Assimilation of airborne gamma observations provides utility for snow estimation in forested environments

Eunsang Cho¹², Yonghwan Kwon¹²*, Sujay V. Kumar¹, Carrie M. Vuyovich¹

¹Hydrological Sciences Laboratory, NASA Goddard Space Flight Center, Greenbelt, MD, USA
²Earth System Science Interdisciplinary Center, University of Maryland, College Park, MD, USA

*Correspondence to: Yonghwan Kwon (yongwhan.kwon@nasa.gov)

Abstract. An airborne gamma-ray remote sensing technique provides a strong potential to estimate reliable snow water equivalent (SWE) in forested environments where typical remote sensing techniques have large uncertainties. This study explores the utility of assimilating the temporally (up to four measurements during a winter period) and spatially sparse airborne gamma SWE observations into a land surface model to improve SWE estimates in forested areas in the northeastern U.S. Here, we demonstrate that the airborne gamma SWE observations add value to the SWE estimates from the Noah land surface model with multiple parameterization options (Noah-MP) via assimilation despite the limited number of the measurements. Improvements are witnessed during the snow accumulation period while reduced skills are seen during the snow melting period. The efficacy of the gamma data is greater for areas with lower vegetation cover fraction and topographic heterogeneity ranges, and it is still effective in reducing the SWE estimation errors for areas with higher topographic heterogeneity. The gamma SWE data assimilation (DA) also shows a potential of extending the impact of flight line-based measurements to adjacent areas without observations by employing a localization approach. The localized DA reduces the modeled SWE estimation errors for adjacent grid cells up to 32-km distances from the flight lines. The enhanced performance of the gamma SWE DA is evident when the results are compared to those from assimilating the existing satellite-based SWE retrievals from the Advanced Microwave Scanning Radiometer 2 (AMSR2) for the same locations and time periods. Although there is still room for improvement, particularly for the melting period, this study shows that the gamma SWE DA is a promising method to improve the SWE estimates in forested areas.
1 Introduction

Seasonal snowpack is an important freshwater resource in snow-dominated regions, and thus, accurate estimation of snow water equivalent (SWE), has been a pressing issue for managing water supply and forecasting snowmelt-driven flood events in a changing climate (Barnett et al., 2005; Cho et al., 2021; Sturm et al., 2017; Musselman et al., 2021). Due to its large variability, spatiotemporally continuous estimates of SWE cannot be generated by the existing in situ measurement network alone (e.g., Dozier, 2011). Large-scale distributions of SWE can be obtained from satellite remote sensing techniques such as passive microwave sensors (Derksen et al., 2005; Vuyovich et al., 2014); however, these are subject to errors resulting from retrieval algorithm limitations and uncertainties in certain conditions (Kang et al., 2014). Spatiotemporally continuous snow estimates at large scales can be generated by land surface modeling, which however suffer from large uncertainties associated with model physics, parameterizations, and meteorological boundary conditions (Broxton et al., 2016b; Cho et al., 2022; Kim et al., 2021; Raleigh et al., 2015; Yoon et al., 2019). Given the limitations of each method, data assimilation (DA) has been considered as a promising alternative to improve the SWE estimation skill as it systematically merges remote sensing observations with land surface model (LSM) predictions (e.g., Durand et al., 2009; Forman et al., 2012; Kwon et al., 2019; Liu et al., 2013; Zhang et al., 2014). Given the sensitivity to snow properties and long record of observations, passive microwave brightness temperature ($T_b$) observations have been used to retrieve SWE or snow depth (e.g., Change et al., 1990; Derksen et al., 2010; Foster et al., 2005; Kelly et al., 2003; Kelly, 2009), and used within data assimilation frameworks, for the assimilation of $T_b$ (e.g., Durand and Margulis, 2006, 2007; Durand et al., 2009; Kwon et al., 2015, 2017; Larue et al., 2018a, 2018b) and assimilation of $T_b$-based retrievals of SWE or snow depth (e.g., Dziubanski and Franz, 2016; Kumar et al., 2014). However, as mentioned above, $T_b$-based approaches are considered suboptimal for the following surface conditions: (1) deep snow, (2) wet snow, and (3) dense forest. Previous studies (e.g., Derksen et al., 2010; Kwon et al., 2019; Lemmetyinen et al., 2015) found that the $T_b$ signal, especially at high frequency (e.g., 36.5 GHz), saturates in deep snowpacks (i.e., when SWE is greater than 100 to 200 mm), hampers microwave $T_b$-based SWE estimates. In the presence of wet snow, the $T_b$ sensitivity to SWE decreases because liquid water of snowpack dominates the $T_b$ signal due to the high emissivity of liquid water (Clifford, 2010; Walker and Goodison, 1993). Thus, the quality of the $T_b$-based SWE estimates is degraded under wet snow conditions (Kwon et al., 2019). The $T_b$ sensitivity to SWE also diminishes in forested areas (Roy et al., 2012) because the forest canopy blocks the microwave $T_b$ emission from the snowpack and emits its own $T_b$ signal (Foster et al., 1991), which adds considerable uncertainties in the $T_b$-based SWE estimates in forested areas (e.g., Kwon et al., 2016, Vuyovich et al. 2014). Vuyovich et al. (2014) showed specifically in the New England area that passive microwave retrievals underestimate SWE, though algorithms that account for forest fraction show improved performance. Although many enhancements have been proposed for the use of $T_b$ observations in estimating SWE, there are still significant limitations to overcome. Recently, airborne remote sensing approaches such as Light detection and ranging (LiDAR) that have potential to overcome the existing challenges have been used within DA schemes to improve snow depth or SWE (e.g., Hedrick et al., 2018; Smyth
et al., 2019; 2020). Hedrick et al. (2018) focused on enhancing snow depth estimations over the Tuolumne River Basin in California by directly inserting the NASA Airborne Snow Observatory (ASO) airborne LiDAR snow data into the iSnobal model (Mark et al., 1999). They found that agreement between the LiDAR snow depth and updated modeled snow depth was improved as compared to original modeled snow depth. Smyth et al. (2020) attempted to assimilate the ASO LiDAR snow depth observations into the Flexible Snow Model to improve snow density and SWE estimations. They showed that DA reduced snow density bias by over 40% and SWE bias by over 70% across eight climate zones in the western U.S. and in both wet and dry years. However, the impacts of known limitations such as forest cover and wet snow (in melting period) within a DA framework have not been widely examined, which were emphasized to be conducted in future research. Furthermore, most previous studies have mainly focused on the western U.S. environments (e.g. mountainous regions) with limited investigations in other regions such as temperate forest environments over northeastern U.S.

