In-situ estimation of soil hydraulic and hydrodispersive properties by inversion of Electromagnetic Induction measurements and soil hydrological modelling

Giovanna Dragonetti[1,Ψ], Mohammad Farzamian[2,3,Ψ], ~~Antonio Coppola[4], ~~Angelo ~~Basile[5]~~Basile[4], Fernando Monteiro ~~Santos[4]~~Santos[3], Antonio Coppola[5]

[1]Mediterranean Agronomic Institute of Bari, Valenzano (BA), 70010, Italy

2Instituto Nacional de Investigação Agrária e Veterinária, Oeiras, 2780-157, Portugal

[3]Instituto Dom Luiz, Faculdade de Ciências da Universidade de Lisboa, Lisboa, 1749-016, Portugal

[4]Institute for Mediterranean Agricultural and Forestry Systems, National Research Council, Portici (NA), 80055, Italy

[5]School of Agricultural, Forestry, Food and Environmental Sciences, University of Basilicata, Potenza, 85100, Italy

Ψ These authors contributed equally to this work.

Correspondence: Mohammad Farzamian (mohammad.farzamian@iniav.pt) and Giovanna Dragonetti (dragonetti@iamb.it)

ABSTRACT

Soil hydraulic and hydrodispersive properties ~~is crucial~~are necessary for ~~the sustainable management of~~modelling water ~~resources~~ and solute fluxes in agricultural ~~land. Due to the local heterogeneity of soil hydrological properties~~ and ~~the lack of fast in-situ measurement techniques, it is hard to assess these properties at the field scale. The present study proposes a methodology based on the integration of~~environmental systems. Despite the large efforts in developing methods (e.g., lab-based, PTF), their characterization at applicative scales is still an imperative requirement. Accordingly, this paper proposes a non-invasive in situ method integrating Electromagnetic

Induction (EMI) and hydrological ~~modeling~~modelling to estimate soil hydraulic and transport properties at the ~~field~~plot scale.

To this aim, we carried out two sequential water infiltration and solute transport experiments ~~were carried out over a small field plot. The propagation of wetting front and solute concentration along the soil profile was monitored~~and conducted time-lapse EMI surveys using ~~an EMI sensor (i.e.~~ a CMD mini-Explorer~~), Time Domain Reflectometry (TDR) probes, and tensiometers. Time-lapse apparent electrical conductivity (σ_a) data obtained from the EMI sensor were inverted to estimate the evolution of the vertical distribution of the bulk electrical conductivity (σ_b) over time. The σ_b distributions were converted to water content and solute concentration by using a laboratory calibration, relating σ_b to water content (θ) and soil solution electrical conductivity (σ_w). The hydraulic and hydrodispersive properties were then obtained by an optimization procedure minimizing the deviations between the numerical solution of the water flow and solute transport processes and the estimated water contents and concentrations inferred from the EMI results. The EMI-based results were finally compared to the results obtained from the in-situ TDR and tensiometer measurements.~~

~~In general, the EMI readings lead to underestimated water contents as compared to the TDR data. And yet, the water content changes over time detected by the EMI closely followed those observed by TDR and contain enough information for effective EMI-based reconstructions of water retention and hydraulic conductivity curves for the soil profile. In addition, this allowed us to reproduce the solute concentration distributions and thus the hydro-dispersive properties of the soil profile. Overall, the results suggest that time-lapse EMI measurements could~~ to examine how well this methodology can be used ~~as a rapid, non-invasive, field-scale method to assess soil~~

~~hydraulic and hydro-dispersive properties, which are critical to hydrological models for agro-environmental applications.~~

~~1. INTRODUCTION~~

~~Irrigated agriculture plays a crucial role in the food supply in many countries where ecological conditions are characterized by warm and dry summers with high solar radiation and evapotranspiration rates. Evaluating spatio-temporal variability of soil water and solute content is critical for optimal~~to i) monitor water content dynamic after irrigation ~~scheduling in timing, quantity, and quality (Coppola et al., 2019) and soil salinization assessment which depends on the variability of soil hydrological behavior (Chaali et al., 2013; Coppola et al., 2015). Soil hydrological behavior is generally described by solving the Richards' equation (RE) for water flow and the Advective-Dispersive equation (ADE) for solute transport, which is frequently assumed to apply at different spatial scales, from laboratory to field to larger scales (Sposito, 1998). These equations require the soil water retention and the soil hydraulic conductivity functions, as well as the hydro-dispersive properties, to be known at the scale of concern (Basile et al., 2003, 2006; Zech et al., 2015). Thus, the measurement methods and, consequently, the volumes investigated must be able to capture the hydraulic functions and~~ and to estimate the soil hydraulic van Genuchten–Mualem parameters from the water infiltration experiment and ii) to monitor solute concentration, and to estimate solute dispersivity from the solute transport experiment. We then compared the obtained results to those estimated by direct TDR and tensiometer probes measurements. ~~at the appropriate scale.~~

~~Yet, laboratory-scale~~ Our results show a good agreement between EMI-based estimation of soil hydraulic and transport properties with those obtained from the direct TDR and tensiometer probes measurements. When compared with direct TDR measurements ~~of hydraulic properties and~~

~~dispersivity have been frequently used for field-scale studies (Coppola et al., 2011a; Comegna et al., 2012). However, one has to be aware that the validity of these lab-based properties for solving RE and ADE at field scale is essentially~~, the EMI significantly underestimated the water content distribution, but the water content evolved similarly over time. This did not have a significant impact on the hydraulic conductivity curves since the hydraulic conductivity is mainly a function of water content variation, not its absolute value. On the other hand, this underestimation led to lower saturated water content, reflected in the water retention curve. The latter can be scaled by measuring the actual saturated water content at the end of the experiment with TDR probes or even by weighing soil samples.~~related to the size of the volume investigated, which has to appropriately represent the heterogeneity of the medium being studied (Wessolek et al., 1994; Ellsworth et al., 1996; van Genuchten et al., 1999; Inoue et al., 2000; Basile et al., 2003, 2006). An additional concern in lab-scale measurements is determining the hydrological properties of different soil horizons separately and then combining these properties to determine the behavior of the entire soil profile. This is especially important in the case of solute transport, where the transport process may change significantly depending on the solute travel times correlation among different layers (Coppola et al., 2011b).~~

1. INTRODUCTION

Dynamics agro-hydrological models are more and more used for interpreting and solving agro-environmental problems (Hansen et al., 2012; Coppola et al., 2015; Kroes et al., 2017; Coppola et al., 2019). The soil hydrological component of these models is frequently based on mechanistic descriptions of water and solute fluxes in soils. Richards equation (RE) for water flow and Advection-Dispersion equation (ADE) for solute transport is generally accepted to apply at a local scale (plot scale, for example). Solving RE requires the determination of the hydraulic properties, namely the water retention curve relating the soil water content, θ, to the soil water pressure head, *h*, and the hydraulic conductivity curve, relating the hydraulic conductivity, *K* to either the water content, θ or the pressure head, *h*. Similarly, ADE requires the dispersivity, λ, to be also known. In the last decades several laboratory and in-situ methods have been developed for characterizing soil hydraulic properties (e.g. Dane and Topp, 2020) and dispersive properties (e.g. Vanderborght and Vereecken, 2007). Lab-based characterizations may be carried out under more controlled conditions. Nevertheless, for simulating water and solute dynamics in the real field context, the in-situ methods are obviously more representative than the lab ones. This is firstly related to the size of the volume investigated, which has to appropriately represent the heterogeneity of the medium being studied (Wessolek et al., 1994; Ellsworth et al., 1996; van Genuchten et al., 1999; Inoue et al., 2000~~In situ methods also provide the proper properties to solve RE and ADE at the field scale. In~~). Actually, a water flow process observed in situ will be influenced by the heterogeneities (stones, macropores, etc.) found in the field. This is the main limitation of the relatively small soil columns generally analysed in the laboratory. By contrast, an in-situ characterization method, for example the well-known instantaneous profile method (Watson et al., 1966), can catch the hydraulic properties which are effective in describing the flow process observed in-situ. This will also depend on the measurement scale (the size of the plot) and on the observation scale of the sensors used. These issues have been dealt with in detail for example in Coppola et al. (2012; 2016) and in Dragonetti et al., (2018). Besides, the experimental boundary conditions used to carry out the hydraulic characterization in lab and in-situ may also induce a different shape of the hydraulic properties as determined in the lab and in-situ (Basile et al., 2006).

In-situ methods typically evaluate soil ~~hydrological~~hydraulic properties by monitoring an infiltration and/or a redistribution water flow ~~processes, and~~process (Watson et al., 1966). Similarly, in situ methods for determining hydro-dispersive parameters ~~by~~are generally based on monitoring of mixing processes following pulse or step inputs of a tracer on ~~a~~either large ~~plot~~plots or ~~a long~~along field transect (Severino et al., 2010; Coppola et al., ~~2011b).~~2011; Vanderborght and Vereecken, 2007). Inverse ~~modeling~~modelling is ~~then~~ frequently used to estimate the hydraulic and transport parameters simultaneously (Šimůnek et al., 1998; Abbasi et al., 2003; Groh et al., 2018). ~~Tension infiltrometers are also commonly used to monitor infiltration processes in situ for inverse modeling of parameters (Simunek et al., 1998; Coppola et al., 2011a; Wang et al., 2013); however, the measurement volume is too small to accurately characterize the behavior of a~~Yet, even by shortening the measurement procedure by simplified assumptions (e.g., Sisson and van Genuchten 1991; Basile 2006) all in-situ methods for the characterization of the whole soil profile~~.~~ ~~Thus, in general, for larger scale studies, in situ methods looking at the whole soil profile are generally desirable. Yet, where a large number of field locations have to be characterized, all the in-situ methods~~ remain extremely difficult to implement ~~and it remains critical to finding alternative methods of characterization of soil hydrology, which are fast enough and actually represent the in-situ behavior of the soil.~~also because they generally require installing sensors at different depths (e.g. TDR probes, tensiometers, access tubes for neutron probe) which are cumbersome and may induce soil disturbance, unless the installation is made much earlier than the experiment, to at least partly allowing the soil to recover through several wetting-drying cycles its natural structure.

~~Geophysical~~In this direction, geophysical non-invasive methods ~~such as~~based on the electrical resistivity tomography (ERT) ~~technique are used as~~ and Electromagnetic Induction (EMI) techniques represent a promising alternative to traditional ~~techniques~~sensors for soil hydraulic and transport parameters assessment. Many researchers have used the time-lapse ERT data (Binley et al., 2002; Kemna et al., 2002; Singha and Gorelick, 2005~~; Farzamian et al., 2015a~~) to monitor temporal water content and solute concentration changes ~~for the estimation of soil hydraulic and transport properties~~ in flow and transport models. The ~~electrical conductivity of any subsurface material is a complex function of different soil properties such as soil texture (Farzamian et al., 2020). However, the~~ dependence of ~~variations of~~ soil electrical conductivity on ~~changes in~~ soil water content and concentration is the key mechanism that permits the use of time-lapse ERT to monitor water and solute ~~movement~~dynamics in time-lapse mode along a soil profile, by relating resistivities to water contents and solute concentration distributions through empirical or semi-empirical relationships (e.g. Archie, 1942) or established in-situ relationships (e.g. Binley et al., 2002~~; Farzamian et al. 2017). While this method is still widely used for soil hydraulic parameters assessment, the efficiency of this method is limited in the root-zone investigation on a field scale, given the large number of electrodes that need to be installed for shallow investigation.~~).

~~To improve soil electrical conductivity surveying over large areas and within the root zone for agricultural and environmental applications, electromagnetic~~Electromagnetic induction (EMI) ~~can~~sensors may be used as an alternative to the ERT technique as ~~it allows for rapid survey at~~they allow for monitoring water and solute propagation through a ~~relatively low cost for shallow investigation. Apparent~~soil profile by simply moving the sensor above the soil surface without the need to install electrodes. An EMI sensor provides measurements of the depth-weighted apparent electrical conductivity (σ_a) ~~data,~~according to the specific distribution of the bulk electrical conductivity (σ_b), as well as the depth response function of the sensor used (McNeill, 1980). σ_a obtained from EMI sensors ~~at field-scale has~~have been used to map the geospatial and temporal variability of the soil water content and salinity (Corwin and Lesch, 2005; Bouksila et al. 2012; ~~Coppola et al., 2016;~~ Saeed et al., 2017). However, monitoring the ~~usefulness~~propagation of ~~σ_a is limited when studying~~ the ~~variation of the soil parameters~~water and solutes with depth~~,~~ along a soil profile (as ~~σ_a is a depth-weighted, average conductivity measurement and does not represent the soil bulk electrical conductivity (~~during a water infiltration or a solute transport experiment) requires the distribution of the σ_b~~)~~ distribution with depth ~~(~~to be known over time, which can be obtained by inversion of the σ_a observations from the EMI sensor (see for example, Borchers et al., 1997; Hendrickx et al., 2002; Lavoué et al., 2010; Mester et al., 2011; Deidda et al., 2014; Von Hebel et al., 2014; Dragonetti et al., 2018; Moghadas et al., 2019; Farzamian et al., 2019a; Zare et al. 2020; Mclachlan et al. 2020). More recently, ~~technological advances have seen~~this inversion has been facilitated by the development of multi-coil EM sensors which are designed to collect σ_a at multiple coil spacing and orientations simultaneously in one ~~pass.~~sensor reading. This allows a rapid investigation of the soil's electrical conductivity at several depth ranges~~. In addition, several inversion methods have been proposed~~ to obtain ~~the distribution of the σ_b from σ_a measurements (Monteiro Santos, 2004; Farzamian et al., 2015b; Moghadas et al., 2019; Zare et al.~~ soil~~The EMI survey and inversion algorithm has now led to significant improvement in soil digital mapping and equipped soil scientists with a field-scale and cost-effective technology to obtain soil moisture and salinity (Koganti et al., 2018; Dragonetti et al., 2018; Farzamian et al., 2019; Paz et al., 2019; 2020a) with depth over large areas quickly and cheaply. Most recently, time-lapse EMI surveys and inversion modeling have been also used to study the dynamic of~~ water content (Huang et al., 2016; Whalley et al., 2017) and ~~soil salinity~~solute concentrations (Paz et al~~. 2020b; Farzamian~~., 2020; Gomez Flores et al~~. 2021).~~., 2022) quickly and cheaply. However, the potential of ~~this method in assessing~~EMI sensors to assess soil hydraulic and hydro-dispersive parameters has not been yet studied due to the lack of high-resolution and well-controlled experiments, required to catch the complexity of water flow and transport process during infiltration ~~events~~experiments.

With these premises, in this paper we propose a procedure based on a sequence of water infiltration and solute transport experiments, both monitored by an EMI sensor, with the objective of estimating ~~field~~in-situ the parameters of soil hydraulic properties and ~~solute~~the dispersivity ~~parameters~~ of a soil profile with a non-invasive EMI sensor and relatively short ~~field~~ experiments at the plot scale. The sequence of water and solute infiltration has the main aim to discriminate the contribution of the water content and the soil solution electrical conductivity to the EMI-based σ_b. ~~This issue~~All the EMI data will be ~~clarified~~analysed by a hydrological model within a so-called uncoupled framework, which will be discussed in detail in the *Hydro-Geophysical uncoupled approach* section. The goodness of ~~these parameter estimations~~the adopted approach will be evaluated by comparing the EMI-based hydraulic and hydrodispersive properties to those obtained from in-situ TDR and tensiometer measurements. Our aim is to explore an approach that doesn't need sensors installation and minimise data necessary for the in-situ assessment of soil hydraulic and hydrodispersive properties.

