



# Machine Learning Deciphers CO<sub>2</sub> Sequestration and Subsurface Flowpaths from Stream Chemistry

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10 **Abstract.** Endmember mixing analysis (EMMA) is often used by hydrogeochemists to interpret the sources of stream solutes, but variations in stream concentrations and discharges remain difficult to explain. We discovered that machine learning can be used to reveal patterns in stream chemistry that pertain to information about weathering sources of solutes and also about subsurface groundwater flowpaths. The investigation has implications, in turn, for the balance of CO<sub>2</sub> in the atmosphere. For example, CO<sub>2</sub>-driven weathering of silicate minerals removes carbon from  
15 the atmosphere over ~10<sup>6</sup>-yr timescales. Weathering of another common mineral, pyrite, releases sulfuric acid that in turn causes dissolution of carbonates. In that process, however, CO<sub>2</sub> is released instead of sequestered from the atmosphere. Thus, to understand long-term global CO<sub>2</sub> sequestration by weathering requires quantification of CO<sub>2</sub>- versus H<sub>2</sub>SO<sub>4</sub>-driven reactions. Most researchers estimate such weathering fluxes from stream chemistry but interpreting the reactant minerals and acids dissolved in streams has been fraught with difficulty. We use a new  
20 machine learning technique in three watersheds to determine the minerals dissolved by each acid. The results show that the watersheds continuously or intermittently sequester CO<sub>2</sub> but the extent of CO<sub>2</sub> drawdown is diminished in areas heavily affected by acid rain. Sulfide oxidation contributes ~23% to 62% of sulfate fluxes. Without the new algorithm to deconvolve the mineral weathering, CO<sub>2</sub> drawdown was always overestimated. The new technique, which also elucidated the importance of different subsurface flowpaths and long-timescale changes in the watersheds,  
25 should have great utility as a new EMMA for investigating water resources worldwide.

## 1 Introduction

We need to understand the long-term controls on atmospheric CO<sub>2</sub> because of the impact of this greenhouse gas on global climate. This is important because humans are increasingly burning fossil fuels and releasing long-sequestered  
30 carbon to the atmosphere (Kasting and Walker, 1992). This new C flux upsets the natural long-term balance in the atmosphere between volcanic degassing and weathering-induced drawdown of CO<sub>2</sub> over millennial timescales. Chemical weathering of the most common rock-forming minerals, silicates and carbonates, removes CO<sub>2</sub> from the atmosphere by forming dissolved inorganic carbon that is carried in rivers to the ocean (DIC; Fig. 1). Within 10<sup>3</sup>-10<sup>4</sup> yr, this DIC is precipitated as marine calcite, releasing half or all of the atmospherically derived CO<sub>2</sub> back to the  
35 atmosphere for silicates and carbonates, respectively (Fig. 1). Thus, over this timescale, CO<sub>2</sub>-driven weathering (CO<sub>2</sub>-weathering) of silicates sequesters CO<sub>2</sub> out of the atmosphere while CO<sub>2</sub>-weathering of carbonates neither removes nor releases CO<sub>2</sub> to the atmosphere (Fig. 1). Recently, researchers have emphasized that this simple picture is made more complex because of another ubiquitous mineral, pyrite (Lerman et al., 2007). When pyrite weathers, it produces sulfuric acid that also dissolves silicates and carbonates, i.e., H<sub>2</sub>SO<sub>4</sub>-weathering. When DIC generated



40 through  $\text{H}_2\text{SO}_4$ -weathering of carbonates is carried to the ocean, marine calcite precipitates and releases  $\text{CO}_2$ ,  
increasing atmosphere concentrations (Calmels et al., 2011; Torres et al., 2014; Kölling et al., 2019). Thus,  
determination of the weathering contributions of silicates, carbonates, and pyrite is essential toward understanding  
how long-term  $\text{CO}_2$  drawdown will occur. In this paper we describe a new and powerful technique to interpret the  
sources of stream solutes to understand problems such as weathering. While we show the importance of this new  
45 machine learning technique to the weathering question, we also emphasize how machine learning can teach  
hydrogeochemists about subsurface flow paths and other characteristics of stream systems.

The most common way hydrogeochemists interpret the fluxes of weathering are to investigate stream and  
river chemistry. Determining the endmembers of weathering is important because streams integrate the byproducts of  
weathering reactions over drainage basins, allowing assessment of regional to global understanding of fluxes – but  
50 only if minerals weathered by different acid sources can be deconvoluted (Li et al., 2008; Calmels et al., 2011; Torres  
et al., 2016; Winnick et al., 2017; Burke et al., 2018; Killingsworth et al., 2018). In small-scale studies in the  
laboratory or soil profiles, mineral reactions can be inferred, but these cannot be scaled up easily (Navarre-Sitchler  
and Brantley 2007). Here we show that machine learning can decipher the balance of fluxes of  $\text{CO}_2$ - versus  $\text{H}_2\text{SO}_4$ -  
weathering over millennial timescales as written in stream chemistry. Using a new technique, we discovered that  
55 catchments partition water into subsurface flowpaths that can be i) deciphered with respect to the extent of pyrite,  
silicate, and carbonate weathering in different lithologies, and ii) interpreted with respect to whether weathering is  
driven by  $\text{CO}_2$  or  $\text{H}_2\text{SO}_4$ . This elucidates the long-term effects on the  $\text{CO}_2$  balance in the atmosphere.

Although geochemists commonly use stream chemistry to determine mineral sources of solutes via  
weathering reactions over large aerial extents (Gaillardet et al., 1999) and hydrologists commonly use end member  
60 mixing analysis (EMMA) to determine the sources of solutes in a stream (Christophersen et al., 1990), stream  
datasets remain difficult to interpret because of spatial inhomogeneities and temporal variations in endmember  
composition. For example, sulfur isotopes in stream solutes can distinguish pyrite-derived from rain-derived sulfate  
because pyrite typically is depleted in  $^{34}\text{S}$  (Burke et al., 2018; Killingsworth et al., 2018). But this attribution is  
difficult, more expensive, and often ambiguous because pyrite  $\delta^{34}\text{S}$  varies between formations (Gautier, 1986) or  
65 within a single catchment (Bailey et al., 2004). Likewise, inputs of sulfate to watersheds, such as acid rain, can  
swamp out the signal from mineral reactions, and can change significantly over time (e.g., because of changing acid  
rain deposition) (Lynch et al., 2000; Lehmann et al., 2007). These factors make it difficult to determine sulfur sources  
to varying stream chemistries over time.

