



# **Spatiotemporal changes of drought area as input for a machine-learning approach for crop yield prediction**

Vitali Diaz<sup>1,2</sup>, Ahmed A.A. Osman<sup>3</sup>, Gerald A. Corzo Perez<sup>1,2</sup>, Henny A.J. Van Lanen<sup>4</sup>,  
Shreedhar Maskey<sup>1</sup>, Dimitri Solomatine<sup>1,2,5</sup>

<sup>1</sup>IHE Delft Institute for Water Education, Delft, 2601 DA, the Netherlands

<sup>2</sup>Delft University of Technology, Delft, the Netherlands

<sup>3</sup>Arcadis, Wales, United Kingdom

<sup>4</sup>Hydrology and Quantitative Water Management Group, Wageningen University, Wageningen, the Netherlands

<sup>5</sup>Water Problems Institute of the Russian Academy of Sciences, Moscow, Russia

**Corresponding author:** Vitali Diaz; v.diazmercado@tudelft.nl; vitalidime@gmail.com

## **Abstract**

Climate change has increased the possibility of more severe and prolonged droughts worldwide, which requires innovative methods to predict their impacts on different sectors such as agriculture. Crop growth models calculate yield and variables related to plant development and are used for crop yield estimation, a useful variable for monitoring drought impacts. Although used for prediction, these crop models are not explicit forecasting models; they are limited to the physical assumptions reflected in their conceptual model. In addition, the input data availability, the spatial and temporal aggregation, and different sources of uncertainty make the crop yield prediction challenging. Given these limitations, machine learning (ML) models are often utilised following a multivariable forecasting approach, but their use with the spatial characteristics of droughts as input data is limited. This research explored the spatial extent of drought as input data for building an approach for predicting seasonal crop yield. This ML approach is made up of two components. The first includes polynomial regression (PR) models, and the second considers artificial neural network (ANN) models. This approach aimed to evaluate both types of ML models (PR and ANN) and integrate them into one operational tool. The logic is as follows: ANN models determine the most accurate predictions, but in practice, issues regarding data retrieval and processing can make the use of equations, i.e. PR, preferable. The proposed approach provides these PR equations with early and preliminary input to perform such calculations. The estimates can be further improved when the ANN models are run with the final input data. The results indicated that the empirical equations (PR) produced good predictions when using drought area as the input. ANN provides better estimates, in general. The results presented are a proof of concept showing the capabilities of this ML approach to predict drought impacts with a certain degree of confidence. Research results show that the spatiotemporal changes of drought area and its temporal aggregation provide an important pre-processing alternative to implement ML models for drought impact prediction.

## **Keywords**

Spatio-temporal analysis, crop yield, drought impact, machine learning, agricultural drought



## 37 **1 Introduction**

38 Drought frequently hits many regions across the world. It negatively affects various human  
 39 activities such as agriculture, which not only generates economic losses but can also trigger  
 40 famine, causing millions of deaths (Below et al., 2007; Food and Agriculture Organization of  
 41 the United Nations (FAO), 2017; Kim et al., 2019; Sheffield and Wood, 2011; World  
 42 Meteorological Organization (WMO), 2006). Hence, methods that help to improve strategies  
 43 for drought mitigation are necessary. Within these methods are those that allow predicting the  
 44 impacts of drought.

45 Assessments of drought impacts confirm that the presence of drought on human activities can  
 46 be devastating. For instance, the Food and Agriculture Organization of the United Nations  
 47 (FAO) calculated the damage and losses in the agricultural sector caused by five types of  
 48 hazards, including drought. FAO estimates that drought causes damages and losses to the  
 49 agricultural sector by up to 80% (FAO, 2017). Although multiple factors are involved in  
 50 agriculture affectation, drought often plays the primary role, as literature confirms (Dai, 2011;  
 51 FAO, 2017; Kim et al., 2019).

52 The assessment of drought impacts on agriculture can be performed with the help of crop yield.  
 53 FAO defines crop yield as the measure of the yield of a crop per unit area of land cultivation  
 54 (in kg/ha or ton/ha) (FAO and DWFI, 2015). For assessing crop yield under drought affectation,  
 55 physical models based on crop properties turn out to be more comprehensive and descriptive  
 56 (Huang et al., 2019; Reynolds et al., 2000; White et al., 1997; Wu et al., 2016). However, an  
 57 important barrier to such models' realisation is the lack of detailed crop data and the difficulty  
 58 representing all the processes involved in all stages of crop development (Huang et al., 2019;  
 59 Reynolds et al., 2000; Wu et al., 2016).

60 Statistical and machine-learning (ML) models, which involve mathematical equations to  
 61 calculate the output of a model with suitable input(s), can be used to assess crop yield impact  
 62 by drought without considering any biological or physical process of the crop but the analysis  
 63 of the input and output data (Araneda-Cabrera et al., 2021; Chlingaryan et al., 2018; Rahmati  
 64 et al., 2020; Udmale et al., 2020; van Klompenburg et al., 2020). There have been studies where  
 65 various inputs, ML techniques, and architectures (configurations) have been tested for crop  
 66 yield prediction mainly following a multivariable forecasting approach (e.g., Chlingaryan et  
 67 al., 2018; van Klompenburg et al., 2020). However, the use of spatial characteristics of drought  
 68 such as its spatial extent has not been fully explored to crop yield prediction. The prediction  
 69 refers to the calculation of crop yield at the end of the growing season (harvesting) with



70 information available before or during the crop development season (pre-harvesting). Previous  
71 studies have found the spatial extent of drought to be highly correlated with the variation of  
72 crop yield, which motivates its use in the construction of crop yield prediction models in this  
73 research (Araneda-Cabrera et al., 2021; Diaz et al., 2016; Osman, 2018; Osman et al., 2018).  
74 This research aims to develop an ML approach to calculate seasonal crop yield (CY) with the  
75 monthly drought areas (DAs) as input. The ML approach comprises two components. Each  
76 component includes a set of the following types of ML models: polynomial regression (PR)  
77 and artificial neural network (ANN). The goal is to build both types of ML models (ANN and  
78 MR) and use them as an integrated tool to support the decisions made based on crop yield  
79 prediction. The logic is as follows. PR provides the prediction where the crop yield calculation  
80 is "clear" to the performer (the end-user) because she/he has access to the equations that have  
81 a straightforward interpretation and calculations can be done with early and preliminary input  
82 data. For its part, ANN is used as the most accurate model, although the output calculation is  
83 not as "clear" as in the case of PR due to the difficulty of interpreting the structure of the  
84 resulting ANN. The ANN is expected to be used with the final input data.  
85 Three East Indian regions where agriculture plays an important role were chosen as a case  
86 study. ML models were built for the period 1967-2015. ML models aim to predict rice crop  
87 yield since rice is the most cultivated crop in these regions. The ML approach was applied  
88 separately in each of the three regions.

### 89 **Crop yield prediction in India**

90 In India, as in many other countries, the official crop yield prediction is mainly based on  
91 conventional data collections techniques such as ground-field visits (Bhatt et al., 2014;  
92 Reynolds et al., 2000; Sawasawa, 2003). The crop yield is measured through crop cutting  
93 experiments carried out over sample crop areas. In this country, crops' area and yield  
94 calculations are released through the Directorate of Economics and Statistics, Ministry of  
95 Agriculture (DESMOA). A specific crop's production (in kg or ton) is calculated by  
96 multiplying the whole field area (cultivation district) by its crop yield. The crop production is  
97 needed for the decision-makers to take various policy decisions relating to pricing, marketing,  
98 distribution, exportation and importation.  
99 The Kharif season, as it is locally known, represents about 80% of the annual rainfall (Naresh  
100 Kumar et al., 2012). This monsoon season generally goes from June to October. In this season,  
101 the highest agricultural production is obtained. Estimation of Kharif crop yield and production  
102 is released four times during the year with different levels of sophistication and precision,



103 where the last one is considered the most accurate. The first calculation is presented in  
104 September, the second one in January, the third one in March/April, and the fourth, and the last  
105 one, in June/July. It should be noted that the last two calculations of crop yield and production  
106 become available much after the crops have already been harvested in December/January.  
107 From the four calculations, the first two can be considered predictions. These two first  
108 predictions serve as primary estimations about how much the final yield and production will  
109 be.

110 The existing ground-field visits-based crop yield calculation system provides reliable  
111 information for various crops, including rice, at the district, state, and country level for each of  
112 the four realisations previously described; however, it lacks pre-harvesting forecasting. This  
113 limitation of crop yield prediction motivated the creation of a satellite-based forecasting system  
114 to have information at the early stages of crop growth. The system is carried out by the  
115 Mahalanobis National Crop Forecast Centre (NCFC) (Sawasawa, 2003). The NCFC system is  
116 continuously verified and updated. Although the NCFC system advances the one based on  
117 ground-field visits by providing information in the early stages of crop growth, the data  
118 required for its execution may not always be available. Therefore, it is necessary to explore  
119 other solutions.

120 In this study, it is not intended to replace the previous and new forecasting systems in India but  
121 to provide a complement to corroborate calculations from both types of systems and, in a  
122 broader sense, to provide the scientific community with an approach to crop yield prediction  
123 with information on the spatial extent of drought.

## 124 **2 Data**

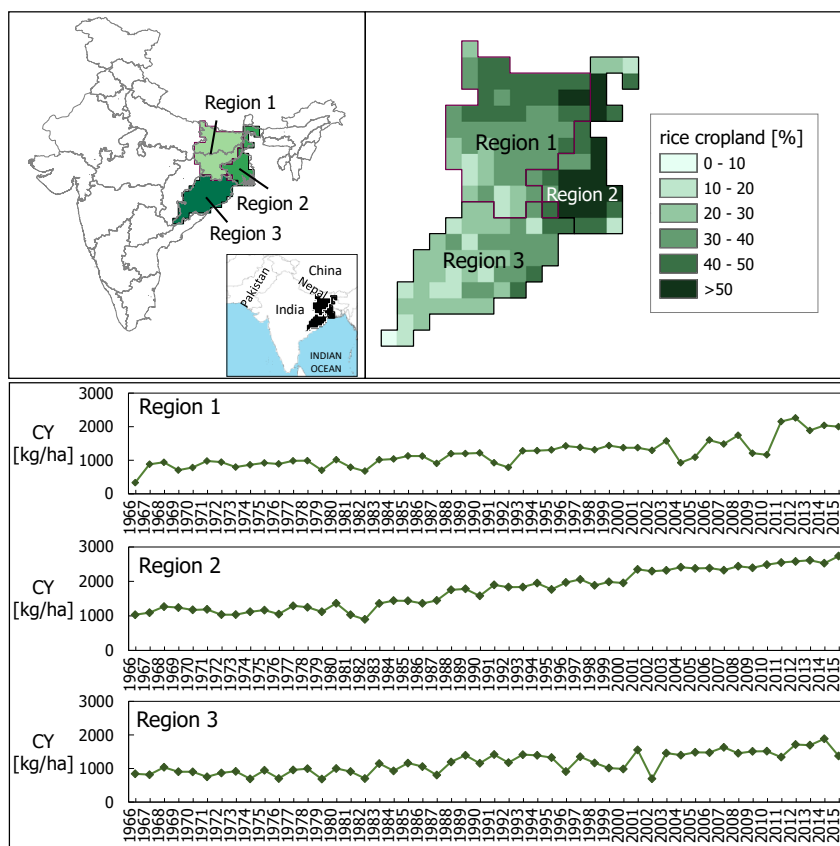
### 125 **2.1 Crop yield**

126 Rice is the most important food grain in East India, so it was selected to assess our ML-oriented  
127 crop-yield predictions. Rice from this region accounts for roughly 85 percent of the total rice  
128 production in India (Ghosh et al., 2014). As mentioned, ML models were constructed for three  
129 regions of the eastern Indian (Figure 1). State-wise crop-yield data was retrieved from 1966 to  
130 2015 (49 years) through the Indian Directorate of Economic and Statistics from the Department  
131 of Agriculture (DAC) (<http://eands.dacnet.nic.in/>).

132 Time series of crop yield data were arranged as follows. There are three crop seasons in India:  
133 Rabi, Kharif, and Zaid. Of these, the Kharif season was chosen for study because it is the largest  
134 in terms of crop production. Kharif crops are sown in June and harvested in  
135 November/December. Seasonal crop-yield data was obtained from the DAC website and



arranged into time series per region. In this way, one value was assigned to each year of crops harvested in the Kharif season (Figure 1). In the arrangement of the time series of the yield data, no data filling was carried out since there are data for each year in the three regions. Figure 1 also shows the location of the three regions. These regions are made up as follows. Region 1 includes the current states of Bihar and Jharkhand; region 2 corresponds to the state of West Bengal; and region 3 makes up the state of Odisha. Two important clarifications have to be made regarding crop yield data retrieving for these regions. First, in late 2000, Bihar was divided into two states: Bihar and Jharkhand. Thereafter, rice data was reported separately. In this study, both states are marked as region 1; the crop-yield data from 2000 to 2015 is the reported sum of current Bihar and Jharkhand. Second, in 2011, Orissa was renamed Odisha (region 3), but the territory remains the same. In this case, crop yield data for Odisha is that reported for the former Orissa and the current Odisha.



**Figure 1** Case study location (top) and crop yield (CY) data (bottom). Case study comprises region 1 (Bihar and Jharkhand), region 2 (West Bengal), and region 3 (Odisha). The rice cropland (in percentage) is indicated. Source of rice cropland: Monfreda et al. (2008).



## 152 **2.2 Drought indicator**

153 Soil moisture is the preferred variable for calculating agricultural drought indicators. However,  
 154 another widely disseminated way to indirectly infer this type of drought indicator is to use  
 155 meteorological drought indicators as proxies. Among these, the Standardised Precipitation  
 156 Evaporation Index (SPEI) proposed by Vicente-Serrano et al. (2010) has shown to be useful in  
 157 assessing agricultural drought. The SPEI follows a similar methodology as that of the widely  
 158 used Standardized Precipitation Index (SPI) (McKee et al., 1993), but with added consideration  
 159 for the difference between precipitation and evapotranspiration. SPEI data was retrieved from  
 160 the SPEI Global Drought Monitor (<https://spei.csic.es>) between 1901 and 2015. The spatial  
 161 resolution of the drought indicator data is 0.5 degrees. The SPEI data was available at different  
 162 aggregation periods; for this study, it was retrieved for the aggregation periods of 1, 3, 6, 9,  
 163 and 12 months, indicated as DI1, DI3, DI6, DI9, and DI12, respectively.

