

1 **On the similarity of hillslope hydrologic function: a clustering approach based**  
2 **on groundwater changes**  
3

4 Fadji Z. Maina<sup>1,2\*</sup>, Haruko M. Wainwright<sup>1</sup>, Peter James Dennedy-Frank<sup>1</sup>, Erica R. Siirila-  
5 Woodburn<sup>1</sup>

6 <sup>1</sup> Energy Geosciences Division, Lawrence Berkeley National Laboratory 1 Cyclotron Road, M.S.  
7 74R-316C, Berkeley, CA 94704, USA

8 <sup>2</sup>now at NASA Goddard Space Flight Center, Hydrological Sciences Laboratory, 8800 Greenbelt  
9 Rd, Greenbelt, 20771, MD, USA

10 \*Corresponding Author: fadjizaouna.maina@nasa.gov

11                    **Abstract**

12                    Hillslope similarity is an active topic in hydrology because of its importance to improve  
13 our understanding of hydrologic processes and enable comparisons and paired studies. In this  
14 study, we propose a holistic bottom-up hillslope clustering based on a region’s integrative  
15 hydrodynamic response quantified by the seasonal changes in groundwater levels  $\Delta P$ . The main  
16 advantage of the  $\Delta P$  clustering is its ability to capture recharge and discharge processes. We test  
17 the performance of the  $\Delta P$  clustering by comparing it to seven other common hillslope clustering  
18 approaches. These include clustering approaches based on the aridity index, topographic wetness  
19 index, elevation, land cover, and machine-learning that jointly integrate multiple data. We assess  
20 the ability of these clustering approaches to identify and categorize hillslopes with similar static  
21 characteristics, hydroclimate, land surface processes, and subsurface dynamics in a mountainous  
22 watershed, the East River, located in the headwaters of the Upper Colorado River Basin. The  $\Delta P$   
23 clustering performs very well in identifying hillslopes with 6 out of the 9 characteristics studied.  
24 The variability among clusters as quantified by the coefficient of variation (0.2) is less in the  $\Delta P$   
25 and the machine learning approaches than in the others ( $>0.3$  for TWI, elevation, and land cover).  
26 We further demonstrate the robustness of the  $\Delta P$  clustering by testing its ability to predict hillslope  
27 responses to wet and dry hydrologic conditions, of which it performs well when based on average  
28 conditions.

29                    **Keywords:** Hillslope, similarity, seasonal groundwater variations, integrated hydrologic  
30 modeling, hillslope clustering, hydrologic function

31 **1. Introduction**

32 The ability to delineate areas into spatially defined regions for their use in characterizing  
33 hydrologic flow and transport behavior is important for several reasons, including the assessment,  
34 monitoring, and modeling of water quantity and quality. Hillslopes are the scale at which  
35 hydrologic flow and transport processes can be tractably and frequently measured. It is also the  
36 scale at which flow and travel time are quantified, and the instrumentation, conceptualization, and  
37 modeling of hydrologic processes occur (Fan et al., 2019, Wainwright et al., 2022). While  
38 advancements have been made in the general understanding of hillslope dynamics over the last  
39 several decades, there is yet to be a globally agreed-upon classification and/or clustering for this  
40 important scale of interest in hydrology (McDonnell & Woods, 2004). Hydrologic signatures  
41 within hillslopes are the results of several simultaneous and nonlinear above- and below-ground  
42 processes. The uniqueness of a given location’s characteristics (for example, the topography,  
43 geology, vegetation, etc.) limits our ability to draw general hypotheses and to develop a similarity  
44 framework (Beven, 2000). Nevertheless, a classification is needed to provide guidance on  
45 catchments and hillslopes comparisons (McDonnell & Woods, 2004), paired studies (Andréassian  
46 et al., 2012; Bosch & Hewlett, 1982; Brown et al., 2005), and improve our understanding of the  
47 changes in hydrologic processes across the world. Further, hillslope similarity is potentially an  
48 important step toward developing reduced-order models and machine learning algorithms, where  
49 identifying regions based on their similarities can substantially reduce computational costs  
50 (Chaney et al., 2018). The scaling of hillslope to catchment classifications can also be useful in  
51 the prediction of hydrologic behavior in ungauged basins (Sivapalan et al., 2003), an exceedingly  
52 important challenge.

53 Hillslope similarity clustering approaches include the Topographic Wetness Index TWI  
54 (Beven & Kirby, 1979), which was proposed to quantify the topographic control on hydrology as

55 topography plays a key role in the movement of water. Many other variants of this index have been  
56 later proposed to improve the definition of topographic similarity (Grabs et al., 2009; Hjerdt et al.,  
57 2004; Loritz et al., 2019). Other clustering approaches are based on hydroclimate (Carrillo et al.,  
58 2011), soil type and texture (Bormann, 2010), and land cover type (e.g., forest, urban, etc.  
59 (Wagener et al., 2007)). These indices assume that hillslopes with similar topography and land  
60 cover will have similar hydrologic responses. However, given that hydrologic processes are  
61 governed by many characteristics of the hillslope, clustering approaches relying on multiple  
62 landscape characteristics have also been proposed (Aryal et al., 2002; Sawicz et al., 2011). These  
63 top-down clustering approaches assume that areas with similar physical characteristics will lead  
64 to similar hydrologic processes (Oudin et al., 2010). Other clustering approaches use a bottom-up  
65 approach, where similarity is based on the hydrologic process. This clustering allows the  
66 estimation of the “hidden” hillslope characteristics such as soil texture, and geology that may drive  
67 similar hydrologic responses (Carrillo et al., 2011). Among the process-based clustering  
68 approaches existing in the literature we can cite: the Péclet number characterizing the diffusive  
69 and advective transfer of water at hillslope scale (Berne et al., 2005; S. W. Lyon & Troch, 2007;  
70 Steve W. Lyon & Troch, 2010) and the catchment seasonal water balance (Berghuijs et al., 2014).  
71 Other authors have derived hillslope similarities from subsurface flow dynamics (Harman &  
72 Sivapalan, 2009).

73         One challenge in developing a similarity framework is the inherent heterogeneity of a given  
74 hillslope. For example, Snow Water Equivalent (SWE), infiltration (I) and actual  
75 evapotranspiration (ET) distributions can range over an order of magnitude within a single  
76 hillslope (Wainwright et al., 2022). Defining a single integrative measure that can capture this  
77 spatio-temporal variability is difficult. However, groundwater fluctuations are often tightly linked



78 to seasonal changes in climate and have been shown to play an important role in surficial processes  
79 such as ET (Maina et al., 2022; Maina & Siirila-Woodburn, 2020; Maxwell & Condon, 2016).  
80 Thus, groundwater measures may serve as a good proxy for the aggregated hydrologic response.  
81 Groundwater dynamics could help overcome the issue of uniqueness of place because even if there  
82 are strong differences in the characteristics of the hillslope, the integrated response may be similar  
83 as some of the processes might not be important. Finally, the implications of groundwater changes  
84 are also important. For example, many regions are characterized by groundwater-dependent  
85 ecosystems or are hypothesized to have water table fluctuations affecting bedrock weathering rates  
86 and therefore the concentration and fluxes of metals and nutrients exports (e.g., Winnick et al.,  
87 2017).

88 In this study, we define a holistic bottom-up hillslope clustering using the integrative  
89 hydrologic response quantified by the seasonal changes in groundwater levels. A caveat to this  
90 clustering is that groundwater dynamics are difficult to quantify, and their measurements are  
91 frequently scarce. Hence, there are very few studies that use this variable to develop a hillslope  
92 similarity classification (Aryal et al., 2002; S. W. Lyon & Troch, 2007). However, today, thanks  
93 to advances in integrated hydrologic modeling (Brunner & Simmons, 2012; Maxwell & Miller,  
94 2005), accurate quantification of the groundwater dynamics at high resolution in both time and  
95 space, as well as their interaction with the key land surface processes and features, is now feasible.  
96 These models (e.g., HydroGeoSphere (Brunner and Simmons, 2012), ParFlow (Maxwell & Miller,  
97 2005), Advanced Terrestrial Simulator, (Coon et al., 2016)) that can be constrained with ground  
98 observations and measurements at ultra-high resolutions through aerial or remote sensing (i.e.,  
99 drones, planes, or satellites) account for the two-way interactions between groundwater and land  
100 surface processes. Spatially resolved hydrologic flow models also enable us to jointly quantify

101 other hydrologic variables useful to identify hillslope with similar hydrologic responses, namely  
102 trends in ET, SWE, and I. Nevertheless, we acknowledge that groundwater dynamics in some  
103 regions such as arid areas could be disconnected to land surface processes and less dependent to  
104 many key physical features of the hillslope, which may impede the ability of the proposed  
105 clustering in these regions.

106 We test the proposed hillslope clustering on the site of the Department of Energy's (DOE)  
107 Watershed Function Scientific Focus Area (SFA) located in the headwaters of the Upper Colorado  
108 River Basin. The East River watershed is not only representative of many headwater catchments  
109 in the western United States in terms of its spatial heterogeneity of above and below-ground  
110 characteristics but also serves as an important proxy of water quantity and quality trends which  
111 ultimately impact a large population of water supply in the western United States for municipal,  
112 agriculture, and industrial use (Hubbard et al., 2018). We test the robustness of the proposed  
113 hillslope clustering by comparing it to seven other common hillslope clustering approaches based  
114 on the aridity index (AI), TWI, elevation, land cover and machine-learning approaches that jointly  
115 integrate multiple input data layers such as elevation, land cover, and geology, and model outputs  
116 including ET, and SWE. We assess the ability of these clustering approaches to identify and  
117 categorize hillslopes with similar physical characteristics (land cover and elevation), hydroclimate  
118 (precipitation and temperature), land surface processes (ET and SWE), subsurface dynamics (soil  
119 saturation, water table depth WTD, and seasonal changes in groundwater). We aim to provide  
120 answers to the following questions:

- 121 • What are the best clustering approaches for identifying hillslopes with similar  
122 hydrologic processes?

- 123                   • Is a similarity index based on the seasonal groundwater variations sufficient to  
 124                   capture all the complex processes taking place at a hillslope scale?

125

126                   **2. Methodology**

127                   **2.1. Modeling framework**

128                   **2.1.1. Selected integrated hydrologic model: ParFlow-CLM**

129                   We use the integrated hydrologic model, ParFlow, which has the advantages of simulating  
 130                   the water and energy balance from the bedrock to the lower atmosphere and therefore connect  
 131                   groundwater dynamics with land surface processes. ParFlow solves the subsurface flow using the  
 132                   three-dimensional mixed form of the Richards equation (Richards, 1931) given by the following  
 133                   equation:

$$134 \quad S_S S_W(\psi_P) \frac{\partial \psi_P}{\partial t} + \phi \frac{\partial S_W(\psi_P)}{\partial t} = \nabla \cdot [K(x) k_r(\psi_P) \nabla(\psi_P - z)] + q_s \quad (1)$$

135                   Where is  $S_S$  the specific storage [ $L^{-1}$ ],  $S_W(\psi_P)$  is the degree of saturation [-] associated  
 136                   with the subsurface pressure head  $\psi_P$  [L],  $t$  is the time [T],  $\phi$  is the porosity [-],  $k_r$  is the relative  
 137                   permeability [-],  $z$  is the depth [L],  $q_s$  is the source/sink term [ $T^{-1}$ ] and  $K(x)$  is the saturated  
 138                   hydraulic conductivity [ $L T^{-1}$ ] which is assumed to be a diagonal tensor with entries given as:  
 139                    $k_x(x)$ ,  $k_y(x)$  and  $k_z(x)$ . We assumed in this work that the domain is isotropic, and that the tensor  
 140                   is equal to 1 for all the three directions at each cell of the discretized model. In the unsaturated  
 141                   zone, both  $S_W$  and  $k_r$  depend on the  $\psi$ . The relationships between  $S_W$  and  $k_r$  and  $\psi$  are described  
 142                   by the van Genuchten model (van Genuchten, 1980).

143                   Overland flow (equation 2) is solved by the kinematic wave equation in two dimensions.

$$144 \quad -k(x) k_r(\psi_0) \nabla(\psi_0 - z) = \frac{\partial \|\psi_0, 0\|}{\partial t} - \nabla \cdot \vec{v} \|\psi_0, 0\| - q_r(x) \quad (2)$$

145                   Where  $\psi_0$  is the ponding depth,  $\|\psi_0, 0\|$  indicates the greater term between  $\psi_0$  and 0,  $\vec{v}$  is  
 146                   the depth averaged velocity vector of surface runoff [ $L T^{-1}$ ],  $q_r$  is a source/sink term representing

147 rainfall and evaporative fluxes [L T<sup>-1</sup>]. Surface water velocity at the surface in  $x$  and  $y$  directions,  
148 ( $v_x$ ) and ( $v_y$ ) respectively, is computed using the following set of equations:

$$149 \quad v_x = \frac{\sqrt{S_{f,x}}}{m} \psi_0^{\frac{2}{3}} \text{ and } v_y = \frac{\sqrt{S_{f,y}}}{m} \psi_0^{\frac{2}{3}} \quad (3)$$

150 Where  $S_{f,x}$  and  $S_{f,y}$  friction slopes along  $x$  and  $y$  respectively and  $m$  is the manning's coefficient.  
151 ParFlow employs a cell-centered finite difference scheme along with an implicit backward Euler  
152 scheme and the Newton Krylow linearization method to solve these nonlinear equations. The  
153 computational grid follows the terrain to mimic the slope of the domain (Maxwell, 2013).

154 ParFlow is coupled to the Community Land Model (CLM, (Dai et al., 2003)) which allows  
155 for the simulation of important land surface processes such as ET and SWE and the quantification  
156 of water leaving or entering the surface and subsurface ( $q_s$  and  $q_r$  respectively in the Richards and  
157 kinematic wave equations). CLM models the thermal processes by closing the energy balance at  
158 the land surface given by:

$$159 \quad R_n(\theta) = LE(\theta) + H(\theta) + G(\theta) \quad (4)$$

160 Where  $R_n$  is the net radiation at the land surface [E/LT] a balance between the shortwave  
161 and longwave radiation,  $LE$  is the latent heat flux [E/LT] which captures the energy required to  
162 change the phase of water to or from vapor,  $H$  is the sensible heat flux [E/LT] and  $G$  is the ground  
163 heat flux [E/LT]. All terms are a function of  $\theta$ , the water content, which is computed by ParFlow.