Several so-called “inverse models” have been used successfully to partition sulfate into endmember sources  
70 for streams and rivers. These include the two prominent modeling approaches by Torres et al. (2016) and Burke et al.  
(2018). However, because the chemistry of acid rain has varied over the past decades, utilizing the full range of rain  
chemistry in those models results in unrealistic contributions of acid rain (i.e., > 100%) or models that fail to  
converge. This is because the chemistry of acid rain has been so variable that it spans the entire measured range of  
stream samples. Additionally, utilizing the approach of Burke et al. (2018), based on the approach of Gaillardet et al.  
75 (1999), requires a priori assignment of accurate endmember chemistries. Often, the researcher must rely on a few  
samples to characterize endmembers, resulting in large uncertainties in endmember chemistry and in source



apportioning. The machine-learning approach we describe here de-convolves sources of stream chemistry without pre-defining the endmembers. We demonstrate this with data from three well-studied watersheds with different characteristics. The new method discovers the endmember chemistries and, as a result, documents new findings of importance previously undiscovered with the other methods.

In the following, we focus first on Shale Hills, an acid rain-impacted shale watershed in Pennsylvania USA with extensive data for water/rock chemistry (Jin et al., 2010; Brantley et al., 2013a; Sullivan et al., 2016). This watershed allows the most complete understanding of solute sources. Although we do not show this here, if we use either of the two previously used models for source attribution, stream chemistry data for Shale Hills either does not separate acid rain and pyrite as a sulfate source (if we use the model of Torres et al., 2016) or yields a proportion for acid rain which is larger than 100% (if we use the model of Burke et al., 2018). As shown below, the NMF model easily defines endmembers and proportions.

We then show the utility of the machine learning method for watersheds where less geological information has been published: we investigate sulfide oxidation in East River and Hubbard Brook catchments. Like Shale Hills, East River is shale-hosted, but it receives little acid rain (Winnick et al., 2017). In contrast, Hubbard Brook has been extensively impacted by acid rain but is underlain by schist and glacial till (Likens et al., 2002). In both cases, NMF successfully determines endmembers and source proportions.

Reaction Number		Net Effect on Atmospheric CO <sub>2</sub>
<b>CO<sub>2</sub>-Weathering of Silicates</b>		
1	$\text{CaSiO}_3(\text{s}) + 2\text{CO}_2(\text{g}) + \text{H}_2\text{O} \rightarrow \text{Ca}^{2+}_{(\text{aq})} + 2\text{HCO}_3^{-}_{(\text{aq})} + \text{SiO}_2(\text{aq})$ Silicate Dissolution → Riverine DIC  -----  <10 <sup>4</sup> years	-2 CO <sub>2</sub>
2	$\text{CaSiO}_3(\text{s}) + 2\text{CO}_2(\text{g}) + \text{H}_2\text{O} \rightarrow \text{CaCO}_3(\text{s}) + \text{CO}_2(\text{g}) + \text{H}_2\text{O} + \text{SiO}_2(\text{aq})$ Silicate Dissolution → Marine Carbonate Precipitation  -----  <10 <sup>6</sup> years	-1 CO <sub>2</sub>
<b>CO<sub>2</sub>-Weathering of Carbonates</b>		
3	$\text{CaCO}_3(\text{s}) + \text{CO}_2(\text{g}) + \text{H}_2\text{O} \rightarrow \text{Ca}^{2+}_{(\text{aq})} + 2\text{HCO}_3^{-}_{(\text{aq})}$ Terrestrial Carbonate Dissolution → Riverine DIC  -----  <10 <sup>4</sup>	-1 CO <sub>2</sub>
4	$\text{CaCO}_3(\text{s}) + \text{CO}_2(\text{g}) + \text{H}_2\text{O} \rightarrow \text{Ca}^{2+}_{(\text{aq})} + 2\text{HCO}_3^{-}_{(\text{aq})} \rightarrow \text{CaCO}_3(\text{s}) + \text{CO}_2(\text{g}) + \text{H}_2\text{O}$ Terrestrial Carbonate Dissolution → Marine Carbonate Precipitation  -----  <10 <sup>6</sup> years	0 CO <sub>2</sub>
<b>H<sub>2</sub>SO<sub>4</sub>-Weathering of Silicates</b>		
5	$\text{CaSiO}_3(\text{s}) + \frac{1}{2}\text{FeS}_2(\text{s}) + \frac{15}{8}\text{O}_2(\text{g}) + \frac{7}{4}\text{H}_2\text{O} \rightarrow \text{Ca}^{2+}_{(\text{aq})} + \text{SO}_4^{2-}_{(\text{aq})} + \text{SiO}_2(\text{aq}) + \frac{1}{2}\text{Fe}(\text{OH})_3(\text{s})$ Silicate Dissolution → Riverine Sulfate  -----  <10 <sup>6</sup> years	0 CO <sub>2</sub>
<b>H<sub>2</sub>SO<sub>4</sub>-Weathering of Carbonates</b>		
6	$2\text{CaCO}_3(\text{s}) + \frac{1}{2}\text{FeS}_2(\text{s}) + \frac{15}{8}\text{O}_2(\text{g}) + \frac{7}{4}\text{H}_2\text{O} \rightarrow 2\text{Ca}^{2+}_{(\text{aq})} + 2\text{HCO}_3^{-}_{(\text{aq})} + \text{SO}_4^{2-}_{(\text{aq})} + \frac{1}{2}\text{Fe}(\text{OH})_3(\text{s})$ Terrestrial Carbonate Dissolution → Riverine DIC  -----  <10 <sup>4</sup> years	0 CO <sub>2</sub>
7	$2\text{CaCO}_3(\text{s}) + \frac{1}{2}\text{FeS}_2(\text{s}) + \frac{15}{8}\text{O}_2(\text{g}) + \frac{7}{4}\text{H}_2\text{O} \rightarrow \text{CaCO}_3(\text{s}) + \text{CO}_2(\text{g}) + \text{SO}_4^{2-}_{(\text{aq})} + \text{Ca}^{2+}_{(\text{aq})} + \frac{1}{2}\text{Fe}(\text{OH})_3(\text{s})$ Terrestrial Carbonate Dissolution → Marine Carbonate Precipitation  -----  <10 <sup>6</sup> years	+1 CO <sub>2</sub>

**Figure 1.** Schematic summarizing the reactions, timescales, and net CO<sub>2</sub> uptake or release for weathering of silicate and carbonate minerals at global scales by sulfuric acid and CO<sub>2</sub>.