As a historically well-established remote sensing technique, the airborne gamma radiation technique provides an opportunity to estimate reliable SWE, because the gamma approach uses the attenuation of the terrestrial gamma-ray emission by water in the snowpack (any phase) with minimal effects by wet snow and dense forest (Carroll, 2001; Carroll and Vose, 1984; Goodison et al., 1984). Since the early 1980s, airborne gamma radiation snow surveys operated by the National Oceanic and Atmospheric Administration's (NOAA) Office of Water Prediction (OWP; formerly by the National Operational Hydrologic Remote Sensing Center [NOHRSC]) have provided SWE observations to regional NOAA National Weather Service (NWS) River Forecast Centers (RFCs) and other agencies across the United States and southern Canada to support operational flood forecasting system and water supply outlooks (Carroll, 2001; Peck et al., 1980). Recently, Cho et al. (2020b) found that the long-term gamma SWE observations have a remarkable agreement with ground-based gridded SWE products particularly in forest regions (R-value = 0.73 and 0.72 and Bias = 0.0 and -1.3 cm for mixed forest and deciduous forest, respectively), implying that the gamma-based SWE observations have the potential to be used in a DA framework to improve modeled SWE estimates. While the airborne gamma SWE products along with in-situ snow depth and SWE and satellite-based snow cover areas are currently assimilated into the NWS SNOW Data Assimilation System (SNODAS) to provide the near-real-time, high spatial resolution (1 km² gridded) SWE information (Barrett, 2003), how much the gamma radiation SWE retrievals help improve the modeled SWE estimates is not well quantified particularly in a forested region.

The objective of this study is to evaluate the potential of the airborne gamma SWE retrievals within a DA framework to enhance SWE estimates in a temperate forest environment in the northeastern U.S. More specifically, we aim to answer three research questions: (1) How much is the modeled SWE improved by assimilating the airborne gamma SWE into a model? (2) Do land surface characteristics such as forest density, slope, and elevation affect the assimilation performance? (3) Can the spatial sparseness of the gamma SWE observations be overcome by employing the localized data assimilation approach? In this study, the Noah land surface model with multi-parameterization options (Noah-MP) is used to assimilate the long-term airborne gamma radiation SWE observations with the ensemble Kalman filter (EnKF) scheme within the NASA Land Information System (LIS). This paper is organized as follows. Section 2 provides the study area with general land cover characteristics. Section 3 describes the datasets including the airborne gamma radiation survey, reference SWE data, tree cover...
fraction, and topographic feature variables. The description of the Noah-MP model with assimilation scheme is included in the section 4. Section 5 presents evaluation results of DA SWE performances with discussion about the similarities, differences, and new findings in the results with respect to previous studies. Conclusion and future perspectives are drawn in section 6.