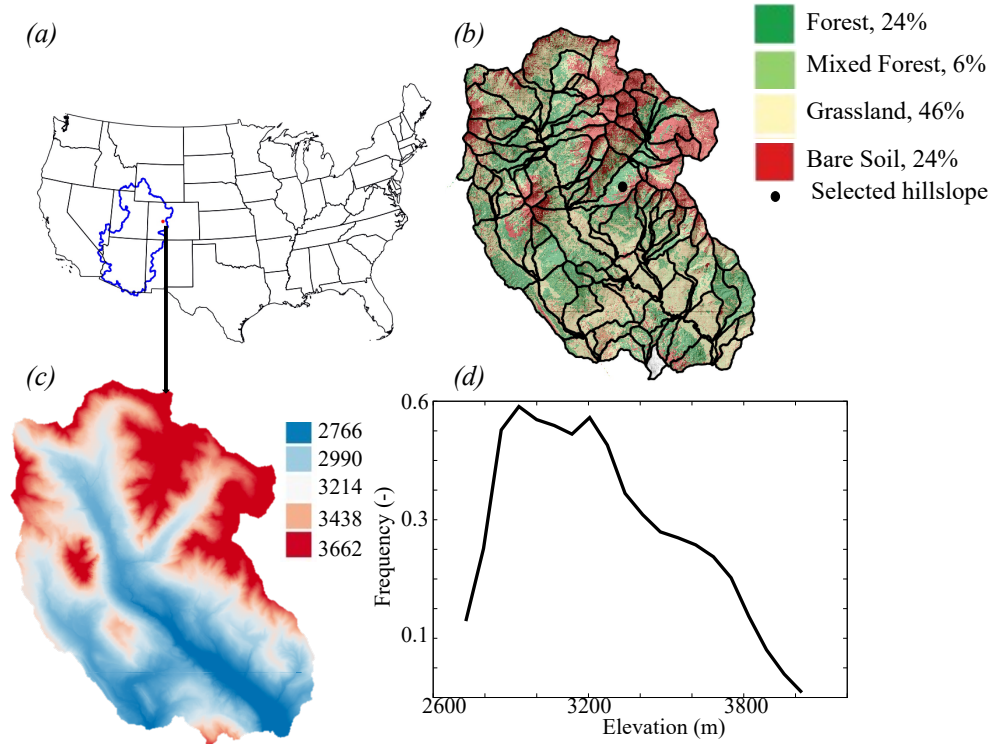
164 Computing the different components of the energy balance requires meteorological  
165 forcing, vegetative parameters, and soil moisture. The latter is computed by ParFlow using  
166 equations 1 and 2. Meteorological forcing includes precipitation, temperature, east to west and  
167 north to south wind speed, longwave and shortwave solar radiation, air pressure, and relative  
168 humidity. Vegetative parameters include maximum and minimum leaf area index, stem area index,  
169 aerodynamic roughness height, optical properties, stomatal physiology, roughness length, and

170 displacement height. More details about the coupling between ParFlow and CLM as well as the  
171 equations governing the snow dynamics and *ET* can be found in the following papers: Jefferson et  
172 al., (2015); Maxwell & Miller, (2005); Ryken et al., (2020). ParFlow-CLM has been used in many  
173 studies to understand the interactions between groundwater dynamics and lower atmosphere  
174 (Maina et al., 2022; Maina and Siirila-Woodburn, 2020) at different scales from watershed (Foster  
175 and Maxwell, 2019; Maina et al., 2020) to continental scale (Maxwell and Condon, 2016).

176  
177  
178  
179

**2.1.2. East River watershed model set-up**

The East River watershed (Figure 1), located in the Upper Colorado Basin, is one of the  
180 two major tributaries that form the Gunnison River, which in turn accounts for just under half of  
181 the Colorado River's discharge at the Colorado-Utah border. The total area of this watershed is  
182 approximately 255 km<sup>2</sup> and the elevation varies from approximately 2700 to 3900 m. The  
183 watershed is characterized by strong heterogeneities in vegetation, geomorphology, and bedrock  
184 composition (Hubbard et al., 2018). The vegetation includes grasses, conifers, mixed conifers,  
185 aspens, and meadows and lies on a complex geologic terrain, which is comprised of a diverse  
186 collection of Paleozoic and Mesozoic sedimentary and unconsolidated rocks. The watershed is  
187 also characterized by a strong hydroclimate gradient. The average precipitation is 1200 mm/year  
188 while the average temperature is around 0°C. Because of its very low cold winter with temperature  
189 below 0°C, most of the winter precipitation is in the form of snow.



190  
 191 Figure 1: (a) location of the East River watershed, (b) land cover (NEON dataset, 2020), (c) LiDAR  
 192 Digital elevation, and (d) elevation distribution within the East River.

193  
 194 ParFlow-CLM used here is based on a previous version of the East River watershed model,  
 195 as described by Foster and Maxwell (2019). 5 layers constitute the model in the vertical direction  
 196 with varying thickness from 0.1 m at the land surface to 21 m at the bottom of the domain. The  
 197 land use and land cover are derived from the high-resolution airborne remote sensing NEON  
 198 campaign (Chadwick, et al., 2020; Falco, et al., 2019; Goutlten, et al., 2020). From the  
 199 hyperspectral spectrometer and LiDAR readings, 4 major types of land cover are grouped as  
 200 follows: forests (i.e., conifers and aspens), mixed forests, grasses, and bare soil. Parameterization  
 201 of these different land cover types is derived from the IGBP database (IGBP, 2018).

202 The subsurface of the study area is heterogeneous in both vertical and horizontal directions.  
 203 The subsurface of the top 1 m corresponds to three soil layers as defined by the SSURGO database

204 and then corrected based on the land cover and geologic maps to include the outcropping of the  
205 bedrock. Two main types of soil are distinguished within the area: sandy loam and clay loam. The  
206 geology of the subsurface between 1 m and 8 m below the ground was defined with USGS maps,  
207 which were further improved by local knowledge by Pribulick et al., (2016). This subsurface  
208 region is highly heterogeneous with different formations such as crystalline, sedimentary rocks,  
209 unconsolidated rocks, alluvial deposits, and debris flow. The bottom layer of the domain  
210 (extending from 8 m below the ground surface to the bottom of the model) is assumed  
211 homogeneous and represents the fractured bedrock.

212 We simulated the water year (WY) 2015, a relatively average WY in the region based on  
213 average precipitation and temperature patterns. The meteorological forcing of the model has a  
214 resolution of an hour and is derived from two gridded datasets: PRISM and NLDAS. The PRISM  
215 dataset (Daly et al., 2008) is used for precipitation and temperature because of its accuracy and  
216 high spatial resolution (800m). However, the daily resolution of PRISM impedes its ability to be  
217 used to reproduce diurnal cycles, an important factor when studying land surface processes  
218 requiring hourly forcing. The phase 2 of the North America Land Data Assimilation System  
219 NLDAS-2 forcing (Cosgrove et al., 2003) on the contrary provides hourly changes in precipitation  
220 and temperature yet are only available at coarser, 1/8 degree, resolutions. As such, we employ a  
221 mass-conservative temporal interpolation, which disaggregates the total daily PRISM precipitation  
222 into an hourly time series based on the signal of the NLDAS-2 precipitation and temperature  
223 trends. For the other forcing variables (i.e., shortwave and longwave radiation, wind speed,  
224 atmospheric pressure, and specific humidity), we use NLDAS-2 forcing, (Cosgrove et al., 2003).  
225 Simulated river stages and SWE were compared to observations in previous studies (Maina et al.,  
226 2022; Foster and Maxwell, 2019). Groundwater measurements are scarce in the watershed and the

227 majority of the measurements are performed near a station measuring changes in river stages.  
228 Therefore, river stages and groundwater measurements at this point provide similar information.

## 229 **2.2. Hillslopes delineation**

230 As shown in Figure 1b, 127 hillslopes are delineated in the East River watershed based on  
231 the elevation following (Noël et al., 2014) and using Topotoolbox developed by (Schwanghart &  
232 Scherler, 2014). A threshold of flow accumulation was set to match the stream observations at  
233 major tributaries of the East River (Carroll et al., 2018). Because the hillslope delineation could  
234 be sensitive to the threshold of the drainage area, we tested different threshold values to find that  
235 the selected threshold value (810,000 m<sup>2</sup>) represents the scale of hillslope at which the within-  
236 hillslope variability of key properties (such as elevation and aspect) is minimized and hillslope-  
237 averaged properties can account for the majority of watershed-scale variability (Wainwright et al.,  
238 2022).

## 239 **2.3. Hillslopes clustering approaches**

240 We use eight hillslope clustering approaches:

- 241 1. The  $\Delta P_1$  clustering, proposed in this study, identifies hillslopes with similar groundwater  
242 dynamics. Figure 2 shows the temporal variations of the simulated SWE and WTD at a  
243 selected hillslope (see its location in Figure 1). All hydrologic variables have been  
244 computed at a hillslope scale by computing the arithmetic average of all cells in each  
245 hillslope. In this mountainous watershed, where the largest changes in WTD are mostly a  
246 result of snowmelt, WTD decreases from the beginning of the WY (i.e., October) to the  
247 beginning of snowmelt (i.e., starting from April). As the snow starts to melt and  
248 precipitation starts to fall as rain instead of snow, WTD starts to rise. The shallowest WTD  
249 is June and July when the snow has completely melted and has had time to percolate

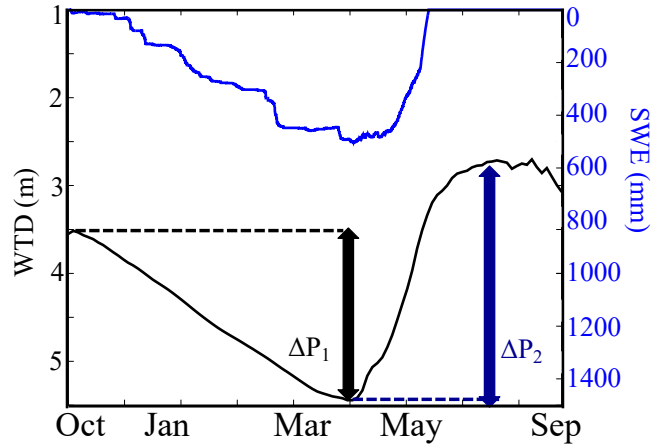


250 through the unsaturated zone into the groundwater. This period also corresponds to the  
251 period of high ET, because both the evaporative demand and the water availability are high.  
252 The dynamics show two periods characterize the dynamics of the hillslope: from the initial  
253 conditions to the baseflow conditions when the hillslope is losing water, then from  
254 baseflow conditions to the peak of WTD when the hillslope is gaining water. To  
255 characterize these groundwater dynamics, we define two variables:

- 256 •  $\Delta P_1$  represents the change in WTD between the beginning of the water year and the  
257 deepest WTD during the baseflow conditions. This variable quantifies the amount  
258 of water released by the hillslope during the dry period at the beginning of the water  
259 year. It thus contains information about the amount of water that the hillslope  
260 typically releases/loses, mainly by ET and discharge, given its physical  
261 characteristics and climate dynamics.
- 262 •  $\Delta P_2$  represents the changes in WTD between the peak flow (i.e., the period with the  
263 shallowest WTD) and the baseflow conditions.  $\Delta P_2$  quantifies the amount of water  
264 gained in the hillslope by recharge, and thus contains information about the  
265 recharge ability of the hillslope given its physical characteristics and climate  
266 dynamics.

267 These two key variables allow us to quantify water release ( $\Delta P_1$ ) and recharge ( $\Delta P_2$ ) within  
268 a hillslope, two key dynamics of the watershed hydrologic function (Sivapalan, 2006; Wagener et  
269 al., 2007, Wainwright et al., 2022). We note that these dynamics are also illustrated by the changes  
270 in measured groundwater levels as depicted in Appendix A.

271



272

273 Figure 2: Temporal variations of water table depth (WTD) and SWE at an example hillslope. The

274

location of the hillslope is shown in Figure 1.

275

2. Elevation: in mountainous watersheds, because the differences in hydroclimate are primarily driven by elevation, hillslopes with similar elevations could potentially have similar land surface processes signatures.

277

278

3. Land cover: hillslopes can also be clustered by their dominant land cover. Land cover shapes land surface processes, which in turn affect subsurface dynamics and the water balance at the hillslope scale.

280

281

4. TWI: The Topographic Wetness index commonly used to cluster hillslopes is given by:

282

$$\ln \left( \frac{\alpha}{\tan(\beta)} \right).$$

Where  $\alpha$  is the upslope draining area and  $\beta$  the local angle.

283

5. AI: the AI (ETP/Precipitation, where ETP is the potential evapotranspiration) represents the ratio of the average demand for moisture to the average supply of moisture. We derive the spatial distribution of the AI in the East River from the Global Aridity Index dataset (CGIAR-CSI, 2019).

286

287

6. Machine learning based clustering: we define the hillslope similarity using the clustering of ParFlow-CLM input and output data layers. Clustering was performed in three different

288

289 ways, using the following data: (1) model input (elevation, percentage of the main land  
290 cover type, TWI, and AI), referred to hereafter as the “clustering input” (C.I.) method, (2)  
291 model output (ET, SWE, WTD, and  $\Delta P_1$ ), referred to hereafter as the “clustering output”  
292 (C.O.) method, and (3) both model input and output data layers, referred to hereafter as the  
293 “clustering input-output” (C.I.O.) method. We use hierarchical clustering, which is a  
294 decision-tree-based method that divides data points based on a series of binary splits  
295 (Devadoss et al., 2020; Kassambara, 2017; Wainwright et al., 2022). We define the linkage  
296 (or the distance) between any two clusters based on the Euclidian distance and the Ward  
297 method that computes the variance within each cluster, measuring the distance between  
298 each observation and the cluster’s mean, and then taking the sum of the distances’ squares.

