Evaporation from a large lowland reservoir – observed dynamics during a warm summer

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Abstract. Evaporation forms a large loss term in the water balance of inland water bodies. During summer seasons, which are projected to become warmer with more severe and prolonged periods of drought, the combination of high evaporation rates and increasing demand on freshwater resources forms a challenge for water managers. Correct parameterisation of open water evaporation is crucial to include in operational hydrological models to make well supported predictions of the loss of water through evaporation. Here, we aim to study the controls on open water evaporation of a large lowland reservoir in the Netherlands. To this end, we analyse the dynamics of open water evaporation at two locations, i.e. Stavoren and Trintelhaven, at the border of Lake IJssel (1100 km²) where eddy covariance systems were installed during the summer seasons of 2019 and 2020. From these measurements we find that wind speed and the vertical vapour pressure gradient, but not available energy, can explain most of the variability of observed hourly open water evaporation. This is in agreement with Dalton’s model which is a well-established model often used in oceanographic studies for calculating open water evaporation. At the daily timescale, we find that wind speed and water temperature are the main drivers in Stavoren.

These observed driving variables of open water evaporation are used to develop simple data-driven models for both measurement locations. Validation of these models demonstrates that a simple model using only two variables, performs well both at the hourly timescale (R² = 0.84 in Stavoren, and R² = 0.67 in Trintelhaven), and at the daily timescale (R² = 0.72 in Stavoren, and R² = 0.51 in Trintelhaven). Using only routinely measured meteorological variables leads to well performing simple data-driven models at hourly (R² = 0.78 in Stavoren, and R² = 0.51 in Trintelhaven) and daily (R² = 0.85 in Stavoren, and R² = 0.43 in Trintelhaven) timescales. These results for the summer periods show that global radiation is not directly coupled to open water evaporation at the hourly or even daily timescale, but rather wind speed and vertical gradient of vapour pressure are variables that explain most of the variance of open water evaporation. However, when we extend the time series to a complete year, we find a distinct yearly cycle reflecting the yearly dynamics of global radiation. We find that the commonly used model of Penman (1948) produces results that resemble the yearly cycle of observed evaporation. However, at the diurnal scale estimated evaporation using Penman’s model disagrees with observed evaporation. Therefore, using the Penman equation to model open water evaporation for shorter periods of time is questioned. We would like to stress the importance of including the correct drivers in the parameterization of open water evaporation in hydrological models to adequately represent the role of evaporation in the surface-atmosphere interaction of inland water bodies.
1 Introduction

Inland water bodies are known to interact with the local, regional and even global climate and are therefore highly sensitive to climate change (Adrian et al., 2009; Liu et al., 2009; Wang et al., 2018). Evaporation is a large loss term of water bodies and therefore it becomes most critical to understand how open water evaporation ($E_{\text{water}}$) will respond to these changing conditions, especially during summer seasons. During the summer season evaporation rates are highest and, depending on the functions of the water body, the water demand is largest for other purposes such as drinking water extraction and agricultural irrigation practices. Summers are projected to become warmer, with more severe and prolonged periods of drought (Seneviratne et al., 2006, 2012; Teuling, 2018; Christidis and Stott, 2021). Only if we are able to correctly parameterise $E_{\text{water}}$, implying that the employed model is right for the right reasons, it is possible to make well supported short-term predictions and long-term projections of $E_{\text{water}}$ during these critical summer periods. These predictions and projections could assist water managers to make appropriate decisions to guarantee ample access to freshwater.

In terms of thermodynamics an inland water body can be considered as a system that can be placed somewhere in between an ocean system, or another deep water body, and an infinite shallow water surface that behaves almost similar to a land surface. An important difference between these two systems at both ends of the spectrum is the location where heat is stored (Brutsaert, 1982; Kleidon and Renner, 2017). In the case of water bodies heat storage takes place below the atmosphere-water interface and is generally mixed away from the surface. This is different for a land surface, where heat is stored in the lower atmosphere, vegetation and the upper soil layers, leading to strongly increasing surface temperatures and warming of the lower atmosphere. This difference is rooted in the distinct surface properties and heat capacity of a water body and a land surface, which is leading to different dynamics of turbulent exchange with the atmosphere and is reflected at both the seasonal and daily cycle of latent heat flux (Brutsaert, 1982). In contrast to a land surface, solar radiation is able to penetrate through the water surface, thereby delivering and storing its energy down to deeper water layers, depending on the light absorption characteristics of the water. There, subsurface redistribution of energy can take place through turbulent mixing and non-turbulent flow of the water, and the energy can be released back into the atmosphere through sensible and latent heat fluxes. The subsurface energy exchange within a water body suggests that instead of focussing at the surface only, rather the whole volume of the system should be considered. It is essential to understand how differences in properties of a system result into distinct drivers of evaporation and to include and represent those in the parameterisation of evaporation in hydrological models.

The frequently used method of Penman (1948) is widely recognized as the standard for calculating both terrestrial evaporation and $E_{\text{water}}$ for shallow water surfaces for which the model was originally developed. Penman (1948) based his model on the historical model originally developed by Dalton in 1802. The latter model, and variations of it in the form of bulk transfer models, has been adopted and reviewed by many oceanographic studies and was found to perform well in estimating $E_{\text{water}}$ from oceans (Brutsaert, 1982; Josey et al., 2013; Pinker et al., 2014; Bentamy et al., 2017; Cronin et al., 2019). Dalton (1802) recognized the importance of using the gradient of vapour pressure at the water-air interface, where the exchange of water takes place, to model $E_{\text{water}}$. This gradient is subject to change when energy enters the water body, is stored, and released again, thereby changing the temperature and thus the vapour pressure at the water surface. Dalton (1802) proposed that $E_{\text{water}}$ can best
be described by the product of a wind function, acting as transport mechanism, and the gradient between the saturation vapour pressure at the water surface and the vapour pressure at 2 metres above the water surface. Penman (1948) eliminated the surface temperature, which is often difficult to determine, by assuming energy balance at the surface. This assumption results in the essential difference between the models of Dalton and Penman, where Dalton uses the vertical gradient of vapour pressure, while Penman uses the vapour pressure deficit at 2 metres height. Omitting the water heat flux (G) for infinitely shallow water surfaces reduces Penman’s model to a combination of a radiation term that is driven by net radiation and an aerodynamic term.