## 164 **3 ML modelling methodology**

165 The experiment was carried out with the following methodology that involves the ML  
 166 construction. The next paragraphs show each step in detail. These steps are (1) data preparation,  
 167 (2) input variable selection, (3) polynomial regression models calculation, (4) artificial neural  
 168 network models calculation, and (5) models application and combination.

### 169 **3.1 Step 1. Data preparation**

170 Two types of data were prepared, the crop yield (CY) and the drought areas (DA). For data  
 171 preparation, three tasks were carried out (1) data retrieving, (2) drought areas calculation, and  
 172 (3) data de-trending.

#### 173 **3.1.1 Data retrieving**

174 Section 2 showed what corresponds to data retrieving for crop yield (CY) and the drought  
 175 indicator (DI). A summary of CY and DI is as follows. Seasonal CY data correspond to the  
 176 largest growing season. CY time series has a value for each year for the period 1966-2015 (49  
 177 years). CY was available for each region. On the other hand, drought indicator data is on a  
 178 monthly basis for the period 1901-2015. The spatial resolution is half a degree.

#### 179 **3.1.2 Drought areas calculation**

180 The drought areas were calculated following the methodology presented below. These areas  
 181 were calculated for the three regions. Drought areas were calculated from the drought indicator  
 182 data that is in a grid format, i.e., each cell has associated a geographic location and a time step.  
 183 The calculation of drought areas started with the reclassification of all the cells of the drought  
 184 indicator data by non-drought and drought cells. The drought indicator data was evaluated cell



by cell to determine those that are in drought, i.e. drought condition. To determine drought and non-drought condition ( $D_s$ ), the Eq. 1 was applied (Corzo Perez et al., 2011; Diaz et al., 2019, 2020; Herrera-Estrada et al., 2017). Eq. 1 represents the following. When the drought indicator is below to the chosen threshold  $\tau$ , the value of 1 is used to indicate drought in the cell and non-drought is represented by the value of 0. This classification is performed for all the cells of the grid data in each time step ( $t$ ).

$$D_s(t) = \begin{cases} 1 & \text{if } DI(t) \leq \tau \\ 0 & \text{if } DI(t) > \tau \end{cases} \quad (\text{Eq. 1})$$

Once the ones-and-zeros data was obtained, the drought areas (DAs) were calculated for each region with Eq. 2. DA was computed as the ratio between the cells in drought and the total number of cells of the region ( $N$ ). In Eq. 2, the number of cell is denoted by  $c$ .

$$DA(t) = 100/N \cdot \sum_{c=1}^N D_s(t) \quad (\text{Eq. 2})$$

The number of cells ( $N$ ) of the mask is 63, 31 and 54 for region 1, 2 and 3. The masks in raster format were built for each region. The mask is an array of ones and zeros, where the value of 1 indicates the land. We used the threshold  $\tau = -1$  to calculate cells in droughts. This threshold is widely used to identify a cell in drought when working with standardised indices such as the used in this research (Sect. 2.2). Usually, drought indicator data is calculated at different aggregations periods. We retrieved this data for 1, 3, 6, 9, and 12 months of aggregation period (Sect. 2.2). DAs' time series were calculated for each aggregation period and are indicated as DA1, DA3, DA6, DA9, and DA12 (Figure 2).

### 3.1.3 Data de-trending

Data stationarity is typically assumed when modelling. However, the present study uses crop yield, which is non-stationary in nature. The crop yield depends on factors that affect its trend, such as drought, flood, cultivars, and its own management. Therefore, it is advisable to remove short-term fluctuations in crop yield before constructing the model (Montesino Pouzols and Lendasse, 2010).

Among the methods available to de-trend data, the 'first difference' method is popular due to its simplicity. In this method, the trend is removed from the time series by subtracting the previous value  $x^*(t-1)$  from the current one  $x^*(t)$ , as shown in Eq. 3. The de-trended value for the first time step ( $t = 1$ ) is not calculated. The length of the de-trended time series is  $n = m - 1$ , where  $m$  is the length of the original time series. The de-trended data  $x(t)$  has the same units as the original data  $x^*(t)$ .

$$x(t) = x^*(t) - x^*(t-1) \quad (\text{Eq. 3})$$



Once the trend is removed, all the steps for constructing the ML models are carried out with the de-trended time series. After the ML models are built, the de-trending procedure must be applied in reverse after calculating a new prediction  $x(t+1)$  to have that prediction in the magnitude to the original time series. The reverse de-trending procedure can be done with Eq. 4, which is the solution for Eq. 3 for the de-trended prediction  $x(t+1)$ . In practical terms, the prediction  $x^*(t+1)$  in the original magnitude is calculated by adding the de-trended prediction  $x(t+1)$  to the last value of the original time series, i.e.  $x^*(t)$ .

$$x^*(t+1) = x^*(t) + x(t+1) \quad (\text{Eq. 4})$$

The trend of the CY and DA time series was removed with Eq. 3. As can be observed, the method for removing the trend does not generate the value for the first time step; therefore, the de-trended CY data corresponds to the period 1967-2015 (49 years).

In the case of DA, Eq. 3 was applied as follows. Because the DA data is monthly, i.e. 12 values per year, and CY data is seasonal, i.e. one value per year, the DA time series were extracted and organised for each month from January to December to match them with the CY data (Figure 2). This extraction/organisation procedure was carried out for each of the five aggregation periods DA1, 3, 6, 9 and 12 months. A total of 60 DA time series ( $12 \times 5$ ) were obtained. To refer to these time series, a number (suffix) was added to indicate the month. In this way, for example, the time series DA3\_7 indicates the drought areas for July calculated from the drought indicator with 3-month aggregation period. Eq. 3 for the removal of the trend was applied to each of the 60 DA time series (Figure 2). The DA time series run from 1901 to 2015. For the construction of the ML models, the common period 1967-2015 (49 years) was chosen.

### 3.2 Step 2. Input variable selection

In an ML model, the input, known as the predictor, is generally made up of independent variables. These input variables are often arranged or aggregated in different ways to determine the best model input representation. An example of arrangement is by considering different previous time steps of the input variable, such as  $t-1$  (the previous time),  $t-2$ , and so on. Another way is by aggregating the input variable in different periods. For instance, when using drought indicators as the predictors (input), the aggregation periods include 3, 6, 9, 12, and 24 months. Other aggregations include the average, or other statistics, over a period. In this step, the idea is not to include all the variables and all their different possible arrangements or aggregations but rather to choose the suitable input variables and discard those that do not contribute significantly to the model's results.





250 There are different methods for selecting input variables. Based on the procedure, these  
 251 methods are classified into model-based and filter types (May et al., 2011). The model-based  
 252 type includes all those where the model runs and based on its performance, a specific variable  
 253 is chosen or discarded. The filter type includes methods where the variable is chosen *a priori*  
 254 through a generally statistical process and does not require the model to be run. Correlation  
 255 analysis, which falls under the second category, is often chosen for its simplicity and wide  
 256 application. Correlation is calculated between the time series of the output variable (CY in this  
 257 case) and the different input variables, including their various arrangements or aggregations.  
 258 In this study, for the selection of the relevant input variables, the correlation analysis was done.  
 259 The correlation was calculated between the de-trended time series of the seasonal CY and the  
 260 60 DAs (Figure 2). As mentioned before, due to DAs are monthly and CY is seasonal, 12 time  
 261 series of DAs were prepared, one per month, for each aggregation period. The DAs were then  
 262 correlated with the CY. Another option could be to use the yearly average value of the DAs,  
 263 such as the average of the DAs of the months of the cultivation period, or something similar.  
 264 However, we opted to identify the DAs of the months that have the highest correlation with the  
 265 seasonal CY and use them as inputs.

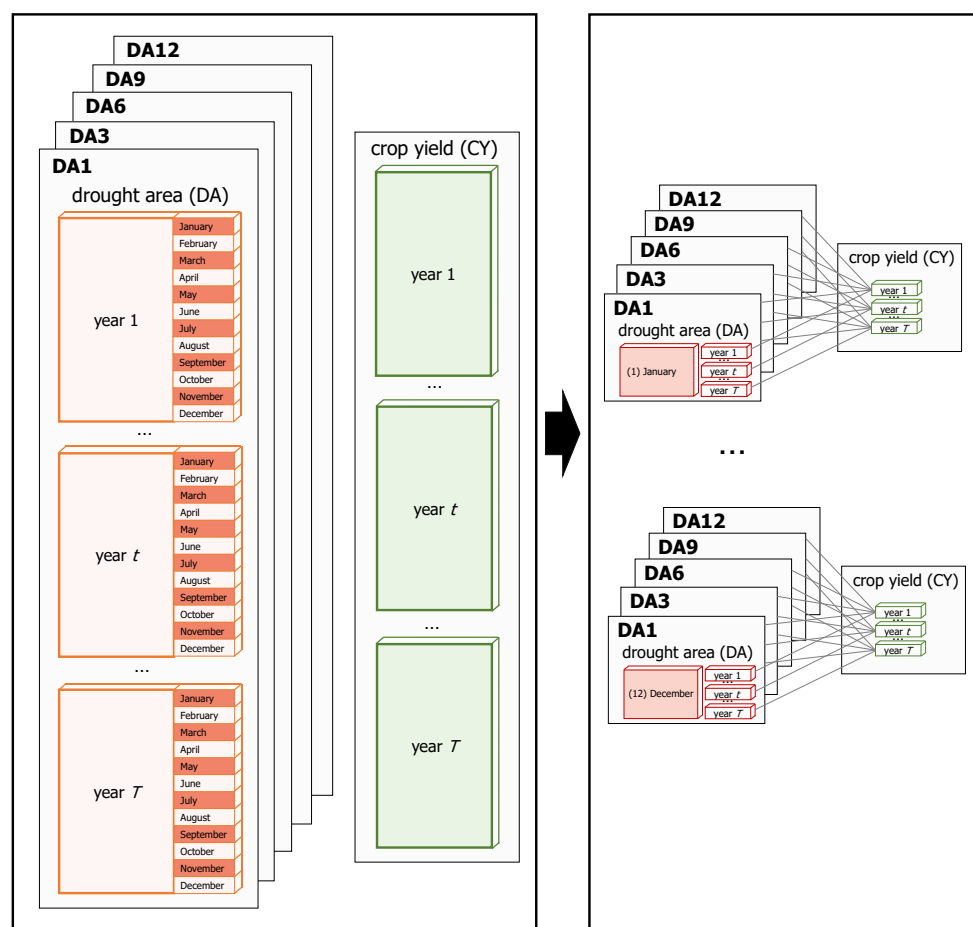
266 The approach of the selection of the most correlated DAs was chosen for two main reasons.  
 267 First, on the one hand, rice responds to the climate variations differently from one growth stage  
 268 to another over the year, which could be better captured with the information of some months  
 269 than others. On the other hand, different types of drought (i.e. meteorological, agricultural, and  
 270 hydrological) are expected to affect (impact) the crop yield to varying degrees throughout the  
 271 different stages of crop growth. This level of impact could be taken into account either by using  
 272 different hydro-meteorological variables or selecting different aggregation periods of the  
 273 meteorological variables, as in this case. An average of DAs could "hide" a significant drought  
 274 area that could contribute more (or less) to the final crop yield.

275 Second, in this research, ML models were built to be used at different stages of crop cultivation,  
 276 i.e. models to be applied in June, July, and so on, each of them with a different expected degree  
 277 of accuracy. Therefore, the use of time series for each month extracted from the DAs for all  
 278 the different aggregation periods (1, 3, 6, 9, and 12 months) is more appropriate than the  
 279 average (Figure 2).

280 Based on the correlation coefficient, the input variables were chosen. In total, 15 sets of input  
 281 variables (Table 2) were selected. Each set is made up of the different DA time series, i.e. DA1,  
 282 3, 6, 9, and 12. The number of variables is different in each set. These sets of input variables  
 283 are presented in the results section. All sets also include the de-trended CY from the previous



year ( $CY_{t-1}$ ).  $CY_{t-1}$  was used because, in the particular case of the study area, CY of the current year is planned to be reached based on data of the previous year. The ML models were built for each month (from January to December). The sets of inputs presented in Table 2 (Sect. 4.2) indicate which time series of DAs have to be considered for the ML model's construction. The models were built for each of the 15 input sets, more details are in the following sections. It should be noted that for each month the DAs are those corresponding to the same month.



**Figure 2** Diagram showing how time series of monthly drought areas (DAs) are extracted and organised to match them with the seasonal crop yield (CY) data. For each year there are 12 DA values and one CY value. DAs were calculated for the aggregation periods 1, 3, 6, 9, and 12 months (DA1 to DA12). DAs were extracted and organised by month, from January to December. For each month, the procedures of data de-trending, correlation, input variable selection, and ML models construction were carried out. The entire flow was conducted for each of the three regions analysed.



### 3.3 Step 3. Polynomial regression models calculation

For the case of PR, four types of models were tested (Table 1). All the PR models were built for each month from January to December following Eq. 5 to 8. A total of 15 sets of combinations of input variables were tested in each PR model. The best PR model was identified for each month following the RMSE criterion (Eq. 9). MATLAB software was used for implementation.

PR is an extension of linear regression that allows the use of more than one input variable to calculate the output variable (Eq. 4).

$$y = b_0 + \sum_{i=1}^n b_i x_i + e \quad (\text{Eq. 4})$$

In Eq. 4,  $y$  is the output variable, also known as the response, which in this case is the crop yield. The term  $x_i$  is the  $i$ -th input variable (predictor) from a total of  $n$  variables. The regression coefficients vector is represented by  $b$ . From the coefficients vector,  $b_0$  is known as the intercept. The vector of errors is indicated by  $e$ .

Table 1 shows four formulations of PR. The PR models are indicated as linear, pure-quadratic, quadratic, and interactions. Descriptions of each and their equations are presented in Table 1 (Eq. 5 to 8). The input variable ( $x_i$ ) was selected based on the correlation analysis (Sect. 2.2).

