectives.

Table 1 Summary of the alternative problem formulations.

Formulation	Name	Objectives	Including equity (YES/NO)
F1	Traditional	J^F, J^I	NO
F2	Traditional & fair	J^F, J^I, ζ	YES
F3	Inclusive	J^F, J^I, J^R, J^E	NO
F4	Inclusive & fair	$J^F, J^I, J^R, J^E, \zeta$	YES

The parameters in RBFs-based policies are optimized using the Borg MOEA evolutionary algorithm (Hadka and Reed, 2013) which proves highly robust in solving many-objective control policy optimization problems (Salazar et al., 2016). The number of the function evaluations is 2 million, the same as in previous Lake Como operation optimization (Denaro et al., 2017). To ensure solution diversity and reduce the impact of stochastic factors on the optimal solutions, each optimization was randomly repeated ten times (i.e., the final set of nondominated solutions for each formulation are obtained from 10 random optimization trials). In total, the analysis comprises 80 million simulations that required approximately 600 computing hours on an Intel Xeon E5-2660 2.20 GHz with 32 processing cores and 96 GB RAM.

4.1. Multi-objective optimization and equity operationalization

The optimization results of problems F1-F4 can be evaluated in terms of four operation objectives along with the equity index using the parallel coordinates plots in Figure 3, where each line crossing multiple axes represents one Pareto optimal solution. The leftmost axis represents different problem formulations (e.g., the value “2” refers to F2; apart from the axis, the line color is also used to differentiate various problem formulations), and other axes represent solution performance in terms of flood control, irrigation water supply, recreation, environment, and equity. The axis for equity is reversed to ensure that the direction of preference is always upward, and the ideal solution would thus be a horizontal line at the top of each plot. The diagonal lines between adjacent axes infer the conflicts between different objectives. The density distributions of the solutions’ performance across the four formulations is illustrated in Supplementary Figure S1.

215 According to Figure 3 (a), different problem formulations generate diverse solution spaces. F1 attains good performance in the objectives J^F and J^I (up to 0.99 and 0.91, respectively) that this formulation is optimizing, but low performance on the non-optimized objectives J^R and J^E (lower than 0.67 and 0.72, respectively). Consequently, the equity of these solutions across the four objectives is low. Moving from F1 to F2 allows the attainment of better equity values, which, however, induces performance degradation in terms of J^F . The inclusive optimization supports the full exploration of the trade-offs between the four objectives, **remarkably improving J^R but degrading the performance in terms of J^F and J^I** (i.e., the maximum performance in J^R is equal to 1, while the worst solution in flood and irrigation supply is much lower than with F1 or F2). Notably, the solutions of F3 attain worse values of equity than the solutions of F2. Lastly, moving from F3 to F4 produces a small improvement in terms of equity with minor differences in the performance across the four objectives. Interestingly, F2 generates solutions that perform very well in terms of J^E although this objective is not directly included in the optimization, but only indirectly considered through the minimization of ζ . This happens because the upper bound of J^E in F1 is much lower than other objectives, and thus the equity index tends to decrease as the value of J^E increases. Optimizing equity can therefore be a way for improving the objective(s) of marginalized stakeholders with the lowest level of satisfaction (e.g., the J^E with the lowest upper bound in this case study). **It needs to be noted that F3 which directly includes J^E should theoretically outperform F2 in the environmental objective. The difference in the best environment performance between F2 and F3 is likely attributable to the increasing challenges introduced by the additional objectives considered in this work. According to the boxplot of best performance of 10 random optimization trials reported in Supplementary Figure S2, the median of the best performance of F2 and F3 is indeed almost equivalent. Moreover, a new problem formulation F3b including flood, irrigation, and environment (i.e., removing the recreation objective from F3 to have the same number of objectives as F2) can obtain better performance than F2 by directly optimizing the environment. Including in F3 an additional and strongly conflicting objective (recreation) makes the search for the best environment more challenging.**

To better quantify the differences in the solutions obtained with F1-F4, we computed the Hypervolume indicator along with the best and worst performance in each objective across the four formulations (see Figure 4). Results show that F3 and F4 have similar and the highest hypervolume, followed by F2, while F1 has much lower hypervolume. Apparently, non-dominated solutions obtained from F3 and F4 tend to be efficient on J^R and J^E , which are not explicitly optimized in F1 and F2. **It needs to be noted that formulation F2 attains a very good performance in the environment objective because the upper bound of J^E is lower than other objectives, and thus the equity index tends to improve as the value of J^E increases.**

To further understand the benefit of adding an equity objective to both the traditional (F1) and the inclusive (F3) formulations, in Figure 5 we compute the number of compromise solutions for each formulation considering only the policies that exceed

245 increasing performance thresholds in all objectives. There are 0, 47, 30, and 49 solutions having reliability greater than 0.85
in all objectives in F1, F2, F3, and F4, respectively, clearly demonstrating how including the equity metric discovers favorable
compromises that are not found by conventional formulations. Interestingly, these compromise solutions account for 0%,
15.8%, 4.3%, and 6.1% of the total number of solutions obtained in each formulation, suggesting that formulation F2 is the
most “efficient” in finding compromise solutions. This is also confirmed by observing how the slope of the yellow (F3) and
brown (F4) lines are steeper than the cyan one (F2), meaning that the number of compromise solutions in F3 decreases more
250 evidently than in F2 for increasing performance thresholds.

These results motivate investigating how the considered equity metric changes across the different sets of solutions. Figure 6
shows that the values of the equity index vary mainly with the standard deviation σ of the performance in terms of the four
objectives instead of the corresponding mean μ : the equity index consistently increases with σ , but can have different values
for the same μ value, especially in the situation of inequity. The reason is that the trade-off between different objectives can
255 lead to notably different σ but similar μ for two different solutions (e.g., in Fig. 2 (b), high values of J^I generally correspond to
low values of J^R). The results in Figure 5 show that the maximum μ value increases from 0.81 for F1 to 0.90 and 0.91 for F2
and F3, respectively. The μ here can be considered a proxy of overall performance, and its significant increase indicates the
advantages of solutions from F2 and F3 over F1. Yet, higher μ does not precisely refer to a better solution as the profits per
unit increment of the four objectives are different. In the traditional formulation, the non-optimized objectives introduce
260 variability in system-wise performance that leads to low equity. Conversely, F2 optimizes the equity index computed across
the 4 objectives, and this generates a substantial improvement at the system level because of the indirect consideration of the
marginalized objectives in the policy design. When transiting from F3 to F4, the equity index instead conveys smaller
additional information, so the advantage of F4 over F3 is less evident.

