

Plant Hydraulic Transport Controls Transpiration Sensitivity to Soil Water Stress

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Abstract. Plant transpiration downregulation in the presence of soil water stress is a critical mechanism for predicting global water, carbon, and energy cycles. Currently, many terrestrial biosphere models (TBMs) represent this mechanism with an empirical correction function (β) of soil moisture—a convenient approach that can produce large prediction uncertainties. To reduce this uncertainty, TBMs have increasingly incorporated physically-based Plant Hydraulic Models (PHMs). However, PHMs introduce additional parameter uncertainty and computational demands. Therefore, understanding why and when PHM and β predictions diverge would usefully inform model selection within TBMs. Here, we use a minimalist PHM to demonstrate that coupling the effects of soil water stress and atmospheric moisture demand leads to a spectrum of transpiration [response responses](#) controlled by soil-plant hydraulic transport (conductance). Within this transport-limitation spectrum, β emerges as an end-member scenario of PHMs with infinite conductance, completely decoupling the effects of soil water stress and atmospheric moisture demand on transpiration. As a result, PHM and β transpiration predictions diverge most for soil-plant systems with low hydraulic conductance (transport-limited) that experience high variation in atmospheric moisture demand and have moderate soil moisture supply [to-for](#) plants. We test these minimalist model results by [land-surface-modeling-using-a-land-surface-model-at](#) an Ameriflux site. At this transport-limited site, a PHM downregulation scheme outperforms the β scheme due to its sensitivity to variations in atmospheric moisture demand. Based on this observation, we develop a new ‘dynamic β ’ that varies with atmospheric moisture demand—an approach that overcomes existing biases within β schemes and has potential to simplify existing PHM parameterization and implementation.

1 Introduction

Plants control their transpiration (T) and CO₂ assimilation by adjusting leaf stomatal apertures in response to environmental variations (Katul et al., 2012; Fatichi et al., 2016). In doing so, they mediate the global water, carbon, and energy cycles. The performance of most terrestrial biosphere models (TBMs) relies on accurately representing leaf stomatal responses in terms of stomatal conductance (g_s). Extensive research has established the relationships between g_s and atmospheric conditions like photosynthetically active radiation, humidity, CO₂ concentration, and air/leaf temperature under well-watered conditions, though the specific forms of these relationships vary (Damour et al., 2010; Buckley et al., 2014; Buckley, 2017). However, representing the dynamics of g_s in response to soil water stress remains problematic.

25 Many TBMs represent declining g_s and, in turn, transpiration reduction (i.e., downregulation) in response to soil water stress with an empirical function of soil water availability. This method, known as β (Powell et al., 2013; Verhoef and Egea, 2014; Trugman et al., 2018; Paschalis et al., 2020), reduces g_s from its peak value under well-watered conditions ($g_{s,ww}$), i.e., $g_s = \beta \cdot g_{s,ww}$, $0 \leq \beta \leq 1$. (We use the term ‘ β ’ in this paper to refer to the downregulation model itself, and the terms ‘ β function’ or ‘ β factor’ to refer to the empirical function and its values, respectively.) The term ‘well-watered’ refers to moist soil conditions where stomatal aperture is unaffected by ~~soil-water-uptake-plant water uptake from the soil~~, i.e., no soil water stress. ~~Using a~~
30 ~~The first β function to reduce well-watered transpiration (or g_s) originated-like function appeared,~~ to the best of our knowledge, ~~as a heuristic assumption in an early global heat balance study (Budyko, 1956) to reduce ‘evaporability’ (i.e., well-watered g_s or T) for unsaturated land surfaces using a normalized soil moisture value. This method was eventually incorporated into the hydrology component one of the first global circulation models (Manabe, 1969). However, many current β functions appear~~
35 ~~to stem from the heuristic root water uptake assumptions originally implemented~~ in the crop transpiration model, SWATR ~~(Feddes et al., 1978)(Feddes et al., 1976, 1978), which evolved into the widely-used SWAP model (Kroes et al., 2017).~~ Since then, ~~it-~~ β has gained widespread use within TBMs and hydrological models due to its parsimonious form.

However, mounting evidence indicates that using β in TBMs is a major source of uncertainty and bias in plant-mediated carbon and water flux predictions. Multiple studies have implicated the lack of a universal β formulation as a primary source
40 of inter-model variability in carbon cycle predictions (Medlyn et al., 2016; Rogers et al., 2017; Trugman et al., 2018; Paschalis et al., 2020). For example, different β formulations among nine TBMs accounted for 40%-80% of inter-model variability in global gross primary productivity (GPP) predictions (on the order of 3-283% of current GPP) (Trugman et al., 2018). Aside from the uncertainty in functional form, β appears to fundamentally misrepresent the coupled effects of soil water stress and atmospheric moisture demand on stomatal closure. Recent work using model-data fusion at FLUXNET sites highlighted that β
45 produces stomatal responses that are overly sensitive to soil water stress and unrealistically insensitive to atmospheric moisture demand (Liu et al., 2020). Furthermore, TBM validation experiments have found β schemes produce unrealistic GPP prediction during drought at Amazon rainforest sites (Powell et al., 2013; Restrepo-Coupe et al., 2017) and systematic overprediction of evaporative drought duration, magnitude and intensity ~~(Ukkola et al., 2017)~~ at several Ameriflux sites ~~(Ukkola et al., 2017)~~. The apparent inadequacy of β has led to the adoption of physically-based Plant Hydraulic Models (PHMs) in TBMs (Williams
50 et al., 2001; Bonan et al., 2014; Xu et al., 2016; Kennedy et al., 2019; Eller et al., 2020; Sabot et al., 2020).

PHMs represent water transport, driven by a gradient of water potential energy, through the soil-plant-atmosphere continuum via flux-gradient relationships (based on Hagen-Poiseuille flow), which use measurable soil properties and plant traits as parameters (Mencuccini et al., 2019). The implementation of PHMs in several popular TBMs (e.g., CLM, JULES, etc.) has improved predictions in site-specific GPP and evapotranspiration (ET) predictions (Powell et al., 2013; Bonan et al., 2014;
55 Eller et al., 2020; Sabot et al., 2020; Kennedy et al., 2019) as well as soil water dynamics (Kennedy et al., 2019) compared to β . PHMs also exhibit more realistic sensitivity to atmospheric moisture demand than β (Liu et al., 2020). However, these improvements from PHMs come at the cost of an increased number of plant hydraulic trait parameters and computational burden, which can reduce the reliability of the predictions (Prentice et al., 2015). Additionally, obtaining representative plant hydraulic trait values for a soil-plant system is difficult for two main reasons: i) traits vary widely across and within species

60 (Anderegg, 2015) and exhibit plasticity through acclimation and adaptation (Franks et al., 2014), and ii) trait measurements are typically made at a single point (e.g., stem, branch, leaf), which may not ~~be able to reliably scaled~~ reliably scale to represent whole-plant or ecosystem-level responses due to the effects of nonlinear trait variations along the soil-plant system (Couvreur et al., 2018). These difficulties result in uncertainty in the model predictions that may be further compounded at the ecosystem level (Fisher et al., 2018; Feng, 2020). Consequently, modelers continue to rely on β as a parsimonious alternative to PHMs
65 (Paschalis et al., 2020).

The relative strengths and weaknesses of β and PHMs suggest that informed model selection requires a better understanding of when the complexity of a PHM is justified over the simplicity of β . This paper informs such understanding by: i) analyzing the fundamental differences between PHMs and β , ii) defining the parameters controlling the differences (Sect. 3.2) and iii) demonstrating how PHMs outperform β for a real soil-plant system (Sect. 3.3). Then, leveraging our theoretical insights,
70 we create a new ‘dynamic β ’ as a potential tool to correct the biases from the original β while reducing the parameter and computational demands of PHMs (Sect. 3.3). To accomplish these goals, we first analyze a minimalist PHM using a water supply-demand framework, then corroborate the results for a more widely-used, complex PHM, and, finally, perform a case study with a calibrated land surface model (LSM), which employs β , PHM, and ‘dynamic β ’ downregulation schemes.

2 Methods

75 2.1 Minimalist PHM

Our minimalist (Sect. 3.1-3.2) and complex PHM formulations (Sect. 3.3), illustrated in Fig. 1, rely on a supply-demand framework that conceptualizes transpiration as the joint outcome of soil water supply and atmospheric moisture demand (Gardner, 1960; Cowan, 1965; Sperry and Love, 2015; Kennedy et al., 2019). In this framework, ‘supply’ refers to the rate of water transport to the leaf mesophyll cells from the soil, into the roots, and through the xylem. ‘Demand’ refers to the rate of wa-
80 ter vapor outflux through the stomata, driven by the transport capacity of the air surrounding the plant and regulated by the stomatal response to atmospheric conditions (Buckley, 2017) and leaf water status (Klein, 2014; Buckley, 2019). We assume steady-state transpiration fluxes (i.e., supply equals demand), which means we neglect the effects of plant capacitance (Bohrer et al., 2005) and also assume that the mean plant and atmospheric states equilibrate quickly over short timescales.