Most studies in the past have been dedicated to measuring terrestrial evaporation to understand its driving variables. However, measurements of $E_{\text{water}}$ from inland water bodies have remained under-represented. This can partly be attributed to practical difficulties when measuring above or close to a water body. There are numerous methods available to measure $E_{\text{water}}$ either through indirect estimations (e.g. water balance method, energy budget approach, bulk transfer method, complementary approaches) or through more direct measurements (e.g. scintillometry, eddy covariance technique, evaporation pan method) (Finch and Calver, 2008; Abtew and Melesse, 2013). Historically, evaporation pans have been widely used because of their relatively simple use and moderate data and installation requirements. However, depending on the installation method of the pan drawbacks that might be encountered are: adverse effects of heat exchange through the side walls, incomparable heat storage properties of the pan and a lake, limited temporal resolution, and splashing in or out of water caused by wind or rain (Allen et al., 1998; Sumner and Jacobs, 2005; Masoner and Stannard, 2010). Scintillometry, a technique that was developed more recently, enables us to quantify $E_{\text{water}}$ integrated over larger surfaces. Scintillometers therefore offer the possibility to account for spatial variability and comparisons with data obtained from satellite images (McJannet et al., 2011). However, scintillometers only indirectly measure the turbulent fluxes through the use of the Monin-Obukhov Similarity Theory (MOST) of which the assumptions do not always hold (Beyrich et al., 2012). In general, the eddy covariance technique is considered to be the most accurate method to quantify $E_{\text{water}}$ (Lenters et al., 2005). In contrast to scintillometry, eddy covariance is based on a point measurement with a smaller footprint at the hectare to square kilometer scale, depending on the meteorological conditions and the height of the sensor. It measures the vertical moisture flux through the covariance of the vertical wind speed and the concentration of water vapour. This concept renders it the most direct flux measurement technique available and it provides continuous observations suitable for studying the evaporation process.

In the past, a number of studies reported measurements of $E_{\text{water}}$ from which modelling concepts to estimate $E_{\text{water}}$ were developed. Some of these concepts are based on different drivers of evaporation and they disagree on the (meteorological) variables to be included. Some studies have for instance found that global radiation is not a direct driver of $E_{\text{water}}$ at shorter timescales and should therefore not be included in the parameterisation (Venäläinen et al., 1999; Blanken et al., 2011; Kleidon and Renner, 2017). Rather, the product of vapour pressure deficit (VPD) and wind speed should be used as argued by Blanken et al. (2000); Granger and Hedstrom (2011). Jansen and Teuling (2020) studied the (dis)agreement among a number of concepts that are commonly used. They found that the models of Penman (1948), Makkink (1957), De Bruin and Keijman (1979), Granger and Hedstrom (2011), Hargreaves (1975), and Mironov (2008) result in different representations of especially the diurnal cycle of evaporation. Additionally, at the yearly timescale the methods disagree on the average increasing historical
trend of the evaporation rate, as well as for the projected future trends. This underlines the importance of modeling $E_{\text{water}}$ using the correct process representation even more.

In the Netherlands measurements of $E_{\text{water}}$ have been under-represented as well, although measured by their extent ($\sim 17\%$ of the total area (Huisman, 1998)), inland water bodies form a crucial element in its water management system. Lake IJssel is the largest freshwater reservoir in the Netherlands fulfilling crucial hydrological functions, both in flood prevention and freshwater supply for agricultural irrigation and drinking water extraction. The water level of the lake is managed to have a distinct summer and winter level. This flexibility provides the opportunity to raise the water level before the start of the summer with typically higher evaporation rates. In this way, a buffer can be created to ensure that its functions can be fulfilled continuously throughout the summer season. Currently, the Dutch operational hydrological models use Makkink’s equation (Makkink, 1957) to quantify $E_{\text{water}}$ for Lake IJssel. Makkink is a radiation-based model which finds its origin in Penman’s equation through the Priestley-Taylor equation (explained in Sect.2.5) and has been developed to estimate evapotranspiration over well-watered grasslands at daily timescale. Although a correction factor is applied to account for the difference between terrestrial evaporation and $E_{\text{water}}$, Makkink’s equation is not able to capture the dynamics of $E_{\text{water}}$ as estimated with physically-based lake models such as FLake (Jansen and Teuling, 2020). This calls for improving and implementing our understanding of the driving process of $E_{\text{water}}$ by building on previous studies about $E_{\text{water}}$ of Lake IJssel (Keijman and Koopmans, 1973; De Bruin and Keijman, 1979; Abdelrady et al., 2016). The goal of our study is therefore to analyse the dynamics of $E_{\text{water}}$ of Lake IJssel supported by a data-driven analysis with the aim to parameterise $E_{\text{water}}$ based on its main drivers. To this end, we performed a long-term measurement campaign focussing on two summer periods (2019 – 2020) at two locations using the eddy covariance technique to measure $E_{\text{water}}$, along with observations of related meteorological variables over Lake IJssel in the Netherlands.

2 Data, Materials and Methods

2.1 Study area

In this research study the latent heat flux of Lake IJssel was analysed. Lake IJssel, also referred to as IJsselmeer in Dutch, is the largest freshwater lake in the Netherlands, bordering the provinces of Flevoland, Friesland, and Noord-Holland (see Fig. 1a). The lake covers an area of 1100 km$^2$ and is enclosed by the Afsluitdijk embankment in the north and by the Houtribdijk embankment in the south-west. With an average depth of 5.5 m and a maximum depth of 7 m, the lake can be considered a large shallow lake. The river IJssel is the main vein that supplies the lake with freshwater. Together with the inflow from the neighbouring polder systems the lake receives on average 340 m$^3$s$^{-1}$. Its main outflow occurs under gravity at the sluices of the Afsluitdijk where water is discharged to the Waddenzee. During summertime a flexible water level is used, which can vary between $-0.10$ m NAP (Normal Amsterdams Peil, the local sea level reference) and $-0.30$ m NAP. During wintertime the lake level should at least be kept at $-0.40$ m NAP. Lake IJssel fulfills an important hydrological role in the low-lying Netherlands, both in flood mitigation and in freshwater supply for agricultural and drinking water purposes. The flexible lake
Figure 1. Map of the study region and location of the measurement sites. The black dots in panel (a) represent the locations of the turbulent flux observations (Stavoren and Trintelhaven) and the locations where supplementary meteorological data was gathered by the Royal Netherlands Meteorological Institute (Stavoren and Lelystad). The orange triangles are the locations of water temperature measurements performed by Rijkswaterstaat. Black arrow indicates the location where water from the IJssel river enters Lake IJssel. Panels (b) and (c) illustrate the sampling area that is measured by the flux tower for onshore wind conditions by contour lines (20, 40, 60, and 80% from inside to outside). This was based on a flux footprint analysis using the model of Kljun et al. (2015). The circular inset on the bottom side of both panels indicates the wind directions that are included in the analysis of open water evaporation. At location Trintelhaven (c) this angle has shifted from the year 2019 to 2020 following the change of direction of the eddy-covariance instrument (see text). The circular inset at the top of both panels represents the average wind conditions as illustrated by a windrose.

level management during the year provides the water managers with a tool to respond to the meteorological conditions and the need for fresh water.