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## 2 Methods

### 2.1 Study Sites

Where previous deconvolutions of endmembers were based on assumptions of the chemistry of dissolving minerals alone, data for watersheds shows that not only does mineral chemistry affect stream chemistry, but the flowpath of the water affects this chemistry (e.g. Brantley et al 2017). We demonstrate this with data from three well-studied watersheds with different characteristics. We focus first on Shale Hills, a small (0.08 km<sup>2</sup>), acid-rain impacted forested watershed underlain by Rose Hill Shale located in central Pennsylvania, USA (Brantley et al., 2018). The Rose Hill Formation shale contains ~0.14 wt% S as pyrite (FeS<sub>2</sub>) (Gu et al., 2020).

We then show utility of the method in East River (shale-hosted but it receives little acid rain) and Hubbard Brook (extensively impacted by acid rain but is underlain by schist and glacial till) catchments. Specifically, East River is a large (85 km<sup>2</sup>), mountainous watershed underlain by Mancos Shale that is located near Gothic, Colorado USA within the Gunnison River basin (Winnick et al., 2017). The Mancos is a black shale that contains ~1.6 wt% S as pyrite (Wan et al., 2019). Lastly, Hubbard Brook (Nezat et al., 2004), located in the White Mountains of New Hampshire USA, consists of a series of nine small (0.14-0.77 km<sup>2</sup>), forested watersheds underlain by Rangeley Formation metamorphosed shale (schist) and sandstone generally covered by glacial till derived mostly from the Kinsman granodiorite. The schist bedrock contains ~0.2-0.9 wt% S and till contains ~0.1-0.2 wt% S. Again, almost all S is present as iron sulfide (pyrite or pyrrotite). Both bedrock and till are largely carbonate-free.

### 2.2 Data Acquisition

For Shale Hills, daily stream chemistry has been reported from 2008-2010 (Brantley et al., 2013b; Brantley et al., 2013c; Brantley et al., 2013d). Additional samples were measured in other time intervals for sulfur isotopes and alkalinity (Jin et al., 2014). All samples were filtered through a 0.45 μm Nylon filter and aliquots for cation analysis were acidified with nitric acid. Cations were measured on a Leeman Labs PS3000UV (Teledyne Leeman Labs, Hudson, NH) inductively coupled plasma–optical emission spectrometer (ICP-OES), and anions were measured on a Dionex Ion Chromatograph (Sunnyvale, CA). Alkalinity was measured by titration with 0.16 M H<sub>2</sub>SO<sub>4</sub>. Discharge data are available online ([http://www.czo.psu.edu/data\\_time\\_series.html](http://www.czo.psu.edu/data_time_series.html)).

All published data from East River were used in analysis (Winnick et al., 2017), except for two samples with extremely high values of chloride (246 and 854 μM) because they differed significantly from the remaining sample chemistry (average Cl concentration = 21 μM). Hubbard Brook weekly chemistry from 2000-2017 was downloaded for the sub-catchments (3, 6, 7, 8, 9) that were not experimentally manipulated (Bernhardt et al., 2019). Stream flow data for each sub-catchment are from USDA Forest Service (USDA, 2019).

### 2.3 Machine Learning Model

To assign the proportion of sulfate in streams to sources, we first bootstrapped measurements to increase data volume and then used a method of blind source separation (Alexandrov and Vesselinov, 2014; Vesselinov et al., 2018) called



non-negative matrix factorization (NMF). NMF is unique from previously used methods in that it allows calculation of endmember compositions and mixing proportions simultaneously and does not rely on measurements or assumptions of endmembers a priori (Fig. 2A; see SM section 1). Specifically, NMF decomposes the  $n \times m$  matrix of stream sample chemistries,  $V$ , into two matrices  $W$  and  $H$ :

$$V = WH \quad (1)$$

Here,  $V$  is an  $n \times m$  matrix whose cell entries are solute concentration ratios,  $[X]/[SO_4^{2-}]$ , for stream samples. Here  $n$  refers to the sampling date,  $m$  refers to different solutes  $X$  ( $= Ca^{2+}, Mg^{2+}, Na^+, K^+, Cl^-$ ), and brackets refer to concentrations.  $W$  is the  $n \times p$  matrix whose cell entries are proportions,  $\alpha$ , for each endmember in each stream sample. Again,  $n$  refers to sampling dates, but  $p$  is the number of sources of solutes (referred to as endmembers). The proportions refer to the fractions of sulfate in each sample that derive from an individual endmember, where the sum of proportions equals  $1 \pm 0.05$  for each sample. As discussed later, we inferred after running the algorithm for the three watersheds that the endmembers represent different flowpaths in the subsurface. Therefore, these proportions of sulfate are referred to here as shallow, moderately shallow, and deep flowpaths, i.e.  $\alpha_{shallow}$ ,  $\alpha_{moderate}$ , and  $\alpha_{deep}$  respectively (only one of our target watersheds revealed all three flowpaths).  $H$  is the  $p \times m$  matrix whose cell entries are the concentration ratios that define the chemical signature of each of the  $p$  endmembers. The key to NMF is that these concentration ratios are not determined prior to apportionment but rather are determined from the data itself. In addition, the chemical signatures of each endmember can vary temporally around central tendencies. Because the solution to eq. 1 is non-unique, we run the model 20,000 times, apply a filter to the models, and then calculate the mean and standard deviation of the remaining models for trend and error analysis (see SM section 1; Eq. S1).

