Streamflow indices to identify catchment drivers of hydrograph

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Abstract. Streamflow indices are flow descriptors that quantify the streamflow dynamics, which are usually determined for a specific basin and are distinct from other basin features. The flow descriptors are appropriate for large-scale and comparative hydrology studies, independent of statistical assumptions and can distinguish signals that indicate basin behavior over time. In this paper, the characteristic features of the hydrograph's temporal asymmetry due to its different underlying hydrologic processes are primarily highlighted. Streamflow indices linked to each limb of the hydrograph within the time irreversibility paradigm are distinguished with respect to its processes driving the rising and falling limbs. Various streamflow indices relating the rising and falling limbs, and the catchment attributes such as climate, topography, vegetation, geology and soil are then correlated. Finally, the key attributes governing rising and falling limbs are identified. The novelty of the work is on differentiating hydrographs by their time irreversibility property and offering an alternative way to recognize primary drivers of streamflow hydrographs. A set of streamflow indices at the catchment scale for 671 basins in the Contiguous United States (CONUS) is presented here. These streamflow indices complement the catchment attributes provided earlier (Addor et al., 2017) for the CAMELS data set. A series of spatial maps describing the streamflow indices and their regional variability over the CONUS is illustrated in this study.

1 Introduction

Hydrologists use data to underpin the hydrologic system by identifying several unique catchment signatures and employ various flow descriptors independent of statistical assumptions yet capable of capturing signals that reflect the basin's long-term unique behavior. Hydrological indices, commonly referred to as hydrologic metrics, hydrologic signatures, or diagnostic signatures, are quantitative flow metrics that characterize statistical or dynamical hydrological data series (McMillan, 2021). Specifically, streamflow indices are flow descriptors derived from discharge time-series data, and a considerable collection of indices are available to aid in the better characterization of hydrological features, ranging from basic statistics like the mean to more sophisticated metrics (Addor et al., 2018; McMillan, 2021). In many cases, daily streamflow records are not permitted for redistribution; however, researchers have computed streamflow indices and made them publicly accessible.

Hydrological indices are increasingly used in emerging areas such as global-scale hydrologic modeling and large-sample hydrology to extract relevant information and compare the different watershed processes (Addor et al., 2017, 2018; McMillan, 2021). These indices offer an indirect way to explore hydrological processes as well as provide insights into hydrologic behavior in catchments where data other than streamflow is restricted and are...
widely used in process exploration, model calibration, model selection, and catchment classification (Addor et al., 2018; Clark et al., 2011; Kuentz et al., 2017; McMillan et al., 2011; Sawicz et al., 2011). McMillan (2021) presented a classification that differentiates between statistics- and dynamics-based signatures and between signatures at different timescales.

The relevance of time irreversibility (or temporal asymmetry) of streamflow variability on a daily scale has been emphasized in recent studies (Koutsoyiannis, 2020; Mathai and Mujumdar, 2019; Serinaldi and Kilsby, 2016) the disparity in physical mechanisms driving the hydrograph's ascension and recession limbs (Fig.1) contributes to time irreversibility. Unlike other variables such as temperature, wind, precipitation, time irreversibility has been marked for streamflow at a daily scale (Koutsoyiannis, 2020). Moreover, the various segments of the recession phase represent different phases in the flow process. As a result, time irreversibility must be acknowledged in streamflow analysis, accounting for the distinction of the recession into different segments, with a faster recession induced by high discharges caused by surface runoff and a slower recession caused by baseflow (Fig.1), and the characterization of the recession rates separately (Mathai and Mujumdar, 2019). In this study, streamflow indices are chosen to better understand different hydrological processes by recognizing the streamflow hydrograph's temporal asymmetry.