2. HYDRO-GEOPHYSICAL UNCOUPLED APPROACH

~~A~~ Figure 1 provides a schematic view of a six-step (+ one step for comparison) procedure, ~~schematized~~based on an uncoupled approach (Camporese et al., 2015) which will be adopted in ~~Fig. 1, was taken in order to investigate the potential of the EMI method in estimating the~~ this work to estimate the soil hydraulic and ~~hydro-dispersive~~hydrodispersive properties~~: 1) inversion~~ using the data obtained from the EMI sensor. All the steps summarised below will be described in detail in the Materials and Methods section.

(i) Inversion of time-lapse σ_a EMI data obtained during ~~two experiments~~(i) a water infiltration experiment, hereafter 1^{st} experiment, and (ii) a subsequent solute transport experiment, hereafter 2^{nd} experiment, to generate EMI-based σ_b distributions for each experiment;~~ 2) laboratory~~

(ii) Laboratory calibration of the relationship θ-σ_b-σ_w in order to convert σ_b distributions to water content~~ (first~~, θ, (1^{st} experiment) and to soil solution electrical conductivity, σ_w, and therefore solute concentrations, ~~[Cl⁻], (second~~*C*, (2^{nd} experiment); ~~3) converting~~

(iii) Converting the σ_b distributions obtained from the ~~first~~1^{st} experiment to ~~as many~~ water content distributions, using the θ-σ_b-σ_w relationship, to be used in the next ~~step; 4)~~ numerical simulation ~~(~~step;

(iv) Numerical simulation, by using the HYDRUS-1D model~~)~~ (Šimůnek et al., 1998), of the ~~first water infiltration process~~1^{st} experiment in order to estimate the van Genuchten-Mualem ~~model~~ (vG-M) parameters through an inversion procedure based on the water contents inferred from step ~~3; 5) converting~~ (iii);

(v) Conversion of the σ_b distributions ~~inferred~~obtained from the ~~second~~2^{nd} experiment to ~~[Cl⁻]~~solute concentration distribution in order to estimate longitudinal dispersivity~~.~~, λ. In this step, ~~the soil solution electrical conductivity (σ_w)~~σ_w distribution was estimated by using the laboratory θ-σ_b-σ_w calibration. The θ distribution in the ~~second~~2^{nd} experiment was simulated based on the vG-M parameters obtained in step ~~4.~~(iv). This is a crucial step in the proposed procedure, as ~~this~~it allows to discriminate the contribution of the soil water electrical conductivity~~ to the EMI-based σ_b.~~, and thus of the solute concentration, to the σ_b EMI readings during the 2^{nd} experiment. The σ_w distributions were thus converted to ~~[Cl⁻]~~solute concentration by a ~~calibration σ_w-[Cl$^-$]; 6) numerical~~simple standard lab-based solute specific σ_w-C relationship;

~~(i)~~(vi) Numerical simulation of the second solute infiltration process in order to estimate ~~dispersivity~~λ through an inversion procedure based on the concentrations ~~coming~~obtained from step ~~5.~~(v).

~~(ii)~~(vii)An alternative dataset of θ and σ_b obtained from direct TDR measurements, as well as tensiometer pressure head (h) readings, collected during the two experiments, allowed us to obtain independent hydraulic and hydrodispersive properties (hereafter TDR-based for sake of simplicity) to be used as a reference to evaluate the EMI-based parameter estimation~~.~~ (see the horizontal grey box in Fig. 1).

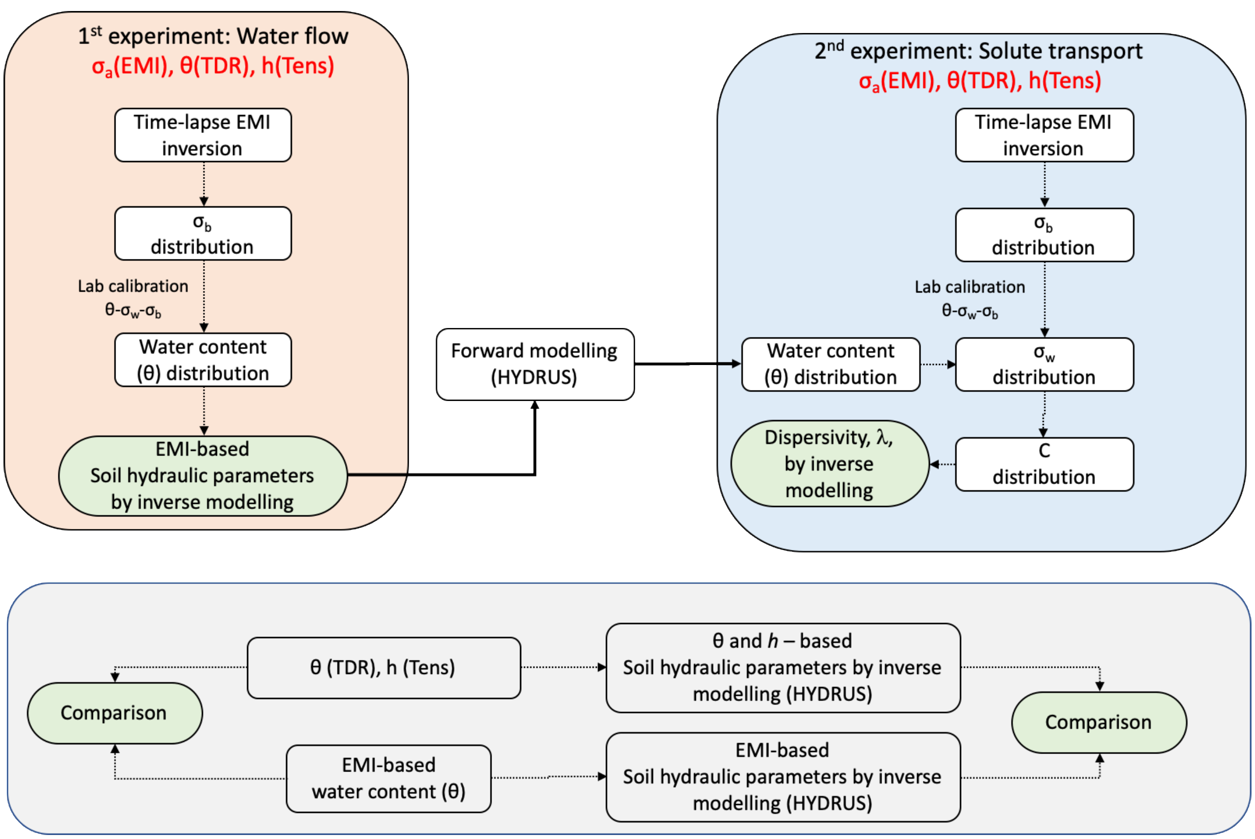


Figure 1: Schematic diagram of the proposed Hydro-Geophysical uncoupled approach

3. MATERIAL AND METHODS

3.1. Study area

The experiment was performed at the Mediterranean Agronomic Institute of Bari (CIHEAM-IAM), south-eastern coast of Italy. The study area is located at an altitude of 72 m with 41° 3' 13.251" N, ~~the~~a longitude of 16° 52' 36.274" E, and an elevation of about 68 m a.s.l. with a typical Mediterranean climate with rainy winters and very hot dry summers. The soil is a Colluvic Regosol consisting of silty loam layers of an average depth of 70 cm on a shallow fractured calcareous rock. ~~The soil is frequently tilled at 25~~Two main horizons on the calcareous rock may be identified: an Ap horizon (depth 0-30 cm~~,~~) and ~~scattered~~a Bw horizon (depth 30-70 cm). Scattered calcareous fragments are present due to the ~~frequent~~ breaking and grinding of the bedrock operated in the past by using heavy machinery in order to improve the soil structure and increase the soil depth for plantation~~.~~

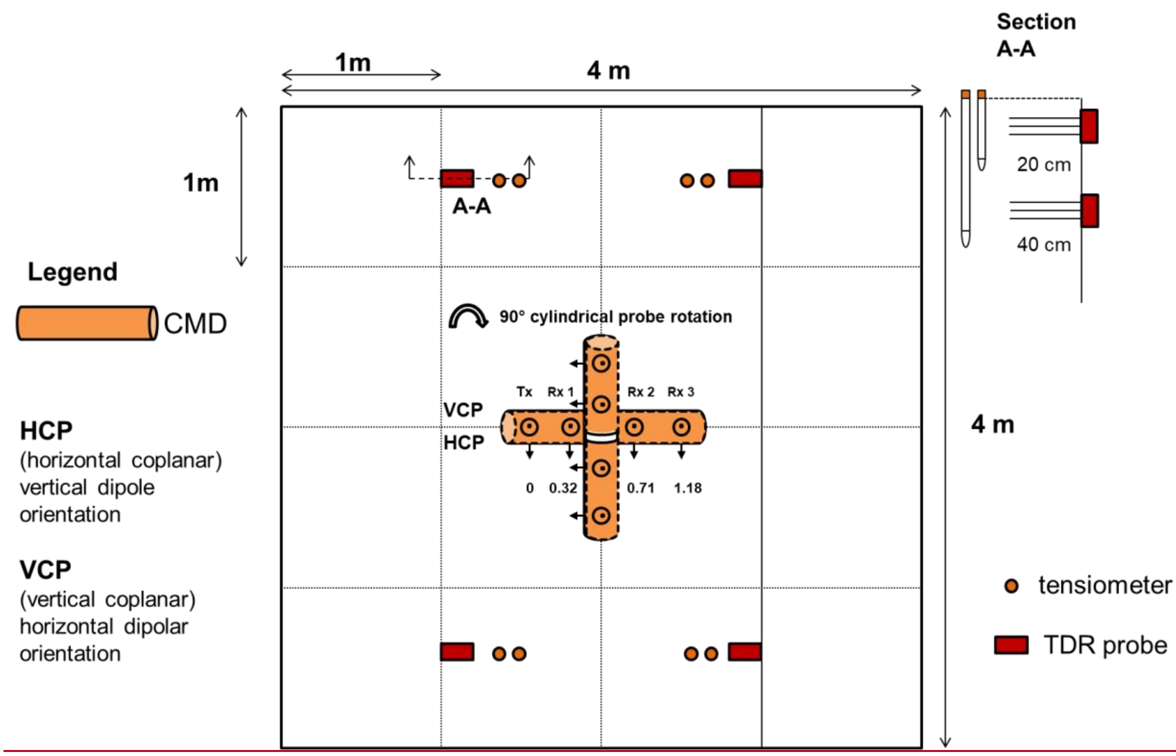
3.2. Experimental set-up

A layout of the experimental setup is shown in Fig. 2. The plot ~~sizes~~size is 4 × 4 m. Water was applied by using a drip irrigation system consisting of 20 lines, with drippers spaced 0.20 m and delivering a nominal flow rate of 10 l h^{-1}. Thus 400 drippers were installed, capable of delivering 4000 l h^{-1} on the whole plot. The dripper's grid spacing and the flow rate were selected to ensure that a 1D flow field rapidly developed after starting irrigation. The drip irrigation system was placed on a metallic grid to be easily moved away from the plot and whenever EMI measurements were taken on the ground soil. ~~The experimental plot was covered with a plastic sheet about four months prior to the experiment to keep the experimental plot under dry and a uniform water content condition at the beginning of the experiment.~~

~~Prior to the water infiltration experiments~~Several months before starting the 1st experiment, after digging a small pit, eight three-wire TDR probes, 7 cm long, 2.5 cm internal distance, and 0.3 cm in diameter, were inserted horizontally at 2 depths − 20 and 40 cm, corresponding to the Ap and the Bw horizon − in the 4 corners of the experimental plot (at 1 m distance from the plot edge), as shown in Fig. 2. A Tektronix 1502C cable tester (Tektronix Inc., Baverton, OR) was used in this study, enabling simultaneous measurement of water content, θ, and bulk electrical conductivity, σ_b, of the soil volume explored by the probe (Robinson et al., 2003; Coppola et al., ~~2011a, b~~2011; 2013). Furthermore, eight tensiometers were vertically inserted near each TDR probe to acquire water potentials by a Tensicorder sensor (Hydrosense3 SK800). Both TDR probes and tensiometers were installed for the evaluation of the EMI-based parameter estimation (step (vii)).

The experimental plot was firstly irrigated by using tap water with an electrical conductivity of about 1 dS m^{-1}~~. Eleven irrigation supplies were applied at regular intervals during one day at a 1 h frequency. Overall, an average water volume of 2000 l was supplied.~~ (1st experiment). We applied eleven irrigations, each lasting about 3 minutes to deliver about 180 l on the whole 16 m^2 plot for each irrigation (the volume was measured by a flowmeter). Irrigations were separated by about a 1-hour shutoff. At each irrigation starting, due to the short inertia of the irrigation system just after its switching on, for some seconds drippers delivered less than 10 l h^{-1}. For each irrigation an average flow rate of about 0.375 cm min^{-1} was applied, which generated a small ponding at the soil surface for a short time. Overall, an average water volume of 2000 l was supplied.

The propagation of the wetting front along the soil profile was monitored by using an EMI sensor (i.e. CMD mini-Explorer, GF Instruments, Czech Republic), positioned horizontally in the middle of the plot (see Fig. 2) in order to measure the apparent electrical conductivity, σ_a, in the soil profile in VCP (vertical coplanar, i.e., horizontal magnetic dipole configuration) mode and then HCP (horizontal coplanar, i.e., vertical magnetic dipole configurations) mode by rotating the probe 90° axially to change the orientation from VCP to HCP mode. The CMD Mini-Explorer operates at 30 kHz frequency and has three receiver coils with 0.32, 0.71 and 1.18 m distances from the transmitter coil, referred to hereafter as $\rho 32$, $\rho 71$, and $\rho 118$. The manufacturer indicates that the instrument has an effective depth range of 0.5, 1.0 and 1.8 m in the HCP mode, which is reduced to half (0.25, 0.5, and 0.9 m) by using the VCP orientation. As a consequence, this EMI sensor returns six different σ_a values (utilizing three offsets with two coil orientations) with each corresponding to different depth sensitivity ranges. All measurements were performed five minutes after each water pulse application by temporarily removing the irrigation grid~~.~~ and placing the EMI sensor in the middle of the plot. The infiltration was also monitored by TDR probes and tensiometers in order to monitor the space-time evolution of water content, θ, pressure head, h, as well as bulk electrical conductivity, σ_b. The distance of the TDR probes and tensiometers to the middle of the plot was specifically designed to avoid any interference with the EMI measurements.