The only parameter that must be defined to run NMF a priori is the number of endmembers,  $p$ . We used principal component analysis (PCA) to determine the number of components needed to explain >90% of the variance in stream solute ratios, and trained NMF to the bootstrapped data while assuming that number of endmembers. Machine learning determined the compositions defining the endmembers and the mixing proportions of each endmember in each sample. After running NMF, we interpreted each endmember composition based on geological and watershed knowledge.

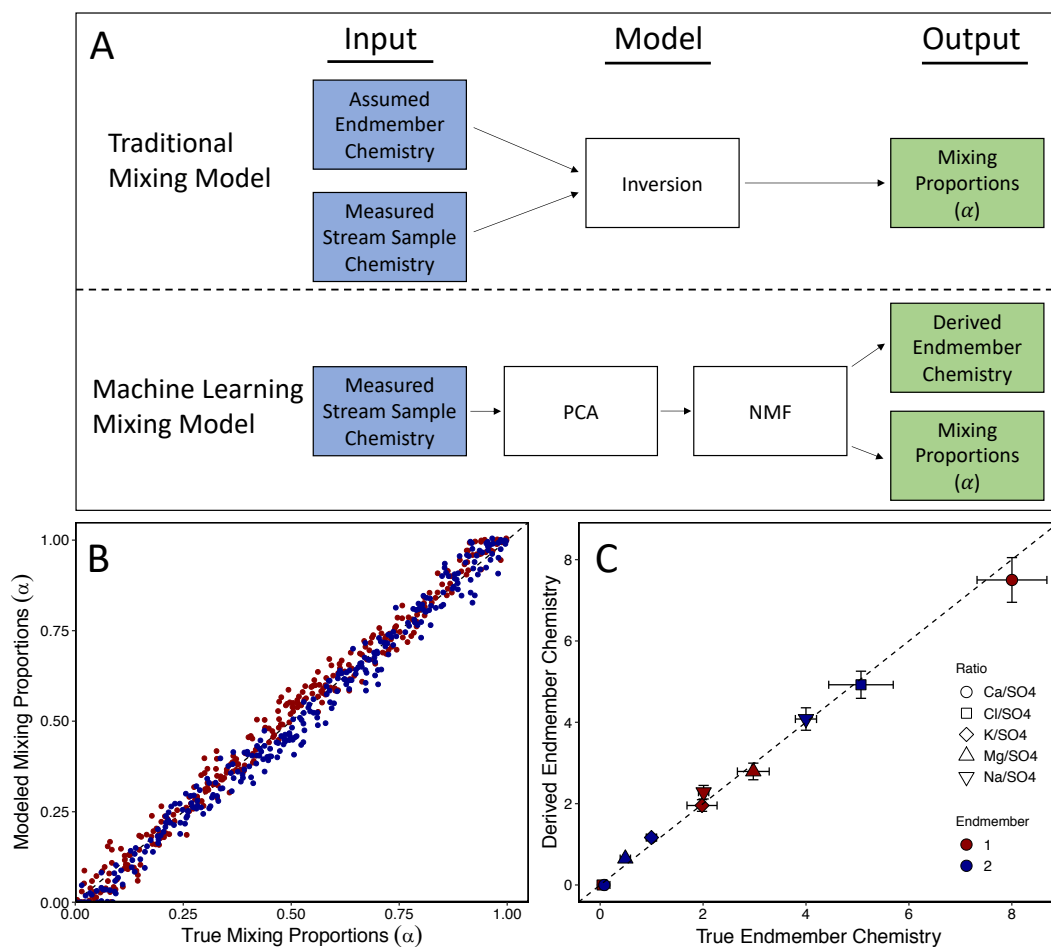
Based on the outputs of the NMF model, we calculated the weathering rates of sulfide, carbonate, and silicate minerals in the watersheds. Additionally, we calculated the relative contributions of sulfuric and carbonic acid driving those weathering reactions. For details on the weathering calculations see SM section 2.

## 2.4 Synthetic Dataset

NMF is an algorithm that has been used for many applications (e.g., spectral analysis, email surveillance, cluster analysis) but not, to our knowledge, for stream chemistry (Berry et al., 2007). To exemplify the validity of our modeling approach, we generated a dataset of synthetic stream chemistry versus time and ran it through our NMF model. First, we defined known endmember compositions, which are shown in Table S4. Next we randomly generated 300 synthetic stream samples that were each calculated as a mixture of the two endmembers. Lastly, we



ran NMF on the synthetic stream chemistry to determine the mixing proportions ( $\alpha$ ) and endmember compositions ( $[X]/[SO_4^{2-}]$ ), for the five solutes.



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Figure 2. Schematic diagram showing the differences between input, model type, and output of a traditional mixing model and our machine learning mixing model (A). Notably, in the machine learning mixing model, endmember chemistry is not assigned *a priori*, but rather derived from patterns in the data. Results from using our machine learning mixing model (i.e., NMF) on a synthetic dataset of known endmember chemistry and mixing proportions (i.e.,  $\alpha$ ) are shown in B and C. Using only the synthesized stream samples, the model adequately recovered the correct mixing proportions (B) and endmember chemistry (C).

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### 3 Results and Discussion

#### 3.1 Synthetic Data Model

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After generating the synthetic dataset of stream samples, we utilized NMF to determine the mixing proportions and endmember compositions. We then filtered out the poor fitting models (see SM Eq. 4). As described more fully in the SM, this left an average number of valid models of 62 (range: 42-77). The average variance between valid models was <10%. Without any prior information about the system, NMF accurately determined the correct mixing



proportions (RMSE = 0.04;  $R^2 = 0.98$ ;  $p < 0.001$ ; Fig. 2B) and endmember compositions (RMSE = 0.21;  $R^2 = 0.99$ ;  $p < 0.001$ ; Fig. 2C). In effect, the model was able to use patterns in the data to accurately unmix the samples.

