



Assessing K_{DP} -based QPE for the record-breaking rainfall over Zhengzhou city on 20 July 2021

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Abstract. Although radar-based quantitative precipitation estimation (QPE) has been widely investigated from various perspectives, very few studies have been devoted into extreme rainfall QPE. In this study, the performance of K_{DP} -based QPE during the record-breaking Zhengzhou rainfall event occurred on 20 July 2021 was assessed. Firstly, OTT disdrometer observations were used as input to T-matrix simulation and different assumptions were made to construct $R(K_{DP})$ estimators. Then, K_{DP} estimates from three algorithms were compared for obtaining best K_{DP} estimates, and gauge observations were used to evaluate $R(K_{DP})$ estimates. Our results in general agree with previous known-truth tests, and provide more practical insights from the perspective of QPE applications. For rainfall rates below 100 mm h^{-1} , $R(K_{DP})$ agrees rather well with gauge observations, and the selection of K_{DP} estimation method or controlling factor has minimal impact on QPE performance provided that the used controlling factor is not too extreme. For higher rain rates, significant underestimation was found for $R(K_{DP})$, and a smaller window length results in higher K_{DP} thus less underestimation of rain rates. We show that the “best K_{DP} estimate”-based QPE cannot reproduce the gauge measurement of 201.9 mm h^{-1} with commonly used assumptions for $R(K_{DP})$, and potential responsible factors were discussed. We further show that the gauge with the 201.9 mm h^{-1} report was located at the vicinity of local rainfall hot spots during 16:00 ~ 17:00 LST, while the 3-h rainfall accumulation center was located at the southwest of Zhengzhou city.

1 Introduction

Extreme rainfall can lead to high-impact events, such as soil erosion, debris flows and flash floods, and therefore poses a serious threat to both life and properties. In a warming climate, the occurrence frequency of regional extreme rainfall events is expected to increase (Allan and Soden, 2008; Donat et al., 2016), and this increase is particularly highlighted in regions of rapid urbanization (Zhang, 2020) where both the intensity of precipitation and the risk of flooding tend to be exacerbated (Zhang et al., 2018).

To mitigate potential damages induced by extreme rainfall events, great efforts have been devoted to improving the prediction and monitoring of extreme rainfall. While the prediction technologies based on numerical models are confronting major challenges (Luo et al., 2020), a collection of in-situ and remote sensing instruments is in operation to observe precipitation, thanks to the development of surface observing systems. The “ground truth” of surface precipitation map is customarily made



25 from rain gauge observations. However, the rain gauge spacings are usually beyond several kilometers, and such “point” obser-
vations are inadequate to represent the localized rainfall centers produced by rapidly evolving storms (Schroeer et al., 2018).
Gauge measurements seem falling short to support flood controlling in urban areas, where the inhomogeneity of underlying
surfaces and complexity of fine-grained drainage connections call for rainfall observations with fine resolutions (Paz et al.,
2020) and the simulated runoff is even more sensitive to the spatial resolution than to the temporal resolution (Bruni et al.,
30 2015). The areal rainfall map can be seamlessly made with remote sensing observations. Weather radars have been used for
quantitative precipitation estimation (QPE) based on parameterized reflectivity factor (Z_e), polarimetric observations (differ-
ential reflectivity Z_{DR} , specific differential phase K_{DP} , and cross correlation ratio ρ_{HV}) or the attenuation effects. From the
perspective of DSD moments, K_{DP} and specific attenuation, corresponding to the estimators of $R(K_{DP})$ and $R(A)$ respec-
tively, are better correlated with rain rates. Therefore, $R(K_{DP})$ and $R(A)$ approaches are more efficient than Z_e -based ones in
35 reducing uncertainties caused by the drop size distribution (DSD) variability (Ryzhkov et al., 2022). For lower rain rates, $R(A)$
has shown apparent advantages, whereas $R(K_{DP})$ is optimal for heavy rain (Ryzhkov et al., 2022). However, the accuracy of
 K_{DP} estimation can be significantly dependent on the methods used (Reimel and Kumjian, 2021). To the best of our knowl-
edge, the performance of K_{DP} -based heavy rainfall estimation has hardly been addressed despite a large volume of works on
radar-based QPE (Schleiss et al., 2020; Cremonini et al., 2022).

40 On 20 July 2021, a devastating rainfall event hit Zhengzhou (Fig. 1a), one of the largest cities in central China, which hosts
over 12 million residents. This event took place following the continuous, relatively weaker, rainfall on 18 and 19 July, and
caused severe flooding over Zhengzhou city that led to around 300 fatalities and tremendous economic losses (Yin et al., 2022).
In Zhengzhou city, the infrastructures are mostly constructed with impervious materials, the so-called “gray urbanization” (gray
area in Fig. 1b), making the city vulnerable to waterlogging in the presence of short-duration extreme rainfall. Given the limited
45 emergency resources, it is therefore imperative to accurately locate the worst hit area. The most intense rainfall was produced
during 14:00 ~ 17:00 local solar time (LST) on July 20 (Yin et al., 2022) (Fig. 1c). Although a gauge (the site is marked with
a black cross in Fig. 1a, b) located in Zhengzhou reported the maximum hourly rainfall of 201.9 mm at 17:00 LST, an hourly
rainfall rate exceeding or close to the historical record in mainland China (Ding, 2019), location and extremity of other local
rainfall hotspots are still unclear.

50 In this study, we aim to quantitatively assess the performance of different K_{DP} -estimation algorithms in this extreme rainfall
event and analysis the areal precipitation map over Zhengzhou city. The paper is organized as follows. The description of
data and K_{DP} estimation methods is presented section 2. The methods of comparing K_{DP} estimates from different algorithms,
constructing different $R(K_{DP})$ estimators, and merging radar observations at multiple elevation angles are given in section
3. Section 4 compares the QPE performance of K_{DP} estimated from different approaches. The areal precipitation map over
55 Zhengzhou city is analyzed in section 5, and conclusions are given in section 6.

