Anonymous Referee #2

As this referee has already reviewed the first submission of the manuscript, we are glad to read that the referee appreciates our changes to the script.

Recommendation: minor revisions

This manuscript presents the 'Empirical Quantile Adjustment' (EQM) method for statistical bias correction of climate model output, including a version that allows to increase the number of dry days (EQAd). The EQA method is a development of existing versions for bias correction, while the dry-day correction is a new approach. The manuscript compares EQAd with two frequently used alternative approaches to bias correction, with respect to the representation of the mean, of the climate change signal (CCS), and of the number of dry days. These criteria reflect practical requirements well.

It is found that EQAd performs as well or better than the other methods on each of the criteria. This is not surprising because EQAd has been designed to do well with respect to all of these criteria. The value of the manuscript is that it demonstrates that other methods have some practically relevant shortcomings, and that it is possible to construct a bias correction method that addresses these.

I have reviewed a previous submission by the authors on this topic, which was not published, mainly because the bias correction approach taken was not justified well enough. The new manuscript is substantially improved, much more systematic, and now explains most conceptual and technical aspects very well. In addition, it provides a systematic overview on the various approaches to bias correction with a good discussion of their structural differences.

This paper is now a very useful contribution to the development and understanding of bias correction methods. It is concisely written and it was a pleasure reading it. The points listed below should be further clarified. I recommend publication after they have been addressed.

Specific comments

1)

The authors frequently mention that EQA and similar methods are based on quantiles, that the biases at quantiles do not change over time etc., whereas QM is said to be based on specific values. This terminology is not wrong, but I don't think it is the best choice to reduce confusion. Many researchers would presumably consider QM to also be based on quantiles (hence the name). The key question is from which distribution the quantiles are determined for a given value in the future. As mentioned by the authors in the last sentence of section 3.4 QM determines the quantile for a given future value from the calibration distribution. This point should be clarified already in the introduction when the different approaches are discussed.

Thanks for this clarification. We will mention this after the paragraph in the introduction (line 62), where we discuss the methods that do not alter the CCS. Both the CCS discussion and whether the quantiles (CDF) are calculated from the calibration or from the future period are highly related to each other.

Also, we will change this in the lines 181-183 and in the conclusion around line 420.

2)

The point above also applies to the discussion of stationarity in lines 63-68. QM assumes stationarity of the bias for each quantile with quantiles derived from the calibration distribution, regardless of whether a value is taken from the calibration or the future periods. EQA and similar methods assume a stationary bias for

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each quantile, but with the quantiles for a value from the future period derived from the future distribution. As discussed in the manuscript, the latter is for additive corrections equivalent to assuming a stationary bias in the mean, but this is not the case for multiplicative methods.

This is an interesting perspective, that will be included in the above-mentioned paragraph.

3)

Fig 3. is very helpful, but I am not convinced it is in the right place in the paper. The figure illustrates the two basic options for distribution-based bias correction. This is a general issue and not specific to EQA. The related discussion could be part of the method review in the introduction, or a new subsection could be included at the beginning of the method section that systematically discusses the two options (this section could also address the next two points). The very large changes in the CCS introduced by QM in Fig. 3 are essentially caused by the fact that the raw CCS is large compared to the standard deviation of the distributions, and that the standard deviations of the model and the observations are quite different. This is useful to clarify the argument, but it might be interesting to also consider a less extreme example.

As the introduction is already very long, a new subsection "3.1 Definition of quantile-based methods" in section 3 makes more sense. In this subsection, we will discuss Fig. 3. We also can include new subplots in the figure where the CCS is smaller than the standard deviation of the data.

4)

In section 3.1 the authors attempt to explain why the EQA and other approaches that determine the quantile for a future value from the future distribution are better justified than the QM approach. The argument is based on the claim that RCMs are 'able to predict a ranked' category, and on 'a specific weather pattern will have different absolute values in the future but the same quantile'. The arguments are not clear to me. Ranking is an ordering of a set of values. Which values are considered here? What means a weather pattern has the same quantile? These arguments should be clarified and may add interesting aspects, but views on these issues might differ. I don't think these are the key arguments in support of bias correction methods that use future distributions.