#### 299 **2.4. Hillslope clustering comparisons**

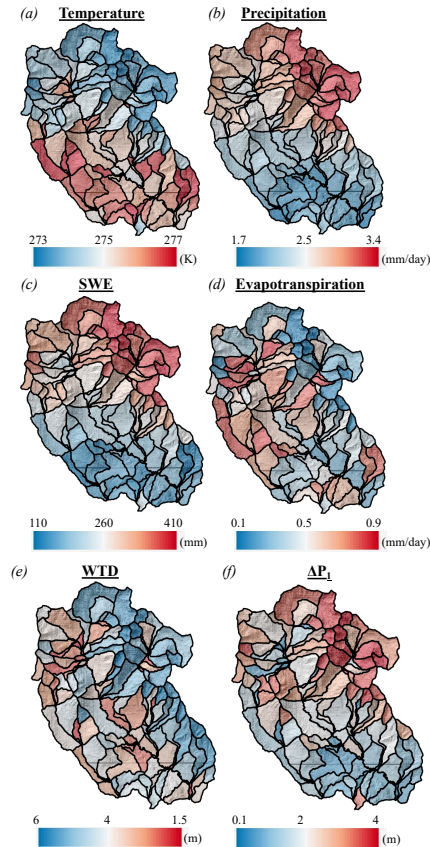
300 To test the ability of the eight selected clustering approaches to identify and categorize  
301 hillslopes with similar static characteristics and dynamics, we assess each clustering’s ability to  
302 describe several characteristics of the hillslope: elevation, land cover, hydroclimate (i.e.,  
303 precipitation), land surface processes (SWE and ET), and subsurface dynamics (WTD values and  
304 variations). For each clustering, we define three zones. For each variable, zone, and clustering, we  
305 compute the mean ( $\mu$ ) of the hillslope values and the corresponding coefficient of variation (CV).  
306 We also calculate the mean of the CV of the different zones for each variable and clustering.

307

### 308 **3. Results**

#### 309 **3.1. Hillslope characteristics**

310 Figure 3 shows the spatial distribution of hillslope temperature, precipitation, SWE, ET,  
311 WTD, and  $\Delta P_1$ .

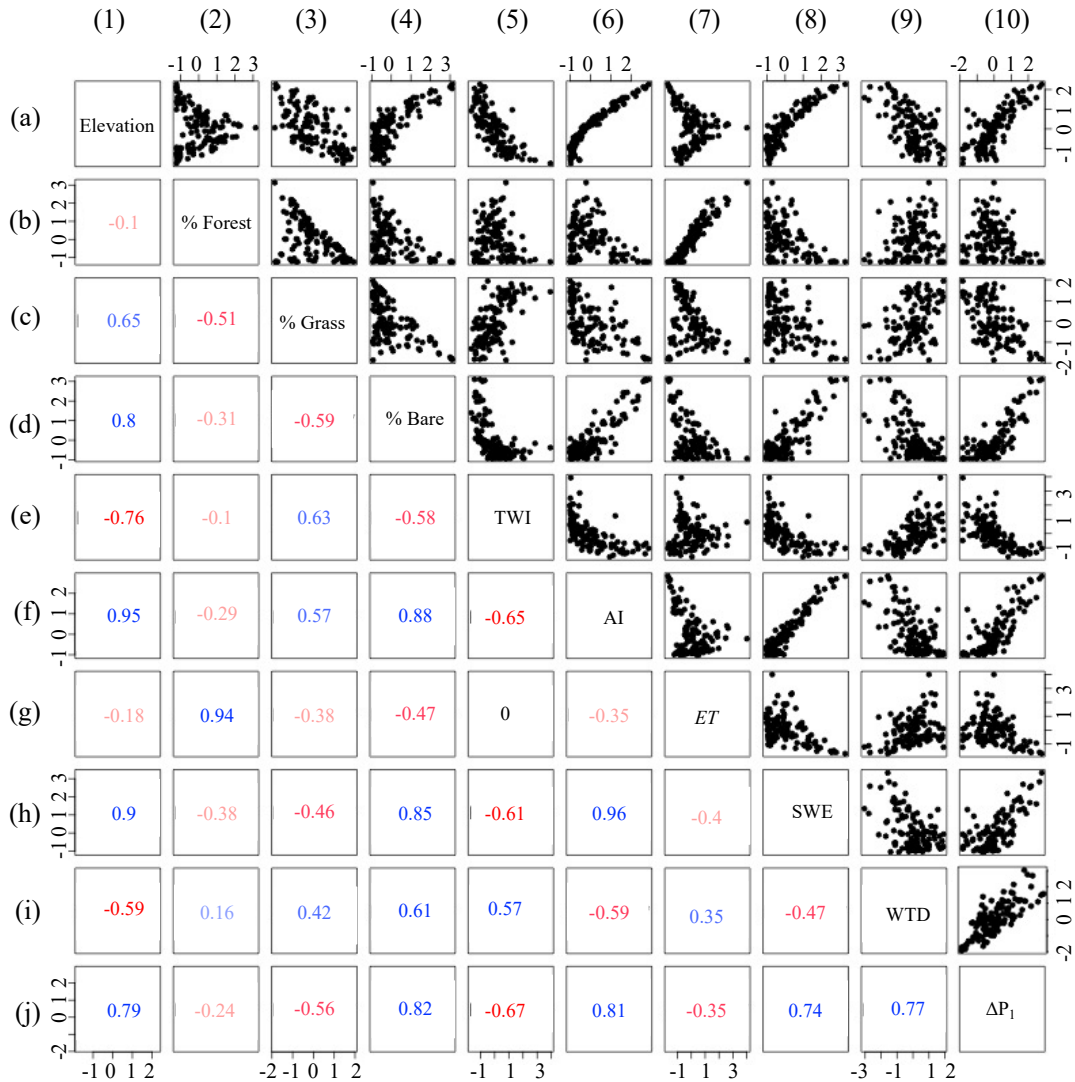


312

313 Figure 3: Spatial distributions of hillslope annual average values of (a) temperature, (b)  
 314 precipitation, (c) snow water equivalent (SWE), (d) evapotranspiration, (e) water table depth  
 315 (WTD) and (e)  $\Delta P_1$

316 As expected, the hillslopes characterized by high SWE have high precipitation and low  
 317 temperatures in contrast to the hillslopes with low SWE. However, ET shows a different pattern,  
 318 because it depends on both water availability and ET demands, which depends on the type of land  
 319 cover. The mid-elevation zone (i.e., zone 2) with a high coverage of forests has high ET. Hillslope  
 320 with high  $\Delta P_1$  have a deep WTD on average, this is because the WTD increases significantly during  
 321 baseflow conditions and reaches very large values as quantified by  $\Delta P_1$ . Hillslopes with high  $\Delta P_1$   
 322 values generally correspond to hillslopes with high precipitation and low temperature and therefore  
 323 high SWE values.

324 To better understand the relationship between  $\Delta P_1$  and the hillslope physical characteristics  
 325 and hydrologic processes, we study the Pearson correlation coefficient between  $\Delta P_1$  and the  
 326 elevation, the percent of the dominant land cover, TWI, AI, ET, SWE, and WTD (Figure 4).



327  
 328 Figure 4: Pearson's correlations between the selected variables for hillslope clustering approaches:  
 329 elevation, percent of the main land cover type (forest, grassland, and bare soil), topographic  
 330 wetness index (TWI), aridity index (AI), evapotranspiration (ET), snow water equivalent (SWE),  
 331 water table depth (WTD), and seasonal changes in groundwater  $\Delta P_1$ . Note that correlation  
 332 coefficients are colored coded based on their values.

333 Results for  $\Delta P_2$  are not shown because  $\Delta P_2$  is strongly correlated to  $\Delta P_1$ . Bare soil, TWI,  
334 AI, SWE, and  $\Delta P_1$  are strongly correlated (we define this as Pearson's correlation coefficient  
335 higher than 0.7) with elevation (Figure 4, column 1, lines d, e, f, h, and j). In particular, elevation  
336 has a dominant control on AI and SWE with a Pearson's correlation coefficient higher than 0.9.  
337 We observe nonlinearity such that TWI increases in the lower elevation and that AI becomes  
338 constant at the lower elevation. High percentage of forests is only found in mid-elevation (Figure  
339 4, 2a) whereas high percentage of grassland is well correlated to low elevations (Figure 4, 3a). ET  
340 is positively correlated to the percent of forests (Pearson's correlation coefficient is higher than  
341 0.9, Figure 4 2g).  $\Delta P_1$  has a Pearson's correlation coefficient higher than 0.7 for 6 out of 9 studied  
342 variables (elevation, percent of bare soil, TWI (correlation coefficient equal to 0.67), AI, SWE,  
343 and WTD, Figure 4, line j, columns 1, 4, 5, 6, 8 and 9); it, therefore, indicates that changes  $\Delta P_1$   
344 can reflect the changes of these variables. The two variables with low correlations with  $\Delta P_1$  are ET  
345 and the percent of forests (Figure 4, line j, column 2 and 7). ET is related to groundwater dynamics  
346 in a nonlinear way (Condon et al., 2013; Ferguson & Maxwell, 2010; Rahman et al., 2016). As  
347 shown in these studies, regions with shallow WTDs have the highest ET fluxes and this flux  
348 typically decreases significantly with WTD. When WTD reaches a critical depth, the groundwater  
349 and the atmosphere disconnect and changes in WTD do not impact ET.

350

### 351 **3.2.Hillslopes clustering**

352 For each clustering, we identify three zones (Figure 5). For the  $\Delta P_1$ , elevation, TWI, and  
353 AI clustering approaches, we define the thresholds of each zone by analyzing the distributions of  
354 the hillslope values of these indices.

355 1.  $\Delta P_1$ : Zone 1 comprises hillslopes whose  $\Delta P_1$  are less than 1.5 m,  $\Delta P_1$  of hillslopes of zone 2 are  
356 comprised between 1.5 m and 2.5 m, and Zone 3 group all hillslopes with  $\Delta P_1$  greater than 2.5 m.

357 1. Elevation: Zone 1 characterizes low elevation areas (average hillslope elevation less than 3000  
 358 m), Zone 2 mid (average hillslope elevation comprises between 3000 m and 3500 m), and Zone 3  
 359 high elevation (hillslope with an average elevation greater than 3500 m).

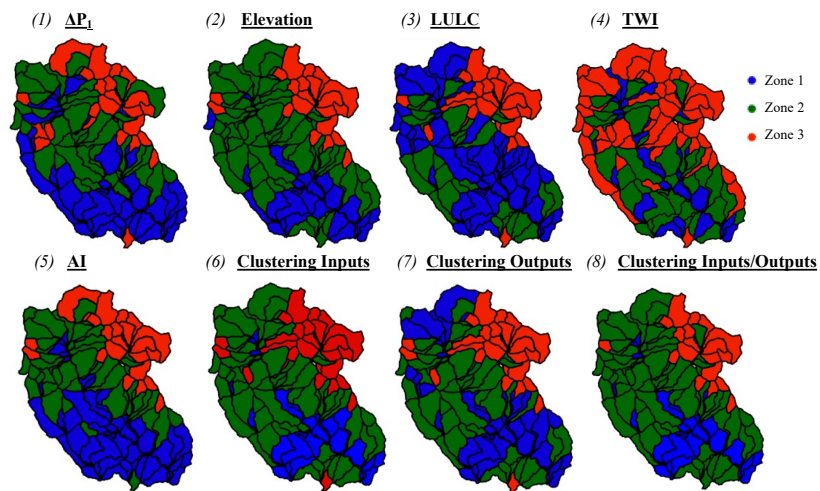
360 3. Land Cover: Zone 1 describes hillslopes that have predominantly grasses as land cover, Zone 2  
 361 for hillslopes with more than 50% of forest, and Zone 3 for hillslopes where bare soil is the  
 362 dominant land cover.

363 4. TWI: We define 3 zones with high (TWI>1, Zone 1), mid (TWI comprises between 1 and 0.2  
 364 Zone 2), and low (TWI<0.2, Zone 3) TWI.

365 5. AI: Zone 1 comprises hillslopes with AI less than 0.45, Zone 2 describes hillslopes with AI  
 366 between 0.45 and 0.55, and hillslopes of Zone 3 have an AI greater than 0.55.

367 6. Machine learning based clustering: the approaches automatically regroup the similar hillslopes  
 368 into three zones.

369



370

371 Figure 5: Spatial distribution of hillslope zones derived from the eight selected clustering  
 372 approaches (1)  $\Delta P_1$ , (2) elevation, (3) land cover (LULC), (4) topographic wetness index (TWI),

373 (5) aridity index (AI), and clustering with (6) inputs, (7) outputs, and (8) inputs and outputs  
 374 variables.