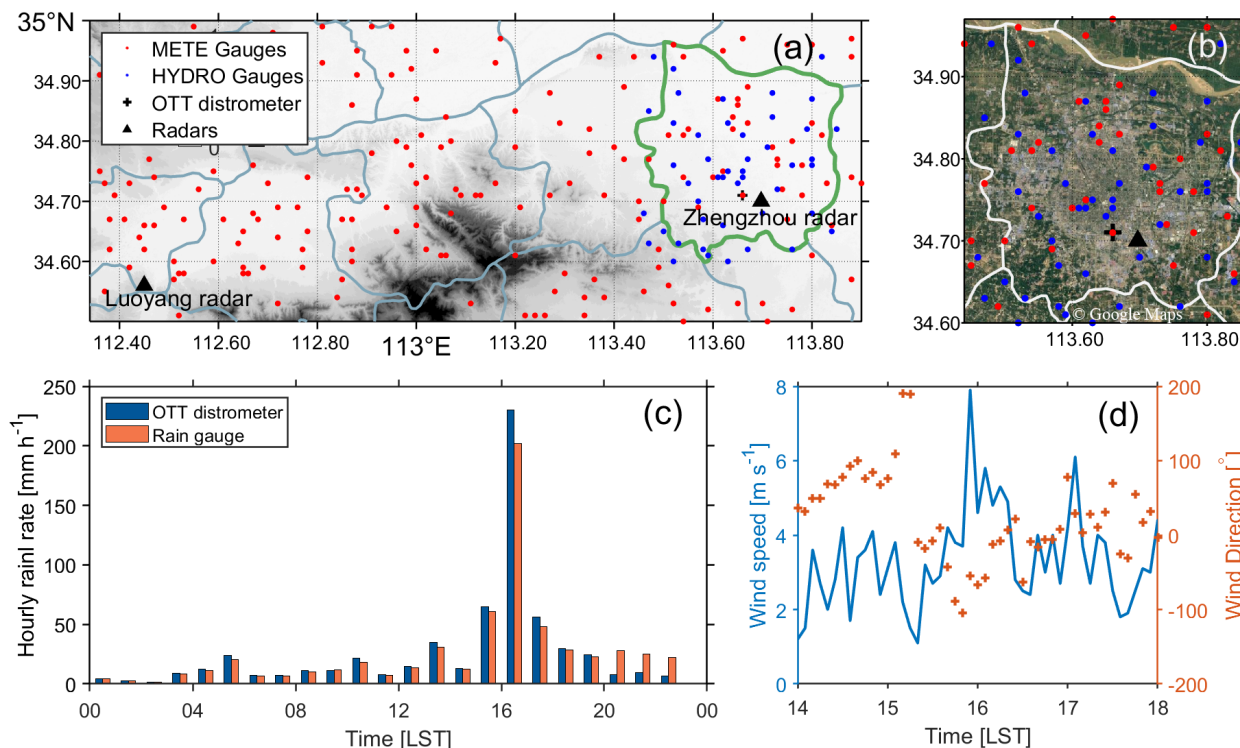


Figure 1. (a) Topography over and around Zhengzhou overlaid with the two operational S-band dual-polarization radars (black triangles), meteorological rain gauges (METE gauges; red dots), hydrological rain gauges (HYDRO gauges; blue dots) and one OTT disdrometer (black cross). (b) Satellite image of Zhengzhou city (modified from © Google Maps). (c) Hourly rain rate recorded by the gauge and the OTT disdrometer located at the Zhengzhou national reference climatological station (113.66 °E, 34.71 °N, the site where the OTT disdrometer is deployed) on 20 July 2021. (d) 5-min horizontal wind speed (left) and direction (right) from 14:00 to 18:00 LST. The light blue curves in (a) indicate county boundaries and Zhengzhou city is outlined in dark green. Note that the HYDRO gauges are widely distributed, although only those over Zhengzhou city are presented in (a).

2 Data

2.1 Dual-polarization weather radars

Since the late 1990s, a nationwide weather radar network composing of over 200 China's New Generation Doppler Weather Radars (CINRADs) has been built in China. CINRADs typically work in the volume coverage pattern 21 mode, which consists of nine plan position indicator scans (0.5° , 1.5° , 2.4° , 3.3° , 4.3° , 6.0° , 9.9° , 14.6° , and 19.5°) with the volumetric update time of 6 min. In recent years, more than 100 CINRADs have been upgraded to dual-polarization systems and others are in the progress. As shown in Fig. 1(a), two S-band dual-polarization CINRADs are deployed in Luoyang city (112.44 ° E, 34.5 ° N) and Zhengzhou city (113.6972 ° E, 34.704 ° N), respectively. Both Luoyang and Zhengzhou radars have the



same configurations, e.g., the range resolution of 0.25 km, azimuth resolution of 1° and the time resolution of 6 min. Mt. Song, located between Luoyang and Zhengzhou, is around 0.9 km above mean sea level (amsl), and the altitude of Luoyang radar is 0.209 km amsl. Therefore, the mountains partially block Luoyang radar's lowest radar beam (0.5°), which may affect reflectivity observations but K_{DP} is immune to this effect. The altitude of Zhengzhou radar is 0.18 km. We have checked Luoyang and Zhengzhou radar observations at different elevation angles, and no second-trip echoes can be identified. Due to the power outage, the Zhengzhou radar data was missing from 17:18 to 19:48 LST. Still, this extreme precipitation event over Zhengzhou city was successfully captured by the Zhengzhou radar, since the majority of the precipitation system moved out of urban Zhengzhou after 17:00 LST.

K_{DP} is the derivation of differential phase shift (Φ_{DP}), while radars measure the total differential phase shift which is a combination of K_{DP} and backscatter differential phase (δ). The impact of δ on K_{DP} estimation in rain is negligible at S-band, while it can be significant at shorter radar wavelengths (Trömel et al., 2013). There are a number of algorithms available for K_{DP} estimation, and some of them are accessible in the open-source tool Py-ART (Helmus and Collis, 2016). Reimel and Kumjian (2021) have used a known-truth framework to evaluate commonly used K_{DP} estimation algorithms. They have found that the algorithm accuracy is dependent on the raw Φ_{DP} , and concluded that each algorithm has its apparent strengths and weakness. They have further shown that (Maesaka et al., 2012) method and Linear programming (Giangrande et al., 2013) are the two that can change the overall behavior between oversmoothing and undersmoothing. This means that a couple of K_{DP} estimates generated with different tuned parameters may yield a range of values where the “best K_{DP} ” falls in, despite that it is challenging to determine the best controlling parameter. In this study, we will assess the performance of using different tuning parameters in K_{DP} -based QPE. A brief introduction of K_{DP} -estimation algorithms is given below.

- The operationally used K_{DP} estimation algorithm in CINRADs is a traditional least square fitting (LSF). As a regression approach, LSF is easy to implement and is commonly used for estimating K_{DP} in weather radars. For a given window of smoothed Φ_{DP} , linear regression is done to estimate K_{DP} . The window length is adaptive and depends on observed Z_e (Wang and Chandrasekar, 2009). Due to this dependence on Z_e , which can be affected by data quality issues such as ground clutter, K_{DP} estimates with ρ_{HV} below 0.8 are removed.
- Linear programming (LP). This algorithm assumes that Φ_{DP} monotonically increases with range and uses self-consistency between Z_e and K_{DP} . Since the self-consistency relation is developed for rainfall, the algorithm does not process Φ_{DP} values above melting layer as defined by users (4.5 km in this study) or in presence of hail. The algorithm is proposed by Giangrande et al. (2013) and is compiled in Py-ART (Helmus and Collis, 2016). The user can define a self-consistency coefficient for K_{DP} - Z_e as well as a self-consistency factor or use the default settings. For S-band radars, the self-consistency factor below 40000 may degrade the estimation performance (Reimel and Kumjian, 2021), while it should be tuned at C-band (Cremonini et al., 2022). In this study, the default setting in Py-ART was used. We have further compared the Φ_{DP} reconstructed by the LP method with the raw Φ_{DP} in radar radials, and found that the algorithm works reasonably well. In addition, the user should set a window length in which a Sobel filter is imposed, and the length



of this window effectively affects the smoothness of the K_{DP} field. For a comparison, we have tried the window lengths of 5, 15, 25, 35 and 45 in this study.

100 – Maesaka et al. (2012) method. This algorithm assumes monotonic increase of Φ_{DP} below the melting layer, namely applicable in rain. It applies a low-pass filter to smooth the observed Φ_{DP} and the weight of this filter depends on a user-defined parameter Clpf. It can be understood that larger Clpf values lead to smoother profiles. A thorough introduction of the algorithm is referred to (Maesaka et al., 2012). Similar with (Reimel and Kumjian, 2021), we have used values of 10^0 , 10^2 , 10^4 and 10^6 for Clpf in this study for K_{DP} estimation.