![Figure 1. Schematic representation of rising limb and falling limb](source: Environment Southland; https://www.es.govt.nz/environment/water/groundwater/groundwater-monitoring)

2 Methods
To facilitate a comprehension of various hydrological processes and streamflow hydrograph drivers, the study employs streamflow indices considering the streamflow hydrograph's temporal asymmetry. The description of indices used in this study are tabulated in Table 1. Streamflow indices linked to each limb of the streamflow hydrograph within the time-irreversibility paradigm are distinguished since hydrographs have rising and falling
limbs. The following indices are considered in the rising limb category: 1) rising limb density, 2) rising limb shape parameter, and 3) rising limb scale parameter. In contrast, 1) falling limb density 2) slope of upper recession (upper recession coefficient) 3) slope of lower recession (lower recession coefficient) are selected in falling limb category. The next step is to compute these indices for a large number of catchments and correlate them with attributes such as climate, topography, vegetation, geology, and soil. The streamflow indices can be correlated explicitly since sub-categories are involved in each of the catchment attributes discussed above. Finally, the key attributes governing ascension and recession limbs can be summarized and identified. This work's main novelty is to differentiate hydrographs by their time irreversibility property and using their associated indices by offering an alternative way to recognize primary drivers of streamflow hydrographs. The specifics of indices are explained further below.

Rising limb density (RLD) is defined as the ratio of the number of rising limbs and the cumulative time of rising limbs (Shamir et al., 2005). RLD is a hydrograph shape descriptor without considering the flow magnitude (Fig. 2) and the expression for RLD is given as,

\[ \text{RLD} = \frac{N_{RL}}{T_{RL}} \]  

The ratio of the number of falling limbs to the cumulative time of falling limbs is termed as falling limb density (FLD) (Fig. 2) (Shamir et al., 2005). The expression for FLD is given as,

\[ \text{FLD} = \frac{N_{FL}}{T_{FL}} \]  

Table 1. Hydrological descriptors with temporal asymmetry.

<table>
<thead>
<tr>
<th>Sl.no</th>
<th>Attribute</th>
<th>Description</th>
<th>Unit</th>
<th>Data source</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>RLD</td>
<td>Rising limb density</td>
<td>day(^{-1})</td>
<td>N15 – USGS data</td>
<td>Shamir et al. (2005)</td>
</tr>
<tr>
<td>2</td>
<td>FLD</td>
<td>Falling limb density</td>
<td>day(^{-1})</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>a</td>
<td>ascension limb scale parameter</td>
<td>-</td>
<td>Mathai and Mujumdar, (2019)</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>b</td>
<td>ascension limb shape parameter</td>
<td>-</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>b(_1)</td>
<td>Upper recession coefficient</td>
<td>-</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>b(_2)</td>
<td>Lower recession coefficient</td>
<td>-</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Figure 2. Schematic example of rising limb density (RLD) and falling limb density (FLD) calculation (Shamir et al., 2005).

The diurnal increments of streamflow are fitted with an appropriate probability density function to depict the shape of the ascension limbs which occur on wet days. The Weibull distribution reflects the diurnal increments of streamflow that occur on wet days reasonably well (Mathai and Mujumdar, 2019; Stagge and Moglen, 2013; Szilagyi et al., 2006). The scale ‘a’ and shape ‘b’ parameters of the Weibull distribution are computed for each catchment by using observed diurnal increments of streamflow. In contrast, an exponential recession is used to capture the shape of the recession limbs on dry days of the daily hydrograph, representing the falling limbs’ underlying dynamics (Mathai and Mujumdar, 2019). As the upper recession refers to the fast flow following a storm event and the lower recession refers to the baseflow recession, falling limb modeling is done in two stages.

The study uses indices related to ascension limb (viz., RLD, ascension limb scale parameter, ascension limb shape parameter) and recession limb (viz., FLD, upper recession coefficient, lower recession coefficient) to summarize the characteristic shape of steeper rising and gradually declining falling limb and its application in understanding the role of various drivers of catchment attributes in streamflow generation.

3 Contributions of the Study

The analysis employs a collection of indices drawn from hydrograph shape diagnoses, which extracts information about a basin’s ascension and recession limbs’ inherent properties. The principle of time irreversibility is encapsulated by six streamflow indices that describe and characterize a streamflow hydrograph’s shape, and indices for a particular basin are consistent and distinct from indices from other basins.
The goals of this study are as follows: i) to identify the key drivers of streamflow hydrographs (in terms of catchment attributes) using time-irreversibility-based indices ii) to present a spatial map-based attribute class of time-irreversibility-based indices for a large sample hydrology dataset.