2.2 Site description, instrumentation and data

An eddy covariance (EC) measurement system was mounted in a telecommunication tower that is located at the shoreline in the city of Stavoren at the north-east coast of the lake (see Fig. 1a). Its favourable position in relation to the predominant south-westerly wind direction in combination with an already existing telecommunication tower renders this location suitable for the measurements needed to analyse the dynamics of open water evaporation. An additional benefit of this location is that it allows a comparison of the dynamics of terrestrial evaporation and open water evaporation by selecting time intervals based on the footprint of the flux tower. An open path-integrated gas analyser and sonic anemometer (IRGASON) from Campbell Scientific was installed at a height of 7.5 m above the land surface and was pointed towards 220°. The IRGASON measures the water vapour and CO2 concentration, air temperature by the sonic anemometer, barometric pressure, and the three wind components at a sampling frequency of 20 Hz. In addition, air temperature and relative humidity were both measured at 5.9 m and 7.4 m height using HMP155A sensors (Campbell Scientific).
In the harbour Trintelhaven located in the middle of the Houtribdijk embankment another telecommunication tower was equipped with the same EC system, installed at a height of 10.8 m above the surface. This location is surrounded by water with Lake IJssel on the east side and lake Marker on the west side of the embankment. The IRGASON pointed in a 240° direction for the summer period of 2019, and to 92° as of January 2020. The latter change maximized the suitable viewing angle of the IRGASON, taking into account the dominant wind direction and the position of the telecommunication tower and Lake IJssel. HMP155A sensors were used to measure the air temperature and relative humidity at two heights, namely 9.1 m and 10.9 m.

Practical issues precluded observations of the four radiation components and water temperature at the sites. Therefore, observations of global radiation were obtained from the automated weather stations in Stavoren and Lelystad employed by the Royal Netherlands Meteorological Institute (KNMI). The KNMI weather station in Lelystad is assumed to be representative for Trintelhaven. The sub-skin water temperature, used to estimate the water vapour pressure at the air-water surface, was retrieved from the hourly sub-skin Sea Surface Temperature product with 0.05° spatial resolution derived from the Meteosat-11 satellite. From this product, the grids belonging to the locations of Stavoren (52°53′06.2″N 5°21′04.1″E) and Trintelhaven (52°38′03.8″N 5°25′03.8″E) were retrieved. Data were only available during cloudless days. Furthermore, routinely measured water temperatures of Lake IJssel by the Directorate-General for Public Works and Water Management (Rijkswaterstaat) were retrieved. For this, the stations Friese Kust and Marker Wadden (orange triangles in Fig. 1a) were used, where the water temperature is measured at a depth of 1.5 m and 1.2 m below NAP, respectively.

### 2.3 Data processing

The analysis in this study is focussing on the data collected during the summer periods of 2019 and 2020. Latent heat flux (LE) and sensible heat flux (H) can be calculated using the covariance of vertical wind speed and specific humidity or temperature, respectively, as follows:

\[
LE = \rho_a L_v w' q',
\]

\[
H = \rho_a c_p w' T',
\]

where \( \rho_a \) [kg m\(^{-3}\)] is the air density, \( L_v \) [J kg\(^{-1}\)] is the latent heat of vaporization, \( c_p \) [J K\(^{-1}\) kg\(^{-1}\)] the specific heat of air at constant pressure, \( w \) [m s\(^{-1}\)] the vertical wind speed, \( q \) [kg m\(^{-3}\)] the specific humidity, and \( T \) [K] the air temperature.

For this, raw EC data were processed according to Foken et al. (2012). The processing steps were performed using the EddyPro software (EddyPro, 2021). This software package was chosen because it is widely used for processing eddy covariance measurements. The results compare well with the results directly obtained through the incorporated EasyFlux DL software made for the IRGASON (EasyFlux, 2017).

Firstly, it was tested if the raw data were faulty or corrupted based on a number of criteria. This included testing on completeness. If more than 5% of the high-frequency data of what is expected within the chosen averaging interval was missing it was flagged. Unrealistic values for each variable based on fixed individual thresholds were removed. Spikes were detected and
eliminated in accordance with the algorithm of Mauder et al. (2013). Furthermore, according to the approach of Vickers and Mahrt (1997) the data was screened on too many bad resolution records, and too many so-called dropouts referring to jumps in the data that continue over a longer period and therefore are not recognized as spikes. Density fluctuations were compensated using the WPL approach (Webb et al., 1980). If the signal strength of the gas analyzer falls below 70% the data was removed as well. Secondly, this quality checked dataset was further processed to obtain calculated raw fluxes. Next, coordinate rotation of the sonic anemometer using the double rotation method (Wilczak et al., 2001) was applied to correct for a not perfectly levelled sonic anemometer, and trends were removed using block averaging.

From this point, the final co-variances were calculated, which were subject to two essential tests as described by Foken et al. (2004), namely (i) to test stationarity during the averaging interval (30 min) and (ii) whether there are well-developed turbulent conditions such as required for proper usage of the Monin-Obukhov similarity theory. This yielded time series containing raw fluxes. As a final step, spectral corrections were applied to account for high and low frequency losses (Massman, 2000; Moncrieff et al., 2004), as well as the correction developed by Schotanus et al. (1983) to account for the humidity effect on the sonic temperature, which becomes specifically important for locations near water bodies. After iterating the last steps and incorporating the quality tests, a fully quality checked half-hourly flux dataset is obtained.

2.4 Flux footprint analysis

The flux footprint is computed to quantify the sampling area which contains the sinks and sources contributing to the measurement point and the relative contribution of each upwind location to the measured flux. In figures 1b and 1c the contour lines represent 20%, 40%, 60%, and 80% of the footprint area. This footprint analysis helps to make decisions on which wind directions to include in the analysis based on the area of interest. The size of the footprint depends on the measurement height, atmospheric stability and surface roughness (McGloin et al., 2014). In this study we have used the footprint model developed by Kljun et al. (2004) using the Flux Footprint Prediction (FFP) R code (Kljun et al., 2015). This footprint analysis showed that in Stavoren the flux data for wind directions between 163° and 349° are available for analysis of $E_{\text{water}}$, while the remaining wind directions represent the fetch over land and could therefore be used for comparison with terrestrial evaporation. At the Trintelhaven we were only interested in the fetch above Lake IJssel. Therefore, the flux data in Trintelhaven were removed for wind directions between 170° and 70° for the summer of 2019. After changing the direction of the IRGASON this yielded a larger angle from which data could be used during the summer of 2020, namely for wind directions between 0° and 170°. Given the dominant south-westerly wind direction, visualized with a windrose (inset at the top of both panels (b) and (c) in Fig. 1), this means that unfortunately a large part of the data had to be rejected at location Trintelhaven.