265 Lastly, the impacts of problem formulations on the resulting dynamics of Lake Como can be evaluated by comparing the
simulated trajectories of lake levels under the best equitable solution for F1-F4. Results in Figure 7 show that the best equitable
solution of F1 leads to the lowest water level especially during the late spring to reduce the flood risk and, at the same time,
the water level drops significantly during the summer for better irrigation water supply, which are the only two objectives
considered in this formulation. Conversely, the inclusive formulation F3 increases the lake level especially in the late summer,
as required to attain high performance in J^R . The water level under the equitable solutions of F2 and F4 is between that of F1
270 and F3, which indicates the identification of a compromise alternative balancing the conflicting objectives.

4.2. Impacts of objectives’ aggregation into the equity index

To investigate the role of alternative formulations of the equity index corresponding to different aggregations of the multiple
objectives, we repeated our analysis using a linear and a non-linear value function (see Figure 2) to map the original objectives
into satisfaction values. Figure 8 illustrates the results for the traditional & fair formulation (F2), where each line represents
275 the performance of the optimized solution in terms of J^F , J^I , J^R , J^E (as in Fig. 2) along with three equity indexes computed with
either the original values of reliability or the satisfaction values returned by the linear and non-linear value functions. Since
the performance difference between linear and non-linear value functions is less notable for F4, the corresponding comparisons
are not reported.

280 According to Figure 8 (a), using standard equity (violet lines) yields solutions with a high level of J^E , which can be explained
by the low upper bound of J^E as also noted in Figure 3. Conversely, using the equity index computed on satisfaction values
tends to obtain a high level of performance in terms of J^F due to the upper bound of J^F , leading to relatively lower J^E but higher
 J^F than using the standard equity. Furthermore, using a linear or non-linear value function also affects the equitable operating

policy design. The non-linear value function tends to get relatively higher J^F and J^R but lower J^E than the linear value function because steeper slopes in value function curves occur in a high level of J^F and J^R (i.e., the improvement of J^F and J^R will be considered more important than the improvement of J^E). Thus, the preferences of stakeholders and decision-makers should be embedded in the equity index formulation to ensure better performance in terms of more important objectives.

Figure 8 (b-c-d) illustrates the 5% most equitable solutions with respect to the different formulations of the equity index. The nearly horizontal lines between axes J^F and J^E represent solutions attaining an equity index close to zero. Solutions using standard equity tend to get higher J^E (close to 0.88) but lower J^F , J^I , and J^R than using normalized equity. When J^F , J^I , and J^R are higher than 0.88, decreasing the standard equity index will always increase the J^E but may deteriorate other objectives (i.e., there will exist a clear trade-off between equity index minimization and J^F , J^I , and J^R maximization). Standard equity leads to all objective performance values close to 0.88 (Figure 8 (b)). In contrast, linearly and non-linearly normalized equity yields more evenly distributed performance scores. The horizontal red lines in Figure 8 (c) show all objectives having the same linearly normalized score as the y-axis limits of Figure 8 (c) are actually the objective ranges, while cyan horizontal lines in Figure 8 (d) mean the same non-linearly normalized score for all objectives. Also, using linearly normalized equity to some degree improves J^I (Figure 8 (c)), while using non-linearly normalized equity tends to get more solutions with a high level of J^F than linearly normalized equity, which is especially notable from the comparisons of performance scores in Figure 8 (d). It is worth noting that the mean of all objective values from solutions using these three types of equity index seems close to each other, with non-linear normalization getting higher J^F and J^R but lower J^I and J^E than linear normalization, and no normalization producing relatively higher J^E but lower J^F , J^I , and J^R . This further indicates that a low equity index is achieved mainly by lowering the standard deviation of the performance instead of increasing the mean of objective values in accordance with the results in Figure 6.

5. Conclusions

In this paper, we incorporated equity principles into the operation design of multipurpose water reservoirs. Using the real-world case study of Lake Como in Northern Italy, the potential for operationalizing equity indexes is assessed by means of a rival framings experiment where we compare the solutions obtained formulating alternative problems with a different number of objectives. Moreover, we assess the sensitivity of the proposed approach with respect to the value functions adopted for aggregating the different objectives in the computation of the equity index.

The comparison between operating policies designed with and without considering equity amongst the operating objectives shows that (1) including equity in the operation design can indirectly improve marginalized objectives that are not explicitly considered in the optimization problem; (2) when also explicitly including marginalized objectives, still the addition of an equity indicator generates more compromise solutions mitigating the conflicts between the operating objectives.

Our work also emphasizes that the search for equitable solutions across multisectoral interests depends on how the multiple objectives are combined to formulate the equity index. Results show that using an equity index based on the original reliabilities can favor or negatively impact some objectives in a difficult way to control. The adoption of participatory approaches for eliciting the preference structure of stakeholders and policymakers thus becomes paramount for the operationalization of equity principles to re-scale the objectives and represent a fair balance across competing interests.

Our methodology is demonstrated using the Lake Como as a case study where the lake is operated by a single authority (i.e. Consorzio dell'Adda), which somehow acts as a social planner that first analyzes the trade-offs across the interests of multiple stakeholders and then implements a selected compromise policy. However, the same approach can also serve as the basis for

an interactive negotiation with multiple stakeholders that can discuss and analyze the same set of solutions examined by the social planner in order to find an acceptable compromise. It is important to stress that in both cases, however, the formulation of the equity index should be co-designed with the stakeholders through the identification of suitable value functions to map the original objectives into satisfaction values that allow the aggregation of the originally incommensurable objectives into an equity index.

