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Machine-learning approach to crop yield prediction with the spatial extent of drought

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Abstract

Crop yield is one of the variables used to assess the impact of droughts on agriculture. Crop growth models calculate yield and variables related to plant development and become more suitable for crop yield estimation. However, these models are limited in that specific data are needed for computation. Given this limitation, machine learning (ML) models are often widely utilised instead, but their use with the spatial characteristics of droughts as input data is limited. This research explored the spatial extent of drought (area) as input data for building an approach to predict seasonal crop yield. This ML approach is made up of two components. The first includes polynomial regression (PR) models, and the second considers artificial neural network (ANN) models. In this approach, the purpose was to evaluate both types of ML models (PR and ANN) and integrate them into one operational tool. The logic is as follows: ANN models determine the most accurate predictions, but in practice, issues regarding data retrieval and processing can make the use of equations, i.e. PR, preferable. The proposed approach provides these PR equations to perform such calculations with early and preliminary input. The estimates can be further improved when the ANN models are run with the final input data. The results indicated that the empirical equations (PR) produced good predictions when using drought area as the input. ANN provides better estimates, in general. This research will improve drought monitoring systems for assessing drought effects. Since it is currently possible to calculate drought areas within these systems, the direct application of the prediction of drought effects is possible to integrate by following approaches such as the one presented or similar.

Keywords

Spatio-temporal analysis, crop yield, drought impact, machine learning, agricultural drought

1 Introduction

Drought continually hits many regions across the world. It negatively affects various human activities such as agriculture, which not only generates economic losses but can also trigger

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

famine, causing millions of deaths (Below et al., 2007; Food and Agriculture Organization of the United Nations (FAO), 2017; Kim et al., 2019; Sheffield and Wood, 2011; World Meteorological Organization (WMO), 2006). Hence, methods that help to improve strategies for drought mitigation are necessary. Within these methods are those that allow predicting the impacts of drought.

Assessments of drought impacts confirm that the presence of drought on human activities can be devastating. For instance, the Food and Agriculture Organization of the United Nations (FAO) calculated the damage and losses in the agricultural sector caused by five types of hazards, including drought. FAO estimates that drought causes damages and losses to this sector by up to 80% (FAO, 2017). Although multiple factors are involved in agriculture affectation, drought often plays the primary role, as literature confirms (Dai, 2011; FAO, 2017; Kim et al., 2019).

The assessment of drought impacts on agriculture can be performed in terms of crop yield. FAO defines crop yield as the measure of the yield of a crop per unit area of land cultivation (in kg/ha or ton/ha) (FAO and DWFI, 2015). For assessing crop yield under drought affectation, physical models based on crop properties turn out to be more comprehensive and descriptive (Huang et al., 2019; Reynolds et al., 2000; White et al., 1997; Wu et al., 2016). However, an important barrier to such models' realisation is the lack of detailed crop data and the difficulty representing all the processes involved in all stages of crop development (Huang et al., 2019; Reynolds et al., 2000; Wu et al., 2016).

Statistical and machine-learning (ML) models, which involve mathematical equations to calculate the output of a model with suitable input(s), can be used to assess crop yield impact by drought without considering any biological or physical process of the crop but the analysis of the input and output data (Chlingaryan et al., 2018; Rahmati et al., 2020; Udmale et al., 2020; van Klompenburg et al., 2020). There have been studies where various inputs, ML techniques and architectures (configurations) have been tested for crop yield prediction (e.g., Chlingaryan et al., 2018; van Klompenburg et al., 2020). However, the spatial extent of drought (area) is an input that has not been fully explored previously to crop yield prediction. The prediction refers to the calculation of crop yield at the end of the growing season (harvesting) with information available before or during the crop development season (pre-harvesting).

This research aims to develop an ML approach to calculate seasonal crop yield (CY) with the monthly drought areas (DAs) as input. The ML approach comprises two components. Each component includes a set of the following types of ML models: polynomial regression (PR) and artificial neural network (ANN). The goal is to build both types of ML models (ANN and

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

MR) and use them as an integrated tool to support the decisions made based on crop yield prediction. The logic is as follows. PR provides the prediction where the crop yield calculation is "clear" to the performer (the end-user) because she/he has access to the equations that have a straightforward interpretation and calculations can be done with early and preliminary input data. For its part, ANN is used as the most accurate model, although the output calculation is not as "clear" as in the case of PR due to the difficulty of interpreting the structure of the resulting ANN. ANN are expected to be used with the final input data.

Three East Indian regions where agriculture plays an important role were chosen as a case study. ML models were built for the period 1967-2015. ML models aim to predict rice crop yield since rice is the most cultivated crop in these regions. The ML approach was applied separately to the three regions.

Crop yield prediction in India

In India, as in many other countries, the official crop yield prediction is mainly based on conventional data collections techniques such as ground-field visits (Reynolds et al., 2000; Sawasawa, 2003). The crop yield is measured through crop cutting experiments carried out over sample crop areas. In this country, principal crops' calculations of area and yield are released through the Directorate of Economics and Statistics, Ministry of Agriculture (DESMOA). The production (in kg or ton) of a specific crop is calculated by multiplying the whole field area by its crop yield. The crop production is needed for the decision-makers to take various policy decisions relating to pricing, marketing, distribution, exportation and importation.

The Kharif season, as it is locally known, represents about 80% of the annual rainfall (Naresh Kumar et al., 2012). This monsoon season generally goes from June to October. In this season, the highest agricultural production is obtained. Estimation of Kharif crop yield and production is released four times during the year with different levels of sophistication and precision, where the last one is considered the most accurate. The first calculation is presented in September, the second one in January, the third one in March/April, and the fourth, and the last one in June/July. It should be noted that the last two calculations of crop yield and production become available much after the crops have already been harvested in December/January. From the four calculations, the first two can be considered as predictions. These two first predictions serve as primary estimations about how much the final yield and production will be.

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences Discussions

The existing ground-field visits-based agricultural forecasting system provides reliable information; however, it lacks pre-harvesting forecasting. This limitation motivated the creation of a satellite-based forecasting system to have information at the early stages of crop growth. This system is called the National Crop Forecasting Centre (NCFC) (Sawasawa, 2003). NCFC is continuously verified and continuously updated. Although NCFC advances the one based on ground-field visits, data needed for its execution could be not always available. Therefore, it is necessary to explore other solutions. In this study, it is not intended to replace the previous and new forecasting systems, but to provide a complement to corroborate both estimates, and in a broader sense, to provide the scientific community with an approach to crop yield prediction with information on the spatial extent of drought.

2 ML modelling methodology

The experiment was carried out with the following methodology that involves the ML construction. The next paragraphs show each step in detail. These steps are (1) data preparation, (2) input variable selection, (3) polynomial regression models calculation, (4) artificial neural network models calculation, and (5) models application and combination.

2.1 Step 1. Data preparation

Two types of data were prepared, the crop yield and the percentage of drought areas. For data preparation, three tasks were carried out (1) data retrieving, (2) drought areas calculation, and (3) data de-trending.

2.1.1 Data retrieving

Section 3 shows what corresponds to data retrieving for crop yield (CY) and the drought indicator. CY data correspond to the largest growing season. CY time series has a value for each year for the period 1966-2015 (49 years). CY was available for each region. On the other hand, drought indicator data is on a monthly basis for the period 1901-2015. The spatial resolution is half a degree.

2.1.2 Drought areas calculation

The drought areas were calculated following the methodology presented below. These areas were calculated for the three regions. Drought areas were calculated from the drought indicator data that is in a grid format, i.e., each cell has associated a geographic location and a time step. The calculation of drought areas started with the reclassification of all the cells of the drought indicator data by non-drought and drought cells. The drought indicator data was evaluated cell by cell to determine those that are in drought, i.e. drought condition. To determine drought and non-drought condition (D_S), the Eq. 1 was applied (Corzo Perez et al., 2011; Diaz et al., 2019, 2020; Herrera-Estrada et al., 2017). Eq. 1 represents the following. When the drought indicator is below to the selected threshold *T*, the value of 1 is used to indicate drought in the cell and non-drought is represented by the value of 0. This classification is performed for all the cells of the grid data in each time step (*t*).

$$D_S(t) = \begin{cases} 1 \text{ if } \mathrm{DI}(t) \leq T \\ 0 \text{ if } \mathrm{DI}(t) > T \end{cases} \quad \text{(Eq. 1)}$$

Once the ones-and-zeros data was obtained, the drought areas (DAs) were calculated for each region with Eq. 2. DA was computed as the ratio between the cells in drought and the total number of cells of the region (*N*). In Eq. 2, the number of cell is denoted by *c*.

$$\mathrm{DA}(t) = 100/N \cdot \sum_{c=1}^{N} D_S(t) \quad \text{(Eq. 2)}$$

The number of cells (*N*) of the mask is 63, 31 and 54 for region 1, 2 and 3. The masks in raster format were built for each region. The mask is an array of ones and zeros, where the value of 1 indicates the land. We used the threshold $T = -1$ to calculate cells in droughts. This threshold is widely used to identify a cell in drought when working with standardised indices such as the used in this research (Sect. 3.2). Usually, drought indicator data is calculated at different aggregations periods. We retrieved this data for 1, 3, 6, 9, and 12 months of aggregation period (Sect. 3.2). DAs' time series were calculated for each aggregation period and are indicated as DA1, DA3, DA6, DA9, and DA12.

2.1.3 Data de-trending

Data stationarity is typically assumed when modelling. However, the present study uses crop yield, which is non-stationary in nature. The crop yield depends on factors that affect its trend, such as drought, flood, cultivars and its own management. Therefore, it is advisable to remove short-term fluctuations in crop yield before constructing the model (Montesino Pouzols and Lendasse, 2010).

Among the methods available to de-trend data, the 'first difference' method is popular due to its simplicity. In this method, the trend is removed from the time series by subtracting the previous value $x^*(t-1)$ from the current one $x^*(t)$, as shown in Eq. 3. The de-trended value for the first time step ($t = 1$) is not calculated. The length of the de-trended time series is $n = m - 1$, where *m* is the length of the original time series. The de-trended data $x(t)$ has the same units as the original data $x^*(t)$.

$$x(t) = x^*(t) - x^*(t-1) \quad \text{(Eq. 3)}$$

The trended of CY and DA time series was removed with Eq. 3. For the case of CY, the de-trended time series retained one value per season, i.e. one per year. As noted, the method for removing the trend does not generate the value for the first time step; therefore, the de-trended CY data corresponds to the period 1967-2015 (49 years).

In the case of DA, Eq. 3 was applied as follows. Because the DA data is monthly, i.e. 12 values per year, and CY data is seasonal, i.e. one value per year, first DA time series were extracted for each month. The monthly values for January were extracted for each year and so on until December. These twelve DA time series were compiled for each of the five DA1, 3, 6, 9 and 12 time series. A total of 60 DA time series (12 × 5) were obtained. To refer to these time series, a number (suffix) was added to indicate the month. In this way, for example, the time series DA3_7 indicates the drought areas for July calculated from the drought indicator with 3-month aggregation period. Eq. 3 for the removal of the trend was applied to each of the 60 DA time series. The DA time series run from 1901-2015. For the construction of the ML models, the common period 1967-2015 (49 years) was chosen.

