



Rill Erosion on Slope of Spoil tips: experimental study of runoff scouring erosion in multiple times

Yongcai Lou¹, Zhaoliang Gao^{1,2}, Fuyu Zhou¹, Jianwei Ai¹, Yunfeng Cen¹, Tong Wu² and Jianbin Xie³

¹State Key Laboratory of Soil Erosion and Dryland Farming on the Loess Plateau, Institute of Water and Soil Conservation, Northwest A&F University, Yangling, Shaanxi, China.

²Institute of Soil and Water Conservation, Chinese Academy of Sciences and Ministry of Water Resources, Yangling, Shaanxi, China.

³College of Architecture and Planning, Kunming, Yunnan, China.

Correspondence to: Zhaoliang Gao (gzl@ms.iswc.ac.cn)

Abstract. The soil erosion of the spoil tips seriously threatens the safety of people's lives and property and the surrounding ecological environment. Rill erosion is an important cause of water and soil loss in spoil tips. This study was conducted to investigate the process of rill erosion on the slopes of spoil tips, changes in the morphological characteristics of rills and the mechanisms of rill erosion. A Field runoff plot (5 m long, 1 m wide and 0.5 m deep) with three inflow rates (1.6, 2 and 2.4 mm min⁻¹) and three typical slopes (28°, 32° and 36°) was used for runoff simulation experiments. The results showed that, compared with the slope and scouring times, inflow rate was the most important factor affecting rill erosion of the spoil tips. The development of rill mainly goes through three stages: the rill formation stage, the rill development stage and the rill adjustment stage. The overall predominance of parallel-shaped rills at all experiments suggested that the formation of rills was dominated by concentrated runoff. The average rill depth was the best indicator of rill morphology for evaluating rill erosion. The flow regimes under the experimental conditions were supercritical-laminar flow and supercritical-transition flow. The Reynolds number was the best hydraulic parameter for predicting rill erosion. The stream power was the best hydrodynamic parameter to describe rill erosion mechanism. These results contributed to further revealing the rill erosion mechanism on the slope of the spoil tips and provided a scientific basis for its soil erosion control.

1 Introduction

Transportation, water conservancy, mining and other infrastructure construction industries are developing rapidly globally, especially in China. As a result, a large amount of spoil tips has been



31 produced(Niu et al., 2019; Yang et al., 2019). Compared with the undisturbed landscape, the typical
32 characteristics of spoil tips include loose structure without vegetation-covered, slope with steep gradients
33 and short length(Zhang et al., 2015; Lv et al., 2019). Its soil erosion rate and erosion intensity far exceed
34 those of the original landform(Mcclintock and Harbor 2013), causing significantly greater soil loss than
35 that of eroded landform units such as sloping land and forest land(Kaufman 2000). Previous studies
36 showed that spoil tips have become a major source of soil erosion from production and construction
37 projects(Peng et al., 2014). Under the effect of rainfall and runoff, spoil tips are prone to serious
38 secondary hazards such as soil erosion(Guo et al., 2020), landslides and debris flows(Conforti and Ietto
39 2020), affecting soil and water resources(Fransen et al., 2001), and the surrounding environment(Owens
40 et al., 2005), downstream rivers and water and sediment(Morokong and Blignaut 2019). Therefore, it is
41 necessary to study the processes and mechanisms of erosion of spoil tips.

42 Sheet erosion, rill erosion, gully erosion and in-stream erosion are the main types of erosion on
43 slopes(Merritt et al., 2003; Sun et al., 2013). Once rills are formed on the slope, the surface flow will
44 quickly become concentrated flow. The concentrated flow with fast velocity and strong shear force has
45 a much greater capacity to detach and transport soil particles than the erosive force caused by rainfall,
46 which will result in a sudden increase in the amount of erosion on the slope(Auerswald et al., 2009).
47 Therefore, rill erosion is the most severe erosion form among water erosion on slope, and its occurrence
48 often marks the gradual development of soil erosion into gully erosion(Chen et al., 2013). Previous
49 studies have shown that rill erosion is one of the main causes of soil loss and accounts for 70-97 % of
50 total soil erosion(Zheng and Tang 1997; Whiting et al., 2001; Sun et al., 2013). There are four stages in
51 the formation of rill: sheetflow, flowline development, micro-rills and micro-rills with head-cuts(Merritt
52 1984).Understanding of the rill erosion processes on slopes is important not only for the prevention of
53 soil erosion in spoil tips, but also for soil erosion prediction models.

54 After the appearance of rills, as the rainfall or scouring continued, the rills bifurcated, merged and
55 connected on the slope to form a complex erosion pattern that evolves into a crisscross network of
56 rills(Shen et al., 2015). Rill length, width, depth and related derived indicators (e.g., rill density, rill
57 complexity, rill width-to-depth ratio)(Cerdan et al., 2002; Tian et al., 2017; Zhang et al., 2017; Qin et al.,
58 2018) are often used to describe rill morphology. For example, Shen et al. (2019) indicated that the rill
59 width-depth ratio was a better indicator for analyzing differences in the rill characteristics for treatments
60 with different slope gradients and for assessing the rill cross-sectional features. Shen et al. (2015)



61 concluded that the average rill width was the best basic morphological indicator for evaluating rill erosion.
 62 Gilley et al. (1990) suggested that the rill density was a good description of the degree of development
 63 of rills. In the process of rill erosion, the rill morphology is largely determined by the hydrodynamic
 64 characteristics of the rill flow. In addition, rill flow hydraulic parameters (e.g., flow velocity, flow depth,
 65 Reynolds number, Froude number and Darcy-Weisbach coefficient)(Govers et al., 2007; Niu et al., 2019;
 66 Omidvar et al., 2019; Yang et al., 2020) and dynamic parameters (e.g., shear stress, stream power and
 67 unit stream power)(Zheng et al., 2004; Li et al., 2016; Guo et al., 2018) are also often used to describe
 68 the rill erosion mechanism on slopes. For example, by studying the hydrodynamic characteristics of rill
 69 erosion, Nearing et al. (1997), Reichert and Norton (2013) and Shen et al. (2016) found that stream power
 70 can more accurately to characterize the dynamic mechanisms of rill erosion. However, Tian et al. (2017)
 71 showed that shear stress is the best hydrodynamic parameter to describe rill erosion under scouring
 72 conditions. Rill morphology is the result of the interaction between the hydrodynamic factors of runoff
 73 and the soil(Zhang et al., 2015). The development of soil erosion changes the morphology of the rill bed,
 74 which in turn affects the hydrodynamic and erodibility of runoff, and changes in runoff energy led to
 75 further changes in rill morphology(Chen et al., 2015; Xu et al., 2017). The evolution of the rill
 76 morphology, the hydrodynamic properties of runoff and soil erosion thus form a complex mutual
 77 feedback process(Favis-Mortlock 1998; Gatto 2000). Therefore, it is necessary to study runoff hydraulic
 78 characteristics and dynamic mechanism of rill erosion of spoil tips.

79 Under natural conditions, it has been observed that rills on the slope of spoil tips may be formed by
 80 multiple times rainfall or runoff from upslope. Qin et al. (2018) showed that rill networks evolved in a
 81 converging way, a large number of small rills were formed during the first rainfall, rills were gradually
 82 connected during the second rainfall, the rill network was basically formed, and the rill erosion was
 83 intensified through the process of rill bifurcation, connection and merging, the rill network was further
 84 developed during the third rainfall, and by the fourth rainfall the rill network was mature. However, many
 85 studies have focused on the changes in the rill erosion process of slope during a single rainfall or scouring
 86 process(He et al., 2017; Jiang et al., 2018; Niu et al., 2020; Tian et al., 2020). The impact of multiple
 87 events on rill erosion has been ignored. Therefore, it is necessary to study the rill erosion on the slope of
 88 spoil tips under the multiple times rainfall or scouring conditions.

89 Studying the rill development and morphological characteristics is of great significance to revealing
 90 the nature of soil erosion on slope of spoil tips, and also provides a theoretical basis for the development



91 of erosion prediction models. In this study, field experiment was conducted with the objectives of: 1)
92 analyzing the change process of runoff and sediment yield on slope of spoil tips and quantifying the
93 effect of slope, inflow rate and scouring times on runoff and sediment, 2) quantifying the changes in rill
94 networks and morphological characteristics and elucidating the relationship between rill morphological
95 parameters and rill erosion, and 3) exploring the hydrodynamic mechanism of rill erosion and determine
96 the best hydrodynamic parameters for predicting rill erosion.

97 **2 Materials and Methods**

98 **2.1 Experimental site and soil samples**

99 The experimental site is located at Yangling Ling Hou Experimental Station
100 (34°19'24"N, 107°59'36"E) (Fig.1a), Institute of Soil and Water Conservation, Ministry of Water
101 Resources, Chinese Academy of Sciences. The experimental station has a continental monsoon climate,
102 with an average annual temperature and precipitation of 13°C and 610 mm, respectively, of which more
103 than 80 % is of short-duration and high-intensity and concentrated in July to September. The runoff plots
104 are built on hand-excavated side slopes, 20 m long and 5 m wide, with slopes of 28°, 32° and 36°
105 respectively (Fig.1b).

106 The experimental soil was obtained from the excavation of the extension project of the experimental
107 station. The soil used in this experiment was clay loam according to the International Soil Texture
108 Classification with 28.72 % sand (20 µm–2 mm), 40.12 % silt (20–2 µm), and 31.15 % clay (< 2 µm).