As shown in numerous ways/studies in the literature, our notion of time-irreversibility and its indices could also do a reasonable job of articulating the catchment drivers of streamflow hydrographs. This study presents an attribute class of hydrograph shape descriptors with temporal asymmetry. The significance of large sample hydrology datasets in open hydrologic science and their potential to improve hydrological studies' transparency is also underlined in this study.

4 Motivation to extend to large sample hydrology

Large-sample hydrology (LSH) gathers information from a larger number of catchments to gain a more comprehensive understanding of hydrological processes and to go beyond individual case studies. LSH helps identify catchment behavior and leads one to derive precise conclusions regarding different hydrological processes and models (Addor et al., 2020). Studies involving large sample catchments help in understanding the drivers of hydrological change (Blöschl et al., 2019), in assessing hydrological similarity and classification (Berghuijs et al., 2014; K. A. Sawicz et al., 2014), in predictions in ungauged basins (Ehret et al., 2014), and in analysing model and data uncertainty (G. Coxon et al., 2014) and foster hydrology research by standardizing and automating the creation of large sample hydrology datasets worldwide (Addor et al., 2020). LSH assists in exploring interrelationships between numerous catchment attributes related to landscape, climate, and hydrology (Addor et al., 2017; Alvarez-Garreton et al., 2018; Gupta et al., 2014; Newman et al., 2015; K. Sawicz et al., 2011) and generalizing rules that can significantly improve the predictability of the water cycle (Alvarez-Garreton et al., 2018).

The primary challenges in fostering LSH are data availability and accessibility, which seriously hinder its use in data-scarce regions. Despite the fact that a few large-scale hydrology studies have been undertaken, the number of publicly available large-scale datasets is still restricted (Addor et al., 2017, 2020; Coxon et al., 2020). Moreover, licensing restrictions and strict access policies make the datasets rarely available to the public (Coxon et al., 2020).

Model Parameter Estimation Experiment project (MOPEX) dataset (Duan et al., 2006), Canadian model parameter experiment (CANOPEX) database (Arsenault et al., 2016), Global Streamflow Indices and Metadata Archive (Do et al., 2018; Guðmundsson et al., 2018), Global Runoff Reconstruction (Ghiggi et al., 2019), HydroATLAS (Linke et al., 2019) and the Catchment Attributes and MEteorology for Large-Sample studies (CAMELS) (Addor et al., 2017) are notable contributions of open and accessible large sample catchment datasets (Coxon et al., 2020).

Addor et al. (2017) introduced a new dataset (CAMELS) made publicly available for large-sample hydrological studies. This dataset covers meteorological and streamflow datasets provided by Newman et al. (2015) and provides quantitative metrics for a large variety of attributes for 671 catchments in the contiguous United States (CONUS). Streamflow records are available in the dataset from 1990 to 2009 for the 671 catchments, which are minimally influenced by human activities (Addor et al., 2017).
The CAMELS dataset prompted hydrological research by enabling open access to hydrologic data and establishing a common standard across the database. CAMELS promoted open access to datasets for the United States, and it is eventually expanded to the United Kingdom (CAMELS-GB), Chile (CAMELS-CL), and Brazil (CAMELS-BR). The CAMELS proposes five classes of catchment attributes, namely location, topography, geology, land cover characteristics, climatic indices, and hydrological signatures, in order to promote common standards and formats in large sample studies (Addor et al., 2017). The concept of time irreversibility-based streamflow indices is then applied to CAMELS catchments with the goal of encouraging large sample hydrology studies.

5 Dataset used

Section 5 provides the description of the dataset used and the study area chosen. This study employs the CAMELS dataset, which encompasses daily discharge data and catchment attributes for 671 catchments (Fig. 3) across the continental United States, representing a diverse set of catchments with long streamflow time series covering a wide range of hydro-climatic conditions (Addor et al., 2017). The time frame chosen for the analysis is from 1 October 1989 to 30 September 2009 (Addor et al., 2017). The topographic characteristics of CAMELS dataset are represented in Fig. 4. Except for the Appalachian Mountains, the eastern part of the Continental United States is much flatter than the western portion, according to mean elevation and mean slope maps (Fig. 4.a and 4.b). Figure 4.c depicts the spatial pattern of catchment size, highlighting presence of some catchments with an area greater than 10,000 km².
Figure 3. (a) Map of 671 CAMELS catchments in the continental United States considered in this study. (b) Geographical regions of US according to NOAA National Centers for Environmental Information referred for the analysis (source: NOAA National Centers for Environmental Information; https://www.ncdc.noaa.gov/temp-and-precip/drought/nadm/geography).
Figure 4. Maps of topographic characteristics of CAMELS catchments over the CONUS (Addor et al., 2017). (a) Mean elevation [m above sea level] (b) Mean slope [m km$^{-1}$] (c) Area [km$^2$]. The eastern US seems to have a much flatter mean elevation and mean slope than the western US, which significantly influences catchment behavior. The majority of the catchments are noticed to be smaller, with an area of fewer than 3000 km$^2$. 
5.1 Catchment attributes