2.2 Step 2. Input variable selection

In an ML model, the input, known as the predictor, is generally made up of independent variables. Often these variables are arranged in different ways to determine the best model input representation. An example arrangement is the selection of the independent variable using different previous time steps, such as $t-1$ (the previous time), $t-2$ and so on. When using drought indicators as the predictors, these arrangements include the different aggregation periods (i.e. different aggregation periods are tested). The idea is not to include all the variables and all their different possible arrangements but rather to find the best ones and discard those that do not contribute significantly to the model's results. Other arrangements of the input variable include the average, or other statistics, over a period.

There are different methods for selecting input variables. Based on the procedure, these methods are classified into model-based and filter types (May et al., 2011). The first includes all those where the model runs, and based on its performance, a specific variable is chosen or discarded. The latter include methods where the variable is chosen *a priori* through a generally statistical process and does not require the model to be run. Correlation analysis, which falls under the second category, is often chosen for its simplicity and wide application. Correlation is calculated between the time series of the output variable (CY in this case) and the different input variables, including their various arrangements.

In this study, for the selection of the relevant input variables, the correlation analysis was done. The correlation was calculated between the de-trended time series of the seasonal CY and the 60 DAs. As mentioned before, due to DAs are monthly and CY is seasonal, 12 time series of

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences
Discussions

DAs were prepared, one per month, for each aggregation period. The DAs were then correlated with the CY. Another option could be to use the yearly average value of the DAs, such as the average of the DAs of the months of the cultivation period, or something similar. However, we opted to identify the DAs of the months that have the highest correlation with the seasonal CY and use them as inputs.

The approach of the selection of the most correlated DAs was chosen for two main reasons. On the one hand, rice responds to the climate variations differently from one growth stage to another over the year, which could be better captured with the information of some months than others. On the other hand, different types of drought (i.e. meteorological, agricultural, and hydrological) are expected to affect (impact) the crop yield to different degrees. This level of affectation could be taken into account either by using different hydro-meteorological variables or selecting different aggregation periods of the meteorological variables, as in this case. An average of DAs could "hide" a significant drought area that could contribute more (or less) to the final crop yield. In addition, in this research, ML models were built to be used at different stages of crop cultivation, i.e. models to be applied in June, July, and so on, each of them with a different expected degree of accuracy. Therefore, the use of time series for each month extracted from the DAs for all the different aggregation periods is more appropriate.

Based on the correlation coefficient, the input variables were selected. In total, 15 sets of input variables (Table 2) were selected for each month from January to December. Each set is made up of different DA time series, out of the 60 de-trended DAs. The number of variables is different in each set. These sets of input variables are presented in the results section. All sets include the de-trended CY from the previous year (CY_{t-1}). CY_{t-1} was used because, in the particular case of the study area, CY of the current year is planned to be reached based on data of the previous year.

2.3 Step 3. Polynomial regression models calculation

For the case of PR, four types of models were tested (Table 1). All the PR models were built for each month from January to December following Eq. 5 to 8. A total of 15 sets of combinations of input variables were tested in each PR model. The best PR model was identified for each month following the RMSE criterion (Eq. 9). MATLAB software was used for implementation.

PR is an extension of linear regression that allows the use of more than one input variable to calculate the output variable (Eq. 4).

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences
Open Access
Discussions

$$y = b_0 + \sum_{i=1}^{n} b_i x_i + e \qquad \text{(Eq. 4)}$$

In Eq. 4, y is the output variable, also known as the response, which in this case is the crop yield. The term x_i is the i-th input variable (predictor) from a total of n variables. The regression coefficients vector is represented by b. From the coefficients vector, b_0 is known as the intercept. The vector of errors is indicated by e.

Table 1 shows four formulations of PR. The PR models are indicated as linear, pure-quadratic, quadratic and interactions. Descriptions of each and their equations are presented in Table 1 (Eq. 5 to 8). The input variable (x_i) was selected based on the correlation analysis (Sect. 2.2).

Table 1 Polynomial regression (PR) types followed in this study.

PR type	Equation	Description
Linear	(Eq. 5) $y = b_0 + \sum_{i=1}^{n} b_i x_i$	It has an intercept and linear terms of predictors
Pure-quadratic	(Eq. 6) $y = b_0 + \sum_{i=1}^{n} b_i x_i + \sum_{i=1}^{n} b_{n+i} x_i^2$	It has an intercept, as well as linear and squared terms of predictors
Quadratic	(Eq. 7) $y = b_0 + \sum_{i=1}^{n} b_i x_i + \sum_{i=1}^{n} b_{n+i} x_i^2 + \sum_{i=1}^{n-1} \sum_{j=i+1}^{n} b_{2n+(i-1)n-\frac{(i-1)i}{2}+(j-i)} x_i x_j$	It has an intercept, linear and squared terms and all products of pairs of distinct predictors
Interactions	(Eq. 8) $y = b_0 + \sum_{i=1}^{n} b_i x_i + \sum_{i=1}^{n-1} \sum_{j=i+1}^{n} b_{n+(i-1)n-\frac{(i-1)i}{2}+(j-i)} x_i x_j$	It has an intercept, linear terms of predictors, all products of pairs of distinct predictors and no squared terms

The best PR model was identified from four types using the root mean square error (RMSE) criterion. The RMSE is calculated between the observations (o) and the predictions (p), as shown in Eq. 9. RMSE is one of the most widely used criteria in the comparison of observations and model calculations.

$$\mathrm{RMSE} = \sqrt{\frac{\sum_{i=1}^{n} (o_i - p_i)^2}{n}} \qquad \text{(Eq. 9)}$$

2.4 Step 4. Artificial neural network models calculation

ANN is a method loosely based on imitating the basic functionality of neurons (i.e. the working units of the human brain) (Govindaraju, 2000; Maier and Dandy, 2000). The input variables

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

(predictors) are connected to each other through mathematical formulations that allow complex non-linear relationships to be represented. These connexions are symbolised as nodes interconnected within a network aimed at calculating the output variable (response).

Of the different proposed ANN architectures (network designs), one of the most widely used is the feedforward neural network (FFNN). The FFNN is schematised by a series of nodes located in one of three layers: input, hidden or output. The number of input nodes is equal to the number of input variables in the input layer (Elshorbagy et al., 2010). This first layer is in turn connected to the hidden layer, which receives this name because the connections made there may not be immediately evident to the model performer. In this hidden layer, the number of nodes is not defined by default; rather, the greater the number of nodes, the more complex the model. Finally, the nodes of the hidden layer are connected to those of the output layer. In a single-output variable problem, there is only one node. ANNs are typically trained by non-linear optimisation gradient-based algorithms, e.g. the Levenberg-Marquardt algorithm.

In the ANN setup, the number of nodes of the input layer was equal to the number of variables of the respective combination. The number of nodes in the output layer was one and corresponded to the seasonal crop production (CY). An iteration optimisation procedure was carried out regarding the hidden layer, varying the number of nodes from 1 to 10. For each number of nodes, 100 iterations were done, being 1,000 in total. For reproducibility of the results, the random values were set to default at the beginning of the number of nodes change. For each month, from January to December, the ANNs were built. MATLAB software was used to implement the ANNs with the Levenberg-Marquardt algorithm for training. In each of the ANNs, 85 % of the data was used for training-validation, and the rest for testing (verification). The best model corresponding to each number of hidden nodes was identified, i.e. ten models per month and the best model for each month. RMSE was used to identify the best models. RMSE was calculated for (1) the training-validation dataset (RMSE_cal), (2) the testing dataset (RMSE_test), and (3) the entire period (RMSE). In all the cases, the final (best) model was chosen based on RMSE for the entire period.

2.5 Step 5. Models application and combination

Once the best ML models, PR and ANN, were known, the pair of models were selected for each month. Depending on the performance of these models (and experience of their use), they can be used either separately or combined, e.g. being run in parallel so that a modeller could see the cases when models produce different results. An alternative is to use a dynamic weighting of the models' outputs (e.g. with the weights being proportional to the historical performance) to form a "model committee".

3 Data

3.1 Crop yield

Rice is the most important food grain in East India, so it was selected to assess our ML-oriented crop-yield predictions. Rice from this region accounts for roughly 85 percent of the total rice production in India (Ghosh et al., 2014). As mentioned, ML models were constructed for three regions of the eastern Indian (Figure 1). State-wise crop-yield data was retrieved from 1966 to 2015 (49 years) through the Indian Directorate of Economic and Statistics from the Department of Agriculture (DAC) (http://eands.dacnet.nic.in/).

There are three crop seasons in India: Rabi, Kharif and Zaid. Of these, the Kharif season was chosen for study because it is the largest in terms of crop production. Kharif crops are sown in June and harvested in November/December. Seasonal crop-yield data was obtained from the DAC website and arranged into time series per region. One value was assigned to each year of crops harvested in the Kharif season.

Figure 1 shows the location of the three regions. These are made up as follows. Region 1 includes the current states of Bihar and Jharkhand; region 2 corresponds to the state of West Bengal; and region 3 makes up the state of Odisha. Two important clarifications have to be made regarding crop yield data retrieving for these regions. First, in late 2000, Bihar was divided into two states: Bihar and Jharkhand. Thereafter, rice data was reported separately. In this study, both states are marked as region 1; the crop-yield data from 2000 to 2015 is the reported sum of current Bihar and Jharkhand. Second, in 2011, Orissa was renamed Odisha (region 3), but the territory remains the same. In this case, crop yield data for Odisha is that reported for the former Orissa and the current Odisha.

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences
Discussions

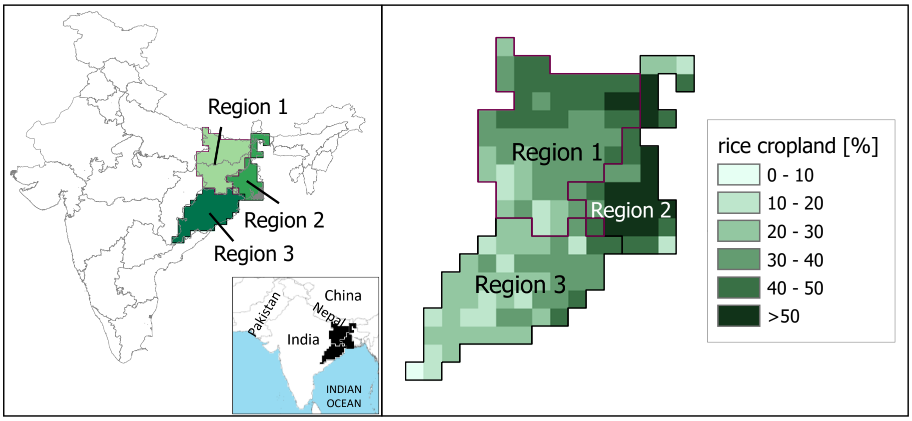

Figure 1 Case study location and rice cropland (in percentage). Case study comprises region 1 (Bihar and Jharkhand), region 2 (West Bengal) and region 3 (Odisha). Source of rice cropland: Monfreda et al. (2008).