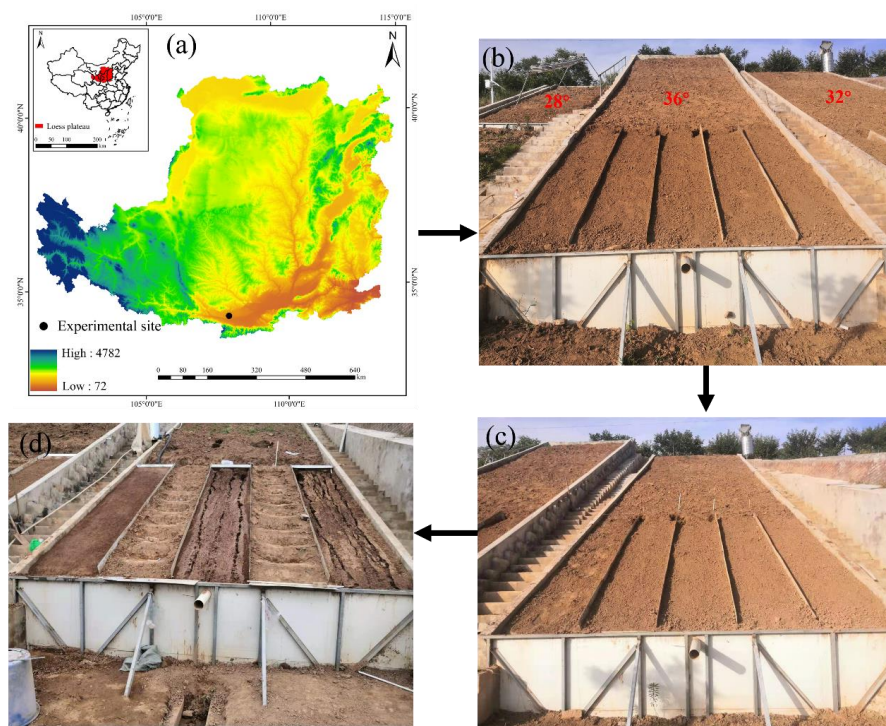


Figure 1. Location of experimental site(a) , runoff plots (b)with 28°, 32° and 36° and layout of the experimental treatments (c, d)

2.2 Experimental design

Spoil tips, as a special type of artificial landform, consists of a platform and a steep slope (Fig. 2), the platform being the main area where runoff collects and the slope being the main source of eroded sediment (Zhang et al., 2016). Therefore, this paper uses field scouring experiments to simulate the rill erosion of slopes by collected runoff from platforms. The field scouring experimental setup included a water supply line, a constant barrel, a valve, a flow meter, a steady flow groove, and collecting barrels (Fig. 3). In this study, two replicates with three slope gradients, each series contained three successive scouring were applied. Based on the short-duration and high-intensity erosive rainfall criteria ($I_5 = 1.52 \text{ mm min}^{-1}$, $I_{10} = 1.05 \text{ mm min}^{-1}$) for the Loess Plateau, inflow rates of 1.6, 2 and 2.4 mm min^{-1} were applied. The results of the field survey of 368 spoil tips show that the length of slope of 2 to 8 m account for 78.4% of the total survey, with the slope mainly concentrated at 25° to 40° (Li et al., 2020). Therefore, in the experiment runoff plots were divided into $5\text{m length} \times 1\text{m width} \times 0.5\text{m depth}$ with slopes of 28° , 32° and 36° using PVC sheets (Figs. 1c, 1d).

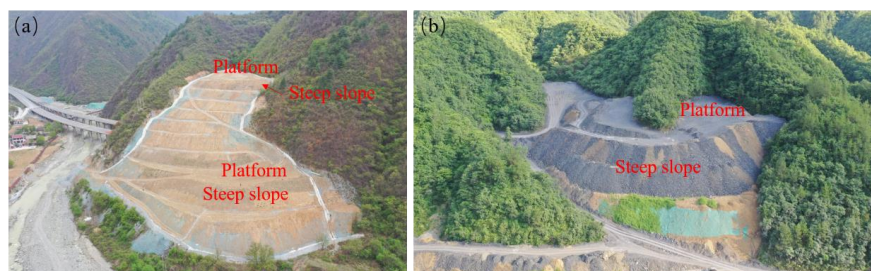


Figure 2 Spoil tips from highway construction in China

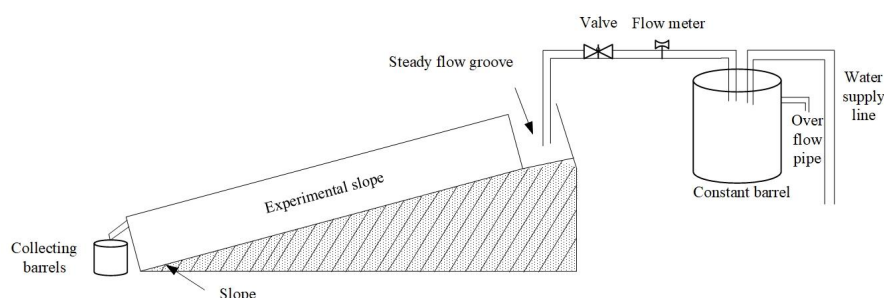


Figure 3 Layout of the field scouring experimental setup.

2.3 Experimental preparation and procedure

The runoff plots were filled with soil by the layered filling method. Firstly, the bottom layer of the plots was 5 cm thick with a soil bulk density of 1.45 g cm^{-3} , and then, a 25 cm-thick layer of lightly disturbed soil with a bulk density of 1.32 g cm^{-3} , and the top layer is a 20cm-thick heavily disturbed soil with a bulk density of 1.25 g cm^{-3} to represent typical spoil tips in the region. It should be noted that in ensuring the natural state of the soil, the experimental soil was filled into the plots without sieving only to remove plant roots, dead leaves and larger clods of soil(Niu et al., 2020).

Before start of the experiment water was sprinkled evenly on the slope to keep the initial moisture content consistent. After that, the plots were covered with plastic sheeting and left for 24 h to allow free infiltration of water close to the natural state of soil moisture distribution. The initial moisture content of the soil was 13 %.

After the experiment started, runoff and sediment samples were collected at 1 min intervals for the first 5 min after runoff generation, and then at 2 min and the sampling time was recorded with a stopwatch. Surface runoff velocities were measured with KMnO_4 coloration. The 5 m long slope were divided into: 0-0.5 m, 0.5-1.5 m, 1.5-2.5 m, 2.5-3.5 m, 3.5-4.5 m, and 4.5-5 m. Among them, 0-0.5 m and 4.5-5 m are



used as transition areas. The average of the runoff velocity of the four sections was corrected (correction factor 0.75) as the average flow velocity of the slope (Luk and Merz 1992). The water temperature was measured with a thermometer. The runoff widths of the four sections were measured with a ruler. The duration of each experiment was 45 min. The runoff and sediment samples were weighed, left for 24 h, then the supernatant was poured off and transferred to aluminum boxes, dried in an oven at 105°C for 24 h and weighed to calculate the sediment amount. A digital camera (SONY A7RII) was used to take photos of the slope surface before and after the experiment, and the overlap of each photo was required to be at least 60%. Based on the 3D photogrammetry technique, high-precision DEMs data of the experimental soil surface were obtained. After completing the slope photography, the experimental plots were covered with plastic sheeting and left for 24 h until the next experiment.

2.4 Data analysis

2.4.1 Rill hydrodynamic parameters

Flow hydrodynamic parameters have a decisive role in the runoff and sediment production characteristics of slope and are the basis for understanding the soil erosion processes and kinetic mechanisms on slope (Cao et al., 2015). Therefore, commonly used hydrodynamic parameters such as flow velocity (V), Reynolds number (Re), Froude number (Fr), Darcy-Weisbach coefficient (f), shear stress (τ), stream power (ω) and unit stream power (P) are selected to evaluate the influence of slope (S), inflow rate (I) and scouring times (N) on rill erosion of spoil tips.

The Reynolds number (Re) and the Froude number (Fr) indicate the flow pattern and flow type of the slope surface, and are calculated as follows (An et al., 2014):

$$Re = \frac{Vh}{\gamma} \quad (1)$$

$$Fr = \frac{V}{\sqrt{gh}} \quad (2)$$

where V is the average flow velocity (m s^{-1}), h is the flow depth (m), $h = \frac{q}{vbT}$, q (m^3) is the total amount of flow in a certain time T (s), b is the width of surface flow (m), γ is the kinematic viscosity ($\text{m}^2 \text{s}^{-1}$), $\gamma = \frac{0.01775}{1+0.0337t+0.000221t^2}$, t is the temperature of the water ($^{\circ}\text{C}$) and g is the gravitational acceleration (9.8 m s^{-2}).



170 The Darcy-Weisbach coefficient (f) indicates the magnitude of resistance along the slope during
 171 runoff flow and is calculated as follows (Abrahams et al., 1986):

$$172 \quad f = \frac{8gRJ}{V^2} \quad (3)$$

173 where f is the Darcy-Weisbach coefficient, J is the hydraulic gradient (m m^{-1}), which can be
 174 approximately replaced by the sine of the slope (Zhang et al., 2015), and R is the hydraulic radius (m),
 175 which is often replaced by the flow depth.

176 Shear stress (τ) indicates the runoff scouring force that produces soil particle separation and
 177 sediment transport and is calculated as follows (Nearing et al., 1991):

$$178 \quad \tau = \gamma_m g R \quad (4)$$

179 where τ is the shear stress (Pa), γ_m is the mass density of the water–sediment mixture (kg m^{-3}).

180 The stream power (ω) indicates the power consumed by the flow acting on a unit area and is
 181 calculated as follows (Govers et al., 2007):

$$182 \quad \omega = \tau V \quad (5)$$

183 where ω is the stream power ($\text{N m}^{-1} \text{s}^{-1}$).

184 Unit stream power (P) is calculated as follows (Moore and Burch 1986):

$$185 \quad p = VJ \quad (6)$$

186 where p is unit stream power (m s^{-1}).

187 2.4.2 Rill morphology parameters

188 The parameters of rill erosion such as rill depth, rill width and width-to-depth ratio were selected to
 189 quantify the development characteristics of the rill network on the slope (Cerdan et al., 2002; Shen et al.,
 190 2020) and to reflect the intensity of rill erosion along the vertical and horizontal directions. Based on the
 191 3D photo reconstruction technology (Wu et al., 2018; Di Stefano et al., 2019), the photos taken by digital
 192 cameras were imported into Agisoft Photoscan Professional 1.2.4 (Agisoft LLC, St. Petersburg, Russia)
 193 for aligning photos, generating dense point clouds, generating grid textures, generating and exporting
 194 DEMs, and so on. Afterwards, the DEMs (Resolution of 2 mm x 2 mm) data were imported into ArcGIS
 195 software and the corresponding rill morphology parameters (e.g., rill width and rill depth) were obtained
 196 with the help of mathematical and hydrological analysis functions in its spatial analysis.

197 The rill width and depth were extracted based on the 3D analysis method of ArcGIS, and a section
 198 was selected at 0.5 m intervals starting from the top of the slope to extract the rill width and depth. The
 199 average of the 10 sections was taken as the average width (ARW) and average depth (ARD). Based on the



hydrological analysis method of ArcGIS, a reasonable threshold of the cumulative amount of confluence is set to initially extract the rills on the slope, and then compare the high-resolution photos taken in the experiment to remove the non-existent fine rills.

The width-to-depth ratio of rill is an objective reflection of the variation in groove morphology (Tian et al., 2020), and is calculated as follows:

$$R_{WD} = \frac{ARW}{ARD} \quad (7)$$

where R_{WD} is the rill width–depth ratio, ARW is the average width (cm), and ARD is the average depth (cm).