2.5 Regression model

A regression analysis was performed based on the observations in Stavoren and Trintelhaven to explore which variable, or combination of variables, can best explain the dynamics of $E_{\text{water}}$. To develop the data-driven model to estimate $E_{\text{water}}$ of Lake IJssel numerous variables were included, such as wind speed, VPD, global radiation, vertical vapour pressure gradient, air temperature and water temperature. These variables are generally considered to be important in describing $E_{\text{water}}$ and are
partially included in the models of Dalton and Penman. For each individual variable, as well as for all combinations of variables, both the sum and product, a regression model was created. In the regression analysis simple linear regression models (Eq. 3), multiple linear regression models (Eq. 4), and quadratic regression models (Eq. 5) were considered. The equations of these models are prescribed as:

\[ Y = \beta_0 + \beta_1 X_1 + \epsilon, \]  
\[ Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + ... + \beta_i X_i + \epsilon, \]  
\[ Y = \beta_0 + \beta_1 X_1 + \beta_2 X_1^2 + \epsilon, \]  

where \( Y \) is the dependent variable, \( X_i \) the explanatory variable(s), \( \beta_0 \) the intercept, \( \beta_i \) the parameter(s), and \( \epsilon \) the error term. The explanatory variable(s) \( X_i \) was prescribed to be either a single variable or the product of multiple variables, except for equation 4, where \( X_i \) can only be a single variable. From the multitude of regression models that is resulting from the regression analysis the best model was chosen, using the metrics \( R^2 \) and RMSE to evaluate the fit of each regression model. We not only aimed for finding the best model, but we were also interested to find the best simple model that uses maximum two variables, while still able to explain the dynamics of \( E_{\text{water}} \) well. The summer season of 2019, here taken as May – August, was used as the training dataset to calibrate the data-driven model, and the dataset of the summer of 2020 was used for validation. The analysis was performed at hourly and daily timescales.

The same procedure as described above was repeated but now solely using routinely measured observations. This was done to explore the possibility of using routine observations to make accurate estimations of \( E_{\text{water}} \), instead of continuing the labour intensive and expensive measurements with the eddy covariance systems. As described previously (see Sect. 2.2), data of automatic meteorological stations of the KNMI were used to obtain data of global radiation, complemented with air temperature, wind speed, and relative humidity that are routinely measured at these stations. Water temperature data at depths ranging from 1.2 to 1.5 m was obtained from routine measurements performed by Rijkswaterstaat and were used as a replacement for surface temperature because the latter is not routinely measured.

The resulting regression model was compared to the models of Dalton, Penman and Makkink (see Eq. 6, 8 and 9) to give an indication on the (dis)agreement of the variables involved in explaining the dynamics of \( E_{\text{water}} \) and its form. Dalton’s model is based on the empirical relationship that was found between evaporation and the product of a wind function and the vertical vapour pressure gradient, which can be written as:

\[ LE_{\text{Dalton}} = f(u)(e_s(T_0) - e_2), \]  

in which \( e_2 [\text{kPa}] \) is the vapour pressure at 2 m height, \( e_s(T_0) [\text{kPa}] \) is the saturation vapour pressure at the surface, and \( f(u) [\text{W m}^{-2} \text{ kPa}^{-1}] \) is the wind function which takes the following form (Penman, 1956; De Bruin, 1979):

\[ f(u) = 37 + 40u_2, \]  

in which \( u_2 [\text{m s}^{-1}] \) is the wind speed at 2 m height.
Similarly, Penman’s equation, which is derived from Dalton’s equation, can be written as:

\[ \text{LE}_{\text{Penman}} = \frac{\gamma}{s + \gamma} f(u) (e_s(T_2) - e_2) + \frac{s}{s + \gamma} Q^*, \]

(8)

in which \( s \) [kPa °C\(^{-1}\)] is the slope of the saturated vapour pressure curve at air temperature, \( \gamma \) [kPa °C\(^{-1}\)] the psychrometric constant, \( e_s(T_2) - e_2 \) [kPa] the vapour pressure deficit (VPD) at 2 m height, and \( Q^* \) [W m\(^{-2}\)] the available energy at the surface which can be defined as \( R_n - G \), where \( R_n \) [W m\(^{-2}\)] is net radiation and \( G \) [W m\(^{-2}\)] is the downward heat flux from the water surface.

Priestley and Taylor (1972) found that the aerodynamic term of Penman’s equation is approximately one-fourth of the radiation term. Makkink (1957) found that this equation could be simplified even more for estimating daily evapotranspiration from well-watered surfaces. Under these conditions \( G \) is assumed to be negligible and a constant ration between net radiation and global radiation of on average 0.5 can be assumed, which results in the following equation (Makkink, 1957):

\[ \text{LE}_{\text{Makkink}} = 0.65 \frac{s}{s + \gamma} K_{\text{in}}, \]

(9)

in which \( K_{\text{in}} \) [W m\(^{-2}\)] is the global radiation.

According to Penman’s derivation \( G \) is assumed to be negligible for shallow water surfaces, similar to land surfaces, and the term is often ignored because of the difficulty of measuring it. However, for water bodies of several metres depth the impact on the energy balance by neglecting \( G \) can be considerable (Tanny et al., 2008; van Emmerik et al., 2013). For these water bodies \( G \) should be considered as a result of temperature changes integrated over the volume of the water column in contrast to a land surface where the impact of \( G \) is more superficial. It should be clearly noted, that although Lake IJssel is a lake of several metres depth, we have neglected \( G \) in the following analyses in order to adhere to Penman’s original theory for (infinitely) shallow water surfaces.

3 Results

3.1 Data quality and quantity

To guarantee data quality of the flux measurements quality checks were performed as described in section 2.3. After the quality control 66% and 64% of the latent heat flux data were available in 2019 for Stavoren and Trintelhaven locations, respectively. In 2020 this number was lower with 49% and 59% for Stavoren and Trintelhaven, respectively. Part of the available quality checked data needed to be rejected based on the flux footprint analysis. This led to a reduced number of available data of 42% and 13% of total data in 2019 for Stavoren and Trintelhaven. In 2020 the total available latent heat flux data was 33% and 19% for Stavoren and Trintelhaven, respectively. The reduction of available data at Trintelhaven location is larger given the combination of the dominant south-westerly winds and the location of the instrument at the south-west border of Lake IJssel (see Fig. 1a). The number of total available flux data are at the lower end, but not unusual, of the data availability reported in other studies on lakes which is typically in the range of 16% – 59% (Vesala et al., 2006; Nordbo et al., 2011; Bouin et al., 2012; Mammarella et al., 2015; Metzger et al., 2018).
3.2 Meteorological conditions