**Table 1** Polynomial regression (PR) types followed in this study.

PR type	Equation	Description
Linear	(Eq. 5) $y = b_0 + \sum_{i=1}^n b_i x_i$	It has an intercept and linear terms of predictors
Pure-quadratic	(Eq. 6) $y = b_0 + \sum_{i=1}^n b_i x_i + \sum_{i=1}^n b_{n+i} x_i^2$	It has an intercept, as well as linear and squared terms of predictors
Quadratic	(Eq. 7) $y = b_0 + \sum_{i=1}^n b_i x_i + \sum_{i=1}^n b_{n+i} x_i^2 + \sum_{i=1}^{n-1} \sum_{j=i+1}^n b_{2n+(i-1)n-\frac{(i-1)i}{2}+(j-i)} x_i x_j$	It has an intercept, linear and squared terms and all products of pairs of distinct predictors
Interactions	(Eq. 8) $y = b_0 + \sum_{i=1}^n b_i x_i + \sum_{i=1}^{n-1} \sum_{j=i+1}^n b_{n+(i-1)n-\frac{(i-1)i}{2}+(j-i)} x_i x_j$	It has an intercept, linear terms of predictors, all products of pairs of distinct predictors and no squared terms



317 The best PR model was identified from four types using the root mean square error (RMSE)  
 318 criterion. The RMSE is calculated between the observations ( $o$ ) and the predictions ( $p$ ), as  
 319 shown in Eq. 9. RMSE is one of the most widely used criteria in the comparison of observations  
 320 and model calculations.

$$321 \quad \text{RMSE} = \sqrt{\frac{\sum_{i=1}^n (o_i - p_i)^2}{n}} \quad (\text{Eq. 9})$$

#### 322 **3.4 Step 4. Artificial neural network models calculation**

323 ANN is a method loosely based on imitating the basic functionality of neurons (i.e. the working  
 324 units of the human brain) (Govindaraju, 2000; Maier and Dandy, 2000). The input variables  
 325 (predictors) are connected to each other through mathematical formulations that allow complex  
 326 non-linear relationships to be represented. These connexions are symbolised as nodes  
 327 interconnected within a network aimed at calculating the output variable (response).

328 Of the different proposed ANN architectures (network designs), one of the most widely used  
 329 is the feedforward neural network (FFNN). The FFNN is schematised by a series of nodes  
 330 located in one of three layers: input, hidden or output. The number of input nodes is equal to  
 331 the number of input variables in the input layer (Elshorbagy et al., 2010). This first layer is in  
 332 turn connected to the hidden layer, which receives this name because the connections made  
 333 there may not be immediately evident to the model performer. In this hidden layer, the number  
 334 of nodes is not defined by default; rather, the greater the number of nodes, the more complex  
 335 the model. Finally, the nodes of the hidden layer are connected to those of the output layer. In  
 336 a single-output variable problem, there is only one node. ANNs are typically trained by non-  
 337 linear optimisation gradient-based algorithms, e.g. the Levenberg-Marquardt algorithm.

338 In the ANN setup, the number of nodes of the input layer was equal to the number of variables  
 339 of the respective combination. The number of nodes in the output layer was one and  
 340 corresponded to the seasonal crop production (CY). An iteration optimisation procedure was  
 341 carried out regarding the hidden layer, varying the number of nodes from 1 to 10. For each  
 342 number of nodes, 100 iterations were done, being 1,000 in total. For reproducibility of the  
 343 results, the random values were set to default at the beginning of the number of nodes change.  
 344 For each month, from January to December, the ANNs were built. MATLAB software was  
 345 used to implement the ANNs with the Levenberg-Marquardt algorithm for training. In each of  
 346 the ANNs, 85 % of the data was used for training-validation, and the rest for testing  
 347 (verification). The best model corresponding to each number of hidden nodes was identified,  
 348 i.e. ten models per month and the best model for each month. RMSE was used to identify the



best models. RMSE was calculated for (1) the training-validation dataset (RMSE\_cal), (2) the testing dataset (RMSE\_test), and (3) the entire period (RMSE). In all the cases, the final (best) model was chosen based on RMSE for the entire period. The iteration optimisation procedure, including the calculation of RMSE, was carried out for each of the 15 sets of input variables (Table 2) and for each month (Sect. 4.2).

### 3.5 Step 5. Models application and combination

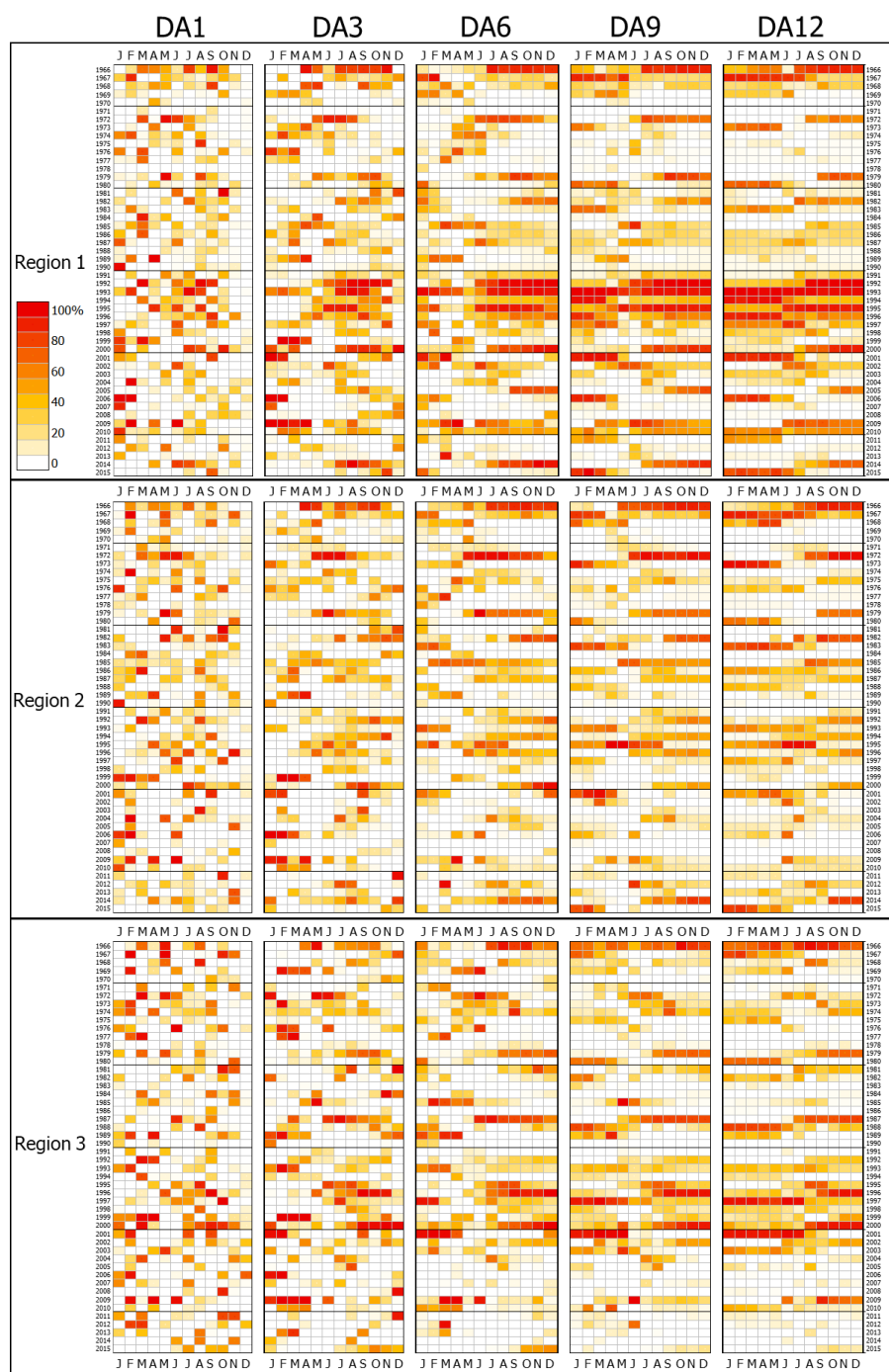
Once the best ML models, PR and ANN, were known, the pair of models were selected for each month. Depending on the performance of these models (and experience of their use), they can be used either separately or combined, e.g. being run in parallel so that a modeller could see the cases when models produce different results. An alternative is to use a dynamic weighting of the models' outputs (e.g. with the weights being proportional to the historical performance) to form a "model committee".

## 4 Results and discussion

### 4.1 Data preparation: drought areas and crop yield

Figure 3 shows the drought areas calculated for the three regions. In this heat map, columns indicate the months and rows point out the years. The redder the colour, the larger the drought area. In general, region 1 (Figure 3, the upper panel) presents the highest values concerning the other two regions. In general, the 1990s show higher values of areas with respect to the rest of the period, which agrees with Guha-Sapir (2019); in this decade, there were three droughts, 1993, 1996 and 2000. At the beginning of the period, large areas are also observed in the three regions; these results align with Bhalme and Mooley (1980).

In Figure 3, a pattern is observed in the drought areas distribution for all the aggregation periods, i.e. from DA1 to DA12. In DA1, the areas mainly concentrate in the first months; even the December column is almost white (without drought). Later, for DA3, the large areas are located from April to November. Successively, for DA6 and DA9, the largest areas are concentrated in the second half of the year. There are even droughts that end in the following year; they are the reddish lines that are observed in the first semester (first columns). Finally, in DA12, there are consecutive large areas indicated by the reddish lines; droughts usually begin in the second semester and extend until the following year. These results show the importance of considering more than one period of aggregation when using indicators based on meteorological variables; each aggregation period can be a proxy for analysing different types of drought and its effects.



**Figure 3** Drought areas (DAs) for each aggregation period (1, 3, 6, 9, and 12 months) and region. Top, middle, and bottom panels indicate region 1 (Bihar and Jharkhand), region 2 (West Bengal) and region 3 (Odisha).



Figure 4 shows the time series of de-trended CY and DA for the three regions. In the case of DA (indicated in red), the values are displayed in inverse order to facilitate interpretation. In general, when drought areas increase, this is expected to affect crop yield (decreasing). Otherwise, when the drought area decreases, this effect favours an increase in crop yield. In general, for the three regions, the decreases in CY coincide with the increases in DA. The general pattern regarding DA variations is as follows. The values fluctuate throughout the year for the aggregation periods of one and three months (DA1 and DA3). Subsequently, for DA6 to DA12, the values are concentrated in the second half of the year. These results also show the usefulness of the different aggregation periods to capture different types of drought. The effect of increasing DA seems not to be observed in decreasing CY for all cases of DAs. For example, in region 1 (Figure 4, the upper panel), the decrease in 2004, one of the maximums, does not coincide with increases in DA9 and DA12, but it does for DA1, DA3 and DA6. These results also support the use of the different aggregation periods on drought assessments.

#### 4.2 Input variable selection (correlation analysis)

Figure 5 summarises the correlation between the de-trended CY and the DAs, and Figure 6 presents the correlation for each monthly DA time series.

Figures 5 and 6 show that the correlation is different over the year in the three regions. In all cases, the correlation coefficient increases until a maximum and then decreases. The month in which the maximum value is reached is different for each region but falls within the crop season (i.e. June to November/December). For region 1, it is in July. For region 2, there are four months with this pattern, June, July, October, and November. Finally, for region 3, it is October, November, and December.

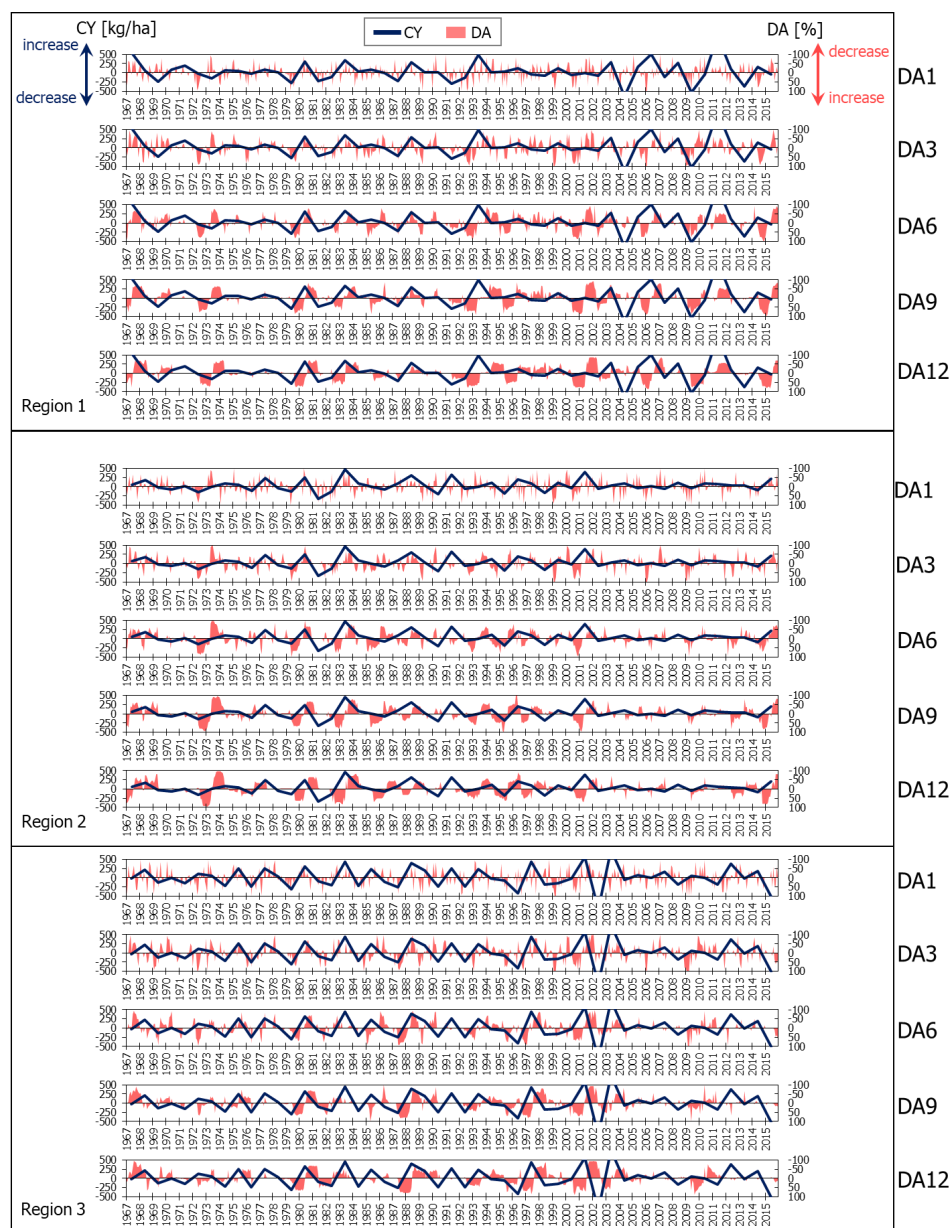
These results of correlation can be useful for monitoring agricultural drought. For example, in region 1, the drought areas calculated from SPEI6 (i.e. DA6) show a maximum correlation in July. This correlation value means that the previous six months' accumulated effect is crucial for the crop yield of the Kharif season, which covers more or less from June to November/December.