3.2 Drought indicator

Soil moisture is the preferred variable for calculating agricultural drought indicators. However, another widely disseminated way to indirectly infer this type of drought indicator is to use meteorological drought indicators as proxies. Among these, the Standardised Precipitation Evaporation Index (SPEI) proposed by Vicente-Serrano et al. (2010) has shown to be useful in assessing agricultural drought. The SPEI follows a similar methodology as that of the widely used Standardized Precipitation Index (SPI) (Mckee et al., 1993), but with added consideration for the difference between precipitation and evapotranspiration. SPEI data was retrieved from the SPEI Global Drought Monitor (https://spei.csic.es) between 1901 and 2015. The spatial resolution of the drought indicator data is 0.5 degrees. The SPEI data was available at different aggregation periods; for this study, it was retrieved for the aggregation periods of 1, 3, 6, 9 and 12 months, indicated as DI1, DI3, DI6, DI9 and DI12, respectively.

4 Results and discussion

4.1 Data preparation: drought areas and crop yield

Figure 2 show the drought areas calculated for the three regions. In this heat map, columns indicate the months and rows point out the years. The redder the colour, the larger the drought area. In general, region 1 (Figure 2, the upper panel) presents the highest values concerning the other two regions. In general, the 1990s show higher values of areas with respect to the rest of the period, which agrees with Guha-Sapir (2019); in this decade, there were three droughts, 1993, 1996 and 2000. At the beginning of the period, large areas are also observed in the theree regions; these results align with Bhalme and Mooley (1980).

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences
Discussions

In Figure 2, a pattern is observed in the drought areas distribution for all the aggregation periods, i.e. from DA1 to DA12. In DA1, the areas mainly concentrate in the first months; even the December column is almost white (without drought). Later, for DA3, the large areas are located from April to November. Successively, for DA6 and DA9, the largest areas are concentrated in the second half of the year. There are even droughts that end in the following year; they are the reddish lines that are observed in the first semester (first columns). Finally, in DA12, there are consecutive large areas indicated by the reddish lines; droughts usually begin in the second semester and extend until the following year. These results show the importance of considering more than one period of aggregation when using indicators based on meteorological variables; each aggregation period can be a proxy for analysing different types of drought and its effects.

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

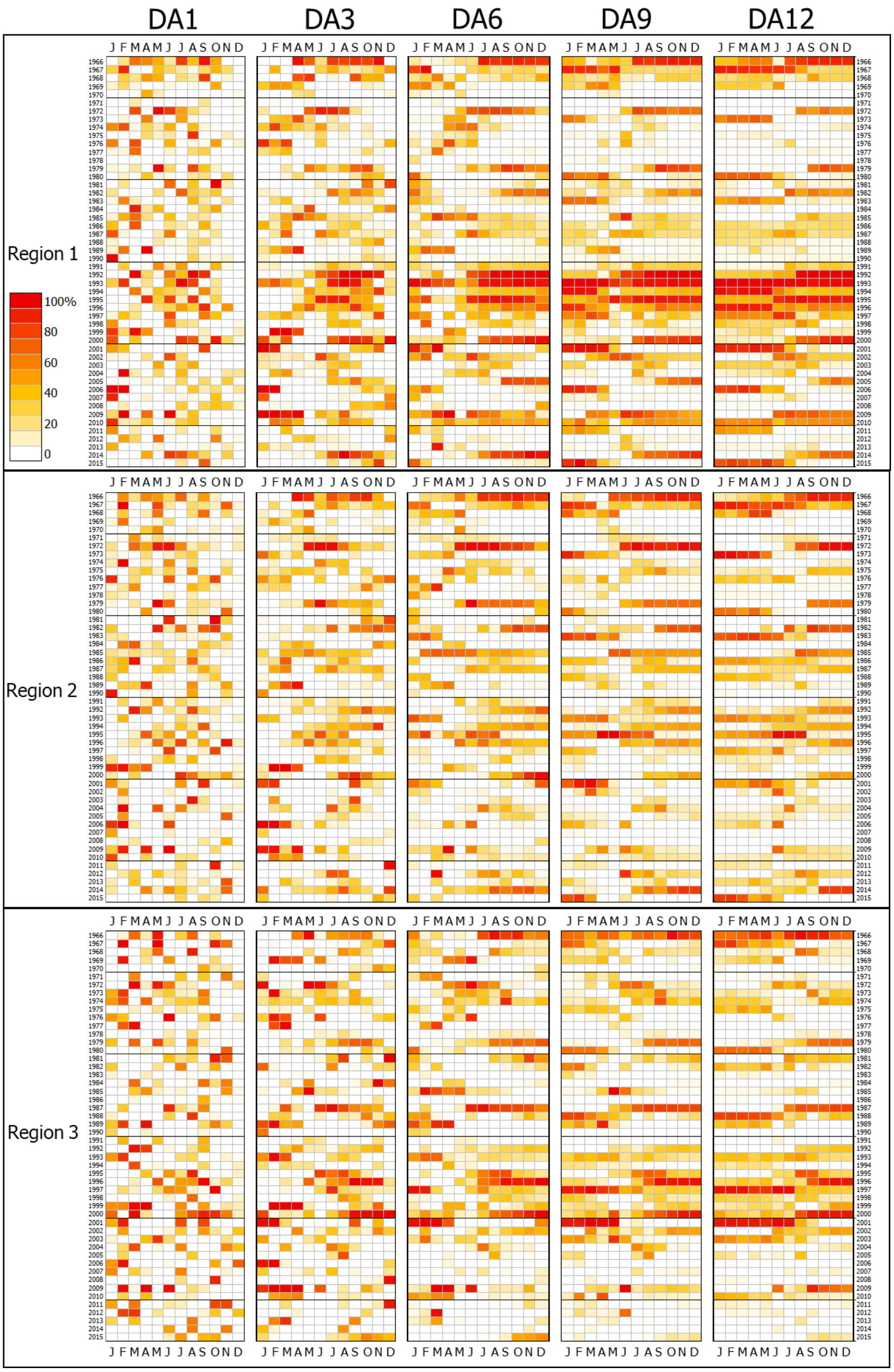

Figure 2 Drought areas (DAs) for each aggregation period (1, 3, 6, 9 and 12 months) and region. Top, middle, and bottom panels indicate region 1 (Bihar and Jharkhand), region 2 (West Bengal) and region 3 (Odisha).

Figure 3 shows the time series of de-trended CY and DA for the three regions. In the case of DA (indicated in red), the values are displayed in inverse order to facilitate interpretation. In general, when drought areas increase, this is expected to affect crop yield (decreasing). Otherwise, when the drought area decreases, this effect favours an increase in crop yield. In general, for the three regions, the decreases in CY coincide with the increases in DA. The general pattern regarding DA variations is as follows. The values fluctuate throughout the year for the aggregation periods of one and three months (DA1 and DA3). Subsequently, for DA6 to DA12, the values are concentrated in the second half of the year. These results also show the usefulness of the different aggregation periods to capture different types of drought. The effect of increasing DA seems not to be observed in decreasing CY for all cases of DAs. For example, in region 1 (Figure 3, the upper panel), the decrease in 2004, one of the maximums, does not coincide with increases in DA9 and DA12, but it does for DA1, DA3 and DA6. These results also support the use of the different aggregation periods on drought assessments.

4.2 Input variable selection (correlation analysis)

Figure 4 summarises the correlation between the de-trended CY and the DAs, and Figure 5 presents the correlation for each monthly DA time series.

Figure 4 and 5 shows that the correlation is different over the year in the three regions. In all cases, the correlation coefficient increases until a maximum and then decreases. The month in which the maximum value is reached is different for each region but falls within the crop season (i.e. June to November/December). For region 1, it is in July. For region 2, there are four months with this pattern, June, July, October, and November. Finally, for region 3, it is October, November and December.

These results of correlation can be useful for monitoring agricultural drought. For example, in region 1, the drought areas calculated from SPEI6 (i.e. DA6) show a maximum correlation in July. This correlation value means that the previous six months' accumulated effect is crucial for the crop yield of the Kharif season, which covers more or less from June to November/December.

Figure 4 shows the following pattern. In general, for region 1, results similar to DA6 are observed for DA3, 9 and 12. For region 2, a similar pattern happens in the peaks, but in this case two, one corresponding to DA1 and 3, and the other to DA6, 9, and 12. The first peak of DA1 and DA3 may indicate that it is crucial to pay attention to the immediate period conditions of one to three months. In the case of the second peak, the medium and long-term conditions, 6 to 12 months, are more important to monitor for the harvest month. For region 3, the peak

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences
Discussions

occurs at the end of the growing season, in almost all cases. Hence, the condition before the growing season is decisive for the crop yield.

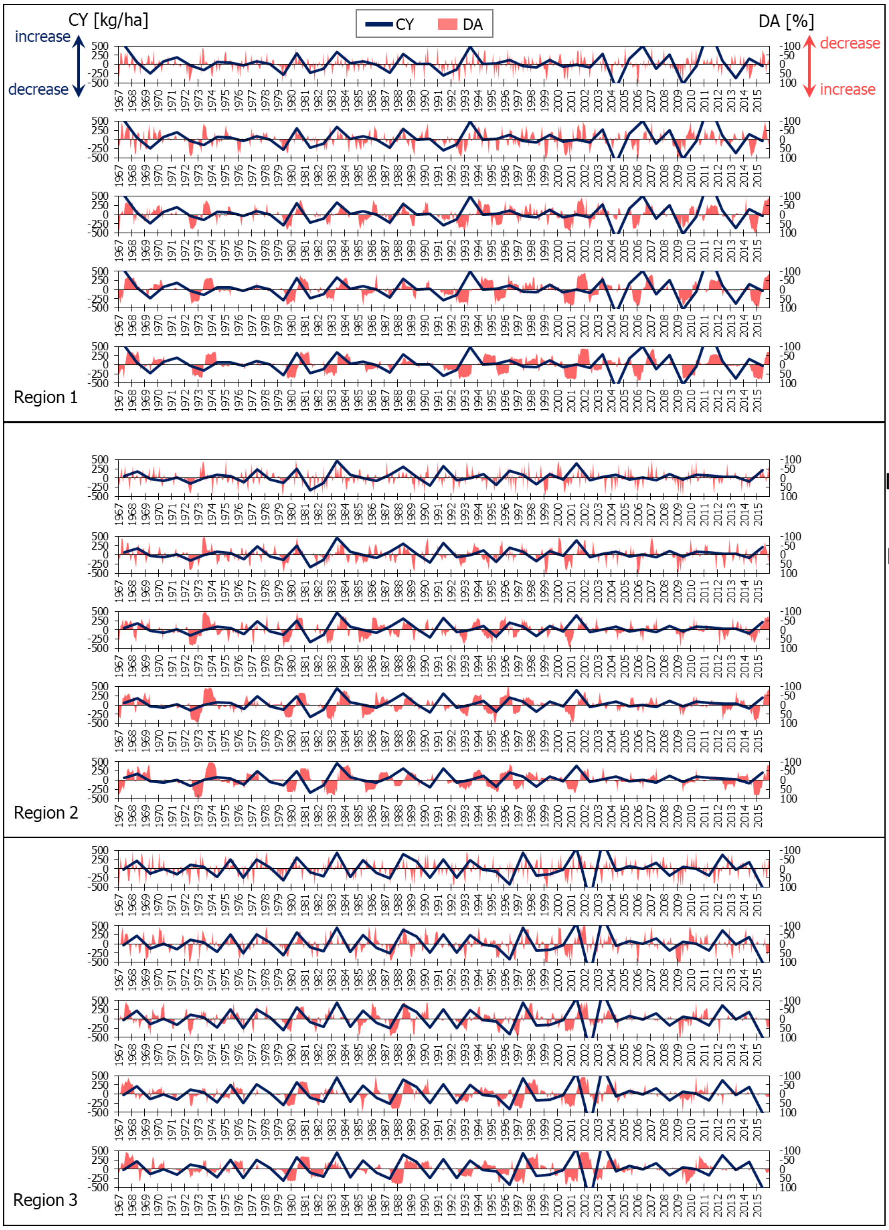

Figure 3 Time series of the de-trended crop yield (CY) and drought areas (DAs) for each aggregation period (1, 3, 6, 9 and 12 months) and region. Top, middle, and bottom panels indicate region 1 (Bihar and Jharkhand), region 2 (West Bengal) and region 3 (Odisha).