Similar dynamics were observed at both locations Stavoren and Trintelhaven, therefore we only show the meteorological conditions observed in Stavoren (Fig. 2). Table 1 provides an indication of the source of the data for the variables that will be elaborated on in this section. According to the measurements of the KNMI both measurement stations received on average the same amount of global radiation for the period May – September 2019, namely: 208 W m\(^{-2}\) in Stavoren, and 204 W m\(^{-2}\) at Lelystad, the latter assumed to be representative for Trintelhaven. The average air temperature that we measured with the HMP155A sensor is lower in Stavoren (16.4 °C), than in Trintelhaven (18.0 °C). These temperatures are higher than the climatological mean observed by the KNMI (period 1991 – 2020) for the same months: 15.9 °C in Stavoren, 16.1 °C in Lelystad (KNMI, 2021a). The water temperature measured by Rijkswaterstaat in the vicinity of Stavoren was on average 17.9 °C, and the water at location Marker Wadden close to the Trintelhaven was on average 18.3 °C. The time series of water temperature shows a more smooth, attenuated and lagged signal compared to the air temperature. At both measurement locations the measured wind speed observed with the IRGASON is similar, with an average wind speed of 5.8 m s\(^{-1}\) in Stavoren and 5.6 m s\(^{-1}\) at Trintelhaven, without a distinct seasonal pattern. The vapour pressure that we measured follows the seasonal cycle of the air temperature, and has a mean value of 1.4 kPa in Stavoren and 1.6 kPa at Trintelhaven. In the bottom panel the observed turbulent fluxes are shown (Fig. 2e). The sensible heat flux remains consistently low throughout the summer period, with an average value of 17 W m\(^{-2}\) in Stavoren and 25 W m\(^{-2}\) at Trintelhaven. The latent heat flux is more than four times as high on average, with values of 88 W m\(^{-2}\) on average in Stavoren and 91 W m\(^{-2}\) in Trintelhaven. The latent heat flux displays similar dynamics as the measured wind speed, indicating a strong correlation between the two variables. Based on the average rates of sensible and latent heat flux the Bowen ratio is 0.19 in Stavoren and 0.27 at Trintelhaven.

Table 1. Sources of data used in this study. The variables measured at our locations in Stavoren at 7.5 m and Trintelhaven at 10.8 m were sampled at high frequency (20 Hz), and aggregated to hourly data. The data retrieved from KNMI stations in Stavoren and Lelystad are provided at hourly timescales and were measured at 1.5 m height above land surface, and 10-minute water temperature data measured by Rijkswaterstaat at locations Friese Kust at -1.5 m NAP and Marker Wadden at -1.2 m NAP were aggregated to hourly timescales.

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<th>Own observations</th>
<th>KNMI</th>
<th>Rijkswaterstaat</th>
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<td>(T_{water})</td>
<td></td>
<td>X</td>
</tr>
<tr>
<td>u</td>
<td>X</td>
<td></td>
</tr>
<tr>
<td>(e_z)</td>
<td>X</td>
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<tr>
<td>LE</td>
<td>X</td>
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</tr>
<tr>
<td>H</td>
<td>X</td>
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</table>
3.3 Diurnal and intra-seasonal variability of latent heat flux

The monthly average diurnal variability of observed LE, based on hourly data, are shown for the summer period of 2019 in the top panels of figure 3 for location Stavoren. The diurnal variability of LE does not have a strong diurnal cycle, but is rather constant throughout the day and night, which is in contrast to terrestrial evaporation which typically peaks during the day. Only in August the LE signal shows a distinct peak during the late afternoon and lower values during the night and early morning. The highest average diurnal LE is reached in July as indicated by the number in the top left-hand corner of each panel. Global radiation measured at the KNMI meteorological stations of Stavoren is shown in the middle panels. A clear distinctive diurnal cycle is visible with a peak in the afternoon, and the highest average value is found in June at both locations. The global radiation has served as input for the commonly used radiation-based models of Penman (1948) and Makkink (1957), of which the average diurnal cycles are shown in the lower panels of the same figures. Recall that G was omitted in Penman’s model in
Figure 3. Illustration of the decoupling in Stavoren in 2019 between monthly average diurnal cycles of observed latent heat flux (top) and global radiation (middle), the latter forming the basis of the frequently used evaporation models of Penman (1948) and Makkink (1957). These models are shown together with the model of Dalton (1802) at the bottom panels. Note that some variables included in the evaporation models are measured at larger heights than the 2 m that are prescribed (see Eq. 6 – 9). Additionally, all three models are generally used on a daily basis, but they are presented here to show the underlying daily cycle. The shaded area represents the uncertainty, which is defined as the standard deviation divided by the square root of the number of observations. Average daily means of the respective variables are indicated by the number at the top left of each panel displaying the average course over the summer period.

In contrast to observed LE which is found to be highest a month later. In the lower panels the average diurnal cycle of LE that follows from Dalton’s model is shown as well. There is no strong diurnal cycle visible, similar to the observed LE, but generally rates are highest during daytime. Highest average LE values are found in August. The observed monthly average diurnal dynamics observed were found similar in Trintelhaven, which is therefore not shown here.

Extension of the time series to a complete year in order to visualize the seasonal variability, shows a clear seasonal cycle that is reminiscent of the influence of a radiation component on $E_{\text{water}}$ (Fig. 4). The bars represent the monthly average $E_{\text{water}}$ rate based on hourly data. For the year 2019 the evaporation rate is highest in July for both locations: 4.3 mm d$^{-1}$ in Stavoren and 3.8 mm d$^{-1}$ in Trintelhaven. Lowest values are 0.2 mm d$^{-1}$ in Stavoren (February) and 0.6 mm d$^{-1}$ in Trintelhaven (December, note: data of January/February of 2019 is lacking). In 2020 similar rates are found in winter: 0.1 mm d$^{-1}$ in Stavoren (December) and 0.5 mm d$^{-1}$ in Trintelhaven (November), while the summer of 2020 now has a dip in July instead of being the peak.
Figure 4. Yearly cycle of observed open water evaporation in Stavoren (orange) and Trintelhaven (green) for both years 2019 and 2020. The bars indicate the monthly average evaporation and the whiskers represent the uncertainty, which is defined as the standard deviation divided by the square root of the number of observations.

3.4 Drivers of open water evaporation

Based on the historical theory it is known that governing factors of $E_{\text{water}}$ include the gradient of vapour pressure above the water surface and some measure for the strength of the turbulence (Dalton, 1802; Penman, 1948; De Bruin, 1979; Brutsaert, 1982). These variables form the ingredients of the so-called aerodynamic method or mass transfer approach (Brutsaert, 1982). Here we tested which variable or combination of variables can best explain the dynamics of observed $E_{\text{water}}$ at Lake IJssel at both hourly and daily temporal resolution. The variables included in this analysis are global radiation, vertical gradient of vapour pressure, vapour pressure deficit, sub-skin water temperature, and wind speed. These variables were chosen based on literature and data availability.