The minimalist PHM supply (T_s [mm day⁻¹]; Eq. 1 and blue segment in Fig. 1a) is represented by a steady-state, integrated
85 1-D flux-gradient relationship, bounded by the root zone average soil water potential (ψ_s [MPa]) and leaf water potential (ψ_l [MPa]) and mediated by the bulk conductance along the flowpath ($g_{sp}(\psi)$ [mm day⁻¹ MPa⁻¹]). For simplicity, we assume constant soil-plant conductance (g_{sp}) and ignore its dependence on water potential (i.e., hydraulic limits (Sperry et al., 1998)).

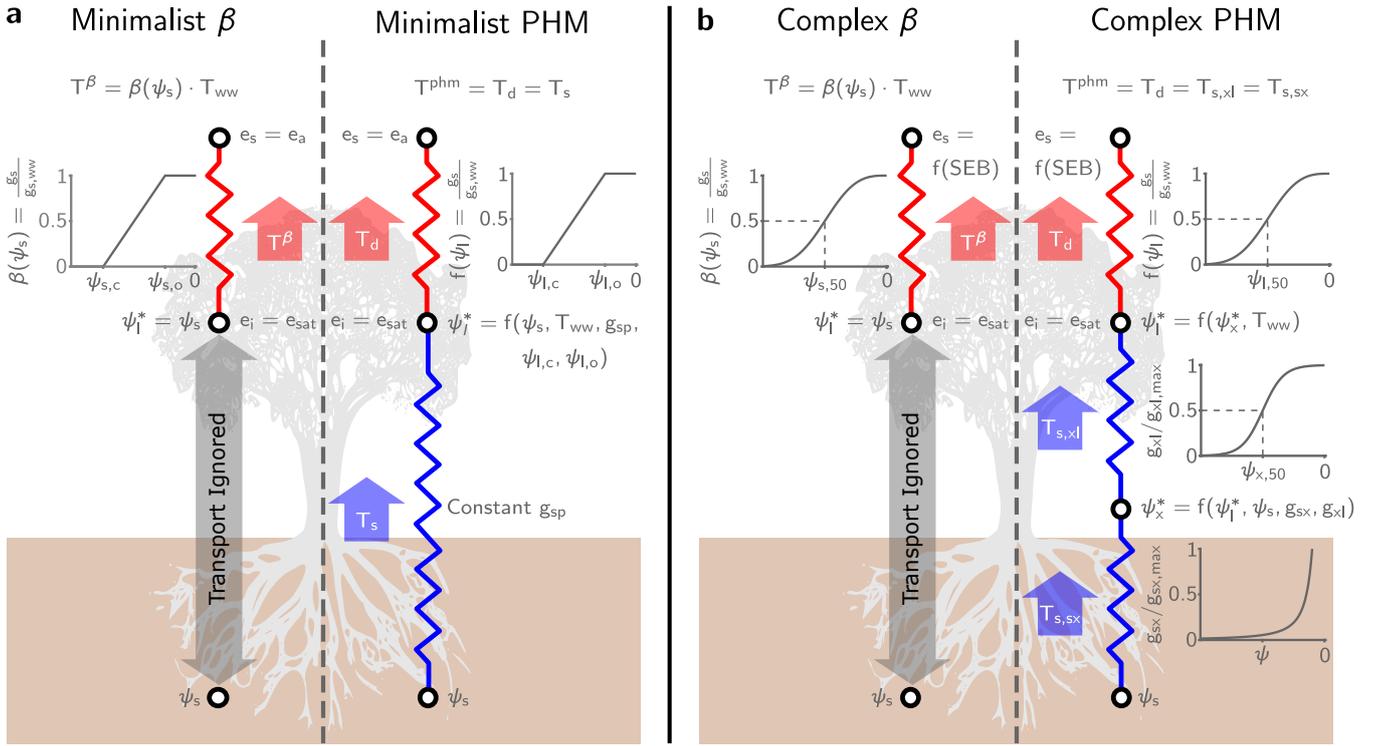


Figure 1. Schematic for the minimalist and complex β and PHM models used in this analysis. The resistors represent the conductance between soil-plant segments (i.e., an analogy to Ohm’s Law) that mediate liquid water supply (blue) and atmospheric water vapor demand (red). Next to each resistor is the segment-specific conductance downregulation curve dependent on water potential (ψ). The white circles indicate segment endpoints where we calculate the potentials (ψ) for liquid water transport and vapor pressures (e) for water vapor transport. The segment subscripts represent soil (s), xylem (x), leaf (l), inside the leaf (i) and ambient air (a). For water vapor transport, we assume saturation vapor pressure inside the leaf ($e_i = e_{sat}$) for both models. Furthermore in the minimalist models, we assume the leaf surface vapor pressure (e_s) is the atmospheric vapor pressure (e_a), which makes the driving force for water vapor transport the minimalist model vapor pressure deficit ($D = e_{sat} - e_a$). Alternately, while in the complex models, e_s is a function of the surface energy balance ($f(SEB)$) calculations at each time step for the complex formulation. is a function of the surface energy budget solution at each time step. The thick arrows represent the water transport through each segment calculated by the integrated, steady-state flux-gradient relationships discussed in Sect. 2.1-2.2 and Sect. 2.5. We use the minimalist models (left panel) for Sect. 3.1-3.2 and the complex models (right panel) for the LSM analysis in Sect. 3.3 (Note: We only illustrate a single-leaf single big-leaf formulation here, but see Sect. S2 for full details of the two-leaf two-big-leaf implementation.).

This assumption simplifies the integral in Eq. 1 to the product of g_{sp} and the water potential difference, $\psi_s - \psi_l$, which drives the flow.

$$90 \quad T_s = - \int_{\psi_s}^{\psi_l} g_{sp}(\psi) d\psi = g_{sp} \cdot (\psi_s - \psi_l) \quad (1)$$

The minimalist PHM demand (T_d [mm day⁻¹]; Eq. 2 and red segment in Fig. 1a) uses a similar conductance-difference formulation (i.e. integrated flux-gradient relationship). Transpiration is driven by the leaf-to-air water vapor pressure deficit (D [mol H₂O/mol air]) and mediated by the well-watered stomatal conductance ($g_{s,ww}$ [mol air m⁻² s⁻¹]), a stomatal closure term ($f(\psi_l)$), and the leaf area index (LAI [m² leaf m⁻² ground]). Additionally, we convert T_d from a molar flux to a volume flux using the conversion factor C_a (i.e., [the molar weight of water](#) (M_w [kg mol⁻¹]) divided by water density (ρ_w [kg m⁻³]) and multiplied by the conversion from m s⁻¹ to mm day⁻¹). The driving force D assumes saturation vapor pressure inside the leaf (i.e., $e_i = e_{sat}$) and that the leaf surface (e_s) and atmospheric vapor pressure (e_a) are the same [\(i.e., the leaf is well-coupled to the atmosphere \(Jarvis and Mcnaughton, 1986\)\); however, the leaf temperature can differ from the atmosphere, which differentiates \$D\$ from atmospheric vapor pressure deficit \(Grossiord et al., 2020\)](#). The parameter $g_{s,ww}$ encapsulates the stomatal response to atmospheric conditions only (i.e., light, temperature, humidity, and CO₂ concentration). We define the product of LAI , $g_{s,ww}$ and D as the well-watered transpiration rate (T_{ww})—which represents atmospheric moisture demand throughout this paper—and specify its value for the minimalist analysis. The term ‘well-watered’ refers to abundant soil water conditions under which water transport to the leaves maintains ψ_l high enough to avoid stomatal closure. During water-stressed conditions, the $f(\psi_l)$ term represents stomatal closure (i.e., downregulating $g_{s,ww}$) to lowering leaf water status (Buckley, 2019). We assume a normalized, piecewise linear $f(\psi_l)$ (Eq. 3 and illustrated in Fig. 1a), parametrized by the leaf water potential at incipient ($\psi_{l,o}$) and complete stomatal closure ($\psi_{l,c}$). This simple multiplicative reduction of $g_{s,ww}$ (similar to the approach of Jarvis (1976)) captures the observed non-unique relationship between g_s and ψ_l (Anderegg and Venturas, 2020) while facilitating comparison with the similar minimalist β formulation (see Sect. 2.5).

$$T_d = LAI \cdot f(\psi_l) \cdot g_{s,ww} \cdot D \cdot C_a = f(\psi_l) \cdot T_{ww} \cdot C_a \quad (2)$$

$$f(\psi_l) = \frac{g_s(\psi_l)}{g_{s,ww}} = \begin{cases} 1 & \psi_l \geq \psi_{l,o} \\ \frac{\psi_{l,c} - \psi_l}{\psi_{l,c} - \psi_{l,o}} & \psi_{l,c} < \psi_l < \psi_{l,o} \\ 0 & \psi_l \leq \psi_{l,c} \end{cases} \quad (3)$$

The PHM supply and demand are coupled through their mutual dependence on leaf water potential. The ψ_l value that balances supply (Eq. 1) and demand (Eq. 2)—which we will call ψ_l^* (Eq. 4)—yields the steady state transpiration rate for the minimalist PHM (T^{phm} ; Eq. 5). The full derivation of ψ_l^* and T^{phm} is shown in Sect. S1.

$$\psi_l^* = \frac{\psi_s \cdot (\psi_o - \psi_c) + \frac{T_{ww} \cdot \psi_c}{g_{sp}}}{(\psi_o - \psi_c) + \frac{T_{ww}}{g_{sp}}} \quad (4)$$

$$115 \quad T^{phm} = \begin{cases} T_{ww} & \psi_s > \psi_{l,o} + \frac{T_{ww}}{g_{sp}} \\ T_{ww} \cdot \frac{(\psi_{l,c} - \psi_s)}{(\psi_{l,c} - \psi_{l,o}) - \frac{T_{ww}}{g_{sp}}} & \psi_{l,c} < \psi_s \leq \psi_{l,o} + \frac{T_{ww}}{g_{sp}} \\ 0 & \psi_s \leq \psi_{l,c} \end{cases} \quad (5)$$

2.2 Complex PHM

The LSM analysis (Sect. 3.3) uses a **more**-complex PHM formulation following Feng et al. (2018). The PHM separates supply into soil-to-xylem and xylem-to-leaf segments and demand into a leaf-to-atmosphere segment (Fig. 1b). Here, we briefly discuss the complex PHM components for a single big-leaf formulation; however, we refer the reader to Sect. S2-S3 for full
 120 model details and parameter values for the **two big-leaf two-big-leaf** formulation used in our LSM.