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Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences
Discussions
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Figure 5 shows how the correlation coefficients between CY and DA are positive outside the growing season and negative within that season. However, this pattern is less evident for DA1 and DA3. The pattern shown by the correlation coefficients in Figure 5 supports the idea that drought is an important factor in crop yield since the months with less drought are more correlated with the increase in CY, and the months with more drought do so with decrease in CY.

Figure 4 (d) shows the percentage of irrigated and rain-fed agriculture. For regions 1 and 2, about half is by irrigation, while in region 3, only 35%. Perhaps this percentage of irrigation for region 3 explains why the correlation coefficients for this region are higher than for the other two (Figure 4, and 5 (c)). Region 3 is more dependent on rain for agriculture; therefore, this condition is best captured when calculating drought with the precipitation, as in this case (Sect. 3.2).

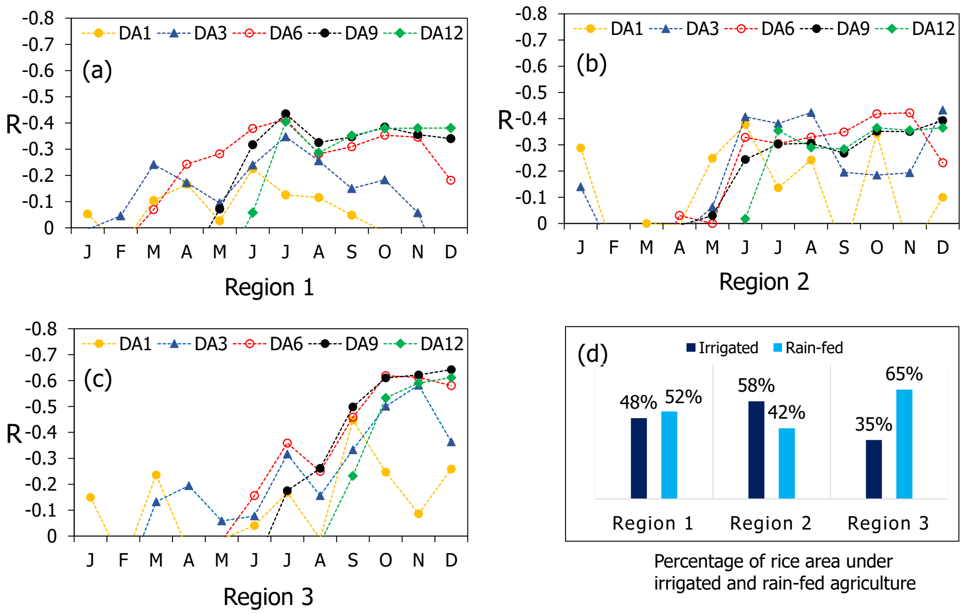

Figure 4 Summary of correlation between de-trended crop yield (CY) and drought areas (DAs) for each aggregation period (1, 3, 6, 9 and 12 months) and region: (a) region 1 (Bihar and Jharkhand), (b) region 2 (West Bengal) and (c) region 3 (Odisha). Percentage of rice area under irrigated and rein-fed agriculture (d). Source of irrigated and rein-fed agriculture data: Directorate of Rice Development (DRD), (2014).

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Preprint. Discussion started: 24 November 2021

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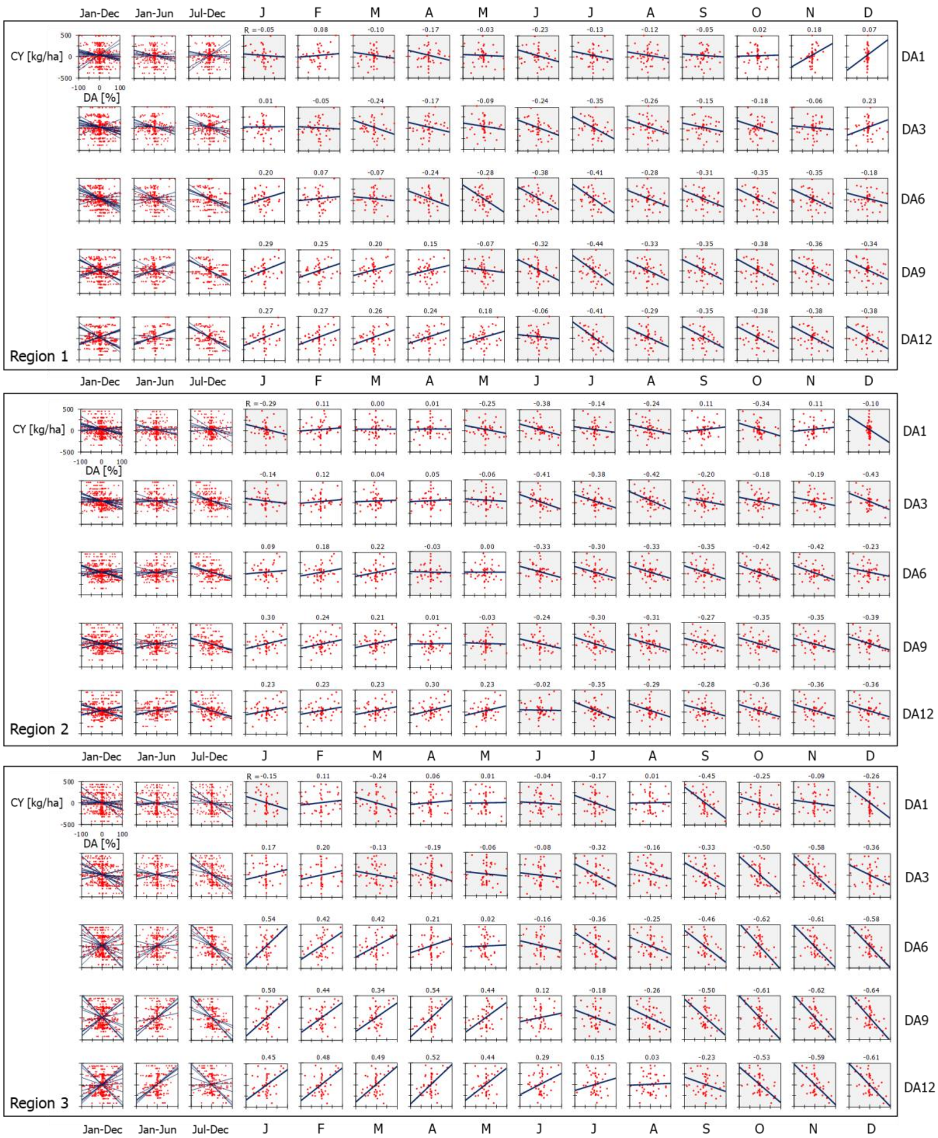

Figure 5 Correlation between de-trended crop yield (CY) and drought areas (DAs) for each aggregation period (1, 3, 6, 9 and 12 months) and region. Results are shown for each monthly DA time series from June to December (J to D). Top, middle, and bottom panels indicate region 1 (Bihar and Jharkhand), region 2 (West Bengal) and region 3 (Odisha).

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

Figure 4 (a, b, and c) shows the following pattern in the three regions. The correlation coefficients between CY and DAs increase according to the aggregation periods and the month of analysis. DA1 and DA3 have a better correlation in the first months of the year. DA6 has a better correlation in the subsequent months, between May and June. Finally, DA9 and 12 do so within the second half of the year.

Each respective DA time series reaches a maximum (or maximums) of correlation, and then correlation decreases. According to this pattern, the 15 combinations of input variables shown in Table 2 were selected. As earlier mentioned, the CY of the previous year was included in all combinations and is indicated as CY_{t-1}. Combinations 1 to 5 only include a DA time series. Combinations 6 to 9 are DA pairs that were calculated with the drought indicator of successive aggregation times. For example, combination 6 forms DA1 and 3, combination 7 includes DA3 and 6, and so on. Similarly, combinations 10 to 13 are proposed, but for triples. Combinations 13 and 14 are fourfold. Finally, the last combination (15th) is made up of all the DA series.

As mentioned, the models were built for each DA time series using the 15 combinations corresponding to each month. For example, the monthly series of DAs extracted for January were used for the case of January. These DAs are DA1_1, DA3_1, DA6_1, DA9_1 and DA12_1. The suffix indicates the month. Then, the different DA1_1 to DA12_1 were used following the 15 combinations shown in Table 2 to build the ML models (ANN and PR) for January. Similarly, it was carried out from February to December.

Table 2 Input sets (combinations) to build the ML models. CY and DA stand for crop yield and drought area. DAs are calculated with the drought indicator for the aggregate period of 1, 3, 6, 9 and 12 months.

Input set (combination)	Input variables
1	CY_{t-1}, DA1
2	CY_{t-1}, DA3
3	CY_{t-1}, DA6
4	CY_{t-1}, DA9
5	CY_{t-1}, DA12
6	CY_{t-1}, DA1,3
7	CY_{t-1}, DA3,6
8	CY_{t-1}, DA6,9
9	CY_{t-1}, DA9,12
10	CY_{t-1}, DA1,3,6
11	CY_{t-1}, DA3,6,9
12	CY_{t-1}, DA6,9,12
13	CY_{t-1}, DA1,3,6,9
14	CY_{t-1}, DA3,6,9,12
15	CY_{t-1}, DA1,3,6,9,12

4.3 ANN and PR models

The results show different magnitudes of error between the observed and predicted CY. The models with the lowest error are presented in Figures 6, 7 and 8, for each of the three regions. The pair of ANN and PR that best predicts CY is shown for each month. The RMSE is also indicated in each case. On the other hand, Figure 9 shows the error for each input set (combination); the lowest error achieved in each month is presented in each case both for each ANN and PR.

In general, ANN shows the least errors, as expected (Figure 9). However, the results of PR are not much worse compared to those of ANN; for example, in some cases, the errors shown by linear PR are very close to those of ANN (e.g. Figure 9, region 2). In general, it is observed that the models with the lowest errors correspond to region 2, followed by region 3 and region 1 (Figure 9). It is attributed to the different degrees of crop irrigation with surface and mostly groundwater, which determines the accuracy of the modelling in the different regions. Another factor contributing to the models' performance is the drastic changes in the CY data, where regions 1 and 3 are the ones that presented the most, and to a much lesser extent, region 2.

Figure 9 shows that in the three regions, different types of PR showed better results. In general, linear and pure-quadratic indicate more stable results (no sudden changes among the different realisations) but not better than quadratic and interactions. In general quadratic and interactions present better results, being in some cases very close to those shown by ANN, e.g. PR interactions (Figure 9, region 1).