The proportion of the dynamics of $E_{\text{water}}$ that can be explained by the variable or combination of variables is shown in Venn diagrams with the adjusted coefficient of determination ($R^2$) written inside (see Fig. 5). The higher $R^2$, the more green the colour is. Venn diagrams (a) and (c) on the left-hand side illustrate the analysis based on hourly data, and the diagrams (b) and (d) on the right-hand side are based on daily data. The outer ‘leaves’ of the diagram represent the separate variables, while moving towards the centre of the diagram combinations of variables are taken into account to explain the dynamics of $E_{\text{water}}$. Both the sums and the products of the combined variables are analysed (Fig. 5 and Appendix A, respectively). Based on these diagrams, the decision was made which variables to include in the data-driven model to estimate $E_{\text{water}}$. The prominent green colour connected to wind speed already tells us that this is an important variable to include, which is in agreement with Dalton’s model and with the strong correlation visible in figure 2. Global radiation correlates least with $E_{\text{water}}$, which agrees with our findings in figures 2 and 3.
For both locations two models were developed, namely: (i) a model that includes the variable(s) that explains most of the variability of $E_{water}$, thus with the highest adjusted $R^2$, and (ii) a model that only uses one or two variables which are still able to explain a significant portion of the variability of $E_{water}$ (number depicted in red in the Venn diagrams). The highest $R^2$ is reached when the sum of (almost) all five variables are included. Considering the analysis based on hourly data we find that all variables except for global radiation have to be included to find the best model in Stavoren, which gives an $R^2$ of 0.74. In Trintelhaven all variables are included to find the best model with an $R^2$ of 0.71. Moving from the outer leaves towards the centre of the diagram, we find that the most simple model that still explains a large portion of the variance (red numbers in Fig. 5) includes only wind speed and vertical gradient of vapour pressure ($R^2$ is 0.70 in Stavoren, and 0.68 in Trintelhaven). This is again in agreement with Dalton’s model. The high $R^2$ values of these simple models, compared to models including more than two variables (Fig. 5), indicate that added value of using more than two variables is virtually nil. The results from the Venn diagrams form the base to create the data-driven models for which the data collected in 2019 is used. Both linear and quadratic regression models were considered as explained in section 2.5. The procedure described above was repeated, but now for daily aggregated data (Figures 5b and 5d). There we see a shift in which variables are included in the ‘simple’ model in the case of Stavoren. A combination of wind speed and water temperature reaches highest $R^2$ ($= 0.61$) in that case. In Trintelhaven wind speed and vertical gradient of vapour pressure are the variables included in the ‘simple’ model ($R^2 = 0.45$).

The results presented in the Venn diagrams are used to calibrate the regression models. Both the ‘simple’ and ‘best’ fitted model, based on hourly data and daily data, are presented in the top panels ((a) and (b)) of figures 6 (Stavoren) and 7 (Trintelhaven). The light coloured dots represent the simple model and the darker coloured dots the best model. In some cases the simple model is found to be the best model, which is then given in light coloured dots. The models found are validated using the data collected in 2020 and the results are presented in the lower panels ((c) and (d)) of the same figures. The high $R^2$ values in the validation give confidence in the performance of the models. Values of $R^2$ are in several cases higher in the validation period compared to the calibration period. This can be attributed to the lower variability in the data in the validation period. For reference, estimated daily evaporation rates using Makkink’s model are plotted as well because this model is currently used in the operational water management of Lake IJssel. Makkink’s model fails to explain the dynamics of $E_{water}$ on a daily temporal resolution with $R^2$ values near zero. For both locations the regression analysis based on hourly data has shown that the product of wind speed and vertical gradient of vapour pressure explains most of the variability of $E_{water}$. This confirms that the same physics applies to what was found at the two locations of Stavoren and Trintelhaven. The same ingredients are used in Dalton’s model. To determine if the coefficients found for the regression models of the two measurements locations significantly differ, an ANOVA statistical analysis was performed (not shown here). From this analysis we cannot rule out that the sites are different. This may be attributed to the difference in measurement height or the inherently different meteorological conditions we measure, because the two measurement sites are located on opposite sites of the lake.

The analysis as described above was repeated but now using only routinely measured observations of meteorological variables at 2 m height and water temperatures by KNMI and Rijkswaterstaat, respectively (Tables 2a and 2b). This was done to get to know the possibility of using these routine measurement to estimate $E_{water}$, instead of using the expensive and labour intensive eddy covariance instruments. The regression models found using these routine observations are, especially for the
Figure 5. Systematic exploration which variable or combination of variables can best explain the dynamics of open water evaporation. The outer ‘leaves’ of the Venn diagram represent the single variables, while moving towards the centre of the diagram the summed combination of variables are represented. Within each leaf the adjusted $R^2$ value is depicted. The higher this value, the greener the colour of the leaf. The red number indicates the highest $R^2$ value, indicating the best combination found for a maximum of two variables, i.e the best ‘simple’ model. The analysis is done at hourly timescale (left panels: Stavoren (a), Trintelhaven (c)) and daily timescale (right panels: Stavoren (b), Trintelhaven (d)).
location Stavoren, well able to explain the dynamics of $E_{\text{water}}$, where again wind speed and vertical gradient of vapour pressure are the main ingredients for the simple model ($R^2=0.83$ using hourly data and $R^2=0.66$ using daily data). Validation using data from summer 2020 also yields satisfactory results, with high $R^2$ of 0.78 and 0.85 for hourly and daily data, respectively. Again here, $R^2$ values during the validation period are higher in several cases which can be attributed to the lower variability in the data during that period compared to the calibration period. The results for the location of Trintelhaven fall short compared to Stavoren, with $R^2$ of 0.28 and 0.33 for hourly and daily data, respectively. The validation period does not yield satisfactory results either ($R^2=0.51$ using hourly data and $R^2=0.43$ using daily data). An explanation for these observations may be that the location of the routine observations is situated at a larger distance from the aimed location of Trintelhaven compared to Stavoren (Fig. 1a).
Figure 7. Evaluation of the developed ‘simple’ and ‘best’ data-driven models based on our own observations to estimate open water evaporation in Trintelhaven at hourly (a) and daily (b) timescales. The simple model was found to be the best model and is given light coloured dots. The model equations are shown in the top panels, which differ from the models found based on routinely measured observations (see Table 2b). Results of the validation of the models are presented in panels c and d for hourly and daily timescales, respectively. The light coloured dots illustrate the simple model, while the darker coloured dots illustrate the best model found. Results of estimated evaporation using Makkink’s model (light blue) is added to the validation plots as a reference. Model performance is indicated by the values of the coefficient of determination (R²) shown in each panel.

4 Discussion

Our results have shown that the diurnal cycle of observed $E_{\text{water}}$ shows a distinctively different pattern compared to evaporation estimated using the evaporation models of Penman (1948) and Makkink (1957). It should be reminded that in this study we have omitted $G$ in Penman’s model, corresponding to estimating $E_{\text{water}}$ for shallow water surfaces. The estimated evaporation by the models of Penman and Makkink resembles better the cycle that was observed at our station in Stavoren when we filtered on wind directions coming from the land surface, i.e. representing terrestrial evaporation (see Fig. 8). In contrast to the observed terrestrial evaporation, the observed $E_{\text{water}}$ is not directly coupled to (global) radiation at these time scales, which is demonstrated by the difference in diurnal variability between global radiation and observed LE (middle and upper panels of figure 3). A better agreement of the observed diurnal cycle was found for Dalton’s model, which is more constant throughout the day. Nevertheless, until now Makkink’s model has been used as a base for calculating $E_{\text{water}}$ at Lake IJssel (Jansen and...
Table 2. Evaluation of the developed ‘simple’ and ‘best’ data-driven models based on routinely measured observations (see Section 3.4) to estimate open water evaporation in Stavoren (Table 2a) and Trintelhaven (Table 2b) at hourly and daily timescales. These models presented here are independent of the results found based on our own observations. Results of estimated evaporation using Makkink’s model are provided as a reference. Model performance is indicated by the values of the coefficient of determination ($R^2$).