375 **3.3.Comparisons of the eight selected hillslope clustering approaches**  
 376 Table 1 depicts the mean ( $\mu$ ) and the corresponding coefficient of variation (CV) of  
 377 hillslope values for each variable, zone, and clustering.  
 378

<i>Variable: Elevation</i>			
<b><u><math>\Delta P_1</math></u></b>	<b><u>Elevation</u></b>	<b><u>LULC</u></b>	<b><u>TWI</u></b>
Zone 1: $\mu=3027$ ; CV=0.25	Zone 1: $\mu=2884$ ; CV=0.02	Zone 1: $\mu=3099$ ; CV=0.06	Zone 1: $\mu=2853$ ; CV=0.25
Zone 2: $\mu=3226$ ; CV=0.06	Zone 2: $\mu=3233$ ; CV=0.06	Zone 2: $\mu=3065$ ; CV=0.16	Zone 2: $\mu=2637$ ; CV=0.41
Zone 3: $\mu=3593$ ; CV=0.04	Zone 3: $\mu=3641$ ; CV=0.04	Zone 3: $\mu=3595$ ; CV=0.04	Zone 3: $\mu=1999$ ; CV=0.84
<b><u>AI</u></b>	<b><u>Clustering Input</u></b>	<b><u>Clustering Output</u></b>	<b><u>Clustering I. O.</u></b>
Zone 1: $\mu=2947$ ; CV=0.03	Zone 1: $\mu=3202$ ; CV=0.04	Zone 1: $\mu=3029$ ; CV=0.07	Zone 1: $\mu=3232$ ; CV=0.049
Zone 2: $\mu=3285$ ; CV=0.03	Zone 2: $\mu=2903$ ; CV=0.03	Zone 2: $\mu=3175$ ; CV=0.04	Zone 2: $\mu=2904$ ; CV=0.034
Zone 3: $\mu=3625$ ; CV=0.03	Zone 3: $\mu=3592$ ; CV=0.03	Zone 3: $\mu=3605$ ; CV=0.03	Zone 3: $\mu=3658$ ; CV=0.025
<i>Variable: Precipitation</i>			
<b><u><math>\Delta P_1</math></u></b>	<b><u>Elevation</u></b>	<b><u>LULC</u></b>	<b><u>TWI</u></b>
Zone 1: $\mu=2.24$ ; CV=0.21	Zone 1: $\mu=2.11$ ; CV=0.22	Zone 1: $\mu=2.42$ ; CV=0.22	Zone 1: $\mu=2.38$ ; CV=0.23
Zone 2: $\mu=2.68$ ; CV=0.18	Zone 2: $\mu=2.77$ ; CV=0.22	Zone 2: $\mu=2.39$ ; CV=0.20	Zone 2: $\mu=2.37$ ; CV=0.22
Zone 3: $\mu=3.26$ ; CV=0.15	Zone 3: $\mu=3.55$ ; CV=0.09	Zone 3: $\mu=3.26$ ; CV=0.16	Zone 3: $\mu=2.74$ ; CV=0.23
<b><u>AI</u></b>	<b><u>Clustering Input</u></b>	<b><u>Clustering Output</u></b>	<b><u>Clustering I. O.</u></b>
Zone 1: $\mu=2.10$ ; CV=0.15	Zone 1: $\mu=2.68$ ; CV=0.18	Zone 1: $\mu=2.33$ ; CV=0.22	Zone 1: $\mu=2.73$ ; CV=0.18
Zone 2: $\mu=2.74$ ; CV=0.17	Zone 2: $\mu=2.06$ ; CV=0.16	Zone 2: $\mu=2.63$ ; CV=0.18	Zone 2: $\mu=2.07$ ; CV=0.17
Zone 3: $\mu=3.39$ ; CV=0.12	Zone 3: $\mu=3.41$ ; CV=0.11	Zone 3: $\mu=3.43$ ; CV=0.11	Zone 3: $\mu=3.56$ ; CV=0.06
<i>Variable: Temperature</i>			
<b><u><math>\Delta P_1</math></u></b>	<b><u>Elevation</u></b>	<b><u>LULC</u></b>	<b><u>TWI</u></b>
Zone 1: $\mu=276.5$ ; CV=0.001	Zone 1: $\mu=276.2$ ; CV=0.003	Zone 1: $\mu=276.1$ ; CV=0.002	Zone 1: $\mu=276.3$ ; CV=0.001
Zone 2: $\mu=275.9$ ; CV=0.002	Zone 2: $\mu=276.0$ ; CV=0.003	Zone 2: $\mu=276.4$ ; CV=0.001	Zone 2: $\mu=276.2$ ; CV=0.002
Zone 3: $\mu=274.5$ ; CV=0.002	Zone 3: $\mu=274.1$ ; CV=0.002	Zone 3: $\mu=274.4$ ; CV=0.002	Zone 3: $\mu=275.6$ ; CV=0.003
<b><u>AI</u></b>	<b><u>Clustering Input</u></b>	<b><u>Clustering Output</u></b>	<b><u>Clustering I. O.</u></b>
Zone 1: $\mu=276.6$ ; CV=0.001	Zone 1: $\mu=276.2$ ; CV=0.002	Zone 1: $\mu=276.2$ ; CV=0.002	Zone 1: $\mu=276.1$ ; CV=0.002
Zone 2: $\mu=275.8$ ; CV=0.002	Zone 2: $\mu=276.5$ ; CV=0.001	Zone 2: $\mu=276.3$ ; CV=0.002	Zone 2: $\mu=276.5$ ; CV=0.001
Zone 3: $\mu=274.3$ ; CV=0.002	Zone 3: $\mu=274.4$ ; CV=0.003	Zone 3: $\mu=274.3$ ; CV=0.002	Zone 3: $\mu=274.1$ ; CV=0.002
<i>Variable: SWE</i>			



<b><u><math>\Delta P_1</math></u></b>	<b><u>Elevation</u></b>	<b><u>LULC</u></b>	<b><u>TWI</u></b>
Zone 1: $\mu=152$ ; CV=0.30 Zone 2: $\mu=204$ ; CV=0.34 Zone 3: $\mu=335$ ; CV=0.31	Zone 1: $\mu=149$ ; CV=0.38 Zone 2: $\mu=201$ ; CV=0.43 Zone 3: $\mu=389$ ; CV=0.26	Zone 1: $\mu=181$ ; CV=0.34 Zone 2: $\mu=151$ ; CV=0.29 Zone 3: $\mu=339$ ; CV=0.29	Zone 1: $\mu=169$ ; CV=0.50 Zone 2: $\mu=165$ ; CV=0.39 Zone 3: $\mu=234$ ; CV=0.46
<b><u>AI</u></b>	<b><u>Clustering Input</u></b>	<b><u>Clustering Output</u></b>	<b><u>Clustering I. O.</u></b>
Zone 1: $\mu=137$ ; CV=0.18 Zone 2: $\mu=206$ ; CV=0.25 Zone 3: $\mu=360$ ; CV=0.24	Zone 1: $\mu=191$ ; CV=0.32 Zone 2: $\mu=145$ ; CV=0.17 Zone 3: $\mu=359$ ; CV=0.25	Zone 1: $\mu=173$ ; CV=0.34 Zone 2: $\mu=179$ ; CV=0.30 Zone 3: $\mu=365$ ; CV=0.23	Zone 1: $\mu=200$ ; CV=0.33 Zone 2: $\mu=146$ ; CV=0.20 Zone 3: $\mu=396$ ; CV=0.18
<b><i>Variable: ET</i></b>			
<b><u><math>\Delta P_1</math></u></b>	<b><u>Elevation</u></b>	<b><u>LULC</u></b>	<b><u>TWI</u></b>
Zone 1: $\mu=0.42$ ; CV=0.47 Zone 2: $\mu=0.41$ ; CV=0.47 Zone 3: $\mu=0.17$ ; CV=0.74	Zone 1: $\mu=0.35$ ; CV=0.75 Zone 2: $\mu=0.48$ ; CV=0.54 Zone 3: $\mu=0.15$ ; CV=0.90	Zone 1: $\mu=0.31$ ; CV=0.36 Zone 2: $\mu=0.61$ ; CV=0.27 Zone 3: $\mu=0.19$ ; CV=0.69	Zone 1: $\mu=0.37$ ; CV=0.58 Zone 2: $\mu=0.41$ ; CV=0.49 Zone 3: $\mu=0.35$ ; CV=0.56
<b><u>AI</u></b>	<b><u>Clustering Input</u></b>	<b><u>Clustering Output</u></b>	<b><u>Clustering I. O.</u></b>
Zone 1: $\mu=0.40$ ; CV=0.46 Zone 2: $\mu=0.45$ ; CV=0.45 Zone 3: $\mu=0.14$ ; CV=0.58	Zone 1: $\mu=0.49$ ; CV=0.37 Zone 2: $\mu=0.25$ ; CV=0.32 Zone 3: $\mu=0.19$ ; CV=0.68	Zone 1: $\mu=0.27$ ; CV=0.29 Zone 2: $\mu=0.55$ ; CV=0.29 Zone 3: $\mu=0.18$ ; CV=0.65	Zone 1: $\mu=0.48$ ; CV=0.38 Zone 2: $\mu=0.25$ ; CV=0.31 Zone 3: $\mu=0.12$ ; CV=0.57
<b><i>Variable: Saturation</i></b>			
<b><u><math>\Delta P_1</math></u></b>	<b><u>Elevation</u></b>	<b><u>LULC</u></b>	<b><u>TWI</u></b>
Zone 1: $\mu=0.77$ ; CV=0.14 Zone 2: $\mu=0.69$ ; CV=0.10 Zone 3: $\mu=0.66$ ; CV=0.11	Zone 1: $\mu=0.75$ ; CV=0.23 Zone 2: $\mu=0.73$ ; CV=0.16 Zone 3: $\mu=0.67$ ; CV=0.13	Zone 1: $\mu=0.75$ ; CV=0.14 Zone 2: $\mu=0.71$ ; CV=0.15 Zone 3: $\mu=0.68$ ; CV=0.09	Zone 1: $\mu=0.81$ ; CV=0.14 Zone 2: $\mu=0.72$ ; CV=0.12 Zone 3: $\mu=0.70$ ; CV=0.13
<b><u>AI</u></b>	<b><u>Clustering Input</u></b>	<b><u>Clustering Output</u></b>	<b><u>Clustering I. O.</u></b>
Zone 1: $\mu=0.75$ ; CV=0.15 Zone 2: $\mu=0.73$ ; CV=0.13 Zone 3: $\mu=0.68$ ; CV=0.11	Zone 1: $\mu=0.72$ ; CV=0.11 Zone 2: $\mu=0.77$ ; CV=0.16 Zone 3: $\mu=0.69$ ; CV=0.09	Zone 1: $\mu=0.76$ ; CV=0.15 Zone 2: $\mu=0.72$ ; CV=0.10 Zone 3: $\mu=0.68$ ; CV=0.09	Zone 1: $\mu=0.72$ ; CV=0.10 Zone 2: $\mu=0.78$ ; CV=0.15 Zone 3: $\mu=0.66$ ; CV=0.08
<b><i>Variable: WTD</i></b>			
<b><u><math>\Delta P_1</math></u></b>	<b><u>Elevation</u></b>	<b><u>LULC</u></b>	<b><u>TWI</u></b>
Zone 1: $\mu=2.9$ ; CV=0.06 Zone 2: $\mu=3.7$ ; CV=0.05 Zone 3: $\mu=4.8$ ; CV=0.07	Zone 1: $\mu=3.4$ ; CV=0.1 Zone 2: $\mu=3.2$ ; CV=0.07 Zone 3: $\mu=4.6$ ; CV=0.08	Zone 1: $\mu=3.0$ ; CV=0.06 Zone 2: $\mu=3.5$ ; CV=0.07 Zone 3: $\mu=4.7$ ; CV=0.07	Zone 1: $\mu=2.4$ ; CV=0.04 Zone 2: $\mu=3.3$ ; CV=0.04 Zone 3: $\mu=4.0$ ; CV=0.1
<b><u>AI</u></b>	<b><u>Clustering Input</u></b>	<b><u>Clustering Output</u></b>	<b><u>Clustering I. O.</u></b>
Zone 1: $\mu=3.1$ ; CV=0.06 Zone 2: $\mu=3.5$ ; CV=0.07 Zone 3: $\mu=4.7$ ; CV=0.08	Zone 1: $\mu=3.2$ ; CV=0.04 Zone 2: $\mu=2.6$ ; CV=0.04 Zone 3: $\mu=4.4$ ; CV=0.06	Zone 1: $\mu=2.8$ ; CV=0.05 Zone 2: $\mu=3.2$ ; CV=0.04 Zone 3: $\mu=4.5$ ; CV=0.05	Zone 1: $\mu=3.3$ ; CV=0.04 Zone 2: $\mu=2.5$ ; CV=0.04 Zone 3: $\mu=4.8$ ; CV=0.05
<b><i>Variable: <math>\Delta P_2</math></i></b>			

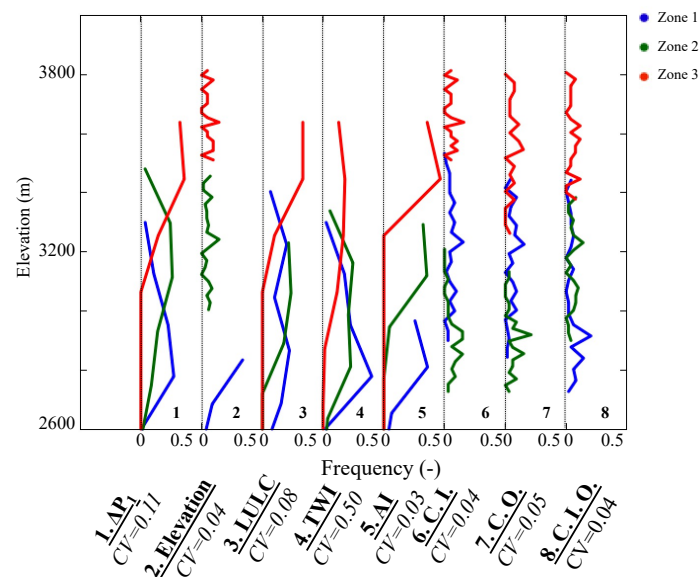
<u><math>\Delta P_1</math></u>	<u>Elevation</u>	<u>LULC</u>	<u>TWI</u>
Zone 1: $\mu=2.9$ ; CV=0.06	Zone 1: $\mu=3.4$ ; CV=0.1	Zone 1: $\mu=3.0$ ; CV=0.06	Zone 1: $\mu=2.4$ ; CV=0.04
Zone 2: $\mu=3.7$ ; CV=0.05	Zone 2: $\mu=3.2$ ; CV=0.07	Zone 2: $\mu=3.5$ ; CV=0.07	Zone 2: $\mu=3.3$ ; CV=0.04
Zone 3: $\mu=4.8$ ; CV=0.07	Zone 3: $\mu=4.6$ ; CV=0.08	Zone 3: $\mu=4.7$ ; CV=0.07	Zone 3: $\mu=4.0$ ; CV=0.1
<u>AI</u>	<u>Clustering Input</u>	<u>Clustering Output</u>	<u>Clustering I. O.</u>
Zone 1: $\mu=3.1$ ; CV=0.06	Zone 1: $\mu=3.2$ ; CV=0.04	Zone 1: $\mu=2.8$ ; CV=0.05	Zone 1: $\mu=3.3$ ; CV=0.04
Zone 2: $\mu=3.5$ ; CV=0.07	Zone 2: $\mu=2.6$ ; CV=0.04	Zone 2: $\mu=3.2$ ; CV=0.04	Zone 2: $\mu=2.5$ ; CV=0.04
Zone 3: $\mu=4.7$ ; CV=0.08	Zone 3: $\mu=4.4$ ; CV=0.06	Zone 3: $\mu=4.5$ ; CV=0.05	Zone 3: $\mu=4.8$ ; CV=0.05

379 Table 1: Mean  $\mu$  and coefficient of variation CV of each variable and hillslope zone derived from  
380 the 8 clustering approaches.