All data analysis was performed using the SPSS16.0 software (IBM Corp., Armonk, NY, USA). Regression analysis was used to establish the equation simulation. Origin 8.5 software (Origin Lab Corp., Northampton, MA, USA) was used to visualize the data.

3 Results

3.1 Runoff rate

Fig. 4 illustrates the changes in runoff rate with time for three successive scouring at different slope and inflow rates. According to Fig. 4, the runoff rate showed two characteristics variation: i.e., under the lowest inflow rate (1.6 mm min^{-1}), the runoff rate increased with time in the early stages of the experiment and then gradually stabilized. The runoff rate tends to increase and then fluctuate under relatively high inflow rates (2 and 2.4 mm min^{-1}). At the early stages of the experiment, the low soil moisture content and high soil infiltration rates result in low runoff rates. As the soil moisture content increased rapidly and the soil infiltration rate decreased, runoff rates increased rapidly. When the soil infiltration rates reach a stable stage, the runoff rates also became stable. Fluctuations in runoff rates are mainly related to the development of rills (e.g., headward erosion, sidewall collapse and downcutting erosion) and are relatively greater with increasing slope and inflow rate (Jiang et al., 2018). Overall, runoff rates increase with slope, inflow rate and scouring times.

Regression analyses of slope, inflow rate and scouring times were performed to quantify their effects on runoff rate. The best-fit equation to describe the mean runoff rate as a function of the adjusted slope, inflow rate and scouring times is as follows:

$$RR = 0.0024S^{1.1076}I^{1.8603}N^{0.3367} \quad (R^2=0.9549, P<0.001, n=27) \quad (8)$$



where RR is the mean runoff rate (mm min^{-1}), S is the slope (%), I is the inflow rate (mm min^{-1}) and N is the scouring times.

The exponents in Eq. (8) are all positive, indicating that inflow rate, slope and scouring times all have a positive effect on runoff rate. The exponents for slope, inflow rate and scouring times were 1.1076, 1.8603 and 0.3367, respectively. This indicates that the inflow rate plays an important role in the runoff rate than the slope and scouring times.

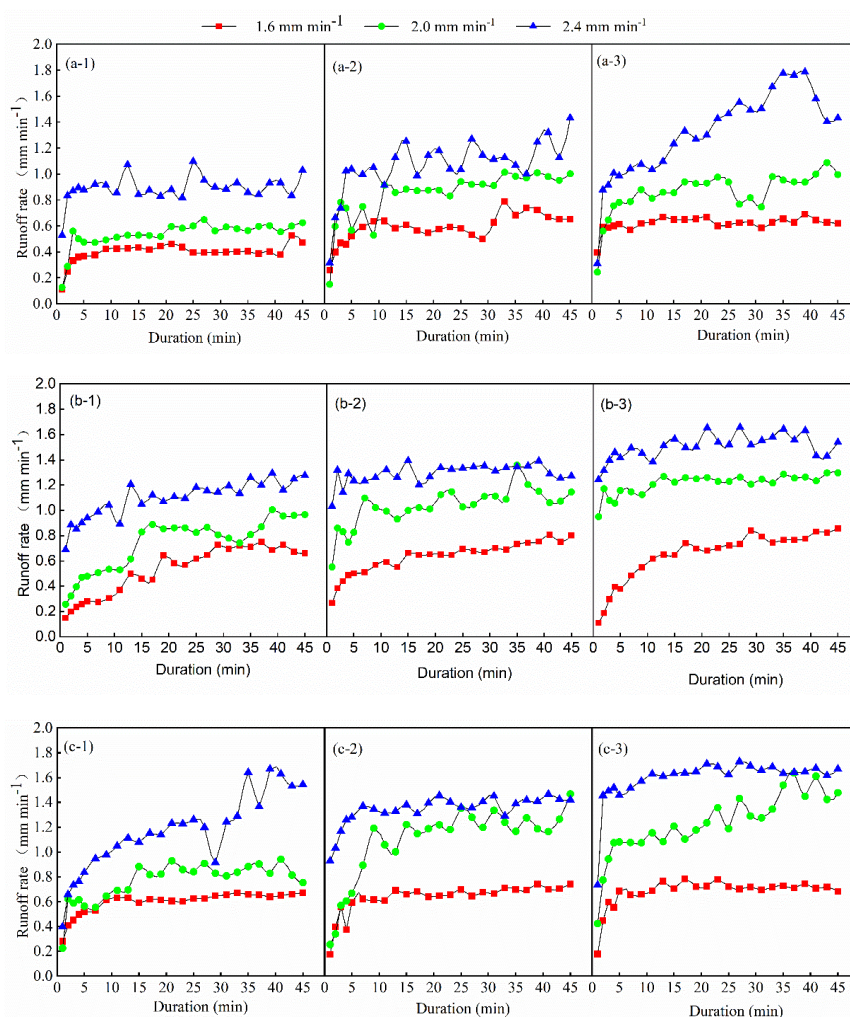


Figure 4 Variations in the runoff rate with time for three scourings at slope of 28°(a-(1-3)), 32°(b-(1-3)) and 36°(c-(1-3)).



239 3.2 Soil loss rate

240 The changes in three successive scouring soil loss rates with time for different inflow rates and
 241 slopes are shown in Fig. 5. Under the lowest inflow rate (1.6 mm min^{-1}), the soil loss rates were also low.
 242 The soil loss rates were large and fluctuated under relatively high inflow rates (2 and 2.4 mm min^{-1}). The
 243 higher the inflow rate and slope, the greater the fluctuation (Fig.5. a-1, b-1, c-1). In the process of slope
 244 erosion, the rill interconnection erosion intensified, and the side walls on both sides of the rill began to
 245 collapse (Fig.6). With the blocking and scouring of the side walls, the erosion and collapse occurred
 246 repeatedly, and erosion fluctuates, so that multiple peaks and lows occur during the erosion process (Peng
 247 et al., 2014; Niu et al., 2020). It is worth noting that for a given slope, the average soil loss rate increases
 248 with increasing number of scouring under the lowest inflow rate (1.6 mm min^{-1}). However, with the
 249 increase of inflow rate (2 and 2.4 mm min^{-1}), the average soil loss rate decreases with the increasing
 250 number of scouring. The reason may be due to the fact that at lower inflow rate (1.6 mm min^{-1}), runoff
 251 erosivity is relatively weak, and the rill networks gradually develop and mature with the number of
 252 scouring, resulting in an increase in average soil loss rates. However, at higher inflow rates (2 and 2.4
 253 mm min^{-1}), the erosivity of runoff increases, and rill networks are basically mature after the first scouring,
 254 and as the number of scouring increases, the amount of material available for erosion decreases, leading
 255 to a decrease in average soil loss rates.

256 Regression analyses of slope, inflow rate and scouring times were performed to quantify their effects
 257 on soil loss rate. The best-fit equation to describe the mean soil loss rate as a function of the adjusted
 258 slope, inflow rate and scouring times is as follows:

$$259 \quad SR = 0.0024S^{1.6128}I^{2.8883}N^{-0.1777} \quad (R^2=0.7955, P<0.001, n=27) \quad (9)$$

260 where SR is the mean soil loss rate ($\text{g m}^{-2} \text{ min}^{-1}$), S is the slope (%), I is the inflow rate (mm min^{-1})
 261 and N is the scouring times.

262 Eq. (9) shows that inflow rate and slope have a positive effect on soil loss rate, while the scouring
 263 times has a negative effect. The exponents for slope, inflow rate and scouring times were 1.6128, 2.8883
 264 and -0.1777, respectively. This indicates that the inflow rate was the most important factor that affects
 265 soil loss rates.

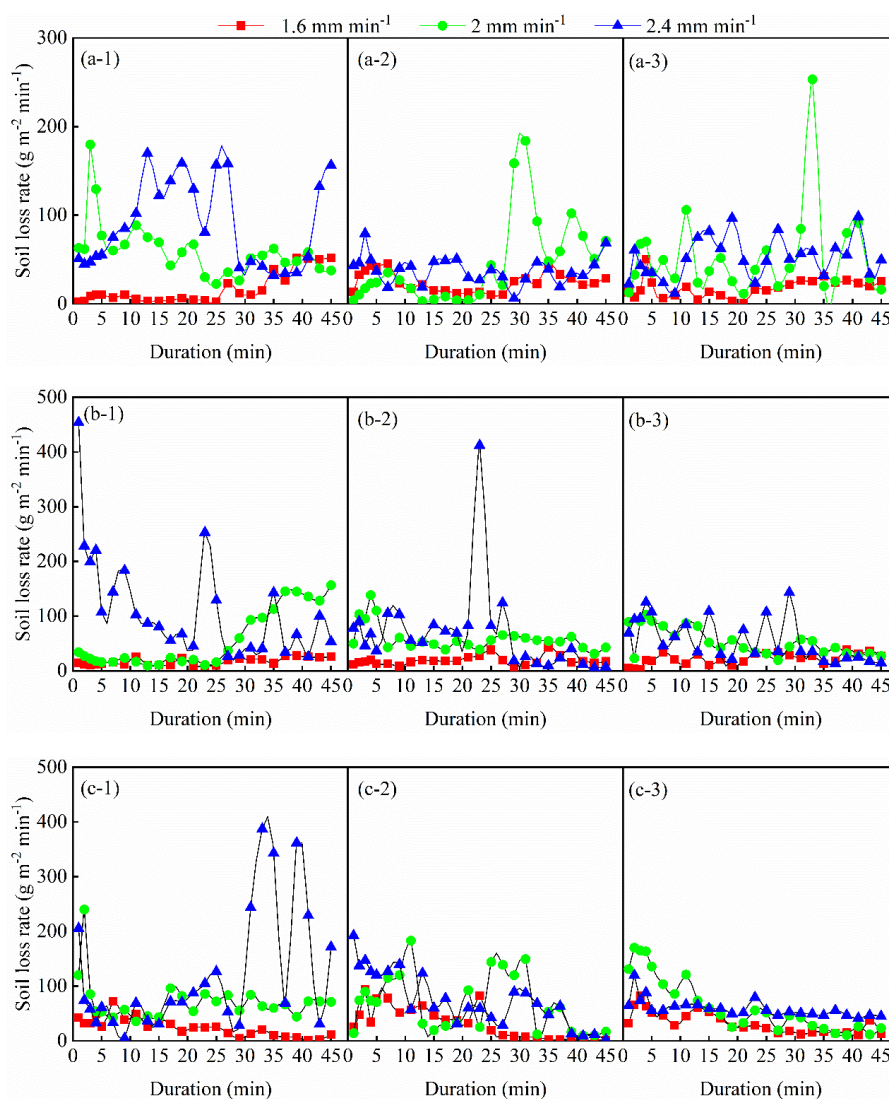


Figure 5 Variations in the soil loss rate with time for three scourings at slope of 28°(a-(1-3)), 32°(b-(1-3)) and 36°(c-(1-3)).



