



# 1 Development of flexible double distribution quantile mapping for better

## 2 bias correction in precipitation of GCMs

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10

### 11 Abstract

12 The double gamma quantile mapping (DGQM) can outperform single gamma quantile 13 mapping (SGQM) for bias correction of global circulation models (GCMs) using two gamma 14 functions for two segments based on 90<sup>th</sup> quantile. However, there are two ambiguous points: 15 the 90<sup>th</sup> quantile and considering only the Gamma probability function. Therefore, this study 16 introduced a flexible dividing point,  $\delta$  (%), which can be adjusted to the regionally observed 17 values at the station and considered the combination of various probability distributions, 18 Weibull, lognormal, and Gamma, for two separate segments. The newly proposed method, 19 flexible double distribution quantile mapping (F-DDQM), was employed to correct the bias of 20 8 GCMs of Coupled Model Intercomparison Project Phase 6 (CMIP6) to correct bias at 22 21 stations in South Korea. The results clearly showed higher performance of F-DDQM than 22 DGQM and Flexible-DGQM (F-DGQM) by 25% and 5%, respectively, in root mean square 23 error. The F-DGQM also showed better performance in replicating probability distribution, 24 spatial variability and extremes of observed precipitation than other methods. This study 25 contributes to improving the bias correction method for the better projection of extreme values. 26 27 Keywords: Double gamma quantile mapping, Bias correction method, Flexible double gamma 28 quantile mapping, Flexible double distribution quantile mapping

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### 32 1. Introduction

33 Global circulation models (GCM) provide insight into the historical and possible future climate 34 variabilities and the occurrence of extreme events (Ahmed et al., 2018; Pour et al., 2018). 35 Therefore, climate studies generally use GCMs to simulate historical and future climate 36 conditions (Shiru et al., 2022; Song et al., 2022c; Iqbal et al., 2020). The reliable simulation of 37 precipitation is important for climatological and hydrological science. However, the GCMs 38 outputs have biases in the simulation due to imperfect model parameterization, inadequate 39 reference data, and incomplete knowledge (Wilby and Harris 2006; Woldemeskel et al., 2014). 40 Besides, the previous studies showed that raw GCMs can not replicate the observed climate of 41 South Korea due to its complicated geographical characteristics (Song et al., 2021a). Therefore, 42 various bias correction techniques have been used to correct the bias in GCM simulations 43 before their use for climatic studies. 44 The distribution-derived transformations, such as quantile mapping (QM), are most widely 45 used for bias corrections because of their simplicity and easy employability but higher 46 proficiency (Ringard et al., 2017; Maraun et al., 2010; Ines and Hansen, 2006; Li et al., 2010). 47 The QM shows high performance in bias correcting stationary climate variables but low

reliability for nonstationary data. Cannon et al. (2015) proposed a quantile delta mapping (QDM) method to preserve the relative change in all quantiles to address the nonstationary issue. Several methods have been developed in recent years based on QDM to enhance the bias-correction ability, including scaled distribution mapping (Switanek et al., 2017), multivariate quantile delta mapping (Cannon, 2017), and the occurrence-and intensity biasadjusting methods (Van de Velde et al., 2020).

54 The QM method replaces the quantiles of simulated data corresponding to a given probability 55 and the observed quantile corresponding to the same probability (Cannon, 2008; Piani et al., 56 2010; Cannon, 2012; Heo et al., 2019). The QM uses different probability distributions for this 57 purpose, such as Gamma, Weibull, and exponential. Besides, Ye et al. (2018) suggested the 58 three-parameter Gamma distribution. Nevertheless, QM does not always outperform other 59 bias-correction methods at all locations (Song et al., 2020). This emphasizes choosing an 60 appropriate probability distribution function (PDF) for successful bias correction. 61 In general, the gamma distribution is used in QM. The gamma quantile mapping (GQM)

62 inflates the extreme precipitations (Cloke et al., 2013, Huang et al., 2014). Several studies have

63 demonstrated that GQM underestimates the extremes which affects the design precipitation





64 (Hundecha et al., 2009; Volosciuk et al., 2017; Vrac and Naveau, 2007; Kim et al., 2018). Yang 65 et al. (2015) proposed double gamma quantile mapping (DGOM) to efficiently correct the 66 biases in extreme precipitation, which has demonstrated superior performance to single GQM. 67 Pasten-Zapata et al. (2020) showed that the bias performance of DGQM is higher than single GQM. In DGQM, the fixed value, 90<sup>th</sup> quantile, is popularly used to divide the entire data set 68 69 into two segments for two separate GQMs. However, the 90th is not always accurate in 70 estimating precipitation extremes at all locations because, theoretically, this value is not fixed. 71 In addition, the gamma distribution function is popularly used for the bias correction in 72 precipitation. However, the most appropriate distribution can be different for different regions. 73 This indicates the need for selecting appropriate probability distribution based on study 74 location to improve the performance of the bias correction method.