The landscape of each catchment is described using multiple attributes, which can be divided into various classes as shown in Table 2 (Addor et al., 2017). The details of the attributes used in this study is summarized in Table 2.

Table 2. CAMELS attributes (Addor et al., 2017)

<table>
<thead>
<tr>
<th>Sl.no</th>
<th>Attribute</th>
<th>Description</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>aridity</td>
<td>aridity (ratio of mean PET to mean precipitation)</td>
<td>-</td>
</tr>
<tr>
<td>2</td>
<td>p_seasonality</td>
<td>seasonality and timing of precipitation (positive (negative) values indicate that precipitation peaks in summer (winter); values close to 0 indicate uniform precipitation throughout the year)</td>
<td>-</td>
</tr>
<tr>
<td>3</td>
<td>frac_snow</td>
<td>fraction of precipitation falling as snow</td>
<td>-</td>
</tr>
<tr>
<td>4</td>
<td>high_prec_freq</td>
<td>frequency of high precipitation days</td>
<td>days yr⁻¹</td>
</tr>
<tr>
<td>5</td>
<td>high_prec_dur</td>
<td>average duration of high precipitation events</td>
<td>days</td>
</tr>
<tr>
<td>6</td>
<td>low_prec_freq</td>
<td>frequency of dry days</td>
<td>days yr⁻¹</td>
</tr>
<tr>
<td>7</td>
<td>low_prec_dur</td>
<td>average duration of dry periods</td>
<td>days</td>
</tr>
<tr>
<td>8</td>
<td>Forest_frac</td>
<td>forest fraction</td>
<td>-</td>
</tr>
<tr>
<td>9</td>
<td>Lai_max</td>
<td>maximum monthly mean of the leaf area index</td>
<td>-</td>
</tr>
<tr>
<td>10</td>
<td>Gvf_max</td>
<td>maximum monthly mean of the green vegetation fraction</td>
<td>-</td>
</tr>
<tr>
<td>11</td>
<td>soil_depth_pelletier</td>
<td>depth to bedrock</td>
<td>m</td>
</tr>
<tr>
<td>12</td>
<td>sand_frac</td>
<td>sand fraction</td>
<td>%</td>
</tr>
<tr>
<td>13</td>
<td>clay_frac</td>
<td>clay fraction</td>
<td>%</td>
</tr>
<tr>
<td>14</td>
<td>geol_porosity</td>
<td>subsurface porosity</td>
<td>-</td>
</tr>
<tr>
<td>15</td>
<td>geol_permeability</td>
<td>subsurface permeability (log10)</td>
<td>m²</td>
</tr>
</tbody>
</table>
6 Results and Discussion

The first sub-section below looks at the regional variability of the streamflow indices used in this study. For the 671 CAMELS catchments, rising limb density, falling limb density, ascension limb scale parameter, ascension limb shape parameter, upper recession coefficient, and lower recession coefficient are computed and given as spatial maps. Streamflow indices are then presented in hydrological clusters to incorporate a more explicit spatial representation of catchment behavior across the CONUS. Catchment attributes cover a broad range of aspects of catchment hydrology such as, land cover, soil, climate, geology, topography and the association between these attributes and streamflow indices is discussed further in the subsequent section. As the climate is the most important factor in the US for the hydrological behavior for the CAMELS dataset (Jehn et al., 2020), the influence of climatic factors on streamflow indices is finally studied.