105 Note that the data quality of Φ_{DP} , which is also critical for K_{DP} estimation, can be heavily affected by ground clutter which usually leads to significant spikes of Φ_{DP} . Those spikes were removed and the interpolation was made before K_{DP} estimation.

2.2 Surface observations

The most widely used rainfall measuring instrument in operational weather services is the tipping bucket rain gauge. The buckets are mounted on a fulcrum and located below a funnel. Once one bucket is filled with water channeled through the funnel, it tips down and the other bucket raises. At the same time, a switch records an electronic signal, which is then converted to the amount of rain. The gauges used in this study are from both meteorological (METE) and hydrological (HYDRO) rain gauge stations, respectively. For the METE gauges, the volume of a bucket is 0.1 mm, which corresponds to the minimal detectable rain accumulation of 0.1 mm. Every one minute, the number of tips is recorded. Liu et al. (2019) have pointed out that the uncertainty of such gauges is about 4 % for rain rates exceeding 10 mm h^{-1} . HYDRO gauges employ tipping buckets as well, but the instrument model is different that of METE gauges. The minimal detectable rain accumulation of the HYDRO gauges is 0.5 mm and the time resolution is 1 h. The high temporal resolution of the METE gauges enables the inspection of the data quality. For the HYDRO gauges with hourly measurements, the inverse distance weighting (IDW) approach (Chen and Liu, 2012) was implemented to remove the data significantly deviating from the expected value.

120 Different from tipping buckets gauges, OTT PARSIVEL disdrometer (OTT) measures rainfall by accounting every raindrop that severely attenuates the light signal emitted from a laser sheet. This different measuring principle makes the OTT an independent instrument that can be used to evaluate gauge observations. Figure 1 (c) compares hourly rain rate measurements recorded by a rain gauge and the OTT at Zhengzhou national reference climatological station in 20 July 2021. During most of the period, OTT slightly overestimates hourly rainfall accumulations compared to the gauge observations. This may attribute to the overestimation of large drops as caused by several factors, such as the assumed oblate shape and the coincidence effect (Tokay et al., 2013; Park et al., 2017).

125 2.3 Comparison of Luoyang and Zhengzhou radar observations

Zhengzhou radar is located in the southeast of Zhengzhou city and Luoyang radar is around 120 km away from the Zhengzhou city. Since the lowest beam of Luoyang radar is about 2.2 km over the Zhengzhou city while the lowest beams of Zhengzhou radar are rather close to the surface, the agreement between Luoyang and Zhengzhou radar observations is an potential issue



that should be addressed. Given the hourly precipitation from 16:00 to 17:00 LST reached the peak, radar retrievals during this
130 period were used for an assessment. To provide a reference for the operational service, we have used K_{DP} from CINRAD's
operational products (LSF method) in the comparison. The lowest elevation angle of Luoyang radar (0.5° , the radar beam is
about 2.2 km over Zhengzhou city) was used, while the selection of 1.5° for the Zhengzhou radar was due to significant clutter
issues at 0.5° . An linear interpolation was applied to range gates that were severely affected by ground clutter as characterized
by ρ_{HV} below 0.8. The raw data was interpolated into the spatial resolution of 0.5 km using PyART (Helmus and Collis, 2016).
135 Note that we did not find significant evidence of hail from Luoyang radar ρ_{HV} observations, and therefore hail is anticipated to
be absent below 2.2 km.

As shown in Fig. 2, the heaviest rainfall poured over the area around the Zhengzhou radar site during 16:00 ~ 17:00 LST,
which may explain the breakdown of Zhengzhou radar at 17:12 LST. A closer inspection to Fig. 2b shows that the location of
precipitation center retrieved from the Luoyang radar (black isolines) is on the east side of that from Zhengzhou radar. This
140 deviation seems to be associated with the structure of the convection whose upper portion slightly tilting eastward (Yin et al.,
2022). Given the significant range degradation effects present in Luoyang radar observations, Zhengzhou radar will be used for
QPE in this study.

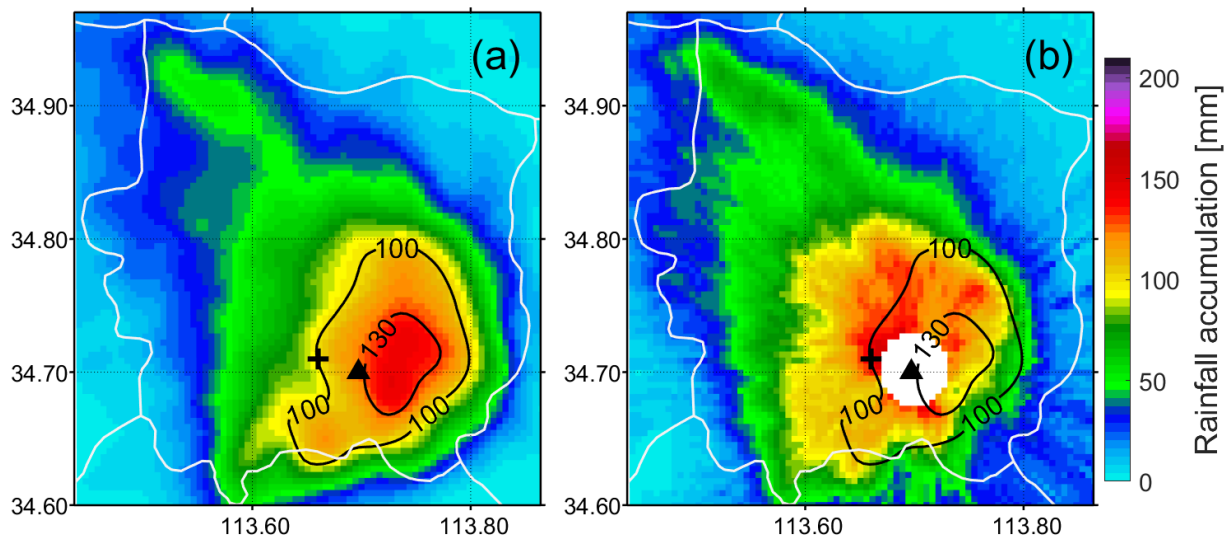


Figure 2. Rainfall accumulation from 16:00 to 17:00 LST estimated using $R = 51K_{DP}^{0.86}$, in which K_{DP} estimates were from the operational data products (LSF method). (a) Luoyang radar data at the elevation angle of 0.5° and (b) Zhengzhou radar data at the elevation angle of 1.5° were used for comparison. Note that K_{DP} estimates within 3 km to the Zhengzhou radar site were removed. The black triangle and cross denote the Zhengzhou radar and the gauge/OTT site, respectively. The black isolines indicate the rainfall accumulation of 100 mm and 130 mm observed by the Luoyang radar, respectively.



3 Methods

As pointed by Bringi and Chandrasekar (2001), the accuracy of K_{DP} -based QPE is dependent on not only the K_{DP} estimation
145 from radars but also on the parameterization of $R(K_{DP})$. Therefore, this section will address these two aspects respectively.