75 This study proposed a new flexible double distribution quantile mapping (F-DDQM) method 76 considering adjustable dividing points and two individually selected distributions for two 77 segments. Three PDFs, Weibull, lognormal, and Gamma distributions, were considered for 78 selecting appropriate PDF for two segments. The dividing point was determined based on the 79 optimal RMSE of the overall precipitation distribution. The proposed method was employed 80 for correcting the bias of 8 GCMs of Coupled Model Intercomparison Project 6 (CMIP6) at 22 81 stations in South Korea. The performance of the proposed was compared with the DGOM and 82 the Flexible DGQM (F-DGQM) using five evaluation metrics to show its efficacy. Furthermore, 83 the performance of the proposed method in correcting the bias of extreme precipitation based 84 on GEV distribution. Besides, the difference between the simulated precipitation distribution 85 and the observed distribution was compared using Jensen-Shannon (JSD) and Kullback-Leibler 86 divergence (KLD). This study contributes to improving the bias correction method for the 87 better projection of extremes.

88

### 89 2. Study area and data

## 90 2.1 Study area

South Korea, located in Asia, lies between Japan and China. The country has four distinct seasons: winter (DJF), spring (MAM), summer (JJA), and autumn (SON). South Korea has mountainous topography in more than half of its total area. Therefore, the climate varies significantly among regions due to large topographical variability. The annual average





- precipitation ranges between 1000 mm and 1600 mm. The majority of precipitation occurs insummer.
- 97 **2.2 Dataset and sources**
- 98 This study used monthly precipitation simulations of 8 GCMs of CMIP6, as listed in Table 1.
- 99 The resolutions of the GCMs range from 0.98° to 2.81°. The CMIP6 GCMs selected in this
- 100 study are frequently used in East Asia, including South Korea climate studies (China: Wu et
- 101 al., 2020; Yue et al., 2021; Lun et al., 2021, South Korea: Song et al., 2021b; Kim et al., 2021;
- 102 Chae et al., 2022). Some studies also evaluated the performance of these GCMs in South Korea
- 103 (Song et al., 2020). The CMIP6 GCMs outputs were collected from data portals (https://esgf-
- 104 <u>node.llnl.gov/search/cmip6/</u>).
- The monthly precipitation of 22 gauges was used in this study (Figure 1). They were selected
  from 96 gauges available in South Korea, considering the availability of monthly rainfall
- 107 records without missing data for the historical period (1970-2014). The selected stations are
- 108 exposed to several hydrological disasters, such as floods and heavy snow. Therefore, the high
- 109 reproducibility of precipitation can improve the accuracy of precipitation projections when
- 110 analyzing disasters due to precipitation changes in South Korea.



111

112 Figure 1. Location of the selected stations in South Korea.

113





114

### 115 Table 1. Information about GCMs used in this study.

		Resolution	
Institute	Models	(Longitude ×	
		Latitude)	
Commonwealth Scientific and Industrial			
Research Organisation, and Bureau of	ACCESS-ESM1-5	$1.25^{\circ} \times 1.875^{\circ}$	
Meteorology			
Canadian Earth System Model version 5,			
Canadian Centre for Climate Modelling and	CanESM5	$2.81^\circ  imes 2.81^\circ$	
Analysis (Canada			
NASA Goddard Institute for Space Studies	GISS-E2-1-G	$2.0^{\circ} \times 2.5^{\circ}$	
Institute for Numerical Mathematics, Russian	INIM CM4 8	1 5° × 2 0°	
Academy of Science, (Russia)	111111-CIV14-0	1.5* * 2.0*	
Institut Pierre Simon Laplace	IPSL-CM6A-LR	$2.5^{\circ} \times 1.26^{\circ}$	
Max Planck Institute for Meteorology (MPI-M)	MDI ESM1 2 I P	1 125° × 1 12°	
(Germany)	IVII I-LOIVII-Z-LK	1.123 ^ 1.12	
Meteorological Research Institute (Japan)	MRI-ESM2-0	1.125° × 1.125°	
Norwegian Climate Centre (Norway)	NorESM2-MM	$1.25^{\circ} \times 0.9375^{\circ}$	

116

## 117 3. Methodology

### 118 **3.1 Inverse distance weighted method**

119 The CMIP6 GCMs outputs are in the form of a grid with fixed resolution. The geographical interpolation methods are used to remove the spatial difference between the GCM simulation 120 121 and the observed data. The inverse distance weighted (IDW) method has been widely used for 122 geographical interpolation (Longley et al., 2005). The concept of IDW is based on Tobler's first 123 law, in which data from the nearby point are more relevant than distant point (Tobler, 1970). 124 Equation 1 is used to estimate the CMIP6 GCM precipitation at the observed locations from 125 their values in nearby locations. Equation 2 computes the interpolation weight for the distance 126 between the grid and the interpolation points.