6.1 Spatial Variability in Streamflow Indices

Streamflow indices related to rising limbs and falling limbs are computed for the selected catchments and displayed in spatial maps as shown in Fig. 5 and Fig. 6, respectively. The spatial analysis is based on the United States’ geographical areas (for details, refer to Fig. 3b) as defined by NOAA’s National Centers for Environmental Information and is referred to in the following spatial maps. Furthermore, ten clusters provided by Jehn et al. (2020) to represent the discrete hydrological behaviors of the continental United States are adopted in this study to understand the regional variability of catchment behavior. Figure S1 and Table S1 present the location map and details of the ten clusters.

In terms of geographical regions, the rising limb density is highest over the Atlantic coast states, Ohio valley, Lower Mississippi Valley, Southern Great Plains, Southwest and Pacific, and lowest along the Upper Great Lakes region, Upper Mississippi Valley, Great Basin, and Northern Rocky Mountains, Northern Interior Plains, and East of Gulf Coast (Fig. 5.a). Further, in terms of hydrological clusters, Appalachian Mountains (Cluster 10), Southeastern and Central Plains (Cluster 1) and all Southern most states of the US (Cluster 9) witness high rising limb densities and these clusters are characterized by a high forest fraction, low aridity, and high frequency of high precipitation events, respectively (Fig. 6.a). Northwestern Forested Mountains (Clusters 3, 4), located in the mountains of the western US, experience low values of rising limb density as these clusters are characterized by a dominant summer peak of discharge caused by rapid snowmelt (Fig. 6.a).

Considerably low values of rising limb scale parameters are experienced over the Rocky Mountains, High Plains, Great Plains, Upper Mississippi Valley, Great Basin, Southwest, and the Great Lakes regions, whereas the Pacific Northwest shows high values of rising limb scale parameters (Fig. 5.b). Clusters (5, 7) over the Northwestern Forested Mountains of CONUS experience very high values of rising limb scale parameters (Fig. 6.b). These catchments have the highest discharge, especially in the early summer, due to a combination of high precipitation and snowmelt. Further, the region in the Continental US which receives the highest precipitation is included in Cluster 5. Moreover, Cluster 5 consists of a large proportion of forest. Again, Cluster 7 with high values of rising limb scale parameter is characterized by high fraction of precipitation falling as snow. Low values of rising limb scale parameters are shown by Clusters 2, 8, 9. This is because of low water availability, low snow fraction precipitation falling as snow, and high evaporation experienced in these regions.
Low rising limb shape parameter occurs along the Great Plains, Mississippi Valley, Pacific coast, and the west of Gulf Coast (Fig. 5.c). In contrast, the shape parameter over the Rocky Mountains, High Plains, Great Basin, Pacific Northwest, and the Great Lakes region witnesses the highest values of rising limb shape parameters (Fig. 5.c). All the catchments located in the Southern states of the US (Cluster 9), Great Plains and North American deserts (Cluster 8), and the Central Plains (Cluster 2) characterize low values of rising limb shape parameters (Fig. 6.c).

This is due to low water availability, low snow fraction precipitation falling as snow, low leaf area index, and high evaporation experienced in these regions. High values of rising limb shape parameters are seen in Clusters 3, 4 (Fig. 6.c) located in the Northwestern Forested Mountains of the western US, dominant with a summer peak of discharge caused by rapid snowmelt.

Catchments with a high falling limb density are predominantly located along the Great Basin and the Rocky Mountains and in the High Plains region (Fig. 7.a). Clusters 4, 2, 8 over Northwestern Forested Mountains, Central Plains, Great Plains, and North American deserts characterize higher magnitudes of falling limb density, and Clusters 6, 7 over Marine West Coast Forests and Western Cordillera smaller falling limb densities (Fig. 8.a).

This is due to less presence of forest cover in these arid regions.