3.1 Approaching the “best K_{DP} estimate”

The calculation of K_{DP} with (Maesaka et al., 2012) and (Giangrande et al., 2013) methods requires a presetting of Clpf and
window length, respectively, which control the smoothing effect. Bringi and Chandrasekar (2001) have concluded that the
minimal window length required for K_{DP} estimation decreases with precipitation intensity. Reimel and Kumjian (2021) have
150 further shown that the “best K_{DP} estimate” falls in a range of values produced by varying the parameters in known-truth
simulations, and used real data to show that the retrieved K_{DP} is heavily dependent on the algorithm and tuning parameter
employed for steep real K_{DP} regions. In this study, the Zhengzhou national reference climatological station hosts both the
OTT and the gauge with the 201.9 mm h⁻¹ report and is 3.15 km away from 274° azimuth of Zhengzhou radar site. We
have compared different K_{DP} estimates over this site. In addition, the elevation angle dependence of K_{DP} is expected to be
155 negligible for small radar elevation angles, i.e., smaller than 4.3° (Bringi and Chandrasekar, 2001). Given the strong ground
clutter contamination, we discarded the data recorded at the lowest elevation angle and K_{DP} estimates at elevation angles of
1.5°, 2.4°, 3.3° and 4.3° corresponding to heights about 0.083 km, 0.132 km, 0.182 and 0.237 km, respectively, over the
station were used. Given the small changes of heights, we assume that the real K_{DP} values over the Zhengzhou station at these
elevation angles did not change.

160 Bearing the considerations above, K_{DP} estimates using Maesaka et al. (2012) method and LP are presented in Fig. 3. Inter-
estingly, our results resemble what is presented in Fig. 16 of (Reimel and Kumjian, 2021) in following aspects:

- Stronger dependence of K_{DP} on the tuning parameter is found for LP than for Maesaka et al. (2012) method.
- Smaller window length used in the LP method generally leads to higher K_{DP} in heavy rainfall periods. In comparison,
 K_{DP} does not significantly change by varying Clpf from 10⁰ to 10⁴ for the Maesaka method.
- 165 – LP can produce higher K_{DP} values than Maesaka et al. (2012) method
- In presence of relatively light rainfall, see for example before 15:00 LST, longer window length in LP agrees better with
Maesaka et al. (2012) method.
- K_{DP} values retrieved from both the LSF and Maesaka et al. (2012) method are less noisy than LP.

However, the impact of changing the window length does not seem to be as significant as in (Reimel and Kumjian, 2021).
170 The K_{DP} values with a window length of 5 which is expected to yield nearly the most extreme K_{DP} (Reimel and Kumjian,
2021) are comparable with the window length of 15 (Fig. 3b). Namely, it appears that the K_{DP} estimated from the LP algorithm
has reached “saturation” at the window length of 15.

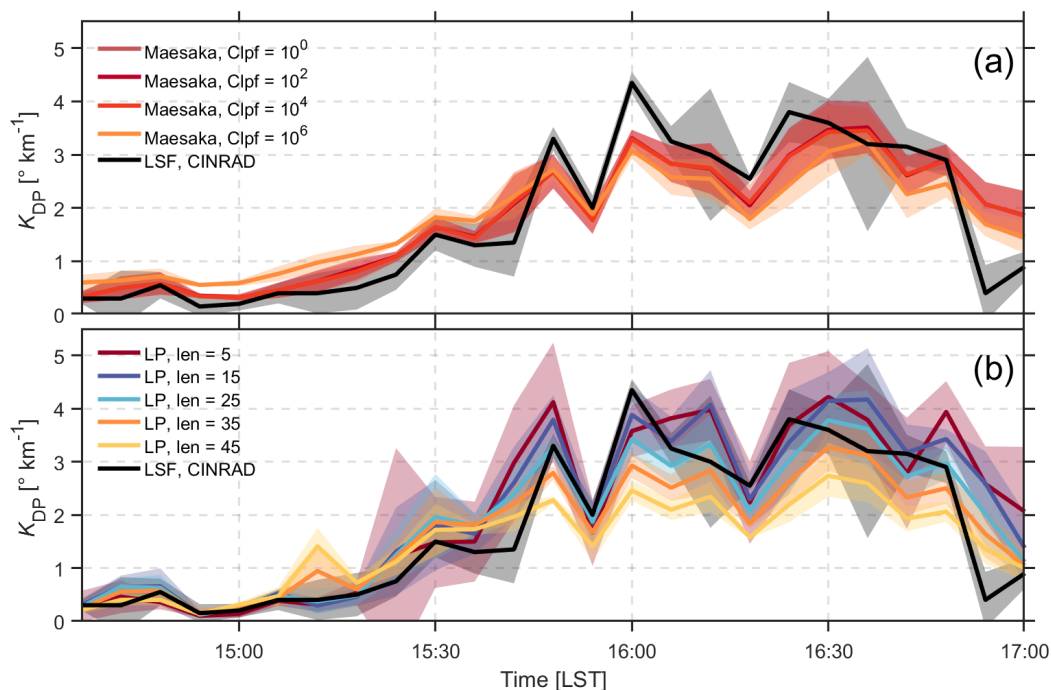


Figure 3. K_{DP} estimates using (a) Maesaka (2012) method and (b) LP over Zhengzhou national reference climatological station. Tick lines and shading areas indicate the median values and standard deviations of K_{DP} at elevation angles of 1.5° , 2.4° , 3.3° and 4.3° . LP: linear programming method (Giangrande et al., 2013); LSF: least square fitting, the CINRAD’s operational algorithm. Colored lines indicate different window length (len) used in LP.

3.2 Parameterizations of $R(K_{DP})$

Although K_{DP} is less dependent on DSDs, a localized $R(K_{DP})$ parameterization is suggested to minimize the impact of varying
 175 DSDs (e.g., Chen et al., 2022). In this study, the OTT disdrometer observations on 20 July 2021 were used as input to PyTMatrix
 (Leinonen, 2014) to calculate radar polarimetric variables. Before the calculation, we have removed raindrops with the velocity
 outside of $\pm 50\%$ of empirical relations (Atlas et al., 1973) or with the volume equivalent diameter higher than 6 mm. It was
 assumed that raindrops are oblate spheroids with the aspect ratio parameterized by the equivolumetric spherical drop diameter
 (Thurai et al., 2007). The water temperature was set to 20°C , and the orientation of rain drops was assumed to be normally
 180 distributed with zero mean and a certain value of standard deviation (σ). We will discuss the factors affecting the accuracy of
 $R(K_{DP})$ parameterization as follows.

- DSDs. Zhang et al. (2022) have shown that for a given K_{DP} the fitted relation for OTT observations during $16 \sim 17$ LST
 yields higher precipitation rates than that for the whole day, but the value does not exceed $\sim 15 \text{ mm h}^{-1}$. In addition,
 most rain rates above 200 mm h^{-1} are from $16 \sim 17$ LST, and they follow the fitted curves rather well. Therefore, we
 185 have used the OTT data from 00:00 to 24:00 LST 20 July 2021.