127 
$$P_i = \sum_{k=1}^{N} \frac{w_s(x)}{\sum_{k=1}^{N} w_s(x)} P_i(x_s)$$
(1)





128 
$$w_s(\mathbf{x}) = \frac{1}{b_{(x,x_0)}^c}$$
 (2)  
where  $P_i$  is the precipitation in the interpolation area,  $P_i(x_s)$  is the GCM precipitation at  
grids surrounding the observed location,  $w_s$  is the interpolation weight, and  $D_{(x,x_s)}$  is the  
131 distance between the interpolation and grid point. This study used the Shepard method to  
132 estimate the interpolation weight, and the pattern is interpolated narrowly  $(0 < D^c < 1)$  or  
133 widely  $(D^c > 1)$  depending on  $D^c$ . This study used 50 grids close to 22 stations for spatial  
134 downscaling.  
135  
3.2 Single & Double gamma quantile mapping  
137 Distribution-derive transformations of QM are bias-correction techniques depending on  
138 distribution parameters. These methods use distribution functions, such as Gamma, Lognormal,  
139 and Weibull, to reduce the differences between the observed and GCM raw data (Piani et al.,  
140 2010). The single gamma quantile mapping (SGQM) is most widely used to reduce the  
141 differences between GCM outputs and observed data using their cumulative distribution  
142 function (CDF), as shown in Equation 3.  
143  
144  $P_o(t) = F_g^{-1}(F_g(P_m(t), \alpha_m, \beta_m), \alpha_o, \beta_o)$  (3)  
145  
146 where  $P_o(t)$  denotes the bias-corrected monthly precipitation,  $P_m(t)$  represents GCM raw  
147 data,  $F_g^{-1}$  is the inverse CDF of the observed data to which the gamma function is applied,  
148 and  $F_g$  is the CDF of the GCM outputs.  $\alpha_o$ ,  $\alpha_m$ ,  $\beta_o$  and  $\beta_m$  represent shape and scale  
149 parameters of observed and GCM simulation, respectively.  
150 The SGQM tends to be more inflated than the observed data. Therefore, some studies used  
151 double gamma quantile mapping (DGQM) for bias correction. DGQM is similar in  
152 methodology to SGQM, with the difference being the division of the simulated precipitation

154 determining the criterion of  $\delta$  in most studies (Pastén-Zapata et al., 2020; Meresa et al., 2021).

distribution into two segments by  $\delta$ . However, the bias correction is performed by randomly

- 155 Therefore, this study proposed a double distribution bias correction that can flexibly use  $\delta$ .
- 156

153

### 157 **3.3 Flexible double gamma quantile** mapping (F-DGQM)





- 158 The F-DGQM is similar to the methodology of DGQM but uses  $\delta$  to separate the two segments
- 159 flexibly. Figure 2 shows the concept of F-DGQM. The upper  $\delta$ , representing quantiles between
- 160 80% and 95%, is selected based on the optimal root mean square error (RMSE). The upper  $\delta$
- 161 is determine based on optimal RMSE of the distributions of quantiles among 80–95%.
- 162



163

164 Figure 2. Concept of flexible double gamma quantile mapping (F-DGQM) based on optimal

- 165 RMSE
- 166

#### 167 **3.4 Flexible double distribution quantile mapping**

168 The gamma distribution may not be appropriate for all observed data. Indeed, some studies169 have argued that other distributions perform better than Gamma distribution (Gudmundsson et

- 170 al., 2012). Therefore, this study proposed determining the appropriate distribution for upper  $\delta$
- 171 and lower  $\delta$  based on the RMSE from three distribution functions, Weibull, Lognormal, and
- 172 Gamma. The F-DDQM selects the optimal distribution for each segment after determining  $\delta$
- 173 based on the optimal RMSE, as shown in Figure 3.







175 Figure 3. Concept of flexible double distribution quantile mapping (F-DDQM) based on

- 176 RMSE
- 177

174

178 The proposed method can be used for bias correction of various climate variables. However,

179 since the natural variability of precipitation is higher than the other climate variables, this study

180 considered only precipitation bias correction (Deser et al., 2012; Cannon et al., 2015).