For PHM supply (T_s ; blue segments in Fig. 1b), the water potential gradient drives flow through the soil-plant system mediated by the segment-specific conductance. Unlike the minimalist PHM (Sect. 2.1), we assume the conductance in each segment depends on water potential, which represents ‘hydraulic limits’ (Sperry et al., 1998) that arise via (i) the inability of roots to remove water from soil pores at low ψ_s and (ii) xylem embolism caused by large hydraulic gradients required under low
 125 ψ_s and/or high T_{ww} . The soil-to-xylem conductance (g_{sx} [mm day⁻¹ MPa⁻¹]; Eq. 6 and illustrated in Fig. 1b) is its maximum value ($g_{sx,max}$) downregulated by the unsaturated soil hydraulic conductivity curve (Clapp and Hornberger, 1978), which is parametrized by the saturated soil water potential (ψ_{sat}), soil water retention exponent (b), unsaturated hydraulic conductivity exponent ($c = 2b + 3$), and a correction factor (d) to account for roots’ ability to reach water (Daly et al., 2004). The xylem-to-leaf conductance (g_{xl} [mm day⁻¹ MPa⁻¹]; Eq. 7 and illustrated in Fig. 1b) is its maximum value ($g_{xl,max}$) downregulated by
 130 a sigmoidal function (Pammenter and Willigen, 1998), which is parametrized by the vulnerability exponent (a) and the xylem water potential (ψ_x) at 50% loss of conductance ($\psi_{x,50}$). We estimate the maximum conductance values for each segment ($g_{sx,max}$ and $g_{xl,max}$) with trait-based equations following Feng et al. (2018) (see Sect. S2.5.3). Given that conductance varies with water potential, we utilize a Kirchhoff transform (Eq. 8) to approximate the water supply from each segment ($T_{s,sx}$ and $T_{s,xl}$ [mm day⁻¹]; Eq. 9-10) as the difference in the matric flux potential (Φ [mm day⁻¹]) at the segment endpoints. Therefore,
 135 given a value of ψ_s (i.e., root zone average **water** potential) and ψ_l , the ψ_x that balances $T_{s,sx}$ and $T_{s,xl}$ —called ψ_x^* —yields the steady-state supply rate (T_s).

$$g_{sx}(\psi) = g_{sx,max} \cdot \left(\frac{\psi_{sat}}{\psi} \right)^{\frac{c-d}{b}} \quad (6)$$

$$g_{xl}(\psi) = g_{xl,max} \cdot \left[1 - \frac{1}{1 + e^{a(\psi - \psi_{x,50})}} \right] \quad (7)$$

$$\Phi(\psi) = \int_{-\infty}^{\psi} g(\psi') d\psi' \quad (8)$$

$$140 \quad T_{s,sx} = \Phi_{sx}(\psi_s) - \Phi_{sx}(\psi_x) \quad (9)$$

$$T_{s,xl} = \Phi_{xl}(\psi_x) - \Phi_{xl}(\psi_l) \quad (10)$$

The complex PHM demand (T_d [mm day⁻¹]; Eq. 11 and red segment in Fig. 1b) mirrors the minimalist version (Eq. 2) with modifications to fit into a dual-source LSM scheme (Sect. 2.3) that explicitly represents the coupled mass, heat and energy transfer between the plant ~~and its microclimate~~, its microclimate, and the atmosphere. The driving force of transpiration is no longer D (i.e., the leaf-to-air vapor pressure deficit) but rather the difference between leaf internal (e_i [kPa]) and surface (e_s [kPa]) vapor pressure (normalized by atmospheric pressure (P_{atm} [kPa]) to obtain units mol H₂O/mol air). We still assume e_i is the saturation vapor pressure at leaf temperature (e_{sat}), but e_s depends on the plant microclimate determined by the LSM energy balance solution at each time step (see Sect. S2.6). This plant microclimate is coupled to the well-watered stomatal conductance ($g_{s,ww}$ [mol air m⁻² s⁻¹]) via the optimality-based stomatal response model of Medlyn et al. (2011). The Medlyn model (Eq. 12) depends on the leaf vapor pressure difference ($e_i - e_s$ [kPa]), net CO₂ assimilation rate (A_n [mol CO₂ m⁻² s⁻¹]), and the leaf surface CO₂ mole fraction (approximated by the ratio of leaf surface CO₂ partial pressure (c_s [kPa]) and P_{atm} to give units mol CO₂/mol air) and is parametrized by the minimum stomatal conductance (g_o [mol air m⁻² s⁻¹]) and a slope parameter (g_1 [kPa^{0.5}]). Furthermore, we couple $g_{s,ww}$ to the Farquhar et al. (1980) photosynthesis model through A_n to ensure CO₂ diffusion into the leaf balances carbon assimilation (Collatz et al., 1991) (see Sect. S2.4). As in the minimalist model, the product of $g_{s,ww}$, driving force, and LAI yields the well-watered transpiration rate, T_{ww} , which we take to represent atmospheric moisture demand. Under water-stressed conditions, we keep a Jarvis-like stomatal closure term ($f(\psi_l)$) to downregulate $g_{s,ww}$ because it facilitates easy comparisons between our minimalist and complex formulations. However, we upgrade $f(\psi_l)$ from a piecewise linear form (Eq. 3) to a more realistic Weibull form (Eq. 13 and illustrated in Fig. 1b) parametrized by a shape factor (~~b_l~~) describing stomatal sensitivity (b_l) and the leaf water potential at 50% loss of stomatal conductance ($\psi_{l,50}$ [MPa]) (Klein, 2014; Kennedy et al., 2019).

$$T_d = LAI \cdot f(\psi_l) \cdot g_{s,ww} \cdot \frac{e_i - e_s}{P_{atm}} \cdot C_a = f(\psi_l) \cdot T_{ww} \cdot C_a \quad (11)$$

$$g_{s,ww} = g_o + \left(1 + \frac{g_1}{\sqrt{e_i - e_s}}\right) \cdot \frac{1.6 \cdot A_n}{c_s/P_{atm}} \quad (12)$$

$$f(\psi_l) = \frac{g_s(\psi_l)}{g_{s,ww}} = 2^{-\left(\frac{\psi_l}{\psi_{l,50}}\right)^{b_l}} \quad (13)$$

As in the minimalist PHM, the complex PHM supply and demand are coupled through their mutual dependence on ψ_l . The ψ_l^* that balances T_s (found at ψ_x^* for Eq. 9-10) and T_d (Eq. 11) yields the steady-state transpiration rate for the complex PHM

(T^{phm}). We numerically calculate this solution by recasting Eq. 9-11 as a nonlinear least squares problem and finding the ψ_l^* and ψ_x^* that ensure mass balance between the segments (see Sect. S2.5.3).

2.3 LSM Description and Calibration

We created an LSM to ~~allow testing test~~ of several transpiration downregulation schemes (Sect. 3.3) and ~~allow~~ removal of
170 modules (e.g. subsurface heat and mass transfer) that would unnecessarily complicate our comparisons. Our LSM is a dual-
source, ~~two-big-leaf two-big-leaf~~ approximation (Bonan, 2019) adapted from CLM v5 (Oleson et al., 2018) with several key
simplifications: i) steady-state conditions (i.e., no above ground mass, heat or energy storage), ii) neutral atmospheric stability,
iii) implemented the Goudriaan and Laar (1994) radiative transfer model in lieu of the two-stream approximation (Oleson
et al., 2018), and iv) forced LSM with soil moisture, soil heat flux and down-welling radiation data. We refer the reader to Sect.
175 S2 for full model details and justifications. We formulated the LSM in MATLAB and have made the codes available online :
https://github.com/sloan091/HESS_LSM.