2 Study Area

The study area comprises parts of the northeastern United States, including New Hampshire and Maine with heavily forested regions which remain a challenging region in snow remote sensing and modeling communities. The dominant seasonal snow class in this region is montane forest (Figure 1a; Sturm & Liston, 2021). Land cover types are mainly deciduous broadleaf forest and mixed forest. Fractional tree cover over the study area ranges from 70 to 100% based on the vegetation continuous field (VCF) map from the NASA Making Earth System Data Records for Use in Research Environments (Hansen & Song, 2018; Figure 1b). The NOAA OWP airborne gamma snow surveys occur almost every year over the designated flight lines (yellow lines in Figure 1b).

Figure 1. (a) Sturm and Liston’s new seasonal snow classification (Sturm and Liston, 2021), and (b) Vegetation Continuous Field maps of the study area over the northeastern United States with the NOAA airborne gamma flight lines.
3 Data

3.1 NOAA airborne gamma snow survey

The operational airborne gamma radiation snow and soil moisture survey operated by the NOAA’s OWP has been conducted to observe near real-time areal SWE (Carroll, 2001) throughout the United States and Canada provinces since 1979. The gamma SWE observations have been used by the NWS Hydrologic Services Program for spring flood forecasts and water supply outlook. The key principle of the gamma SWE technique is the attenuation of the natural gamma-ray signal due to the snowpack (Carroll, 2001; Peck et al., 1980). The gamma SWE values are estimated using the difference in the rates of gamma radioisotopes (\(^{40}\)K, \(^{208}\)Tl, and gross count, GC) between over bare and snow-covered land surface (Cho et al., 2020a). The gamma-ray signal for designated flight lines are measured in the fall prior to freezing onset and then revisited in the winter. A gamma radiation detector equipped on a low-flying aircraft observes the gamma-ray particles. This detector measures terrestrial gamma radiation naturally emitted from trace elements of the three radioisotopes in the upper 20 cm of soil. The operational approach assumes the gamma rates over bare ground from the fall survey remain constant during the winter surveys. A typical gamma flight footprint covers approximately 5 km\(^2\) (a 300 m wide and 16 km long). The final gamma SWE value is generated as an area-mean value for each flight path. The airborne gamma SWE values are estimated using the equations below:

\[
SWE(\text{\(40\)K}) = \frac{1}{A} \cdot \left[ \ln \left( \frac{40K_h}{40K_s} \right) - \ln \left( \frac{100+1.11 SM(40K_s)}{100+1.11 SM(40K_h)} \right) \right] \tag{1}
\]

\[
SWE(\text{\(208\)Tl}) = \frac{1}{A} \cdot \left[ \ln \left( \frac{208Tl_b}{208Tl_s} \right) - \ln \left( \frac{100+1.11 SM(208Tl_s)}{100+1.11 SM(208Tl_b)} \right) \right] \tag{2}
\]

\[
SWE(GC) = \frac{1}{A} \cdot \left[ \ln \left( \frac{GC_b}{GC_s} \right) - \ln \left( \frac{100+1.11 SM(GC_s)}{100+1.11 SM(GC_b)} \right) \right] \tag{3}
\]

where \(^{40}\)K\(_b\), \(^{208}\)Tl\(_b\), and GC\(_b\) and \(^{40}\)K\(_s\), \(^{208}\)Tl\(_s\), and GC\(_s\) are uncollided gamma count rates in the top 20 cm of soil over bare and snow-covered grounds, respectively. \(SM(\text{\(40\)K}_s)\), \(SM(\text{\(208\)Tl}_s)\), and \(SM(GC_s)\) and \(SM(\text{\(40\)K}_b)\), \(SM(\text{\(208\)Tl}_b)\), and \(SM(GC_b)\) are the corresponding soil moisture values by weight (%). The airborne gamma SWE (\(SWE_{\text{gamma}}\); g cm\(^{-2}\)) is a weighted value by multiplying the three independent SWE estimates by weighting coefficients, 0.346, 0.518, and 0.136, and summing the calculated three values as below (Jones and Carroll, 1983; Carroll, 2001).

\[
SWE_{\text{gamma}} = 0.346 \cdot SWE(\text{\(40\)K}) + 0.518 \cdot SWE(\text{\(208\)Tl}) + 0.136 \cdot SWE(GC) \tag{4}
\]

The final SWE value is reported in the Standard Hydrometeorological Exchange Format (SHEF) product through the NOHRSC website (https://www.nohrsc.noaa.gov/snowsurvey/) (Carroll, 2001). In this study for dense forest environments, 1,508
airborne gamma SWE observations covering 79 flight lines flown over densely forested environments in the northeastern United States are used from January 1985 to May 2017.