Figure 6 Slope erosion after each scouring at the 2.4 mm min⁻¹ inflow rate and a slope of 28 °.

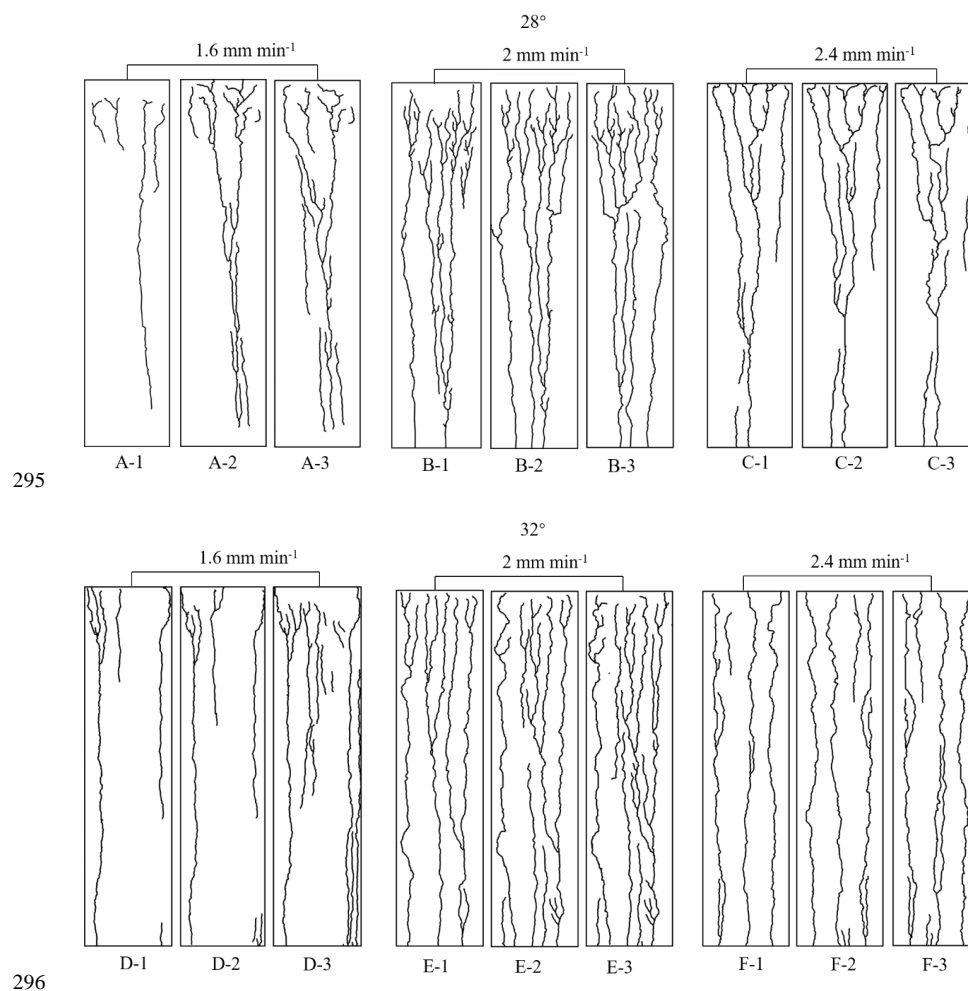
3.3 Rill networks and morphology

3.3.1 Rill networks

In order to explore the development of rill networks at different slopes, inflow rates and scouring times, the rill network at the end of each experiment was shown in Fig.7. As can be seen from Fig.7, there was significant variability in the development of rill networks at different slopes, inflow rates and scouring times. When the inflow rate was low (1.6 mm min⁻¹), many intermittent rills and drop-offs appeared on the slope as the scouring continues. As the number of scours and the slope increased, the intermittent rills gradually became connected along the slope to form continuous rills, and rill networks became relatively dense. In the process of the experiment, we observed that at the end of the third experiment, the rills were still in the developmental stage, i.e., the rill network was not mature, which may be related to the weak soil denudation capacity of the runoff (Fig.7 A-(1-3), D-(1-3), G-(1-3)). The erosive force of the runoff increased with the inflow rate gradually (2 and 2.4 mm min⁻¹). Along with the continuous scouring, the rill network on the slope has basically developed after the first experiment (Fig.7 B-1, C-1, E-1, F-1, H-1, I-1). In addition, the greater the inflow rate and slope, the faster the rill network developed (Fig.7 I-1). We noted that at an inflow rate of 2 mm min⁻¹, the rill density was greatest (Fig.7 E-(1-3)), while at an inflow rate of 2.4 mm min⁻¹, the rill network was relatively sparse, suggesting that there may be a critical inflow rate (2 mm min⁻¹) for the development of rills under the experiment



290 conditions. In general, the distribution of rills was denser at the top of the slope than at the bottom,
 291 probably due to the main driver of soil erosion and rill development was upslope runoff with high erosive
 292 capacity of the low sediment concentration(Tian et al., 2020). The overall predominance of parallel-
 293 shaped rills at all experiments suggested that the formation of rills on slope were dominated by
 294 concentrated runoff(Tian et al., 2017).



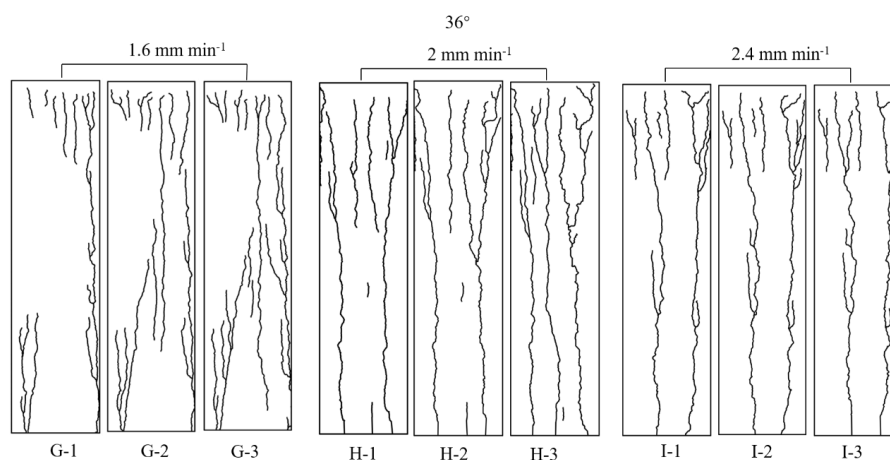
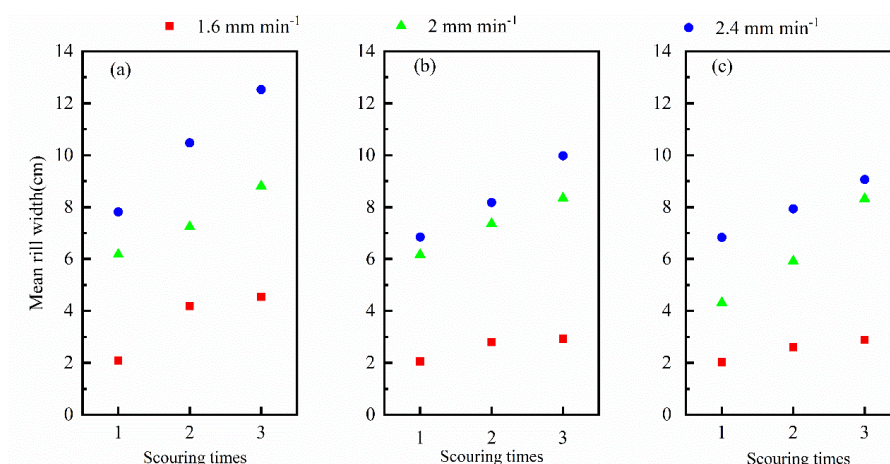


Figure 7 Rill networks change at the end of each the experiment. A(1-3), B(1-3) and C(1-3) represent development of rill networks in three scouring, respectively under slope of 28°, inflow rates of 1.6, 2 and 2.4 mm min⁻¹. D(1-3), E(1-3) and F(1-3) represent development of rill networks in three scouring, respectively under slope of 32°, inflow rates of 1.6, 2 and 2.4 mm min⁻¹. G(1-3), H(1-3) and I(1-3) represent development of rill networks in three scouring, respectively under slope of 36°, inflow rates of 1.6, 2 and 2.4 mm min⁻¹.

3.3.2 Rill characteristics

The mean rill width increased with the inflow rate and scouring times, however, decreased with increasing slope (Fig. 8(a-c)). The mean rill depth increased with the slope, inflow rate and scouring times (Fig. 8(d-f)). Furthermore, the increase in average rill depth was greater than the increase in average rill width. With the same inflow rate, the rill width-to-depth ratio decreased with increasing slope and scouring times (Fig. 8(g-i)), indicating that the increase in undercutting erosion of the rill significantly exceeds the collapse erosion of the rill wall, resulting in a decrease in the rill width-to-depth ratio.