381

### 382 3.1.1. Similarities in hillslope structure

383 Elevation plays an important role in the hydroclimate of a region especially in mountainous  
384 watersheds where it controls snow accumulation and controls the downstream hydrology. Figure  
385 6 shows the elevation frequency distributions associated with the 3 zones derived from the 8  
386 clustering approaches.



387

388 Figure 6: Frequency distributions of hillslope elevation. Clustering approaches are based  
389 on  $\Delta P_1$ , elevation, land cover (LULC), topographic wetness index (TWI), aridity index (AI), and

390 machine-learning approaches (with inputs C.I., outputs C.O., and inputs and outputs C.I.O).  
391 Hillslope clustering approaches are located across the x-axis. Note that we plotted the distributions  
392 of the 8 clustering approaches on the same graph, between each dotted line (frequency from 0 to  
393 0.5) are plotted the frequency distributions of the three zones derived from the clustering.

394

395 By classifying the hillslopes using their similarity in  $\Delta P_1$ , we observe that hillslopes with  
396 low  $\Delta P$  have the lowest elevation while the hillslopes of zone 3 (high  $\Delta P_1$ ) have the highest  
397 elevation. Unsurprisingly, the second clustering (i.e. elevation) clearly identifies the hillslopes with  
398 similar elevation. The AI clustering also identifies hillslopes with similar elevation as shown in  
399 Figures 4 and 6. The TWI clustering performs moderately, where zones 1 and 2 are characterized  
400 by similar elevation distributions. Hillslopes with lower TWI are mostly located in high elevation  
401 areas on the contrary to the low elevation hillslopes. In the land cover clustering, most of the  
402 grassed hillslopes (zone 1) are in low elevation, forests (zone 2) in mid-elevation, and hillslopes  
403 whose landscape is mainly bare soil (zone 3) are in high elevation areas above the tree line. The  
404 three clustering approaches using machine learning allow identifying hillslopes with similar  
405 elevation, their coefficients of variation are of the same order as the elevation clustering.

406 Table 2 describes the average hillslope ratio of land cover type (forests, grassland, and bare  
407 soil) for each zone and type of clustering. The land cover clustering indicates that grassland is the  
408 dominant land cover of zone 1, forests Zone 2, and bare soil zone 3. Only the machine learning  
409 clustering approaches using outputs lead to a similar conclusion whereas while the other clustering  
410 approaches capture the characteristics of zone 1 and 3, they do not identify a distinct forested zone  
411 2. For the  $\Delta P_1$  clustering this could be attributed to the disconnection between groundwater  
412 dynamics and land surface processes that takes place in certain forested zones. Since clustering

413 based on landscape characteristics and  $\Delta P_1$  do not identify such a distinct zone, it suggests that this  
 414 zone may not be indicative of distinct hydrologic behavior.

415

$\Delta P_1$	Forest	Grassland	Bare Soil
<b>Zone 1</b>	0.35	0.55	0.10
<b>Zone 2</b>	0.35	0.43	0.22
<b>Zone 3</b>	0.11	0.27	0.62
<b>CV</b>	0.97	0.56	0.69
<b>Elevation</b>			
Elevation	Forest	Grassland	Bare Soil
<b>Zone 1</b>	0.28	0.56	0.15
<b>Zone 2</b>	0.41	0.42	0.17
<b>Zone 3</b>	0.07	0.26	0.68
<b>CV</b>	1.33	0.76	1.07
<b>Land Cover</b>			
Land Cover	Forest	Grassland	Bare Soil
<b>Zone 1</b>	0.23	0.67	0.14
<b>Zone 2</b>	0.72	0.26	0.12
<b>Zone 3</b>	0.12	0.22	0.66
<b>CV</b>	0.67	0.45	0.64
<b>Topographic Wetness Index (TWI)</b>			
Topographic Wetness Index (TWI)	Forest	Grasslands	Bare Soil
<b>Zone 1</b>	0.24	0.66	0.10
<b>Zone 2</b>	0.35	0.51	0.14
<b>Zone 3</b>	0.32	0.35	0.33
<b>CV</b>	1.47	0.49	0.95
<b>Aridity Index</b>			
Aridity Index	Forest	Grassland	Bare Soil
<b>Zone 1</b>	0.34	0.57	0.09
<b>Zone 2</b>	0.37	0.41	0.22
<b>Zone 3</b>	0.07	0.32	0.61
<b>CV</b>	0.91	0.56	0.69
<b>Clustering with input layers</b>			
Clustering with input layers	Forest	Grassland	Bare Soil
<b>Zone 1</b>	0.44	0.42	0.14
<b>Zone 2</b>	0.11	0.83	0.06
<b>Zone 3</b>	0.12	0.25	0.63
<b>CV</b>	0.83	0.38	0.62

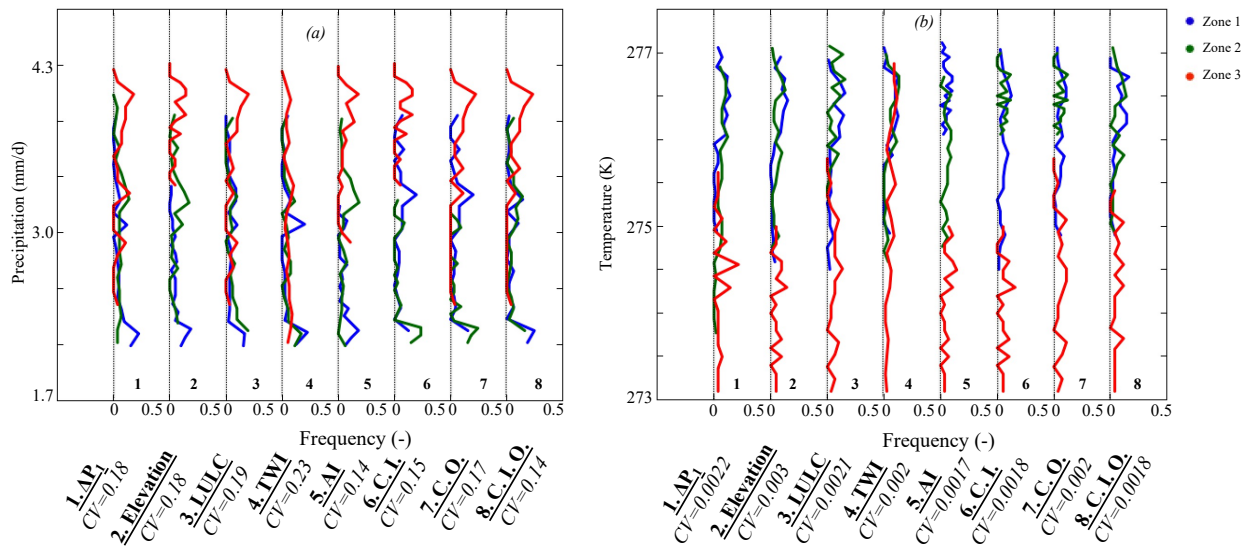
<b>Clustering with output layers</b>	<b>Forest</b>	<b>Grasslands</b>	<b>Bare Soil</b>
<b>Zone 1</b>	0.14	0.77	0.09
<b>Zone 2</b>	0.52	0.34	0.15
<b>Zone 3</b>	0.11	0.25	0.64
<b>CV</b>	0.77	0.38	0.61
<b>Clustering with inputs and outputs</b>	<b>Forest</b>	<b>Grassland</b>	<b>Bare Soil</b>
<b>Zone 1</b>	0.42	0.40	0.18
<b>Zone 2</b>	0.12	0.82	0.06
<b>Zone 3</b>	0.05	0.24	0.70
<b>CV</b>	0.87	0.41	0.65

416 Table 2: Average values of hillslope ratio of forests, grasslands, and bare soils for each zone and  
417 clustering.

### 418 3.1.2. Similarities in hydroclimate

419 Figures 7a and b depict the distributions of precipitation and temperature obtained with the  
420 eight selected clustering approaches. The AI clustering allows identifying hillslope with similar  
421 hydroclimate because it has low values of coefficients of variation. Zone 1 located in low elevation  
422 has low precipitation and high temperatures, contrary to zone 3. Zone 2 is characterized by a  
423 hydroclimate that is in between those of Zone 1 and 3. Our  $\Delta P_1$  clustering leads to conclusions  
424 similar to the machine learning based clustering and AI. These three clustering approaches have  
425 the same average CV and are the only methods that allow identifying hillslopes with similar  
426 hydroclimate. Although, we note that in the three machine learning based clustering as well as in  
427 the  $\Delta P$  clustering, Zones 1 and 2 have similar hydroclimate, which is not the case in the AI  
428 clustering. While the land cover clustering approaches clearly identifies the typical hydroclimate  
429 of the hillslopes of zone 3, the two remaining zones have the same hydroclimate. The TWI  
430 clustering does not identify hillslopes with similar hydroclimates because it relies on the  
431 hydrologic processes driven by the topography. TWI shows that clustering that includes only

432 hydroclimate would miss important information on distinct hillslope hydrologic processes that  
 433 strongly affect the response of the hillslope to meteorological forcing.



434  
 435 Figure 7: Frequency distributions of hillslope (a) annual average daily rates of precipitation and  
 436 (b) annual average temperature. Clustering approaches are based on  $\Delta P_1$ , elevation, land cover  
 437 (LULC), topographic wetness index (TWI), aridity index (AI), and machine-learning approaches  
 438 (with inputs C.I., outputs C.O., and inputs and outputs C.I.O). Hillslope clustering approaches are  
 439 located across the x-axis. Note that we plotted the distributions of the 8 clustering approaches on  
 440 the same graph, between each dotted line (frequency from 0 to 0.5) are plotted the frequency  
 441 distributions of the three zones derived from the clustering.

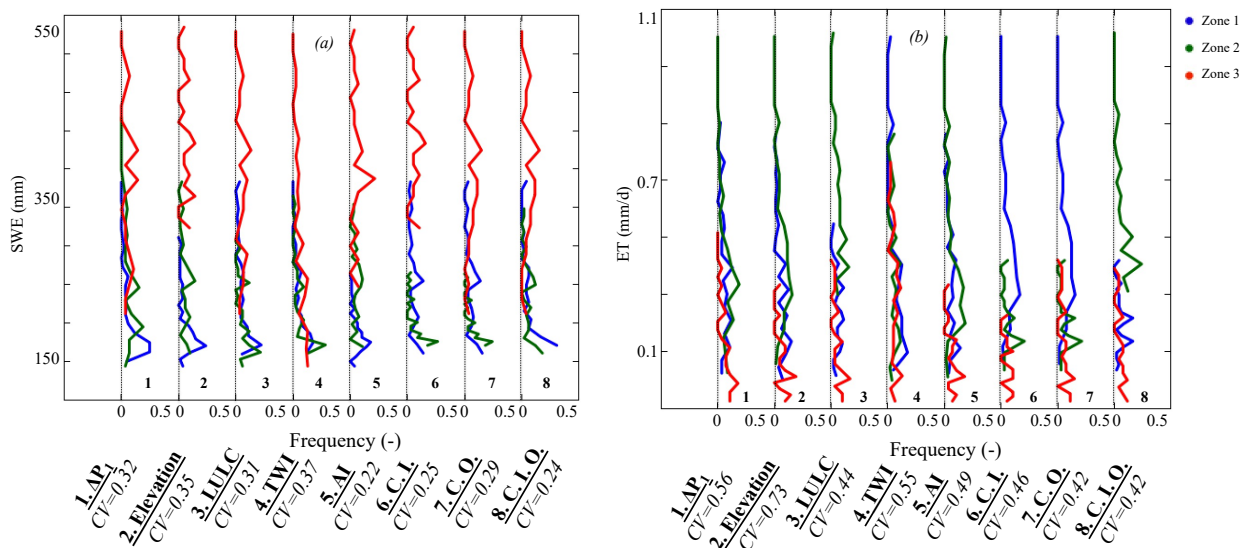
442

### 443 3.1.3. Similarities in hydrologic processes

444 In this section, we study the ability the selected clustering approaches to identify hillslopes  
 445 with similar hydrologic processes: snow dynamics, evapotranspiration, and WTD values and  
 446 variations.

#### 447 3.1.3.1. Land surface processes

448 A robust clustering in mountainous watersheds should identify hillslopes with similar snow  
 449 dynamics. Figure 8a illustrates the SWE frequency distribution associated with each zone and  
 450 clustering. Because SWE dynamics are primarily driven by elevation and the precipitation, the AI  
 451 and machine learning based clustering have the lowest average of the CV followed by the land  
 452 cover and the  $\Delta P_1$  clustering. The land cover spatial distribution contains information about  
 453 elevation especially in high elevation areas where some hillslopes are located above the tree line.  
 454 The  $\Delta P_1$  clustering accounts for SWE dynamics because  $\Delta P_1$  is highly correlated to SWE as  
 455 discussed in section 3.1.



456  
 457 Figure 8: Frequency distributions of hillslope land surface variables (a) annual average SWE and  
 458 (b) annual average daily rates of ET. Clustering approaches are based on  $\Delta P_1$ , elevation, land cover  
 459 (LULC), topographic wetness index (TWI), aridity index (AI), and machine-learning approaches  
 460 (with inputs C.I., outputs C.O., and inputs and outputs C.I.O). Hillslope clustering approaches are  
 461 located across the x-axis. Note that we plotted the distributions of the 8 clustering approaches on  
 462 the same graph, between each dotted line (frequency from 0 to 0.5) are plotted the frequency  
 463 distributions of the three zones derived from the clustering.