Similarities exist between the patterns of the upper recession coefficient and the lower recession coefficient (Fig. 7.b and Fig. 7.c). Clusters 3, 4 located in the Northwestern Forested Mountains, which have overall low discharge, show low values of upper and lower recession coefficients (Fig. 8.b and Fig. 8.c). Clusters 2, 9, located in the eastern US, witness high values of recession coefficients; due to low slope inclinations, water takes a long time to reach the outlet (Fig. 8.b and Fig. 8.c).
Figure 5. Spatial maps of streamflow indices associated with a rising limb (a) rising limb density \(\text{day}^{-1}\), (b) rising limb scale parameter, and (c) rising limb shape parameter over the CONUS. The Atlantic coast states, Ohio Valley, Lower Mississippi Valley, Southern Great Plains, Southwest, and Pacific have the highest rising limb density, while the Upper Great Lakes region, Upper Mississippi Valley, Great Basin, Northern Rocky Mountains, Northern Interior Plains, and East of Gulf Coast have the lowest. The Rocky Mountains, High Plains, Great Plains, Upper Mississippi Valley, Great Basin, Southwest, and Great Lakes regions have low values of rising limb scale parameters, but the Pacific Northwest has high values of rising limb scale parameters. The Great Plains, Mississippi Valley, Pacific coast, and west of Gulf Coast have low rising limb shape parameters. The shape parameter has the greatest values of rising limb shape parameters over the Rocky Mountains, High Plains, Great Basin, Pacific Northwest, and Great Lakes regions.
Figure 6. Boxplots of the hydrological descriptors linked with the rising limb (a) rising limb density [day$^{-1}$], (b) rising limb scale parameter, (c) rising limb shape parameter of the clusters over the CONUS. High rising limb densities are observed in Clusters 10, 1, and 9, which are characterized by a high forest fraction, low aridity, and a high frequency of high precipitation events, respectively. Rising limb scale parameters are exceptionally high in Clusters 5, 7. Due to a combination of high precipitation and snowmelt, these catchments have the highest discharge. Because of the low water availability, low snow fraction precipitation falling as snow, low leaf area index, and high evaporation experienced in these areas, catchments in Cluster 9, Cluster 8, and Cluster 2 have low values of rising limb shape parameters.
Figure 7. Regional variability of streamflow indices associated with the falling limb (a) falling limb density [day⁻¹], (b) upper recession coefficient, (c) lower recession coefficient over the CONUS. The Great Basin and the Rocky Mountains, and the High Plains region have high falling limb density. The patterns of the upper recession coefficient and the lower recession coefficient are similar.
Figure 8. Boxplots of the streamflow indices related with the falling limb (a) falling limb density [day\(^{-1}\)]. (b) upper recession coefficient. (c) lower recession coefficient of the clusters. Clusters 4, 2, 8 have higher falling limb densities, while Clusters 6, 7 have lower falling limb densities due to the less forest cover in these arid areas. Clusters 3, 4, which have a low discharge, have low upper and lower recession coefficients. Clusters 2, 9 have high recession coefficients due to low slope inclinations.
6.2 Relation of the Flow Descriptors and the Catchment Attributes

The association between the flow descriptors related to rising and falling limbs and catchment attributes is examined in this section. Table 3 shows the relation of streamflow indices linked with rising limb, and Table 4 shows the association of indices of the falling limb with catchment attributes. Across all five attribute classes, the vegetation/land cover attributes positively correlate with all rising limb indices (Table 3). It can be seen that the rising limb density shows a positive correlation with all the three vegetation density indicators, namely fraction of forest, maximum leaf area index, maximum green vegetation fraction (Table 3).

However, it is observed that the rising limb scale parameter shows a negative correlation with climate and a positive association with the vegetation attributes (Table 3). Aridity and frequency of precipitation (Table 3) display a strong negative association with the rising limb scale parameter. It is noted that the rising limb shape parameter indicates a positive correlation with vegetation attributes and the fraction of precipitation falling as snow, mean slope, mean elevation, and sand fraction whereas, it negatively correlates with precipitation frequency.

Falling limb density is mainly governed by climate indices and is negatively correlated with the land cover characteristics (Table 4). Mean elevation also strongly characterizes the nature of the falling limb density. Besides, aridity and fraction of precipitation falling as snow are also positively correlated with falling limb density. Recession coefficients are negatively correlated with topographic indices (Table 4). Further, the recession coefficients show a positive correlation with clay and negative correlations with the fraction of precipitation falling as snow, forest fraction, and sand fraction. Moreover, the geology attributes such as subsurface porosity reveal a positive correlation to recession coefficients and a negative with subsurface permeability (Table 4).
Table 3. Correlation between streamflow indices linked with rising limb and the catchment attributes. Green colored coefficients represent positive correlation, and the red-colored correlation coefficients represent the negative correlation. The vegetation/land cover attributes positively correlate with all rising limb indices amongst all five attribute groups. It can be seen that the rising limb density has a positive relationship with all three vegetation density measures. The rising limb scale parameter has a negative association with climate and a positive relationship with vegetation attributes. The rising limb shape parameter positively correlates with vegetation attributes and the fraction of precipitation that falls as snow, mean slope, mean elevation, and sand fraction.