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

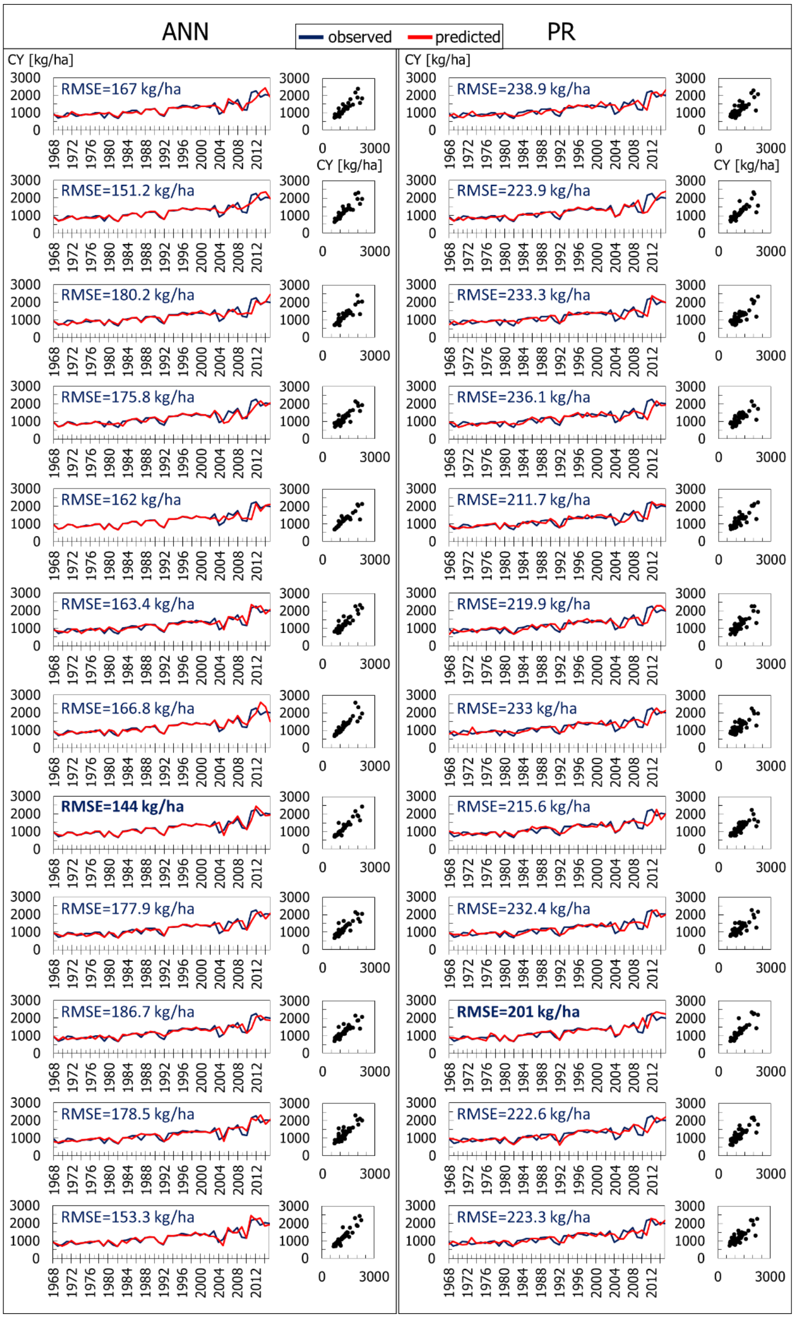

Figure 6 ANN and PR models for predicting seasonal crop yield (CY) built for each time series of monthly drought areas (DAs): region 1 (Bihar and Jharkhand). The model with the lowest error (RMSE) is presented for each month, from January to December (J to D).

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

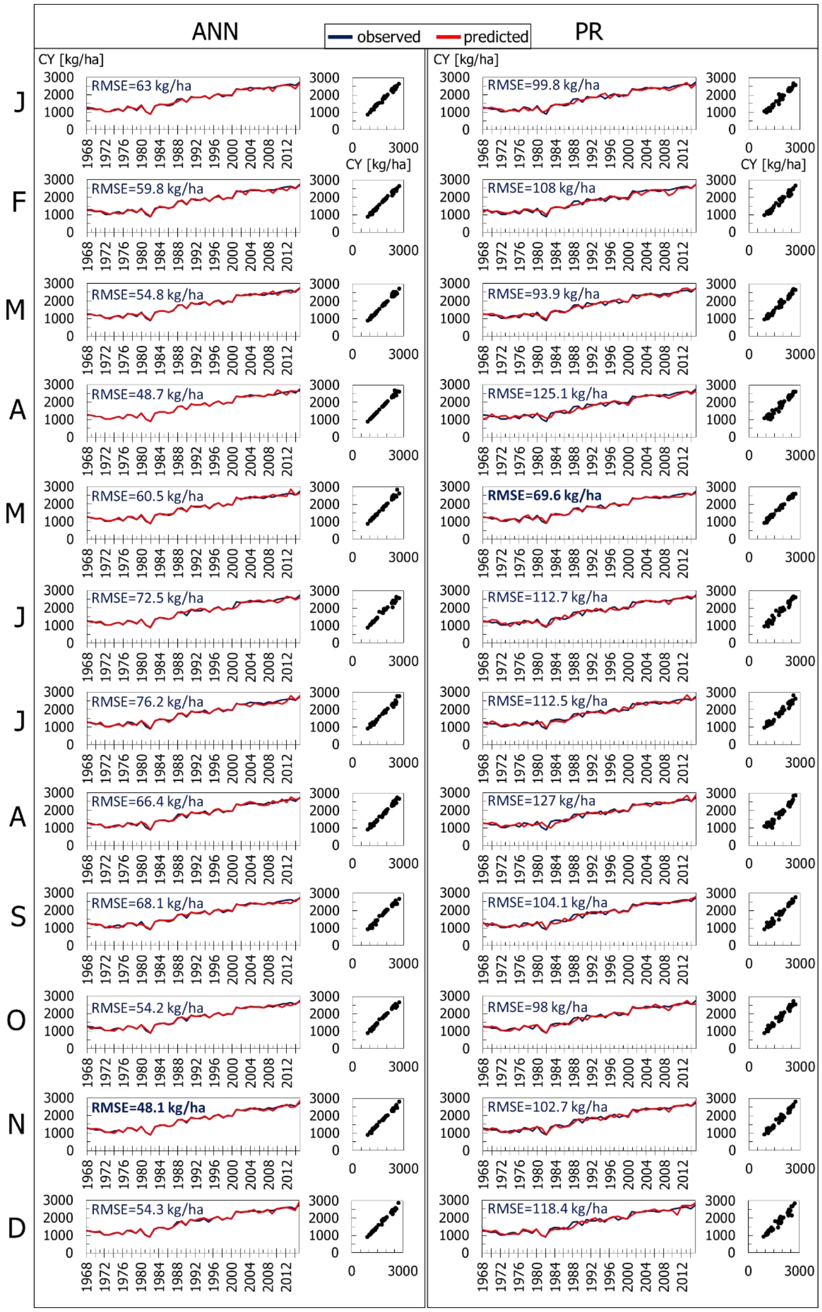

Figure 7 ANN and PR models for predicting seasonal crop yield (CY) built for each time series of monthly drought areas (DAs): region 2 (West Bengal). The model with the lowest error (RMSE) is presented for each month, from January to December (J to D).

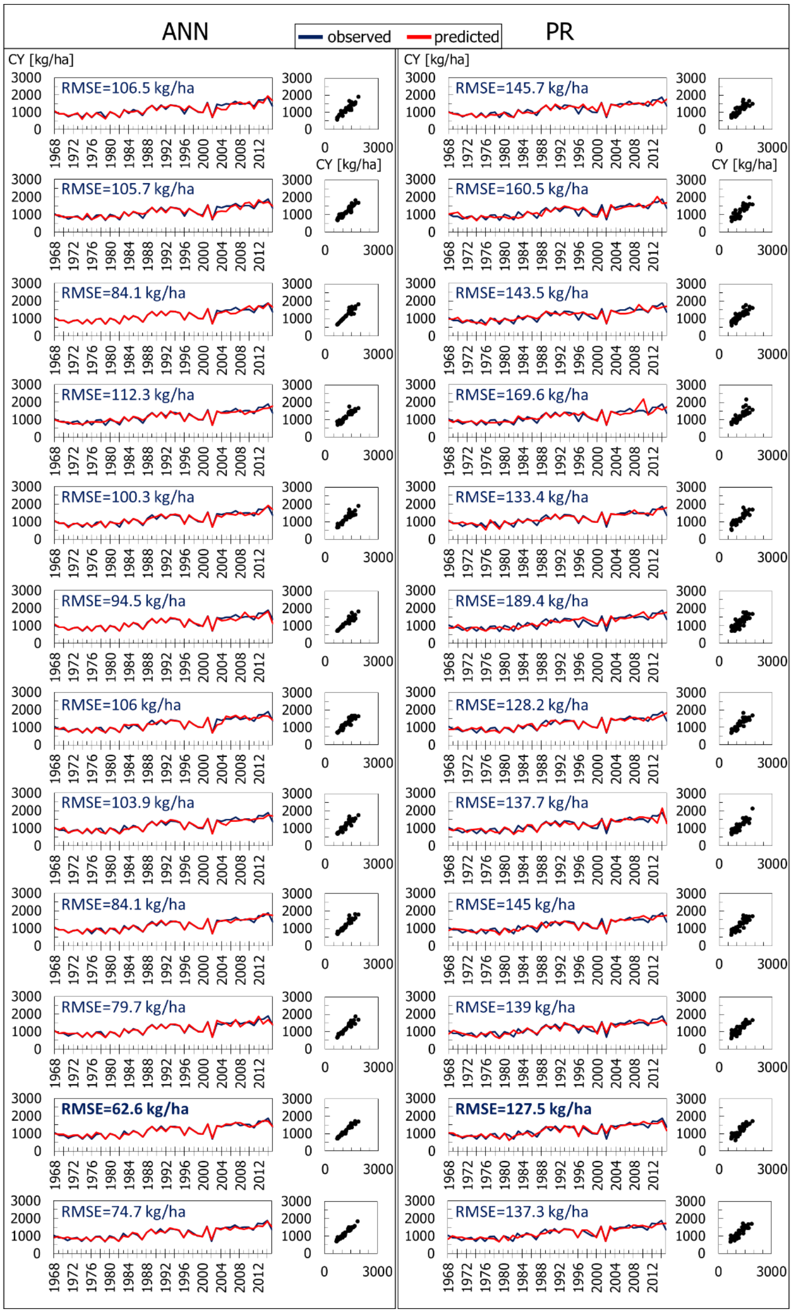

Figure 8 ANN and PR models for predicting seasonal crop yield (CY) built for each time series of monthly drought areas (DAs): region 3 (Odisha). The model with the lowest error (RMSE) is presented for each month, from January to December (J to D).