464

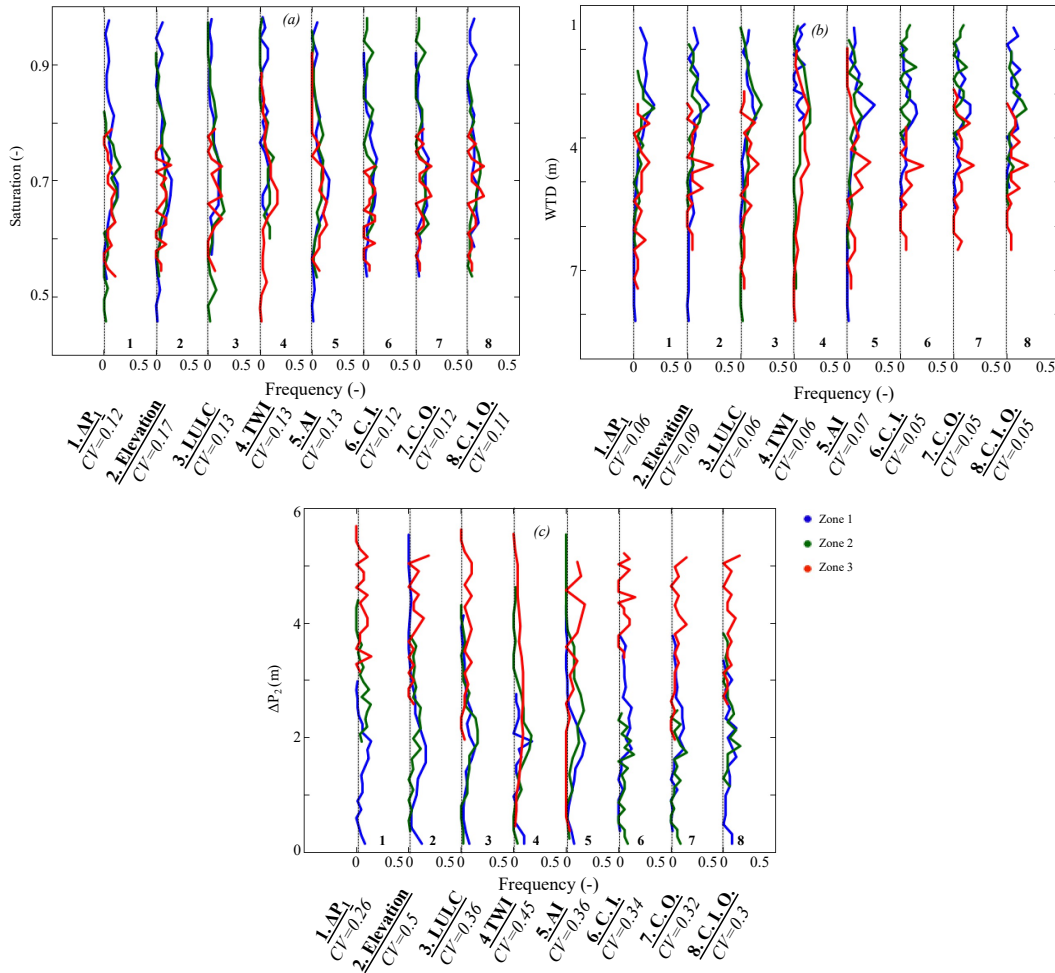
465 The spatial distribution of ET is controlled by many factors, including soil moisture, land cover,  
466 and subsurface flow. The land cover clustering performs well at identifying hillslopes with similar  
467 ET because the latter strongly depends on the land cover (Figure 8b). Consistent with the  
468 aforementioned results, the other clustering approaches performing well are the machine learning  
469 based clustering and the AI. The TWI and elevation clustering approaches do not separate  
470 hillslopes by their ET values because they do not account for varying land cover and soil properties  
471 that influence ET. The average CV of the  $\Delta P_1$  clustering is close to those of the land cover and AI  
472 clustering. As stated in many studies (Ferguson & Maxwell, 2010; Maina & Siirila-Woodburn,  
473 2020, Maina et al., 2022), subsurface flow affects ET, as such information about subsurface flow  
474 contains valuable information about the ET even if the correlation between  $\Delta P_1$  and ET is  
475 nonlinear.

#### 476 **3.1.3.2. Similarities in subsurface hydrodynamics**

477 We investigate the ability of the eight selected clustering approaches to identify hillslopes  
478 with similar subsurface hydrodynamics. We study the average saturation of the first 10 cm of the  
479 soil throughout the WY, the yearly average of WTD and  $\Delta P_2$ . Soil saturation is a key feature in  
480 both subsurface and atmospheric dynamics; it controls ET and groundwater recharge. The averages  
481 CV of the  $\Delta P_1$ , TWI, AI, land cover, and clustering approaches are very similar (Figure 9a). As  
482 the land cover clustering adequately regroup hillslopes with similar ET, it also allows regrouping  
483 hillslopes with similar soil saturation. Because the TWI describes the characteristics that drive  
484 flow, it serves as a good indicator of soil saturation like the AI. Similar to the results above, the  
485 machine learning based clustering perform well. The  $\Delta P_1$  clustering has a low average CV due to  
486 the strong connection between the changes in WTD and soil saturation. It is only the elevation



487 clustering that fails to identify hillslope with similar soil saturation, where the distributions of the  
 488 three defined zones show overlap.



489  
 490 Figure 9: Frequency distributions of hillslope (a) saturation, (b) WTD, and (c)  $\Delta P_2$ . Clustering  
 491 approaches are based on  $\Delta P_1$ , elevation, land cover (LULC), topographic wetness index (TWI),  
 492 aridity index (AI), and machine-learning approaches (with inputs C.I., outputs C.O., and inputs  
 493 and outputs C.I.O). Hillslope clustering approaches are located across the x-axis. Note that we  
 494 plotted the distributions of the 8 clustering approaches on the same graph, between each dotted  
 495 line (frequency from 0 to 0.5) are plotted the frequency distributions of the three zones derived  
 496 from the clustering.  
 497

498 WTD is an important variable for determining groundwater storage. Here, we rely on the  
499 average WTD throughout the year. As expected, the  $\Delta P_1$  clustering identifies hillslopes with  
500 similar WTD (Figure 9b). Zone 1 located in low elevation has the shallowest WTD and the lowest  
501  $\Delta P_1$ , contrary to zone 3. Zone 2 exhibits a behavior that is in between those of Zone 1 and 3. The  
502 TWI and land cover clustering approaches also are good for identifying hillslope with similar  
503 WTD. Hillslopes with low TWI (Zone 3) have the deepest WTD, contrary to the hillslopes of Zone  
504 1. The TWI identifies hillslopes with similar WTD because of the high relief of the watershed that  
505 drive its hydrology (Fan et al., 2019). The land cover clustering indicates that most of the forest  
506 (Zone 2) and bare soil (Zone 3) hillslopes have deep WTD whereas grasses (Zone 1) hillslopes  
507 have the shallowest WTD. The elevation clustering doesn't accurately identify hillslopes with  
508 similar WTD, and its average CV remains higher than the 4 other clustering approaches. The AI,  
509 like the elevation, isn't a good variable for identifying hillslopes with similar WTD. All their three  
510 zones overlap in terms of WTD. Results from the machine learning based clustering are similar to  
511 the  $\Delta P_1$  clustering with a CV of the same order, yet there isn't a clear distinction between Zone 1  
512 and 2 in these machine learning based clustering approaches.

513 Figure 9c illustrates the distributions of the  $\Delta P_2$  for each clustering approach and zone.  $\Delta P_1$   
514 clusters hillslopes with similar  $\Delta P_2$  as expected. Another suitable clustering approach for hillslopes  
515 with similar  $\Delta P_2$  is the land cover. Zone 3 characterizing bare soil hillslopes has the highest  $\Delta P_2$ ,  
516 unlike zones 1 and 2. The AI clustering shows that the majority of zone 3 hillslopes have high  $\Delta P_2$   
517 whereas zone 2 hillslopes have low  $\Delta P_2$ , followed by zone 1 hillslopes. In terms of  $\Delta P_2$  similarity,  
518 the elevation clustering outperforms the TWI. The machine learning based clustering approaches  
519 are good for identifying hillslopes with similar  $\Delta P_2$  especially the clustering using inputs variables

520 (CI). The two other machine learning based clustering approaches (outputs and inputs and outputs)  
521 do not distinguish zone 1 from zone 2.

## 522 **4. Discussions**

523 In this section, we discuss the advantages of the proposed  $\Delta P$  clustering compared to the  
524 other clustering approaches and its ability to capture dry and wet hydrologic conditions.

### 525 **4.1. Advantages of the $\Delta P$ clustering**

526 Depending on the purpose of the identification of similar hillslopes, the appropriate  
527 clustering may change. Nonetheless, it is important for any clustering approach to identify  
528 hillslopes with similar hydrologic processes. As demonstrated here, the advantage of using  $\Delta P_1$  to  
529 identify similar hillslopes is that many hydrologic processes are embedded in  $\Delta P_1$ . Our  
530 comparisons have shown that by using a  $\Delta P_1$  clustering, one is able to identify hillslopes with not  
531 only similar subsurface hydrodynamics but also similar land surface processes. Because these  
532 processes are intimately linked to the physical characteristics of the hillslope, its hydroclimate, and  
533 its land cover, the  $\Delta P_1$  clustering also allows for the identification of hillslopes with the  
534 aforementioned characteristics similar.

535 We, however, highlight that other clustering approaches may outperform the  $\Delta P_1$  when  
536 looking at a single characteristic. For instance, our results show that the elevation and AI (or other  
537 clustering approaches based on the hydroclimate e.g., Carrillo et al., 2011) clustering approaches  
538 may be excellent at identifying hillslopes with similar hydroclimates and snow dynamics. The land  
539 cover clustering allows for better identification of hillslopes with similar land surface processes  
540 such as ET and soil saturation. Lastly, the TWI clustering (e.g., Beven & Kirby, 1979; Grabs et  
541 al., 2009; Hjerdt et al., 2004; Loritz et al., 2019) allows the identification of hillslopes with similar  
542 groundwater dynamics and soil saturation values as it describes the topographic flow. In terms of

543 overall performance, our results show that for the study site considered here, the machine learning  
544 based clustering approaches are also a very good at identifying similar hillslopes.

545 Wainwright et al., (2022) use an unsupervised clustering method and remote sensing data  
546 layers which include elevation, SWE, radiation, resistivity, and Normalized Difference Vegetation  
547 Index NDVI to define 7 clusters in the East River watershed. While their clustering method has  
548 more zones (7) than ours (3), it leads to similar conclusions as our study where zones 1 and 2 are  
549 characterized by low elevation, high TWI, and low SWE values contrary to zones 5 and 6.

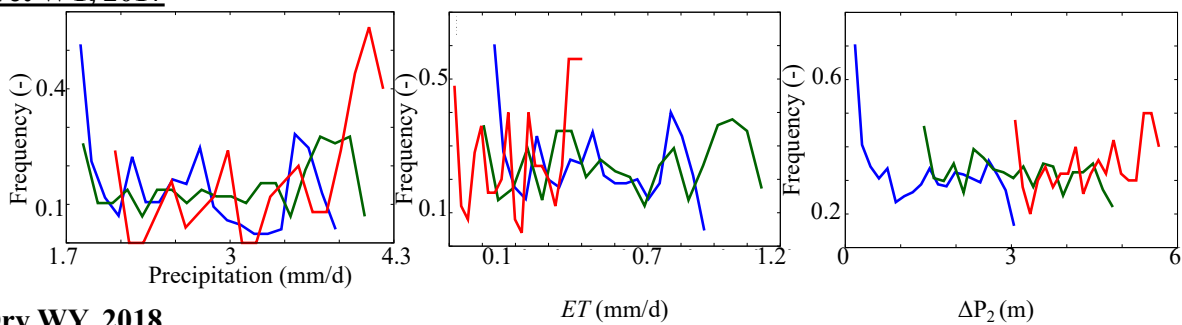
550 Other hillslope clustering approaches based on hydrologic processes relied on the Peclet  
551 number (Berne et al., 2005; S. W. Lyon & Troch, 2007; Steve W. Lyon & Troch, 2010) which  
552 describes the subsurface hydrological response and is derived from an analytical solution of the  
553 subsurface flow (e.g. the Boussinesq storage equation (Steve W. Lyon & Troch, 2010)). However,  
554 while the three-dimensional Richards equation has the advantage of better representing the  
555 subsurface flow it cannot be solved analytically, hence these indices cannot be applied to integrated  
556 hydrologic models. Our approach has demonstrated that the  $\Delta P$  helps quantify the subsurface  
557 hydrologic responses without using these indices and therefore overcomes the limitation of the use  
558 of attributes such as the Peclet number on integrated hydrologic models to categorize hillslopes.