### 3.2 UA SWE

The UA SWE is the ground observation-based 4-km gridded SWE product developed by consistently assimilating the snow telemetry (SNOTEL) SWE and NWS Cooperative Observer Program (COOP) snow depth measurements with the Parameter-elevation Regressions on Independent Slopes Model (PRISM) temperature and precipitation data over the continental United States (Broxton et al., 2016a; Zeng et al., 2018). In this study, the UA SWE is used as reference data to evaluate and compare the open-loop and assimilation results from the Noah-MP simulations. The accuracy and robustness of the UA SWE product have been proven by examinations of point-to-point and pixel-to-pixel interpolations (Broxton et al., 2016a, b), and evaluations against independent airborne snow observatory (ASO) LiDAR-based SWE and gamma radiation SWE measurements (Dawson et al., 2018; Cho et al., 2020b). Cho et al. (2020b) demonstrated that the UA SWE product strongly agreed with the airborne gamma SWE regardless of land cover type and snow classification over the continental U.S. This product has been used as a reference SWE for multiple purposes such as quantifying uncertainties in land surface modeled SWE (Kim et al., 2020; Zhang et al., 2022); characterizing extreme events (Welty and Zeng, 2021), and estimating extreme values for infrastructure design (Cho and Jacobs, 2020). The daily UA SWE product (version 1) from October 1984 to December 2017 is used in this study, which is publicly available from the National Snow and Ice Data Center website (https://nsidc.org/data/nsidc-0719).

### 3.3 AMSR2 Passive Microwave SWE

For comparison purposes, the existing satellite-based SWE retrievals from the Advanced Microwave Scanning Radiometer 2 (AMSR2) were also assimilated in this study. AMSR2 passive microwave sensor is the follow-on instrument to the Advanced Microwave Scanning Radiometer for Earth Observing System on board Aqua satellite (AMSR-E; Imaoka et al., 2010). AMSR2 on board the Global Change Observation Mission - Water (GCOM-W1) satellite has measured daily scans at 1:30 a.m./p.m. local time at 1–2 days revisit frequency since May 2012. AMSR2 SWE product is calculated by using snow depth estimated from an empirical relationship between snow depth and brightness temperatures observations at 19.7 and 36.5 GHz along with higher and lower frequencies and snow density values for each snow class from the Sturm's snow classification system (Kelly, 2009; Sturm et al., 2010). The Level 3 AMSR2 SWE products with the 10 km spatial grid were obtained from the JAXA GCOM-W1 Data providing service (http://gcom-w1.jaxa.jp). In this study, the AMSR2 data at descending overpass (01:30 a.m.) was used only to minimize the wet snow effect.

### 3.4 Tree cover fraction and topographic features

In this study, we used tree cover fraction (TCF) and topographic feature data sets to compare DA performance by the degrees of them. The NASA Making Earth System Data Records for Use in Research Environments (MEaSUREs) Vegetation Continuous Fields (VCF5KYR; Version 1) provides annual global fractional vegetation cover maps with three layers including
percent tree cover, percent bare ground, and percent non-tree vegetation at 0.05 degree spatial resolution from 1982 to 2016 (Hansen and Song, 2018). Among them, the percent tree cover was used. To account for the interannual variations in the fractional tree cover, annual TCF values were obtained for each gamma line. The elevation data (0.0083-degree grid) used in this study were an aggregated map using the Shuttle Radar Topography Mission (SRTM) 90 m resolution elevation data (Farr et al., 2007). The slope and elevation range maps with the same spatial grid were obtained using the “raster” R-package (“terrain” function in this package; Wilson et al., 2007). The elevation range, referred to as “topographic heterogeneity” in this manuscript, was calculated as the difference between the minimum and maximum elevation value among a given grid and its surrounding eight grids (total nine grids). The three topographic features were computed by areal-weighted average for each gamma flight footprint.

4. Model and Methods

4.1 Noah-MP

Noah-MP (v3.6; Niu et al., 2011; Yang et al., 2011) was employed to simulate snow variables such as SWE and snow depth. Noah-MP was developed based on the original Noah LSM (Ek et al., 2003) with improved representations of biophysical and hydrological processes. A grid cell in Noah-MP consists of one vegetation canopy layer, up to three layers (depending on the whole snow depth) of snowpack, four soil layers (with thicknesses of 0.1 m, 0.3 m, 0.6 m, and 1.0 m from top to bottom), and an unconfined aquifer layer. Regarding snow processes, intercepted snow exists in Noah-MP as solid and liquid phases on the vegetation canopy, and melting/refreezing of intercepted snow, dew/evaporation, and frost/sublimation on the vegetation canopy are explicitly represented in the model. Snow depth and SWE are simulated by considering snow layer compaction by the weight of the overlying snow layers, snow metamorphisms (destructive and melt), and snowmelt-refreeze processes. An ensemble of model initial conditions was constructed through a two-step spin-up procedure. First, a single-member model simulation was run for 40 years, from 1 January 1980 to 1 January 2020, driven by NASA Modern-Era Retrospective analysis for Research and Applications, version 2 (MERRA-2; Bosilovich et al., 2015) forcing. Then, using a restart file generated in the first step, an additional 3-year spin-up, from 1 January 1981 to 1 March 1984, was conducted using 20 ensemble members. The open-loop (OL; without assimilation) and data assimilation (DA) experiments were run from 1 March 1984 to 1 October 2017 using the 20-member ensemble initial conditions. A model simulation time-step of 15 minutes was used, and daily mean outputs were evaluated.