181

### 182 **3.5 Evaluation metrics**

183 This study used five evaluation metrics to evaluate bias corrected monthly precipitation 184 performance using four distribution quantile mapping methods. The evaluation metrics used 185 are as follows: normalized root mean square error (NRMSE), the percent bias (Pbias), the 186 Nash-Sutcliffe efficiency (NSE) (Nash and Sutcliffe, 1970), a modified index of agreement 187 (MD) (Willmott, 2013), and the Kling-Gupta efficiency (KGE) (Gupta et al., 2009). The 188 evaluation metrics in this study are presented in Equations 4-8. In all equations,  $X_s$  is the GCM 189 outputs,  $X_o$  is the observed data.

190 NRMSE = 
$$\frac{\sqrt{\frac{1}{n}\sum_{i=1}^{n}(X_{s}-X_{o})^{2}}}{\overline{X_{o}}}$$
 (4)

191 The NRMSE is the result after removing the scale of RMSE. The values closer to 0 indicate192 higher accuracy.

193 Pbias = 
$$\frac{\sum_{i=1}^{n} (X_0 - X_s)}{\sum_{i=1}^{n} X_0}$$
 (5)





- 194 Pbias represents the bias in the GCM and observation values. The tendency of overestimation
- 195 indicated positive value and vice versa.

196 NSE = 
$$1 - \frac{\sum_{i=1}^{n} (X_{s} - X_{o})^{2}}{\sum_{i=1}^{n} (X_{o} - \overline{X}_{o})^{2}}$$
 (6)

- 197 NSE determines the relative magnitude of the residual variance in GCM simulations compared
- 198 to the variance in the station observation (Nash and Sutcliffe, 1970).

199 
$$MD = \frac{[1 - (\sum_{i=1}^{n} abs(X_0 - X_s))]}{(\sum_{i=1}^{n} abs(X_s - \overline{X_0})) + (abs(X_0 - \overline{X_0}))}$$
(7)

MD estimates the sum and proportional difference between the observed and GCM data (Willmott, 2013).

202 
$$KGE = 1 - \sqrt{(1-r)^2 + (1-\alpha)^2(1-\beta)^2}$$
 (8)

KGE is an integrated statistical metric that merges correlations, biases, and variability to assess
associations and errors in the mean and variability of the observed and GCM simulated data.
The optimal value is close to 1 (Gupta et al., 2009).

206

## 207 3.6 Generalized extreme value

The L-moment better estimates the GEV parameters than the maximum likelihood estimation,
particularly for small data samples (Hosking 1985). Since this study used 45 years of monthly
precipitation, the GEV parameters were estimated using the L-moment method (Hosking 1990).
The CDF of the GEV distribution is given in Equation 9.

212 
$$G(x) = \left\{ -\left[1 - \frac{k(x-\xi)}{a}\right]^{1/k} \right\}$$
(9)

where  $\xi$ , *a*, *k* are the location, scale, and shape parameters, respectively. The GEV combines three probability distributions: Fréchet, Weibull, and Gumbel, with different representations of the distributions depending on the value of the location ( $\xi < 0$  is a Weibull;  $\xi = 0$  is a Gumbel, and  $\xi > 0$  is a Frechet). The GEV corresponds to type I, II, and III, respectively, when the *a* equals 0, greater than 0, and lower than 0 (Coles et al., 2001). This study compared the extreme values of monthly precipitations bias-corrected using four QM methods considering GEV distribution.

221 3.7 Kullback–Leibler & Jensen-Shannon divergence





- 222 KLD estimates the difference between PDFs based on their relative entropy (Kullback and
- 223 Leibler 1951). In other words, it estimates how well the model's simulation values preserve the
- amount of information about the observed data. Equation 10 represents the expected value ofthe amount of information loss using KLD.

226 
$$KLD(P||Q) = \int_{-\infty}^{\infty} P(x) \log \frac{P(x)}{Q(x)} dx$$
(10)

- where P(x) and Q(x) are the continuous PDF of observed data and model simulation, respectively, depending on distribution type. KLD is not symmetric for different probability distributions.
- JSD estimates the symmetric relationship and the distance between PDFs (Lin, 1991), as shownin Equation 11.

232 
$$JSD(P,Q) = \frac{1}{2}D_{KL}(P||\frac{P+Q}{2}) + \frac{1}{2}D_{KL}(Q||\frac{P+Q}{2})$$
 (11)

This study compared the difference between the PDFs of observed and the bias-correctedprecipitation using KLD and JSD.