#### 559 **4.2. Similarities in hydrologic responses to wet and dry conditions**

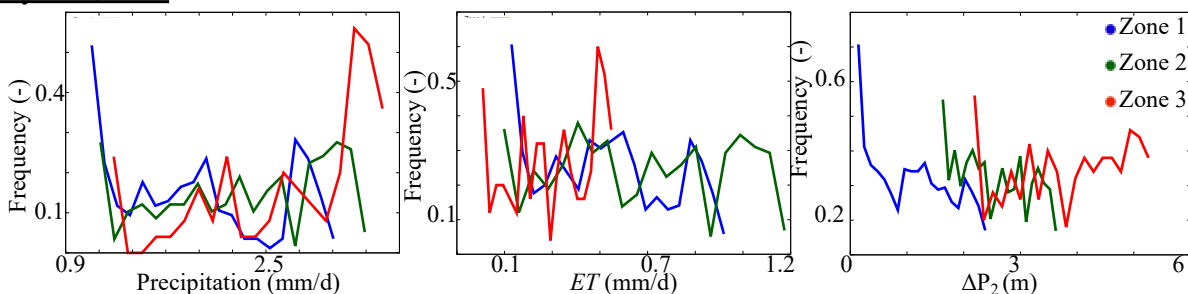
560 According to McDonnell & Woods, (2004) and Wagener et al., (2007), any classification  
561 should be able to predict the dynamics of the hillslopes. We test the ability of the  $\Delta P_1$  clustering to  
562 predict the dynamics of the hillslopes in wet and dry conditions. A possible limitation of a  
563 clustering based on a hydrologic process is that the latter may be linked to the conditions of the  
564 selected year. Hydrologic responses are by essence nonlinear and may strongly change from year  
565 to year. In addition, compared to the intrinsic characteristics of the hillslope (elevation,  
566 topographic index, and land cover), which are only variable if long periods of time are considered;

567 the scale at which hydrologic processes change is much shorter. Therefore, a clustering based on  
 568 a hydrologic process may be time-dependent. We previously quantified  $\Delta P_1$  using an average WY.  
 569 In this section, we compare the response of each zone to dry and wet conditions. We extend our  
 570 simulation from the WY 2015 to include the WYs 2016, 2017, and 2018, then we analyze WYs  
 571 2017 and 2018. This 4-year simulation covers a relatively wet (2017) and dry (2018) WY. The  
 572 annual average precipitation in 2017 was  $\sim 15\%$  higher than the annual average precipitation in  
 573 2015. After this wet WY, the watershed is characterized by a dry climate in 2018, with average  
 574 precipitation almost 50% below the normal conditions. Figure 10 shows the distributions of  
 575 hillslope annual average values of precipitation and ET, and the hillslope  $\Delta P_2$  associated with the  
 576 defined  $\Delta P_1$  zones and for both the wet WY 2017 and the dry WY 2018. We have selected the key  
 577 variables describing the hydroclimate (Precipitation), land surface processes (ET), and subsurface  
 578 hydrodynamics ( $\Delta P_2$ ).

**Wet WY, 2017**



**Dry WY, 2018**



579

580 Figure 10: Frequency distributions of hillslope annual average daily rates of precipitation and  
581 evapotranspiration (ET), and the hillslope seasonal changes in groundwater levels ( $\Delta P_2$ ) in 2017  
582 (wet WY) and 2018 (dry WY) of the three zones derived from the WY 2015  $\Delta P_1$

583

584 At first glance, for both dry and wet years and selected processes, all zones remain distinct.  
585 Zone 1 with hillslopes with low  $\Delta P_1$  located in low elevation remains with low precipitation, high  
586 ET through both wet and dry years. Zone 3 describing hillslopes with high  $\Delta P_1$  has the highest  
587 precipitation in the area during both the wet and dry years. Hillslopes of zone 2, located in mid-  
588 elevation, have most of their hydrologic dynamics in between those of zone 1 and 3 except their  
589 ET, which is the highest in the area due to the presence of forest. Our results show that although  
590 we defined hillslopes clustering based on a hydrologic process during an average WY, our  
591 clustering approach can predict the similarity of the dynamics of these hillslopes in wet and dry  
592 conditions. The  $\Delta P_1$  clustering is, therefore, robust in predicting similarity in hydrologic responses  
593 under both wet and dry conditions.

594

## 595 **5. Summary and conclusions**

596 In this study, we use seasonal changes in groundwater levels termed  $\Delta P_1$  to identify and  
597 categorize similar hillslopes.  $\Delta P_1$  is an important variable controlled by many hydrologic processes  
598 including land surface processes and hydroclimatic. We defined three zones based on their  
599 similarity in  $\Delta P_1$ . For a test case site in the East River watershed, zone 1 characterizes hillslopes  
600 with low  $\Delta P_1$ ; these hillslopes are mostly located in low elevation areas, their main land cover is  
601 grassland, and their ET is high because their WTDs are shallow. Zone 3, on the opposite of zone  
602 1 is located in high elevation areas and has high  $\Delta P_1$ ; the hydroclimate leads to high snow

603 accumulation and low ET. Hillslopes of zone 3 are mostly bare soil. Zone 2 is in-between these  
604 two zones, most of the hillslopes of this zone are covered by forests.

605 We tested the performance of the proposed  $\Delta P_1$  clustering by comparing it with other  
606 existing clustering approaches based on elevation, land cover, aridity index, a topographic wetting  
607 index, and three clustering approaches based on machine learning which uses multiple data layers,  
608 including model inputs and outputs. Our results show that the  $\Delta P_1$  clustering is robust, as it  
609 reasonably identifies and categorizes hillslopes with similar elevation, land cover, hydroclimate  
610 characteristics, land surface processes (ET and SWE), and subsurface hydrodynamics (WTD, soil  
611 moisture, and  $\Delta P_1$ ). In general, the other clustering approaches are good in identifying similarity  
612 in a single characteristic related to the variable determining the clustering. Our work also  
613 demonstrates that a clustering using machine learning, either based on top-down (inputs) or  
614 bottom-up (outputs) performs well. Nevertheless, these clustering approaches like the  $\Delta P_1$ , require  
615 multiple datasets, each one with its own associated uncertainty. We further demonstrate the  
616 robustness of the proposed  $\Delta P_1$  clustering by testing its ability to predict hillslope responses to wet  
617 and dry hydrologic conditions. The  $\Delta P_1$  values are derived from a model and could be a limitation  
618 for sites where simulated outputs are unavailable, or the spatio-temporal resolution of groundwater  
619 observations are limited. In addition, one of the main limitations of the proposed clustering is that  
620 due to the disconnection between land surface processes and structures and the subsurface  
621 dynamics in some regions, this clustering approach cannot be used in these conditions.

622 Future studies could aim to identify similar hillslopes using  $\Delta P_1$  and sophisticated machine  
623 learning approaches or optimization procedures. Our results are limited to one catchment, which  
624 has snow-dominated hydrology. Future studies could expand the comparison shown here to other

625 watersheds, to include additional clustering approaches, and for different hydroclimate and  
626 durations of time (for example, sub-annual or multi-annual clustering).

627 **Data availability**

628 Data supporting the findings of this study are freely available on ESS-DIVE:

629 <https://ess-dive.lbl.gov>

630 **Author contribution**

631 The authors contribute equally to this work.

632 **Competing interests**

633 The authors declare that they have no conflict of interest.

634

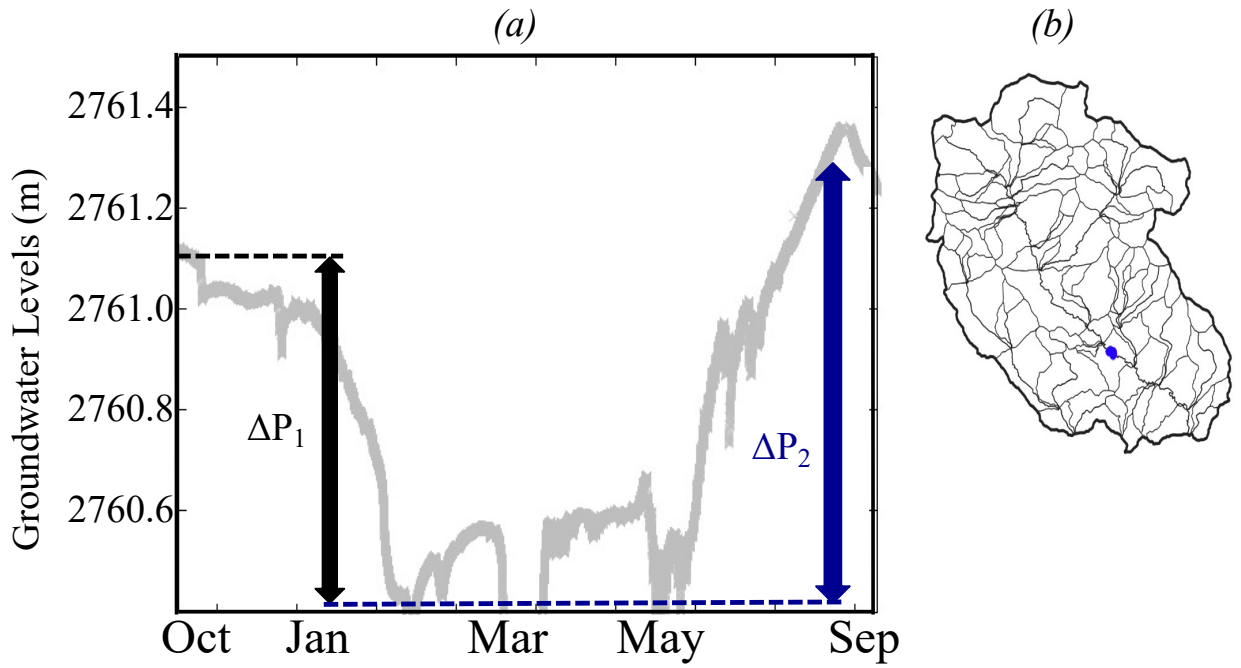
635 **Acknowledgements**

636 This material is based on work supported as part of the Watershed Function Scientific Focus Area

637 funded by the U.S. Department of Energy, Office of Science, Office of Biological and

638 Environmental Research under Award no. DE-AC02-05CH11231.





640

641

Figure A1: (a) Measured groundwater levels in WY2016 at a station located in blue in (b)

642  
643  
644  
645  
646  
647  
648  
649  
650  
651  
652  
653  
654  
655  
656  
657  
658  
659  
660  
661  
662  
663  
664  
665

## References

- Andréassian, V., Lerat, J., Le Moine, N., & Perrin, C. (2012). Neighbors: Nature's own hydrological models. *Journal of Hydrology*, 414–415, 49–58. <https://doi.org/10.1016/j.jhydrol.2011.10.007>
- Aryal, S. K., O'Loughlin, E. M., & Mein, R. G. (2002). A similarity approach to predict landscape saturation in catchments. *Water Resources Research*, 38(10), 26-1-26–16. <https://doi.org/10.1029/2001WR000864>
- Berghuijs, W. R., Sivapalan, M., Woods, R. A., & Savenije, H. H. G. (2014). Patterns of similarity of seasonal water balances: A window into streamflow variability over a range of time scales. *Water Resources Research*, 50(7), 5638–5661. <https://doi.org/10.1002/2014WR015692>
- Berne, A., Uijlenhoet, R., & Troch, P. A. (2005). Similarity analysis of subsurface flow response of hillslopes with complex geometry. *Water Resources Research*, 41(9). <https://doi.org/10.1029/2004WR003629>
- Beven, K. J. (2000). Uniqueness of place and process representations in hydrological modelling. *Hydrology and Earth System Sciences*, 4(2), 203–213. <https://doi.org/10.5194/hess-4-203-2000>
- BEVEN, K. J., & KIRKBY, M. J. (1979). A physically based, variable contributing area model of basin hydrology / Un modèle à base physique de zone d'appel variable de l'hydrologie du bassin versant. *Hydrological Sciences Bulletin*, 24(1), 43–69. <https://doi.org/10.1080/02626667909491834>
- Bormann, H. (2010). Towards a hydrologically motivated soil texture classification. *Geoderma*, 157(3), 142–153. <https://doi.org/10.1016/j.geoderma.2010.04.005>

666 Bosch, J. M., & Hewlett, J. D. (1982). A review of catchment experiments to determine the effect  
667 of vegetation changes on water yield and evapotranspiration. *Journal of Hydrology*, 55(1),  
668 3–23. [https://doi.org/10.1016/0022-1694\(82\)90117-2](https://doi.org/10.1016/0022-1694(82)90117-2)

669 Brown, A. E., Zhang, L., McMahon, T. A., Western, A. W., & Vertessy, R. A. (2005). A review  
670 of paired catchment studies for determining changes in water yield resulting from  
671 alterations in vegetation. *Journal of Hydrology*, 310(1), 28–61.  
672 <https://doi.org/10.1016/j.jhydrol.2004.12.010>

673 Brunner, P., & Simmons, C. T. (2012). HydroGeoSphere: A Fully Integrated, Physically Based  
674 Hydrological Model. *Groundwater*, 50(2), 170–176. [https://doi.org/10.1111/j.1745-](https://doi.org/10.1111/j.1745-6584.2011.00882.x)  
675 [6584.2011.00882.x](https://doi.org/10.1111/j.1745-6584.2011.00882.x)

676 Carrillo, G., Troch, P. A., Sivapalan, M., Wagener, T., Harman, C., & Sawicz, K. (2011).  
677 Catchment classification: hydrological analysis of catchment behavior through process-  
678 based modeling along a climate gradient. *Hydrology and Earth System Sciences*, 15(11),  
679 3411–3430. <https://doi.org/10.5194/hess-15-3411-2011>

680 Carroll, R. W. H., Bearup, L. A., Brown, W., Dong, W., Bill, M., & Williams, K. H. (2018).  
681 Factors controlling seasonal groundwater and solute flux from snow-dominated basins.  
682 *Hydrological Processes*, 32(14), 2187–2202. <https://doi.org/10.1002/hyp.13151>

683 CGIAR-CSI. (2019, January 24). Global Aridity Index and Potential Evapotranspiration Climate  
684 Database v2. Retrieved August 22, 2020, from  
685 [https://cgiarcsi.community/2019/01/24/global-aridity-index-and-potential-](https://cgiarcsi.community/2019/01/24/global-aridity-index-and-potential-evapotranspiration-climate-database-v2/)  
686 [evapotranspiration-climate-database-v2/](https://cgiarcsi.community/2019/01/24/global-aridity-index-and-potential-evapotranspiration-climate-database-v2/)

687 Chadwick, K. D., Brodrick, P. G., Grant, K., Goulden, T., Henderson, A., Falco, N., Wainwright,  
688 H., Williams, K. H., Bill, M., Breckheimer, I., Brodie, E. L., Steltzer, H., Rick Williams,

689 C. F., Blonder, B., Chen, J., Dafflon, B., Damerow, J., Hancher, M., Khurram, A., ...  
690 Maher, K. (2020). Integrating airborne remote sensing and field campaigns for ecology and  
691 earth system science. *Methods in Ecology and Evolution*, 11, 1492–1508.  
692 <https://doi.org/10.1111/2041-210x.13463>

693 Chaney, N. W., Van Huijgevoort, M. H. J., Shevliakova, E., Malyshev, S., Milly, P. C. D.,  
694 Gauthier, P. P. G., & Sulman, B. N. (2018). Harnessing big data to rethink land  
695 heterogeneity in Earth system models. *Hydrology and Earth System Sciences*, 22(6), 3311–  
696 3330. <https://doi.org/10.5194/hess-22-3311-2018>