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences
Discussions

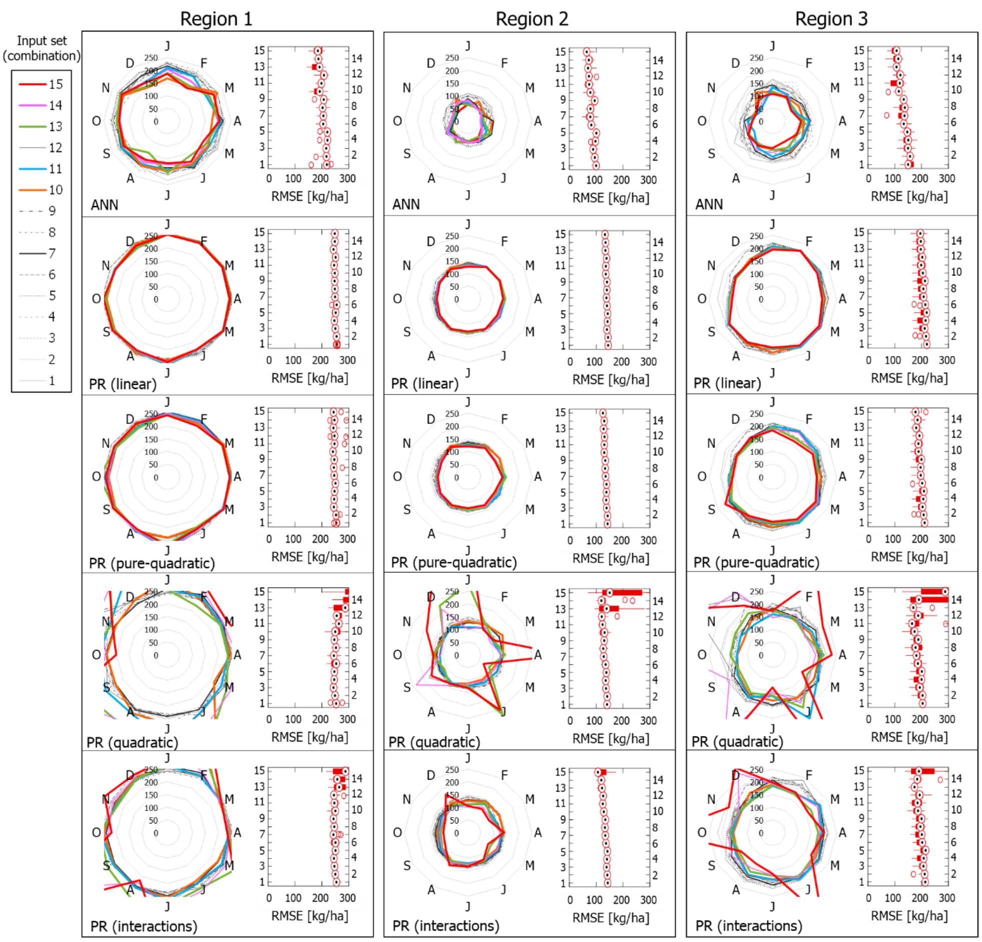

Figure 9 Root mean square error (RMSE) [kg/ha] for each of the 15 input sets (combinations) of the ANN and PR models built for each region. For each set of input (from one to 15), the lowest errors are presented for each month (January to December). Results of each input set are shown with lines to facilitate the analysis. Left, middle, and right panels indicate region 1 (Bihar and Jharkhand), region 2 (West Bengal) and region 3 (Odisha).

4.4 Models application and combination

The best performing models were selected for each month. Table 3 shows the summary of these models, which includes the input set (combination), number of nodes, and errors for ANN, and input set, type and errors for PR. The number of nodes indicates the degree of non-linearity presented in each model. In this way, the more nodes, the more complex the model is in the case of ANN. On the other hand, quadratic and interactions are the types that showed the best performance in PR models. In all cases, within the combinations of input variables, a single DA time series corresponding to one of the various aggregation periods (D1, D3, D6, D9 or

https://doi.org/10.5194/hess-2021-600
Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences Discussions

D12) that by itself produced good results was not found. The input sets are made up of two and up to six different DAs corresponding to the various aggregation periods. Thus, using more than one aggregation period of drought indicator results in better model performance.

Tables 4, 5 and 6 are derived from Table 3. These three tables show the PR formulas for region 1, 2 and 3, respectively. In each table, the PR formula and the inputs are indicated. These formulas are also intended to be a stand-alone tool in the CY prediction for each region.

The proposed procedure for applying the ML models is as follows.

The calculation begins by selecting the formula of the PR model for each month. Then the CY is calculated with the chosen formula and the corresponding input variables. At the same time, or when it can be computed, the ANN model of the month under analysis is applied. An alternative is to use an approach based on the dynamic weighting of the models' outputs to form a model committee.

Table 3 Summary of the ANN and PR models for predicting crop yield (CY) built for each month and region: (1) Bihar and Jharkhand, (2) West Bengal and (3) Odisha. The table shows the models built with the lowest error (RMSE). DA stands for drought area.

	ANN					PR				
Region	Month	Input set (combination)		No. nodes	RMSE [kg/ha]	Month	Input set (combination)		Type	RMSE [kg/ha]
Region 1	Jan	10	CY_{t-1}, DA1,3,6	4	167.0	Jan	8	CY_{t-1}, DA6,9	quadratic	238.9
	Feb	15	CY_{t-1}, DA1,3,6,9,12	6	151.2	Feb	13	CY_{t-1}, DA1,3,6,9	quadratic	223.9
	Mar	11	CY_{t-1}, DA3,6,9	7	180.2	Mar	6	CY_{t-1}, DA1,3	quadratic	233.3
	Apr	10	CY_{t-1}, DA1,3,6	9	175.8	Apr	15	CY_{t-1}, DA1,3,6,9,12	interactions	236.1
	May	15	CY_{t-1}, DA1,3,6,9,12	5	162.0	May	10	CY_{t-1}, DA1,3,6	quadratic	211.7
	Jun	13	CY_{t-1}, DA1,3,6,9	2	163.4	Jun	10	CY_{t-1}, DA1,3,6	interactions	219.9
	Jul	15	CY_{t-1}, DA1,3,6,9,12	10	166.8	Jul	6	CY_{t-1}, DA1,3	quadratic	233.0
	Aug	13	CY_{t-1}, DA1,3,6,9	5	144.0	Aug	15	CY_{t-1}, DA1,3,6,9,12	interactions	215.6
	Sep	6	CY_{t-1}, DA1,3	5	177.9	Sep	7	CY_{t-1}, DA3,6	quadratic	232.4
	Oct	14	CY_{t-1}, DA3,6,9,12	6	186.7	Oct	15	CY_{t-1}, DA1,3,6,9,12	quadratic	201.0
	Nov	8	CY_{t-1}, DA6,9	4	178.5	Nov	13	CY_{t-1}, DA1,3,6,9	interactions	222.6
	Dec	10	CY_{t-1}, DA1,3,6	4	153.3	Dec	13	CY_{t-1}, DA1,3,6,9	pure-quadratic	223.3
Region 2	Jan	13	CY_{t-1}, DA1,3,6,9	8	63.0	Jan	14	CY_{t-1}, DA3,6,9,12	quadratic	99.8
	Feb	11	CY_{t-1}, DA3,6,9	10	59.8	Feb	15	CY_{t-1}, DA1,3,6,9,12	interactions	108.0
	Mar	7	CY_{t-1}, DA3,6	8	54.8	Mar	15	CY_{t-1}, DA1,3,6,9,12	interactions	93.9
	Apr	14	CY_{t-1}, DA3,6,9,12	7	48.7	Apr	14	CY_{t-1}, DA3,6,9,12	interactions	125.1
	May	15	CY_{t-1}, DA1,3,6,9,12	10	60.5	May	15	CY_{t-1}, DA1,3,6,9,12	quadratic	69.6
	Jun	13	CY_{t-1}, DA1,3,6,9	7	72.5	Jun	10	CY_{t-1}, DA1,3,6	quadratic	112.7
	Jul	6	CY_{t-1}, DA1,3	6	76.2	Jul	10	CY_{t-1}, DA1,3,6	quadratic	112.5
	Aug	6	CY_{t-1}, DA1,3	9	66.4	Aug	13	CY_{t-1}, DA1,3,6,9	interactions	127.0
	Sep	6	CY_{t-1}, DA1,3	10	68.1	Sep	15	CY_{t-1}, DA1,3,6,9,12	interactions	104.1
	Oct	7	CY_{t-1}, DA3,6	10	54.2	Oct	15	CY_{t-1}, DA1,3,6,9,12	interactions	98.0
	Nov	7	CY_{t-1}, DA3,6	10	48.1	Nov	15	CY_{t-1}, DA1,3,6,9,12	interactions	102.7
	Dec	15	CY_{t-1}, DA1,3,6,9,12	8	54.3	Dec	14	CY_{t-1}, DA3,6,9,12	interactions	118.4
Region 3	Jan	15	CY_{t-1}, DA1,3,6,9,12	7	106.5	Jan	14	CY_{t-1}, DA3,6,9,12	quadratic	145.7
	Feb	13	CY_{t-1}, DA1,3,6,9	10	105.7	Feb	10	CY_{t-1}, DA1,3,6	quadratic	160.5
	Mar	15	CY_{t-1}, DA1,3,6,9,12	9	84.1	Mar	12	CY_{t-1}, DA6,9,12	quadratic	143.5
	Apr	15	CY_{t-1}, DA1,3,6,9,12	4	112.3	Apr	14	CY_{t-1}, DA3,6,9,12	quadratic	169.6
	May	12	CY_{t-1}, DA6,9,12	10	100.3	May	15	CY_{t-1}, DA1,3,6,9,12	quadratic	133.4
	Jun	15	CY_{t-1}, DA1,3,6,9,12	9	94.5	Jun	12	CY_{t-1}, DA6,9,12	quadratic	189.4
	Jul	15	CY_{t-1}, DA1,3,6,9,12	7	106.0	Jul	15	CY_{t-1}, DA1,3,6,9,12	quadratic	128.2
	Aug	12	CY_{t-1}, DA6,9,12	7	103.9	Aug	15	CY_{t-1}, DA1,3,6,9,12	interactions	137.7
	Sep	11	CY_{t-1}, DA3,6,9	9	84.1	Sep	13	CY_{t-1}, DA1,3,6,9	quadratic	145.0
	Oct	15	CY_{t-1}, DA1,3,6,9,12	10	79.7	Oct	10	CY_{t-1}, DA1,3,6	quadratic	139.0
	Nov	11	CY_{t-1}, DA3,6,9	10	62.6	Nov	10	CY_{t-1}, DA1,3,6	quadratic	127.5
	Dec	11	CY_{t-1}, DA3,6,9	9	74.7	Dec	8	CY_{t-1}, DA6,9	quadratic	137.3

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Preprint. Discussion started: 24 November 2021

Table 4 PR models for predicting crop yield (CY) built for each month: region 1 (Bihar and Jharkhand). For each moth, it is indicated the input (x1 to x6) and the PR formula. DA stands for drought area.