4.2 Assimilation Scheme

Data assimilation experiments were conducted within the NASA LIS (Kumar et al., 2006; Peters-Lidard et al., 2007; Kumar et al., 2008). The ensemble Kalman filter (EnKF) scheme was applied (Reichle et al., 2002) to assimilate airborne gamma radiation-based SWE retrievals into Noah-MP. In the EnKF scheme, model uncertainty is implicitly represented by the ensemble spread and an ensemble size of 20 was used in this study. The ensemble spread was generated by perturbing
meteorological forcing fields and prognostic model state variables with the assumption of a Gaussian distribution. Perturbation parameters applied during the OL and DA runs were adopted from Kwon et al. (2021). When observations (i.e., airborne gamma SWE) are available, EnKF updates forecasted model state variables using the following equation:

\[ M_i^+ = M_i^- + K(Obs - H M_i^-) \]  

(5)

where \( M_i^+ \) is the updated (after assimilation) model states (i.e., SWE); \( M_i^- \) is the forecasted (before assimilation) model states (i.e., SWE); \( Obs \) is the gamma SWE retrievals; \( H \) is the observation operator (\( H = 1 \) in this study); \( i \) denotes the ensemble member; and \( K \) is the Kalman gain given by:

\[ K = \text{Cov}(M_i^-, HM_i^-)\{\text{Cov}(HM_i^-, HM_i^-) + R\}^{-1} \]

(6)

where \( \text{Cov}(M_i^-, HM_i^-) = \text{Cov}(HM_i^-, HM_i^-) \) is the covariance of the model forecasted SWE, and \( R \) is the covariance of the observation error. The gamma SWE retrieval error standard deviation of 23 mm was assumed based on realistic error values from previous studies such as Carroll and Vose (1984). Note that assimilation of gamma SWE updated only modeled SWE while snow ice and liquid water content, and snow depth were adjusted based on the SWE update by assuming that snow density does not change before and after the analysis update.

4.3 DA localization

Due to its sparsity in space, the airborne gamma radiation-based SWE observations can be limited to be used within the DA system. To quantify if the spatially sparse gamma SWE observations can improve the SWE estimates in the surrounding areas, where the observations are not available, we apply a distance-based localization method into the assimilation procedure. That is, the updates of the SWE estimates for the flight lines are added to other grid cells within a specified distance from the flight lines by applying a localization weight (\( W \)), which is calculated using the Gaussian decay-based localization method as follows:

\[ W = \exp \left( \frac{-d^2}{2(\sigma^2)} \right) \]

(7)

where \( d \) is the distance between the updated grid cells (i.e., flight lines) and grid cells without observations within a specified localization radius \( r \). If a grid cell is affected by multiple flight lines, an average of the updates is added to the prior SWE estimates of the grid cell. We apply a localization function with six different distances (e.g., 4, 8, 16, 24, 32, and 48 km from the lines). For an evaluation of the DA SWE with a given localization weight, the areal mean DA SWE time series are obtained.
for an effective area buffered by a specified distance around the gamma flight line. The areal mean OL and UA SWE time series are also obtained in the same way to compare with the corresponding OL and UA SWE values.

5. Results and discussion

5.1 Comparison between DA and OL SWE with airborne gamma SWE

To examine the updated SWE performance over the gamma lines by assimilating airborne gamma observations into Noah-MP, statistical metrics were compared between OL and DA SWE using UA SWE (Figure 2). The values of 1:1 slope were closed to 1 (A median slope of OL was 1.45) and RMSD values decreased, even though negative biases were found. The lower bias of the SWE estimates from the OL as compared to the DA in Figure 2 was a consequence of the fact that the overestimated SWE during the accumulation season and early in the melt season was offset by the underestimated SWE during the snowmelt season (i.e., April and May). When the gamma SWE observations exist during the accumulation period (which is a typical case), DA corrected the overestimated SWE, whereas it further underestimated SWE in the snowmelt season (Figures 3 and 4), resulting in the increased (negative) bias, as presented in Figure 2. The OL SWE was largely deviated from the 1:1 linear relationship during the snow accumulation season (i.e., January, February, and March) and early in the snowmelt season (i.e., April). Figure 3 shows that the deviation was significantly reduced through the assimilation of the gamma SWE retrievals even though a reduced R-value was obtained.