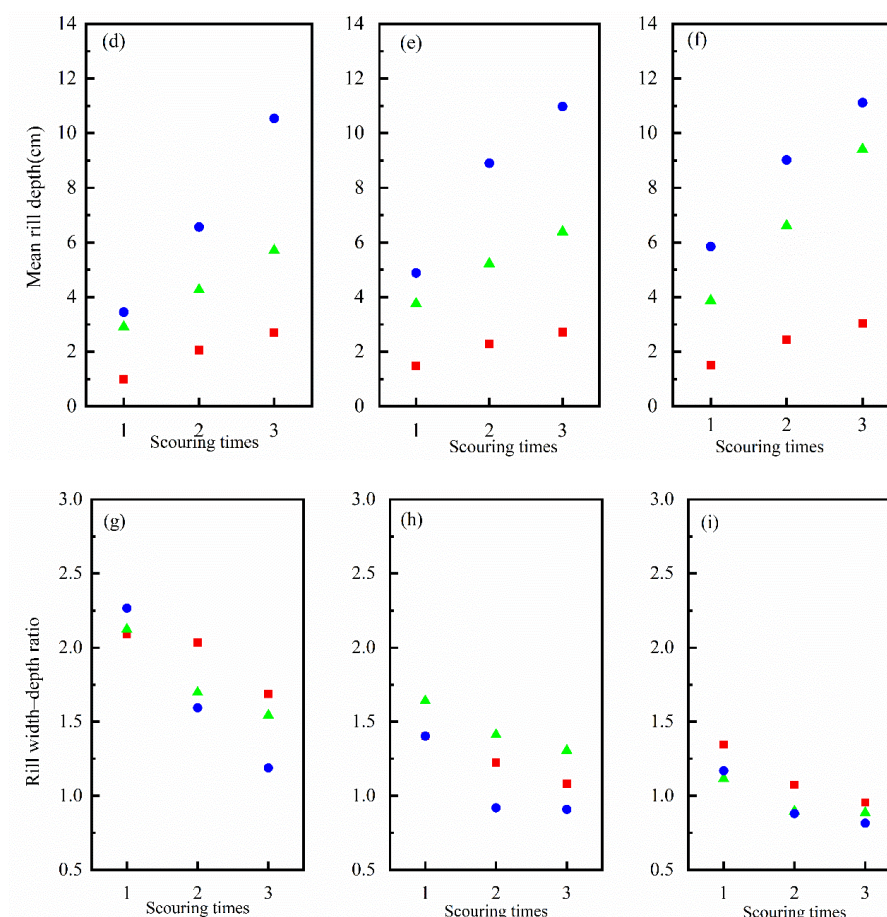


Figure 8 Variation of rill characteristics with scouring times. Variation of the mean rill width with scouring times on slopes of 28°(a), 32° (b)and 36°(c). Variation of the mean rill depth with scouring times on slopes of 28°(d), 32° (e)and 36°(f). Variation of the rill width-depth ratio with scouring times on slopes of 28°(g), 32° (h)and 36°(i).

Based on the above analysis, variation in rill morphological parameters were influenced by slope, inflow rate and scouring times, and regression analysis was used to quantify the effect of these influences on rill morphology. Eq. (10-12) shows that the average rill width, mean rill depth and rill width-to-depth ratio can be expressed as a power function of the slope, inflow rate and scouring times. Moreover, the fitted equations were all extremely significant ($p < 0.001$). The coefficients indicate that the inflow rate has a greater effect on mean rill width and mean rill depth than slope and number of scouring, indicating that high inflow rate was to the main driver of the rill development(Niu et al., 2020). While scouring times has the greatest effect on the rill width-to-depth ratio.



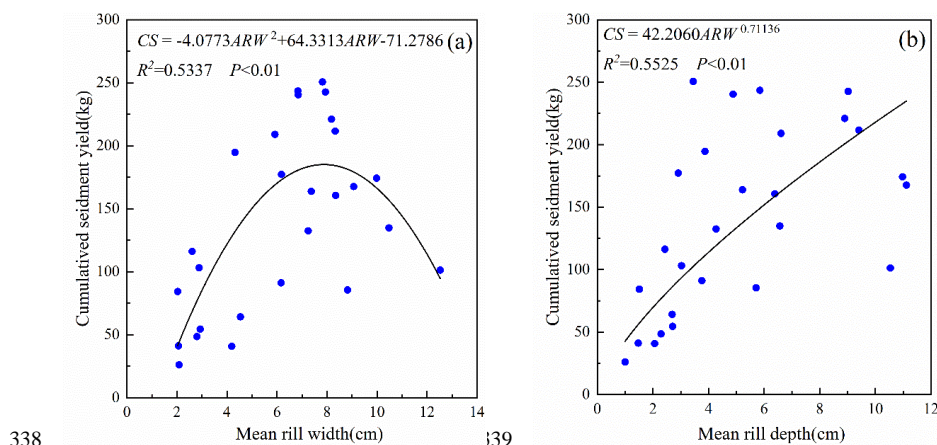
$$ARW = 59.1054S^{-1.471}I^{2.8454}N^{0.3979} \quad (R^2=0.9147, P<0.001, n=27) \quad (10)$$

$$ARD = 0.0012S^{1.3988}I^{3.2357}N^{0.7070} \quad (R^2=0.9607, P<0.001, n=27) \quad (11)$$

$$R_{WD} = 4.8324 \times 10^4 S^{-2.5427}I^{-0.3828}N^{-0.3079} \quad (R^2=0.8911, P<0.001, n=27) \quad (12)$$

where S is the slope (%), I is the inflow rate (mm min^{-1}), N is the scouring times, ARW is the mean rill width (cm), ARD is the mean rill depth (cm) and RWD is the rill width–depth ratio.

The development of rill morphology is ultimately presented in terms of sediment. To reveal the relationship between changes in rill morphology and sediment, data sets of rill morphological parameters (mean rill width, mean rill depth and rill width–depth ratio) and cumulative sediment yield were analyzed (Fig. 9). There is a quadratic function relationship between cumulative sediment yield and mean width ($R^2=0.5337, P<0.01$) (Fig. 9a) and width–depth ration ($R^2=0.2327, P<0.05$) (Fig. 9c). In addition, there is a highly significant power function relationship between cumulative sediment yield and mean rill depth width ($R^2=0.5525, P<0.01$) (Fig. 9b). In other words, the mean rill depth is the best indicator of rill morphology to predict the production of sediment on slope.



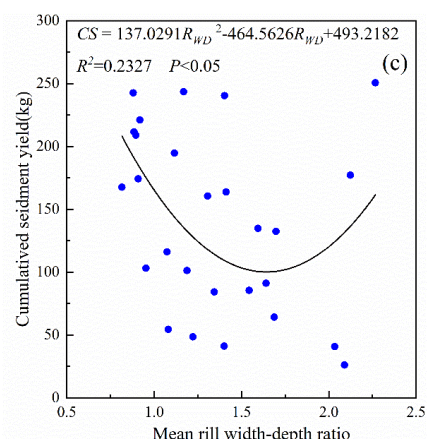
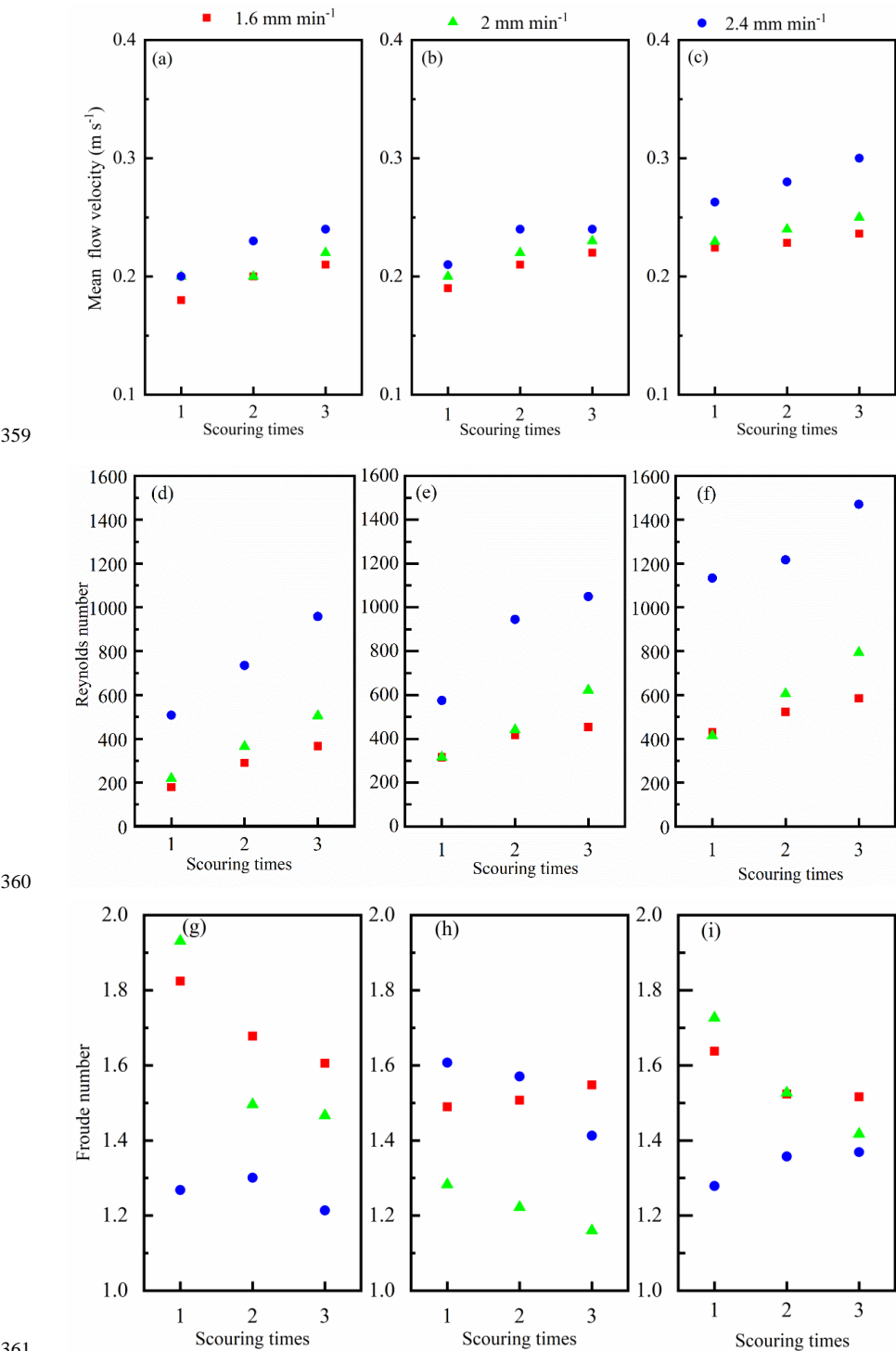


Figure 9 Relationship between cumulative sediment yield and rill morphological parameters including mean rill width (a), mean rill depth (b) and rill width-depth ratio (c).

3.4 Hydraulic characteristics and dynamic mechanisms of rill erosion

3.4.1 Rill flow hydraulic characteristics

Rills formed are the result of concentrated runoff and that the analysis of the rill flow hydraulic parameters can contribute to revealing the mechanism of rill erosion in spoil tips (Jiang et al., 2018). The average rill flow velocity (V) and Reynolds number (Re) ranged from 0.18 to 0.30 m s⁻¹ and 178.85 to 1470.51 respectively, increasing with slope, inflow rate and scouring times (Fig. 10(a-c), (d-f)). The Froude number (Fr) ranged from 1.16 to 1.93, all greater than 1 (Fig. 10(g-i)). The reason for the lack of a significant variable rule of Fr with increasing slope, inflow rate and scouring times may be related to the complexity of the rill morphological development on the slope. Based on the open-channel hydraulics theory, flow regime could be classified into three types, namely laminar flow ($Re < 500$), turbulent flow ($Re > 2000$) and transitional flow ($500 < Re < 2000$). Moreover, $Fr = 1$ distinguishes between subcritical and supercritical flow. According to the results of Guo et al. (2020), the runoff under the experimental conditions were of supercritical-laminar flow and supercritical-transition flow. The Darcy-Weisbach coefficient (f) ranged from 1.14 to 3.15, no obvious relationship observed between f and the slope, the inflow rate and scouring times (Fig. 10(j-l)), the reason for which may be related to the rill beds becoming more irregular, resulting in rill development (Jiang et al., 2018).