We created separate LSM versions to test five different transpiration downregulation schemes: i) well-watered (no downreg-
ulation), ii) a single β (β_s) with static parameters, iii) a β separately applied to sunlit and shaded leaf areas (β_{2L}) with static
parameters, iv) a ‘dynamic β ’ with parameters dependent on T_{ww} (β_{dyn}), and v) a PHM. We calibrated the PHM version using
180 a two-step approach. First, we simulated 13,600 parameter sets using Progressive Latin Hypercube Sampling (Razavi et al.,
2019) on 15 soil and plant parameters (Table S6) and selected the best parameter set based on a comparison of RMSE, cor-
relation coefficient, percent bias and variance to Ameriflux evapotranspiration, sensible heat flux, gross primary productivity,
and net radiation site data (Fig. S5-S8). Unfortunately, the best parameter set contained an unrealistically low $\psi_{l,50}$ value for
ponderosa pine compared to observations (DeLucia and Heckathorn, 1989). Therefore, as a second step, we adjusted the $\psi_{l,50}$
185 and several other soil and plant parameters to more realistic values while ensuring that they ~~replicate~~ ~~replicated~~ the transpi-
ration downregulation behavior of the original parameter set. These parameter adjustments had minimal impact on ~~the~~ LSM
predictions as the underlying equations are highly nonlinear and multiple parameter sets can give near equivalent results (i.e.,
equifinality). We refer the reader to Sect. S4 for a more detailed account of calibration.

We parametrized the three LSM versions containing the β schemes by calibrating the respective β functions to the relative
190 transpiration outputs (T/T_{ww}) of the calibrated PHM version, while we ran the well-watered version using the calibrated pa-
rameters and downregulation turned off. The choice to calibrate a single LSM version ensured that the performance differences
between the schemes would be due to the PHM representing plant water use more realistically and not to the artifact of differ-
ing parameter fits between LSM versions. We refer the reader to Sect. S6.2 for specific details of the parameter fits for the β
schemes.

195 2.4 Site Description and Forcing Data

We calibrated and forced the LSM with half-hourly data from the US-Me2 “Metolius” Ameriflux site (Irvine et al., 2008). The
site consists of intermediate-age ponderosa pine trees on sandy loam soil in the Metolius River Basin in Oregon, USA. We
selected this site specifically for its subsurface soil moisture and temperature profiles as well as its separate measurements of

photosynthetically active radiation (PAR) and near infrared radiation (NIR). We used these boundary condition data to force the
200 LSM in lieu of solving one-dimensional, subsurface mass and heat transfer equations and atmospheric radiation partitioning
models. In particular, we forced the LSM with root zone averaged soil water potential (ψ_s ; estimated from measured soil water
content and a pedotransfer function) and the ground heat flux measurements. We selected the measurement depth of 50 cm
to represent ψ_s based on the deviation of measured *GPP* from its mean in relation to measured soil water content and vapor
pressure deficit (Fig. S10). The 50 cm measurements showed clear *GPP* downregulation under water stress. Furthermore, the
205 depth seemed reasonable given previous modeling at this site estimated an effective rooting depth of 1.1 m (Schwarz et al.,
2004). The atmospheric forcing for the LSM consisted of incoming direct and diffuse NIR and PAR fluxes, CO₂ concentration,
atmospheric pressure, vapor pressure, temperature and wind velocity at the measurement tower height of 32 m. Full description
of the forcing data is given in Sect. S5.

2.5 β Formulations

210 The β function empirically represents stomatal closure to declining leaf water status caused by soil water stress. By design, β
makes the simplifying assumption that stomata respond directly to soil water status (to avoid the complexity of implementing a
PHM ~~shown in~~ as illustrated by Fig. 1), which is readily available in TBM subsurface hydrology schemes as ψ_s or volumetric
soil water content (θ_s). This heuristic approach leads to multiple β functions based on modeler preference (see Supplement
of Trugman et al. (2018) for list of differing β formulations common to TBMs). Furthermore, even if a universal β function
215 existed, there is open debate on how to apply the β factor (Egea et al., 2011); some TBMs apply the β factor directly to
stomatal conductance (Kowalczyk et al., 2006; De Kauwe et al., 2015; Wolf et al., 2016) whereas others indirectly affect
stomatal conductance by applying the β factor to photosynthetic parameters (Zhou et al., 2013; Lin et al., 2018; Kennedy
et al., 2019). Here, we select a single β formulation that easily compares with the demand component of our PHM. Selecting a
different β formulation could alter our values; however, we do not expect our main conclusions about β and PHM differences
220 to change as long as two criteria are met. First, the stomatal downregulation factors for the PHM ($f(\psi_l)$) and β ($\beta(\psi_s)$) are
applied consistently in the transpiration downregulation scheme (to either $g_{s,ww}$ or photosynthetic parameters). Second, if β
is in terms of θ_s , a curvilinear form must be used (Egea et al., 2011) to ensure β can be mapped approximately to the water
potential space of our analysis.

In this paper, we have defined the β function in terms of ψ_s and apply the β factor directly to $g_{s,ww}$ and, in turn, T_{ww} (Eq.
225 14) for three key reasons: i) water transport through the soil-plant-atmosphere continuum follows a gradient of water potential,
not water content, ii) β using ψ_s rather than θ_s produces more realistic downregulation behavior compared to data (Verhoef and
Egea, 2014), and iii) applying the β factor to $g_{s,ww}$ directly corresponds to the PHM demand in both minimalist and complex
formulations. In the minimalist analysis (Sect. 3.1-3.2), $\beta(\psi_s)$ (Eq. 15 and illustrated in Fig. 1a) takes a piecewise linear form
(analogous to Eq. 3) which is parametrized by the soil water potential at incipient ($\psi_{s,o}$) and complete stomatal closure ($\psi_{s,c}$).
230 Similarly, in the LSM analysis (Sect. 3.3), $\beta(\psi_s)$ (Eq. 16 and illustrated in Fig. 1b) takes a Weibull form (analogous to Eq. 13)
parametrized by the soil water potential at 50% loss of stomatal conductance ($\psi_{s,50}$) and a stomatal sensitivity parameter (b_s).
The LSM analysis uses two versions of Eq. 16: i) a static version with constant b_s and $\psi_{s,50}$ (used by the β_s and β_{2L} schemes),

and ii) a dynamic version where b_s and $\psi_{s,50}$ are linear functions of T_{ww} (used by the β_{dyn} scheme). We refer the reader to Fig. S12 for illustrations of the different β versions.

$$235 \quad T^\beta = \beta(\psi_s) \cdot T_{ww} \quad (14)$$

$$\beta(\psi_s) = \begin{cases} 1 & \psi_s \geq \psi_{s,o} \\ \frac{\psi_{s,c} - \psi_s}{\psi_{s,c} - \psi_{s,o}} & \psi_{s,c} < \psi_s < \psi_{s,o} \\ 0 & \psi_s \leq \psi_{s,c} \end{cases} \quad (15)$$

$$\beta(\psi_s, T_{ww}) = 2^{-\left(\frac{\psi_s}{\psi_{s,50}(T_{ww})}\right)^{b_s(T_{ww})}} \quad (16)$$

3 Results

3.1 β as a Limiting Case of PHMs with Infinite Conductance

240 The supply-demand framework reveals that the minimalist PHM and β fundamentally differ in their coupling of the effects of soil water stress (represented by ψ_s) and atmospheric moisture demand (represented by T_{ww}) on transpiration. The PHM supply lines (red lines in Fig. 2a) illustrate soil-to-leaf water transport (Eq. 1) at a fixed soil water availability (ψ_s) under increasing pull from the leaf (lower ψ_l) and constant soil-plant conductance (g_{sp} ; supply line slope). The PHM demand lines (black lines in Fig. 2a) illustrate transpiration reduction under lower ψ_l (from stomatal closure) for two T_{ww} values. The supply
245 and demand lines intersect at the minimalist PHM solution (ψ_l^* and T^{phm} ; Eq. 4-5). Therefore, the minimalist PHM couples the effects of soil water stress to atmospheric moisture demand on transpiration downregulation because leaf water potential responds to ψ_s and T_{ww} until it reaches the point of steady-state transpiration (i.e., $T^{phm}(\psi_l^*) = T_s(\psi_l^*) = T_d(\psi_l^*)$).