235

### 236 **4. Results**

## 237 **4.1 Flexible double gamma quantile mapping**

### 238 4.1.1 Estimation results for $\delta$

In this study, the  $\delta$  of DGQM was determined according to optimum RMSE. Table S1 presents the estimated  $\delta$  of F-DGQM based on the RMSE at 22 stations. Overall, most GCMs showed the highest RMSE at the 80<sup>th</sup> quantile at 22 stations, except IPSL-CM6A-LR and MRI-ESM2.0. IPSL-CM6A-LR showed the highest RMSE at 86<sup>th</sup> quantile and MRI-ESM2-0 at 93<sup>rd</sup> quantile at 22 stations. This study compared the RMSE of 8 CMIP6 GCMs depending on the change in  $\delta$ . Figure 4 presents the calculated RMSE according to  $\delta$  at Seoul station. The most selected quantile was the 80th, followed by the 90<sup>th</sup> at the Seoul station.







248 Figure 4. Comparison of RMSE of 8 CMIP6 GCMs depending on  $\delta$  at the Seoul station.

249

247

250 The  $\delta$  selected at 22 stations is presented using a heatmap in Figure 5. Overall, the selected  $\delta$ 251 was 80<sup>th</sup> quantile at most stations, followed by 95<sup>th</sup> quantile. The lowest selected quantiles were 252 between 87<sup>th</sup> and 89<sup>th</sup>. Therefore, the appropriate  $\delta$  was selected at both extremes of each 253 quantile, whereas the 89-91% for  $\delta$  was the opposite.







254

Figure 5. The heatmap shows the number of selected  $\delta$  for F-DGQM depending on RMSE at 22 stations

257

## 258 4.1.2 Evaluation of results

259 This study compared the performance of F-DGQM with SGQM and DGQM. Figure 6 presents 260 the methods' performances at 22 gages using box plots. The NRMSE for F-DGQM was the 261 lowest (median < 0.1) among the QM methods, and the median NRMSE of F-DGQM was 262 calculated below 0.1. The medians of F-DGQM Pbias was closer to the optimal value, whereas 263 the SGQM overestimated and DGQM underestimated the observation. The median NSE of F-264 DGQM was higher than those for SGQM and DGQM. Besides, the median MD and KGE of 265 F-DGQM were close to the optimum value. The results indicate better performance of F-266 DGQM than DGQM in all evaluation metrics.







268 Figure 6. Performance of three QM methods in correcting GCM simulated monthly

269 precipitation bais at 22 stations in South Korea.

270

267

271 Figure 7 shows the performance of PDFs and CDFs of bias-corrected precipitations of SGQM,

272 DGQM, and F-DGQM at 22 stations based on KLD and JSD. Overall, the PDFs and CDFs of

273 F-DGQM were most similar to the observation than the other two methods. In contrast, the

274 PDFs and CDFs of SGQM showed the largest difference from the observation. The results

275 indicate the better reproducibility of observed precipitation PDF and CDF using F-DGQM.







276

Figure 7. Comparison of bias-corrected monthly precipitation of 8 CMIP6 GCMs at 22

278 stations using three QM methods based on Kullback-Leibler and Jensen-Shannon

divergence.

280

The scatter plots of the bias-corrected monthly precipitation using the methods against observations are shown in Figure 8. Overall, the scatter plots showed a remarkable improvement in F-DGQM bias-corrected precipitation in association with observation. The SGQM tended to inflate or underestimate observation significantly. Although the difference between F-DGQM and DGQM was not high, the F-DGQM showed a more improvement in precipitation reproducibility.









Figure 8. Performance comparison of three quantile mapping methods in correcting bias in 8
CMIP6 GCMs at 22 stations based on scatter plot

290

## 291 4.1.3 Comparison at each station

Figure 9 presents the average RMSE in bias-corrected precipitation of 8 GCMs at 22 stations using different QM methods. The figure shows that the performance of F-DGQM was higher than the other two methods at all stations. DGQM showed a better performance than SGQM but lower than F-DGQM at all locations.









Figure 9. The RMSE in bias-corrected monthly precipitation of 8 CMIP6 GCMs using three quantile mapping methods at 22 stations.

299

This study also compared the performance improvement using other five statistical metrics listed in the method section and presented in Table S2. Overall, the performance of F-DGQM was higher than DGQM and SGQM in all metrics. F-DGQM showed a higher improvement in bias-corrected precipitation at Jinju, where the precipitation is relatively low (Average improvement 55%). Furthermore, the average improvement using F-DGQM compared to DGQM in all stations was 16%. The results indicate that a flexible quantile division location significantly improves the bias correction performance.