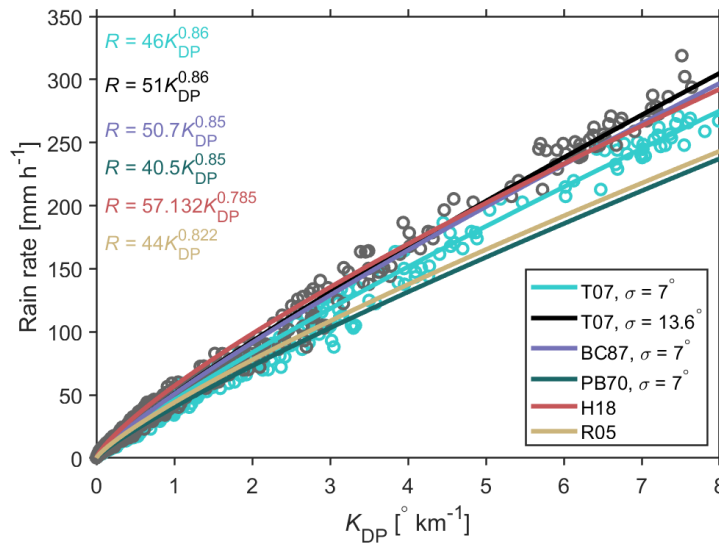


Figure 4. T-Matrix-based simulation of K_{DP} versus rain rate from the OTT observations on 21 July 2021. Black and green circles indicate observations with the $\sigma = 7$ and 13.6° , respectively, assuming the aspect ratio parameterization from (Thurai et al., 2007, T07). The $R(K_{DP})$ relations from (Ryzhkov et al., 2005, R05), (Huang et al., 2018, H18) as well as (Bringi and Chandrasekar, 2001) with aspect ratio parameterizations from (Pruppacher and Beard, 1970, PB70) and (Beard and Chuang, 1987, BC87) are also presented.

– Assumed σ . The simulated radar polarimetric variables are dependent on σ if hydrometeors are assumed to be spheroids (Li et al., 2018). Bringi et al. (2008) have found a σ of around 7° in a stratiform rainfall event with low wind conditions and 12° in moderate wind conditions. In presence of strong winds, this value can be $13.6^\circ \sim 24.7^\circ$ (Bolek and Testik, 2022). The automatic weather station at the OTT site reported that wind speed during this event ranged from 2 to 5 $m s^{-1}$ with a peak of $7.8 m s^{-1}$ at around 16:00 LST. The magnitude of wind speed seems rather close to the condition corresponding to the σ of 13.6° (Bolek and Testik, 2022).

For a given K_{DP} of $5^\circ km^{-1}$, the estimated rain rates are $203.6 mm h^{-1}$ and $183.6 mm h^{-1}$ for σ of 13.6° and 7° , respectively. This value can even be $279.4 mm h^{-1}$ ($R = 70K_{DP}^{0.86}$, not shown) for a σ of 24.7° , which was observed in a tornado event (Bolek and Testik, 2022) and seems to be unrealistically large in this case.

– Aspect ratio parameterization. Assuming a light wind condition ($\sigma = 7^\circ$), the (Pruppacher and Beard, 1970) and (Beard and Chuang, 1987) parameterizations lead to quite different rain rate parameterizations (Fig. 4), as early shown by Bringi and Chandrasekar (2001). Thurai et al. (2007) have shown that the observed raindrop shapes are rather close to the model simulations in (Beard and Chuang, 1987). This is the reason why we have employed the (Thurai et al., 2007) aspect ratio parameterization in K_{DP} calculations.



200 As shown in Fig. 4, the deviation between different parameterizations seems relatively small for smaller rain rates, but significantly enlarges as the precipitation intensity increases. This indicates that a single $R(K_{DP})$ parameterization is applicable for QPE of moderate rainfall. For higher rain rates, the fitted relation for σ of 13.6° agrees rather well with (Beard and Chuang, 1987) and (Huang et al., 2018).

3.3 Merge of Zhengzhou radar observations at multiple elevation angles

205 One of the major challenges of using weather radar observations is to mitigate the ground clutter contamination in the vicinity of radar sites. To remove pixels affected by ground clutters, the threshold of $\rho_{hv} = 0.8$ (Kumjian, 2013) was implemented firstly. In the second step, with the assumption that the rain microphysics within 0.6 km to the surface do not change, the median of radar observations at different elevation angles was used to replace the pixels identified as ground clutter. Because of the rapid increase of the beam height at higher elevation angles, the maximum radar range decreases with the increase of elevation
210 angle for a given height. In this study, we did not employ radar observations at 0.5° due to the strong clutter contamination, and radar data at 9.9° , 14.6° , and 19.5° were discarded given limited valid data and the elevation dependence of polarimetric measurements may start appearing (Bringi and Chandrasekar, 2001). Then, the Inverse Distance Weighting (IDW) interpolation (Cressman, 1959; Goudenhoofdt and Delobbe, 2009) of the radar data was applied to filling in empty regions, and the new constructed radar data was interpolated into the spatial resolution of 500 m using PyART (Helmus and Collis, 2016).

215 4 Results

4.1 K_{DP} -based QPE over the gauge/OTT site

With a parameterized $R(K_{DP})$, we have been able to quantitatively analysis the performance of K_{DP} -based QPE over the gauge site. Given the high rain rates in this event, K_{DP} estimates using the LSF method, Maesaka method with $Clpf = 10^0$ as well as LP method with the window length of 5 are used for comparison. As shown in Fig. 5(a) and (b), $R(K_{DP})$ agrees
220 generally well with gauge and OTT observations before 16:00 LST, regardless of the K_{DP} estimation method or the used $R(K_{DP})$ parameterizations.

From 16:00 to 17:00 LST, decent deviations can be found between gauge and OTT observations. In addition, K_{DP} -based QPE significantly underestimates the surface precipitation during this period. With a larger σ (Fig. 5b), the underestimation is still cry from gauge/OTT observations. Therefore, it is of necessity to discuss factors potentially contributing to this underestimation.

- 225
- Accuracy of K_{DP} estimates. Compared with LSF and Maesaka methods, K_{DP} estimated by the LP method less underestimates the rainfall. Note that the parameterizations used for Maesaka and LP methods are expected to generate the highest K_{DP} values in heavy rainfall (Reimel and Kumjian, 2021). Therefore, we should have good confidence that the uncertainty in K_{DP} estimation is minimized.
 - DSD variations in the air. The lowest radar sampling volume is 0.083 km over the gauge/OTT site (1.5°) while the
230 highest is 0.237 km (4.3°). If DSDs would have significantly varied, K_{DP} estimates at different elevation angles should