The minimalist β transpiration rate (T^β , Eq. 14) ignores this coupling as the β function depends only on ψ_s and independently reduces T_{ww} (shown in Fig. 1). The conditions leading to the decoupling in β only arise if the supply lines are vertical
250 (Fig. 2b), which results in the relative transpiration (T^β/T_{ww}) depending on ψ_s only (single curve in Fig. 2d). Since g_{sp} is the supply line slope (Eq. 1), β represents a limiting case of the PHM in which the soil-plant system is infinitely conductive. More specifically, as g_{sp} increases, the leaf water potential approaches the soil water potential ($\psi_l^* \rightarrow \psi_s$; Eq. 17) and the PHM transpiration rate approaches the β transpiration rate ($T^{phm} \rightarrow T^\beta$; Eq. 18). Therefore, the $\beta(\psi_s)$ function (Eq. 15) equals the $f(\psi_l)$ function (Eq. 3) in PHMs and represents stomatal closure to declining leaf (or soil) water potential. In summary,

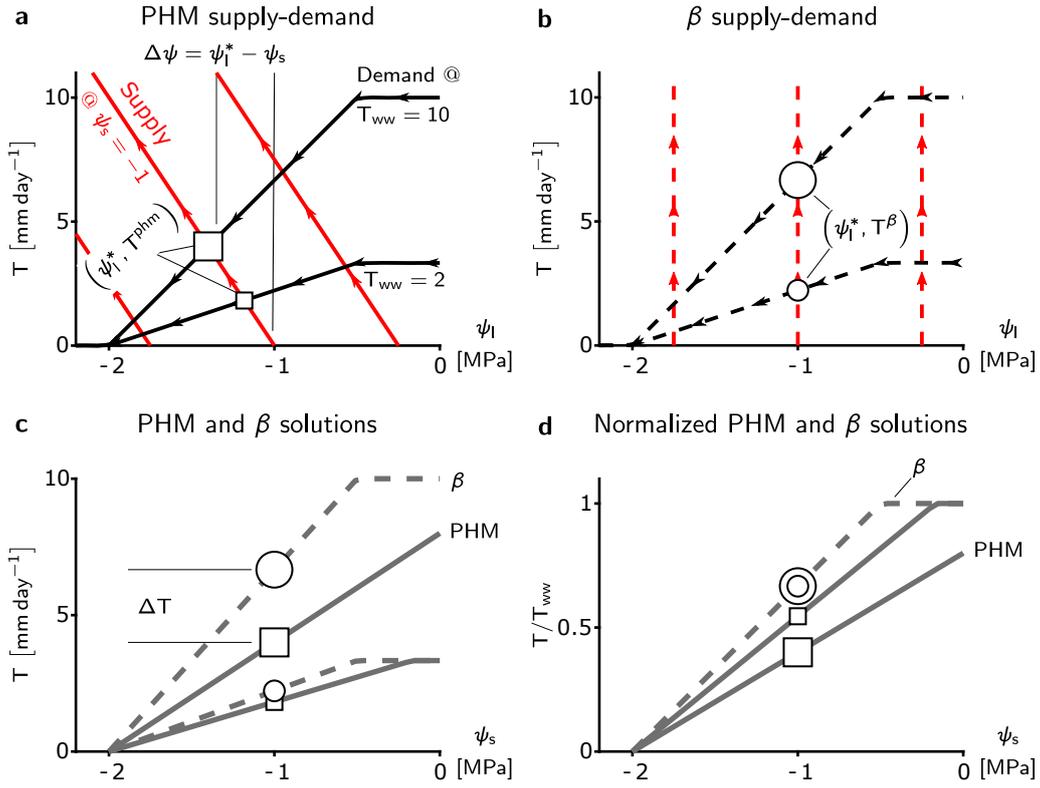


Figure 2. Fundamental differences between minimalist PHM and β . **a-b**, Supply (red) and demand (black) curves for PHM (**a**, solid lines) and β (**b**, dashed lines) under varying leaf water potentials (ψ_l). The squares (circles) represent the PHM (β) solution — i.e., the ψ_l^* where supply equals demand — for a single soil water availability (ψ_s) and two atmospheric moisture demands (T_{ww}). These markers carry through panels **c** and **d** to illustrate how the solutions between the PHM and β diverge at a single ψ_s . The relative size of the markers indicates corresponding T_{ww} . The water potential difference $\Delta\psi$ required to transport water from soil to leaf is shown in panel **a** for $\psi_s = -2$ MPa and $T_{ww} = 10$ mm day⁻¹. **c**, Solutions of panels **a** and **b** mapped to ψ_s , where ΔT is the difference between PHM and β transpiration estimates at $\psi_s = -2$ MPa and $T_{ww} = 10$ mm day⁻¹. **d**, Relative transpiration, in which solutions in panel **c** are normalized by T_{ww} . The β solutions collapse to a single curve, whereas the PHM solutions depend on T_{ww} .

255 the empirical β physically represents an infinitely conductive soil-plant system where stomata close in response to leaf water potential that depends solely on soil water potential with which it is equilibrated.

$$\lim_{g_{sp} \rightarrow \infty} [\psi_l^*] = \lim_{g_{sp} \rightarrow \infty} \left(\frac{\psi_s \cdot (\psi_o - \psi_c) + \frac{T_{ww} \cdot \psi_c}{g_{sp}}}{(\psi_o - \psi_c) + \frac{T_{ww}}{g_{sp}}} \right) = \psi_s \quad (17)$$

$$\lim_{g_{sp} \rightarrow \infty} (\Delta T) = \lim_{g_{sp} \rightarrow \infty} (T^{phm} - T^\beta) = \lim_{g_{sp} \rightarrow \infty} \left(T_{ww} \cdot \left[\frac{(\psi_{l,c} - \psi_s)}{(\psi_{l,c} - \psi_{l,o}) - \frac{T_{ww}}{g_{sp}}} - \frac{(\psi_{l,c} - \psi_s)}{(\psi_{l,c} - \psi_{l,o})} \right] \right) = 0 \quad (18)$$

260 The PHM coupling results in greater transpiration downregulation compared to β under the same environmental conditions (Fig. 2c). For a given soil water stress (ψ_s), β assumes $\psi_s = \psi_l^*$ and downregulates any atmospheric moisture demand (T_{ww}) value a fixed proportion (i.e., it scales linearly with T_{ww}); hence, it can be modeled with a single curve (Fig. 2d). Conversely, the PHM (with finite conductance) requires a water potential difference ($\Delta\psi = \psi_s - \psi_l^*$) to transport water from soil-to-leaf; therefore, ψ_l^* must be less than ψ_s and greater stomatal closure results (Fig. 2c). Furthermore, the PHM downregulates transpiration at a greater proportion with increasing T_{ww} (i.e., it scales nonlinearly with T_{ww}) as it requires a greater $\Delta\psi$ and lower ψ_l^* (Fig. 2d). Hence, PHMs require transpiration downregulation to be described as a function of both ψ_s and T_{ww} .

265 These minimalist model results suggest that the range of soil-plant conductances (g_{sp}) can generate a spectrum of possible transpiration responses to soil water stress (and atmospheric moisture demand). Two classes of behaviors emerge—one in a ‘soil-limited’ soil-plant system, in which g_{sp} is large enough for $\psi_l \approx \psi_s$, thus decoupling the effects of soil water stress and atmospheric moisture demand while allowing the relative transpiration to vary only with ψ_s (Fig. 2d). The other class of behavior arises in ‘transport-limited’ systems with finite g_{sp} , in which a non-negligible water potential difference ($\Delta\psi$) is required to transport the water to the leaf, resulting in additional downregulation compared to soil-limited systems (Fig. 2d) and requiring relative transpiration to depend on both ψ_s and T_{ww} .

3.2 Parameters Controlling the Divergence of β and PHMs

275 The differences in PHM and β transpiration estimates (ΔT) depends not only on g_{sp} , but also on soil water availability (ψ_s), atmospheric moisture demand (T_{ww}) and plant water use strategy ($\psi_{l,c} - \psi_{l,o}$). To disentangle these joint dependencies, we adjust a single variable and explore the impact on ΔT using the supply and demand lines (Fig. 3). The translation of supply lines represents ψ_s changes (indicated in Fig. 3a,c,e) and produces a non-monotonic relationship with ΔT over the range of soil water stress (i.e., $\psi_{l,c} < \psi_s < \psi_{l,o} + T_{ww}/g_{sp}$) (Fig. 3b,d,f). The peak ΔT occurs at the incipient point of stomatal closure ($\psi_{l,o}$) because i) when $\psi_s < \psi_{l,o}$, transpiration begins to decrease, and in its extreme limit, transpiration (and thus ΔT) approaches 0 and ii) when $\psi_s > \psi_{l,o}$, the effects of downregulation diminish in both models. The ΔT - ψ_s behavior acts as a baseline relationship in the following analysis of g_{sp} , T_{ww} , and $\psi_{l,c} - \psi_{l,o}$ controls.

285 The ΔT - ψ_s relationship increases with lower g_{sp} (Fig. 3b; greater transport-limitation) because flatter supply lines increase $\Delta\psi$ (Fig. 3a), requiring greater stomatal closure and hence additional downregulation for a PHM compared to β . Similarly, higher T_{ww} increases ΔT - ψ_s relationship (Fig. 3d), although the increase in $\Delta\psi$ stems from steeper demand line slope (Fig. 3c). In addition to increasing ΔT at each ψ_s value, the effects of g_{sp} and T_{ww} increase the range of soil water stress above $\psi_{l,o}$ (up to saturated soil water potential). This result indicates that PHMs can [model-simulate](#) transpiration downregulation under moist soil conditions that β potentially misses as it does not account for large $\Delta\psi$ values from transport-limitation and/or high atmospheric moisture demand. Finally, as g_{sp} increases (soil-limited) and T_{ww} decreases, ΔT tends to zero, once again, for slightly different reasons: for g_{sp} , the supply lines approach the β assumption (vertical dashed lines in Fig. 3a), whereas for T_{ww} , transpiration approaches zero.