Figure 2. Comparison of statistics between open-loop (OL) SWE and data assimilated (DA) Noah-MP SWE estimates by using airborne gamma radiation SWE observations with the University of Arizona SWE from 1985 to 2017: (a) slope from 1:1 plot, (b) Bias, and (c) RMSE from a linear relationship between the estimated SWE and UA SWE.
A promising aspect is that the assimilation of the temporally sparse (i.e., only one or two data points at the end of the snow accumulation period and/or early in the snowmelt period) airborne gamma SWE retrievals enhanced the model estimates of SWE, which was particularly noticeable in some lines and years, such as the gamma line SJ150 in WY1991 (Figure 4). For comparison purposes, results of assimilating the AMSR2 SWE retrievals were also plotted (green solid line in Figure 4). As
shown in the figure, the AMSR2 SWE was largely deviated (underestimated) from the UA SWE in densely forested areas, and assimilating the AMSR2 SWE data led to degradation of the SWE estimates. This further emphasizes the effectiveness of the gamma SWE data in improving the model estimates of SWE via assimilation in forested areas even with fewer available data compared to the AMSR2 SWE. However, the assimilation of the airborne gamma SWE measurements was not able to improve the snow ablation timing probably due to temporally sparse gamma data as well as limited model physics. As shown in Figure 4, compared to the UA SWE, Noah-MP simulated earlier snow melt-out despite the overestimated snow accumulation, which may be attributed to the Noah-MP model structure and physics (e.g., simplified representations of snow layers). The availability of more frequent gamma observations during the snowmelt season could lead to further improvements in estimating SWE in the ablation period while the Noah-MP snow layer representation needs to be enhanced.
Figure 4. Examples of daily SWE time series of three gamma lines (SJ150, NH106, and NH109) with latitude (Lat), longitude (Lon), elevation (Elev), and vegetation cover fraction (VCF) for individual years including the open-loop (OL) and gamma data assimilated (DA_Gamma) Noah-MP SWE estimates along with the passive microwave SWE data from the Advanced Microwave Scanning Radiometer 2 (AMSR2) and AMSR2 data assimilated SWE (DA AMSR2).
5.2 Effect of land surface characteristics on assimilation performance

To examine effects of land surface characteristics on the DA performances as compared to the OL, the performance of the gamma SWE DA, presented as differences (i.e., DA minus OL) in the 1:1 slope, bias, and RMSD, with the UA SWE were compared by four physical features, TCF, slope, elevation range (i.e., topographic heterogeneity), and elevation (Figure 5). In the figure, two groups of each land surface characteristics were determined by dividing the gamma flight lines into two (i.e., low and high) groups of equal numbers of the flight lines. For TCF, DA SWE in a group with low TCF (less than 85%) has lower bias and RMSD than OL SWE, while the DA performances show relatively marginal improvement in the high TCF. Considering that the TCF values in the low group ranges from 31% to 84% (mean: 62 %), DA using airborne gamma SWE improved SWE over densely forested regions.

Differences in the DA performance between the low and high groups were observed for all surface characteristics. The 1:1 slope was updated by DA for both the lower and higher ranges of all surface characteristics. DA led to larger improvements in the 1:1 slope and RMSD for lower VCF, slope, elevation range, and elevation. With respect to the bias, assimilation of the gamma SWE retrievals improved the group-averaged performance for both the lower and higher groups of the surface characteristics with larger improvement in lower VCF and higher slope, elevation range, and elevation. For individual physical characteristics, the added value of the gamma SWE data on the model SWE estimates via assimilation was greater for the lower VCF range based on both bias and RMSD. It is worth noting that the lower VCF ranges from 31% to 84%, and DA significantly improved the SWE, even for the higher VCF (i.e., greater than 85%). This implies that the gamma-based SWE estimates within DA frameworks can be a promising alternative to traditional \( T_B \)-based approaches in forested areas. Comparable DA performance patterns were also obtained for other land surface characteristics. Although the gamma SWE DA exhibited smaller RMSD improvements in areas with higher topographic heterogeneity, than those with lower ranges, it was still effective in reducing error statistics.
Figure 5. Boxplots of differences in (a) Slope from 1:1 plot, (b) Bias, and (c) RMSD between the DA and OL cases (computed as DA – OL) with respect to vegetation cover fraction (VCF), slope (degree), elevation range (m), and elevation (m). The two groups (low/high) were divided into equal numbers of values. The bottom values are 50% quantile values for each characteristic.
5.3 Localized data assimilation (DA) performance

One of the limitations of the airborne gamma SWE observations is a limited spatial coverage, which is typically 5-7 km² with a swath 300 m wide and 15-30 km long. It is necessary to assess if the spatially sparse airborne gamma SWE observations can also improve the SWE estimates in the surrounding areas, where gamma flights do not exist, via assimilation. Here, the DA experimental cases that employ a localization function with different distances (e.g., 4, 8, 16, 24, 32, and 48 km) for the whole (accumulation and melting periods), accumulation, and melting periods, respectively.