697 Condon, L. E., Maxwell, R. M., & Gangopadhyay, S. (2013). The impact of subsurface  
698 conceptualization on land energy fluxes. *Advances in Water Resources*, 60, 188–203.  
699 <https://doi.org/10.1016/j.advwatres.2013.08.001>

700 Cosgrove, B. A., Lohmann, D., Mitchell, K. E., Houser, P. R., Wood, E. F., Schaake, J. C., et al.  
701 (2003). Real-time and retrospective forcing in the North American Land Data Assimilation  
702 System (NLDAS) project. *Journal of Geophysical Research: Atmospheres*, 108(D22).  
703 <https://doi.org/10.1029/2002JD003118>

704 Dai, Y., Zeng, X., Dickinson, R. E., Baker, I., Bonan, G. B., Bosilovich, M. G., et al. (2003). The  
705 Common Land Model. *Bulletin of the American Meteorological Society*, 84(8), 1013–  
706 1024. <https://doi.org/10.1175/BAMS-84-8-1013>

707 Daly, C., Halbleib, M., Smith, J. I., Gibson, W. P., Doggett, M. K., Taylor, G. H., et al. (2008).  
708 Physiographically sensitive mapping of climatological temperature and precipitation  
709 across the conterminous United States. *International Journal of Climatology*, 28(15),  
710 2031–2064. <https://doi.org/10.1002/joc.1688>

711 Devadoss, J., Falco, N., Dafflon, B., Wu, Y., Franklin, M., Hermes, A., et al. (2020). Remote  
712 Sensing-Informed Zonation for Understanding Snow, Plant and Soil Moisture Dynamics  
713 within a Mountain Ecosystem. *Remote Sensing*, 12(17), 2733.  
714 <https://doi.org/10.3390/rs12172733>

715 Fan, Y., Clark, M., Lawrence, D. M., Swenson, S., Band, L. E., Brantley, S. L., et al. (2019).  
716 Hillslope Hydrology in Global Change Research and Earth System Modeling. *Water*  
717 *Resources Research*, 55(2), 1737–1772. <https://doi.org/10.1029/2018WR023903>

718 Fan, Y., Clark, M., Lawrence, D. M., Swenson, S., Band, L. E., Brantley, S. L., Brooks, P. D.,  
719 Dietrich, W. E., Flores, A., Grant, G., Kirchner, J. W., Mackay, D. S., McDonnell, J. J.,  
720 Milly, P. C. D., Sullivan, P. L., Tague, C., Ajami, H., Chaney, N., Hartmann, A.,  
721 Hazenberg, P., McNamara, J., Pelletier, J., Perket, J., Rouholahnejad-Freund, E., Wagener,  
722 T., Zeng, X., Beighley, E., Buzan, J., Huang, M., Livneh, B., Mohanty, B. P., Nijssen, B.,  
723 Safeeq, M., Shen, C., van Verseveld, W., Volk, J., and Yamazaki, D. (2019). Hillslope  
724 hydrology in global change research and Earth system modeling, *Water Resour. Res.*, 55,  
725 1737–1772, <https://doi.org/10.1029/2018WR023903>.

726 Falco N ; Balde A ; Breckheimer I ; Brodie E ; G. Brodrick P ; Chadwick K D ; Chen J ; Dafflon  
727 B ; Henderson A ; Lamb J ; Maher K ; Kueppers L ; Steltzer H ; Wainwright H ; Williams  
728 K ; S. Hubbard S (2020): Plant species distribution within the Upper Colorado River Basin  
729 estimated by using hyperspectral and LiDAR airborne data. Watershed Function SFA,  
730 ESS-DIVE repository. Dataset. doi:10.15485/1602034 accessed via <https://data.ess->  
731 [dive.lbl.gov/datasets/doi:10.15485/1602034](https://data.ess-dive.lbl.gov/datasets/doi:10.15485/1602034) on 2022-03-29

732 Ferguson, I. M., & Maxwell, R. M. (2010). Role of groundwater in watershed response and land  
733 surface feedbacks under climate change. *Water Resources Research*, 46(10).  
734 <https://doi.org/10.1029/2009WR008616>

735 Freeze, R. A., & Harlan, R. L. (1969). Blueprint for a physically-based, digitally-simulated  
736 hydrologic response model. *Journal of Hydrology*, 9(3), 237–258.  
737 [https://doi.org/10.1016/0022-1694\(69\)90020-1](https://doi.org/10.1016/0022-1694(69)90020-1)

738 Foster, L.M., Williams, K.H., Maxwell, R.M., 2020. Resolution matters when modeling climate  
739 change in headwaters of the Colorado River. *Environ. Res. Lett.*  
740 <https://doi.org/10.1088/1748-9326/aba77f>

741 van Genuchten, M. Th. (1980). A Closed-form Equation for Predicting the Hydraulic Conductivity  
742 of Unsaturated Soils<sup>1</sup>. *Soil Science Society of America Journal*, 44(5), 892.  
743 <https://doi.org/10.2136/sssaj1980.03615995004400050002x>

744 Grabs, T., Seibert, J., Bishop, K., & Laudon, H. (2009). Modeling spatial patterns of saturated  
745 areas: A comparison of the topographic wetness index and a dynamic distributed model.  
746 *Journal of Hydrology*, 373(1), 15–23. <https://doi.org/10.1016/j.jhydrol.2009.03.031>

747 Goulden T ; Hass B ; Brodie E ; Chadwick K D ; Falco N ; Maher K ; Wainwright H ; Williams  
748 K (2020): NEON AOP Survey of Upper East River CO Watersheds: LAZ Files, LiDAR  
749 Surface Elevation, Terrain Elevation, and Canopy Height Rasters. Watershed Function  
750 SFA, ESS-DIVE repository. Dataset. doi:10.15485/1617203 accessed via [https://data.ess-](https://data.ess-dive.lbl.gov/datasets/doi:10.15485/1617203)  
751 [dive.lbl.gov/datasets/doi:10.15485/1617203](https://data.ess-dive.lbl.gov/datasets/doi:10.15485/1617203) on 2022-03-29

752 Harman, C., & Sivapalan, M. (2009). A similarity framework to assess controls on shallow  
753 subsurface flow dynamics in hillslopes. *Water Resources Research*, 45(1).  
754 <https://doi.org/10.1029/2008WR007067>

755 Hjerdt, K. N., McDonnell, J. J., Seibert, J., & Rodhe, A. (2004). A new topographic index to  
756 quantify downslope controls on local drainage. *Water Resources Research*, 40(5).  
757 <https://doi.org/10.1029/2004WR003130>

758 Hubbard, S. S., Williams, K. H., Agarwal, D., Banfield, J., Beller, H., Bouskill, N., et al. (2018).  
759 The East River, Colorado, Watershed: A Mountainous Community Testbed for Improving  
760 Predictive Understanding of Multiscale Hydrological–Biogeochemical Dynamics. *Vadose*  
761 *Zone Journal*, 17(1), 180061. <https://doi.org/10.2136/vzj2018.03.0061>

762 IGBP. (2018). Global plant database published - IGBP [text]. Retrieved October 17, 2018, from  
763 [http://www.igbp.net/news/news/news/globalplantdatabasepublished.5.1b8ae20512db692f](http://www.igbp.net/news/news/news/globalplantdatabasepublished.5.1b8ae20512db692f2a6800014762.html)  
764 [2a6800014762.html](http://www.igbp.net/news/news/news/globalplantdatabasepublished.5.1b8ae20512db692f2a6800014762.html)

765 Jefferson, J. L., Gilbert, J. M., Constantine, P. G., & Maxwell, R. M. (2015). Active subspaces for  
766 sensitivity analysis and dimension reduction of an integrated hydrologic model. *Computers*  
767 *& Geosciences*, 83, 127–138. <https://doi.org/10.1016/j.cageo.2015.07.001>

768 Kassambara, A. (2017). *Practical guide to cluster analysis in R: Unsupervised machine learning*  
769 (Vol. 1). Sthda.

770 Loritz, R., Kleidon, A., Jackisch, C., Westhoff, M., Ehret, U., Gupta, H., & Zehe, E. (2019). A  
771 topographic index explaining hydrological similarity by accounting for the joint controls  
772 of runoff formation. *Hydrology and Earth System Sciences*, 23(9), 3807–3821.  
773 <https://doi.org/10.5194/hess-23-3807-2019>

774 Lyon, S. W., & Troch, P. A. (2007). Hillslope subsurface flow similarity: Real-world tests of the  
775 hillslope Péclet number. *Water Resources Research*, 43(7).  
776 <https://doi.org/10.1029/2006WR005323>

777 Lyon, Steve W., & Troch, P. A. (2010). Development and application of a catchment similarity  
778 index for subsurface flow. *Water Resources Research*, 46(3).  
779 <https://doi.org/10.1029/2009WR008500>

780 Maina, F. Z., & Siirila-Woodburn, E. R. (2020). The Role of Subsurface Flow on  
781 Evapotranspiration: A Global Sensitivity Analysis. *Water Resources Research*, 56(7),  
782 e2019WR026612. <https://doi.org/10.1029/2019WR026612>

783 Maina, Fadji Z., Siirila-Woodburn, E. R., & Denedy-Frank, P. J. (2022) Assessing the impacts of  
784 hydrodynamic parameter uncertainties on simulated evapotranspiration in a mountainous  
785 watershed. *Journal of Hydrology* 608. <https://doi.org/10.1016/j.jhydrol.2022.127620>.

786 Maxwell, R. M. (2013). A terrain-following grid transform and preconditioner for parallel, large-  
787 scale, integrated hydrologic modeling. *Advances in Water Resources*, 53, 109–117.  
788 <https://doi.org/10.1016/j.advwatres.2012.10.001>

789 Maxwell, R. M., & Miller, N. L. (2005). Development of a Coupled Land Surface and  
790 Groundwater Model. *Journal of Hydrometeorology*, 6(3), 233–247.  
791 <https://doi.org/10.1175/JHM422.1>

792 McDonnell, J. J., & Woods, R. (2004). On the need for catchment classification. *Journal of*  
793 *Hydrology*, 299, 2–3. <https://doi.org/10.1016/j.jhydrol.2004.09.003>

794 Noël, P., Rousseau, A. N., Paniconi, C., & Nadeau, D. F. (2014). Algorithm for Delineating and  
795 Extracting Hillslopes and Hillslope Width Functions from Gridded Elevation Data. *Journal*  
796 *of Hydrologic Engineering*, 19(2), 366–374. [https://doi.org/10.1061/\(ASCE\)HE.1943-](https://doi.org/10.1061/(ASCE)HE.1943-5584.0000783)  
797 [5584.0000783](https://doi.org/10.1061/(ASCE)HE.1943-5584.0000783)



798 Oudin, L., Kay, A., Andréassian, V., & Perrin, C. (2010). Are seemingly physically similar  
799 catchments truly hydrologically similar? *Water Resources Research*, *46*(11).  
800 <https://doi.org/10.1029/2009WR008887>

801 Pribulick, C. E., Foster, L. M., Bearup, L. A., Navarre-Sitchler, A. K., Williams, K. H., Carroll, R.  
802 W. H., & Maxwell, R. M. (2016). Contrasting the hydrologic response due to land cover  
803 and climate change in a mountain headwaters system. *Ecohydrology*, *9*(8), 1431–1438.  
804 <https://doi.org/10.1002/eco.1779>

805 Rahman, M., Sulis, M., & Kollet, S. J. (2016). Evaluating the dual-boundary forcing concept in  
806 subsurface–land surface interactions of the hydrological cycle. *Hydrological Processes*,  
807 *30*(10), 1563–1573. <https://doi.org/10.1002/hyp.10702>

808 Richards, L. A. (1931). Capillary conduction of liquids through porous medium. *Journal of*  
809 *Applied Physics*, *1*(5), 318–333. <https://doi.org/10.1063/1.1745010>

810 Ryken, A., Bearup, L. A., Jefferson, J. L., Constantine, P., & Maxwell, R. M. (2020). Sensitivity  
811 and model reduction of simulated snow processes: Contrasting observational and  
812 parameter uncertainty to improve prediction. *Advances in Water Resources*, *135*, 103473.  
813 <https://doi.org/10.1016/j.advwatres.2019.103473>

814 Sawicz, K., Wagener, T., Sivapalan, M., Troch, P. A., & Carrillo, G. (2011). Catchment  
815 classification: empirical analysis of hydrologic similarity based on catchment function in  
816 the eastern USA. *Hydrology and Earth System Sciences*, *15*(9), 2895–2911.  
817 <https://doi.org/10.5194/hess-15-2895-2011>

818 Schwanghart, W., & Scherler, D. (2014). Short Communication: TopoToolbox 2 – MATLAB-  
819 based software for topographic analysis and modeling in Earth surface sciences. *Earth*  
820 *Surface Dynamics*, *2*(1), 1–7. <https://doi.org/10.5194/esurf-2-1-2014>

821 SIVAPALAN, M., TAKEUCHI, K., FRANKS, S. W., GUPTA, V. K., KARAMBIRI, H.,  
822 LAKSHMI, V., et al. (2003). IAHS Decade on Predictions in Ungauged Basins (PUB),  
823 2003–2012: Shaping an exciting future for the hydrological sciences. *Hydrological*  
824 *Sciences Journal*, 48(6), 857–880. <https://doi.org/10.1623/hysj.48.6.857.51421>

825 Wagener, T., Sivapalan, M., Troch, P., & Woods, R. (2007). Catchment Classification and  
826 Hydrologic Similarity. *Geography Compass*, 1(4), 901–931.  
827 <https://doi.org/10.1111/j.1749-8198.2007.00039.x>

828 Wainwright, H. M., Uhlemann, S., Franklin, M., Falco, N., Bouskill, N. J., Newcomer, M.,  
829 Dafflon, B., Woodburn, E., Minsley, B. J., Williams, K. H., and Hubbard, S. S. (2022).  
830 Watershed zonation approach for tractably quantifying above-and-belowground watershed  
831 heterogeneity and functions, *Hydrol. Earth Syst. Sci.*, <https://doi.org/10.5194/hess-2021->  
832 228.

833