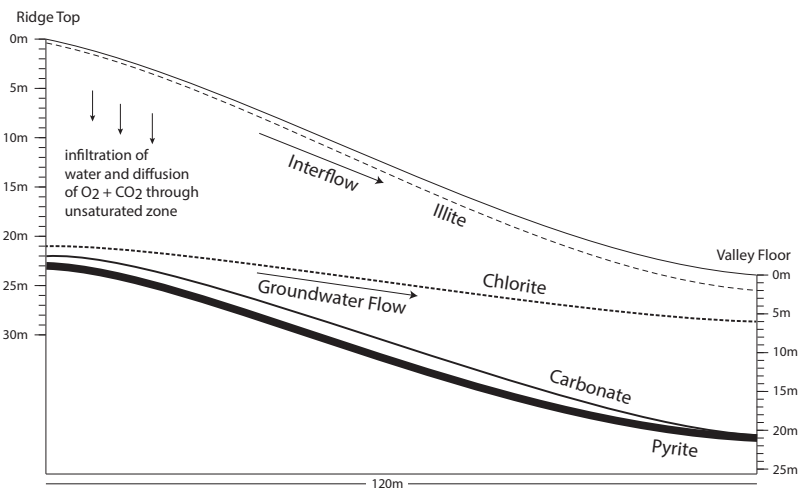
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### 3.2 Application to Shale Hills

While clay minerals in shale-underlain watersheds in rainy climates are found at all depths, pyrite and carbonate minerals are generally only found in unweathered shale at depth because they are depleted from upper layers (Fig. 3; Brantley et al., 2013a; Wan et al., 2019; Gu et al., 2020). For example, at Shale Hills, pyrite and carbonate minerals are only observed deeper than at least 15 meters below land surface (mbls) under the ridges and 2 mbls under the valley. In these deeper zones, calcite ( $\text{CaCO}_3$ ), ankerite ( $\text{Ca}(\text{Fe}_{0.34}\text{Mg}_{0.62}\text{Mn}_{0.04})(\text{CO}_3)_2$ ), and pyrite ( $\text{FeS}_2$ ) dissolve in regional groundwaters that flow to the stream (Brantley et al., 2013a; Gu et al., 2020). These groundwaters thus contribute DIC,  $\text{Ca}^{2+}$ ,  $\text{Mg}^{2+}$ , and  $\text{SO}_4^{2-}$  into the stream.

Like many catchments, water also flows to the stream in Shale Hills along a much shallower near-surface flowpath, referred to here as interflow (Fig. 3). Interflow occurs along a transiently perched water table within the upper 5-8 mbls. The most abundant mineral, illite ( $\text{K}_{0.69}(\text{Si}_{3.24}\text{Al}_{0.76})(\text{Al}_{1.69}\text{Fe}^{3+}_{0.10}\text{Fe}^{2+}_{0.16}\text{Mg}_{0.19})\text{O}_{10}(\text{OH})_2$ ), dissolves in interflow along a flowpath confined largely to the soil and upper weathered rock zone. Illite dissolution releases DIC and  $\text{Mg}^{2+}$  and  $\text{K}^+$  to interflow waters and causes precipitation of clays and iron oxides. Interflow derives ultimately from local precipitation that also contains  $\text{Na}^+$ ,  $\text{Cl}^-$ , and  $\text{SO}_4^{2-}$ . Interflow and deep groundwater flowlines converge under the catchment outlet where the stream, on average, is 90% interflow and 10% deep groundwater (Sullivan et al., 2016; Li et al., 2017). Only one mineral, chlorite ( $(\text{Fe}^{2+}_{0.40}\text{Mg}_{0.15}\text{Al}_{0.35})_6(\text{Si}_{0.76}\text{Al}_{0.24})_4\text{O}_{10}(\text{OH})_8$ ), is observed to begin to weather in the deep groundwater and continue weathering all the way to the surface (Fig. 3; Gu et al., 2020). Chlorite thus weathers to release  $\text{Mg}^{2+}$  to both interflow and deep groundwater. While most water entering the catchment leaves as interflow without entering deep groundwater, the wide reaction zone observed for chlorite is consistent with vertical infiltration of water to the deeper zone (Brantley et al., 2017).

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**Figure 3.** Schematic cross section of Shale Hills showing the depths (labelled lines) where pyrite, carbonate, chlorite, and illite reactions initiate (modified after Brantley et al., 2013a). Illite and chlorite dissolve at all depths above the labelled lines, but carbonate minerals



and pyrite only dissolve in a narrow one-meter wide depth zone under the ridge that widens to tens of meters toward the valley. These  
210 reaction front depths were estimated and extrapolated from bulk chemistry measured in samples from boreholes located at the ridge  
and valley (Jin et al., 2010; Brantley et al., 2013a; Gu et al., 2020).

PCA for stream chemistry (2008-2010) at Shale Hills revealed two sources of sulfate, and this was used to  
set up NMF, i.e.,  $p = 2$  (Table S1). By comparing the compositions from matrix  $H$  determined by NMF to our  
215 knowledge of the subsurface (Fig. 3), we interpreted the two endmembers as deep and shallow weathering along the  
two flowpaths, respectively (Jin et al., 2014; Sullivan et al., 2016). The endmember with high  $[\text{Ca}^{2+}]/[\text{SO}_4^{2-}]$  and  
 $[\text{Mg}^{2+}]/[\text{SO}_4^{2-}]$  was attributed to deep weathering because Ca- and Mg-containing minerals (i.e., calcite and ankerite)  
only dissolve at depth (Fig. 3; Gu et al., 2020). The high  $[\text{Cl}^-]/[\text{SO}_4^{2-}]$  endmember was attributed to shallow water  
dominated by Cl-containing rain (interflow). This attribution revealed, consistent with other studies of the acid rain-  
220 impacted northeastern United States, that precipitation accounts for the majority of sulfate flux (i.e., 77%) at Shale  
Hills.