*Figure 6.* Localized data assimilation (DA) and open-loop (OL) Noah-MP SWE performances as compared to the UA SWE with different localization distances (e.g., 4, 8, 16, 24, 32, and 48 km) for the whole (accumulation and melting periods), accumulation, and melting periods, respectively.

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lines) are evaluated (Figure 6). The OL/DA statistics in the figure are calculated using domain-averaged time series of OL/DA SWE over the effective surrounding areas by localization distances with the corresponding UA SWE. For the whole snow season that includes both accumulation and melting periods, the boxplot of the 1:1 slope shows that the localized DA SWE were remarkably improved as compared to OL. The slope of the DA SWE is closed to 1 by up to 32 km distance while the OL’s slope continually increased by up to 1.4, indicating an overestimation of 40%. The RMSD boxplot also shows that the DA SWE has lower errors than the OL SWE for all localization distances, except 4 km. The OL’s RMSD increased with increasing the distances up to 16 km (median: 66 mm) and above that, the differences remain approximately constant, while the DA’s RMSD values slightly decreased with increasing the distances up to 32 km (median: 53 mm). When the statistics were calculated for the accumulation and melting periods separately, the lower RMSDs and slopes closer to 1 of the localized DA SWE were found consistently. As previously discussed, the efficacy of assimilating the airborne gamma SWE is greater during the accumulation period, especially for bias and RMSD, than during the melting period. Even in the melting period, some improvements in the RMSD and 1:1 slope with longer distances are achieved.

The localized gamma DA outputs using the 32-km localization distance are compared with the AMSR2 DA outputs (Figure 7). Because the AMSR2 SWE was largely underestimated in the study domain (see Figure 4), assimilating the AMSR2 SWE measurements did not improve the modeled SWE estimates. All error metrics of the AMSR2 DA SWE were degraded (e.g. median bias: 160 mm and RMSD: 175 mm) as compared to the OL (bias: 49 mm and RMSD: 76 mm). The localized gamma DA SWE performance is clearly improved based on the error metrics. The positive biases (median: 50 mm) and high slopes of the OL SWE were improved, and the RMSD also decreased approximately by 25 mm.

Overall, we found that the localized DA using the airborne gamma SWE observations reduced the model SWE’s errors up to 32 km distances, which is supported by the recent study that a single gamma SWE observation spatially represents up to 50 km even in dense temperature forest environments (Cho et al., 2022). The study found that there was strong agreement between the gamma SWE observations and in-situ snow course transects (R-value: 0.78; RMSD: 53 mm) at distances up to 50 km in the northeastern U.S. The results in this study indicate that, even though the airborne gamma SWE measurements exist with limited spatial coverages, the combined use of the physical model and DA with the gamma SWE has a potential to improve regional estimations of the SWE.
6. Limitations

We observed two issues associated with the Noah-MP SWE estimates in the study domain: 1) Noah-MP considerably overestimated SWE during the snow accumulation period; while 2) it underestimated SWE (i.e., early snowmelt) during the snow ablation period (see Figure 4). The former issue was mitigated through the assimilation of the gamma SWE retrievals, whereas the latter issue was not. The overestimated SWE during the snow accumulation period was likely attributed to a precipitation phase partitioning method employed in Noah-MP. Given the same amount of total precipitation, different phase partitioning methods lead to substantial differences in the amount of snowfall (Xia et al., 2017; Jennings et al., 2018; Suzuki and Zupanski, 2018; Letcher et al., 2021). Noah-MP uses the scheme of Jordan (1991), in which total precipitation is fractionally divided into rainfall and snowfall using two thresholds of air temperature (i.e., no snowfall when Tair > 2.5°C; all precipitation is snow when Tair ≤ 0°C; and fractional snowfall when 0°C < Tair ≤ 2.5°C). However, Noah-MP uses a spatially uniform threshold of Tair. Jennings et al. (2018) found that rain-snow Tair thresholds exhibited significant spatial variability across the Northern Hemisphere with the warmest thresholds in continental and mountain areas while with the coolest thresholds in maritime areas and lowlands. This implies that the high Tair threshold (i.e., 2.5°C) used in Noah-MP may lead to the overestimated snowfall, and subsequently the overestimated snow depth and SWE as the study area is characterized by
maritime. Letcher et al. (2021) demonstrated that the use of cooler $T_{air}$ thresholds in Noah-MP can significantly improve the estimates of peak SWE in the northeastern United States. The SWE estimates of Noah-MP with the assimilation of the gamma SWE retrievals can be further improved by using more refined precipitation phase partitioning methods that consider both air temperature and humidity as suggested in Jennings et al. (2018).