290 Lastly, we explore the effect of plant water use strategy ($\psi_{l,c} - \psi_{l,o}$)—which approximates the sensitivity of stomatal closure to ψ_l —on ΔT . Altering $\psi_{l,c} - \psi_{l,o}$ does not affect $\Delta\psi$ like the other three variables; however, it modifies the range of soil

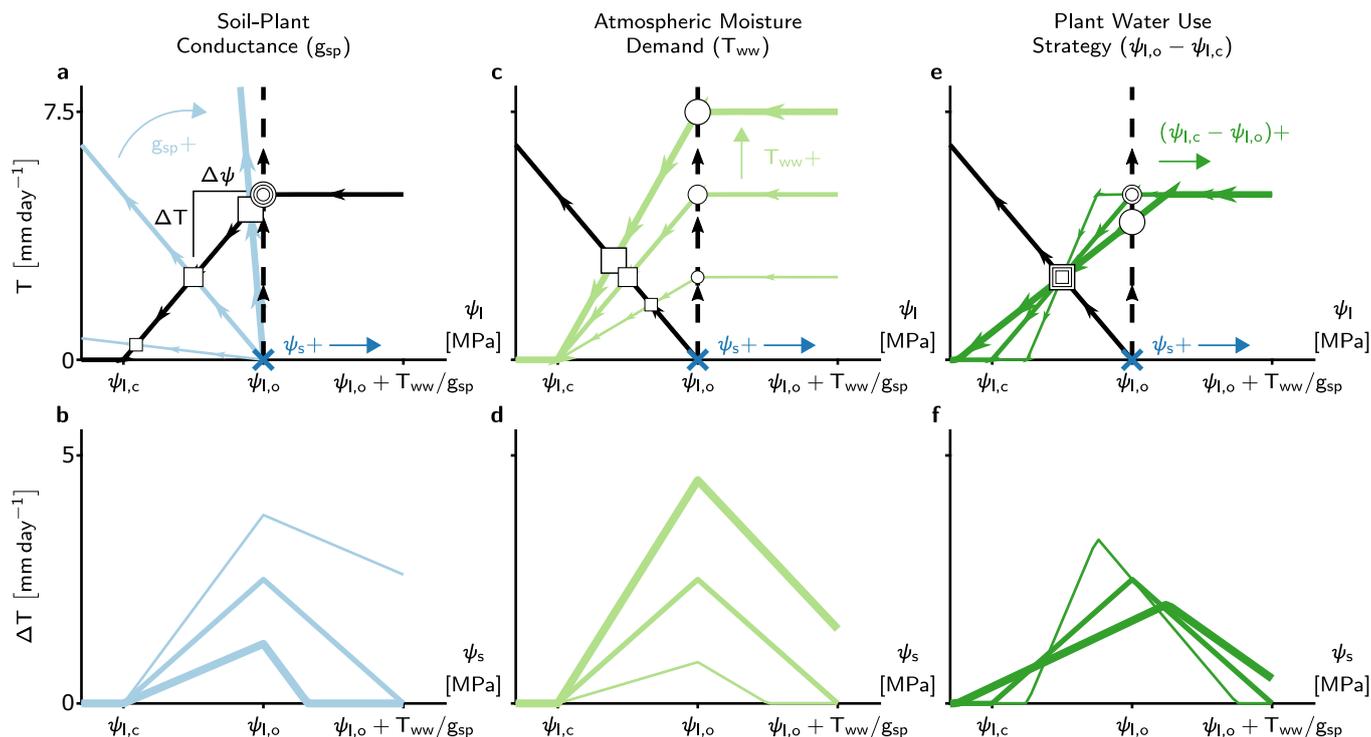


Figure 3. The effect of soil water potential (ψ_s), soil-plant conductance (g_{sp}), atmospheric moisture demand (T_{ww}) and plant water use strategy ($\psi_{l,o} - \psi_{l,c}$) on differences between the minimalist PHM and β models (ΔT). **a,c,e**, Supply-demand curves at a single soil water availability (indicated by the dark blue x at $\psi_s = \psi_{l,o}$), for three prescribed values of g_{sp} , T_{ww} , and $\psi_{l,o} - \psi_{l,c}$, respectively. Each parameter (g_{sp} , T_{ww} , or $\psi_{l,o} - \psi_{l,c}$) is set at 50% above (below) its base values at $g_{sp} = 10 \text{ mm day}^{-1} \text{ MPa}^{-1}$, $T_{ww} = 5 \text{ mm day}^{-1}$, $\psi_o = -1 \text{ MPa}$, $\psi_{l,c} = -1 \text{ MPa}$, and $\psi_o = -2 \text{ MPa}$, $\psi_{l,c} = -2 \text{ MPa}$ using thick (thin) colored lines. The squares (circles) indicate the PHM (β) solutions, with size corresponding to magnitude of the changing parameter values. Note: the vertical distance between correspondingly sized circle and square is ΔT and horizontal distance is $\Delta\psi$. **b,d,f**, The ΔT results from the panels **a**, **c**, and **e** calculated for a range of ψ_s with line thickness proportional to parameters in the aforementioned panels (e.g., thick blue line in panel **b** corresponds to 50% increase in g_{sp} shown in panel **a**). The x-axes are mapped from ψ_l in the top panels to ψ_s in the bottom panels.

water stress and redistributes ΔT to conserve the total error over the range. For example, a more aggressive plant water use
 295 strategy—closing stomata over a narrower range of ψ_l and ψ_s —creates a narrower range of soil water stress with a more
 peaked ΔT - ψ_s relationship due to more vertical demand lines (Fig. 3e). Therefore, whether the plant water use could
 amplify or diminish ΔT for a soil-system relies on how site-specific soil moisture variability overlaps with the range of soil
 water stress (Fig. 3f).

In summary, this minimalist analysis suggest PHMs are most needed to represent transport-limited soil-plant systems under
 300 high atmospheric moisture demand and moderate soil water availability. Plant water use will modulate these results; however,
 the impact depends on how site-specific soil moisture variability overlaps with the range of soil water stress.

3.3 Improving Transpiration Predictions with a PHM and a ‘Dynamic β ’

We now perform a modeling case study of the Ameriflux US-Me2 ponderosa site (Sect. 2.4) using our own calibrated LSM (Sect. 2.3) with five separate transpiration downregulation schemes: i) well-watered (no downregulation), ii) single β (β_s), iii) β separately applied to sunlit and shaded leaf areas (β_{2L}), iv) β_{dyn} , and v) PHM. Specifically we aim to i) ~~validate-verify~~ the transport-limitation spectrum ~~from the minimalist analysis~~ (Sect. 3.1) for a ~~more~~-complex PHM formulation common to TBMs, ii) identify errors incurred by selecting β over a PHM (Sect. 3.2) for a real transport-limited soil-plant system, and iii) develop a new ‘dynamic β ’ that approximates a PHM with simple modifications to the existing β .