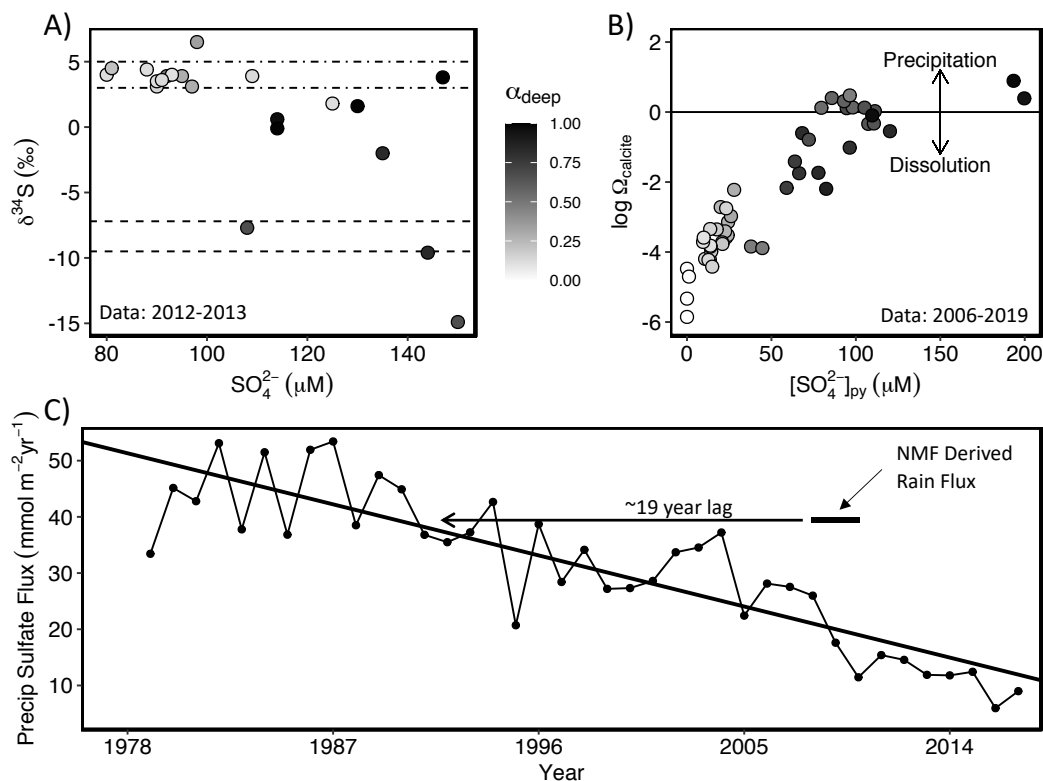
Many lines of evidence back up these endmember attributions. The sulfate in the shallow endmember derives  
from flow well above the pyrite oxidation front through pyrite-depleted rock and is thus attributed to acid rain, while  
the sulfate in the deep endmember is attributed mostly to pyrite oxidation. Some sulfate from acid rain may make it  
225 to the regional groundwater, but the fraction is small. At Shale Hills, acid rain always contains  $\text{Cl}^-$  and pyrite  
oxidation always preferentially dissolves carbonate minerals, giving each flowpath endmember a unique signature.

To test the NMF deconvolution, we compared these attributions to isotopic data. Depletion in isotopically  
heavy S is observed to correlate with increasing concentrations of pyrite-derived sulfate (Fig. 4A), consistent with  
depleted  $\delta^{34}\text{S}$  signatures in pyrite (e.g., -20‰; Killingsworth et al., 2018). In contrast, acid rain shows  $\delta^{34}\text{S}$  values  
230 around +3-5‰ (Bailey et al., 2004), and low sulfate concentrations in stream samples are characterized by  $\delta^{34}\text{S}$   
values within this range. Also, as pyrite oxidizes, the concentration of sulfate increases and the  $\delta^{34}\text{S}$  values decrease  
to reflect the inferred composition of pyrite, -9.5‰ to -7.2‰ (Fig. 4A). Finally, Gu et al. (2020) showed that pyrite  
oxidation drives the calcite dissolution at Shale Hills, and this is corroborated by NMF results showing that samples  
near calcite equilibrium have the highest pyrite-derived sulfate concentrations (Fig. 4B).

235 However, the annual flux of acid rain-derived sulfate in the shallow endmember determined from NMF at  
Shale Hills (Table 1) far exceeds the wet deposition of sulfate during the sampling period (Fig. 4C). But such  
inconsistencies have been noted elsewhere and attributed to travel-time delays over decades between acid rain input  
and stream output (Prechtel et al., 2001; Mörth et al., 2005). Fig. 4C thus allows us to calculate a ~19-31-year lag  
time between input and export of sulfate from the temporally changing acid rain input (see SM section 2.4).

240 Weathering profiles at Shale Hills, the chemistry of the composition ( $H$ ) matrix, sulfur isotopes, calcite  
saturation, and lag in acid rain export all support our interpretation that the two components in the NMF model are  
shallow and deep flowpaths and that sulfate largely derives from acid rain and pyrite respectively.





245 Figure 4. (A) Sulfur isotope composition plotted versus sulfate concentration in stream or groundwater at Shale Hills where S isotopes were measured (symbols; Jin et al., 2014). Dot-dashed lines represent the average sulfur isotope range for acid rain in USA (3-5‰; Bailey et al., 2004) and dashed lines represent the average sulfur isotope range of pyrite calculated from NMF results (-9.5‰ to -7.2‰). Sulfur isotopes in pyrite at Shale Hills are assumed as shown from -1‰ to -15‰ (Jin et al., 2014). (B) Plot showing the logarithm of calcite saturation index vs. the concentration of pyrite-derived sulfate (NMF-derived) in surface and groundwater at Shale Hills. Black line represents calcite solubility. Some samples in B differ from those in A because more samples were collected for alkalinity than sulfur isotopes. In both A and B, color shading represents the fraction of total sulfate derived from pyrite calculated by NMF (i.e.,  $\alpha_{\text{deep}}$ ). (C) Time series plot showing the flux of sulfate in Pennsylvania NADP site PA42 (2.8 km from Shale Hills) from wet and dry deposition (see SM section 2.4). Black symbol shows the NMF results for sulfate flux derived from atmospheric inputs for Shale Hills during our sampling period, and the inferred 19 y lag.

### 255 3.3 Rates of Weathering and CO<sub>2</sub> Sequestration at Shale Hills

260 With these calculations we can use NMF results to elucidate the effect of sequestration or release of CO<sub>2</sub> at Shale Hills over millennial timescales. CO<sub>2</sub>-driven weathering of the silicate minerals chlorite and illite removes carbon from the atmosphere and carries it as DIC in rivers to the ocean where it is buried as carbonate minerals (Figure 1, Table S2). In contrast, calcite and ankerite weathering coupled to pyrite oxidation instead releases CO<sub>2</sub> to the atmosphere over those timescales. Additionally, acid rain can interact with silicate minerals competing with CO<sub>2</sub> for silicate dissolution.