307

## 308 4.2 Flexible double distribution quantile mapping

### 309 4.2.1 Results of $\delta$ and distribution selection

The performance of the QM method by selecting the appropriate distribution fitted on two parts divided based on optimum  $\delta$  is presented in this section. The best distributions determined for above and below of the selected  $\delta$  at 22 stations are provided in Table S3. Overall, the Weibull exhibited the best performance for below  $\delta$  for GCMs and observed precipitation (110 times), followed by Gamma (61 times) and Lognormal (5 times). The Weibull was also the best in fitting GCMs and observed data above  $\delta$  (112 times), followed by Gamma (59 times) and Lognormal (5 times).





317 Table S4 presents the  $\delta$  of F-DDQM based on the RMSE results at 22 stations. Figure 10 318 presents the number of  $\delta$  selected at 22 stations based on the RMSE using a heatmap. The most selected  $\delta$  for CMIP6 GCMs was 80<sup>th</sup> and 95<sup>th</sup> quantiles. However, most GCMs had closer to 319 320 optimum RMSE for higher quantiles (88%-95%) than the lower quantiles (80%-87%). For 321 example, the most δ of GISS-E2-1-G, INM-CM4-8, IPSL-CM6A-LR, and MRI-ESM2-0 was 322 95th quantile. On the other hand, the most  $\delta$  of ACCESS-ESM1-5, CanESM5, MPI-ESM1-2-LR, and NorESM2-MM was 80<sup>th</sup> quantile. Therefore, the 80<sup>th</sup> and 95<sup>th</sup> quantiles were the best 323 324  $\delta$  for the GCMs, whereas the  $89^{th}$  quantile was never chosen.



325

326 Figure 10. The heatmap shows the number of selected  $\delta$  depending on RMSE

327

### 328 4.2.2 Evaluation results for double distribution quantile mapping

- 329 The precipitation of 8 CMIP6 GCMs was bias-corrected at 22 stations using F-DDQM with
- 330 selected  $\delta$  and distributions.
- 331 The performance of the bias-corrected precipitation using F-DDQM, F-DGQM and DGQM at
- 332 22 stations based on five evaluation metrics is presented in Figure 11. The results showed that
- 333 the median NRMSE of bias-corrected precipitation using F-DDQM was higher than the other





- 334 two methods. The Pbias showed that DGQM and F-DGQM underestimated, whereas the F-
- 335 DDQM overestimated the monthly precipitation. The median Pbias of F-DDQM and F-DGQM
- 336 was closer to the optimal value. The median NSE of F-DDQM was closer to the optimal value
- than that for F-DGQM and DGQM. In addition, the median MD of F-DDQM was the highest.
- 338 The median KGE of F-DDQM was also slightly higher than F-DGQM.





<sup>341</sup> simulated monthly precipitation bais at 22 stations based on five statistical metrics.

342

339

343 The performance of the methods based on JSD and KLD is shown in Figure 12. Both metrics

344 showed that PDF and CDF of F-DDQM corrected precipitation were closer to the observation.

345 F-DGQM performed better than DGQM but much lower than F-DDQM.

346







347

Figure 12. Comparison of DGQM, F-DGQM, and F-DDQM methods in bias correcting
monthly precipitation of 8 CMIP6 GCMs at 22 stations using Kullback–Leibler and JensenShannon divergence.

351

## 352 4.2.3 Comparison of performance at each station

- Figure 13 presents the average RMSE in bias-corrected precipitation of 8 CMIP6 GCMs at 22 stations. The figure shows lower RMSE for F-DDQM at all stations than the other two methods. The performance of the methods based on other statistical metrics is presented in Table S6. The results showed average improvement using F-DDQM was 1.1% and 3.3% in RMSE compared to F-DGQM and DGQM. These results indicate an improvement in precipitation bias correction using F-DDQM at different locations having diverse climates.
- 359







360

Figure 13. The RMSE in bias-corrected monthly precipitation of 8 CMIP6 GCMs at the 22
stations using F-DGQM, F-DDQM, and DGQM.

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Figure 14 shows the relative performance of F-DGQM and F-DDQM in correcting precipitation using scatter plots. Overall, F-DDQM improved precipitation performance than F-DGQM. The correlation between F-DDQM corrected and observed precipitation was slightly higher than that obtained for F-DGQM for all GCMs.