Month	Input						PR model
	x_1	x_2	x_3	x_4	x_5	x_6	
Jan	CY_{t-1}	DA6	DA9				$-60.7111 -0.1944x_1 -0.2201x_2 +1.2033x_3 -0.0023x_1x_2 +0.0043x_1x_3 -0.0372x_2x_3 +0.0003x_1^2 +0.0504x_2^2 +0.0308x_3^2$
Feb	CY_{t-1}	DA1	DA3	DA6	DA9		$-27.4716 -0.4688x_1 +1.8718x_2 -1.3313x_3 -0.2611x_4 +1.3878x_5 -0.0137x_1x_2 +0.0135x_1x_3 +0.0032x_1x_4 +0.0064x_1x_5 +0.0823x_2x_3 +0.0574x_2x_4 +0.0935x_2x_5 -0.0544x_3x_4 -0.0746x_3x_5 -0.0241x_4x_5 +0.0014x_1^2 -0.0496x_2^2 -0.0202x_3^2 -0.0016x_4^2 +0.0227x_5^2$
Mar	CY_{t-1}	DA1	DA3				$28.1213 -0.5204x_1 -0.4908x_2 +0.0545x_3 +0.0051x_1x_2 -0.0093x_1x_3 +0.0033x_2x_3 +0.0003x_1^2 -0.0107x_2^2 +0.0086x_3^2$
Apr	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$-24.3419 -0.4785x_1 -0.1965x_2 -0.1356x_3 +0.0848x_4 -0.4774x_5 +0.8029x_6 +0.0066x_1x_2 +0.0031x_1x_3 -0.0128x_1x_4 +0.0081x_1x_5 -0.0003x_1x_6 +0.0067x_2x_3 -0.0604x_2x_4 +0.1495x_2x_5 -0.0169x_2x_6 +0.0248x_3x_4 -0.1295x_3x_5 -0.0306x_3x_6 +0.0458x_4x_5 +0.0516x_4x_6 +0.0595x_5x_6$
May	CY_{t-1}	DA1	DA3	DA6			$113.2521 -0.5132x_1 +1.0101x_2 -1.4019x_3 -1.1130x_4 +0.0100x_1x_2 +0.0150x_1x_3 -0.0027x_1x_4 +0.0250x_2x_3 -0.0655x_2x_4 +0.0596x_3x_4 -0.0006x_1^2 -0.0358x_2^2 -0.0380x_3^2 -0.0495x_4^2$
Jun	CY_{t-1}	DA1	DA3	DA6			$54.3 -0.3715x_1 +1.4832x_2 +0.1432x_3 -3.0648x_4 -0.0106x_1x_2 +0.0256x_1x_3 -0.0111x_1x_4 -0.0556x_2x_3 +0.0648x_2x_4 -0.0172x_3x_4$
Jul	CY_{t-1}	DA1	DA3				$18.7237 -0.3166x_1 +1.3310x_2 -3.0099x_3 -0.0030x_1x_2 +0.0024x_1x_3 +0.0054x_2x_3 +0.0001x_1^2 +0.0065x_2^2 -0.0065x_3^2$
Aug	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$59.2373 -0.6972x_1 +0.1791x_2 +5.1900x_3 -1.3783x_4 -6.9753x_5 +1.5471x_6 -0.0142x_1x_2 +0.0072x_1x_3 +0.1163x_1x_4 -0.1285x_1x_5 +0.0294x_1x_6 -0.3670x_2x_3 +0.0897x_2x_4 +0.2332x_2x_5 +0.0922x_2x_6 +0.3014x_3x_4 +0.3444x_3x_5 -0.4160x_3x_6 -0.5819x_4x_5 -0.0450x_4x_6 +0.3299x_5x_6$
Sep	CY_{t-1}	DA3	DA6				$44.8563 -0.4565x_1 +0.6884x_2 -1.9466x_3 +0.0053x_1x_2 -0.0005x_1x_3 +0.0012x_2x_3 +0.0004x_1^2 -0.0172x_2^2 -0.0002x_3^2$
Oct	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$76.1546 +0.0046x_1 -2.2220x_2 +1.0816x_3 +19.1690x_4 -53.2338x_5 +29.1398x_6 +0.0048x_1x_2 +0.0155x_1x_3 -0.0383x_1x_4 -0.0868x_1x_5 +0.1254x_1x_6 -0.0444x_2x_3 +0.0448x_2x_4 +0.0175x_2x_5 -0.0552x_2x_6 +0.2154x_3x_4 -1.0260x_3x_5 +0.7776x_3x_6 +3.2060x_4x_5 -3.3267x_4x_6 +11.6655x_5x_6 +0.0002x_1^2 -0.0547x_2^2 +0.1171x_3^2 +0.2874x_4^2 -7.7995x_5^2 -4.0845x_6^2$
Nov	CY_{t-1}	DA1	DA3	DA6	DA9		$30.0286 -0.4536x_1 -0.6721x_2 -0.8270x_3 -7.0981x_4 +5.3007x_5 -0.0339x_1x_2 +0.0086x_1x_3 +0.0107x_1x_4 -0.0084x_1x_5 +0.1347x_2x_3 +0.1123x_2x_4 -0.0596x_2x_5 +0.2355x_3x_4 -0.2262x_3x_5 -0.0117x_4x_5$
Dec	CY_{t-1}	DA1	DA3	DA6	DA9		$29.2005 -0.3816x_1 -0.6953x_2 +0.8469x_3 +1.2024x_4 -3.2563x_5 +0.0005x_1^2 -0.5339x_2^2 -0.0047x_3^2 -0.0119x_4^2 +0.0083x_5^2$

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Preprint. Discussion started: 24 November 2021

Table 5 PR models for predicting crop yield (CY) built for each month: region 2 (West Bengal). For each moth, it is indicated the input (x1 to x6) and the PR formula. DA stands for drought area.

Month	Input						PR model
	x_1	x_2	x_3	x_4	x_5	x_6	
Jan	CY_{t-1}	DA3	DA6	DA9	DA12		$8.5606 -0.2404x_1 -1.1236x_2 -0.7606x_3 +6.6535x_4 -5.3772x_5 +0.0087x_1x_2 -0.0044x_1x_3 -0.0182x_1x_4 +0.0234x_1x_5 +0.0080x_2x_3 +0.0234x_2x_4 -0.0037x_2x_5 -0.0402x_3x_4 +0.1648x_3x_5 +0.0200x_4x_5 +0.0001x_1^2 -0.0145x_2^2 -0.0657x_3^2 +0.0544x_4^2 -0.0952x_5^2$
Feb	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$-24.8742 -0.5460x_1 -0.1190x_2 +0.2175x_3 +0.7776x_4 -8.6335x_5 +6.4022x_6 -0.0164x_1x_2 +0.0095x_1x_3 -0.0251x_1x_4 +0.0262x_1x_5 -0.0057x_1x_6 -0.0179x_2x_3 -0.0241x_2x_4 -0.1705x_2x_5 +0.1579x_2x_6 +0.0064x_3x_4 +0.2383x_3x_5 -0.2779x_3x_6 -0.0117x_4x_5 +0.0266x_4x_6 +0.0614x_5x_6$
Mar	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$35.6904 -0.3835x_1 -0.9286x_2 +0.1960x_3 -0.3445x_4 -0.3559x_5 +0.6370x_6 -0.0025x_1x_2 -0.0009x_1x_3 +0.0111x_1x_4 -0.0252x_1x_5 +0.0144x_1x_6 -0.0059x_2x_3 +0.0426x_2x_4 +0.0063x_2x_5 +0.0012x_2x_6 -0.0362x_3x_4 -0.1287x_3x_5 -0.0038x_3x_6 +0.0242x_4x_5 -0.0355x_4x_6 +0.0394x_5x_6$
Apr	CY_{t-1}	DA3	DA6	DA9	DA12		$8.5856 -0.1865x_1 +1.5824x_2 -1.0816x_3 -1.0256x_4 +1.7846x_5 -0.0164x_1x_2 +0.0242x_1x_3 -0.0013x_1x_4 +0.0009x_1x_5 -0.0084x_2x_3 +0.0073x_2x_4 -0.0710x_2x_5 -0.0430x_3x_4 +0.0659x_3x_5 +0.0317x_4x_5$
May	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$-25.0101 -0.8233x_1 -1.8073x_2 +1.1145x_3 +1.6217x_4 +0.9651x_5 +0.5729x_6 +0.0254x_1x_2 -0.1198x_1x_3 +0.0959x_1x_4 -0.0112x_1x_5 +0.0311x_1x_6 -0.2178x_2x_3 +0.3465x_2x_4 -0.3214x_2x_5 +0.0602x_2x_6 -0.9192x_3x_4 +1.2301x_3x_5 -0.2167x_3x_6 -0.8955x_4x_5 +0.1015x_4x_6 +0.0662x_5x_6 +0.0048x_1^2 -0.0096x_2^2 +0.3527x_3^2 +0.4308x_4^2 -0.0492x_5^2 +0.0639x_6^2$
Jun	CY_{t-1}	DA1	DA3	DA6			$90.7623 -0.5785x_1 +0.1582x_2 -2.7914x_3 +0.8655x_4 -0.0176x_1x_2 +0.0093x_1x_3 -0.0108x_1x_4 +0.0533x_2x_3 -0.0521x_2x_4 +0.1589x_3x_4 +0.0012x_1^2 +0.0072x_2^2 -0.0974x_3^2 -0.0714x_4^2$
Jul	CY_{t-1}	DA1	DA3	DA6			$26.1164 -0.6892x_1 -0.6723x_2 -5.5280x_3 +4.6922x_4 +0.0070x_1x_2 +0.0111x_1x_3 -0.0148x_1x_4 -0.1301x_2x_3 +0.0838x_2x_4 +0.5157x_3x_4 +0.0014x_1^2 +0.0679x_2^2 -0.1671x_3^2 -0.3540x_4^2$
Aug	CY_{t-1}	DA1	DA3	DA6	DA9		$55.6167 -0.2284x_1 -0.0182x_2 -1.7996x_3 -4.0674x_4 +3.7965x_5 +0.0117x_1x_2 -0.0259x_1x_3 +0.0556x_1x_4 -0.0484x_1x_5 -0.0176x_2x_3 -0.1459x_2x_4 +0.1017x_2x_5 -0.0487x_3x_4 +0.2346x_3x_5 -0.1273x_4x_5$
Sep	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$35.6058 -0.3263x_1 +1.9755x_2 -0.4197x_3 -3.5963x_4 +2.7383x_5 -1.2234x_6 +0.0013x_1x_2 -0.0057x_1x_3 -0.0470x_1x_4 +0.0042x_1x_5 +0.0475x_1x_6 +0.0033x_2x_3 -0.1889x_2x_4 +0.0749x_2x_5 +0.1060x_2x_6 +0.0179x_3x_4 -0.0003x_3x_5 +0.0412x_3x_6 +0.0291x_4x_5 -0.0312x_4x_6 -0.0379x_5x_6$
Oct	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$7.7675 -0.1875x_1 -0.1476x_2 -0.8333x_3 -5.1327x_4 +15.3857x_5 -10.6323x_6 -0.0012x_1x_2 -0.0011x_1x_3 +0.0588x_1x_4 +0.0365x_1x_5 -0.0886x_1x_6 -0.1339x_2x_3 +0.1763x_2x_4 -0.5955x_2x_5 +0.4854x_2x_6 -0.4231x_3x_4 -0.2159x_3x_5 +0.6868x_3x_6 +0.3521x_4x_5 +0.0666x_4x_6 -0.4145x_5x_6$
Nov	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$38.3601 -0.2443x_1 +1.7236x_2 -0.6584x_3 -6.7484x_4 +13.3609x_5 -9.4895x_6 +0.0114x_1x_2 +0.0162x_1x_3 +0.0331x_1x_4 -0.0817x_1x_5 +0.0478x_1x_6 +0.0370x_2x_3 -0.1350x_2x_4 -0.0212x_2x_5 +0.1631x_2x_6 -0.1562x_3x_4 -0.0082x_3x_5 +0.1229x_3x_6 +0.2672x_4x_5 -0.0938x_4x_6 -0.1335x_5x_6$
Dec	CY_{t-1}	DA3	DA6	DA9	DA12		$24.769 -0.1091x_1 -2.9747x_2 +2.9990x_3 -5.4144x_4 +3.3374x_5 +0.0083x_1x_2 -0.0069x_1x_3 +0.0596x_1x_4 -0.0630x_1x_5 +0.0755x_2x_3 +0.0127x_2x_4 +0.0094x_2x_5 -0.0052x_3x_4 -0.0884x_3x_5 +0.0361x_4x_5$

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Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences
Open Access
EGU
Discussions

Table 6 PR models for predicting crop yield (CY) built for each month: region 3 (Odisha). For each moth, it is indicated the input (x1 to x6) and the PR formula. DA stands for drought area.