Section
A-A
1m
4 m
1m
A-A
20 cm
40 cm
Legend
CMD
90° cylindrical probe rotation
Tx
Rx 1
Rx 2
Rx 3
VCP
HCP
0
0.32
0.71
1.18
4 m
HCP
(horizontal coplanar)
vertical dipole
orientation
VCP
(vertical coplanar)
horizontal dipolar
orientation
tensiometer
TDR probe

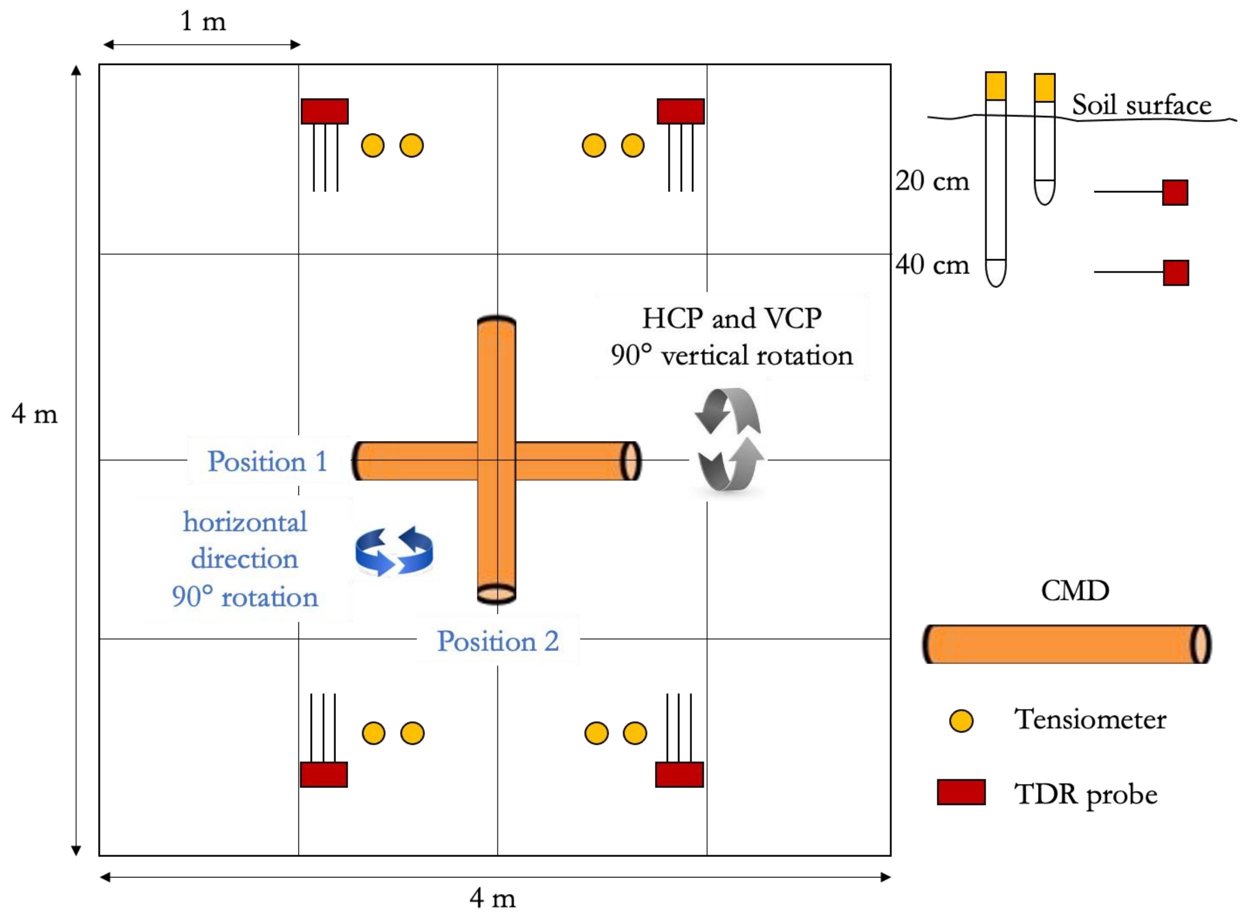


Figure 2. Layout of the experimental and monitoring set-up. HCP (horizontal coplanar) and VCP (vertical coplanar) are the vertical and horizontal dipolar orientations of the CMD probes, respectively.

At the end of the 1st ~~water infiltration~~ experiment, the soil was allowed to dry ~~again (by drainage and evaporation)~~and then covered with a plastic sheet to bring the distribution of water content along the profile similar to the initial one (observed before the water infiltration test). Afterward, a similar infiltration experiment (2nd) was carried out but using saline water at an electrical conductivity of 15 dS m^{-1}, and obtained by mixing $CaCl_2$ into the tap water. Again, eleven saline water supplies were provided at intervals of ~~1h~~about 1 h apart~~. In the 1st experiment, an average saline water~~ and a total volume of 2000 ~~liters~~ l saline water was supplied ~~for all~~

~~irrigation events~~during the experiment. The propagation of the water and chloride during the 2nd infiltration experiment was monitored similarly to the 1st experiment using TDR probes, tensiometers, and the CMD Mini-Explorer sensor.

3.3. Site-specific calibration θ-σ_b-σ_w-~~σ_b~~

The relationship ~~among~~between the bulk electrical conductivity (σ_b), the electrical conductivity of the soil solution soil water (σ_w~~)~~), and the water content, were obtained by using the model proposed by Malicki and Walczak, (1999):

$$\sigma_w = \frac{\sigma_b - a}{(\varepsilon_b - b)(0.0057 + 0.000071\, S)} \quad (1)$$

where ε_b (-) is the dielectric constant, which is related to the water content~~.~~ and *S* is the sand content in percent. The parameters a = 3.6 ~~d Sm~~dS m^{-1}~~;~~ and b = 0.11 were obtained in a laboratory experiment reported in Farzamian et al. (2021). The lab experiment for such a calibration is quite simple, fast, and standard procedure on reconstructed soil samples. An additional linear calibration, obtained by using solutions at different concentrations of calcium chloride was used to relate soil water concentrations of chloride, Cl^-, to σ_w.

3.4. ~~Forward modeling and~~ Inversion of time-lapse ~~inversion of~~ EMI σ_a data

Time-lapse ~~(TL)~~ σ_a data obtained during the experiments were inverted using a modified inversion algorithm proposed by Monteiro Santos et al. (2004) to obtain σ_b distribution in time. The aim of the inversion is to minimize the penalty function that consists of a combination between the observations' misfit and the model roughness (Farzamian et al., ~~2019~~2019b). The earth model used in the inversion process consists of a set of 1D models distributed according to the number of time-lapse measurements. All the models have the same number of layers (i.e. 7) whose thickness is kept constant. The selected thickness of layers is 10, 20, 30, 40, 55, 75 and 180 m. The number and thickness of layers were selected based on several factors including the number of σ_a measurements (i.e., 6), effective depth range of HCP and VCP modes (i.e., 5 of 6 measurements have an effective depth of less than 1m), and site specifications (i.e., the large variability of conductivity of the soil profile over a resistive bedrock). The parameters of each model are spatially and temporally constrained using their neighbours through smooth conditions. The forward modelling is solved based on the full solution of the Maxwell equations (Kaufman and Keller, 1983) to calculate the σ_a responses of the model. The inversion algorithm is Occam-regularization and the objective function was developed based on Sasaki, (2001). Therefore, the corrections of the parameters, in an iterative process are calculated solving the system:

$$[(J^T J + \eta C^T C)] \delta p = J^T b \qquad (2)$$

where δp is the vector containing the corrections applied to the parameters (logarithm of block conductivities, p_j) of an initial model, b is the vector of the differences between the logarithm of the observed and calculated σ_a [$b_i = \ln(\sigma_a{}^o/\sigma_a{}^c)_i$], J is the Jacobian matrix whose elements are given by $(\sigma_j/\sigma_{ai}{}^c)$ $(\partial\sigma_{ai}{}^c\ \partial\sigma_j)$, the superscript T denotes the transpose operation, and η is a Lagrange multiplier that controls the amplitude of the parameter corrections and whose best value is determined empirically. The elements of matrix C are the coefficients of the values of the roughness of each 1D model, which is defined in terms of the two neighbour's parameters and the constraint between the parameters of the different models on time. In this regard and in our temporal 1D experiment, each cell is constrained spatially by its vertical neighbours, while the temporal constraints are imposed using its lateral neighbours. An iterative process allows the final models to be obtained, with their response fitting the data set in a least-square sense. In terms of η, generally, large values will produce smooth inversion results with smoother spatial and temporal variations.

We performed several syntenic tests to determine how well the proposed inversion algorithm can predict spatiotemporal variability of σ_b and to fine-tune the regularization parameters. The syntenic scenarios were selected based on spatiotemporal variability of σ_a in the HCP and VCP modes, the site specification (e.g., shallow bedrock) and the expected evolution of conductive zone due to water and saline water infiltrations.

3.5. Numerical simulation of water flow and chloride transport in soil

The water and the chloride propagation monitored during the experiments were ~~also~~ simulated by using the HYDRUS-1D model (Šimůnek et al., 1998). HYDRUS-1D simulates water flow and solute transport by solving the Richards equation and the Advection-Dispersion equation, respectively.

Richards equation can be written for one-dimensional, unsaturated, non-steady state flow of water in the vertical direction as follows:

$$C_w(\theta)\frac{\partial h}{\partial t} = \frac{\partial}{\partial z}\left[K(h)\frac{\partial h}{\partial z} + K(h)\right] \quad (3)$$

where $C_w(\theta)$, the water capacity, is the slope of the water retention curve, θ is the volumetric water content [L^3L^{-3}], h is the soil water pressure head [L], $K(h)$ is the unsaturated hydraulic conductivity [LT^{-1}].

The Advection-Dispersion equation governing the transport of a single non-reactive and non-adsorbed (a tracer, chloride in our case) ion in the soil can be written as:

$$\frac{\partial(\theta C)}{\partial t} = \frac{\partial}{\partial z}\left[\theta D\frac{\partial C}{\partial z} - qC\right] \quad (4)$$

where q is the darcian flux, C is the solute concentration in the liquid phase [ML^{-3}], D (L^2T^{-1}) is the effective dispersion coefficient, which can be assumed to come from a combination of the molecular diffusion coefficient, D_{diff} (L^2T^{-1}) and the hydrodynamic dispersion coefficient, D_{dis} (L^2T^{-1}):

$$D = D_{\mathrm{diff}} + D_{\mathrm{dis}} \tag{5}$$

where~~ the~~ hydrodynamic dispersion is the mixing or spreading of the solute during transport due to differences in velocities within a pore and between pores. The dispersion coefficient can be related to the average pore water velocity $v=q/\theta$ through:

$$D = \lambda v \tag{6}$$

where λ [L] is the dispersivity, a characteristic property of the porous medium. To solve the Richards equation (Eq. 3), the water retention function, $\theta(h)$, and the hydraulic conductivity function, $K(h)$, must be defined. In this paper we adopted the van Genuchten-Mualem model (vG-M), (Van Genuchten, 1980):

$$S_e = [1 + (\alpha|h|)^n]^{-m} \tag{7}$$

$$K(h) = K_s {S_e}^{\tau}\left[1 - \left(1 - {S_e}^{1/m}\right)^m\right]^2 \tag{8}$$

In ~~the Equations~~Eqs. 7 and 8, $S_e = \frac{(\theta-\theta_r)}{(\theta_S-\theta_r)}$ is the effective water saturation, θ_s the saturated water content, θ_r the residual water content, α, *n* and *m* are fitting parameters with *m* taken as $m=1-1/n$, K_s is the saturated hydraulic conductivity and τ is the pore-connectivity parameter.

3.6. Inverse estimation of soil hydraulic and solute transport parameters

The obtained EMI-based spatiotemporal distribution of σ_b during the ~~water infiltration experiment (the~~ 1st experiment~~)~~ was converted to ~~a~~the θ distribution in order to estimate the temporal evolution of θ during the infiltration process. These water content data were then used in an optimization procedure by using the HYDRUS-1D model, in order to estimate the hydraulic properties of the different horizons in the soil profile. The simulations were carried out by using the actual top boundary flux conditions during the experiment, including the irrigation events. For the bottom boundary, free drainage was considered. A simulation domain of 150 cm depth was considered. The same procedure was repeated using the direct measurements of θ ~~(~~and *h* inferred from TDR~~)~~ and ~~pressure head (Tensiometers)~~tensiometers, respectively, in order to obtain independent hydraulic parameters (TDR-based estimation) to be compared to those inferred from EMI. A three-layer soil profile (0-25; 25-70; 70-150 cm), reflecting the actual pedological layering (i.e. ~~Ap, Bw, and bedrock) were used in all simulations.~~Ap, Bw, and bedrock) was used in all simulations. In terms of the initial condition, a hydrostatic distribution of the pressure heads, *h*, was considered for the TDR-based simulations. On the other hand, the water content distribution, inferred from the first EMI survey (before irrigation) was considered for the EMI-based simulation.

As for the solute transport experiment, a HYDRUS-1D simulation was carried out with the EMI-based hydraulic properties obtained from the 1st experiment to simulate the water content distributions in correspondence with the EMI measurement times. The simulations of water infiltration and solute transport in the 2nd experiment ~~was~~were carried out by using the top boundary fluxes conditions ~~used~~applied during the 2nd experiment along with the same simulation domain, three-layer soil profile, and the bottom boundary and equilibrium initial conditions described above. Thus, for each monitoring time, we had available the σ_b distributions obtained from the EMI and ~~θ~~the θ distributions coming from the HYDRUS-1D simulations. These distributions allowed us to estimate as many σ_w (and thus *C*) distributions by using the θ-σ_b-σ_w

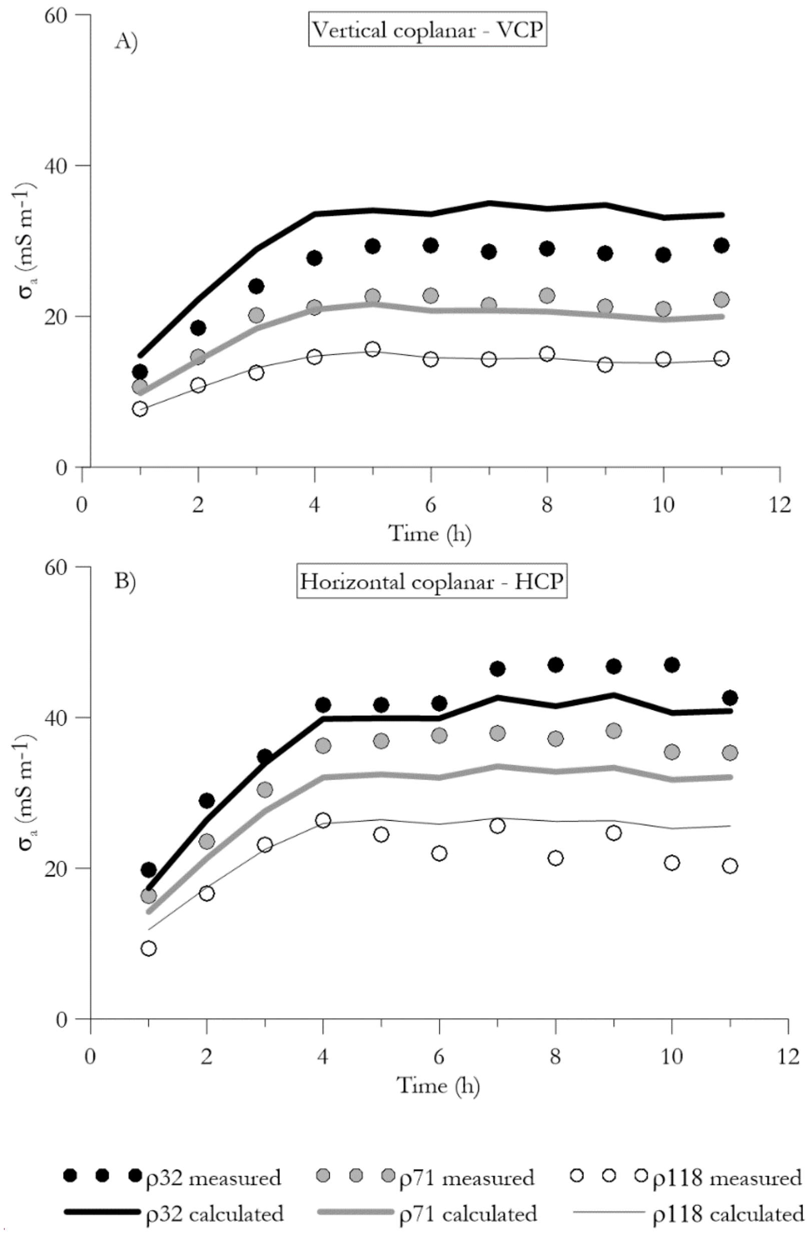
relationship obtained in the laboratory. These *C* distributions were used in a new HYDRUS-1D simulation to estimate the longitudinal dispersivity of the investigated soil. The simulated concentrations, with the optimized dispersivity, λ, were compared to those obtained from the TDR and tensiometer data.