369 Figure 14. Performance comparison of F-DGQM, F-DDQM, and DGQM methods in

370 correcting bias in 8 CMIP6 GCMs at 22 stations based on scatter plot

371

## 372 **4.3 Performance comparison based spatial precipitation indices**

The performance of bais corrected precipitation using F-DGQM, F-DDQM, DGQM and SGQM in simulating the spatial distribution of observed maximum precipitation, median precipitation and standard deviation of precipitation are presented in Figure 15 (a), (b), and (c), respectively. Overall, the spatial distribution of maximum precipitation estimated using F-DDQM was closer to the observation. The maximum precipitation obtained using SGQM





tended to inflate in the northwest, where extreme precipitation occurs more, whereas it underestimated maximum precipitation in the south. The error in DGQM maximum precipitation was narrower than SGQM, but it overestimated maximum precipitation in some regions. F-DGQM captured maximum precipitation in the central region similar to DGQM. In contrast, F-DDQM showed the smallest difference with the observation in most regions and the highest performance.

The precipitation median estimated by SGQM was higher than the observation in the western region. DGQM estimated a smaller precipitation median than SGQM in most regions, whereas overestimated it in the southwest region. F-DGQM showed a negligible difference with observed median precipitation (less than 5 mm in most regions). However, the smallest difference with the observed median precipitation was obtained using F-DDQM.

389 The difference in precipitation standard deviation between SGQM corrected and 390 observed precipitation was the largest (above 5 mm in most regions) compared to other 391 methods. The DGQM showed a smaller difference than SGQM, but it overestimated the 392 standard deviation in some regions. In contrast, F-DGQM showed the lowest difference with 393 observed precipitation standard deviation in most regions (the difference was close to zero). 394 These results indicated better performance of F-DGQM and F-DDQM in caption spatial 395 distribution of precipitation indices. However, F-DDQM showed slightly better performance 396 than F-DGQM.













24







- 403 (c) Standard Deviation
- 404 Figure 15. Performance of different bias correction methods in reconstructing the spatial
- 405 distribution of three precipitation metrics: (a) maximum precipitation; (b) median
- 406 precipitation; and (c) standard deviation of precipitation for the base period 1970-2014 407

408 The average error in estimating the spatial distribution of three precipitation metrics by the bias 409 correction methods is presented in Table 2. Overall, F-DDQM showed the lowest variance with 410 respect to observation in all metrics. The difference between the F-DDQM corrected and 411 observations maximum precipitation was 50.6 mm, median precipitation was 4.5 mm, and 412 standard deviation was 1.2, which were the lowest among all methods.

413

414 Table 2. Errors (mm) in estimating observed precipitation metrics using different bias 415 correction methods.

Metrics SGQM	DGQM	F-DGQM	F-DDQM
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SD	10.7	2.2	1.3	1.2
Max	151.2	82.7	70.2	50.6
Median	8.2	6.1	4.9	4.5

416

### 417 **4.4 Generalized extreme value of the bias corrected precipitation**

418 This study compared the extreme values of historical bias-corrected precipitation four QM 419 methods based on GEV distribution. The precipitation for above the 95th percentiles are 420 presented in Figure 16. L-moment was used to estimate the GEV parameters of bias-corrected 421 GCMs using four QM methods. Overall, the PDF of F-DDQM was the most similar to the 422 observed PDF. Although the extreme precipitation of MRI-ESM2-0 was slightly higher than 423 the observed, most GCMs showed similar extreme precipitation to the observed. F-DGQM 424 estimated extreme precipitation was closer to observed than DGQM and SGQM, but its 425 performance was lower than F-DDQM. The results indicate F-DDQM is the best in correcting 426 bias in precipitation extremes.





429 stations estimated using four QM methods.





### 430

- 431 The differences between the observed and bias-corrected precipitation GEV distributions were
- 432 estimated using KLD and JSD. The obtained results for all the GCMs are presented using
- 433 boxplots Figure 17. Overall, the GEV distribution of the F-DDQM for both divergences was
- 434 the closest to the observed in PDF and CDF, followed by F-DGQM, DGQM and SGQM. The
- 435 again proves the capability of F-DDQM in correcting bias in precipitation extremes.



Figure 17. Differences in GEV distribution between the observed and bias-corrected GCMs'precipitation at 22 stations using KLD and JSD.

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### 440 5. Discussion

441 Although the OM algorithms can effectively eliminate biases and errors in GCM simulations, 442 the performance is dependent on the QM method, such as non-parametric transformation, parametric transformation, and distribution derived transformations (Song et al., 2020). The 443 444 distribution-derived transformation was developed by combining distribution functions like 445 Bernoulli-Gamma. Various functions have been applied to improve its performance 446 (Gudmundsson et al., 2012; Cannon et al., 2015). Nevertheless, the general QM can artificially 447 impair trends in future projections (Cannon et al., 2015). Therefore, improving the GCM's 448 extreme precipitation bias correction method is important. DGQM was the proposed method 449 to solve this problem. However, there is no clear reason for determining 90% or 95% (Pastén-450 Zapata et al., 2020; Yang et al., 2010) as the dividing point. Furthermore, the gamma 451 probability function is generally used to fit two divided segments, but it is not the most 452 appropriate probability distribution function at all locations. Therefore, this study presented F-453 DGQM and F-DDQM that determines  $\delta$  according to optimum RMSE, considering two 454 independent probability distributions for two divided segments.