Figure 5 shows the following pattern. In general, for region 1, results similar to DA6 are observed for DA3, 9, and 12. For region 2, a similar pattern happens in the peaks, but in this case two, one corresponding to DA1 and 3, and the other to DA6, 9, and 12. The first peak of DA1 and DA3 may indicate that it is crucial to pay attention to the immediate period conditions of one to three months. In the case of the second peak, the medium and long-term conditions, 6 to 12 months, are more important to monitor for the harvest month. For region 3, the peak





occurs at the end of the growing season, in almost all cases. Hence, the condition before the  
 growing season is decisive for the crop yield.



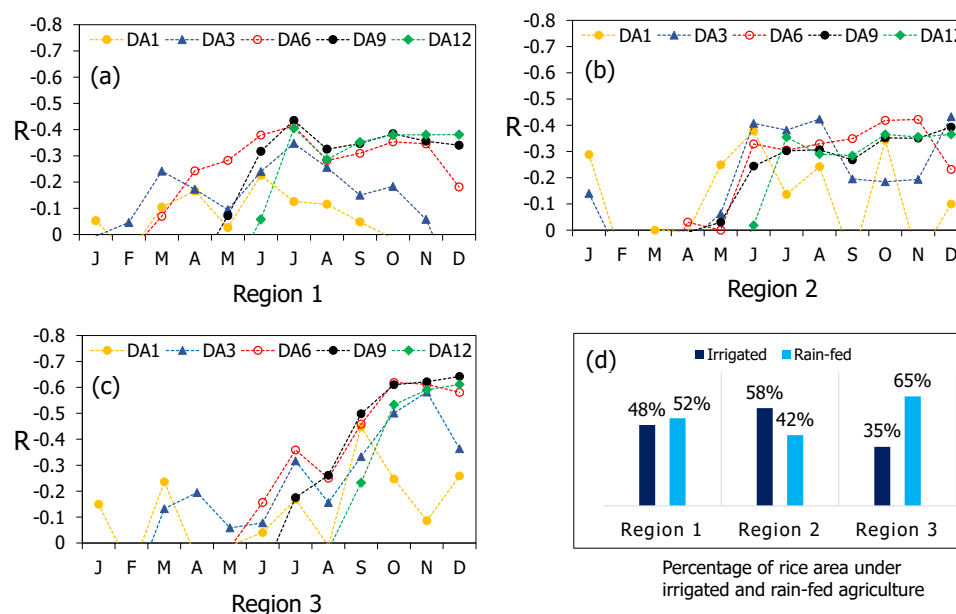
**Figure 4** Time series of the de-trended crop yield (CY) and drought areas (DAs) for each aggregation period (1, 3, 6, 9 and 12 months) and region. Top, middle, and bottom panels indicate region 1 (Bihar and Jharkhand), region 2 (West Bengal) and region 3 (Odisha).





Figure 6 shows how the correlation coefficients between CY and DA are positive outside the growing season and negative within that season. However, this pattern is less evident for DA1 and DA3. The pattern shown by the correlation coefficients in Figure 6 supports the idea that drought is an important factor in crop yield since the months with less drought are more correlated with the increase in CY, and the months with more drought do so with decrease in CY.

Figure 5 (d) shows the percentage of irrigated and rain-fed agriculture. For regions 1 and 2, about half is by irrigation, while in region 3, only 35%. Perhaps this percentage of irrigation for region 3 explains why the correlation coefficients for this region are higher than for the other two (Figure 5, and 6 (c)). Region 3 is more dependent on rain for agriculture; therefore, this condition is best captured when calculating drought with the precipitation, as in this case (Sect. 3.2).



**Figure 5** Summary of correlation between de-trended crop yield (CY) and drought areas (DAs) for each aggregation period (1, 3, 6, 9, and 12 months) and region: (a) region 1 (Bihar and Jharkhand), (b) region 2 (West Bengal) and (c) region 3 (Odisha). Negative R indicates the correlation between the increase in DA and the decrease in CY. Percentage of rice area under irrigated and rain-fed agriculture (d). Source of irrigated and rain-fed agriculture data: Directorate of Rice Development (DRD), (2014).



**Figure 6** Correlation (R) between de-trended crop yield (CY) and drought areas (DAs) for each aggregation period (1, 3, 6, 9, and 12 months) and region. DA is on the x-axis, and CY is on the y-axis. Results are shown for each monthly DA time series from June to December (J to D). Top, middle, and bottom panels indicate region 1 (Bihar and Jharkhand), region 2 (West Bengal), and region 3 (Odisha). Negative R indicates the correlation between increase in DA and decrease in CY.



Figure 5 (a, b, and c) shows the following pattern in the three regions. The correlation coefficients between CY and DAs increase according to the aggregation periods and the month of analysis. DA1 and DA3 have a better correlation in the first months of the year. DA6 has a better correlation in the subsequent months, between May and June. Finally, DA9 and 12 do so within the second half of the year.

Each respective DA time series reaches a maximum (or maximums) of correlation, and then correlation decreases. According to this pattern, the 15 combinations of input variables shown in Table 2 were selected. As earlier mentioned, the CY of the previous year was included in all combinations and is indicated as  $CY_{t-1}$ . Combinations 1 to 5 only include a DA time series. Combinations 6 to 9 are DA pairs that were calculated with the drought indicator of successive aggregation times. For example, combination 6 forms DA1 and 3, combination 7 includes DA3 and 6, and so on. Similarly, combinations 10 to 13 are proposed, but for triples. Combinations 13 and 14 are fourfold. Finally, the last combination (15th) is made up of all the DA series.

As mentioned, the models were built for each month (January to December) using the 15 combinations (Table 2) in each case. For example, for the case of January the monthly series of DAs extracted for January were used. These DAs are DA1\_1, DA3\_1, DA6\_1, DA9\_1, and DA12\_1. The suffix indicates the month. Then, the different DA1\_1 to DA12\_1 were used following the 15 combinations shown in Table 2 to build the ML models (ANN and PR) for January. Similarly, it was carried out from February to December.

**Table 2** Input sets (combinations) to build the ML models. CY and DA stand for crop yield and drought area. DAs are calculated with the drought indicator for the aggregate period of 1, 3, 6, 9, and 12 months (details in Sect. 4.2).

Input set (combination)	Input variables
1	$CY_{t-1}$ , DA1
2	$CY_{t-1}$ , DA3
3	$CY_{t-1}$ , DA6
4	$CY_{t-1}$ , DA9
5	$CY_{t-1}$ , DA12
6	$CY_{t-1}$ , DA1,3
7	$CY_{t-1}$ , DA3,6
8	$CY_{t-1}$ , DA6,9
9	$CY_{t-1}$ , DA9,12
10	$CY_{t-1}$ , DA1,3,6
11	$CY_{t-1}$ , DA3,6,9
12	$CY_{t-1}$ , DA6,9,12
13	$CY_{t-1}$ , DA1,3,6,9
14	$CY_{t-1}$ , DA3,6,9,12
15	$CY_{t-1}$ , DA1,3,6,9,12

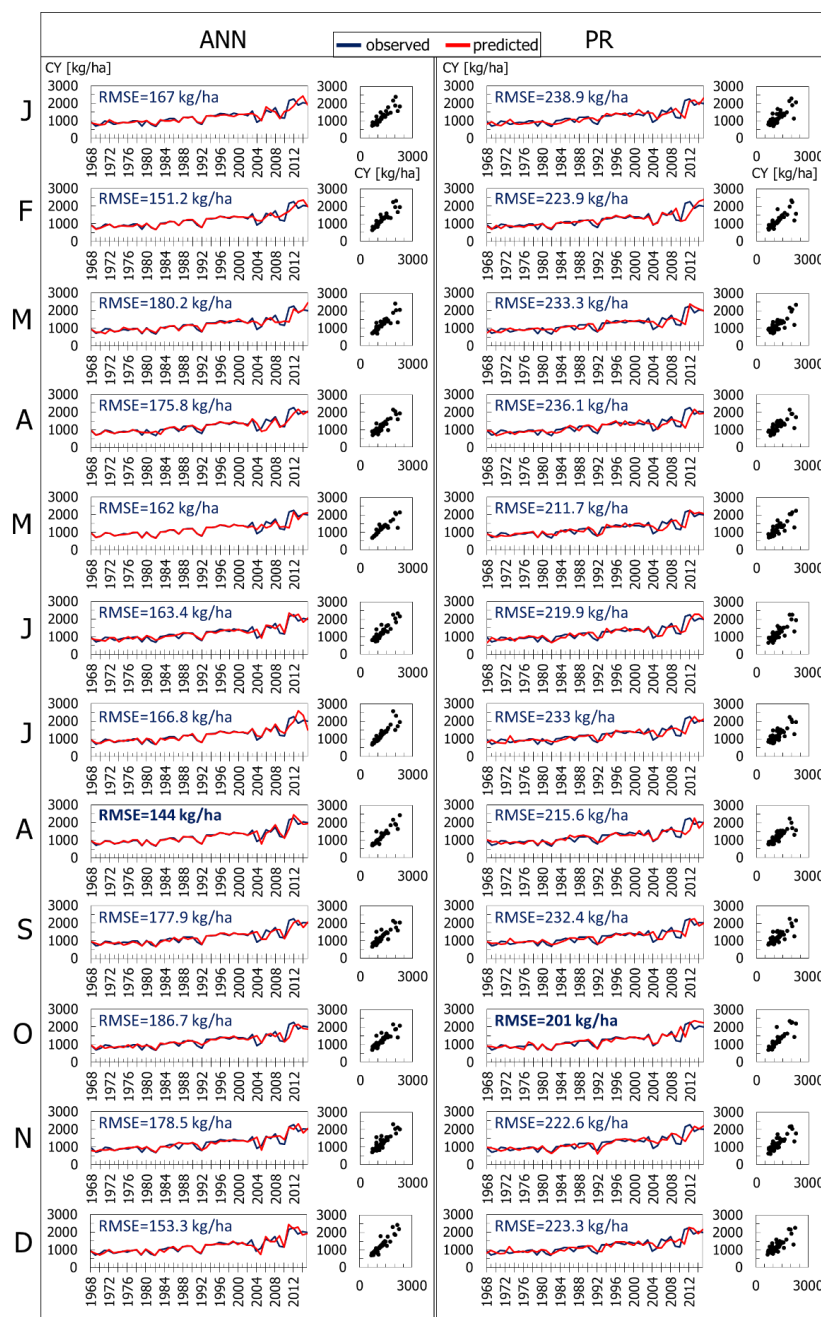


#### 4.3 ANN and PR models

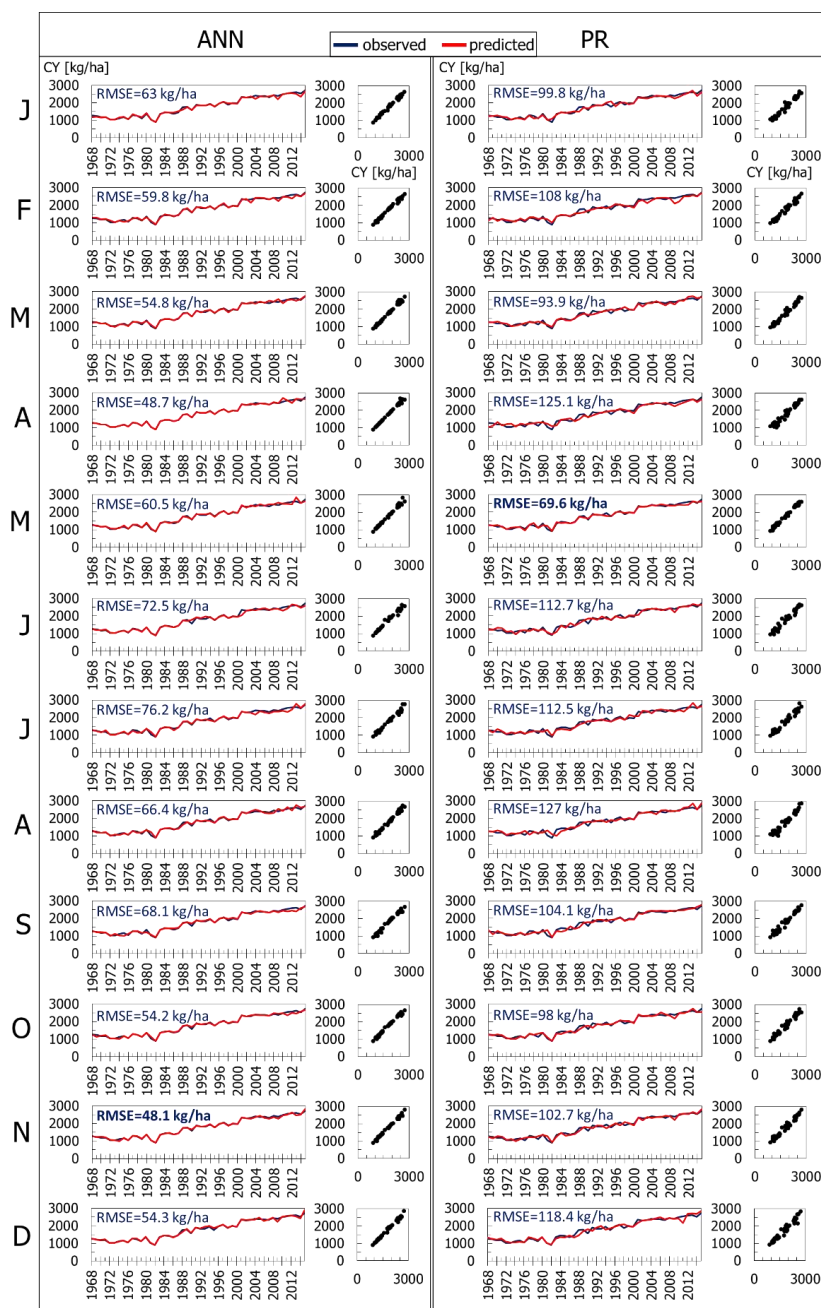
The results show different magnitudes of error between the observed and predicted CY. The models with the lowest error are presented in Figures 7, 8 and 9, for each of the three regions. The pair of ANN and PR that best predicts CY is shown for each month. The RMSE is also indicated in each case. On the other hand, Figure 10 shows the error for each input set (combination); the lowest error achieved in each month is presented in each case both for each ANN and PR.