4. RESULTS AND DISCUSSION

4.1. Water infiltration – 1st experiment

4.1.1. *Time-lapse σ_a data and estimation of σ_b distribution*

Figure 3 shows the σ_a values observed during the water infiltration experiment. Both VCP and HCP modes show a relatively similar pattern of σ_a values with ρ32 and ρ118 being the highest and lowest respectively. HCP mode shows higher values compared to the VCP mode in the same receivers. This pattern of σ_a distribution suggests the presence of a conductive zone over a resistive zone which is expected in this experiment as a result of the waterfront being infiltrated into the soil profile and the presence of a resistive bedrock. In terms of temporal σ_a variabilities, the σ_a increases consistently in both VCP and HCP modes during the first three hours of the experiment. Afterward, σ_a did not change significantly toward the end of the experiment. The range of σ_a variations is relatively small in both VCP and HCP modes with the former in the 10-30 mS m^{-1} range and the latter in the 10-50 mS m^{-1} range.


A)
Vertical coplanar - VCP
B)
Horizontal coplanar - HCP
σa (mS m-1)
Time (h)
0
2
4
6
8
10
12
20
40
60
ρ32 measured
ρ71 measured
ρ118 measured
ρ32 calculated
ρ71 calculated
ρ118 calculated

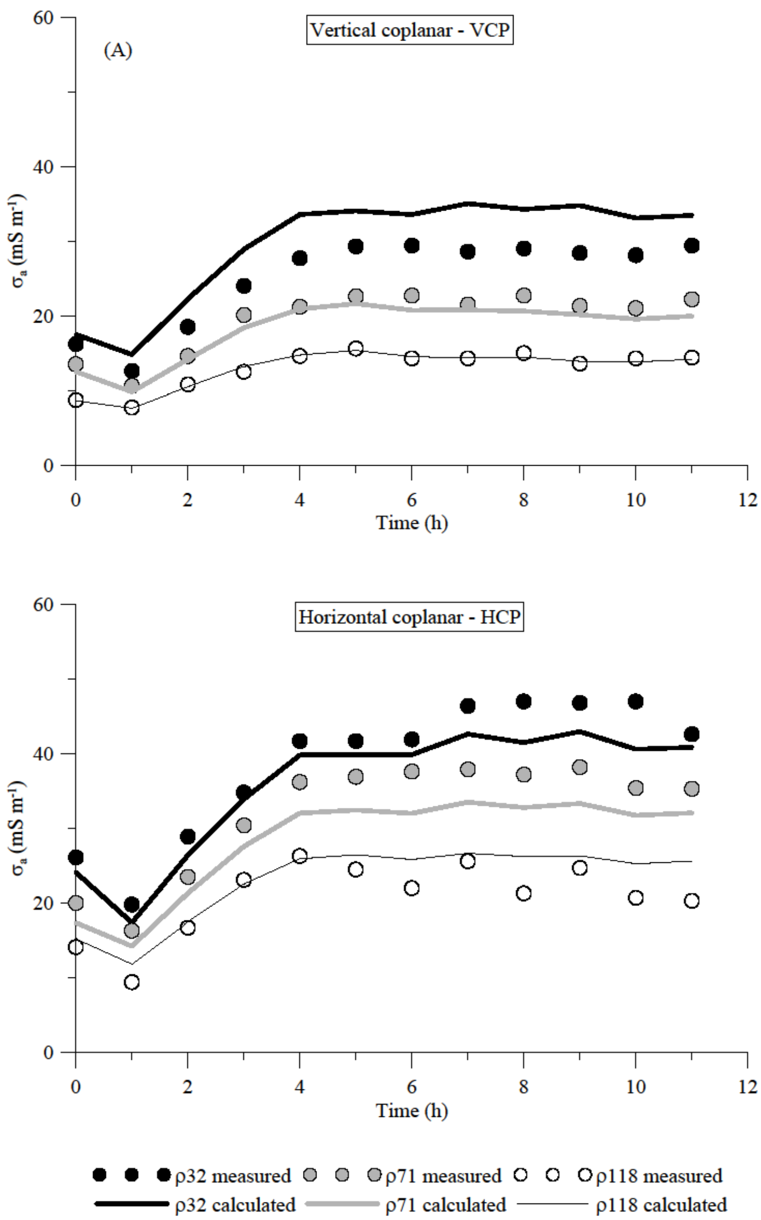


Figure 3: σ_a values observed during the water infiltration experiment. (A) VCP, (B) HCP. The symbols represent the measured data whereas the lines represent the values calculated after the inversion.

~~Fig.~~Prior to the inversion of σ_a data we fine-tuned the regularization parameter, η, as discussed in 3.4. the results of several synthetic tests (not shown here) suggest that a value of η between 1 to 5 provides a better result in resolving the spatio-temporal σ_b distributions in both experiments. Figure 4 depicts the time-lapse σ_b ~~modeling~~modelling results of σ_a shown in Fig. 3. The model shows clearly the evolution of the conductive zone into the soil profile shortly after the irrigation started as expected from the σ_a data. The resistive zone beneath a conductive zone corresponds to the bedrock layer in the experimental plot. The σ_b of the resistive zone remains below 5 mS m^{-1} and does not vary significantly during the experiment, while, in contrast, the σ_b of the upper layers increased significantly from an average of 20 mS m^{-1} at the beginning of the experiment to more than 50 mS m^{-1} after the 5^{th} irrigation. The conductivity of this zone does not increase largely since then, suggesting that the ~~soil is fairly saturated after the 3^{rd} irrigation.~~ upper soil is fairly saturated after the 5^{th} irrigation. The calculated response of this model was shown in Fig. 3. There is a fairly good agreement between σ_a measurements and model response, however, a slight shift can be noticed in the ρ32- VCP mode and ρ71- HCP mode between data and model response. This shift can be due to several reasons such as i) the instrumental shift of one or more channels, ii) the large spatiotemporal variability of soil electrical conductivity in this experiment as well as smoothness constraint performed in the inversion process to stabilize the inversion process which make it difficult to resolve the sharp changes, and iii) the choice of initial model.

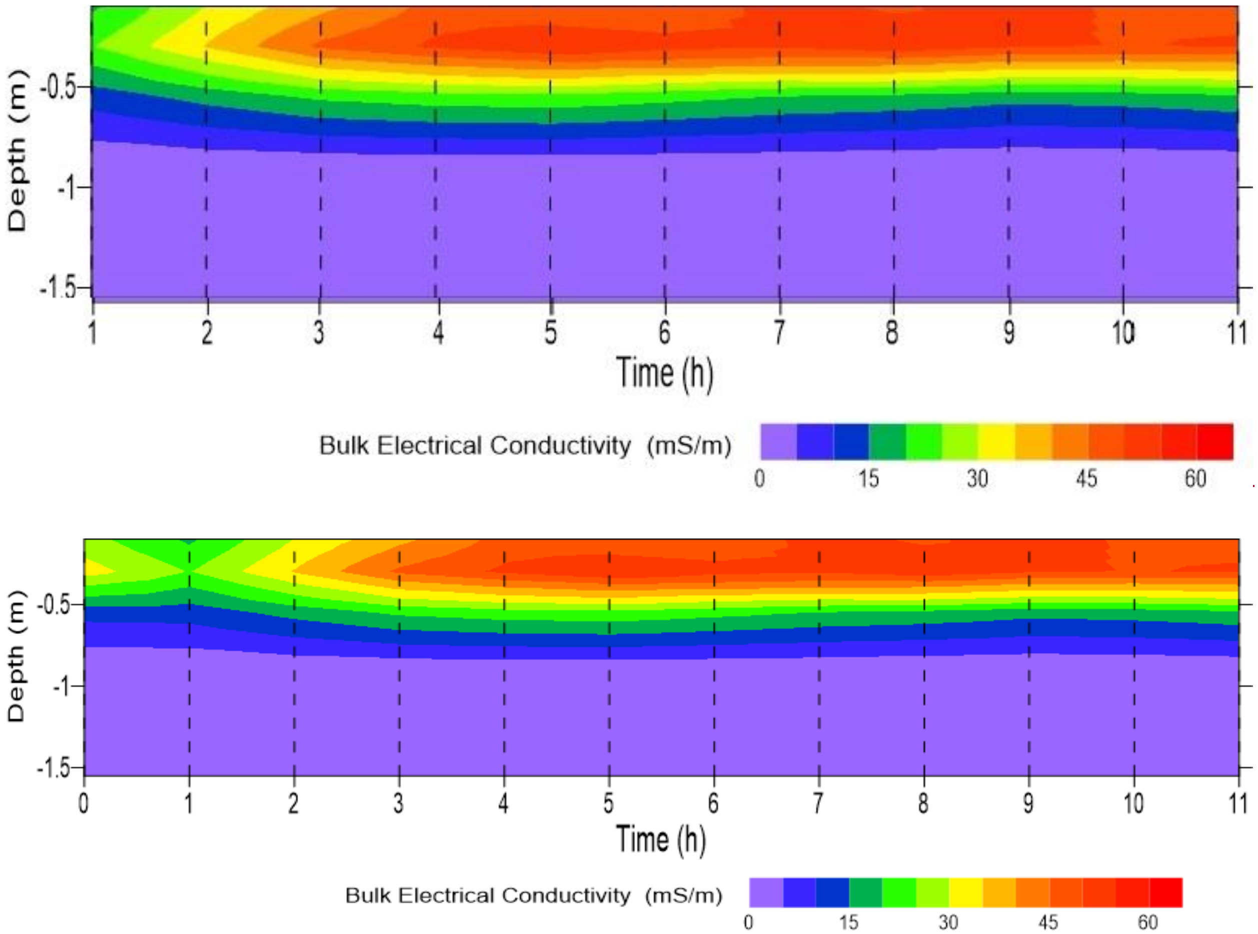


Figure 4. Time evolution of bulk electrical conductivity (σ_b) distribution with depth during the water infiltration experiment.

4.1.2. *Comparison between TDR~~ measurements ~~-based and EMI-based σ_b and θ ~~distribution~~distributions*

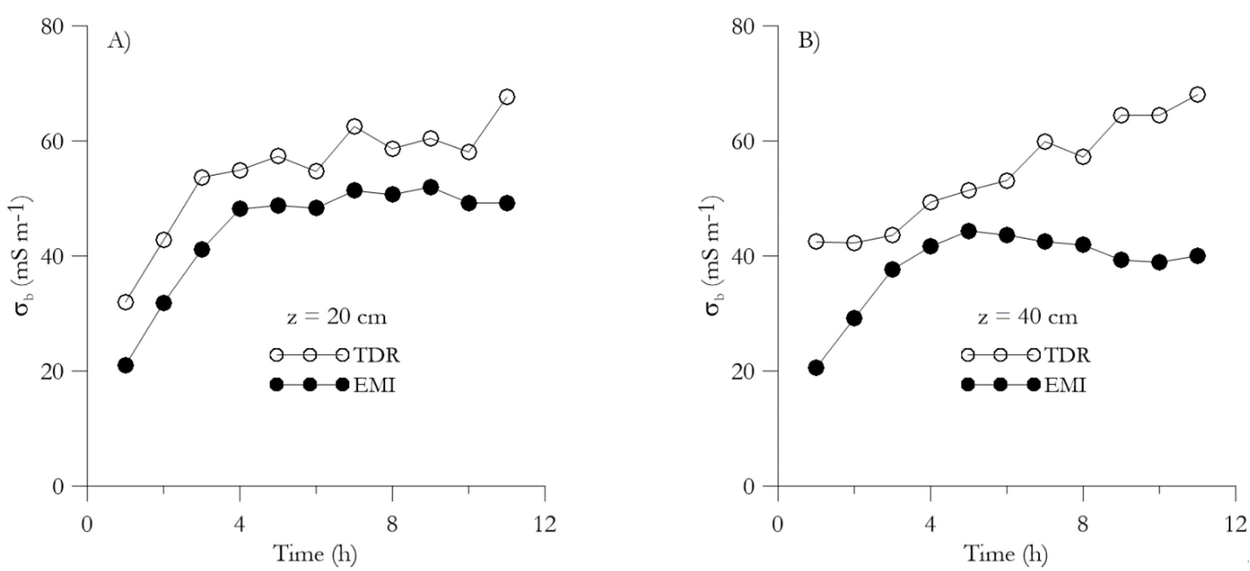
Figure 5 shows the temporal σ_b changes inferred from TDR and EMI observations at two depths, 20 and 40 cm~~, where the TDR probes monitored the water infiltration experiment.~~. As reported by ~~many~~some authors (e.g. Coppola et al., 2016; Dragonetti et al., 2018), both techniques provide σ_b estimations but a direct comparison between σ_b by TDR and EMI is not straightforward due to different ~~volumes of sensor investigation as well as the different nature of~~

~~measurements.~~observation volumes of the two sensors. As argued by Coppola et al. (2016), “because of its relatively small observation volume, a TDR probe provides a quasi-point-like measurements and do not integrate the small-scale variability (in soil water content, solute concentrations, etc.) induced by natural soil heterogeneity. By contrast, EMI data necessarily overrule the small-scale heterogeneities seen by TDR probes as they investigate a much larger volume”. However, this comparison can be used as a means to investigate the consistency of the σ_b trends and to provide an insight into the uncertainty associated with the EMI survey and inversion process in resolving the water infiltration process into the soil profile. Note that the average of TDR measurements in four corners at depths of 20 and 40 cm were considered both in this comparison and in the inversion procedure. The average values and the standard deviation of TDR measurements were presented in Fig. 5.

Focusing on the σ_b series inferred from both TDR observations and EMI inversion, a similar time pattern of σ_b variability is evident, but in general, the EMI model underestimates the σ_b obtained by TDR. A better agreement was observed at 20 cm in terms of both absolute σ_b values and trend (r=0.94; Mean Error=10.1 mS m^{-1}). In contrast, at 40 cm, the mismatch between TDR observations and EMI inversions becomes larger at the end of the experiment~~, but still in an acceptable range (r=0.54; Mean Error=16.1 mS m^{-1}).~~. The EMI σ_b values – especially at 40 cm depth – remain rather invariant in the last part of the infiltration experiment. The general outcome that for both layers the EMI σ_b values underestimate the TDR σ_b measurements has been frequently found in the literature (e.g. Coppola et al., 2015; Dragonetti et al., 2018; Visconti and De Paz, 2021). von Hebel et al. (2014) also found a similar ~~behavior~~behaviour when comparing their EMI results with ERT surveys. In that case, the σ_a values measured by EMI systematically underestimated the σ_a generated by applying EMI forward ~~modeling~~modelling to the σ_b

distribution retrieved from the ERT surveys. Furthermore, TDR measurements show a low local variability, as depicted in Fig. 5 by ~~ERT.~~ the error bars reporting the standard deviation of the σ_b as measured by the four TDR probes.