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The definition of equity is not unique in the literature. Beside the equity index used in this study, it could be interesting to investigate the impacts of alternative definitions of equity on water resources decision-making and how to select an appropriate equity metric for a specific problem. Moreover, although equitable solutions can help to mitigate the conflicts among multiple objectives, it is still not easy to design an objective value function and thus choose an equitable policy agreed by all stakeholders. Further research could focus on the formulation of guidelines for the identification of satisfactory alternative from the set of Pareto optimal solutions. Finally, the equity in this study is assumed static throughout all experiments, but it could dynamically change over time according to the potential evolution of stakeholders' and decision makers' preferences. It would be interesting to evaluate the dynamics of equity under varying conditions, including future climate scenarios and modifications in the irrigation systems.

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Code and data availability. Observations of lake inflows were provided by Consorzio dell'Adda (<http://www.addaconsorzio.it>, Consorzio dell'Adda, 2020). The source code for the Lake Como simulation and EMODPS implementation is available on GitHub (<https://github.com/EILab-Polimi/LakeComo>).

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Author contributions. GY, MG, and AC designed the research. GY conducted the numerical experiments and led the data analysis, including the production of the figures in the paper. MG and AC contributed to the analysis of results. All authors were involved in the writing of the paper.

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Competing interests. The authors declare that they have no conflict of interest.

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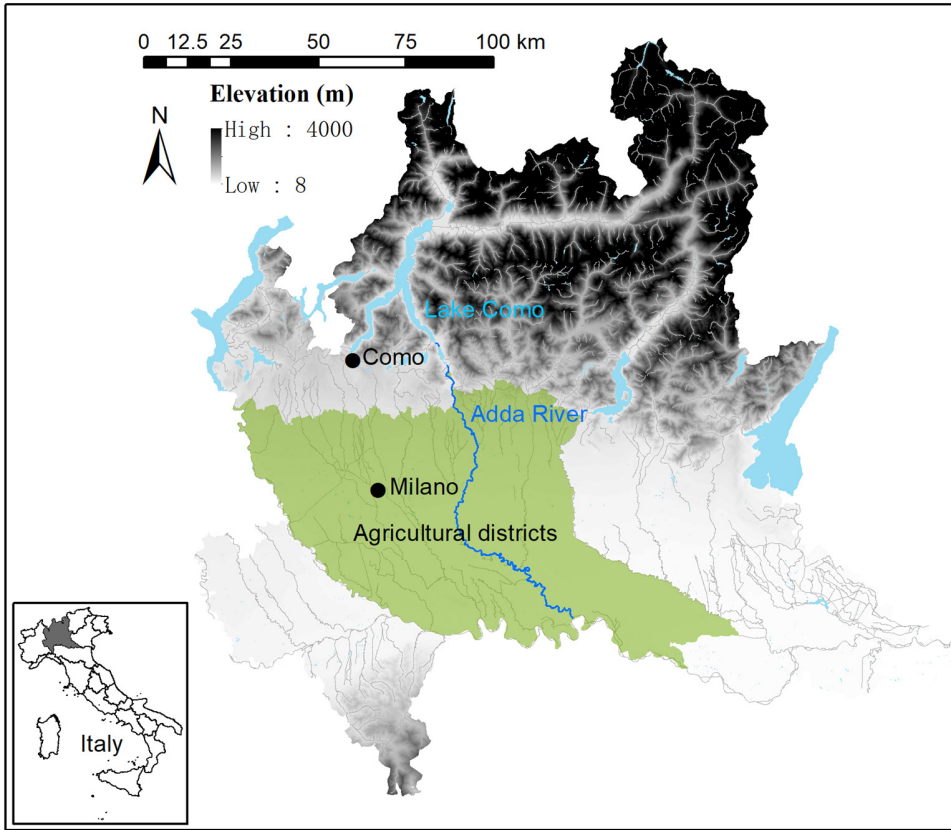
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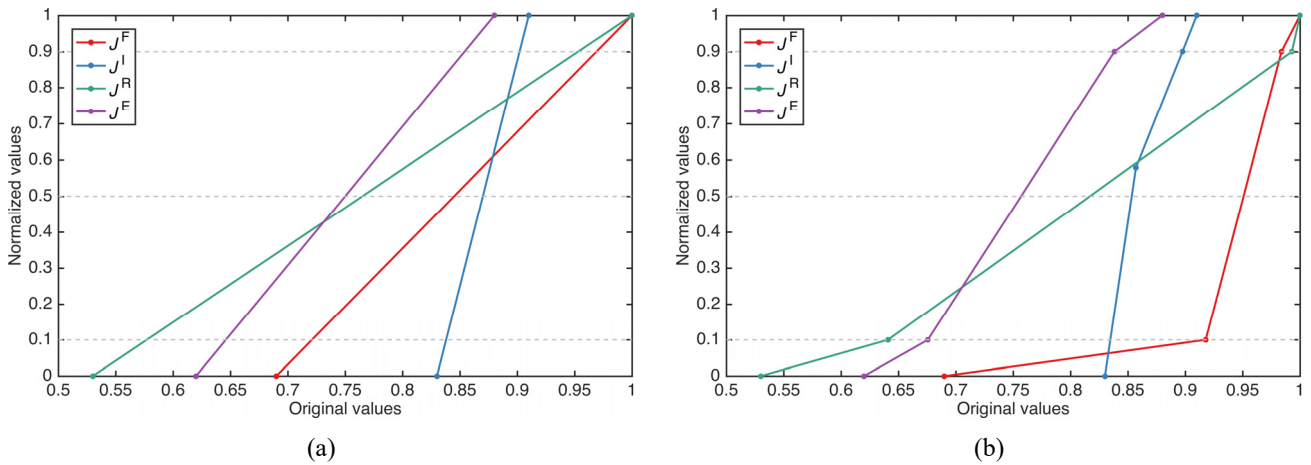
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455 **Figure 1** Map of the Lake Como system in the Lombardy region, Northern Italy. The map was generated via Q-GIS using layers from the Geoportal of Regione Lombardia (<http://www.geoportale.regione.lombardia.it/>, last access: July 2016).