<table>
<thead>
<tr>
<th>Spearman rank correlation coefficients</th>
<th>Topography</th>
<th>Climate</th>
<th>Soil</th>
<th>Land cover</th>
<th>Geology</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Area</td>
<td>Mean elevation</td>
<td>Mean slope</td>
<td>Precipitation seasonality</td>
<td>Frac of precp as snow</td>
</tr>
<tr>
<td>Rising limb density</td>
<td>-0.30</td>
<td>-0.20</td>
<td>-0.33</td>
<td>-0.10</td>
<td>0.08</td>
</tr>
<tr>
<td>Scale parameter</td>
<td>-0.17</td>
<td>-0.13</td>
<td>0.35</td>
<td>-0.36</td>
<td>0.53</td>
</tr>
<tr>
<td>Shape parameter</td>
<td>0.41</td>
<td>0.36</td>
<td>-0.14</td>
<td>-0.16</td>
<td>0.53</td>
</tr>
</tbody>
</table>

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Table 4. Correlation between streamflow indices linked with falling limb and the catchment attributes. Green colored coefficients represent positive correlation, and the red-colored correlation coefficients represent the negative correlation. Climate factors are the principal drivers of falling limb density and are negatively associated with land cover characteristics. Topographic indicators are negatively correlated with recession coefficients. Furthermore, the recession coefficients reveal a positive association with clay and negative correlations with the fraction of precipitation falling as snow, forest fraction, and sand fraction.

<table>
<thead>
<tr>
<th>Spearman rank correlation coefficients</th>
<th>Topography</th>
<th>Climate</th>
<th>Soil</th>
<th>Land cover</th>
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<tr>
<td></td>
<td>Area</td>
<td>Mean elevation</td>
<td>Mean slope</td>
<td>Precipitation seasonality</td>
<td>Frac of precp as snow</td>
</tr>
<tr>
<td>Falling limb density</td>
<td>-0.13</td>
<td>0.55</td>
<td>0.18</td>
<td>0.42</td>
<td>0.39</td>
</tr>
<tr>
<td>Upper recession coefficient</td>
<td>-0.35</td>
<td>-0.40</td>
<td>-0.38</td>
<td>0.22</td>
<td>-0.39</td>
</tr>
<tr>
<td>Lower recession coefficient</td>
<td>-0.37</td>
<td>-0.37</td>
<td>0.27</td>
<td>-0.17</td>
<td>0.19</td>
</tr>
</tbody>
</table>
Figure 9. (a) Comparison of the hydrological clusters of Jehn et al. (2020) with the climate index space (fraction of precipitation falling as snow vs. aridity). Single dots show the catchments and are colored by their hydrological clusters. Comparison of the streamflow indices in climate index space (b) rising limb density, (c) rising limb scale parameter, (d) rising limb shape parameter, (e) falling limb density, (f) upper recession coefficient, (g) lower recession coefficient for all catchments. Single dots show the catchments and are colored according to the value of the streamflow indices. Low values of rising limb density, high values of the rising limb shape parameter, and low values of recession coefficients are seen in catchments with a humid environment and a high fraction of precipitation falling as snow. In arid climates with a low fraction of precipitation falling as snow, the lowest values of rising limb scale and shape parameters, as well as the highest values of falling limb density, can be seen.

6.3 Streamflow Indices with Attributes of Climate

Climate attributes seem to be the most important indicator for hydrological behavior in the United States among the various attribute categories (Jehn et al., 2020). Hence, the flow descriptors are then examined in the climate index space (aridity along x-axis and fraction of precipitation falling as snow along the y-axis) to evaluate the main drivers of the catchments. Single dots show the catchments and are colored by their hydrological clusters (Fig. 9.a).