We postulate that the bias of a climate model is correlated to the modeled weather pattern. If we assume that the frequency of weather patterns does not change significantly over time, this means, that certain quantiles of temperature are linked to certain weather situations. Because QM corrects absolute values, regardless of the underlying weather conditions, trends are modified. Thus, if one wants to preserve trends, one must at least implicitly account for weather conditions. Now, we argue that EQA and similar methods do this implicitly, assuming that weather situation frequencies change little and that biases are primarily weather situation dependent, not absolute value dependent: a weather situation in the future would then have a higher temperature value accordingly, but still the same quantile. An example:

A cold winter day in Austria is related to moderate northeasterly flows and usually high atmospheric pressure with low wind and clear sky conditions. Cold translates to a low quantile for temperature. In future, the error of the model in this weather situation is assumed to stay constant. This weather situation will still translate to a low quantile in the future distribution, however the absolute temperature values are higher (respectively the corresponding quantile calculated from the historical distribution is higher).

If the referee agrees, we will adapt the lines 177-186 to the above said. Also, this is background information and will be shifted to the new subsection 3.1 and the old subsection will be limited to the description of the application of the EQA.

5)

In my understanding the most important justification for using EQA and similar methods is that it preserves the CCS for additive corrections, and with the modification introduced in the paper also for multiplicative corrections.

As I said in my previous review it is far from clear that the CCS should be preserved. Nevertheless, preserving the CCS might in many applications be a more sensible approach than altering it in a rather uncontrolled way by using QM. It is good that the paper makes it clear now that preserving the CCS is a choice, not an a priori given desired property. I think it would be good to emphasise that if researchers decided to retain the CCS the EQA method provides a bias correction method that does this and has additional useful properties.

We agree. That is why in the introduction we will point out more clearly, that preserving the CCS is a choice of the researcher and mention this also in the new subsection 3.1.

6) Line 213:, F_100 are not 'the 100 CVs to correct the model data', they are the percentiles for which the CVs are defined through eqn. 3.

Will be changed to your suggestion.

7) Lines 221-222: What is called 'parameters' here should be 'variables'. A variable is a number that changes, for instance in time and space, and specifies the state of a system. A parameter is a number that can take different values and once specified specifies the system itself (for instance parameterisations in dynamical models or parameters in statistical models).

I know that meteorologist tend to use the former when it should be the latter, but throughout most of the paper variables are correctly called variables, and this should be done everywhere.

Thanks you for this clarification. It will be changed to "variables".

8) Eqns. 5 and 6: The variable names for the ranked variables should be different from those for the unranked variables. This could be done for instance by adding a ',r' to the subscripts.

This will be added to the variables.

9) Lines 246-248: The explanation for step 6 is unclear.

30 years of data is used for bias adjustment. Usually, climate models cover more than 100 years. Theoretically, it is possible to bias adjust 30-year periods that do not overlap, e.g. 1981-2010, 2011-2040, 2041-2070 etc. However, this will introduce inhomogeneities between the periods. This is why the 30 years of data is shifted in 10-year steps and only the middle 10-year period is actually kept as bias adjusted data.

This will be clarified in step 6.

10) Line 300: 'in future' should be 'in the future'

Done.

11) Fig. 5. It would be informative to add a panel that shows the difference between the raw model and the observations.

This is a good suggestion. The figure will be reshaped to a 3x3 plot which contains also the difference between raw model and observations.

hess-2021-498

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12) Line 378: I don't think one should use the formulation 'error in CCS', because the true CCS is unknown. It is better to say that QM modifies the CCS from the raw model, and that the specific modification might be difficult to justify.

This will be changed. Also, in Fig. 7 we will change the "error" to "modification of CCS".

13) Figs. 5 - 9. The interval boundaries for the colour bars are neither linear nor logarithmic, and some of the colours are difficult to distinguish. Is there a clear reason for the choice of the intervals? Can they be defined more systematically?

The colors were chosen because they should be intuitive, e.g. yellow-green-blue for precipitation. However, we will make the bars less arbitrary. The new color bars will be more linear respectively logarithmic:

Annual precipitation sum: 100, 300, 500, 700, 900, 1100, 1300, 1500, 2000, >2000

Annual precipitation difference (Fig.5 and Fig. 8): <-80, -40, -20, -10, 10, 20, 40, 80, >80

CCS modification (Fig.7): <-8, -4, -2, -1, 1, 2, 4, 8, >8

Annual wet days (Fig.9): <90, 90, 100, 110, 120, 140, 160, 180, 200, >200

Annual wet days difference (Fig.9): <-80, -40, -20, -10, 10, 20, 40, 80, >80

14)

There are several sentences where 'which' is used in situations where it should be 'that'. The former should be used if additional information is added, the latter if a defining property is stated.

In our opinion, this refers to the following lines and will be changed: 4, 59, 109, 212, 288, 316, 346 and 416.