460 **Figure 2** Linear and non-linear value functions of J^F , J^I , J^R , and J^E in the formulation of the equity index.

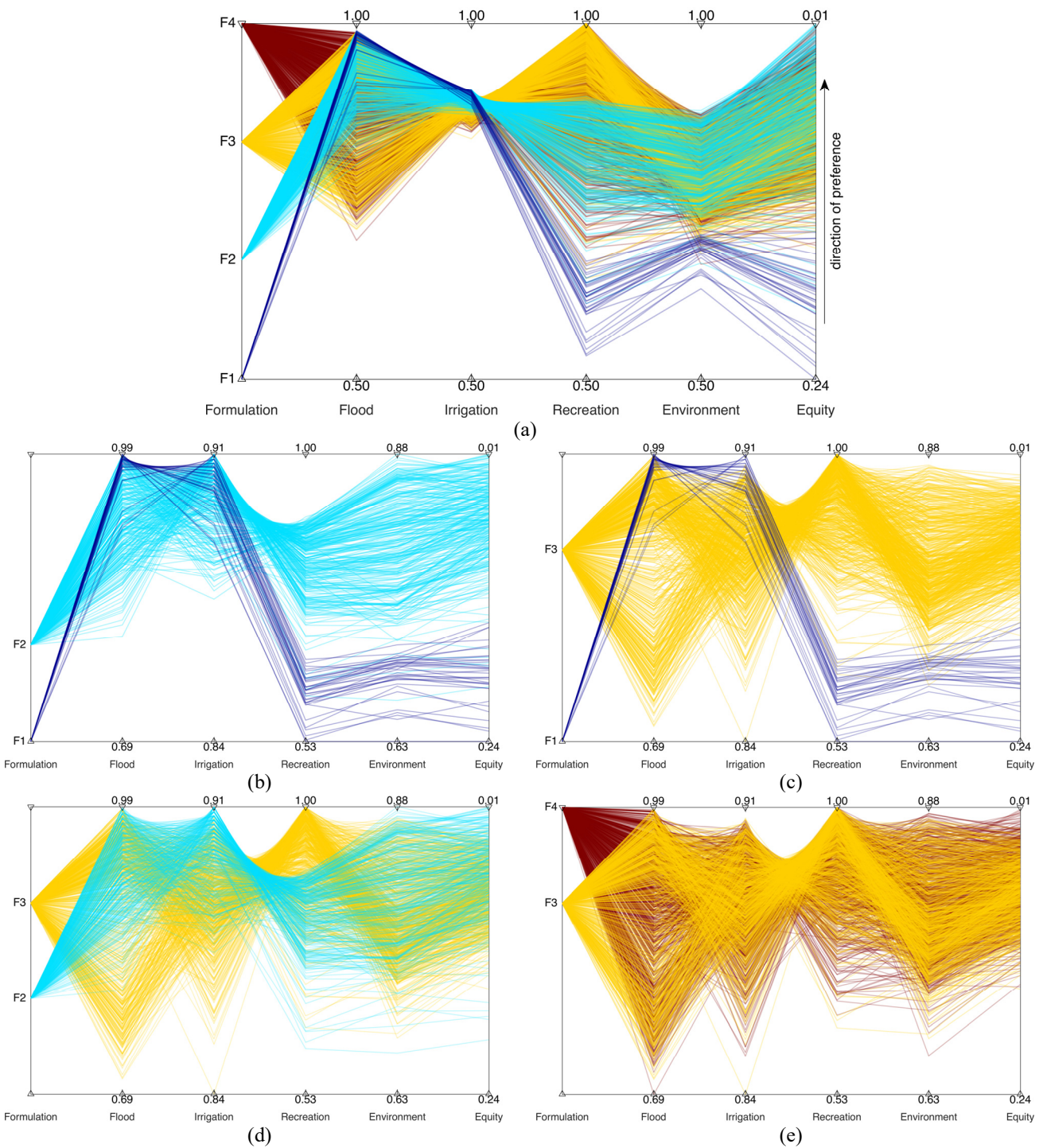


Figure 3 Parallel coordinates plot of comparisons between: (a) all formulations, (b) traditional vs traditional & fair, (c) traditional vs inclusive, (d) traditional & fair vs inclusive, and (e) inclusive vs inclusive & fair. Each line connecting multiple axes represents one optimized solution, the horizontal dash line represents the mean line, and each type of line color represents one problem formulation. The axes with labels “Flood”, “Irrigation”, “Recreation”, “Environment”, and “Equity” refer to the corresponding performances of J^F , J^I , J^R , J^E , and ζ , respectively, and the direction of solution preference is upward. Note: Panel (a) uses the same lower and upper axis bounds for each objective to better compare their best and worst performances and discover compromise solutions (showing with lines approximately horizontal), while Panels (b), (c), (d), and (e) use the minimum and maximum performance values of formulations F1-F4 as the lower and upper axis bounds, respectively.