Figure 6 shows the evolution of θ at the same two depths, 20 and 40 cm as observed by TDR and EMI sensors. ~~While~~ TDR provides the direct ~~measurements~~in-situ measurement of θ~~,~~. In contrast in order to estimate θ from EMI observation, σ_b values extracted at these depths (Fig. 4) were converted to θ by the calibration performed in the laboratory, as detailed in Farzamian et al., (2021). A rapid increase of θ is visible shortly after injection in both EMI-based and TDR-based measurements. The EMI-based θ estimation is able to detect the similar water content evolution (similar water content differences over time) observed by ~~direct~~ TDR measurements but at a ~~slightly~~ different water content level. Specifically, EMI water contents were ~~mostly~~ lower than the TDR ones but the two series showed a quasi-parallel evolution at 20 cm depth (r=0.98; Mean Error=0.09 cm^3 cm^{-3}), while diverging for longer times at 40 cm depth (r=0.60; Mean Error=0.17 cm^3 cm^{-3}).



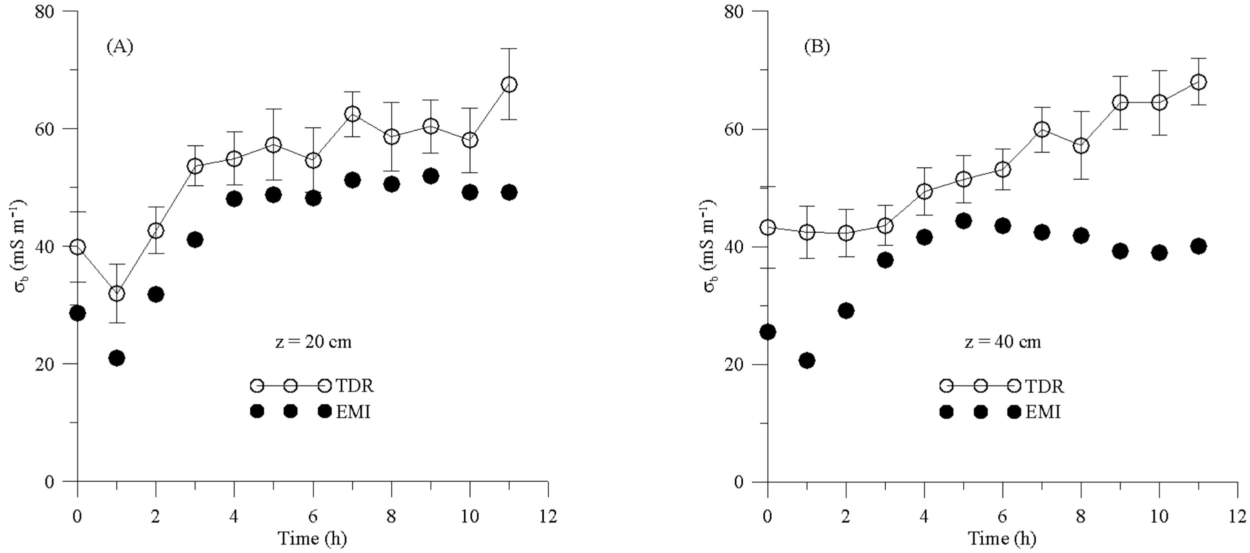
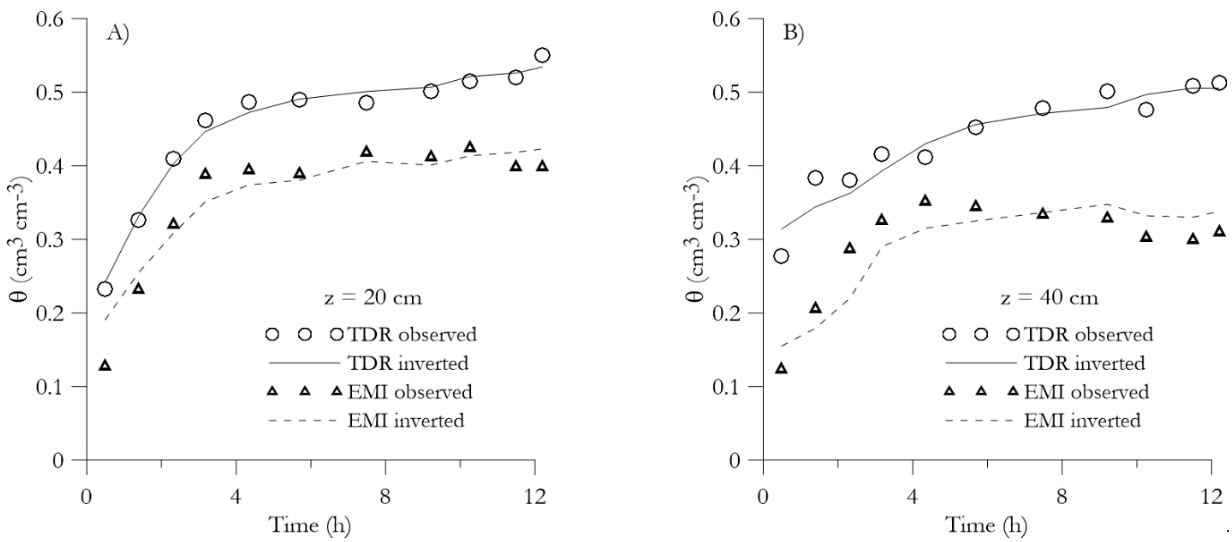


Figure 5. σ_b evolution estimated from the TDR and EMI measurements at 20 cm (A) and 40 cm (B) depths. The vertical bars represent the standard deviation of the measurements obtained by the four TDR sensors.



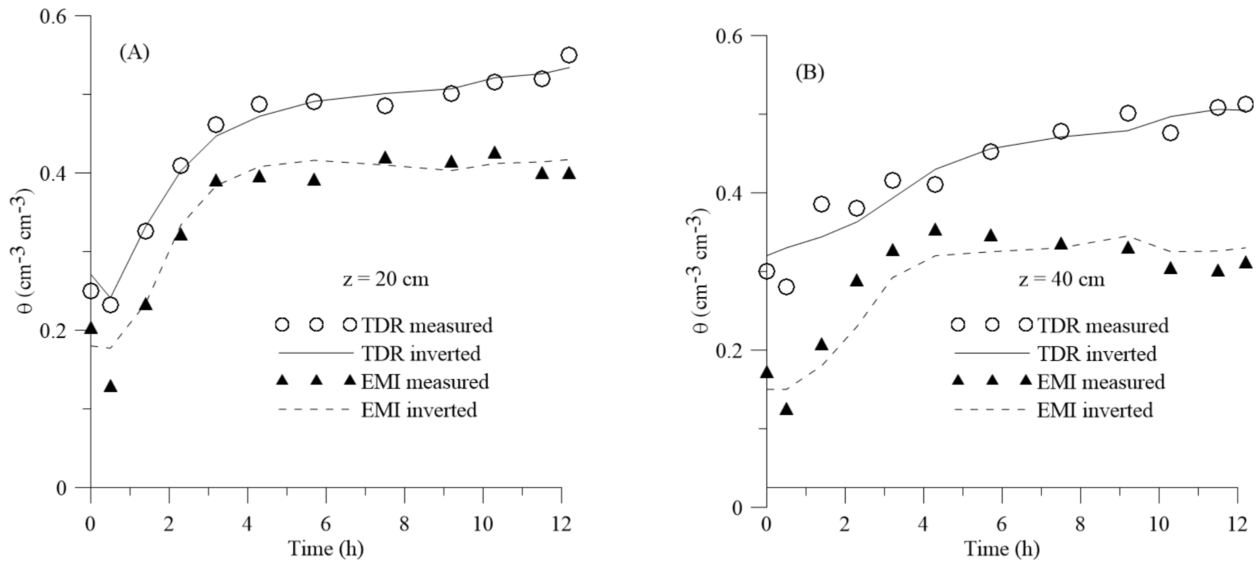


Figure 6. Evolution of θ measured by TDR (circles) and estimated from EMI measurements (triangles) at 20 cm (A) and 40 cm (B) depths. Continuous lines for TDR and dashed lines for EMI refer to the estimation obtained by the inversion procedure of the water infiltration process (see Sect. 4.1.3 below).

4.1.3. *Estimation of hydraulic properties*

In order to estimate hydraulic properties parameters, an inversion procedure was ~~performed using the~~ carried out applying HYDRUS-1D~~ model~~. The first set of hydraulic parameters was obtained by ~~optimizing~~using the soil water ~~content~~contents measured by TDR and the pressure ~~head~~heads measured by tensiometers ~~(hereafter~~ as measured data in the objective function for the optimization procedure (TDR-based~~ for sake of simplicity).~~). The second set of hydraulic parameters was obtained by ~~optimizing~~using the soil water ~~content~~contents estimated by EMI measurements ~~(hereafter~~ as measured data (EMI-based). The inversion simulations were carried out by fixing θ_r=0 and τ=0.5, while θ_s, α, n and K_s were optimized for ~~all~~both the Ap and the Bw layers~~ considered~~. The hydraulic properties of the bedrock were already known and fixed to

θ_r=0.068, θ_s=0.354, α=0.055, n=3.67, τ=0.5 and ~~k_s~~K_s=19.02 according to Caputo et al. (2010; 2015). We want to stress here that an a-priori characterization of the bedrock layer is not essential and the proposed procedure holds independently on the presence of bedrock. We could have treated the bedrock layer as any other layer in the soil profile, but inserting TDR probes and tensiometers into bedrock presents difficulties. Therefore, we decided to fix the bedrock parameters to the values already available from independent measurements. In different soils with either deeper or absent bedrock, we could have inserted TDR probes into deeper layers of the profile and applied the procedure to any of them.

In the inversion procedure, the parameters were determined separately for each horizon of the profile. First, the parameters for the topsoil were estimated and these parameters were then treated as known for the second layer estimation. According to Abbaspour et al. (1999), this approach makes parameter estimation of multi-layered profiles more feasible and accurate. It should be noted that in the case of the TDR-based estimations, optimization involved both measured water contents and pressure head data, whereas the EMI-based estimations only involved "measured" water contents.

Figure 6 reports a comparison between water contents measured (symbols) and estimated (lines) by the inversion procedure. The θ ~~distribution~~evolution was properly estimated at 20 cm depth in both approaches. ~~However, a~~It is worth noting here that, despite the differences in the absolute value of the water contents, a clear parallel behaviour of the two curves was observed, suggesting similar water content changes over time. A lower agreement was obtained at 40 cm but still ~~acceptable.~~ reproduced similar water content changes over time. This is a crucial point in this paper, as it is the main reason for the shape of the hydraulic properties we found for the TDR and EMI-based estimations.

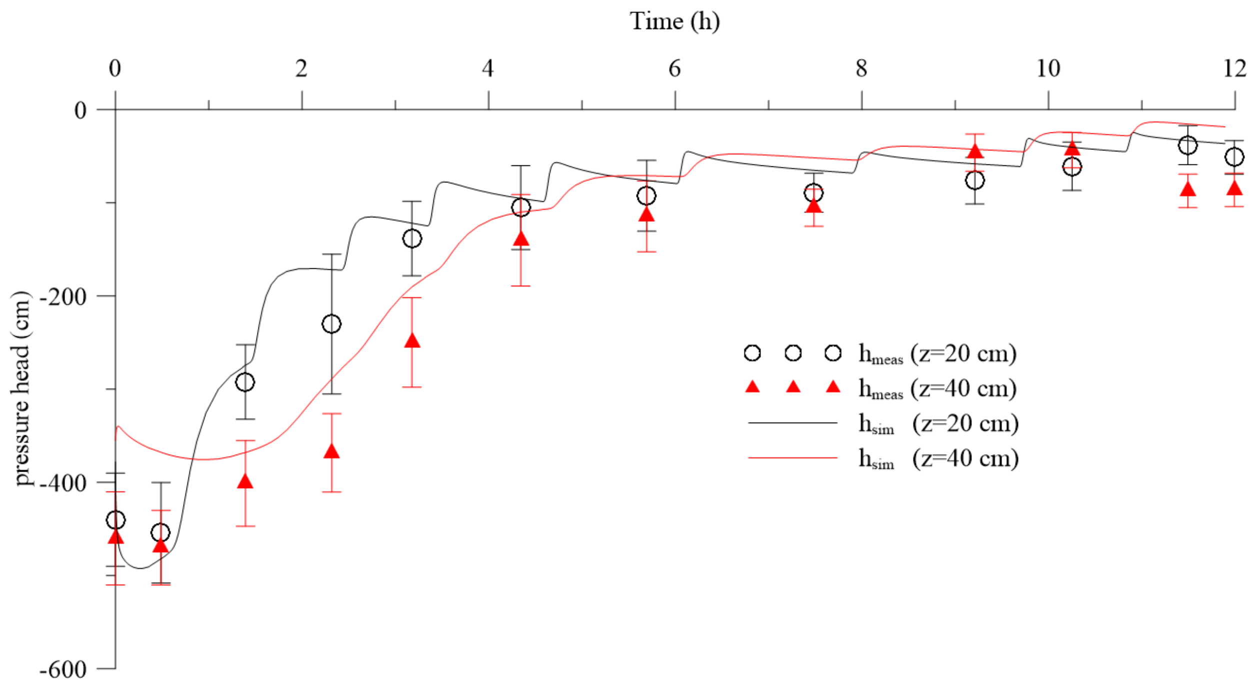


Figure 7. Evolution of pressure head at 20 and 40 cm depth measured by tensiometers (symbols) and estimated by the inversion procedure (lines) of the water infiltration process. The vertical bars represent the standard deviation of the measurements obtained by the four tensiometers.

Similarly, in Fig. 7 the measured (points) and estimated (lines) values of pressure heads are shown. The simulated values of pressure head well follow the measured one (r=0.950 at 20 cm and r=0.986 at 40 cm depth). Furthermore, the error bars, reporting the standard deviation of the pressure head as measured by the four tensiometers, overlap when the profile is wet (i.e. after the 6th irrigation) and separate during the wetting process.

Table 1 reports the parameters of the hydraulic functions, estimated for the first two horizons~~. Figure 7~~ and Fig. 8 reports the water retention curves and the hydraulic conductivity curves corresponding to the parameters shown in table 1 for a better comparison between TDR-based and EMI-based hydraulic properties assessment. Note in the table the high values of n and K_s for the bedrock, which indicate a high conductive porous medium. It is possible to explain this by considering that the bedrock is fractured calcareous, which, contrary to expectation, does not impede water flow.