To determine the effect on CO<sub>2</sub>, we calculate a new parameter which we call the stream CO<sub>2</sub> sequestration coefficient,  $\kappa_{stream}$ . This coefficient, calculated for a single stream sample with units of meq CO<sub>2</sub>/meq cation, reveals the moles of CO<sub>2</sub> sequestered or released during weathering per cation equivalent:

$$\kappa_{stream} = \frac{1}{2}(-1 + \gamma_{stream} + \zeta_{stream}), \quad (2)$$

Here,  $\gamma_{stream}$  is the proportion of cation equivalents in the stream derived from carbonate weathering, and  $\zeta_{stream}$  is the proton equivalents from sulfuric acid in the stream per total base cation equivalent in the stream. We calculate  $\gamma_{stream}$  for a sample by multiplying the pyrite-derived sulfate concentration (i.e.,  $\alpha_{deep}$  multiplied by total sulfate concentration) by the  $[Ca^{2+}]/[SO_4^{2-}]$  and  $[Mg^{2+}]/[SO_4^{2-}]$  ratios of the deep weathering endmember (derived by NMF) and then dividing the result by the total concentration of base cations equivalents measured in the sample. Streams often have non-acid sources of sulfate (e.g., fertilizer, gypsum); thus,  $\zeta_{stream}$  is calculated by multiplying the fraction of sulfate associated with sulfuric acid (e.g.,  $\alpha_{deep} + \alpha_{shallow}$ ) by the total sulfate concentration and dividing that by the total base cation equivalents in the sample. This calculation shows that seasonally, Shale Hills switches between net production and net consumption of CO<sub>2</sub> (Fig. 5D). Using the weathering reactions described in SM section 2.2, we calculate the CO<sub>2</sub> flux and find that annually CO<sub>2</sub> dynamics are net-neutral at Shale Hills (Table 1).

The switch in consumption and production is related to the dominant seasonal flowpath. In the dry season when water tables are low, the stream water is often dominated by deeper groundwater flow that interacts with the deep pyrite reaction front and has little contribution of acid rain. Even though the dry season at Shale Hills is characterized by higher contributions of pyrite-derived sulfate, the watershed acts predominantly as a sink of CO<sub>2</sub> during this time of the year because the drawdown of CO<sub>2</sub> from silicate weathering is larger than the efflux of CO<sub>2</sub> from pyrite-driven weathering of carbonate. In the wet season when water tables are high, the stream is dominated by shallow interflow that does not interact with pyrite but has a large contribution of acid rain. Especially during this wet season, acid rain reduces the CO<sub>2</sub> consumption by dissolving silicates that could otherwise have interacted with carbonic acid. This is similar to the ideas described in Kanzaki et al. (2020). The impacts of acid rain are greatest during the wet season, during which time the rain often causes the watershed to become a CO<sub>2</sub> source by interacting with the deep carbonate minerals and reducing the CO<sub>2</sub> consumption by silicate minerals.

To test the accuracy of these inferences based on NMF, we compare to previous results for Shale Hills. Based on soil pore-water chemistry and rain fluxes at Shale Hills, Jin et al. (2014) estimated the CO<sub>2</sub> drawdown from silicate weathering to be 44 mmol m<sup>-2</sup> yr<sup>-1</sup>. We find that if we assume all silicate weathering is CO<sub>2</sub>-driven, then the silicate weathering drawdown is 38 mmol m<sup>-2</sup> yr<sup>-1</sup>, which is consistent with the estimate of Jin et al (2014). But this value is an overestimate that ignored pyrite and acid rain. When we correct this value for H<sub>2</sub>SO<sub>4</sub>-weathering of carbonate and silicate derived from pyrite and acid rain, we find that Shale Hills is actually neutral when averaged over annual timeframes and does not sequester CO<sub>2</sub> on net (Table 1).



**Table 1. Fluxes of  $\text{SO}_4^{2-}$ , Cations, and  $\text{CO}_2$  and  $\text{CO}_2$  Sequestration Coefficients**

	Shale Hills	East River	Hubbard Brook
	<i>Sulfate Fluxes (<math>\text{mmol m}^{-2} \text{yr}^{-1}</math>)</i>		
Total Sulfate	$52.4 \pm 5.0$	$198 \pm 80.6$	$29.5 \pm 0.4$
Sulfide-derived Sulfate	$12.1 \pm 5.0$	$122 \pm 71.8$	$8.6 \pm 0.3$
Rain-derived Sulfate	$39.5 \pm 6.2$	$76.0 \pm 36.7$	$20.9 \pm 0.4$
	<i>Fluxes (<math>\text{meq m}^{-2} \text{yr}^{-1}</math>)<sup>a</sup></i>		
Total Cations	$331 \pm 78.0$	$1540 \pm 375$	$76.5 \pm 1.3$
$\text{CO}_2$ -weathering of Silicate Cations	$29.6 \pm 13.2$	$316 \pm 252$	$17.5 \pm 0.9$
$\text{CO}_2$ - weathering of Carbonate Cations	$264 \pm 59.3$	$588 \pm 197$	NA <sup>b</sup>
$\text{H}_2\text{SO}_4$ - weathering of Silicate Cations	$53.5 \pm 10.9$	$152 \pm 73.3$	$59.0 \pm 0.8$
$\text{H}_2\text{SO}_4$ - weathering of Carbonate Cations	$69.5 \pm 23.1$	$489 \pm 287$	NA <sup>b</sup>
$\text{CO}_2$ sequestration or release	$2.6 \pm 6.3^c$	$-35.5 \pm 172$	$-8.7 \pm 0.5$
	<i><math>\text{CO}_2</math> Sequestration Coefficients</i>		
$K_{\text{rock}}$	$-0.08 \pm 0.11$	$0.08 \pm 0.17$	$-0.19 \pm 0.11$
$K_{\text{stream}}^{\text{d,e}}$	$0.01 \pm 0.03$	$-0.03 \pm 0.11$	$-0.14 \pm 0.06$

<sup>a</sup>Weathering fluxes calculated following procedure in SM section 2.2

<sup>b</sup>No carbonate cation fluxes reported because the bedrock contains no carbonate