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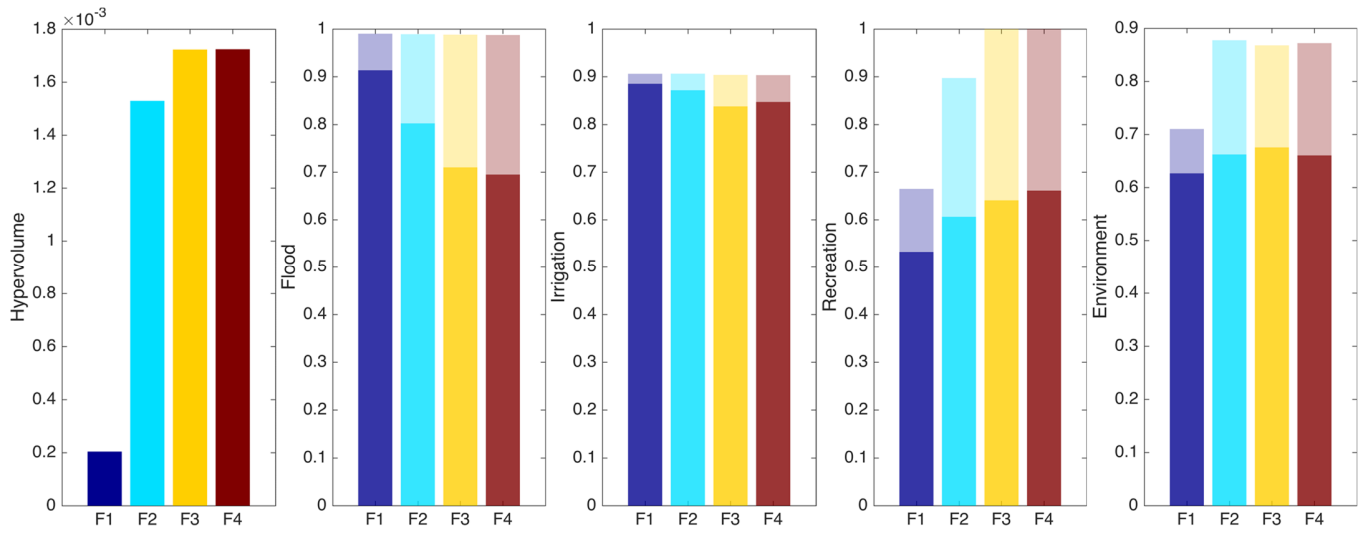
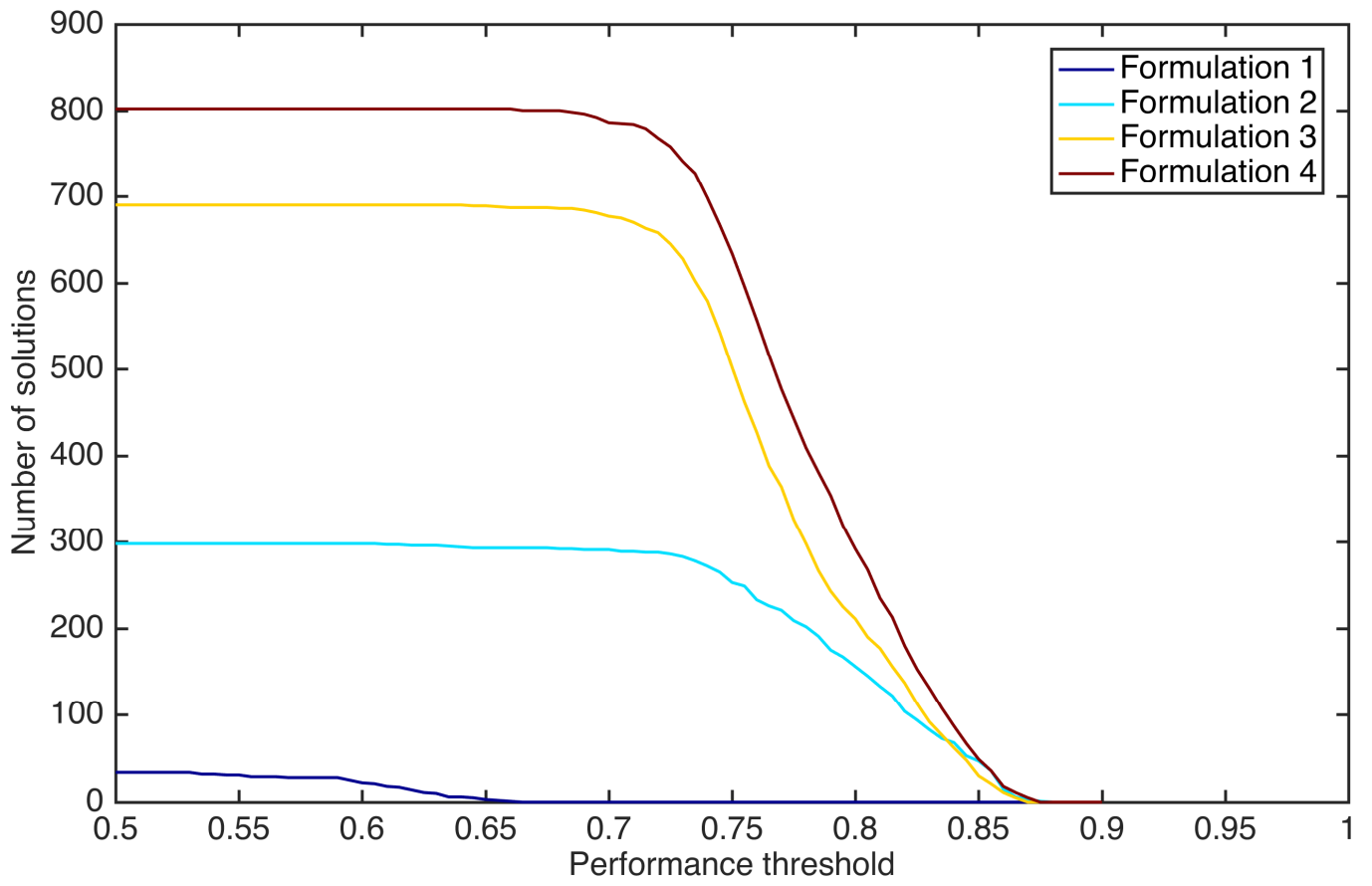


Figure 4 Hypervolume indicator and best (transparent bar) and worst (solid bar) performance in each objective across the four formulations F1-F4.



485 **Figure 5** Number of compromise solutions for formulations F1-F4 that exceed increasing performance thresholds in all objectives.