455 The  $\delta$  of F-DGQM was the 80<sup>th</sup> quantile in this study based on the RMSE at most 456 stations. Conversely, the second-highest performing  $\delta$  was the 95<sup>th</sup> quantile. It means that the 457 suitable  $\delta$  is different at different stations depending on the scale and shape of the GCM 458 precipitation distribution. Therefore, the determination of  $\delta$  can affect the difference between 459 extreme and mean precipitation. Therefore, it was reasonable to use RMSE to determine double 460 distribution.

461 The bias correction performance of F-DGQM showed a large improvement, as shown 462 in Figure 6, in all evaluation metrics compared to DGQM and SGQM. The PDFs and CDFs of 463 the bias-corrected precipitation using three QM methods were compared with the observed 464 PDF and CDF using JSD and KLD. F-DGQM showed better performances than DGQM and 465 SGQM. However, only  $\delta$  determination does not guarantee the superior performance of F-466 DGQM than other methods. The Gamma distribution may not show the best performance at all 467 stations and all GCMs. The combination of different distributions proposed by Gudmundsson 468 et al. (2012) can improve the bias correction performance over a single distribution. Therefore, 469 this study proposed F-DDQM, considering suitable distributions for two individual segments. 470 The performance of F-DDQM showed better performance than F-DGWM because of

471 considering three probability distributions for two individual segments. The most selected  $\delta$  in





472 F-DDQM showed that the high percentiles (88%-95%) were selected more than the low 473 percentiles (80%-87%). Therefore, it can be remarked that a suitable  $\delta$  can be selected at a 474 relatively high quantile. Furthermore, the Weibull distribution performed best for below  $\delta$ . 475 Furthermore, Weibull performed best for above  $\delta$ , followed by Gamma. These results prove 476 that the Lognormal PDF is not proper in analyzing the monthly precipitation of South Korea. 477 The performance of F-DDQM was higher than F-DGQM in all evaluation metrics. Furthermore, 478 the performance improvement using F-DDQM was more than F-DGQM at all stations.

479 This study also presented the spatial differences between the observed and the bias-480 corrected monthly precipitation metrics (Figure 15). Overall, the performance of F-DDQM was 481 the highest. The F-DDQM estimated spatial distribution of all three metrics very similar to 482 observation at all regions of South Korea. On the other hand, SGQM overestimated the 483 maximum precipitation, and thus, the corrected precipitation tends to be inflated for the most 484 frequent values (Cannon et al. al., 2015; Teng et al., 2015; Yang et al., 2010). The results clearly 485 showed that the F-DGQM and F-DDQM improved the performance of the existing versions of 486 QM bias correction methods. The performance of F-DDQM is the best among all. Furthermore, 487 uncertainty in F-DDQM corrected bias is relatively low.

488 The GEV distribution of F-DDGM precipitation was also more similar to the observed 489 precipitation compared to the others. The JSD and KLD also showed that F-DDGM corrected 490 precipitation PDF and CDF are closest to the observed PDF and CDF at all stations. The results 491 indicate the higher performance of F-DDQM in various aspects.

492

## 493 6. Conclusions

494 In this study, two new bias correction methods were proposed to improve the performance of 495 double gamma quantile mapping, F-DGQM and F-DDQM. F-DGQM determines  $\delta$  based on 496 RMSE to distinguish two segments of the gamma distribution for bias correction. F-DDQM 497 uses the optimal probability distribution for two segments defined by  $\delta$  to improve bias 498 correction. Furthermore, the performance of F-DGQM and F-DDQM, proposed in this study, 499 was compared with two existing QM methods, DGQM and SGQM, which have been widely 500 used in different regions for correcting bias in monthly precipitation. This study concluded the 501 following: First, the performance of F-DGQM is generally higher than SGQM and DGQM at 502 all stations. Second, the  $\delta$  (dividing point) of F-DGQM and F-DDQM varies from station to 503 station, indicating a constant  $\delta$  at all stations is not optimal for bias correction. Third, the





judicious selection of the dividing point improves the performance for bias correction. Fourth,
F-DDQM corrected precipitation has lower uncertainty than other methods. Fifth, F-DDQM
performs best in correcting bias in extreme precipitation.
This study contributes to technological development by suggesting a new bias
correction method that can be used more flexibly than the existing DGQM for reliable
correction of GCM biases.
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