In general, ANN shows the least errors, as expected (Figure 10). However, the results of PR are not much worse compared to those of ANN; for example, in some cases, the errors shown by linear PR are very close to those of ANN (e.g. Figure 10, region 2). In general, it is observed that the models with the lowest errors correspond to region 2, followed by region 3 and region 1 (Figure 10). It is attributed to the different degrees of crop irrigation with surface and mostly groundwater, which determines the accuracy of the modelling in the different regions. Another factor contributing to the models' performance is the drastic changes in the CY data, where regions 1 and 3 are the ones that presented the most, and to a much lesser extent, region 2.

Figure 10 shows that in the three regions, different types of PR showed better results. In general, linear and pure-quadratic indicate more stable results (no sudden changes among the different realisations) but not better than quadratic and interactions. In general quadratic and interactions present better results, being in some cases very close to those shown by ANN, e.g. PR interactions (Figure 10, region 1).



**Figure 7** ANN and PR models for predicting seasonal crop yield (CY) built for each time series of monthly drought areas (DAs): region 1 (Bihar and Jharkhand). The model with the lowest error (RMSE) is presented for each month, from January to December (J to D).

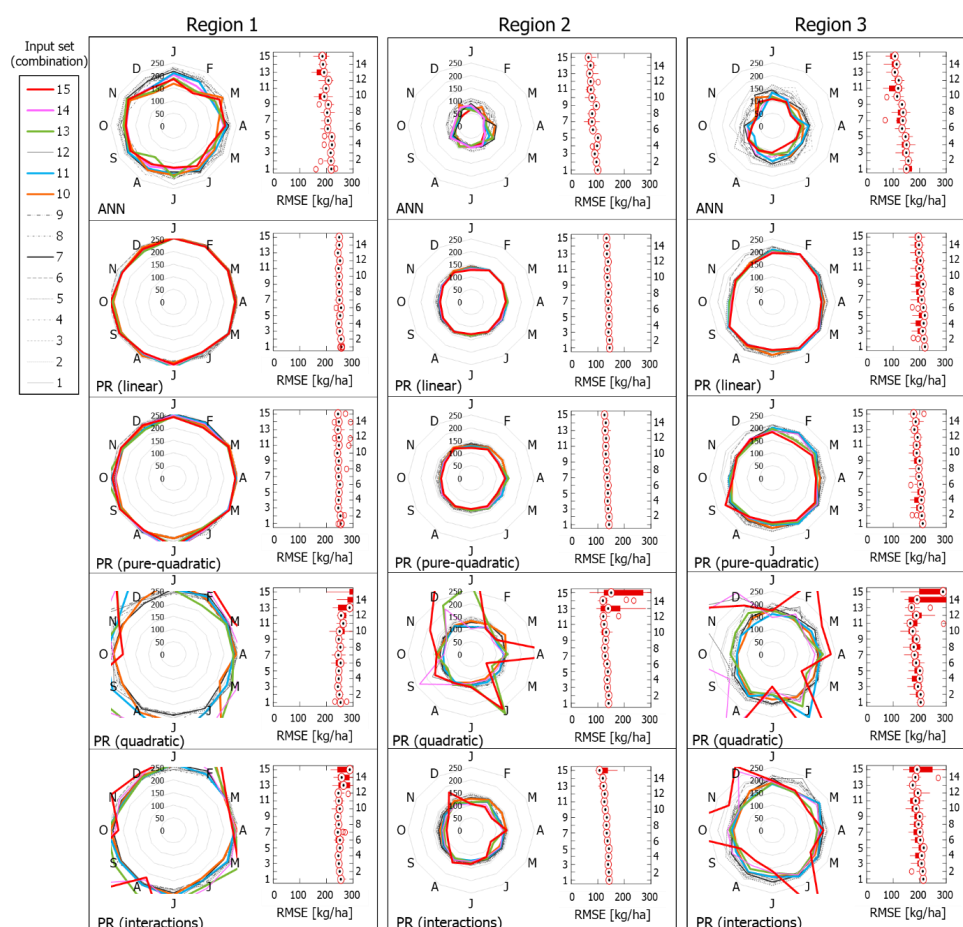


498  
 499 **Figure 8** ANN and PR models for predicting seasonal crop yield (CY) built for each time series of monthly  
 500 drought areas (DAs): region 2 (West Bengal). The model with the lowest error (RMSE) is presented for each  
 501 month, from January to December (J to D).





**Figure 9** ANN and PR models for predicting seasonal crop yield (CY) built for each time series of monthly drought areas (DAs): region 3 (Odisha). The model with the lowest error (RMSE) is presented for each month, from January to December (J to D).



**Figure 10** Root mean square error (RMSE) [kg/ha] for each of the 15 input sets (combinations) of the ANN and PR models built for each region. For each set of input (from one to 15), the lowest errors are presented for each month (January to December). Results of each input set are shown with lines to facilitate the analysis. Left, middle, and right panels indicate region 1 (Bihar and Jharkhand), region 2 (West Bengal) and region 3 (Odisha).

#### 4.4 Models application and combination

The best performing models were selected for each month. Table 3 shows the summary of these models, which includes the input set (combination), number of nodes, and errors for ANN, and input set, type, and errors for PR. The number of nodes indicates the degree of non-linearity presented in each model. In this way, the more nodes, the more complex the model is in the case of ANN. On the other hand, quadratic and interactions are the types that showed the best performance in PR models. In all cases, within the combinations of input variables, a single DA time series corresponding to one of the various aggregation periods (D1, D3, D6, D9 or D12) that by itself produced good results was not found. The input sets are made up of two and





up to six different DAs corresponding to the various aggregation periods. Thus, using more than one aggregation period of drought indicator results in better model performance. Tables 4, 5 and 6 are derived from Table 3. These three tables show the PR formulas for region 1, 2 and 3, respectively. In each table, the PR formula and the inputs are indicated. These formulas are also intended to be a stand-alone tool in the CY prediction for each region. The application of PR models begins by selecting the formula of the PR model (Table 4, 5, or 6). For example, in the case of region 1, if the drought indicator data is available up to March (including it), the formula for March is chosen from Table 4. After, DAs are calculated (Sect. 3.1.2), and the time series of DAs are updated. According to Table 4, the DA1 and DA3 are required in this example. Then, from these time series of DAs, values of March are extracted, i.e. DA1\_3 and DA3\_3 (see Sect. 3.2 and 4.2). Then, the de-trending procedure is applied to each time series (Sect. 3.1.3). After, the CY is calculated. Finally, the reverse de-trending procedure is carried out to have the predicted CY in the same order of magnitude as the original CY data (Sect. 3.1.3). At the same time, or when it can be computed, the ANN model of the month under analysis is applied.

**Table 3** Summary of the ANN and PR models for predicting crop yield (CY) built for each month and region: (1) Bihar and Jharkhand, (2) West Bengal, and (3) Odisha. The table shows the models built with the lowest error (RMSE). DA stands for drought area.

Region	Month	ANN			PR			
		Input set (combination)	No. nodes	RMSE [kg/ha]	Month	Input set (combination)	Type	RMSE [kg/ha]
Region 1	Jan	10 CY <sub>t-1</sub> , DA1,3,6	4	167.0	Jan	8 CY <sub>t-1</sub> , DA6,9	quadratic	238.9
	Feb	15 CY <sub>t-1</sub> , DA1,3,6,9,12	6	151.2	Feb	13 CY <sub>t-1</sub> , DA1,3,6,9	quadratic	223.9
	Mar	11 CY <sub>t-1</sub> , DA3,6,9	7	180.2	Mar	6 CY <sub>t-1</sub> , DA1,3	quadratic	233.3
	Apr	10 CY <sub>t-1</sub> , DA1,3,6	9	175.8	Apr	15 CY <sub>t-1</sub> , DA1,3,6,9,12	interactions	236.1
	May	15 CY <sub>t-1</sub> , DA1,3,6,9,12	5	162.0	May	10 CY <sub>t-1</sub> , DA1,3,6	quadratic	211.7
	Jun	13 CY <sub>t-1</sub> , DA1,3,6,9	2	163.4	Jun	10 CY <sub>t-1</sub> , DA1,3,6	interactions	219.9
	Jul	15 CY <sub>t-1</sub> , DA1,3,6,9,12	10	166.8	Jul	6 CY <sub>t-1</sub> , DA1,3	quadratic	233.0
	Aug	13 CY <sub>t-1</sub> , DA1,3,6,9	5	144.0	Aug	15 CY <sub>t-1</sub> , DA1,3,6,9,12	interactions	215.6
	Sep	6 CY <sub>t-1</sub> , DA1,3	5	177.9	Sep	7 CY <sub>t-1</sub> , DA3,6	quadratic	232.4
	Oct	14 CY <sub>t-1</sub> , DA3,6,9,12	6	186.7	Oct	15 CY <sub>t-1</sub> , DA1,3,6,9,12	quadratic	201.0
	Nov	8 CY <sub>t-1</sub> , DA6,9	4	178.5	Nov	13 CY <sub>t-1</sub> , DA1,3,6,9	interactions	222.6
	Dec	10 CY <sub>t-1</sub> , DA1,3,6	4	153.3	Dec	13 CY <sub>t-1</sub> , DA1,3,6,9	pure-quadratic	223.3
Region 2	Jan	13 CY <sub>t-1</sub> , DA1,3,6,9	8	63.0	Jan	14 CY <sub>t-1</sub> , DA3,6,9,12	quadratic	99.8
	Feb	11 CY <sub>t-1</sub> , DA3,6,9	10	59.8	Feb	15 CY <sub>t-1</sub> , DA1,3,6,9,12	interactions	108.0
	Mar	7 CY <sub>t-1</sub> , DA3,6	8	54.8	Mar	15 CY <sub>t-1</sub> , DA1,3,6,9,12	interactions	93.9
	Apr	14 CY <sub>t-1</sub> , DA3,6,9,12	7	48.7	Apr	14 CY <sub>t-1</sub> , DA3,6,9,12	interactions	125.1
	May	15 CY <sub>t-1</sub> , DA1,3,6,9,12	10	60.5	May	15 CY <sub>t-1</sub> , DA1,3,6,9,12	quadratic	69.6
	Jun	13 CY <sub>t-1</sub> , DA1,3,6,9	7	72.5	Jun	10 CY <sub>t-1</sub> , DA1,3,6	quadratic	112.7
	Jul	6 CY <sub>t-1</sub> , DA1,3	6	76.2	Jul	10 CY <sub>t-1</sub> , DA1,3,6	quadratic	112.5
	Aug	6 CY <sub>t-1</sub> , DA1,3	9	66.4	Aug	13 CY <sub>t-1</sub> , DA1,3,6,9	interactions	127.0
	Sep	6 CY <sub>t-1</sub> , DA1,3	10	68.1	Sep	15 CY <sub>t-1</sub> , DA1,3,6,9,12	interactions	104.1
	Oct	7 CY <sub>t-1</sub> , DA3,6	10	54.2	Oct	15 CY <sub>t-1</sub> , DA1,3,6,9,12	interactions	98.0
	Nov	7 CY <sub>t-1</sub> , DA3,6	10	48.1	Nov	15 CY <sub>t-1</sub> , DA1,3,6,9,12	interactions	102.7
	Dec	15 CY <sub>t-1</sub> , DA1,3,6,9,12	8	54.3	Dec	14 CY <sub>t-1</sub> , DA3,6,9,12	interactions	118.4
Region 3	Jan	15 CY <sub>t-1</sub> , DA1,3,6,9,12	7	106.5	Jan	14 CY <sub>t-1</sub> , DA3,6,9,12	quadratic	145.7
	Feb	13 CY <sub>t-1</sub> , DA1,3,6,9	10	105.7	Feb	10 CY <sub>t-1</sub> , DA1,3,6	quadratic	160.5
	Mar	15 CY <sub>t-1</sub> , DA1,3,6,9,12	9	84.1	Mar	12 CY <sub>t-1</sub> , DA6,9,12	quadratic	143.5
	Apr	15 CY <sub>t-1</sub> , DA1,3,6,9,12	4	112.3	Apr	14 CY <sub>t-1</sub> , DA3,6,9,12	quadratic	169.6
	May	12 CY <sub>t-1</sub> , DA6,9,12	10	100.3	May	15 CY <sub>t-1</sub> , DA1,3,6,9,12	quadratic	133.4
	Jun	15 CY <sub>t-1</sub> , DA1,3,6,9,12	9	94.5	Jun	12 CY <sub>t-1</sub> , DA6,9,12	quadratic	189.4
	Jul	15 CY <sub>t-1</sub> , DA1,3,6,9,12	7	106.0	Jul	15 CY <sub>t-1</sub> , DA1,3,6,9,12	quadratic	128.2
	Aug	12 CY <sub>t-1</sub> , DA6,9,12	7	103.9	Aug	15 CY <sub>t-1</sub> , DA1,3,6,9,12	interactions	137.7
	Sep	11 CY <sub>t-1</sub> , DA3,6,9	9	84.1	Sep	13 CY <sub>t-1</sub> , DA1,3,6,9	quadratic	145.0
	Oct	15 CY <sub>t-1</sub> , DA1,3,6,9,12	10	79.7	Oct	10 CY <sub>t-1</sub> , DA1,3,6	quadratic	139.0
	Nov	11 CY <sub>t-1</sub> , DA3,6,9	10	62.6	Nov	10 CY <sub>t-1</sub> , DA1,3,6	quadratic	127.5
	Dec	11 CY <sub>t-1</sub> , DA3,6,9	9	74.7	Dec	8 CY <sub>t-1</sub> , DA6,9	quadratic	137.3



**Table 4** PR models for predicting crop yield (CY) built for each month: region 1 (Bihar and Jharkhand). For each moth, it is indicated the input (x1 to x6) and the PR formula. DA stands for drought area.