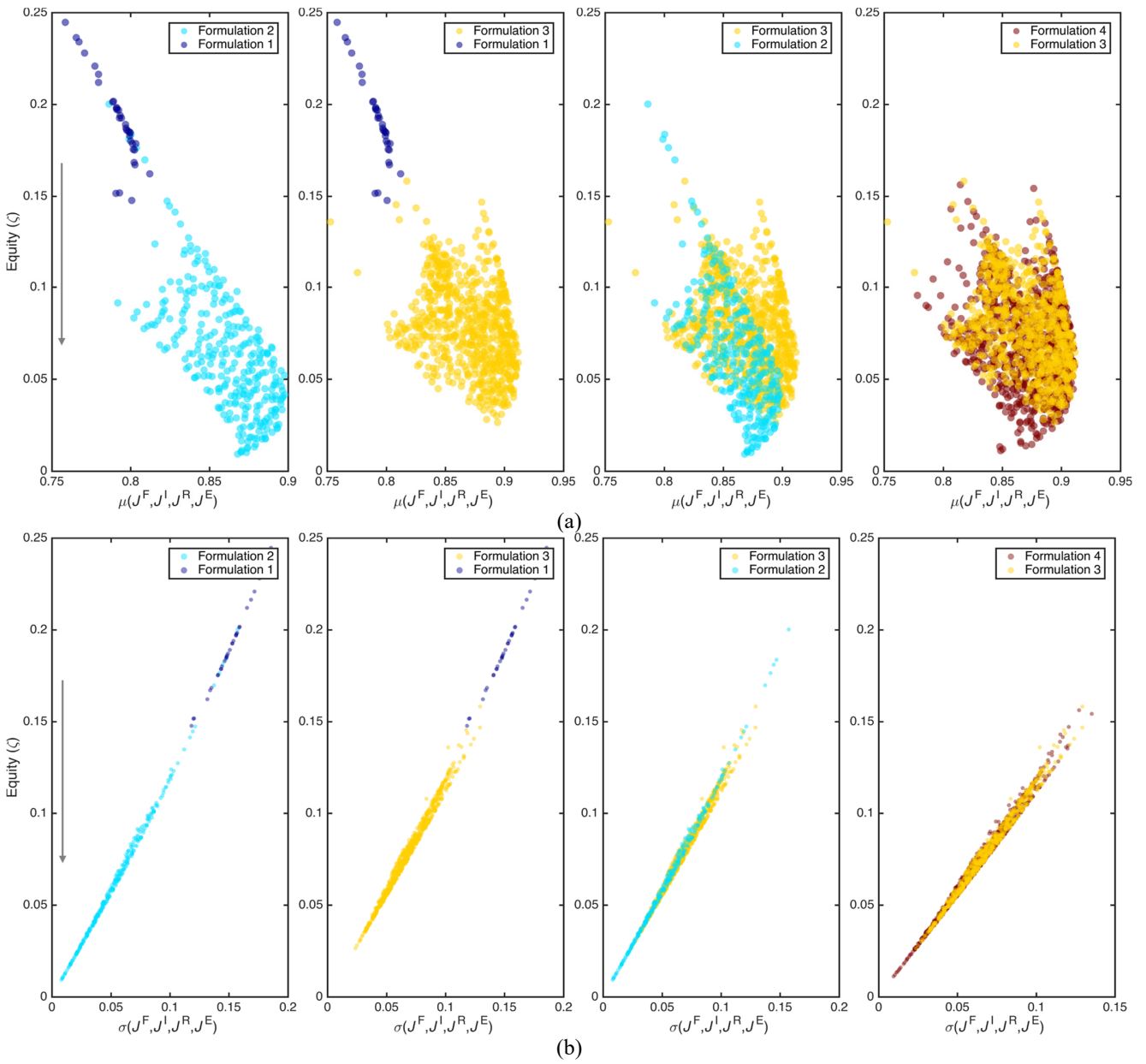


Figure 6 Comparisons of the relationship between equity index and (a) mean μ and (b) standard deviation σ of J^F , J^I , J^R , and J^E for solutions from Problems F1-F4. Each dot in the scatter plots represents one optimal solution. Solutions with lower equity index ζ and higher performance mean value $\mu(J^F, J^I, J^R, J^E)$ are generally preferable. The arrow on y-axis shows the direction of preference.

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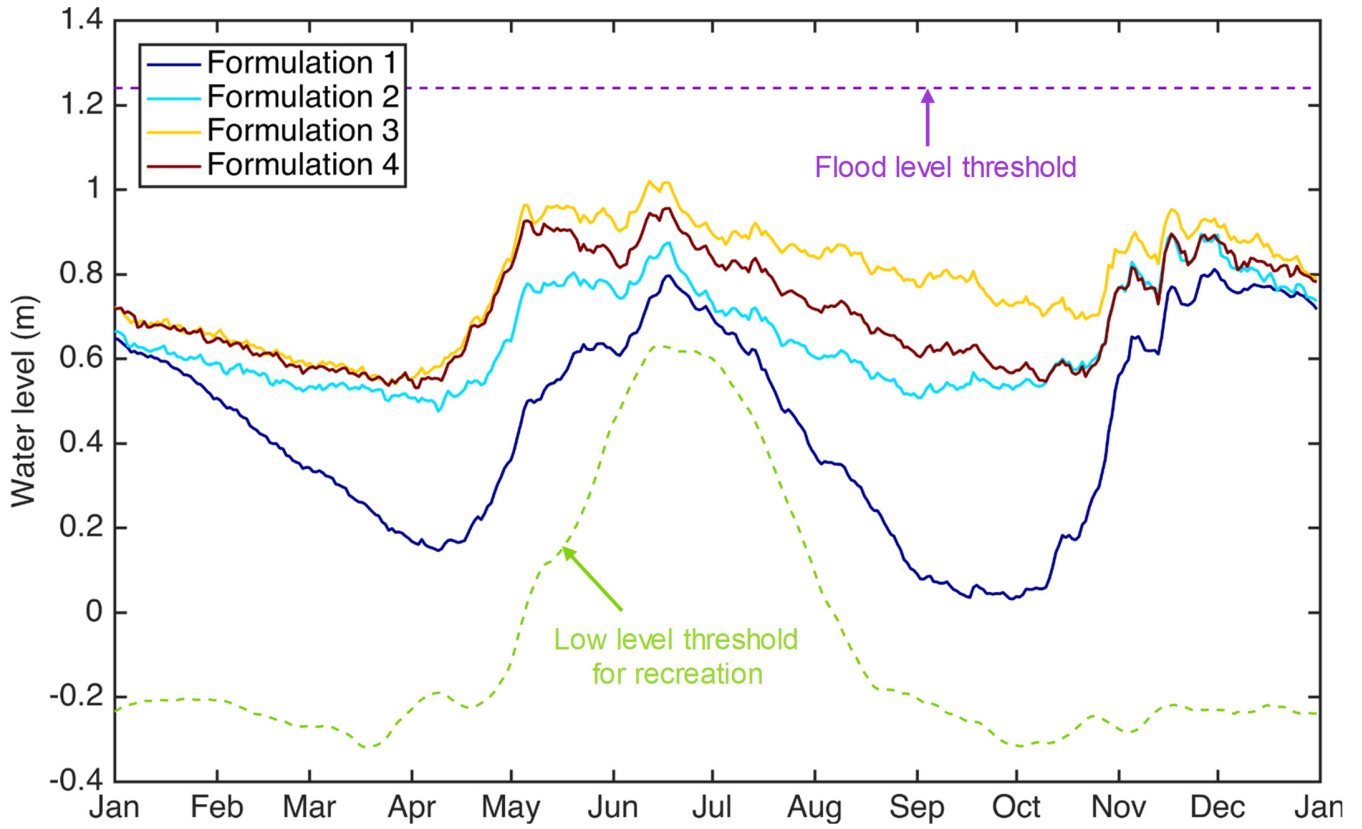