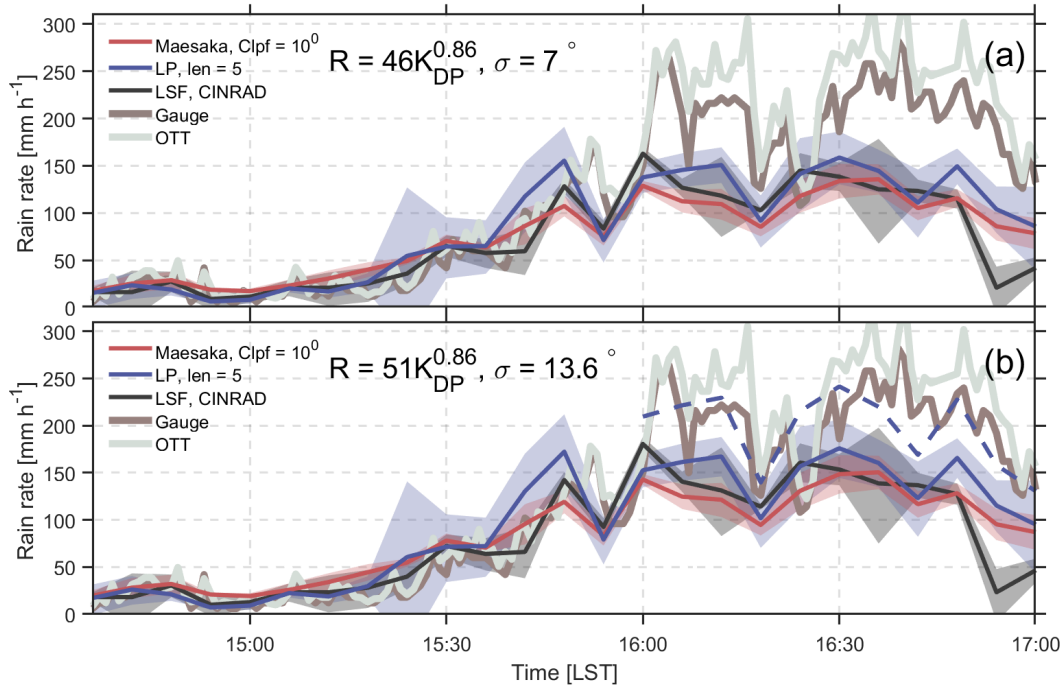


Figure 5. Comparison of rainfall estimates using K_{DP} estimated from different methods over Zhengzhou national reference climatological station. The used parameterizations are (a) $R = 46K_{DP}^{0.86}$ and (b) $R = 51K_{DP}^{0.86}$, respectively. The dashed line in (b) is the use of $R = 70K_{DP}^{0.86}$ ($\sigma = 24.7^\circ$) for QPE from 16:00 to 17:00 LST.

also change. However, the uncertainty of K_{DP} estimates at different elevations angles is on the order of $0.5^\circ km^{-1}$. Therefore, the change of DSDs should not be significant, and the DSDs observed by OTT should be applicable to radar observations that are so close to the surface.

- Vertical air motions. The K_{DP} -based QPE assumes the absence of vertical air motions. For a given DSD in the radar sampling volume, downdrafts can lead to the underestimation of rain rates. For such heavy rainfall, a downdraft of $2 \sim 3 m s^{-1}$ can lead to the rain rate underestimation of $30 \sim 40 \%$. However, the diameter-velocity diagram generated by OTT observations agrees rather well with the empirical relation. Namely, no indications of significant downdrafts on the surface.
- Assumption of σ . As shown in Fig. 4, the assumption on σ is critical for the parameterization of $R(K_{DP})$. However, σ cannot be measured by OTT, and very few experiments have been conducted for addressing this (e.g., Bringi et al., 2008; Bolek and Testik, 2022). The wind observations are rather close to what was reported by Bolek and Testik (2022), and $\sigma = 13.6^\circ$ seems to be a good first guess. If the $\sigma = 24.7^\circ$ measured during the passage of a tornado (the horizontal wind speed is $6 \sim 10 m s^{-1}$) is used, the resulted rain rate estimation is rather close to gauge/OTT measurements (dashed



245

line in Fig. 5b). However, the observed horizontal wind speed is $3 \sim 5 \text{ m s}^{-1}$ from 16:00 to 17:00 LST. Therefore, even though we cannot give a more accurate estimate of σ , 24.7° seems to be unrealistically large in this study.

- Different sampling volumes between the radar and the gauge/OTT. The width of the sampling volume for Zhengzhou radar with a beam width of 1° over the gauge site is about 55 m. Although this value is rather small, it is not impossible that the extreme rainfall poured into a very small spot which is smaller than the radar’s sampling volume.

4.2 Statistical evaluation

250

With the gauge network in Zhengzhou city, we have been able to evaluate the performance of K_{DP} -based QPE with a statistical perspective. Since $R(K_{DP})$ is preferably more applicable in heavy precipitation than other approaches (Ryzhkov et al., 2022), the most intensive precipitation period (14:00 ~ 17:00 LST) was investigated. As discussed above, the assumption of $\sigma = 13.6^\circ$ appears to be more suitable than the commonly used 7° in this event, and therefore $R = 51K_{DP}^{0.86}$ was used. Note that the gridded $R(K_{DP})$, as introduced in Sect. 3.3, was used for comparison.

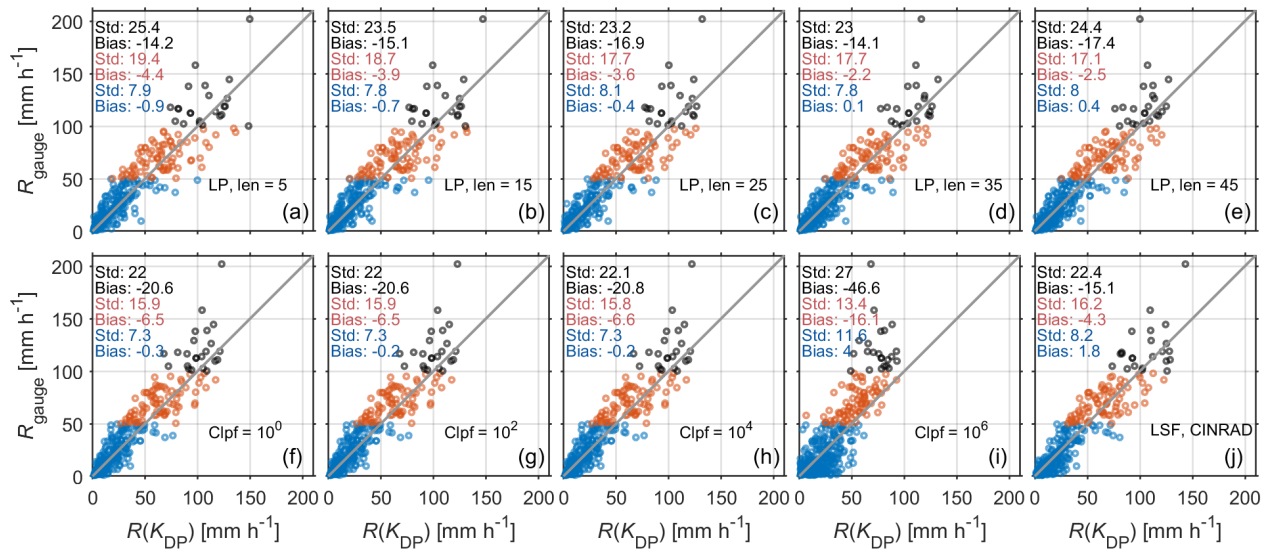


Figure 6. K_{DP} -based hourly rainfall accumulation v.s. gauge observations from 14:00 to 17:00 LST. K_{DP} was estimated using (a-e) LP, (f-i) Maesaka and (j) LSF methods. Rain rates were divided into three groups: $R_{\text{gauge}} < 50 \text{ mm h}^{-1}$ (blue), $50 \text{ mm h}^{-1} \leq R_{\text{gauge}} < 100 \text{ mm h}^{-1}$ (red), and $100 \text{ mm h}^{-1} \leq R_{\text{gauge}}$ (black). The standard deviation (std) and bias between R_{gauge} and $R(K_{DP})$ for each group are marked by corresponding colors. $R = 51K_{DP}^{0.86}$ was used.