Month	Input						PR model
	x <sub>1</sub>	x <sub>2</sub>	x <sub>3</sub>	x <sub>4</sub>	x <sub>5</sub>	x <sub>6</sub>	
Jan	CY <sub>t-1</sub>	DA6	DA9				$-60.7111 - 0.1944x_1 - 0.2201x_2 + 1.2033x_3 - 0.0023x_1x_2 + 0.0043x_1x_3 - 0.0372x_2x_3 + 0.0003x_1^2 + 0.0504x_2^2 + 0.0308x_3^2$
Feb	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9		$-27.4716 - 0.4688x_1 + 1.8718x_2 - 1.3313x_3 - 0.2611x_4 + 1.3878x_5 - 0.0137x_1x_2 + 0.0135x_1x_3 + 0.0032x_1x_4 + 0.0064x_1x_5 + 0.0823x_2x_3 + 0.0574x_2x_4 + 0.0935x_2x_5 - 0.0544x_3x_4 - 0.0746x_3x_5 - 0.0241x_4x_5 + 0.0014x_1^2 - 0.0496x_2^2 - 0.0202x_3^2 - 0.0016x_4^2 + 0.0227x_5^2$
Mar	CY <sub>t-1</sub>	DA1	DA3				$28.1213 - 0.5204x_1 - 0.4908x_2 + 0.0545x_3 + 0.0051x_1x_2 - 0.0093x_1x_3 + 0.0033x_2x_3 + 0.0003x_1^2 - 0.0107x_2^2 + 0.0086x_3^2$
Apr	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$-24.3419 - 0.4785x_1 - 0.1965x_2 - 0.1356x_3 + 0.0848x_4 - 0.4774x_5 + 0.8029x_6 + 0.0066x_1x_2 + 0.0031x_1x_3 - 0.0128x_1x_4 + 0.0081x_1x_5 - 0.0003x_1x_6 + 0.0067x_2x_3 - 0.0604x_2x_4 + 0.1495x_2x_5 - 0.0169x_2x_6 + 0.0248x_3x_4 - 0.1295x_3x_5 - 0.0306x_3x_6 + 0.0458x_4x_5 + 0.0516x_4x_6 + 0.0595x_5x_6$
May	CY <sub>t-1</sub>	DA1	DA3	DA6			$113.2521 - 0.5132x_1 + 1.0101x_2 - 1.4019x_3 - 1.1130x_4 + 0.0100x_1x_2 + 0.0150x_1x_3 - 0.0027x_1x_4 + 0.0250x_2x_3 - 0.0655x_2x_4 + 0.0596x_3x_4 - 0.0006x_1^2 - 0.0358x_2^2 - 0.0380x_3^2 - 0.0495x_4^2$
Jun	CY <sub>t-1</sub>	DA1	DA3	DA6			$54.3 - 0.3715x_1 + 1.4832x_2 + 0.1432x_3 - 3.0648x_4 - 0.0106x_1x_2 + 0.0256x_1x_3 - 0.0111x_1x_4 - 0.0556x_2x_3 + 0.0648x_2x_4 - 0.0172x_3x_4$
Jul	CY <sub>t-1</sub>	DA1	DA3				$18.7237 - 0.3166x_1 + 1.3310x_2 - 3.0099x_3 - 0.0030x_1x_2 + 0.0024x_1x_3 + 0.0054x_2x_3 + 0.0001x_1^2 + 0.0065x_2^2 - 0.0065x_3^2$
Aug	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$59.2373 - 0.6972x_1 + 0.1791x_2 + 5.1900x_3 - 1.3783x_4 - 6.9753x_5 + 1.5471x_6 - 0.0142x_1x_2 + 0.0072x_1x_3 + 0.1163x_1x_4 - 0.1285x_1x_5 + 0.0294x_1x_6 - 0.3670x_2x_3 + 0.0897x_2x_4 + 0.2332x_2x_5 + 0.0922x_2x_6 + 0.3014x_3x_4 + 0.3444x_3x_5 - 0.4160x_3x_6 - 0.5819x_4x_5 - 0.0450x_4x_6 + 0.3299x_5x_6$
Sep	CY <sub>t-1</sub>	DA3	DA6				$44.8563 - 0.4565x_1 + 0.6884x_2 - 1.9466x_3 + 0.0053x_1x_2 - 0.0005x_1x_3 + 0.0012x_2x_3 + 0.0004x_1^2 - 0.0172x_2^2 - 0.0002x_3^2$
Oct	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$76.1546 + 0.0046x_1 - 2.2220x_2 + 1.0816x_3 + 19.1690x_4 - 53.2338x_5 + 29.1398x_6 + 0.0048x_1x_2 + 0.0155x_1x_3 - 0.0383x_1x_4 - 0.0868x_1x_5 + 0.1254x_1x_6 - 0.0444x_2x_3 + 0.0448x_2x_4 + 0.0175x_2x_5 - 0.0552x_2x_6 + 0.2154x_3x_4 - 1.0260x_3x_5 + 0.7776x_3x_6 + 3.2060x_4x_5 - 3.3267x_4x_6 + 11.6655x_5x_6 + 0.0002x_1^2 - 0.0547x_2^2 + 0.1171x_3^2 + 0.2874x_4^2 - 7.7995x_5^2 - 4.0845x_6^2$
Nov	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9		$30.0286 - 0.4536x_1 - 0.6721x_2 - 0.8270x_3 - 7.0981x_4 + 5.3007x_5 - 0.0339x_1x_2 + 0.0086x_1x_3 + 0.0107x_1x_4 - 0.0084x_1x_5 + 0.1347x_2x_3 + 0.1123x_2x_4 - 0.0596x_2x_5 + 0.2355x_3x_4 - 0.2262x_3x_5 - 0.0117x_4x_5$
Dec	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9		$29.2005 - 0.3816x_1 - 0.6953x_2 + 0.8469x_3 + 1.2024x_4 - 3.2563x_5 + 0.0005x_1^2 - 0.5339x_2^2 - 0.0047x_3^2 - 0.0119x_4^2 + 0.0083x_5^2$



**Table 5** PR models for predicting crop yield (CY) built for each month: region 2 (West Bengal). For each moth, it is indicated the input (x1 to x6) and the PR formula. DA stands for drought area.

Month	Input						PR model
	X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>5</sub>	X <sub>6</sub>	
Jan	CY <sub>t-1</sub>	DA3	DA6	DA9	DA12		$8.5606 - 0.2404x_1 - 1.1236x_2 - 0.7606x_3 + 6.6535x_4 - 5.3772x_5 + 0.0087x_1x_2 - 0.0044x_1x_3 - 0.0182x_1x_4 + 0.0234x_1x_5 + 0.0080x_2x_3 + 0.0234x_2x_4 - 0.0037x_2x_5 - 0.0402x_3x_4 + 0.1648x_3x_5 + 0.0200x_4x_5 + 0.0001x_1^2 - 0.0145x_2^2 - 0.0657x_3^2 + 0.0544x_4^2 - 0.0952x_5^2$
Feb	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$-24.8742 - 0.5460x_1 - 0.1190x_2 + 0.2175x_3 + 0.7776x_4 - 8.6335x_5 + 6.4022x_6 - 0.0164x_1x_2 + 0.0095x_1x_3 - 0.0251x_1x_4 + 0.0262x_1x_5 - 0.0057x_1x_6 - 0.0179x_2x_3 - 0.0241x_2x_4 - 0.1705x_2x_5 + 0.1579x_2x_6 + 0.0064x_3x_4 + 0.2383x_3x_5 - 0.2779x_3x_6 - 0.0117x_4x_5 + 0.0266x_4x_6 + 0.0614x_5x_6$
Mar	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$35.6904 - 0.3835x_1 - 0.9286x_2 + 0.1960x_3 - 0.3445x_4 - 0.3559x_5 + 0.6370x_6 - 0.0025x_1x_2 - 0.0009x_1x_3 + 0.0111x_1x_4 - 0.0252x_1x_5 + 0.0144x_1x_6 - 0.0059x_2x_3 + 0.0426x_2x_4 + 0.0063x_2x_5 + 0.0012x_2x_6 - 0.0362x_3x_4 - 0.1287x_3x_5 - 0.0038x_3x_6 + 0.0242x_4x_5 - 0.0355x_4x_6 + 0.0394x_5x_6$
Apr	CY <sub>t-1</sub>	DA3	DA6	DA9	DA12		$8.5856 - 0.1865x_1 + 1.5824x_2 - 1.0816x_3 - 1.0256x_4 + 1.7846x_5 - 0.0164x_1x_2 + 0.0242x_1x_3 - 0.0013x_1x_4 + 0.0009x_1x_5 - 0.0084x_2x_3 + 0.0073x_2x_4 - 0.0710x_2x_5 - 0.0430x_3x_4 + 0.0659x_3x_5 + 0.0317x_4x_5$
May	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$-25.0101 - 0.8233x_1 - 1.8073x_2 + 1.1145x_3 + 1.6217x_4 + 0.9651x_5 + 0.5729x_6 + 0.0254x_1x_2 - 0.1198x_1x_3 + 0.0959x_1x_4 - 0.0112x_1x_5 + 0.0311x_1x_6 - 0.2178x_2x_3 + 0.3465x_2x_4 - 0.3214x_2x_5 + 0.0602x_2x_6 - 0.9192x_3x_4 + 1.2301x_3x_5 - 0.2167x_3x_6 - 0.8955x_4x_5 + 0.1015x_4x_6 + 0.0662x_5x_6 + 0.0048x_1^2 - 0.0096x_2^2 + 0.3527x_3^2 + 0.4308x_4^2 - 0.0492x_5^2 + 0.0639x_6^2$
Jun	CY <sub>t-1</sub>	DA1	DA3	DA6			$90.7623 - 0.5785x_1 + 0.1582x_2 - 2.7914x_3 + 0.8655x_4 - 0.0176x_1x_2 + 0.0093x_1x_3 - 0.0108x_1x_4 + 0.0533x_2x_3 - 0.0521x_2x_4 + 0.1589x_3x_4 + 0.0012x_1^2 + 0.0072x_2^2 - 0.0974x_3^2 - 0.0714x_4^2$
Jul	CY <sub>t-1</sub>	DA1	DA3	DA6			$26.1164 - 0.6892x_1 - 0.6723x_2 - 5.5280x_3 + 4.6922x_4 + 0.0070x_1x_2 + 0.0111x_1x_3 - 0.0148x_1x_4 - 0.1301x_2x_3 + 0.0838x_2x_4 + 0.5157x_3x_4 + 0.0014x_1^2 + 0.0679x_2^2 - 0.1671x_3^2 - 0.3540x_4^2$
Aug	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9		$55.6167 - 0.2284x_1 - 0.0182x_2 - 1.7996x_3 - 4.0674x_4 + 3.7965x_5 + 0.0117x_1x_2 - 0.0259x_1x_3 + 0.0556x_1x_4 - 0.0484x_1x_5 - 0.0176x_2x_3 - 0.1459x_2x_4 + 0.1017x_2x_5 - 0.0487x_3x_4 + 0.2346x_3x_5 - 0.1273x_4x_5$
Sep	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$35.6058 - 0.3263x_1 + 1.9755x_2 - 0.4197x_3 - 3.5963x_4 + 2.7383x_5 - 1.2234x_6 + 0.0013x_1x_2 - 0.0057x_1x_3 - 0.0470x_1x_4 + 0.0042x_1x_5 + 0.0475x_1x_6 + 0.0033x_2x_3 - 0.1889x_2x_4 + 0.0749x_2x_5 + 0.1060x_2x_6 + 0.0179x_3x_4 - 0.0003x_3x_5 + 0.0412x_3x_6 + 0.0291x_4x_5 - 0.0312x_4x_6 - 0.0379x_5x_6$
Oct	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$7.7675 - 0.1875x_1 - 0.1476x_2 - 0.8333x_3 - 5.1327x_4 + 15.3857x_5 - 10.6323x_6 - 0.0012x_1x_2 - 0.0011x_1x_3 + 0.0588x_1x_4 + 0.0365x_1x_5 - 0.0886x_1x_6 - 0.1339x_2x_3 + 0.1763x_2x_4 - 0.5955x_2x_5 + 0.4854x_2x_6 - 0.4231x_3x_4 - 0.2159x_3x_5 + 0.6868x_3x_6 + 0.3521x_4x_5 + 0.0666x_4x_6 - 0.4145x_5x_6$
Nov	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$38.3601 - 0.2443x_1 + 1.7236x_2 - 0.6584x_3 - 6.7484x_4 + 13.3609x_5 - 9.4895x_6 + 0.0114x_1x_2 + 0.0162x_1x_3 + 0.0331x_1x_4 - 0.0817x_1x_5 + 0.0478x_1x_6 + 0.0370x_2x_3 - 0.1350x_2x_4 - 0.0212x_2x_5 + 0.1631x_2x_6 - 0.1562x_3x_4 - 0.0082x_3x_5 + 0.1229x_3x_6 + 0.2672x_4x_5 - 0.0938x_4x_6 - 0.1335x_5x_6$
Dec	CY <sub>t-1</sub>	DA3	DA6	DA9	DA12		$24.769 - 0.1091x_1 - 2.9747x_2 + 2.9990x_3 - 5.4144x_4 + 3.3374x_5 + 0.0083x_1x_2 - 0.0069x_1x_3 + 0.0596x_1x_4 - 0.0630x_1x_5 + 0.0755x_2x_3 + 0.0127x_2x_4 + 0.0094x_2x_5 - 0.0052x_3x_4 - 0.0884x_3x_5 + 0.0361x_4x_5$



**Table 6** PR models for predicting crop yield (CY) built for each month: region 3 (Odisha). For each moth, it is indicated the input (x1 to x6) and the PR formula. DA stands for drought area.