Simplified snow layering schemes (i.e., single snow layer) with the assumption of the same snow density for the entire snow column cause rapid snowmelt (e.g., Kwon et al., 2014; Suzuki and Zupanski, 2018). Although the snowpack in Noah-MP can have up to three snow layers, it may not be enough to accurately reproduce the energy budget within the snowpack in the study area. Further improvement in the modeled SWE during the melting season can be achieved by employing a more sophisticated snow model. Meanwhile, the current DA framework does not perform assimilation if one or more of the prior model ensemble members do not have snow. Thus, the gamma SWE retrievals could not add value to the SWE estimates during the snow melting period. To address this issue, a rule-based approach (e.g., Kwon et al., 2019), that adds a thin snow layer when the model simulates snow-free conditions, but observations have snow, can be explored in a future study.

While the airborne gamma radiation SWE was used to enhance SWE estimations by assimilating into Noah-MP land surface models, it is possible that the inherent uncertainties in the gamma radiation method limit the potential improvements through DA. The potential sources of error in the gamma SWE retrievals have been explored in previous findings (Carroll & Carroll, 1989a, 1989b; Glynn et al., 1988; Offenbacher & Colbeck, 1991). An impact of forest biomass on the accuracy of airborne gamma SWE measurements has been examined over forested watersheds (Carroll & Vose, 1984; Vogel et al., 1985). Carroll and Vose (1984) presented that there was 23 mm of RMSE between airborne gamma SWE and in-situ SWE for the moderate snowpack (20 to 470 mm of in-situ SWE) in Lake Superior and Saint John basins, New Brunswick, Canada. Spatial variability in elevations over the gamma flight footprint can cause larger errors in SWE (Cho et al., 2020b; Carroll & Carroll, 1989b; Cork & Loijens, 1980). Cho et al. (2020b) found that heterogeneous characteristics (e.g. elevation range and slope) within a flight line cause underestimates of gamma SWE as compared to UA SWE. Cork & Loijens (1980) discussed that the measurements of the attenuation of the gamma count rate over the snowpack with its large spatial variability were systematically underestimated leading to the SWE underestimation. Because the results use the NOAA standard gamma radiation SWE retrievals without manual corrections, the DA results would be improved with the updated gamma SWE products in regions by correcting the existing potential errors. Lastly, the spatiotemporal sparseness of the airborne gamma SWE observations due to the operational costs is an inherent issue that may limit the widespread use of gamma SWE observations for DA work. However, as proven in our findings, effective uses of the gamma SWE (e.g. localization function) will maximize the utility of the gamma SWE into the DA framework.
7 Conclusion and Future Perspectives

In the snow hydrology community, DA has been used as a promising alternative to improve SWE estimation at a large spatial scale by merging remote sensing observations with LSM predictions. In densely forested regions, however, most remote sensing techniques have limited performance of SWE due to attenuating or/and scattering radiation signals by canopy (e.g. passive microwave $T_b$ and Lidar), resulting in large uncertainty in DA outputs. The historically well-established, airborne gamma radiation technique has provided a strong potential in wet snow and dense forest conditions, because the gamma approach uses an attenuation difference in the terrestrial gamma-ray emission by water in the snowpack (any phase) between snow-off and snow-on conditions. In this study, the airborne gamma SWE observations are assimilated with the Noah-MP model’s SWE in densely forested regions in the northeastern U.S. We found that the assimilation of the airborne gamma SWE observations enhanced the model SWE estimates despite the limited number of the measurements (up to four SWE values during a winter period). The added value of the gamma data on the model SWE estimates was greater for the relatively lower VCF range. For areas with higher topographic heterogeneity, the gamma-based DA SWE was still effective in reducing the errors. We also found that the localized DA with the gamma SWE observations with distances up to 32 km reduced the model SWE’s errors, indicating the gamma SWE has a potential to improve regional estimations of the SWE and subsequently snowmelt runoff. Despite the accuracy of the gamma data on the DA framework, the improvements were limited by the spatial and temporal sparseness of the gamma measurements and the uncertainties in the Noah-MP physics (i.e. precipitation partitioning and simplified snow layers). With the enhanced physics in LSMs and optimal uses of the gamma data using enhanced DA/interpolation methods, future studies may achieve a further improvement of the modeled SWE for larger areas where gamma flights do not exist.

Data availability. The airborne gamma radiation SWE data are freely available from the NOAA NWS NOHRSC website (http://www.nohrsc.noaa.gov/snowsurvey/). The UA daily 4-km SWE data (Version 1) and JAXA AMSR2 L3 Global Daily 10 km SWE data (Version 1) are available from the website (https://nsidc.org/data/nsidc-0719 and https://gportal.jaxa.jp/gpr/information/download, respectively). The MERRA2 forcing dataset is distributed by the NASA Goddard Global Modeling and Assimilation Office (GMAO; https://gmao.gsfc.nasa.gov/reanalysis/MERRA-2/data_access/). To replicate the land surface model simulation and data assimilation, users can freely access the NASA Land Information System at https://github.com/NASA-LIS/LISF.

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