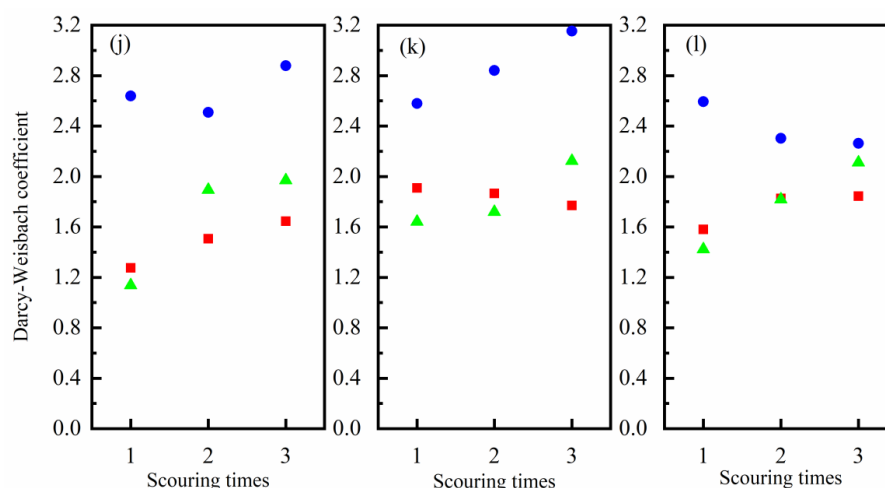


Figure 10 Variation in rill flow hydraulic parameters. Variations in the mean flow velocity with inflow rate and scouring times at slope of 28°(a), 32°(b) and 36°(c). Variations in the Reynolds number with inflow rate and scouring times at slope of 28°(d), 32°(e) and 36°(f). Variations in the Froude number with inflow rate and scouring times at slope of 28°(g), 32°(h) and 36°(i). Variations in the Darcy-Weisbach coefficient with inflow rate and scouring times at slope of 28°(j), 32°(k) and 36°(l).

To examine the relationship between changes in rill flow hydraulic characteristics and rill erosion, data sets of rill flow hydraulic parameters (mean flow velocity, Reynolds number, Froude number and Darcy-Weisbach coefficient) and soil detachment rate were analyzed (Fig. 11). The soil detachment rate (D_r) can be expressed as a power function of the velocity (V) ($R^2 = 0.4992$, $P < 0.01$) (Fig. 11a), Reynolds number (Re) ($R^2 = 0.6033$, $P < 0.01$) (Fig. 11b), Froude number (Fr) ($R^2 = 0.3969$, $P < 0.01$) (Fig. 11c) and Darcy-Weisbach coefficient (f) ($R^2 = 0.3981$, $P < 0.01$) (Fig. 13d), respectively. In other words, Reynolds number (Re) was the best hydraulic parameter to describe rill erosion on spoil tips.

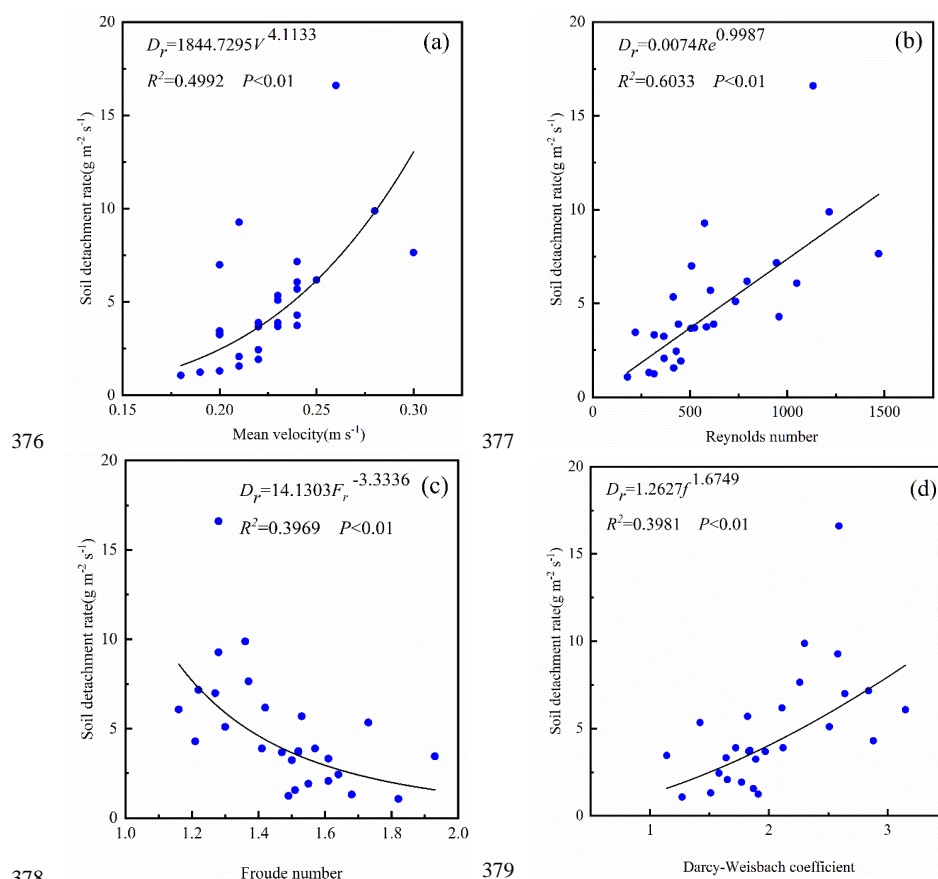
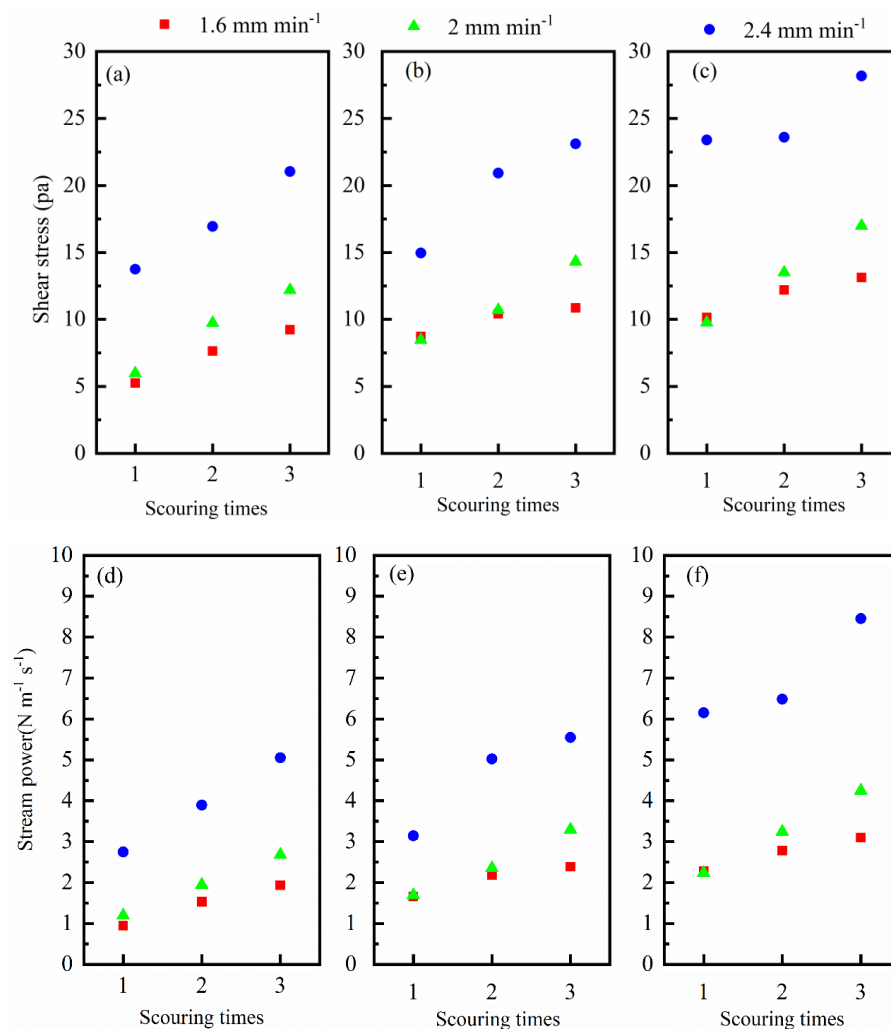


Figure 11 The relationship between soil detachment rate and rill flow hydraulic parameters including flow velocity(a), Reynolds number(b), Froude number(c) and Darcy-Weisbach coefficient(d).

3.4.2 Hydrodynamic mechanisms of rill erosion

The process of detachment and sediment transport by runoff is an energy-consuming. Therefore, in order to further reveal the mechanism of rill erosion, three hydrodynamic indicators were selected and calculated, as shown in Fig. 12. The mean shear stress (τ), stream power (ω) and unit stream power (p) ranged from 5.25 to 28.18 Pa (Fig. 12(a-c)), 0.95 to 8.45 $N m^{-1} s^{-1}$ (Fig. 12(d-f)), and 0.08 to 0.18 $m s^{-1}$ (Fig. 12(g-i)), respectively, and both of them increased with increasing slope, inflow rate and scouring times.