Month	Input						PR model
	x_1	x_2	x_3	x_4	x_5	x_6	
Jan	CY_{t-1}	DA3	DA6	DA9	DA12		$-149.3429 -0.4867x_1 -1.5749x_2 +2.0827x_3 +5.9761x_4 -6.0586x_5 -0.0022x_1x_2 +0.0100x_1x_3 +0.0200x_1x_4 +0.0045x_1x_5 -0.0142x_2x_3 -0.2414x_2x_4 +0.1392x_2x_5 -0.1332x_3x_4 +0.1123x_3x_5 +0.2083x_4x_5 +0.0022x_1^2 +0.0262x_2^2 +0.0771x_3^2 +0.0431x_4^2 -0.1405x_5^2$
Feb	CY_{t-1}	DA1	DA3	DA6			$-90.6767 -0.6674x_1 +0.1283x_2 +0.2580x_3 +0.4540x_4 -0.0041x_1x_2 +0.0141x_1x_3 -0.0009x_1x_4 +0.0055x_2x_3 -0.0195x_2x_4 +0.0771x_3x_4 +0.0006x_1^2 +0.0313x_2^2 -0.0207x_3^2 +0.0129x_4^2$
Mar	CY_{t-1}	DA6	DA9	DA12			$-168.6741 -0.7249x_1 +0.2079x_2 -2.2594x_3 +2.2421x_4 +0.0074x_1x_2 -0.0102x_1x_3 +0.0347x_1x_4 -0.0159x_2x_3 +0.0009x_2x_4 +0.1147x_3x_4 +0.0025x_1^2 +0.0454x_2^2 -0.0197x_3^2 +0.0318x_4^2$
Apr	CY_{t-1}	DA3	DA6	DA9	DA12		$-116.7973 -0.6789x_1 -0.4066x_2 -0.5459x_3 +3.4428x_4 -3.2126x_5 +0.0008x_1x_2 -0.0110x_1x_3 +0.0063x_1x_4 +0.0337x_1x_5 +0.0647x_2x_3 -0.1280x_2x_4 +0.0847x_2x_5 -0.0041x_3x_4 -0.1576x_3x_5 -0.0357x_4x_5 +0.0025x_1^2 -0.0386x_2^2 +0.0180x_3^2 +0.0968x_4^2 +0.1431x_5^2$
May	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$-56.0895 -0.8435x_1 -1.5688x_2 +5.5848x_3 -5.6556x_4 -0.0876x_5 -0.4449x_6 +0.0396x_1x_2 -0.0552x_1x_3 +0.0130x_1x_4 +0.0414x_1x_5 -0.0155x_1x_6 +0.0691x_2x_3 -0.1386x_2x_4 +0.4106x_2x_5 +0.0874x_2x_6 +0.2997x_3x_4 -0.2552x_3x_5 -0.4282x_3x_6 -0.0482x_4x_5 +0.2264x_4x_6 -0.2702x_5x_6 +0.0040x_1^2 -0.0721x_2^2 -0.0198x_3^2 -0.2076x_4^2 +0.2160x_5^2 -0.0223x_6^2$
Jun	CY_{t-1}	DA6	DA9	DA12			$-23.8562 -0.3639x_1 -1.8924x_2 -0.0052x_3 +1.3074x_4 -0.0060x_1x_2 -0.0057x_1x_3 +0.0205x_1x_4 -0.0135x_2x_3 -0.0965x_2x_4 +0.1034x_3x_4 +0.0004x_1^2 +0.0110x_2^2 -0.0171x_3^2 +0.0913x_4^2$
Jul	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$-18.8884 -0.7725x_1 +2.8997x_2 -1.9129x_3 -0.9194x_4 -0.5636x_5 -0.6886x_6 -0.0070x_1x_2 +0.0320x_1x_3 -0.0220x_1x_4 -0.0221x_1x_5 -0.0042x_1x_6 +0.3776x_2x_3 -0.0748x_2x_4 -0.1803x_2x_5 -0.2590x_2x_6 -0.5984x_3x_4 +0.6811x_3x_5 -0.0178x_3x_6 +0.8957x_4x_5 +0.0173x_4x_6 -0.1524x_5x_6 +0.0012x_1^2 -0.1151x_2^2 -0.1006x_3^2 -0.0306x_4^2 -0.7603x_5^2 +0.1200x_6^2$
Aug	CY_{t-1}	DA1	DA3	DA6	DA9	DA12	$4.8997 -0.7900x_1 -0.9225x_2 +3.8372x_3 -0.0832x_4 -9.7835x_5 +4.0199x_6 -0.0065x_1x_2 +0.0352x_1x_3 +0.0005x_1x_4 -0.0461x_1x_5 -0.0019x_1x_6 -0.0759x_2x_3 -0.1196x_2x_4 +0.1775x_2x_5 +0.0748x_2x_6 +0.0694x_3x_4 +0.2503x_3x_5 -0.3715x_3x_6 -0.2022x_4x_5 +0.4167x_4x_6 -0.2192x_5x_6$
Sep	CY_{t-1}	DA1	DA3	DA6	DA9		$41.4745 -0.5431x_1 -0.0366x_2 -0.9681x_3 +3.6023x_4 -4.3272x_5 -0.0002x_1x_2 +0.0115x_1x_3 -0.0191x_1x_4 +0.0139x_1x_5 -0.0809x_2x_3 +0.0508x_2x_4 +0.0205x_2x_5 +0.4602x_3x_4 -0.5016x_3x_5 +0.3000x_4x_5 +0.0002x_1^2 +0.0172x_2^2 -0.0339x_3^2 -0.3409x_4^2 +0.0831x_5^2$
Oct	CY_{t-1}	DA1	DA3	DA6			$-48.806 -0.6966x_1 -0.4241x_2 -1.7664x_3 -3.0097x_4 +0.0040x_1x_2 +0.0053x_1x_3 -0.0175x_1x_4 -0.0038x_2x_3 +0.0111x_2x_4 -0.1443x_3x_4 +0.0008x_1^2 +0.0073x_2^2 +0.0861x_3^2 +0.0558x_4^2$
Nov	CY_{t-1}	DA1	DA3	DA6			$47.8316 -0.6925x_1 +0.7765x_2 -2.3671x_3 -2.9813x_4 +0.0043x_1x_2 +0.0011x_1x_3 -0.0066x_1x_4 +0.0797x_2x_3 -0.0306x_2x_4 -0.0144x_3x_4 +0.0004x_1^2 -0.0064x_2^2 -0.0407x_3^2 +0.0200x_4^2$
Dec	CY_{t-1}	DA6	DA9				$13.0378 -0.5111x_1 +0.5765x_2 -3.4820x_3 +0.0177x_1x_2 -0.0158x_1x_3 +0.0155x_2x_3 +0.0004x_1^2 -0.0691x_2^2 +0.0343x_3^2$

4.5 ML modelling limitations

The limitations of the presented approach are the following.

(1) To determine drought areas, a threshold value of the Standardised Precipitation Evapotranspiration Index (SPEI) drought index (SPEI ≤ -1) was used. Using just one threshold might lead to over or underestimation of the actual drought impacts over crop yield.

(2) Gridded data of SPEI at spatial resolution (0.5°x0.5°) was used in this study over each region individually. Using such a coarse spatial resolution on different region sizes might not capture the drought area correctly, leading to over or underestimating its magnitude.

(3) The study area has a diverse ecosystem of irrigated and rain-fed land, which may influence the correlation between DA and crop yield more or less.

(4) This study assumes that drought is the only causative factor; however, floods negatively impact crop yield in the region, thus in the total production in the regions. Flood impacts are not considered in the models.

(5) Many other factors might influence rice yield, such as market, technologies, management, etc. In this study, it was assumed that drought plays the prominent role.

(6) Insufficient crop yield data for the ML model building was an issue because the CY time series only had one value for each year.

5 Summary and conclusions

This research introduced a step-by-step ML approach for predicting crop yield (CY) with drought areas (DAs) as input. The ML approach comprises two components. Each component employs two types of ML models: polynomial regression (PR) and artificial neural network (ANN). The goal was to build the ML models (ANN and PR) and use them as an integrated tool to crop yield prediction. The formulas of the PR models were also provided. The ML approach was applied in three East India regions.

The following conclusions are drawn from this research.

- Based on the performance of PR and ANN models, results show drought area to be a suitable variable to predict crop yield.
- The correlation analysis between DA and CY showed high negative correlations in Odisha (region 3). The correlation gradually decreases in Bihar and Jharkhand (region 1) and West Bengal (region 2). These correlation values can be because West Bengal has better access to irrigation facilities than Odisha and Bihar & Jharkhand.
- On comparing ANN models and PR models, the ANN were more accurate than PR models to predict crop yield for all regions. This could have been expected since the drought–crop relationship is a highly non-linear problem.
- It can be concluded that ANN has a high capability to predict CY in the pre-harvesting stage with good accuracy, considering the drought indicator used (SPEI), which uses climate variables such as precipitation and temperature (for evapotranspiration calculation).

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Preprint. Discussion started: 24 November 2021

Hydrology and Earth System Sciences
Discussions

From the analysis and findings of this research, the following recommendations can be provided for further improvement.

- Sensitivity analysis should be performed to identify the parameters that can impact the model results. For instance, different spatial resolutions of drought indicator and different thresholds should be investigated.
- Wet extreme events should be considered, especially in the flood-prone regions such as the coastal areas of West Bengal (region 2) and Odisha (region 3) and North Bihar (region 1), where floods also influence crop yield.
- Non-climatic factors such as econometric, fertilisers, and management practices might be considered because they influence crop yield.
- In order to improve the model accuracy, more input data should be used in further studies. For CY, this can be estimated by remote sensing techniques on a monthly basis so that the ML models can be built for this temporal resolution and the spatial coverage can be better addressed.
- The performance of other ML models has to be investigated, especially committee (ensemble) methods like random forests or boosting methods. In the case of data at scales less than monthly, the use of deep learning algorithms (e.g. LSTM networks) could be recommended to explore.

We envision that this research will improve drought monitoring systems for assessing drought effects. Since it is currently possible to calculate drought areas within these systems, the direct application of the prediction of drought effects is possible to integrate by following approaches such as the one presented or similar.

Coda and data availability

State-wise crop-yield data was retrieved through the Indian Directorate of Economic and Statistics from the Department of Agriculture (DAC) (http://eands.dacnet.nic.in/). The SPEI data was retrieved from the SPEI Global Drought Monitor (https://spei.csic.es). The code is available upon request from the corresponding author.

Competing interests

An author is member of the editorial board of journal HESS. The peer-review process was guided by an independent editor, and the authors have also no other competing interests to declare.

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