Figure 7 Trajectories of average lake level for the best equitable solution in each problem formulation.

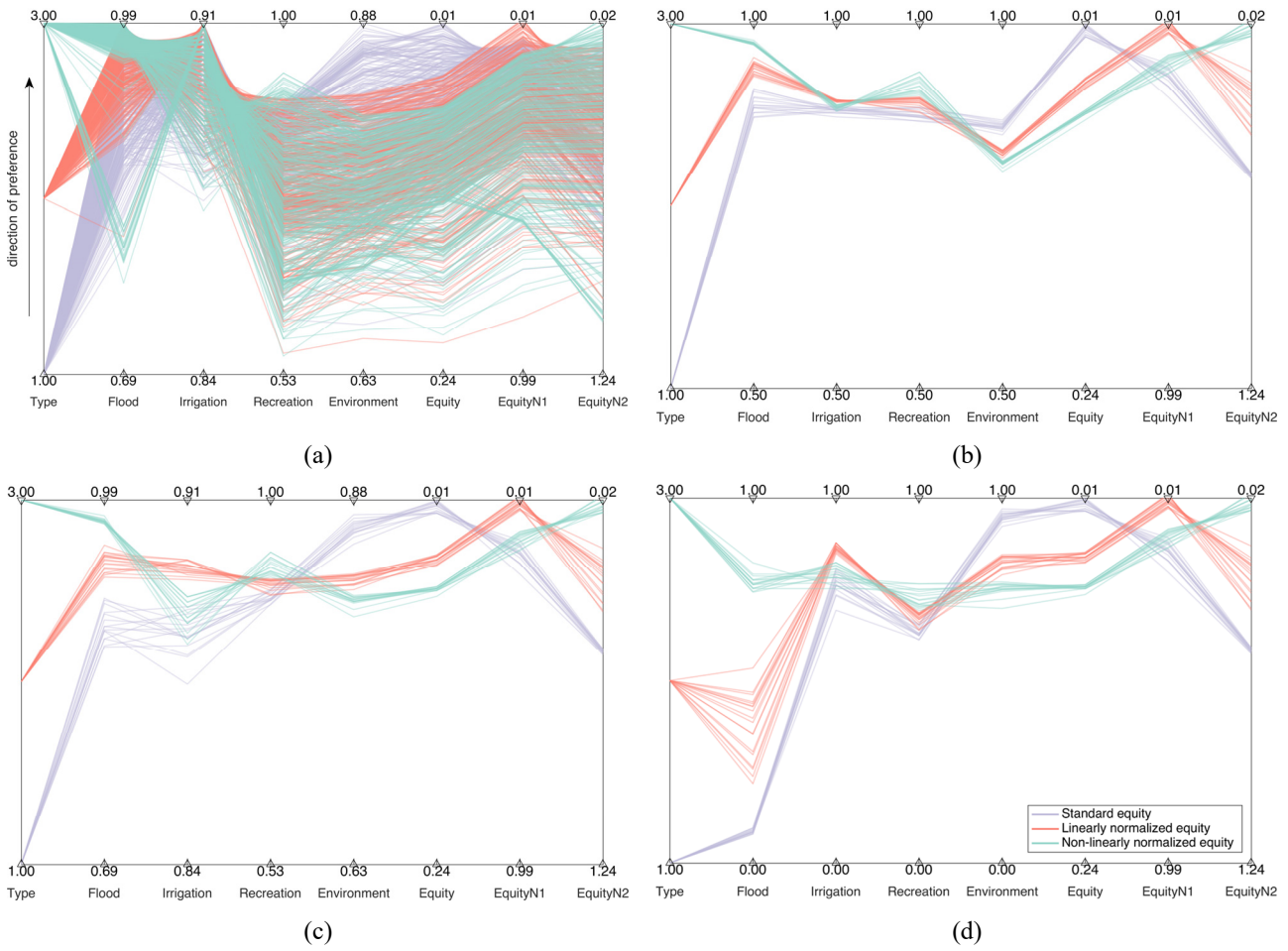
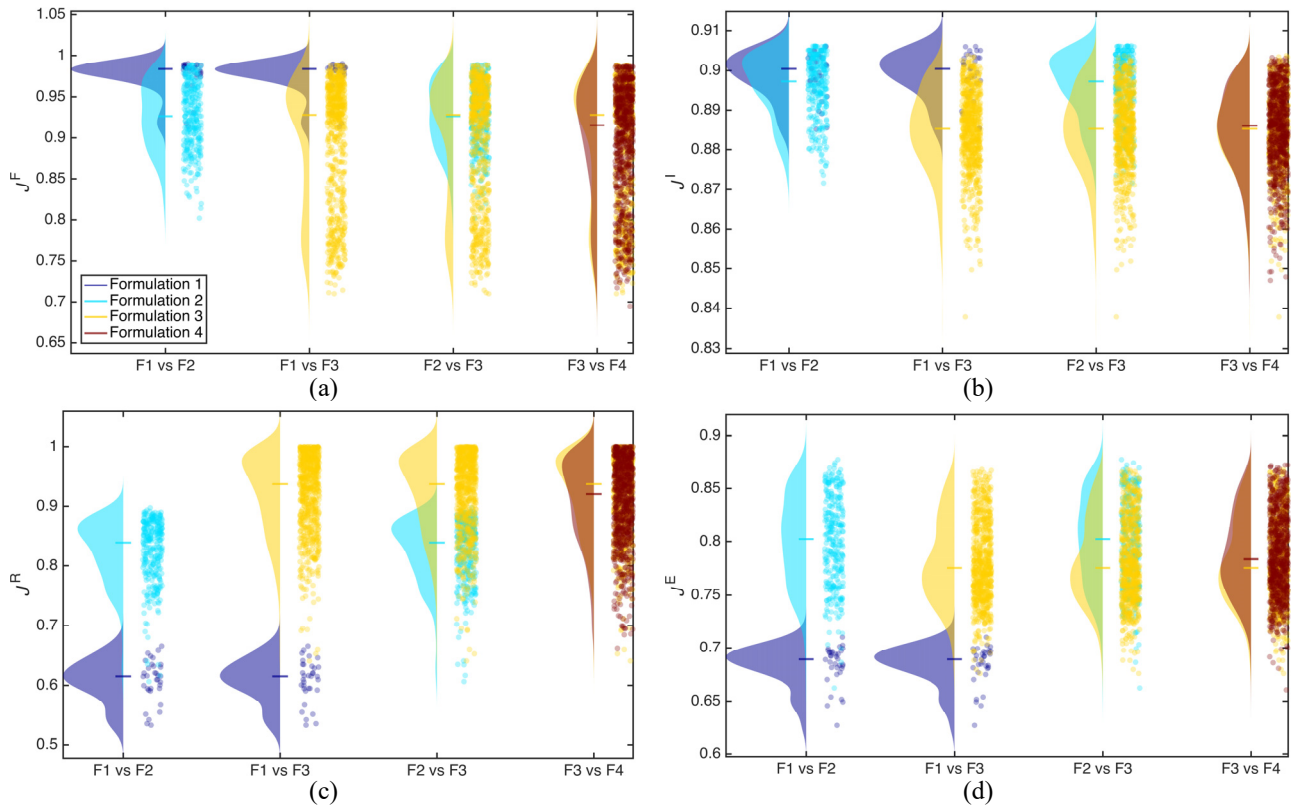
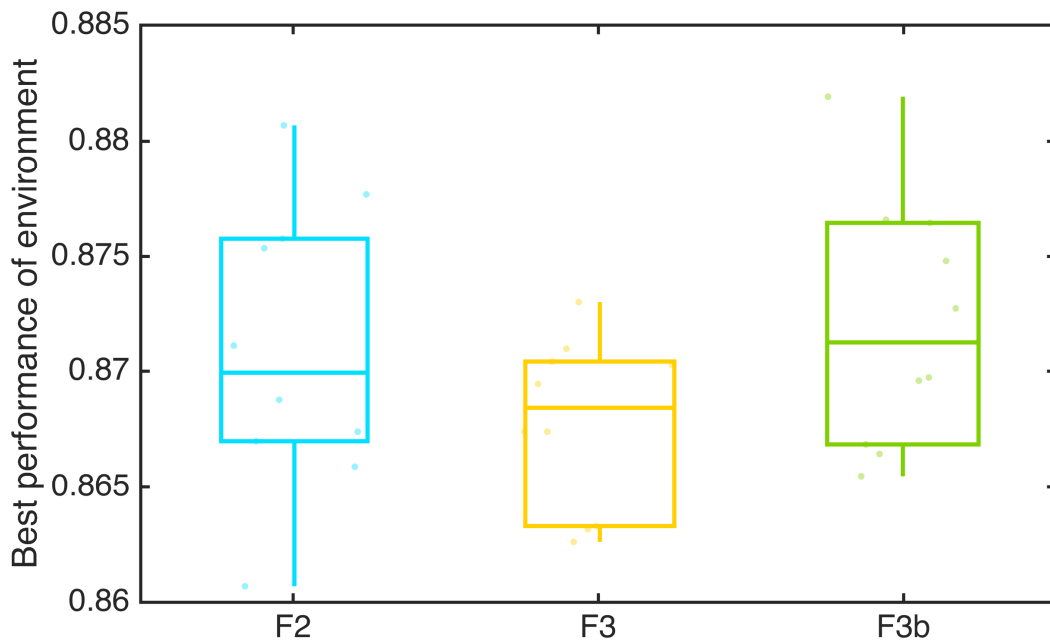


Figure 8 Parallel plot of (a) all solutions and (b) (c) (d) 5% solutions with lowest (standard, linearly normalized, or non-linearly normalized) equity index in problem formulation 2. Type 1, 2, and 3 refer to optimizations minimizing standard, linearly normalized, and non-linearly normalized equity index, respectively. Figures (a), (b), and (c) show performance value, while figure (d) shows performance scores; Figures (b) and (d) have the same lower and upper bounds for all axes (of J^F , J^I , J^R , and J^E), while figures (a) and (c) use the minimum and maximum performance values of problems F1-F4 as the lower and upper axis bounds.

APPENDIX



510 **Figure S1. Density distribution comparisons of (a) J^F , (b) J^I , (c) J^R , and (d) J^E between problems F1 & F2, F1 & F3, F2 & F3, and F3 & F4. The density distribution is estimated by using kernel density estimation. Horizontal dash line refers to the median value of all solutions. The x-axis represents the comparison between various problem formulations.**



515 **Figure S2. Boxplot of best performance of 10 random optimization trials of F2, F3, and F3b, which refers to a new problem formulation including flood, irrigation, and environment.**