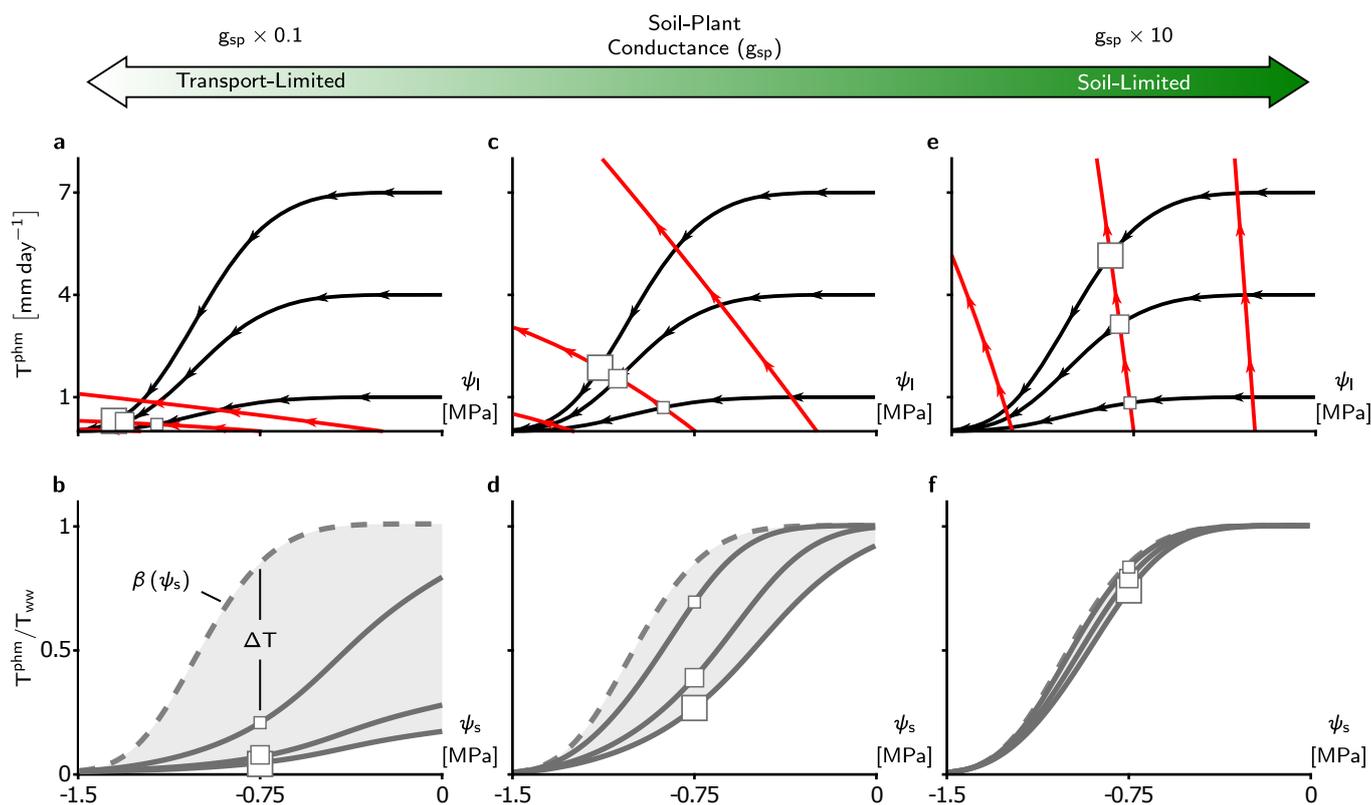


Figure 4. Transport-limitation spectrum observed in ~~the~~ complex PHM formulation. **a,c,e**, Supply-demand curves for three values of soil-plant conductance, g_{sp} , using the ~~more~~-complex PHM formulation. Panel **c** ~~is based on~~ ~~uses the~~ calibrated LSM parameters ($g_{sp} \approx 13 \text{ mm day}^{-1} \text{ MPa}^{-1}$) from the US-Me2 Ameriflux site ~~containing mature ponderosa pines that were determined for the LSM analysis discussed in this paper Sect. 2.3~~. Panels **a** and **e** contains the calibrated g_{sp} conductance ($g_{sp} \approx 13 \text{ mm day}^{-1} \text{ MPa}^{-1}$) multiplied by 0.1 and 10, respectively. The supply lines (red) are shown at ψ_s equal to 0, -0.75, and -1.5 MPa and demand lines (black) are shown at T_{ww} equal to 1, 4, and 7 mm day^{-1} . The PHM solution for ψ_s at -0.75 MPa is shown by the squares with size corresponding to T_{ww} magnitude. **b,d,f**, The relative transpiration for the PHM (solid) in panels **a**, **c**, and **e** and the infinitely conductive β solution (dashed line).

To aid our comparison of LSM transpiration downregulation schemes, we must first verify that the spectrum of transport-
310 limitation found in our minimalist analysis (Sect. 3.1) adequately describes the differences between ~~PHMs and the~~ PHM and
 β formulations common to TBMs. Our calibrated LSM uses a ~~more~~-complex PHM formulation (Sect. 2.2 and Fig. 1b) that
partitions the soil-plant-atmosphere continuum into soil-to-xylem, xylem-to-leaf, and leaf-to-atmosphere segments, each with
conductance curves that depend nonlinearly (e.g., sigmoidal or Weibull) on water potential. This added complexity does not
affect the spectrum of transport-limitation (Fig. 4). For clarity, we reiterate two main points from the minimalist PHM analysis
315 found in this complex analysis. First, soil-plant conductance (g_{sp}) controls whether the soil-plant system is soil-limited (high
 g_{sp} ; Fig. 4e-f) or transport-limited (low g_{sp} ; Fig. 4a-b) due to non-negligible water potential differences ($\Delta\psi$) creating large
differences between PHMs and β (high ΔT) at intermediate ψ_s values (Fig. 4b,d). Second, for a transport-limited system, ΔT
increases with higher variability in atmospheric moisture demand (T_{ww}), where the importance of ‘variability’ expands on our
minimalist results. To clarify, β should be considered an empirical model that could be fit anywhere within the range of the
320 PHM downregulation envelope (light gray shading in Fig. 4b,d,f). Therefore, greater T_{ww} variability creates a larger PHM
downregulation envelope and makes a single β increasingly inadequate for modeling transpiration downregulation.

The consistency between the minimalist and ~~more~~-complex PHM suggests that the divergence between PHMs and β in
transport-limited systems are not sensitive to the linear or nonlinear forms of supply or demand lines, but are rather controlled
by the existence of a finite conductance itself. Furthermore, these results strongly support the need to use two independent
325 variables, ψ_s and T_{ww} (rather than only ψ_s in β), to capture the coupled effects of soil water stress and atmospheric moisture
demand on transpiration downregulation in transport-limited soil-plant systems. In light of these findings, we have developed
a new ‘dynamic β ’ (β_{dyn}) that has an additional functional dependence on T_{ww} (Eq. 16) and compared it against four other
downregulation schemes in this LSM analysis.

We now assess the errors incurred by using a β rather than PHM downregulation scheme to model the US-Me2 ponderosa
330 pine site. The median diurnal evapotranspiration (ET; bare soil evaporation plus transpiration) for each LSM version for early
summer 2013-2014 (Fig. 5c-d) indicates that all downregulation schemes perform similarly due to high soil moisture and
minimal downregulation (Fig. 5c). However, as soil moisture declines during late summer (Fig. S11) the differences between
schemes emerge: the PHM and β_{dyn} schemes fit the ET observations the best, while β_{2L} , β_s , and well-watered schemes over-
predict ET (Fig. 5d). We explain the poor performance of the static β schemes by plotting the reduction in absolute percent
335 bias between the β_s and PHM schemes (Fig. 5e) ~~of~~ with respect to soil water stress (represented by volumetric soil water
content measurements at the site (θ_s [m^3 water m^{-3} soil])) and atmospheric moisture demand (represented by T_{ww} from the
well-watered LSM version). The PHM scheme provides substantial percent bias reduction relative to the static β_s scheme
under soil water stress ($\theta_s < 0.2$) for above- and below-average T_{ww} values ($T_{ww} \approx 4 \text{ mm day}^{-1}$). This result is true for both
static β schemes (β_s and β_{2L}) because they are fit to the average T_{ww} behavior over the simulation period (Fig. 5a-b and
340 Sect. S6.2). Therefore, as T_{ww} becomes higher (lower) than the average, these static β schemes will overpredict (underpredict)
transpiration. The PHM also improves performance during wetter soil conditions ($\theta_s > 0.2$) with high T_{ww} —which do not
represent typical ‘drought’ conditions—suggesting that PHMs capture transpiration downregulation that β potentially misses
as it cannot account for large soil-plant potential differences ($\Delta\psi$) under transport-limitation and/or high atmospheric moisture