Clusters 5, 6, 7, 1, 10 are characterized by a low fraction of precipitation falling as snow and humid climate, whereas Clusters 3, 4 have humid climate experiencing a high fraction of precipitation falling as snow (Fig. 9.a). Clusters 2, 8, 9 are featured by a low fraction of precipitation falling as snow and arid climate (Fig. 9.a). The three categories mentioned above are referred to as G1, G2, and G3, respectively.
Clusters G1 with a low fraction of precipitation falling as snow with humid climate show (Clusters 1, 9, 10) high rising limb densities (Fig. 9.b) and (Clusters 5, 7) high rising limb scale parameters (Fig. 9.c). This is because the rising limb density negatively correlates with fraction of precipitation falling as snow (Fig. 9.b), whereas the rising limb scale parameter negatively correlates with aridity (Fig. 9.c). Moreover, these Clusters G1 experience a low value of (Clusters 6, 7) falling limb density (Fig. 9.e). This is because the falling limb density positively correlates with the climate indices (Fig. 9.e).

As mentioned earlier, Clusters G2 with humid climate and with a high fraction of precipitation falling as snow (Clusters 3, 4) display low values of rising limb density as rising limb density correlates negatively with the fraction of precipitation falling as snow (Fig. 9.b). G2 witnesses higher values of rising limb shape parameter due to its negative correlation with aridity and positive correlation with the fraction of precipitation falling as snow (Fig. 9.d). Furthermore, the Clusters of G2 (Clusters 3, 4) show low values of recession coefficients as they depict a strong negative correlation with the fraction of precipitation falling as snow (Fig. 9.f, g).

Low values of rising limb scale and shape parameters are noticed for the Clusters 2, 9, 8 (Clusters G3) with arid climate and low fraction of precipitation falling as snow (Fig. 9.c, d) due to its negative correlation with aridity as stated earlier. Cluster 8 experiences the maximum values of falling limb density (Fig. 9.e) where the region witnesses low fraction of snow and arid catchments, due to its strong positive correlates with the aridity.

7 Concluding remarks

Streamflow hydrograph portrays the time distribution of runoff at the point of measurement by a single curve, and the hydrographs are characterized by their time irreversibility property. In this study, the indices related to this characteristic feature are used to study the catchment drivers of streamflow hydrograph. The streamflow indices associated with the time irreversibility of hydrograph open new opportunities to investigate the interaction between topography, soil, climate, vegetation, geology that drive the hydrological behavior of catchments. Moreover, most of the previously presented hydrologic indices are employed only for time-symmetric processes; the importance of the time irreversibility of streamflow is highlighted in this study. The indices associated with rising and falling limbs are primarily correlated to distinct catchment attributes, establishing a relationship between the indices and catchment attributes such as climate, topography, soil, geology, and vegetation to delineate the controlling drivers in corresponding hydrograph sections. A set of streamflow indices with temporal asymmetry for 671 catchments in the United States is presented in this study. The regional variations among catchments over the United States are compared and discussed using the spatial maps of streamflow indices. Such spatial maps of the streamflow indices supplement the hydrometeorological time series and catchment attributes provided by Addor et al. (2017).

The study revealed that the rising limb indices such as rising limb density, rising limb shape parameter and rising limb scale parameter correlate positively with vegetation indices. Falling limb density is primarily controlled by climate indices and is negatively correlated with land cover characteristics; the structure of the falling limb density is also closely influenced by mean elevation. Finally, flow descriptors are studied in the climate index space to isolate the runoff generation's leading drivers. High rising limb densities and rising limb scale parameters are observed in catchments with low precipitation falling as snow and a humid climate. It is observed that the catchments with a humid climate and a high fraction of precipitation falling as snow display low values of rising
limb density, high values of the rising limb shape parameter, and low values of recession coefficients. The lowest values of rising limb scale and shape parameters, and the highest values of falling limb density, are seen in catchments of arid climates and a low fraction of precipitation falling as snow.

In general, the contribution of this work lies in differentiating hydrographs depending on their time irreversibility property and using the corresponding indices to provide an alternative methodology for identifying the drivers of streamflow hydrographs. In the context of large sample hydrology research, the concept of time-irreversibility and the indices associated with it could also be used to describe the drivers at catchment scale.

Data availability. The CAMELS dataset can be found at https://doi.org/10.5194/hess-2017-5293 (Addor et al. 2017).

Competing interests. The authors declare that they have no conflict of interest.

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