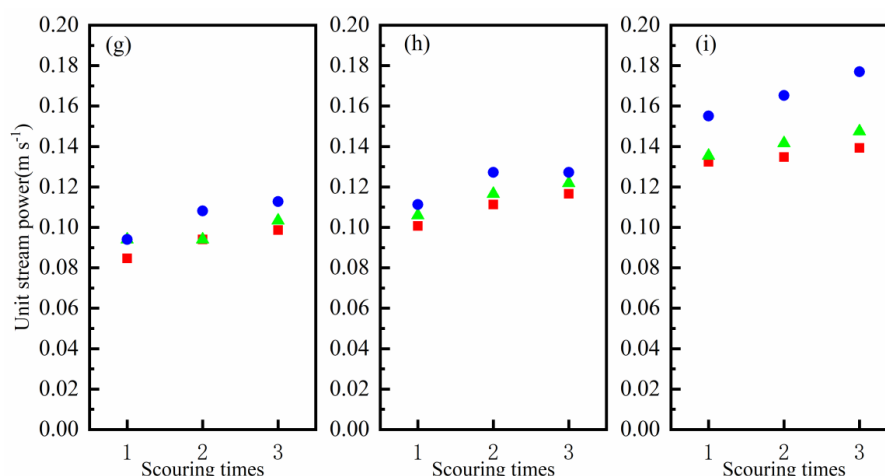
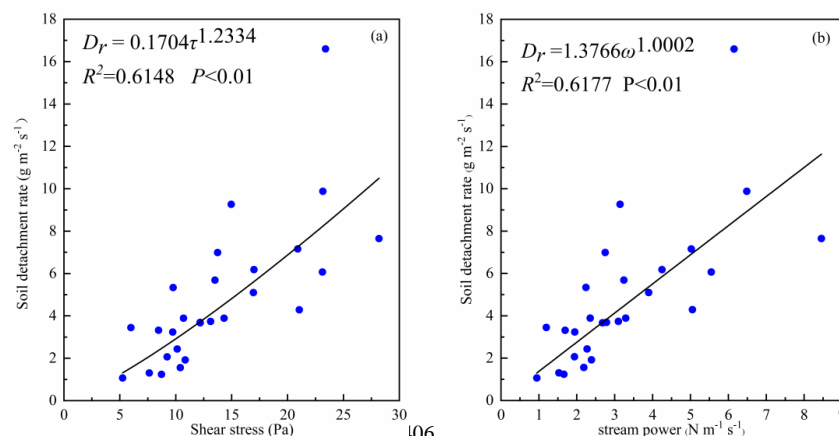
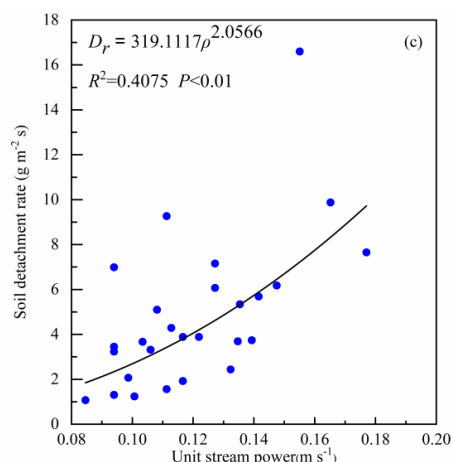


Figure 12 Variation in rill flow hydrodynamic parameters. Variations in the shear stress with inflow rate and scouring times at slope of 28°(a), 32°(b) and 36°(c). Variations in the stream power with inflow rate and scouring times at slope of 28°(d), 32°(e) and 36°(f). Variations in the unit stream power with inflow rate and scouring times at slope of 28°(g), 32°(h) and 36°(i).

To reveal the relationship between changes in rill flow hydrodynamic characteristics and rill erosion, data sets of rill flow hydrodynamic parameters (shear stress, stream power and unit stream power) and soil detachment rate were analyzed (Fig. 13). The soil detachment rate (D_r) can be expressed as a power function of the shear stress (τ) ($R^2 = 0.6148$, $P < 0.01$) (Fig. 13a), stream power (ω) ($R^2 = 0.6177$, $P < 0.01$) (Fig. 13b) and unit stream power (p) ($R^2 = 0.4075$, $P < 0.01$) (Fig. 13c), respectively. Furthermore, stream power (ω) was the best hydrodynamic parameter to describe rill erosion on spoil tips.





407
 408 **Figure 13 Relationship between soil detachment rate (D_r) hydrodynamic parameter including Reynolds number (a), flow**
 409 **shear stress (b), stream power(c) and unit stream power(d).**

410 4. Discussion

411 4.1 Effects of slope, inflow rate and scouring times on runoff and soil loss

412 According to Eq. (8) and (9), the importance of slope (S), inflow rate (I) and scouring times (N) on runoff rate and
 413 soil loss rate are in the following order: $I > S > N$. Inflow rate is the most important factor affecting soil erosion on the
 414 slope of spoil tips. The runoff coming from above the platform is involved in all aspects of soil erosion as a
 415 transmission link between the erosive power of the runoff and the energy of the flow on the slope, and can cause soil
 416 erosion on the steep slope (Zheng et al., 2000). The results of the study by Zheng et al. (2004) showed runoff and
 417 sediment from the upslope and rill flow hydraulic parameters have an important influence on rill sediment detachment
 418 and transport under the process of rill erosion. Therefore, in the management of soil erosion in spoil pits, the focus
 419 should be on how to effectively regulate runoff. For example, the use of vegetation measures to divide the spoil tips
 420 platform into a number of runoff dispersal units, so that heavy rainfall caused runoff is evenly dispersed among the
 421 units, this way it can effectively increase rainfall retention and infiltration, disperse runoff, dissipate runoff energy and
 422 reduce the soil erosion of the slope (Zhang et al., 2015; Zhang et al., 2016). For a given slope, vegetation or engineering
 423 measures (Pan and Ma 2020) can be used to regulate slope runoff and reduce its erosive energy to achieve soil and
 424 water conservation.

425 In addition, the effect of slope on runoff rate and soil loss rate is second only to the inflow rate. On the one hand,
 426 it is generally accepted that the greater the slope, the greater the partitioning of soil particles in the downhill direction,
 427 the less stable the soil particles and the more susceptible they are to erosion. On the other hand, an increase in the
 428 slope increases the runoff velocity (Tian et al., 2020) and reduces the residence time and infiltration time of the runoff
 429 on the slope, which increases the runoff and sediment yield on the slope. Wu et al. (2018) reported that sediment yield
 430 tends to increase with increasing slope. Therefore, it is necessary to take the slope factor into account when managing
 431 water and soil loss in spoil pits. For instance, slope grading and slope cutting to reduce slope lengths and slope,



432 together with vegetation and engineering measures, can reduce the probability of landslides and debris flows in heavy
 433 rainfall conditions.

434 **4.2 Rill networks and morphology characteristics**

435 The development of rill on the slope mainly goes through a rill formation stage, a rill development stage and a
 436 rill adjustment stage (Fig.14). The results of this study are similar to Jiang et al. (2018). After the first experiment, rill
 437 network was basically formed, and the higher the inflow rate and the steeper the slope the more developed the rills
 438 (Fig. 14 A-1, B-1). During the second experiment, with the initial formation of rills, the slope runoff mainly
 439 converges to the outlet in the form of rill flow, during which the erosive force of the rill flow increases and the
 440 headwater erosion of the downhill can proceed rapidly, forming a continuous rill (Fig. 14 C-2). Undercutting erosion
 441 of the rill bottom and spreading erosion of the rill wall increase, and the rill depth and rill width increase (Fig. 14 A-
 442 2, B-2). In the third experiment, the rill flow adjusted some parts of the already developed rill. The bottom and inner
 443 walls of rills were mainly scoured, and the rills collapsed due to the hollowing of the walls by the rill flow, which
 444 caused rills to become less stable under gravity (Fig. 14 A-3, B-3, C-3).

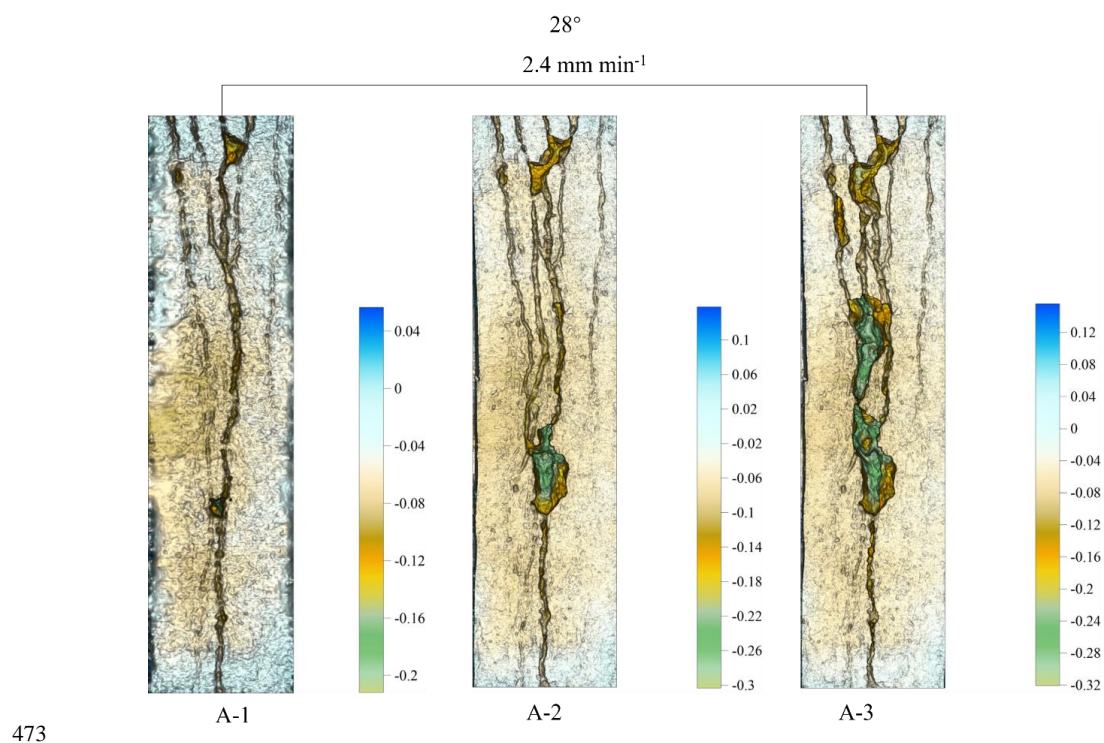
445 The overall predominance of parallel-shaped rills at all three experiments (Fig. 7) is consistent with the findings
 446 of Fang et al. (2015) and Tian et al. (2020). However, Shen et al. (2020) showed that the rill network mainly exhibits
 447 a dendritic pattern. The difference may be due to the fact that slope surface flow under scour conditions is surface-
 448 produced flow and is point-produced flow under rainfall conditions (Zhang et al., 2013), and the difference in the way
 449 they produce flow may lead to a different development of the rill network. The high clay content (31.15%) of the soils
 450 in this experiment results in relatively strong inter-soil adhesion and resistance to erosion by runoff, but the poor
 451 infiltration rate results in relatively high runoff volumes, and the slopes often form multiple rills of approximately
 452 parallel width and depth.