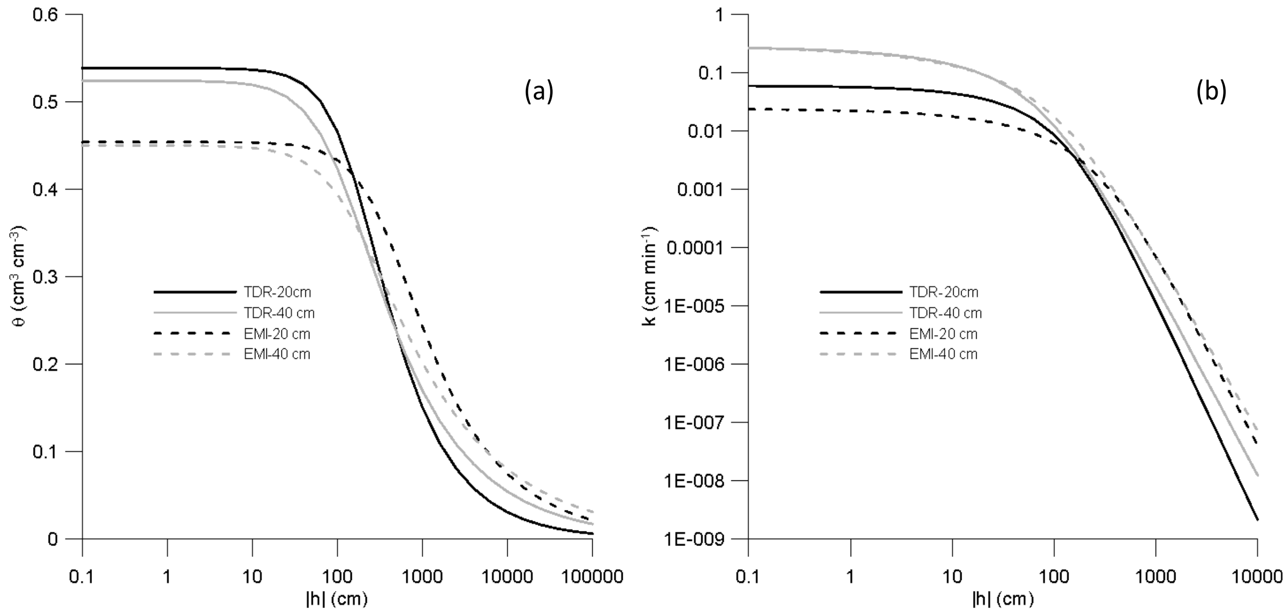
Table 1. vG-M Hydraulic parameters (Eqs. 7 and 8) and dispersivity, λ (Eq. 6) as estimated for Ap and Bw horizons, and fixed for the bedrock layer.

Soil hydraulic and transport parameters*		Ap		Bw		Bedrock
		TDR-based	EMI-based	TDR-based	EMI-based	Fixed a-priori
θ_s	[cm^3 cm^{-3}]	0.54	0.45	0.52	0.45	0.354
α	[cm^{-1}]	0.006	0.003	0.009	0.007	0.055
n	[-]	1.70	1.54	1.50	1.41	3.67
k_s	[cm min^{-1}]	0.06	0.02	0.28	0.29	19
λ	[cm]	10	12	0.5	0.8	30

* For all horizons θ_r=0 and τ=0.5.

As for water retention, the TDR and EMI water retention curves showed similar shapes but with slightly different saturated water contents. As discussed earlier, the lower saturated water content is not surprising for the EMI-based estimation due to the overall underestimation of water content. The two curves almost overlapped once scaling the EMI curve by the ratio of the saturated water contents. Obviously, this result is consistent with the underestimation of EMI-based θ distributions as shown in Fig. 6.

As for the hydraulic conductivity, TDR-based and EMI-based hydraulic conductivity curves at both 20 and 40 cm appear to almost overlap, with similar saturated hydraulic conductivity and curve shape. This result is expected because the hydraulic conductivity is mainly a function of the variation of θ and not the absolute value of θ itself. It is worth mentioning that the same top boundary flux and different water contents in the soil profile provided similar EMI-based and TDR-based hydraulic conductivity. These conditions ~~lead~~led to two different water flow processes, with simulations predicting higher water stored in the soil profile and lower downward fluxes (data not shown) when TDR-based results are compared to the EMI-based results.



~~Table 1. vG-M Hydraulic parameters (Eqs. 7 and 8) and dispersivity, λ (Eq. 6) for Ap and Bw horizons~~

~~Soil hydraulic and transport parameters~~		~~Ap~~		~~Bw~~	
		~~TDR-based~~	~~EMI-based~~	~~TDR-based~~	~~EMI-based~~
$\cancel{\theta_r}$	~~[cm^3 cm^{-3}]~~	~~0.00~~	~~0.00~~	~~0.00~~	~~0.00~~
$\cancel{\theta_s}$	~~[cm^3 cm^{-3}]~~	~~0.54~~	~~0.45~~	~~0.52~~	~~0.45~~
$\cancel{\alpha}$	~~[cm^{-1}]~~	~~0.006~~	~~0.003~~	~~0.009~~	~~0.007~~
$\cancel{n}$	~~[-]~~	~~1.70~~	~~1.54~~	~~1.50~~	~~1.41~~
$\cancel{k_s}$	~~[cm min^{-1}]~~	~~0.06~~	~~0.02~~	~~0.28~~	~~0.29~~
$\cancel{\tau}$	~~[-]~~	~~0.5~~	~~0.5~~	~~0.5~~	~~0.5~~
$\cancel{\lambda}$	~~[cm]~~	~~10~~	~~12~~	~~0.5~~	~~0.8~~

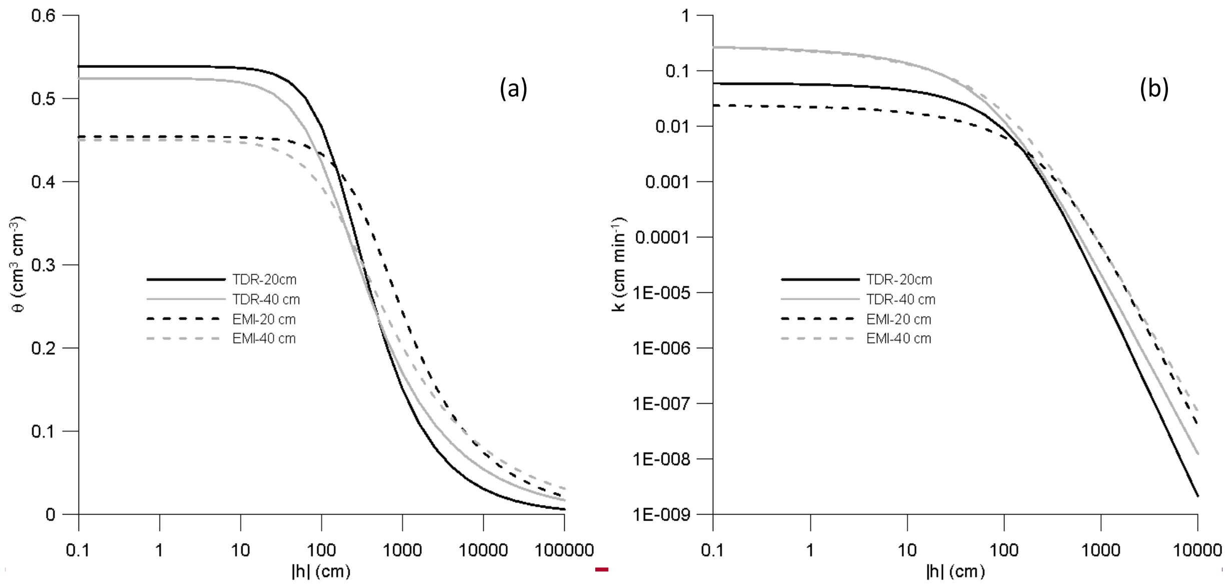


Figure ~~7~~8. Soil water retention (A) and unsaturated hydraulic conductivity (B) curves, estimated from the TDR and EMI measurements at 20 cm and 40 cm depths.

4.2. Solute Infiltration – 2nd Experiment

4.2.1. *Time-lapse σ_a data and estimation of σ_b distribution*

Figure ~~8~~9 shows the σ_a data collected during the solute infiltration experiment. Again, as for the ~~water infiltration~~1st experiment, both VCP and HCP modes show a relatively similar pattern of σ_a values with ρ32 and ρ118 being the highest and lowest respectively. HCP mode shows higher values on average compared to the VCP mode. Similarly, to the water infiltration experiment, σ_a increases consistently during the first three hours of the experiment, then it does not change significantly or consistently until the end of the experiment. Much higher ranges of σ_a variations were measured in both VCP and HCP configurations, with σ_a values ranging in 20-200 and 50-250 mS m^{-1} respectively.

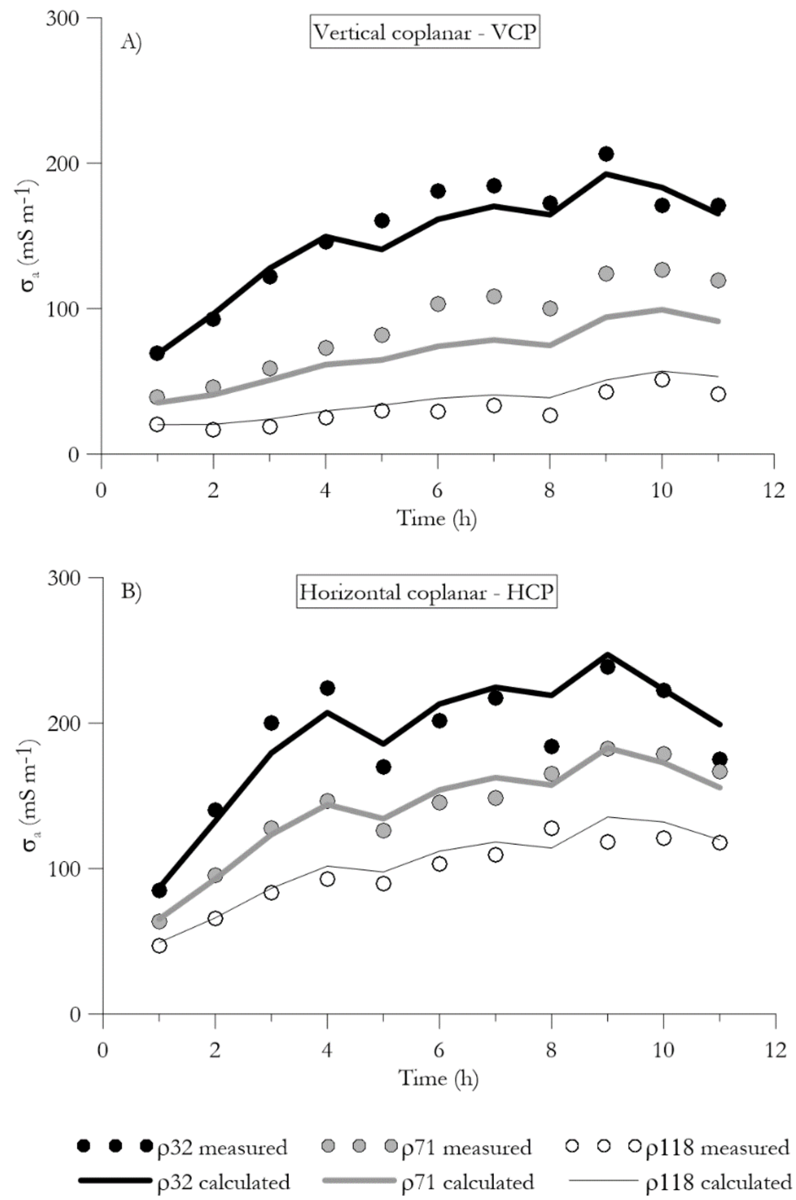
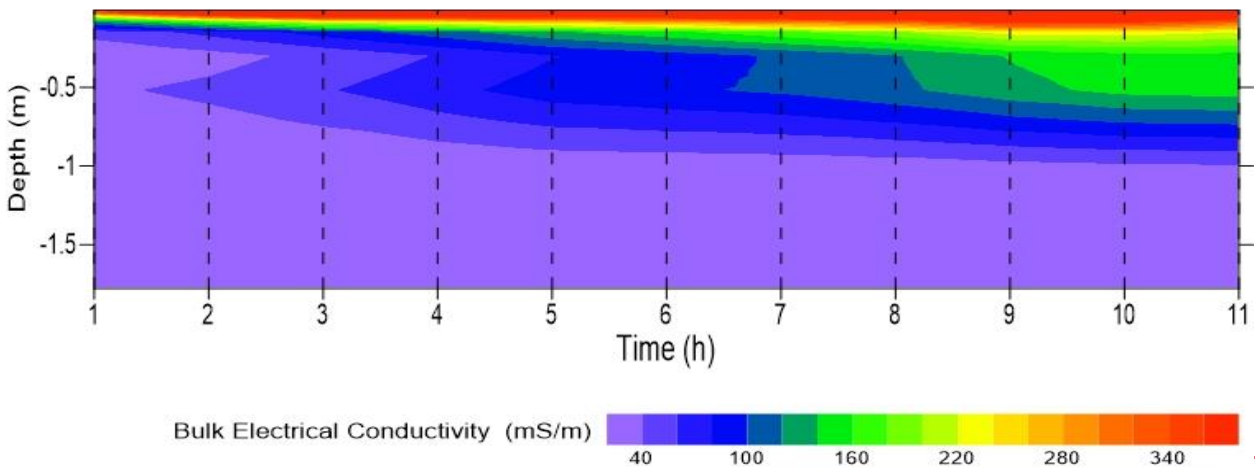


Figure 8: ~~σa values observed during the solute infiltration experiment. (A) VCP, (B) HCP. The symbols represent the measured data whereas the lines represent the values calculated after the inversion.~~

Figure~~Figure 9~~10 depicts the σ_b evolution for the ~~solute infiltration~~2nd experiment, obtained by time-lapse inversion of σ_a data. σ_a measurements and model response agrees fairly as shown in

Fig. 9, however a slight shift can be noticed in the ρ71- VCP mode between data and model response. The results show the rapid evolution of the conductive zone to the soil profile shortly after the irrigation started. In comparison to the obtained σ_b in the 1st experiment, the results reveal significantly higher soil conductivity in topsoil but a much slower evolution. The conductivity of the top layer exceeds 300 mS m^{-1} shortly after the irrigation. The higher topsoil conductivity results from injection of high-saline water (about 15 dS m^{-1}) that dramatically increases soil conductivity whereas the smaller evolution of the conductive zone is caused by significantly slower concentration propagation into the soil profile.