255 For rainfall rates below 50 mm h^{-1} , the standard deviation (std) and bias of $R(K_{\text{DP}})$ are mostly on the order of $7 \sim 8$
 mm h^{-1} and $-1 \sim 0 \text{ mm h}^{-1}$, respectively. Regarding the LP method, the used window length does not significantly degrade
the accuracy of QPE (Fig. 6a-e). The performance of the Maesaka method is comparable with that of the LP method (Fig.
6f-h), except for $\text{Clpf} = 10^6$ (Fig. 6i) which imposes obviously oversmoothing filter and results in much larger std and bias. The
operationally used LSF method (Fig. 6j) shows relatively large bias (1.8 mm h^{-1}), indicating that the K_{DP} as derived from the
260 LSF method in rainfall rates below 50 mm h^{-1} should be used with caution.

For rainfall rates above 50 mm h^{-1} , $R(K_{\text{DP}})$ in general underestimates hourly rainfall accumulation, and this underesti-
mation becomes more significant as the rain rate increases (smaller bias and std of red dots than those of black dots). K_{DP}
values estimated from the Maesaka methods is on average smaller than that from the LP and LSF methods, which is consistent
with the results in Fig. 3. Interestingly, the std and bias of LP method are very close to those of the LST method regardless of
265 the used window length. This indicates that varying the window length from 5 to 45 has minimal impact on the accuracy of
 $R(K_{\text{DP}})$ for rain rates of $50 \sim 100 \text{ mm h}^{-1}$ in this event.

Reimel and Kumjian (2021) have shown that smaller window length employed in the LP method yields higher K_{DP} . This
appears to be true for the gauge with the 201.9 mm h^{-1} report, but decreasing the window length did not significantly amelio-
rate the underestimation in a statistical perspective (Fig. 6a-e). Specifically, the highest hourly rainfall accumulation was found
270 for the LP method, and the value rises from 100 mm h^{-1} ($\text{len} = 45$) to 149.6 mm h^{-1} ($\text{len} = 5$). For a reference, the value was
 122.9 mm h^{-1} and 143.3 mm h^{-1} for Maesaka method with $\text{Clpf} = 10^0$ and LSF method, respectively.

5 Analysis of areal rainfall map

As discussed above, the use of window length (LP method) and Clpf (Maesaka method) has limited impact on heavy rainfall
QPE and the window length of 5 generates the closest rainfall estimation to the 201.9 mm h^{-1} report. Therefore, we have
275 compared the areal hourly rainfall accumulation based on K_{DP} generated by these three methods during the most intensive
period (14:00 \sim 17:00 LST).

As shown in Fig. 7, the hot spots of rainfall rates can be manually identified and the results of the three methods generally
agree with each other for $R(K_{\text{DP}}) < 100 \text{ mm h}^{-1}$. However, a depth-in analysis reveals that the magnitudes of rainfall accu-
mulations are different at higher rain rates. From 16:00 to 17:00 LST (the right column in Fig. 7), the rainfall hot spots are in
280 the vicinity of the Zhengzhou radar site (black triangle Fig. 7). The LP method is characterized by the largest area of $R(K_{\text{DP}})$
 $> 130 \text{ mm h}^{-1}$ (Fig. 7a₃), while the smallest area was found for the Maesaka method (Fig. 7b₃). However, due to the scarcity
of gauges in the area of rainfall hot spots, this difference is noticeable only for the gauge with the 201.9 mm h^{-1} report (black
cross Fig. 7).

The areal hourly rainfall accumulation enables the analysis of the evolution of this event. As shown in Fig. 7a, the precipita-
285 tion system moved into Zhengzhou city from the southwest pouring rainfall up to 130 mm h^{-1} from 14:00 to 15:00 LST (Fig.
7a). Then it slowly propagated northeastwards in the next one hour with increased precipitation intensity. The hourly rainfall
beyond 100 mm h^{-1} covered a north-south oriented, ellipse-shaped area of about 115.5 km^2 . From 16:00 to 17:00 LST, the

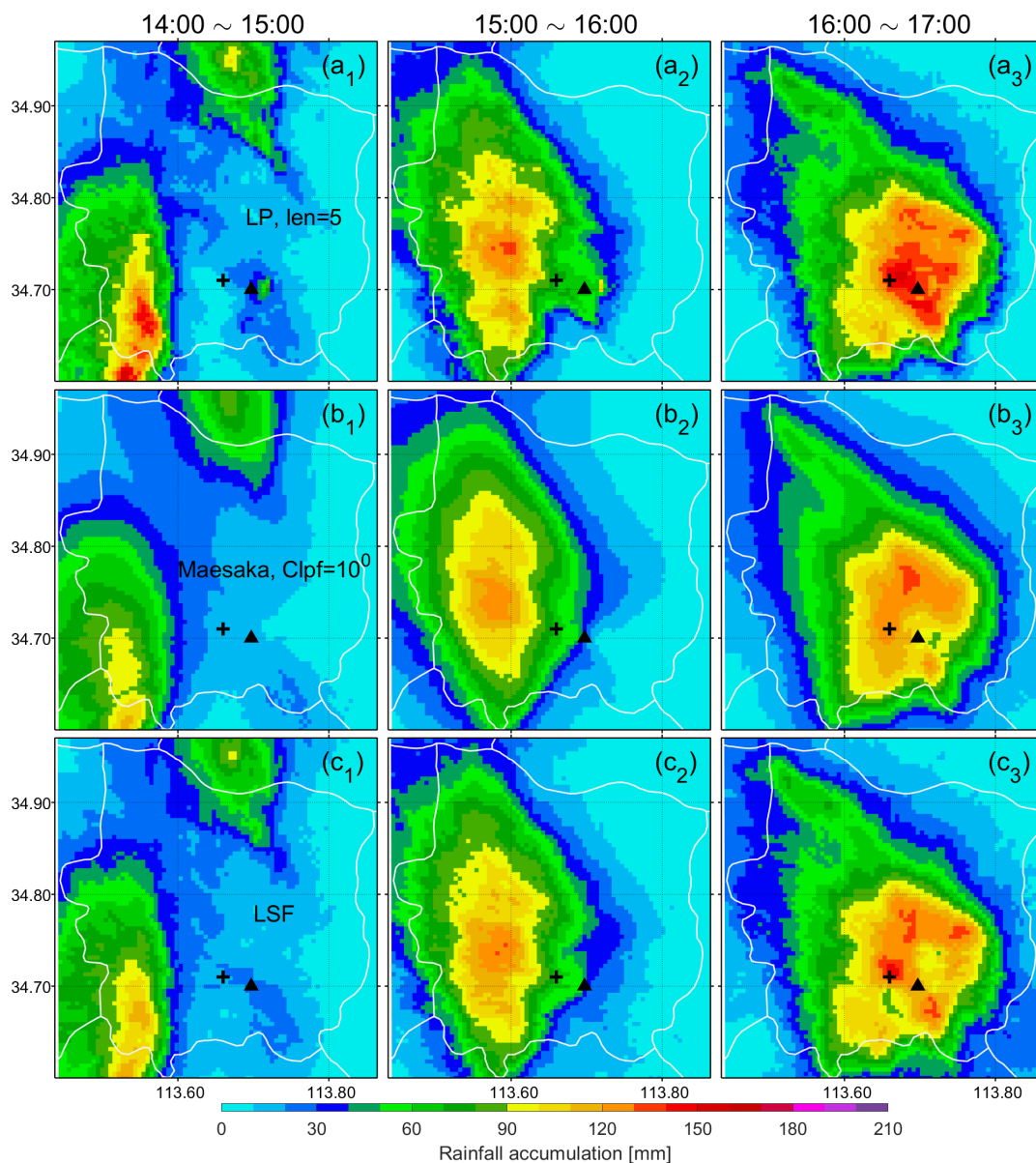


Figure 7. Hourly areal rainfall map from 14:00 to 17:00 LST. K_{DP} was estimated from the (a) LP method with $LP = 5$, (b) Maesaka method with $Clpf = 10^0$, and (c) LSF method. The black triangle and cross denote Zhengzhou radar and the site hosting the gauge with the 201.9 mm h^{-1} report, respectively. $R = 51K_{DP}^{0.86}$ was used.

precipitation system moved eastwards and poured the most intense hourly rainfall over the center of Zhengzhou city (Fig. 7c). The rainfall rate beyond 100 mm h^{-1} covered an area of about 198.25 km^2 , which is 171.7% of that in the previous one hour.