Month	Input						PR model
	X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	X <sub>4</sub>	X <sub>5</sub>	X <sub>6</sub>	
Jan	CY <sub>t-1</sub>	DA3	DA6	DA9	DA12		$-149.3429 - 0.4867x_1 - 1.5749x_2 + 2.0827x_3 + 5.9761x_4 - 6.0586x_5 - 0.0022x_1x_2$ $+ 0.0100x_1x_3 + 0.0200x_1x_4 + 0.0045x_1x_5 - 0.0142x_2x_3 - 0.2414x_2x_4 + 0.1392x_2x_5$ $- 0.1332x_3x_4 + 0.1123x_3x_5 + 0.2083x_4x_5 + 0.0022x_1^2 + 0.0262x_2^2 + 0.0771x_3^2 + 0.0431x_4^2$ $- 0.1405x_5^2$
Feb	CY <sub>t-1</sub>	DA1	DA3	DA6			$-90.6767 - 0.6674x_1 + 0.1283x_2 + 0.2580x_3 + 0.4540x_4 - 0.0041x_1x_2 + 0.0141x_1x_3$ $- 0.0009x_1x_4 + 0.0055x_2x_3 - 0.0195x_2x_4 + 0.0771x_3x_4 + 0.0006x_1^2 + 0.0313x_2^2 - 0.0207x_3^2$ $+ 0.0129x_4^2$
Mar	CY <sub>t-1</sub>	DA6	DA9	DA12			$-168.6741 - 0.7249x_1 + 0.2079x_2 - 2.2594x_3 + 2.2421x_4 + 0.0074x_1x_2 - 0.0102x_1x_3$ $+ 0.0347x_1x_4 - 0.0159x_2x_3 + 0.0009x_2x_4 + 0.1147x_3x_4 + 0.0025x_1^2 + 0.0454x_2^2 - 0.0197x_3^2$ $+ 0.0318x_4^2$
Apr	CY <sub>t-1</sub>	DA3	DA6	DA9	DA12		$-116.7973 - 0.6789x_1 - 0.4066x_2 - 0.5459x_3 + 3.4428x_4 - 3.2126x_5 + 0.0008x_1x_2$ $- 0.0110x_1x_3 + 0.0063x_1x_4 + 0.0337x_1x_5 + 0.0647x_2x_3 - 0.1280x_2x_4 + 0.0847x_2x_5$ $- 0.0041x_3x_4 - 0.1576x_3x_5 - 0.0357x_4x_5 + 0.0025x_1^2 - 0.0386x_2^2 + 0.0180x_3^2 + 0.0968x_4^2$ $+ 0.1431x_5^2$
May	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$-56.0895 - 0.8435x_1 - 1.5688x_2 + 5.5848x_3 - 5.6556x_4 - 0.0876x_5 - 0.4449x_6 + 0.0396x_1x_2$ $- 0.0552x_1x_3 + 0.0130x_1x_4 + 0.0414x_1x_5 - 0.0155x_1x_6 + 0.0691x_2x_3 - 0.1386x_2x_4$ $+ 0.4106x_2x_5 + 0.0874x_2x_6 + 0.2997x_3x_4 - 0.2552x_3x_5 - 0.4282x_3x_6 - 0.0482x_4x_5$ $+ 0.2264x_4x_6 - 0.2702x_5x_6 + 0.0040x_1^2 - 0.0721x_2^2 - 0.0198x_3^2 - 0.2076x_4^2 + 0.2160x_5^2$ $- 0.0223x_6^2$
Jun	CY <sub>t-1</sub>	DA6	DA9	DA12			$-23.8562 - 0.3639x_1 - 1.8924x_2 - 0.0052x_3 + 1.3074x_4 - 0.0060x_1x_2 - 0.0057x_1x_3$ $+ 0.0205x_1x_4 - 0.0135x_2x_3 - 0.0965x_2x_4 + 0.1034x_3x_4 + 0.0004x_1^2 + 0.0110x_2^2 - 0.0171x_3^2$ $+ 0.0913x_4^2$
Jul	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$-18.8884 - 0.7725x_1 + 2.8997x_2 - 1.9129x_3 - 0.9194x_4 - 0.5636x_5 - 0.6886x_6 - 0.0070x_1x_2$ $+ 0.0320x_1x_3 - 0.0220x_1x_4 - 0.0221x_1x_5 - 0.0042x_1x_6 + 0.3776x_2x_3 - 0.0748x_2x_4$ $- 0.1803x_2x_5 - 0.2590x_2x_6 - 0.5984x_3x_4 + 0.6811x_3x_5 - 0.0178x_3x_6 + 0.8957x_4x_5$ $+ 0.0173x_4x_6 - 0.1524x_5x_6 + 0.0012x_1^2 - 0.1151x_2^2 - 0.1006x_3^2 - 0.0306x_4^2 - 0.7603x_5^2$ $+ 0.1200x_6^2$
Aug	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9	DA12	$4.8997 - 0.7900x_1 - 0.9225x_2 + 3.8372x_3 - 0.0832x_4 - 9.7835x_5 + 4.0199x_6 - 0.0065x_1x_2$ $+ 0.0352x_1x_3 + 0.0005x_1x_4 - 0.0461x_1x_5 - 0.0019x_1x_6 - 0.0759x_2x_3 - 0.1196x_2x_4$ $+ 0.1775x_2x_5 + 0.0748x_2x_6 + 0.0694x_3x_4 + 0.2503x_3x_5 - 0.3715x_3x_6 - 0.2022x_4x_5$ $+ 0.4167x_4x_6 - 0.2192x_5x_6$
Sep	CY <sub>t-1</sub>	DA1	DA3	DA6	DA9		$41.4745 - 0.5431x_1 - 0.0366x_2 - 0.9681x_3 + 3.6023x_4 - 4.3272x_5 - 0.0002x_1x_2$ $+ 0.0115x_1x_3 - 0.0191x_1x_4 + 0.0139x_1x_5 - 0.0809x_2x_3 + 0.0508x_2x_4 + 0.0205x_2x_5$ $+ 0.4602x_3x_4 - 0.5016x_3x_5 + 0.3000x_4x_5 + 0.0002x_1^2 + 0.0172x_2^2 - 0.0339x_3^2 - 0.3409x_4^2$ $+ 0.0831x_5^2$
Oct	CY <sub>t-1</sub>	DA1	DA3	DA6			$-48.806 - 0.6966x_1 - 0.4241x_2 - 1.7664x_3 - 3.0097x_4 + 0.0040x_1x_2 + 0.0053x_1x_3$ $- 0.0175x_1x_4 - 0.0038x_2x_3 + 0.0111x_2x_4 - 0.1443x_3x_4 + 0.0008x_1^2 + 0.0073x_2^2 + 0.0861x_3^2$ $+ 0.0558x_4^2$
Nov	CY <sub>t-1</sub>	DA1	DA3	DA6			$47.8316 - 0.6925x_1 + 0.7765x_2 - 2.3671x_3 - 2.9813x_4 + 0.0043x_1x_2 + 0.0011x_1x_3$ $- 0.0066x_1x_4 + 0.0797x_2x_3 - 0.0306x_2x_4 - 0.0144x_3x_4 + 0.0004x_1^2 - 0.0064x_2^2 - 0.0407x_3^2$ $+ 0.0200x_4^2$
Dec	CY <sub>t-1</sub>	DA6	DA9				$13.0378 - 0.5111x_1 + 0.5765x_2 - 3.4820x_3 + 0.0177x_1x_2 - 0.0158x_1x_3 + 0.0155x_2x_3$ $+ 0.0004x_1^2 - 0.0691x_2^2 + 0.0343x_3^2$



#### 565 **4.5 Modelling limitations**

566 The modelling limitations of the presented approach are the following.

567 (1) To determine drought areas, a threshold value of the Standardised Precipitation  
568 Evapotranspiration Index (SPEI) drought index ( $\text{SPEI} \leq -1$ ) was used. Using just one threshold  
569 might lead to over or underestimation of the actual drought impacts over crop yield.

570 (2) Gridded data of SPEI at spatial resolution ( $0.5^\circ \times 0.5^\circ$ ) was used in this study over each  
571 region individually. Using such a coarse spatial resolution on different region sizes might not  
572 capture the drought area correctly, leading to over or underestimating its magnitude.

573 (3) The study area has a diverse ecosystem of irrigated and rain-fed land, which may influence  
574 the correlation between DA and crop yield more or less.

575 (4) This study assumes that drought is the only causative factor; however, floods negatively  
576 impact crop yield in the region, thus in the total production in the regions. Flood impacts are  
577 not considered in the models.

578 (5) Many other factors might influence rice yield, such as market, technologies, management,  
579 etc. In this study, it was assumed that drought plays the prominent role.

580 (6) Insufficient crop yield data for the ML model building was an issue because the CY time  
581 series only had one value for each year.

#### 582 **4.6 Crop yield calculation systems**

583 The crop yield calculation is often based on at least one or both types of systems, the one based  
584 on ground-field visits and the one based on remote-sensing information. Regarding the  
585 temporal scale, those based on ground-field visits are usually issued twice or even four times,  
586 as in the case of India, depending on the agricultural calendar. On the other hand, in the case  
587 of remote-sensing information, they are usually more continuous, in fortnightly or monthly  
588 periods, and aggregated by seasonal periods. The calculations are based on data-driven  
589 equations to more complicated models based on crop growth and development. About the  
590 spatial scale, ground-field visits-based calculations are generally issued for the different  
591 cultivation districts or aggregated by regions and the whole country. In the case of remote-  
592 sensing-based calculations, it depends on the spatial resolution of the input data. In theory, the  
593 outputs can be scaled down to the district level, although calculations aggregated by district,  
594 region, and country are often presented in practice. Although the remote-sensing-based systems  
595 have an advance over ground-field visits based method by providing information in the early  
596 stages of crop growth, the data required for its execution may not always be available. The ML



597 approach presented here falls into the second group; therefore, it shares similar limitations on  
598 latency, data availability, and spatial and temporal resolution.

#### 599 **4.7 On the consideration of other factors, types of drought and indices**

600 Although many drought indices are initially created to analyse a specific type of drought, it is  
601 also possible to identify other drought types for which indices were created by considering  
602 different aggregation periods. In our study, this was the case. For this reason, we do not  
603 emphasise agricultural drought throughout the manuscript because we are not using only  
604 aggregation periods usually used for agricultural drought analysis. From our correlation  
605 analysis between crop yield and drought areas, we infer that different types of drought (i.e.  
606 meteorological, agricultural, and hydrological) affect the crop yield to varying degrees  
607 throughout the months of the crop period. This level of affectation could be considered to build  
608 the ML models by using the different hydro-meteorological variables or selecting different  
609 aggregation periods of the meteorological variables, as was the case in this research.

610 Although we have tried to describe how the monthly time series on the calculated drought areas  
611 were matched with the seasonal crop yield data to build our ML approach, some readers may  
612 find the procedure complicated to replicate. If this is the case, we propose two alternatives. One  
613 is to consider an agricultural drought indicator, such as those based on soil moisture. The  
614 second is using a single aggregation period and concentrating on the construction of the ML  
615 model, exploring different types of ML models and modelling strategies.

616 For the agricultural drought assessment, soil moisture is one of the most suitable variables for  
617 correct monitoring and analysis. The use of soil moisture depends mainly on the availability  
618 and accuracy of this information. We envision using soil-moisture-derived drought indicators  
619 in future studies in similar applications like the one presented here.

620 Methodologies that consider other factors such as agricultural practices, soil properties and  
621 conditions, among others, are ideal to follow; however, this is not always possible. Our study  
622 presents a methodological alternative for predicting crop yield. There are current approaches  
623 for crop yield calculation in the study area, one based on field visits and another based on  
624 remote-sensing inputs. The main drawbacks and advantages are indicated in the Introduction  
625 Sect. Our methodology complements these two mentioned tools by providing crop yield  
626 prediction that can be compared with the current tools, with the difference that our ML  
627 approach produces results before the harvest (i.e. prediction).

628 Our research could be extended further. In subsequent studies, we consider that irrigation  
629 practices could be analysed, where the best practices could be identified. Our results indicate



630 that the increase in drought area is highly correlated with the decrease in crop yield. A more  
631 detailed analysis will make it possible to identify the best agricultural management practices,  
632 identify sub-regions more/less vulnerable to the effects of the different types of drought, and  
633 detect various demands on water resources throughout the different farming systems.  
634 The degree of influence of anthropogenic factors, such as farmer operational practices, and  
635 other factors such as soil conditions, or other natural phenomena such as floods, could be  
636 included in the ML approach. One way to implement the above is as follows. Three or more  
637 types of inputs could be classified: anthropogenic, natural, and different types of combinations.  
638 The variable selection analysis could be carried out for each set of inputs to identify the ones  
639 that primarily drive agricultural production. Subsequently, the ML models could be built  
640 following our proposed approach, i.e. the use of ANN models (or similar models) and  
641 equations.  
642 Weighting the drought areas can be another way to include anthropogenic factors or other  
643 variables. Factors calculated with the additional variables can be used to modify the drought  
644 areas. In this way, the areas would be altered to a greater or lesser extent, increasing or  
645 attenuating the effects of the drought.  
646 Another line that we see much development in the future is the construction of ML models  
647 considering the study area spatially discretised in cells. The availability of spatial data is crucial  
648 in this type of analysis; advances in remote sensing and the different earth monitors developed  
649 in the last decades could facilitate the implementation of this spatially-distributed methodology  
650 using more advanced ML approaches.  
651 Finally, this research can also be extended to analyse the climate change scenarios, either to  
652 elucidate the consequences over crop yield or to find the best crop management practices to  
653 face the predicted problems.

## 654 **5 Summary and conclusions**

655 This research introduced a step-by-step ML approach for predicting crop yield (CY) with  
656 drought areas (DAs) as input. The ML approach comprises two components. Each component  
657 employs two types of ML models: polynomial regression (PR) and artificial neural network  
658 (ANN). The goal was to build the ML models (ANN and PR) and use them as an integrated  
659 tool to crop yield prediction. The formulas of the PR models were also provided. The ML  
660 approach was applied in three East India regions.

661  
662



663 The following conclusions are drawn from this research.

- 664 • Based on the performance of PR and ANN models, results show drought area to be a  
 665 suitable variable to predict crop yield.
- 666 • The correlation analysis between DA and CY showed high negative correlations in  
 667 Odisha (region 3). The correlation gradually decreases in Bihar and Jharkhand (region  
 668 1) and West Bengal (region 2). These correlation values can be because West Bengal  
 669 has better access to irrigation facilities than Odisha and Bihar & Jharkhand.
- 670 • On comparing ANN models and PR models, the ANN were more accurate than PR  
 671 models to predict crop yield for all regions. This could have been expected since the  
 672 drought–crop relationship is a highly non-linear problem.
- 673 • It can be concluded that ANN has a high capability to predict CY in the pre-harvesting  
 674 stage with good accuracy, considering the drought indicator used (SPEI), which uses  
 675 climate variables such as precipitation and temperature (for evapotranspiration  
 676 calculation).

677 From the analysis and findings of this research, the following recommendations can be  
 678 provided for further improvement.

- 679 • Sensitivity analysis should be performed to identify the parameters that can impact the  
 680 model results. For instance, different spatial resolutions of drought indicator and  
 681 different thresholds should be investigated.
- 682 • Wet extreme events should be considered, especially in the flood-prone regions such as  
 683 the coastal areas of West Bengal (region 2) and Odisha (region 3) and North Bihar  
 684 (region 1), where floods also influence crop yield.
- 685 • Non-climatic factors such as econometric, fertilisers, and management practices might  
 686 be considered because they influence crop yield.
- 687 • In order to improve the model accuracy, more input data should be used in further  
 688 studies. For CY, this can be estimated by remote sensing techniques on a monthly basis  
 689 so that the ML models can be built for this temporal resolution and the spatial coverage  
 690 can be better addressed.
- 691 • The performance of other ML models has to be investigated, especially committee  
 692 (ensemble) methods like random forests or boosting methods. In the case of data at  
 693 scales less than monthly, the use of deep learning algorithms (e.g. LSTM networks)  
 694 could be recommended to explore.