Depth (m)
-0.5
-1
-1.5
1
2
3
4
5
6
7
8
9
10
11
Time (h)
Bulk Electrical Conductivity (mS/m)
40
100
160
220
280
340

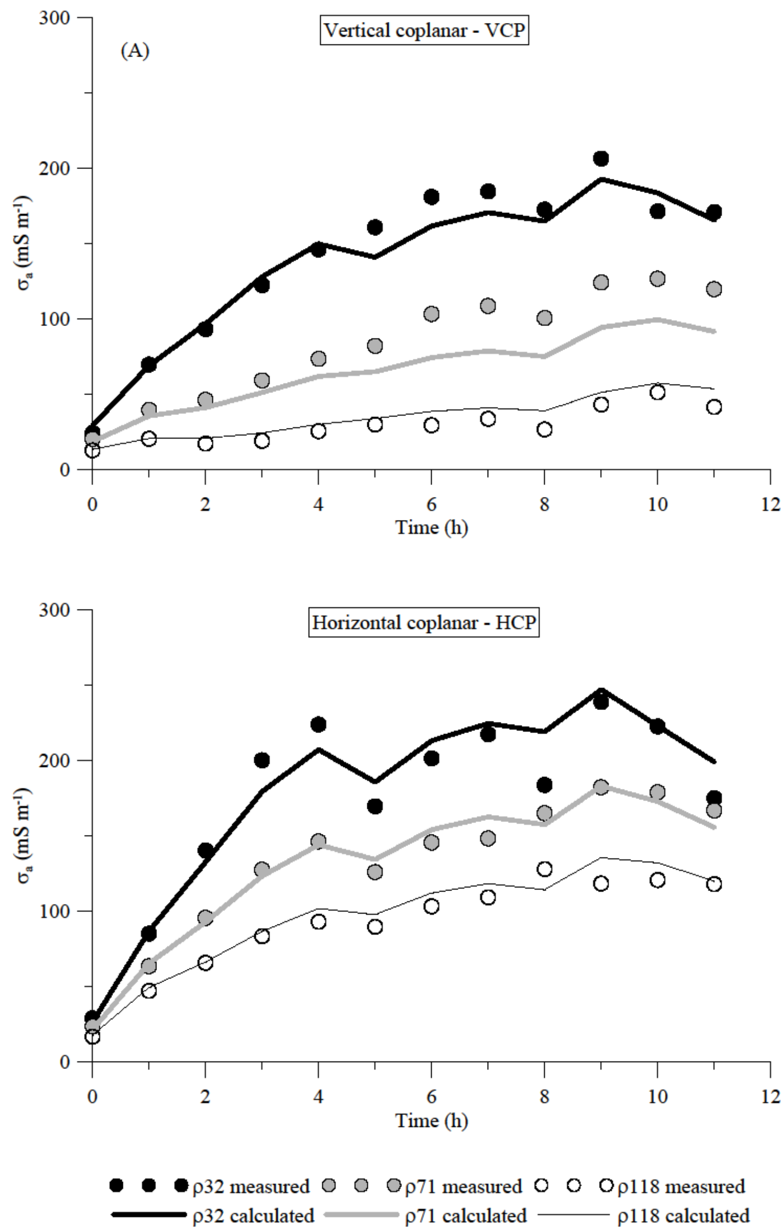


Figure 9: σ_a values observed during the solute infiltration experiment. (A) VCP, (B) HCP. The symbols represent the measured data whereas the lines represent the values calculated after the inversion.

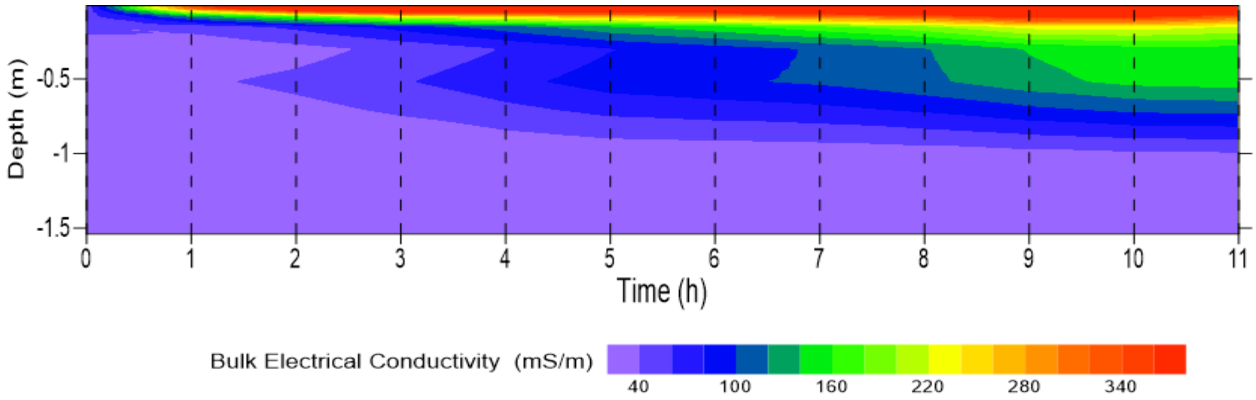


Figure 10. Time evolution of bulk electrical conductivity (σ_b) during the solute infiltration experiment.

4.2.2. *Comparison between TDR~~ measurements ~~-based and EMI-based σ_b and [Cl^-] ~~distribution~~distributions*

Figure ~~10~~11 shows the comparison between the σ_b values obtained by the TDR measurements and those obtained from the EMI inversion (Fig. ~~9~~10) during the 2nd experiment. As discussed above, this comparison is to provide an insight into the potential of the EMI survey and inversion process in monitoring a solute transport experiment into a soil profile. The comparison shows a similar time pattern of σ_b variability, but in general~~,~~ the EMI model~~ slightly~~ underestimates the σ_b obtained by TDR. The results of this comparison agree with the 1st experiment where, again, the EMI-based σ_b are lower compared to those measured by the TDR. In contrast to the 1st experiment, the differences between the two techniques and in terms of the absolute σ_b values are of minor concern. This ~~is expected to~~could be due to the larger conductivity contrast that tracer introduced into the soil profile in the 2nd experiment which became easier to detect by using the EMI sensor. On the other hand, the TDR probes show more fluctuations in σ_b measurements, especially at 20 cm. We attribute these fluctuations to the smaller volume of investigation of the TDR probes which are very sensitive to the process taking place very close to the probe and, therefore, strongly influenced by small-scale ~~local variability~~heterogeneities.

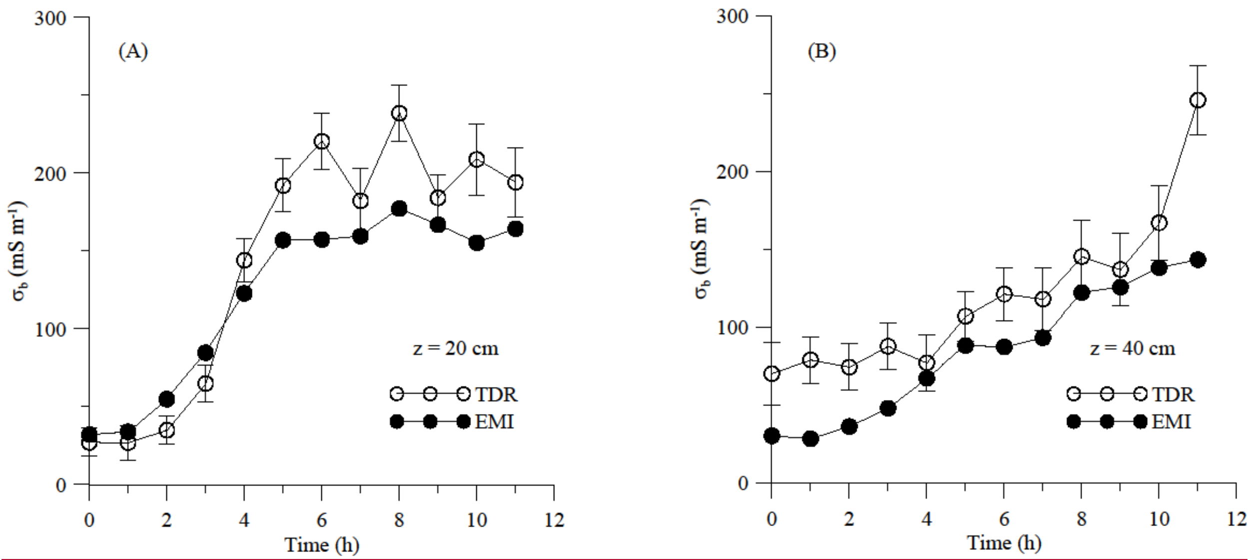
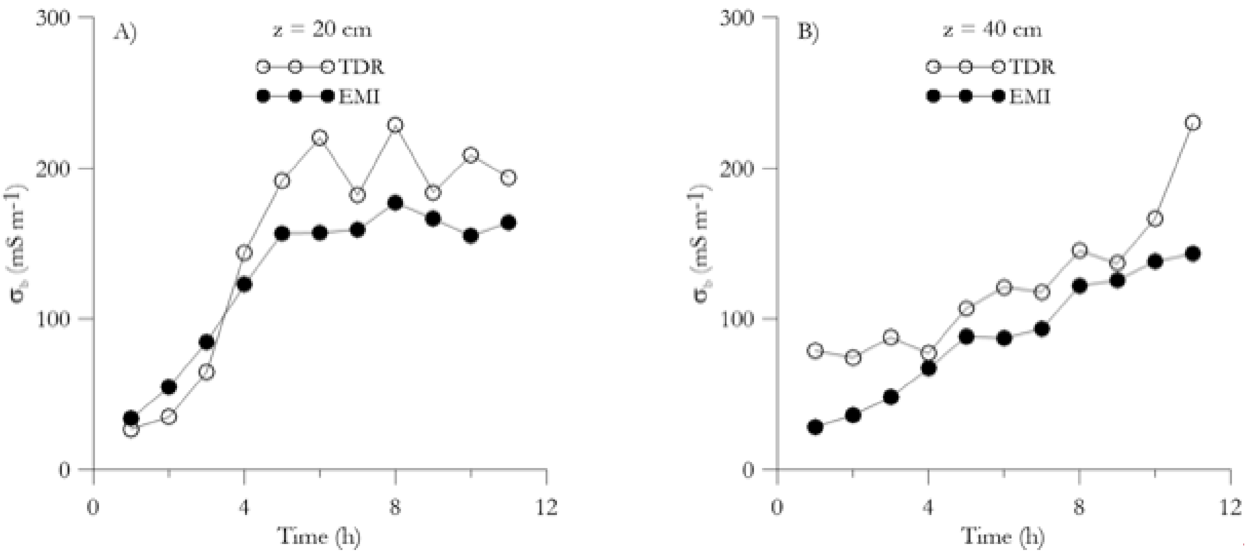
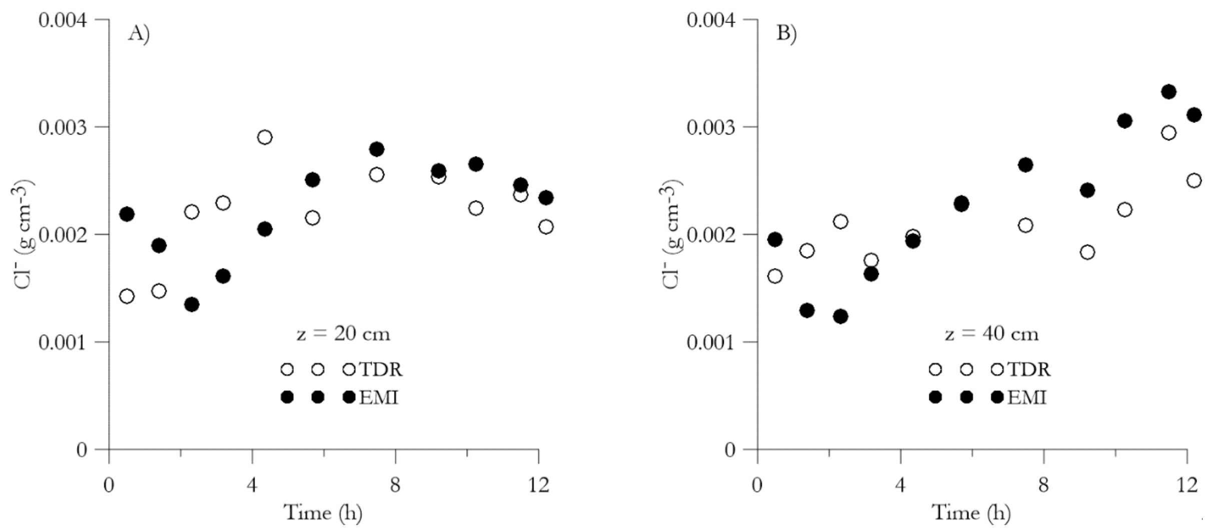


Figure 11. σ_b evolution estimated by TDR and EMI measurements at 20 cm (A) and 40 cm (B) depth.

The next step in the procedure allows us to determine the distribution of Cl^- concentrations by ~~both TDR and~~ EMI sensors~~.~~ (Sect. 4.2.3.) used for estimating the longitudinal dispersivity of the two soil layers investigated. For the sake of comparison, TDR-based $[Cl^-]$ distributions were obtained directly in the field from a direct measurement of the impedance Z along the TDR transmission line embedded in the soil. As for the EMI-based Cl^- concentrations, a forward HYDRUS-1D simulation was carried out using the EMI-based hydraulic properties obtained from the 1st experiment and reported in Table~~.~~ 1 to estimate the water content distributions in correspondence with the EMI measurement times of the 2nd experiment. These water contents, combined with the available σ_b distribution obtained from the EMI inversion, allowed us to obtain the σ_w distributions (through the θ-σ_b-σ_w calibration relationship) for both depths and, consequently, the ~~Cl^- distributions. Finally, the latter was used again for estimating the longitudinal dispersivity of the two soil layers investigated (Sect. 4.2.3.).~~[Cl^-] distributions.



~~Figure 10. σ_b evolution estimated by TDR and EMI measurements at 20 cm (a) and 40 cm (b) depth.~~



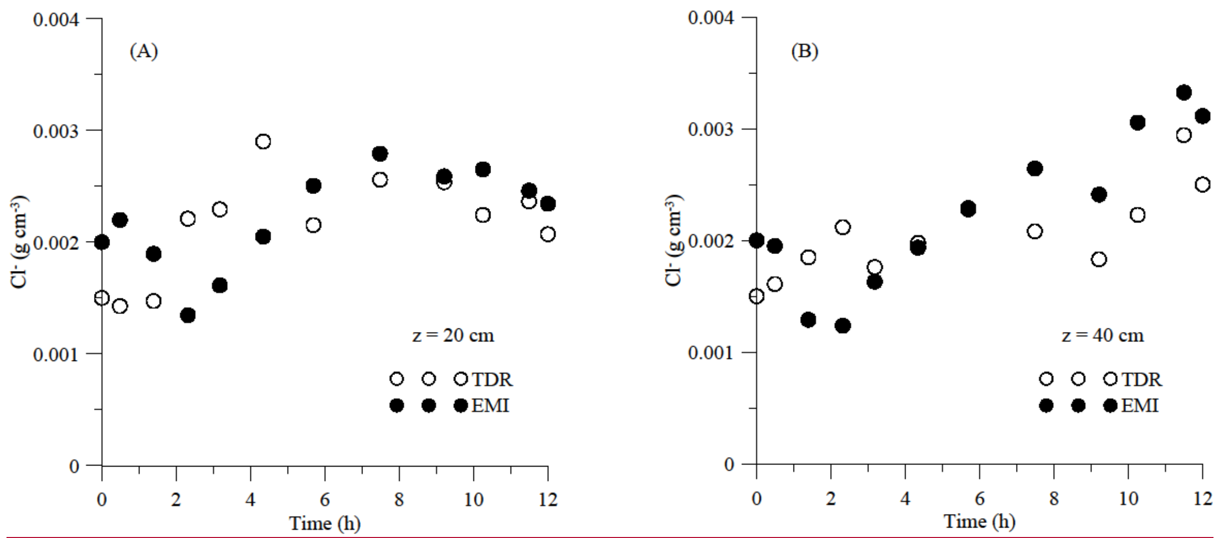


Figure ~~11.~~ 12. $[Cl^-]$ distributions inferred from EMI and TDR measurements, at 20 (A) and 40 (B) cm depth.