290 The increased rainfall extremity and the more localized extreme rainfall likely resulted from merging of convective cells and

formation of an arc-shaped convergence zone which favored the development of convective updrafts in a three-quarter circle around the storm (Yin et al., 2022). Interestingly, the gauge with the 201.9 mm h^{-1} report was almost exactly located in the high-value center of the hourly rainfall map at 17:00 LST.

The accumulated rainfall from 14:00 to 17:00 LST is presented in Fig. 8. As expected, the results of the LP method and the LSF method are similar, while the area of rainfall accumulation exceeding 200 mm generated by the Maesaka method is significantly different from other two methods. Interestingly, we have found that the center of 3-h rainfall accumulation was off from the hot spot with the record-breaking hourly rainfall accumulation (16:00 ~ 17:00 LST, Fig. 7a₃). Specifically, the center of 3-h rainfall accumulation was located at the southwest of Zhengzhou city, fortunately an urban-rural fringe area where the surface is less impervious and relatively fewer residents were living.

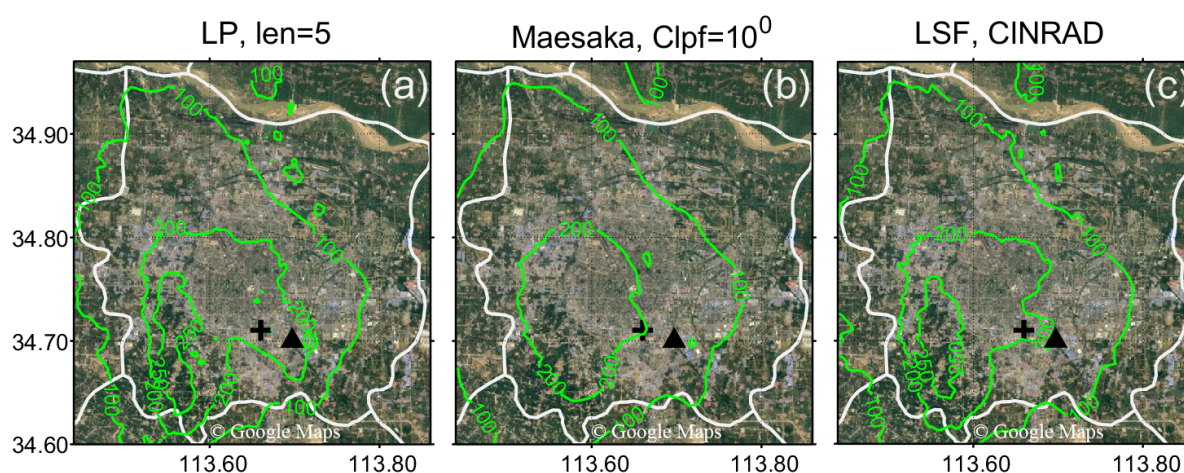


Figure 8. Areal rainfall accumulation over the Zhengzhou city (modified satellite images from © Google Maps) from 14:00 to 17:00 LST. K_{DP} was estimated from the (a) LP method with $LP = 5$, (b) Maesaka method with $Clpf = 10^0$, and (c) LSF method. The black triangle and cross denote Zhengzhou radar and the site hosting the gauge with the 201.9 mm h^{-1} report, respectively. $R = 51K_{DP}^{0.86}$ was used.

300 6 Conclusions

In this study, we have examined the K_{DP} -based QPE for the record-breaking extreme rainfall event occurred at Zhengzhou, 14:00 ~ 17:00 20 July 2021 LST. The rain drop size distribution observations obtained by an OTT disdrometer was used to develop $R(K_{DP})$ parameterizations. The K_{DP} estimates generated by operationally used LSF method were compared with two parameter-controlled methods. The K_{DP} estimates were grided with a spatial resolution of 500 m and the results of $R(K_{DP})$ were compared with gauge observations. The results can be summarized as follows.



- Range degradation effect significantly affected the performance radar-based QPE in this event. The precipitation center as identified by the Luoyang radar, which is about 120 km from the Zhengzhou city center, significantly deviates from Zhengzhou radar estimates.
- The assumed σ in T-matrix simulation has decent impact on the development of $R(K_{DP})$ parameterizations. Higher σ results in smaller K_{DP} in simulations for a given rain drop size distribution. The previous Brangi et al. (2008) experimental study on σ was made in low-wind conditions, while the applicability of σ assumption in moderate to strong winds should be addressed in future studies.
- Gauges deployed over the Zhengzhou city were used to evaluate the accuracy of $R(K_{DP})$. The results show that all methods agree with each other rather well for $R(K_{DP}) < 100 \text{ mm h}^{-1}$. The LP method is capable of producing the highest rainfall accumulation. In a statistical sense, changing the window length from 5 to 45 in LP method or Clpf from $10^0 \sim 10^4$ in Maesaka method does not significantly affect the QPE performance, while the oversmoothing was found for the Maesaka method with Clpf= 10^6 .
- K_{DP} estimates of three algorithms over the gauge with the 201.9 mm h^{-1} report were compared, and the results are generally similar with (Reimel and Kumjian, 2021). One notable difference is that the estimated K_{DP} almost reached "saturation" at the window length of 15, and the increase of K_{DP} with the decrease of window length is not as significant as that in (Reimel and Kumjian, 2021). The results of LP method with a window length of 5 are close to those of the LSF method, but significantly larger than the highest values obtained from the Maesaka method.
- $R(K_{DP})$ with the K_{DP} estimated from the three methods cannot reproduce the gauge-observed 201.9 mm h^{-1} . Our comparisons suggest that this underestimation is unlikely attributed to the K_{DP} estimation process. Rather, the adequacy of assumed σ and different sampling volumes between the gauge and the radar may explain this underestimation.
- The gauge with the 201.9 mm h^{-1} report was located at the vicinity of local rainfall hot spots during 16:00 ~ 17:00 LST, but the center of the 3-h areal rainfall accumulation was found to be located at the southwest of Zhengzhou city, deviating from the site with the 201.9 mm h^{-1} record.

Data availability. The data used in this study can be accessed by contacting the first author. The merged K_{DP} figures are available at https://github.com/HaoranLiHelsinki/Figs_Zhengzhou. The hourly QPE products generated in this study are available at https://github.com/HaoranLiHelsinki/QPE_zhengzhou.

Author contributions. HL and DM conceptualized the study. HL performed the experiment and wrote the paper. All the authors took part in the interpretation of the results and edits of the paper.



Competing interests. The authors declare that they have no conflict of interest.

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