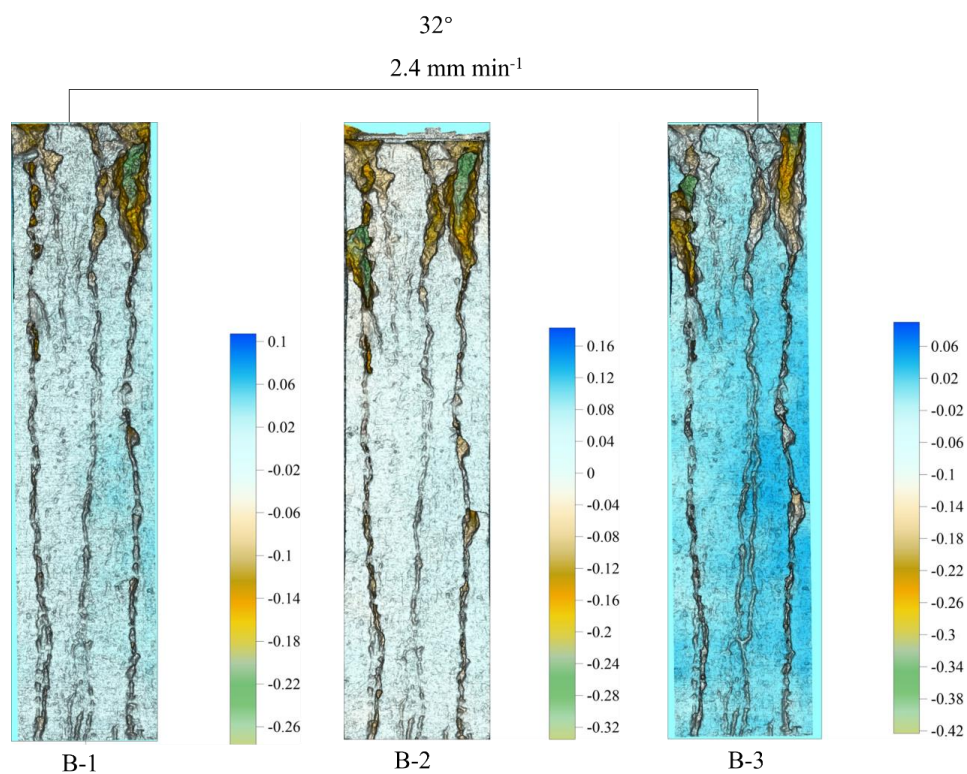
453 The most eroded parts of the slope under scour conditions are mostly located in the middle and upper parts of the
 454 slope (Fig. 7, 14). This result is similar to that obtained by Yang et al. (2019), who noted that the highest proportion of
 455 rill erosion was generated on the upper part of the slope, reaching over 60 %. The reason is that the flow and erosion
 456 forces are greatest when the water enters the slope from the top of the slope, thus the rill head appears at the top of the
 457 slope, and once the drop can begin to appear and develop into a rill at the top of the slope, rill erosion will rapidly
 458 undergo headwater erosion, undercutting erosion and lateral erosion. Sediment yield, rill width and depth increase
 459 rapidly. As the runoff infiltrates and is subjected to resistance along its course, the energy of the runoff is gradually
 460 depleted and the increased sediment content of the runoff reduces its separation capacity, which in turn reduces the
 461 proportion of rill erosion in the lower part of the slope. However, under rainfall conditions the most severe erosion is
 462 observed in the middle and lower parts of the slope (Jiang et al., 2018). The reason for this is that under rainfall
 463 conditions, the runoff gradually tends to increase along the slope length, the runoff velocity increases, and the ability
 464 of the runoff to strip the soil increases as well. The lower and middle parts of the slope are prone to the development
 465 of rills.

466 The rill depth and cumulative sediment yield exhibited significant power relationship (Fig. 9b). The mean rill
 467 depth is the best rill morphological parameter for predicting sediment. However, the results of Niu et al. (2020)

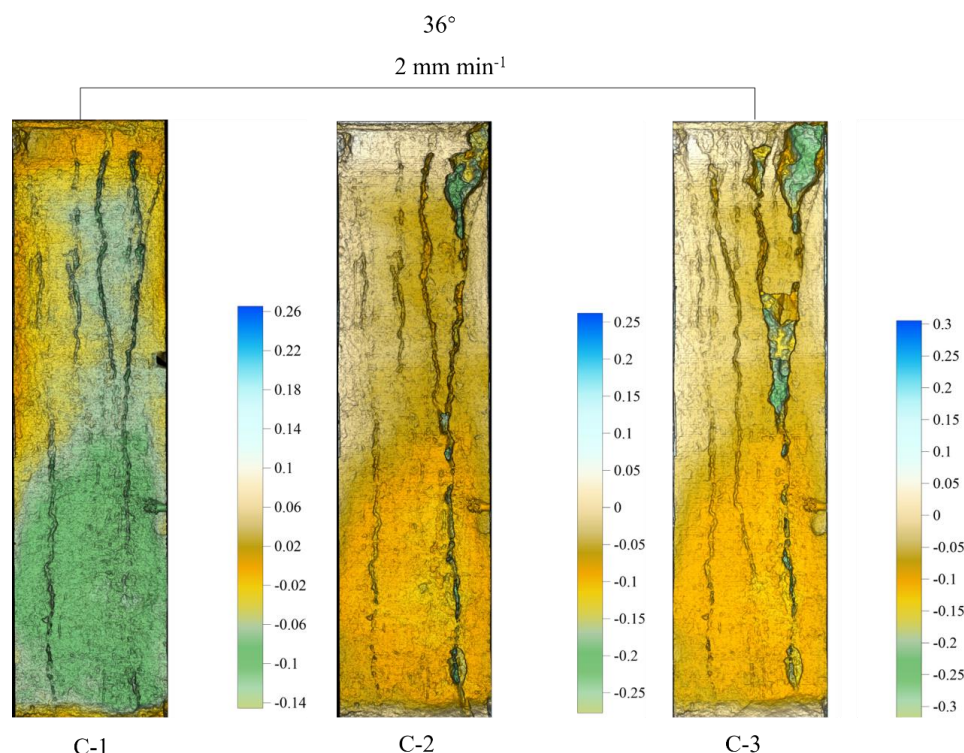


468 showed that cumulative sediment yield can be expressed as a power function of cross-sectional area. Shen et al. (2015)
 469 investigated the development of rill networks and the quantitative description of rill morphology through continuous
 470 rainfall experiments. The results showed that the mean rill width was the best basic morphological indicator for
 471 evaluating rill erosion. Differences in experimental methods, soil types, rainfall conditions and topography may have
 472 contributed to the above differences in the results.





474



475
 476 **Figure 14** DEMs of different slope, inflow rate and scouring times. A(1-3) represent change of DEMs in three scouring,
 477 under slope of 28°, inflow rates of 2.4 mm min⁻¹. B(1-3) represent change of DEMs in three scouring, under slope of 32°,
 478 inflow rates of 2.4 mm min⁻¹. C(1-3) represent change of DEMs in three scouring, under slope of 36°, inflow rates of 2 mm
 479 min⁻¹.

480 4.3 Hydraulic characteristics and dynamic mechanisms of rill erosion

481 The runoff hydrodynamic characteristics largely determine the rill erosional and morphological characteristics
 482 on slopes. The runoff hydrodynamic characteristics can describe the energy changes in runoff (Xiao et al., 2009),
 483 which in turn have an impact on the stripping, transport and deposition of soil on slopes. The Reynolds number is the
 484 best hydraulic parameter for predicting rill erosion (Fig. 11b). This result is similar to that obtained by Guo et al.
 485 (2018), who found the Reynolds number (Re) was the best predictor for sediment load. However, (An et al.,
 486 2014) considered the Froude number (F_r) as a key hydraulic parameter affecting soil loss, because the Froude number
 487 (F_r) is the ratio of inertial forces to gravitational forces, and these forces were closely related to sediment concentration.
 488 Li et al. (2016), Shen et al. (2016) and Jiang et al. (2018) considered that among the various hydraulic parameters, the
 489 flow velocity (V) best represents the hydraulic characteristics of the rill flow. The process of runoff stripping and
 490 transporting of soil is actually a process of doing work and consuming energy. Therefore, in the process of rill
 491 development, changes in hydrodynamic characteristics play an important role in the erosion characteristics of rill
 492 runoff. Our results show that stream power (ω) was the best hydrodynamic parameter to describe rill erosion
 493 mechanism (Fig. 13b), which is consistent with the results of Al-Hamdan et al. (2012) and Niu et al. (2020). But, Li



et al. (2016) considered that shear stress provides the best characterization of hydrodynamic parameters in rill erosion.

5 Conclusions

The rill erosion process, the rill morphological characteristics and the rill erosion hydrodynamic mechanism of spoil tips, were studied by multiple scouring experiments in the field. The results showed that the importance of slope(S), inflow rate(I) and scouring times(N) on runoff rate and soil loss rate are in the following order: $I > S > N$, indicating that inflow rate was the most important factor affecting rill erosion on the slope of the spoil heaps. Therefore, in the management of soil erosion in spoil tips, the focus should be on how to effectively regulate runoff from the platform and slope.

The development of rill mainly goes through three stages: the rill formation stage, the rill development stage and the rill adjustment stage. The overall predominance of parallel-shaped rills at all experiments suggested that the formation of rills was dominated by concentrated runoff. The most eroded parts of the slope were mostly located in the middle and upper parts of the slope of spoil tips. Rill depth was the best rill morphological parameter for evaluating spoil tips rill erosion.

The Reynolds number (Re) and stream power (ω) were the best hydraulic parameter and hydrodynamic parameter for predicting rill erosion, respectively. The study has some importance practical implications for the management of soil erosion and the establishment of erosion prediction models for spoil tips.

Acknowledgments. This work was supported by the National Natural Science Foundation of China (Grant No. 41671283 and 2016YFC0501706-02).

Author contribution. Zhaoliang Gao and Yongcai Lou designed the experiment. Fuyu Zhou, Jianwei Ai, Yunfeng Cen, Tong Wu and Jianbin Xie carried out the experiment. Yongcai Lou prepared the manuscript with contributions from all co-authors.

Data availability. Not applicable.

Compliance with ethical standards

Competing interests. The authors declare that they have no conflict of interest.

Ethical approve. Not applicable.

Consent to publish. The authors confirm that final version of the manuscript has been reviewed, approve and consented for publication by all authors.

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