Figure ~~11~~12 shows the $[Cl^-]$ distributions inferred from EMI compared to the TDR measurements. The comparison suggests a good agreement between the two time~~-~~-series. The EMI-based concentrations underestimate – on average – the TDR-based ones by 4% and by 7% at 20 cm and 40 cm depths, respectively. The time evolution of the two data series reveals marked differences, as shown by the very different correlation: r = - 0.04 for the 20 cm depth and r = 0.70

for the 40 cm depth. The difference between the two data series at both depths can be mostly explained by the differences between σ_b distributions shown in Fig. ~~10~~11. Additionally, another point of difference may arise from the assumption that the water content distribution obtained from the HYDRUS-1D simulation can be used as a substitute for the water content measurements, in order to obtain [Cl$^-$] from the EMI readings. ~~However, this is different compared to the direct measurements of TDR in the 2nd experiment and therefore introduces more mismatch between [Cl$^-$] plots.~~

4.2.3. *Estimation of longitudinal dispersivity*

Inverse HYDRUS-1D simulations were conducted using concentration data provided by both the TDR and EMI results, in order to estimate the longitudinal dispersivity ~~λ~~ for both Ap and Bw horizons. The results are reported in the last row of Table 1. TDR-based and EMI-based procedures provide similar values of λ. Specifically, for the Ap horizon, the obtained values agree with those frequently found in the literature for either large columns or field-measured dispersivity (e.g~~.,~~. Vanderborght and Vereecken, 2007; Coppola et al., ~~2011b~~2011). The TDR and EMI-based estimation of dispersivity for the Bw horizon shows one order of magnitude lower values compared to the Ap horizon. These values are more consistent with values measured in the laboratory (Coppola et al., ~~2009).~~2019). For column scale (undisturbed soil monoliths with a length > 30 cm), Vanderborght and Vereecken (2007) found values in the order of 10 cm. The same values were found by Coppola et al. (2011) at both plot and transect scales. Note in the Table 1 the high value of dispersivity used for the bedrock layer. This is consistent with the nature of the bedrock, which, as mentioned, is a fractured calcareous and highly conductive rock, which may well explain high dispersivity values.

~~1. Conclusion and outlook~~

~~In this study, we carried out two sequential water infiltration and solute transport experiments and conducted time-lapse EMI surveys to examine how well this methodology can be used to i) monitor water content dynamic after irrigation and to estimate the soil hydraulic van Genuchten - Mualem parameters from the first experiment and ii) to monitor solute concentration, C, and to assess solute dispersivity.~~

5. FURTHER DISCUSSION ON THREE KEY POINTS OF THE PROPOSED APPROACH

Following, our discussion will focus on three major aspects of this research in terms of the choice of approach (uncoupled vs coupled), the suitability of EMI as a replacement for invasive sensors, and EMI-related sources of uncertainty.

5.1. Uncoupled vs Coupled approach

In hydro-geophysical studies there is an ample debate on this issue. Camporese et al., 2014, stated in their conclusions: "the relative merit of the coupled approach versus the uncoupled one cannot be assumed a priori and should be assessed case by case. As the information content of the geophysical data remains the same in both the coupled and uncoupled methods, the main difference is the approach taken in order to complement the information content and construct an ''image'' of the process". Based on the methodology proposed in this paper and the corresponding results, the following discussion aims to better clarify why we applied an uncoupled approach.

Let's refer to the vertical water infiltration process monitored by the EMI sensor during the 1st experiment and producing direct measurements of apparent electrical conductivity (σ_{a_meas}). In a coupled approach, the hydrological model is the starting point of the procedure. Guess values of hydraulic and dispersive parameters are initially fixed; thus, a hydrological simulation is carried out producing water content distributions along the soil profile, evolving over time. These water content distributions are converted to corresponding distributions of bulk electrical conductivity, σ_b, by using an empirical relationship (e.g. Binley et al., 2002). These σ_b distributions, in turn, are used as input in an EM forward modelling to produce the estimations of apparent electrical conductivity ($\sigma_{a\ est}$). In this approach, the objective function involves the residuals ($\sigma_{a\ meas}$ - $\sigma_{a\ est}$). This objective function is eventually minimised by optimising the hydraulic parameters in the hydrological model.

The main strength of this approach relies on the fact that no EMI inversion is required. Also, as discussed by Hinnell et al. (2010), the attractiveness of the coupled approach is that the hydrologic model may provide the physical context for a plausible interpretation of the geophysical measurements. Yet, this strength is counterbalanced by a weakness which is crucial in view of simplifying the experimental requirements of hydraulic characterization. Actually, an instrumental shift in EMI σ_a readings has been frequently observed when compared to other sources of measurements such as ERT data (von Hebel et al., 2014; 2019) or direct measurements of TDR (Dragonetti et al. 2018). In the context of a hydraulic parameter estimation procedure, this is a crucial point, as it means that EMI measurements do not immediately provide correct electrical conductivity distributions. Thus, the coupled approach always requires an independent dataset, obtained by different sensors (e.g. ERT, TDR, sampling) to remove the shift in the EMI σ_a readings. Such a scheme would be contrary to the spirit of our paper, which mainly aims at minimising the sensors and the data necessary for in-situ soil hydraulic characterization.

In an uncoupled approach, the geophysical model is the starting point of the procedure. As a result of geophysical inversion, the σ_b distributions are derived, which are then converted to as many distributions of water content (θ_{meas}) through an empirical relationship, determined from laboratory analysis. Afterward, the hydrological model estimates water contents (θ_{est}), and the objective function, involving the residuals (θ_{meas}-θ_{est}), is eventually minimised by optimising the hydraulic parameters. The main weakness of this approach corresponds to the strength of the coupled approach. The uncoupled approach requires geophysical inversion, involving the uncertainty source coming from the ill-posedness problem. However, the main strength of the methodology we propose in our paper – a fast in-situ non-invasive method to estimate soil hydraulic and transport properties at plot scale – does not require preliminary removal of the (unknown) shift in the EMI readings by additional field measurements with other sensors. Conversely, the shift effect is implicitly kept in the σ_b distributions, from this in the measured water content distributions and finally included in the hydrological inversion. This allowed us to reveal the effects of technical limitations of the EMI sensor including the instrumental shift in EMI σ_a readings in the water content estimations and from this in the hydraulic properties' estimation. In the 1st experiment, by comparing the EMI-based water contents to the water contents coming from TDR, it was possible to see that the shift in the EMI readings produced quasi-parallel water content evolutions, thus meaning that the EMI shift is rather stable with water content change. Related to this, in terms of hydraulic properties, the shift simply results in scaled saturated water content. This may well be explained physically by just considering the parallel behaviour of the water contents over time signifies similar water content changes over time. This is translated in similar hydraulic conductivities, which in the van Genuchten-Mualem model means similar α and n parameters, and thus water retention curves are simply scaled by the saturated water content ratio.

As an additional benefit of an uncoupled approach, it allows for the sequential estimation of parameters (from the upper to the lower horizon), which can reduce the problems of parameter correlation and uniqueness. In this work, the parameters were estimated separately for each horizon of the profile according to Abbaspour et al. (1999). This approach makes parameter estimation of multi-layered profiles more feasible and accurate, however, this cannot be done within a coupled model. If more than one layer has to be characterised, the coupled approach requires that all the parameters have to be simultaneously optimised. This is because the electrical conductivity distribution of the whole soil profile must be first simulated in order to generate required σ_{a_est} to compare to σ_{a_meas} in the objective function.

5.2. Suitability of EMI as a replacement for invasive sensors

~~We then compared the obtained results to those estimated by direct TDR and tensiometer probes measurements.~~ ~~Based on our study, the following main conclusions can be drawn:~~

~~1. The EMI-based estimation of θ can detect the similar water content evolution in time when compared to direct TDR measurements in the 1st experiment, however, a significant underestimation was observed in the EMI-based estimation of θ. This is expected when we compare σ_b evolution from the inversion of σ_a data with the TDR-based σ_b measurements. With regard to the 2nd experiment, a similar time pattern of σ_b variability can also be seen between the two approaches. However, the differences between the two approaches are of minor concern in both σ_b distribution and [Cl^-]. We attribute the smaller underestimation of σ_b distribution and [Cl^-] in the 2nd experiment to the larger conductivity contrast that tracer~~

~~introduced into the soil profile in the 2nd experiment which became easier to detect by using the EMI sensor.~~

The proposed methodology for the estimation of vG-M parameters proved to be effective for both Ap and Bw horizons. The overall EMI-based underestimation of θ did not impact the hydraulic conductivity curves significantly as the hydraulic conductivity is ~~the main~~mainly function of the variation of θ and not of its absolute value. On the other hand, this underestimation resulted in lower saturated water content which also appeared in the water retention curve. ~~The overall approach shows the high potential of the EMI sensor to replace TDR and tensiometer probes in the field-scale assessment of soil hydraulic properties. In practice, one could monitor a relatively short infiltration experiment with an EMI sensor and use the water content estimations in an inversion procedure to estimate the hydraulic properties.~~ The latter can be simply converted to more accurate water content distribution by direct measurement of the actual saturated water content at the end of the experiment using TDR probes or even by taking soil samples ~~and~~for laboratory ~~measurements~~weight.

In terms of the longitudinal dispersivity, λ, there was a very good agreement between EMI-based and TDR-based estimation for both Ap and Bw horizons. The finding results are also in very good agreement with previous in-situ and laboratory measurements~~ which suggests that the proposed methodology can be used in the field-scale assessment of the longitudinal dispersivity, λ which is indeed an important parameter in soil salinity simulations in salt-affected regions across the world. ~~. However, this method requires that the hydraulic properties of the investigated soil at the scale of concern be assessed prior to the application of this method to discriminate the contribution of water content and concentration in the EMI-based σ_b estimation.

5.3. EMI-related sources of uncertainty

The application of EMI for detailed investigation of the infiltration process has several limitations, apart from the potential instrumental of EMI sensor and the overall underestimation of water content and concentration, and requires further investigation. Resolving the wetting zone during the water injection is one source of uncertainty in this approach. The water content sharply decreases with depth in this zone to near the initial water content of the soil and causes dramatic resistivity variation. ~~In addition, a very shallow resistive bedrock exists in the study site which added to the complexity of resolving three zones with very different resistivity.~~ The limited number of σ_a measurements (total of 6) is not sufficient for recovering the sharp σ_b variability that takes place during the infiltration. In addition, a smoothness constraint was performed in the inversion process to stabilize the inversion process which further smooths the layer boundaries in this approach. ~~Measuring σ_a at different heights enables us to collect more σ_a data to better resolve changes that occur over short depth increments. More importantly, the application of a coupled Hydro-Geophysical approach (e.g. Hinnell et al. 2010; Huisman et al. 2010) can improve the estimation of the parameters by considering all of the hydrologic and geophysical data in a single inversion. In the coupled approach, geophysical data are not inverted individually and a regularization/smoothness constraint is no longer required to stabilize the geophysical component of the inverse problem.~~Resolving the shallow bedrock interface at depth and beneath a conductive zone was also very challenging. This is because the sensitivity of the EMI signals is generally very limited over the resistive zone and the condition becomes much worse when the resistive zone (bedrock) is located beneath a conductive zone (tracer): the EMI response of the subsurface is dominated by the influence of the near-surface conductive zone. In addition, five of the six depths of investigation of the CMD Mini-Explorer are limited to the first 1 m, and, as a result, a lower resolution is expected at greater depths. This resulted in an even larger underestimation of soil conductivity on top of the bedrock and an overestimation of bedrock conductivity in the close vicinity of soil. These findings from synthetic studies and modelling field data are similar to those reported in Farzamian et al. (2021) due to the similarity of the site, experiment, and the use of the same EMI sensor. Measuring σ_a at different heights or using different EMI sensor with larger number of receivers such as CMD Mini-Explorer 6L enables us to collect more σ_a data to better resolve changes that occur over short depth increments. Accordingly, using optimization techniques such as machine learning methods to select the optimal EMI configurations is also one practical way to achieve this goal, given the specific survey goals and independent knowledge of the subsurface electrical properties, as shown by van't Veen et al. (2022).

6. CONCLUSION

In this paper, we proposed a non-invasive in-situ method integrating EMI and hydrological modelling to estimate soil hydraulic and transport properties at the plot scale. For this purpose, we carried out two experiments involving 1) water infiltration and 2) solute transport over a 4 x 4 m plot. The propagation of wetting front and solute concentration along the soil profile in the plot was monitored using an EMI sensor (i.e. CMD mini-Explorer) and for the sake of procedure evaluation Time Domain Reflectometry probes and tensiometers. Time-lapse apparent electrical conductivity (σ_a) data obtained from the EMI sensor were inverted to estimate the evolution over time of the vertical distribution of the bulk electrical conductivity (σ_b). The σ_b distributions were converted to water content and solute concentration by using a standard laboratory calibration, relating σ_b to water content (θ) and soil solution electrical conductivity (σ_w).

Based on the first water infiltration experiment, the soil water retention and hydraulic conductivity curves were then obtained for two layers of the soil profile by an optimization procedure minimizing the deviations between the numerical solution of the water infiltration experiment and the estimated water contents inferred from the EMI results. EMI-based hydraulic properties were very similar in shape to those obtained by TDR and tensiometers data. This shape-similarity allowed to convert the EMI-based hydraulic properties to the TDR-based ones by simply scaling them by the ratio of the saturated water content for both the soil layers considered. This was a crucial finding in this paper and was mainly ascribed to the fact that the water content changes over time detected by the EMI closely followed those observed by TDR. These EMI-based hydraulic properties were then used as input for hydrological modelling of the second solute transport experiment. This allowed discriminating water content and solute concentration components in the EMI σ_b distributions obtained during the second experiment. These concentrations were afterward used to estimate the dispersivity based on an inversion procedure minimizing the residuals of EMI-based concentration and those simulated by the hydrological model. The reliability of the EMI-based hydraulic properties allowed us to obtain estimations of the dispersivity comparable to those obtained by the same optimization procedure applied to the TDR data.

The overall results show the high potential of the EMI sensor to replace TDR and tensiometer probes in the assessment of soil hydraulic properties. In practice, one could monitor a relatively short infiltration experiment with an EMI sensor and use the water content estimations in an inversion procedure to estimate the hydraulic properties. The underestimated water content observed in the first experiment can be converted to more accurate water content distribution by direct measurement of the actual saturated water content at the end of the experiment using TDR probes or even by taking samples and laboratory measurements.

The EMI-based estimation of longitudinal dispersivity, λ agrees well with TDR-based estimation as well as previous in-situ and laboratory measurements which suggests that the proposed methodology can be used in the assessment of this parameter which is indeed an important parameter in soil salinity simulations in salt-affected regions across the world. However, estimating λ based on only a solute infiltration test is not feasible as the temporal variability of σ_b is a function of both water content and concentration changes. We proposed the sequence of water and solute infiltration tests to discriminate the contribution of the water content and the soil solution electrical conductivity to the EMI-based σ_b.

Water irrigation and soil salinity management and thus hydrological investigations are usually field and even large-scale challenges. The EM method is a non-invasive, fast, and cost-effective technique, covering large areas in less time and at a lower cost. ~~Our study reveals the potential of this method for hydrological studies on large scales. However,~~Although our study was limited to a controlled experiment on a plot scale and a single study report, scaling up from plot scale to field scale assessment might be feasible due to the method's potential for rapid data collection. More investigations have to be conducted in this area to evaluate the potential of EMI sensors under different soil conditions and within the larger 2D and 3D investigations to further address the limitations of this methodology at ~~desired field scale. Our study also shows that we cannot use geophysical imaging alone and we need to use other in-situ data to support Hydro-Geophysical approach. Last but not least, proper estimation of soil hydraulic and hydrodispersive properties relies on an appropriate understanding of both geophysical and hydrogeological data and modeling approaches and requires close collaboration of geophysicists and hydrologists.~~different scales.

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