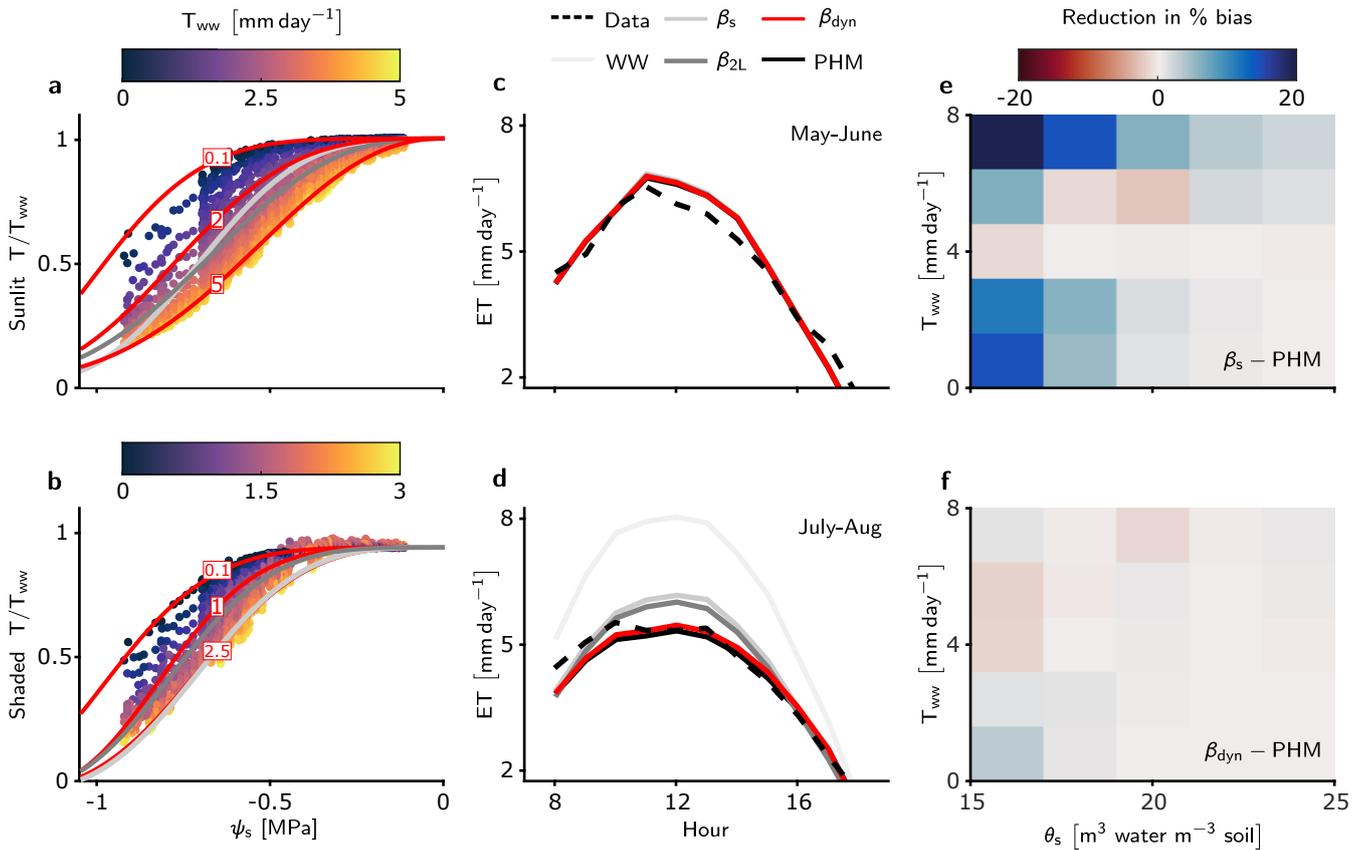


Figure 5. LSM evapotranspiration estimates improved by PHM and new ‘dynamic β ’. **a-b**, Fits of the β_s , β_{2L} , and β_{dyn} schemes to the relative transpiration outputs from the calibrated PHM scheme for the sunlit (**a**) and shaded **big-leaf** **big leaf** (**b**) of the LSM (see Methods). Note that only three of the infinite family of β_{dyn} curves are shown for illustration. Full fitting details of these three schemes are available in Sect. S2. **c-d**, The median diurnal ET estimates for the LSM with five transpiration downregulation schemes compared to Ameriflux observations at the US-Me2 site for early (**c**) and late summer (**d**). The **dual-source** **dual-source** LSM calculates ET as the sum of sunlit and shaded big-leaf transpiration and ground evaporation. Note: β_{dyn} (red) is overlying PHM (black) results as they are essentially the same. **e-f**, Reduction in absolute percent bias of ET between the β_s and PHM schemes (**e**) and β_{dyn} and PHM schemes (**f**) in terms of atmospheric moisture demand (represented by T_{ww}) and soil water status (represented by θ_s). In both plots, blue indicates PHM improvement over the selected β scheme.

demand (similar to Sect. 3.2). Lastly, the near average T_{ww} conditions lead to β providing enhanced performance, which can
 345 be explained by underlying biases in the calibrated parameter estimates (see Fig. S9).

Notably, the β_{dyn} downregulation scheme replicates the performance of the PHM scheme by adding a single dimension of T_{ww} to the original β scheme. This additional dependence on T_{ww} allows β_{dyn} to traverse along the PHM downregulation envelope with atmospheric moisture demand changes, whereas the static β schemes are fixed near mean conditions (Fig. 5a-b). The performance difference between PHM and β_{dyn} schemes is minimal in terms of percent change in bias across all

350 environmental conditions (Fig. 5f; max difference of 3%), median diurnal variations (Fig. 5c-d), and cumulative flux errors (Table S7-S8; max difference of 0.5%). Therefore, this additional dependence on T_{ww} is key to simulating the coupled effects of atmospheric moisture demand and soil water stress in PHMs and accurately modeling transpiration downregulation in transport-limited systems. For this transport-limited system, β_{dyn} requires two more parameters than the original β scheme, which is half the parameters required for our complex PHM formulation (Sect. S6.2). Furthermore, β_{dyn} does not require the
355 iterative solution of water potentials and transpiration in PHMs (Sect. 2.2). Rather, it calculates transpiration downregulation algebraically using ψ_s as in the original β . The β_{dyn} provides a future avenue for correcting existing β model bias without adding the computational and parametric challenges of more realistic PHMs.

4 Discussion and Conclusion

The spectrum of transport-limited transpiration explains why many TBMs that use β to represent transpiration downregulation
360 struggle to predict water, energy, and carbon fluxes under soil water stress (Sitch et al., 2008; Powell et al., 2013; Medlyn et al., 2016; Ukkola et al., 2016; Restrepo-Coupe et al., 2017; Trugman et al., 2018) and why implementing PHMs has led to performance improvements (Kennedy et al., 2019; Anderegg and Venturas, 2020; Eller et al., 2020; Sabot et al., 2020). Transpiration in a transport-limited soil-plant system, characterized by finite soil-plant conductance, depends on non-negligible water potential differences to transport water from the soil to the leaf, which ~~results~~result from the joint effects of atmospheric
365 moisture demand and soil water supply on leaf water potential. It is only when the soil-plant conductance becomes infinite (and the system becomes soil-limited) that leaf water potential approximates soil water potential, and transpiration arises as an independent function of soil water supply and atmospheric moisture demand. These are assumptions inherent to the empirical β and explains why β cannot capture the coupled effects of soil water stress and atmospheric moisture demand.

The implications of continued use of β will vary by site. Ecosystems with soil or plant hydraulic properties resistant to
370 flow (e.g., xeric ecosystems, tall trees, species with low xylem conductivity or roots that hydraulically disconnects from the soil during drought) will have large biases depending on the range of soil water availability and atmospheric moisture demand (T_{ww}) observed at the site (Fig. 3d and 4b). These errors will not be confined to drought periods, as higher atmospheric moisture demand and lower soil-plant conductance can result in errors even during wetter soil conditions (Fig. 3 and Fig. 5e). This is a crucial point, given projections indicate diverging degrees of VPD stress and soil water stress for ecosystems (Novick
375 et al., 2016). On the other hand, for soil-limited systems (e.g., irrigated crops, riparian vegetation, or groundwater-dependent ecosystems), β may adequately capture transpiration dynamics as soil water status may be a suitable proxy for leaf water status. Therefore, further work must identify the combinations of soil parameters and plant hydraulic traits that define transport- or soil-limited systems to identify ecosystems susceptible to bias from β . Our initial estimates indicate a soil-plant conductance value around $30 \text{ mm day}^{-1} \text{ MPa}^{-1}$ may be a rough threshold for transport-limitation (see Sect. S7).

380 Several other factors not covered in this work could exacerbate the differences between β and PHM predictions. We expect plant capacitance (already incorporated into some TBMs (Xu et al., 2016; Christoffersen et al., 2016)) will likely cause further deviations from β . PHMs with capacitance ~~is~~are expected to introduce hysteresis into transpiration downregulation (Zhang

et al., 2014) in transport-limited systems that existing β are not equipped to capture. However, this hysteretic behavior may diminish in a high conductance (i.e., soil-limited) system because plant and soil water potentials will quickly equilibrate, so β may still be an adequate alternative to a PHM. More advanced representation of stomatal response and plant hydraulic transport could further exacerbate β and PHM differences. Recent advances in optimality-based (Eller et al., 2020; Sabot et al., 2020) and mechanistic stomatal response models (Buckley, 2017) as well as more detailed PHM segmentation (Kennedy et al., 2019) may include additional couplings to plant water and metabolism that cannot be easily approximated by β . Regardless, the core message of this work is still relevant: for transport-limited soil-plant systems, PHMs are necessary to couple the effects of soil water stress and atmospheric moisture demand on transpiration, and β fails because soil water status is not an adequate substitute for leaf water status.

The recognition that a ‘dynamic β ’ model can replicate the complexity of a PHM with half the parameters and more direct computation (Sect. S6.2), simply by adding a dependence on atmospheric moisture demand to the β function, provides a useful pathway for overcoming both the limitations of β and the parametric uncertainties of PHMs (Paschalis et al., 2020; Anderegg and Venturas, 2020). The inadequacies of the static β have been noted since its inception. Feddes et al. (1978), who introduced [one of the first \$\beta\$ formulations](#), mentioned β ’s dependence on atmospheric moisture demand based on field data (Denmead and Shaw, 1962; Yang and de Jong, 1972) and early plant hydraulic theory (Gardner, 1960). Unfortunately, there have been only a few attempts to rectify these inadequacies in the modeling community, short of implementing a full PHM. For example, Feddes and Raats (2004) updated their original β model to vary the water potential at incipient stomatal closure linearly with atmospheric moisture demand, which has been adopted in the field scale SWAP model (Kroes et al., 2017), while the Ecosystem Demography-2 model (Medvigy et al., 2009) uses a sigmoidal function for transpiration downregulation that contains the ratio of soil water supply to evaporative demand. Within many TBMs and hydrological models, a ‘dynamic β ’ could easily replace the original β by allowing existing fixed parameters to vary with T_{ww} (already calculated in many transpiration downregulation schemes). In addition to improving TBM performances, ‘dynamic β ’ also has the potential to aid in remote sensing retrievals and indirect inferences of land surface fluxes. Currently, the state-of-the-art ECOSTRESS satellite provides global ET estimates based on a modified Priestley-Taylor formulation that uses a β function to downregulate ET under soil water stress (Fisher et al., 2020). These satellite products could easily implement the ‘dynamic β ’ formulation to correct biases for many transport-limited ecosystems. These potential applications rely on formalizing the relationship between the ‘dynamic β ’ parameters and their dependence on T_{ww} . As it stands, the ‘dynamic β ’ still needs to be calibrated to site-specific data; however, it provides a physically-informed alternative to PHMs with less calculation and fewer parameters. Further work will focus on generalizing the ‘dynamic β ’ by linking its parameters to measurable soil properties, plant hydraulic traits, and atmospheric feedbacks.

Code availability. The MATLAB codes for the LSM in this article are available at https://github.com/sloan091/HESS_LSM.

Author contributions. X.F. and S.T. conceived the idea; B.P.S and X.F. designed the research; B.P.S. performed the research; B.P.S. and X.F. wrote the paper; and S.T. contributed to refining results and revising the paper.

Competing interests. The authors declare no competing interests.

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