<table>
<thead>
<tr>
<th>(a) Stavoren</th>
<th>Model equation for calculating $LE_{mod}$</th>
<th>$R^2_{calibration}$</th>
<th>$R^2_{validation}$</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Hourly</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Simple data-driven model</td>
<td>$29.4, u\Delta e - 4.1$</td>
<td>0.83</td>
<td>0.78</td>
</tr>
<tr>
<td>Best data-driven model</td>
<td>$1.4, u\Delta e T_{water} + 2.8$</td>
<td>0.84</td>
<td>0.81</td>
</tr>
<tr>
<td><strong>Daily</strong></td>
<td></td>
<td></td>
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</tr>
<tr>
<td>Simple data-driven model</td>
<td>$26.5, u\Delta e + 11.0$</td>
<td>0.66</td>
<td>0.86</td>
</tr>
<tr>
<td>Best data-driven model</td>
<td>$18.8, u + 118.4, \Delta e + 63.0, VPD + 2.8, T_{water} - 157.3$</td>
<td>0.77</td>
<td>0.78</td>
</tr>
<tr>
<td>Makkink</td>
<td>$0.65, \frac{a}{\gamma + K_{in}}$</td>
<td>–</td>
<td>-0.02</td>
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<table>
<thead>
<tr>
<th>(b) Trintelhaven</th>
<th>Model equation for calculating $LE_{mod}$</th>
<th>$R^2_{calibration}$</th>
<th>$R^2_{validation}$</th>
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<tbody>
<tr>
<td><strong>Hourly</strong></td>
<td></td>
<td></td>
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</tr>
<tr>
<td>Simple data-driven model</td>
<td>$13, u + 98.1, \Delta e - 21.8$</td>
<td>0.28</td>
<td>0.51</td>
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<tr>
<td>Best data-driven model</td>
<td>$18.5, u + 128.6, \Delta e - 29.0, VPD - 42.0$</td>
<td>0.42</td>
<td>0.54</td>
</tr>
<tr>
<td><strong>Daily</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Simple/Best data-driven model</td>
<td>$22.0, u\Delta e + 0.5, (u\Delta e)^2 + 27.9$</td>
<td>0.34</td>
<td>0.44</td>
</tr>
<tr>
<td>Makkink</td>
<td>$0.65, \frac{a}{\gamma + K_{in}}$</td>
<td>–</td>
<td>0.003</td>
</tr>
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Teuling, 2020). We have shown that Makkink’s model is not able to explain the dynamics of $E_{water}$ for the summer period at the daily timescale. Such a radiation-based approach (including a potential linear correction factor) might lead to the correct daily or monthly evaporation sums, but it will be for the wrong reason.

Resulting from the data-based modelling that was performed we found that not radiation, but a combination of wind speed and vapour pressure gradient are the most important ingredients to explain the variance of $E_{water}$ at short timescales. This is similar to what has been found by studies of for instance Blanken et al. (2011) and McGloin et al. (2014), and the same ingredients that were used in the model by Dalton (1802). By combining and rearranging equations 6 and 7 we can write Dalton’s model in the following form:

$$LE_{Dalton} = 37\Delta e + 40u_2\Delta e,$$

in which $\Delta e$ [kPa] is $e_s(T_0) - e_2$ [kPa]. This highlights the similarity of the form of Dalton’s model and of our data-driven model that resulted from the regression analysis (see Fig. 6 and 7). When the exact form of equation 10, i.e. $LE = a\Delta e + bu_2\Delta e$, is fitted to our hourly observations of 2019, we find that coefficients $a$ and $b$ differ (not shown here). This difference is likely related to the height at which our measurements were done (10.8 and 7.5 metres above the surface in Stavoren and Trintelhaven, respectively) compared to the standard height of 2 metres. Although Penman’s model has been derived from Dalton’s model, we have found that it was not suitable for estimating $E_{water}$ over the summer period in the form that we have used it (i.e. with
Figure 8. Comparison of the average diurnal cycle of open water evaporation (blue) and terrestrial evaporation (orange) observed during the summer period 2019 in Stavoren. The shaded area represents the uncertainty band, which is defined as the standard deviation divided by the square root of the number of observations.

G omitted). However, when we extended the time series from only the summer period to the whole year a clear yearly cycle was visible, with a peak in summer that is similar to the cycle of (available) radiation, and thus to estimates of evaporation using Penman’s model (see Fig. 9a). The benefit of Penman’s model in this case is that it can easily be decomposed into an aerodynamic term and a radiation term. The individual terms are presented in figure 9b. Here a clear distinction between the yearly cycle of the two Penman terms is visible, where the radiation term has a distinct cycle with a peak in June, while the aerodynamic term is more constant over the year. This resembles the constancy of observed $E_{\text{water}}$ found in the diurnal cycle (see Fig. 3).

Linking back to the shorter time series spanning the summer months of May – August, we can see that there is even a simple linear relationship present between observed $E_{\text{water}}$ and the aerodynamic term of Penman’s model. In contrast, the variability of radiation is uncorrelated to observed $E_{\text{water}}$ (see Table 3). Correlation plots (not shown here) reveal that the variations within a month are as big or sometimes bigger than the yearly variations. Apparently, the effect of the seasonal cycle at this timescale is not dominating. When data was aggregated to daily temporal resolutions the correlations found between observed $E_{\text{water}}$ and the two Penman terms were very similar (not shown here). The high correlation between the aerodynamic term of Penman, which includes similar variables as Dalton’s model, and observed $E_{\text{water}}$ strengthens the finding that our data-driven model is embedded into the well-known theory. We are aware that using a statistical modelling approach has its limitations because it does not account for the actual physical processes the way that it might be included in physically-based models such as FLake (Mironov, 2008) for modelling lake evaporation. However, in such physically-based models empirical relations are included as well (e.g. the wind function in Dalton’s and Penman’s model) and parameters need to be statistically estimated. Furthermore, if drivers of open water evaporation appear to be a function of the temporal resolution, it should be concluded that models, including physical models, can only be properly used at the right temporal resolution. Considering this, we think that statistical modelling is a clean and simple approach that can provide a direct indication and insight of the most relevant input parameters involved in explaining the variation of evaporation, without making a priori assumptions on processes or relations that might
Figure 9. Comparison of the annual cycle of observed open water evaporation in Stavoren (orange) and estimated evaporation (blue) using Penman’s model (a). The individual terms of Penman’s model are displayed in the right panel (b), which shows the similarity of the annual cycle between observed open water evaporation and the radiation term of Penman’s model. The bars indicate the monthly average evaporation and the whiskers represent the uncertainty, which is defined as the standard deviation divided by the square root of the number of observations.

We argue therefore that our model is robust for applying to Lake IJssel and to other inland reservoirs of several metres depth in a similar climatic setting.

Table 3. Regression analysis between observed open water evaporation and estimated evaporation using Penman’s model, also broken down to the two individual terms of Penman’s model, i.e. the aerodynamic and radiation term. Analysis is performed for the summer period in 2019 using hourly observations of Stavoren.