695 We envision that this research will improve drought monitoring systems for assessing drought  
 696 effects. Since it is currently possible to calculate drought areas within these systems, the direct  
 697 application of the prediction of drought effects is possible to integrate by following approaches  
 698 such as the one presented or similar.





## 699 **Coda and data availability**

700 State-wise crop-yield data was retrieved through the Indian Directorate of Economic and Statistics from the  
 701 Department of Agriculture (DAC) (<http://eands.dacnet.nic.in/>). The SPEI data was retrieved from the SPEI Global  
 702 Drought Monitor (<https://spei.csic.es>). The code is available upon request from the corresponding author.

## 703 **Competing interests**

704 An author is member of the editorial board of journal HESS. The peer-review process was guided by an  
 705 independent editor, and the authors have also no other competing interests to declare.

## 706 **Acknowledgements**

707 VD thanks the Mexican National Council for Science and Technology (CONACYT) and Alianza FiiDEM for the  
 708 study grand 217776/382365. AAAO was supported by the Orange Knowledge Programme (former NFP) and the  
 709 World Meteorological Organization (WMO). GACP and VD acknowledge the grand No. 2579 of the Prince  
 710 Albert II of Monaco Foundation. HvL is supported by the H2020 ANYWHERE project (Grant Agreement No.  
 711 700099). DS acknowledges the grant No. 17-77-30006 of the Russian Science Foundation, and the  
 712 Hydroinformatics research fund of IHE Delft in whose framework some research ideas and components were  
 713 developed. The study is also a contribution to the UNESCO IHP-VII programme (Euro FRIEND-Water project)  
 714 and the Panta Rhei Initiative on Drought in the Anthropocene of the International Association of Hydrological  
 715 Sciences (IAHS).

## 716 **References**

- 717 Araneda-Cabrera, R.J., Bermúdez, M., and Puertas, J. (2021). Assessment of the performance  
 718 of drought indices for explaining crop yield variability at the national scale:  
 719 Methodological framework and application to Mozambique. *Agricultural Water*  
 720 *Management*, 246(September 2020), 106692.  
 721 <https://doi.org/10.1016/j.agwat.2020.106692>
- 722 Below, R., Grover-Kopec, E., and Dilley, M. (2007). Documenting Drought-Related Disasters:  
 723 A Global Reassessment. *J. Environ. Dev.*, 16(3), 328–344.  
 724 <https://doi.org/10.1177/1070496507306222>
- 725 Bhalme, H.N. and Mooley, D. a. (1980). Large-Scale Droughts/Floods and Monsoon  
 726 Circulation. *Monthly Weather Review*, 108(8), 1197–1211. [https://doi.org/10.1175/1520-0493\(1980\)108<1197:LSDAMC>2.0.CO;2](https://doi.org/10.1175/1520-0493(1980)108<1197:LSDAMC>2.0.CO;2)
- 728 Bhatt, D., Maskey, S., Babel, M.S., Uhlenbrook, S., and Prasad, K.C. (2014). Climate trends  
 729 and impacts on crop production in the Koshi River basin of Nepal. *Regional*  
 730 *Environmental Change*, 14(4), 1291–1301. <https://doi.org/10.1007/s10113-013-0576-6>
- 731 Chlingaryan, A., Sukkarieh, S., and Whelan, B. (2018). Machine learning approaches for crop  
 732 yield prediction and nitrogen status estimation in precision agriculture: A review.  
 733 *Computers and Electronics in Agriculture*, 151(May), 61–69.  
 734 <https://doi.org/10.1016/j.compag.2018.05.012>
- 735 Corzo Perez, G.A., van Huijgevoort, M.H.J., Voß, F., and van Lanen, H.A.J. (2011). On the



- 736 spatio-temporal analysis of hydrological droughts from global hydrological models.  
 737 *Hydrology and Earth System Sciences*, 15(9), 2963–2978. <https://doi.org/10.5194/hess->  
 738 15-2963-2011
- 739 Dai, A. (2011). Characteristics and trends in various forms of the Palmer Drought Severity  
 740 Index during 1900–2008. *Journal of Geophysical Research*, 116(D12), D12115.  
 741 <https://doi.org/10.1029/2010JD015541>
- 742 Diaz, V., Corzo, G., Van Lanen, H.A.J., and Solomatine, D.P. (2019). Spatiotemporal Drought  
 743 Analysis at Country Scale Through the Application of the STAND Toolbox. In  
 744 *Spatiotemporal Analysis of Extreme Hydrological Events* (pp. 77–93). Elsevier.  
 745 <https://doi.org/10.1016/B978-0-12-811689-0.00004-5>
- 746 Diaz, V., Corzo Perez, G.A., Van Lanen, H.A.J., and Solomatine, D. (2016). Spatio-temporal  
 747 analysis of large-scale meteorological drought: helping to achieve the SDGs 6.A and 11.5.  
 748 In *12th Kovacs Colloquium*. Paris, France. <https://doi.org/10.13140/RG.2.1.2595.2888>
- 749 Diaz, V., Corzo Perez, G.A., Van Lanen, H.A.J., Solomatine, D., and Varouchakis, E.A.  
 750 (2020). An approach to characterise spatio-temporal drought dynamics. *Advances in*  
 751 *Water Resources*, 137, 103512. <https://doi.org/10.1016/j.advwatres.2020.103512>
- 752 Elshorbagy, A., Corzo, G., Srinivasulu, S., and Solomatine, D.P. (2010). Experimental  
 753 investigation of the predictive capabilities of data driven modeling techniques in  
 754 hydrology - Part 2: Application. *Hydrology and Earth System Sciences*, 14(10), 1943–  
 755 1961. <https://doi.org/10.5194/hess-14-1943-2010>
- 756 Food and Agriculture Organization of the United Nations (FAO). (2017). *The Impact of*  
 757 *disasters and crises on agriculture and Food Security*. Retrieved from  
 758 [www.fao.org/publications](http://www.fao.org/publications)
- 759 Food and Agriculture Organization of the United Nations (FAO) and Robert B Daugherty  
 760 Water for Food Institute at the University of Nebraska. (2015). *Yield gap analysis of field*  
 761 *crops, Methods and case studies*. (V. O. Sadras, K. G. G. Cassman, P. Grassini, A. J. Hall,  
 762 W. G. M. Bastiaanssen, A. G. Laborte, ... P. Steduto, Eds.), *FAO Water Reports* (Vol.  
 763 41). Rome, Italy.
- 764 Ghosh, K., Balasubramanian, R., Bandopadhyay, S., Chattopadhyay, N., Singh, K.K., and  
 765 Rathore, L.S. (2014). Development of crop yield forecast models under FASAL-a case  
 766 study of kharif rice in West Bengal. *Journal of Agrometeorology*, 16(1), 1–8.
- 767 Govindaraju, R.S. (2000). Artificial Neural Networks in Hydrology. I: Preliminary Concepts.  
 768 *Journal of Hydrologic Engineering*, 5(2), 115–123. [https://doi.org/10.1061/\(ASCE\)1084-](https://doi.org/10.1061/(ASCE)1084-)  
 769 0699(2000)5:2(115)



- 770 Guha-Sapir, D. (2019). EM-DAT: The Emergency Events Database - Université catholique de  
 771 Louvain (UCL) - CRED. Retrieved from [www.emdat.be](http://www.emdat.be)
- 772 Herrera-Estrada, J.E., Satoh, Y., and Sheffield, J. (2017). Spatio-Temporal Dynamics of Global  
 773 Drought. *Geophysical Research Letters*, 2254–2263.  
 774 <https://doi.org/10.1002/2016GL071768>
- 775 Huang, J., Gómez-Dans, J.L., Huang, H., Ma, H., Wu, Q., Lewis, P.E., Liang, S., Chen, Z.,  
 776 Xue, J.H., Wu, Y., Zhao, F., Wang, J., and Xie, X. (2019). Assimilation of remote sensing  
 777 into crop growth models: Current status and perspectives. *Agricultural and Forest*  
 778 *Meteorology*, 276–277(July), 107609. <https://doi.org/10.1016/j.agrformet.2019.06.008>
- 779 Kim, W., Iizumi, T., and Nishimori, M. (2019). Global Patterns of Crop Production Losses  
 780 Associated with Droughts from 1983 to 2009. *Journal of Applied Meteorology and*  
 781 *Climatology*, 58(6), 1233–1244. <https://doi.org/10.1175/JAMC-D-18-0174.1>
- 782 Maier, H.R. and Dandy, G.C. (2000). Neural networks for the prediction and forecasting of  
 783 water resources variables: a review of modelling issues and applications. *Environmental*  
 784 *Modelling & Software*, 15(1), 101–124. [https://doi.org/10.1016/S1364-8152\(99\)00007-9](https://doi.org/10.1016/S1364-8152(99)00007-9)
- 785 May, R., Dandy, G., and Maier, H. (2011). Review of Input Variable Selection Methods for  
 786 Artificial Neural Networks. In G. Dandy (Ed.), *Artificial Neural Networks -*  
 787 *Methodological Advances and Biomedical Applications* (p. Ch. 2). Rijeka: InTech.  
 788 <https://doi.org/10.5772/16004>
- 789 Mckee, T.B., Doesken, N.J., and Kleist, J. (1993). The relationship of drought frequency and  
 790 duration to time scales. *AMS 8th Conf. Appl. Climatol.*, (January), 179–184.  
 791 <https://doi.org/citeulike-article-id:10490403>
- 792 Monfreda, C., Ramankutty, N., and Foley, J.A. (2008). Farming the planet: 2. Geographic  
 793 distribution of crop areas, yields, physiological types, and net primary production in the  
 794 year 2000. *Global Biogeochem. Cycles*, 22(1), 1–19.  
 795 <https://doi.org/10.1029/2007GB002947>
- 796 Montesino Pouzols, F. and Lendasse, A. (2010). Effect of different detrending approaches on  
 797 computational intelligence models of time series. In *The 2010 International Joint*  
 798 *Conference on Neural Networks (IJCNN)* (pp. 1–8). IEEE.  
 799 <https://doi.org/10.1109/IJCNN.2010.5596314>
- 800 Naresh Kumar, M., Murthy, C.S., Sessa Sai, M.V.R., and Roy, P.S. (2012). Spatiotemporal  
 801 analysis of meteorological drought variability in the Indian region using standardized  
 802 precipitation index. *Meteorological Applications*, 19(2), 256–264.  
 803 <https://doi.org/10.1002/met.277>



- 804 Osman, A.A.A. (2018). *Spatiotemporal analysis and prediction of crop yield using data-driven*  
 805 *models and drought areas: case study of India*. UNESCO-IHE Institute for Water  
 806 Education, Delft. Retrieved from  
 807 <https://ihedelftrepository.contentdm.oclc.org/digital/collection/masters1/id/309029/rec/4>
- 808 Osman, A.A.A., Diaz, V., Corzo Perez, G.A., Van Lanen, H.A.J., and Solomatine, D. (2018).  
 809 Finding negative response of crop yield to drought: a spatiotemporal approach over East  
 810 India. In *International Conference on Water, Environment, Energy and Society*  
 811 *(ICWEES)*. Tunisia.
- 812 Rahmati, O., Falah, F., Dayal, K.S., Deo, R.C., Mohammadi, F., Biggs, T., Moghaddam, D.D.,  
 813 Naghibi, S.A., and Bui, D.T. (2020). Machine learning approaches for spatial modeling  
 814 of agricultural droughts in the south-east region of Queensland Australia. *Science of the*  
 815 *Total Environment*, 699, 134230. <https://doi.org/10.1016/j.scitotenv.2019.134230>
- 816 Reynolds, C.A., Yitayew, M., Slack, D.C., Hutchinson, C.F., Huete, A., and Petersen, M.S.  
 817 (2000). Estimating crop yields and production by integrating the FAO Crop Specific  
 818 Water Balance model with real-time satellite data and ground-based ancillary data.  
 819 *International Journal of Remote Sensing*, 21(18), 3487–3508.  
 820 <https://doi.org/10.1080/014311600750037516>
- 821 Sawasawa, H. (2003). *Crop yield estimation: Integrating RS, GIS and management factors, a*  
 822 *case study of Birkoor and Kortigiri Mandals*. MSc thesis. International Institute for Geo-  
 823 information Science and Earth Observation. Retrieved from  
 824 [http://www.itc.nl/library/papers\\_2003/msc/nrm/sawasawa.pdf](http://www.itc.nl/library/papers_2003/msc/nrm/sawasawa.pdf)
- 825 Sheffield, J. and Wood, E.F. (2011). *Drought: Past problems and future scenarios*. (P.  
 826 Earthscan, Ed.). London.
- 827 Udmale, P., Ichikawa, Y., Ning, S., Shrestha, S., and Pal, I. (2020). A statistical approach  
 828 towards defining national-scale meteorological droughts in India using crop data.  
 829 *Environmental Research Letters*, 15(9). <https://doi.org/10.1088/1748-9326/abacfa>
- 830 van Klompenburg, T., Kassahun, A., and Catal, C. (2020). Crop yield prediction using machine  
 831 learning: A systematic literature review. *Computers and Electronics in Agriculture*,  
 832 177(July), 105709. <https://doi.org/10.1016/j.compag.2020.105709>
- 833 White, M.A., Thornton, P.E., and Running, S.W. (1997). A continental phenology model for  
 834 monitoring vegetation responses to interannual climatic variability. *Global*  
 835 *Biogeochemical Cycles*, 11(2), 217–234. <https://doi.org/10.1029/97GB00330>
- 836 World Meteorological Organization (WMO). (2006). *Drought monitoring and early warning:*  
 837 *concepts, progress and future challenges*. WMO-No. 1006. Geneva, Switzerland.



838 Retrieved from  
839 [http://www.droughtmanagement.info/literature/WMO\\_drought\\_monitoring\\_early\\_warni](http://www.droughtmanagement.info/literature/WMO_drought_monitoring_early_warning_2006.pdf)  
840 [ng\\_2006.pdf](http://www.droughtmanagement.info/literature/WMO_drought_monitoring_early_warning_2006.pdf)  
841 Wu, X., Vuichard, N., Ciais, P., Viovy, N., Wang, X., Magliulo, V., and Wattenbach, M.  
842 (2016). ORCHIDEE-CROP (v0), a new process-based agro-land surface model: model  
843 description and evaluation over Europe, 857–873. [https://doi.org/10.5194/gmd-9-857-](https://doi.org/10.5194/gmd-9-857-2016)  
844 2016  
845