<table>
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<tr>
<th>Penman</th>
<th>Regression model</th>
<th>$R^2$</th>
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<tbody>
<tr>
<td>Full Penman model</td>
<td>$0.08 \text{ Penman} + 93.5$</td>
<td>0.03</td>
</tr>
<tr>
<td>Aerodynamic term</td>
<td>$4.3 \text{ Penman}_{\text{aerodynamic}} - 13$</td>
<td>0.75</td>
</tr>
<tr>
<td>Radiation term</td>
<td>$0.05 \text{ Penman}_{\text{radiation}} + 99.1$</td>
<td>0.01</td>
</tr>
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The dynamics of the observed diurnal cycle of $E_{\text{water}}$ agrees to what has been found in studies of for example Tanny et al. (2008), Venäläinen et al. (1999), Granger and Hedstrom (2011) and Nordbo et al. (2011). Additionally, the estimated diurnal cycle by lake model FLake (Mironov, 2008) resembles well our observed $E_{\text{water}}$ (Jansen and Teuling, 2020). All of the studies above have found the occurrence of night-time evaporation as well. This indicates that heat which has been stored during the day, is being released during the night when the lake temperature exceeds the air temperature. The fluxes $LE$ and $H$ are a function of surface and air temperature and through the outgoing and incoming long-wave radiation $R_n$ is a function of surface and air temperature as well. As a consequence of the energy balance, this means that $G$ is also a function of temperature. Through the large heat capacity the system of a water body has a memory. Therefore the fluxes are not directly related to the instantaneous energy balance at the surface, which is how Penman’s model can be interpreted, but rather the fluxes are subject
to a delay following the large heat capacity of the water body. We argue that this effect of delay also leads to the different drivers that have been found at hourly and daily timescales in Stavoren. The volume of a water body of several metres deep with large heat capacity and three dimensional heat transfer through mixing, results in a fundamentally different system compared to a shallow water surface or land surface with different factors that drive evaporation (McMahon et al., 2013).

Not all the components of the energy balance could be measured during our field campaign. Therefore, the closure of the energy balance, which can be calculated as the ratio between the turbulent fluxes and available energy, could not be analysed. Other studies that were able to assess the energy balance closure (EBC) over lakes and/or reservoirs have found imbalances of the energy balance that were within a narrow range, and similar to those over land (Wilson et al., 2002). McGloin et al. (2014) found an average EBC value of 76% over a year, and found little variation over the seasons with a value of 77% for the summer season. Similar values of 82% and 72% for the summer seasons of 2006 and 2007, respectively, were found by Nordbo et al. (2011). A reasonable EBC of 91% was found by Tanny et al. (2008), although this was for a short period of 14 days. The measured imbalance suggests a general underestimation of the turbulent fluxes. Factors that could contribute to this imbalance are: large-scale transport (advection) of heat and water vapour, a systematic instrument bias, mismatch between the frequency of sampling and the turbulent eddies, mismatch of the measurement footprint of the individual terms, and neglected energy sources or sinks (Wilson et al., 2002; Foken, 2008; Mauder et al., 2013, 2020). Despite this likely underestimation of observed $E_{\text{water}}$ following the imbalance of the energy budget, we believe that this bias will not influence the dynamics of $E_{\text{water}}$ and the correlations found with other meteorological variables.

5 Conclusions

In this study, we investigated the dynamics of open water evaporation of Lake IJssel in the Netherlands. To this end, open water evaporation was measured during two summer periods at two locations using eddy covariance instruments. We have shown that the diurnal cycle of open water evaporation is distinctively different from terrestrial evaporation. This difference suggests that a water body is a different system by nature with its own characteristics compared to a land surface, which should be reflected in the parameterisation of open water evaporation. Based on the results of regression analysis, it was found that at hourly timescales wind speed and the vertical vapour pressure gradient are the main drivers of open water evaporation during the observed summer periods of 2019 and 2020. These variables are the same as used in Dalton’s model that is often used for estimating evaporation from deep water bodies. Using the data collected in 2019 data-driven models for both locations were set up ($R^2 = 0.74$ and $R^2 = 0.70$ for Stavoren and Trintelhaven, respectively). Validation of these models using the data collected during the summer of 2020 have shown that a simple data-driven model is able to explain large parts of the dynamics of open water evaporation ($R^2 = 0.84$ and $R^2 = 0.67$ for Stavoren and Trintelhaven, respectively). The absent correlation between observed daily open water evaporation and estimated evaporation using Makkink’s model has shown that this radiation-based model is unable to explain the dynamics of $E_{\text{water}}$, although this is current practice in the operational water management of Lake IJssel. Extension of the analysis from focussing on the summer period only to the full year has revealed a clear yearly cycle, which is reminiscent of the radiation term of Penman’s model. However, the aerodynamic term of Penman’s model
is more apparent in the diurnal cycle of open water evaporation. Applying the Penman model, where both the radiation and aerodynamic terms are combined, for inland water bodies at hourly or daily timescales is therefore questioned. Given the importance of $E_{\text{water}}$ in the large-scale water balance it is necessary that this process is incorporated correctly in hydrological models.

**Code and data availability.** The evaporation datasets of Stavoren and Trintelhaven are available on the 4TU data repository (doi: 10.4121/16601675). The code and accompanying data of the regression analysis is available on the 4TU data repository as well (doi: 10.4121/16913308). The KNMI datasets are available at https://www.knmi.nl/nederland-nu/klimatologie/uurgegevens (last access: 20 August 2021) (KNMI, 2021b). The water temperature datasets of Rijkswaterstaat are available at https://waterinfo.rws.nl/#!/kaart/watertemperatuur/ (last access: 20 August 2021) (Rijkswaterstaat, 2021). The sub-skin Sea Surface Temperature product of the Meteosat-11 satellite is available at https://osisaf.eumetsat.int/products/sea-surface-temperature-products (last access: 20 August 2021) (EUMETSAT, 2021). Codes are available upon request.

**Author contributions.** FAJ designed and carried out the study and field work under supervision of AJT, RU and CMJJ. All authors contributed to the interpretation of the results. FAJ wrote the manuscript and AJT, RU and CMJJ provided their feedback on the manuscript.

**Competing interests.** The authors declare that they have no conflict of interest.
References


Appendix A

Figure A1. Systematic exploration which variable or combination of variables can best explain the dynamics of open water evaporation. The outer ‘leaves’ of the Venn diagram represent the single variables, while moving towards the centre of the diagram the combination of products of variables are represented. Within each leaf the adjusted $R^2$ value is depicted. The higher this value, the greener the colour of the leaf. The red number indicates the highest $R^2$ value indicating the best combination found for a maximum of two variables, i.e. the best ‘simple’ model. The analysis is done at hourly timescale (left panels: Stavoren (a), Trintelhaven (c)) and daily timescale (right panels: Stavoren (b), Trintelhaven (d)).