<sup>c</sup>Negative  $\text{CO}_2$  flux indicates sequestration and positive indicates release to atmosphere

<sup>d</sup>Stream  $\text{CO}_2$  sequestration coefficient reported as discharge-weighted average

<sup>e</sup>Rock and stream  $\text{CO}_2$  sequestration coefficients show that Shale Hills and East River are net-neutral with respect to  $\text{CO}_2$ , and Hubbard Brook is a sink of  $\text{CO}_2$

### 3.4 East River

Shale Hills is unique in that it is a monolithologic catchment and the data volume to constrain endmember apportionment is large. But NMF also works well for watersheds in which the subsurface flow and reactions are less constrained partly due to the more complex subsurface geology. The weathering profile at East River (underlain by black shale) shows that pyrite and carbonate are depleted in upper layers but start dissolving at ~2-4mbls (Wan et al., 2019). PCA shows that the number of components is 2. The composition of the endmembers for East River are similar to Shale Hills (Table S1); however, the endmember composition indicates a higher proportion of carbonate dissolution by sulfuric acid (see SM section 2).

Based on NMF for East River, pyrite contributes 62% of the annual sulfate flux (Table 1). Sulfuric acid drives 29% to 69% of carbonate dissolution depending on the season, and this compares well with previous estimates of 35-75% (Winnick et al., 2017). Unlike Shale Hills, pyrite oxidation at East River is the dominant source of sulfate because acid rain is less important, and the black shale is pyrite-rich (Fig. 5B).

Both Shale Hills and East River intermittently switch between acting as a source or sink of  $\text{CO}_2$  (Fig. 5), and both are net neutral within error with respect to  $\text{CO}_2$  on an annual basis. Interestingly, the seasonality of the switch between Shale Hills and East River is reversed. During baseflow (i.e., flow sustaining stream in between periods of precipitation), Shale Hills is predominantly a sink of  $\text{CO}_2$ , but sometimes it switches to a source of  $\text{CO}_2$  in the wet season because of the impacts of acid rain. Without the large acid rain influx, East River instead acts as a sink of  $\text{CO}_2$  during the wet season of snowmelt and then switches to a source during baseflow. This reflects that most of the



325 sulfate at East River is derived from the pyrite-rich shale (i.e., 65%) and that H<sub>2</sub>SO<sub>4</sub>-weathering of carbonates is a  
more dominant reaction at East River than at Shale Hills. Our results are consistent with previous interpretations  
(Winnick et al., 2017) suggesting CO<sub>2</sub> efflux rates are highest in baseflow-dominated and lowest in snowmelt-  
dominated flow regimes. We agree with the interpretations of Winnick et al. (2017), but NMF adds the new insight  
that on an annual basis, the efflux of CO<sub>2</sub> from H<sub>2</sub>SO<sub>4</sub>-weathering of carbonates is balanced by CO<sub>2</sub>-weathering of  
silicates making East River net neutral with respect to CO<sub>2</sub>.

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### 3.5. Hubbard Brook

Monolithologic shale watersheds are not the only target chemistries that can be deconvoluted with NMF. Large  
variations in the δ<sup>34</sup>S composition of the bedrock at Hubbard Brook (Bailey et al., 2004) mean that sulfur isotopes in  
stream water are difficult to unambiguously apportion sulfate sources. Weathering fluxes from pyrrhotite (FeS), the  
335 sulfide mineral known to be present, have therefore never been fully constrained (Mitchell et al., 2001).

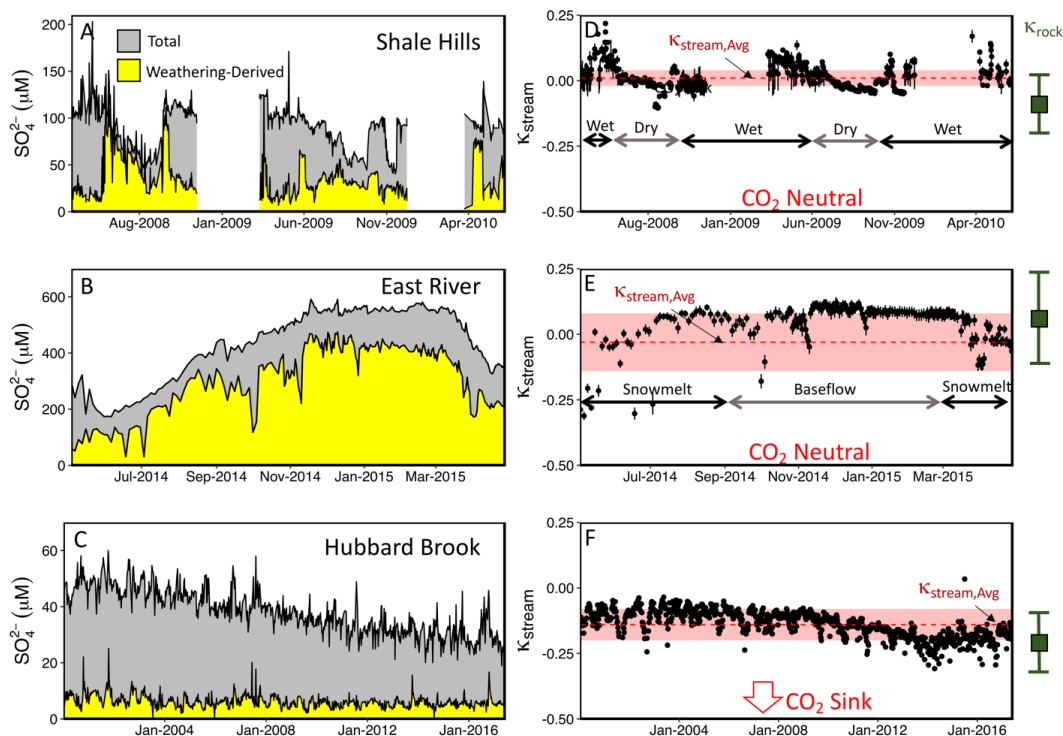
At Hubbard Brook, PCA shows three endmember sources of sulfate. As described below, we attribute these  
to three inferred flow lines, two in till and one at depth: waters flowing through i) shallow soil developed from till, ii)  
moderately-deep, less-weathered till, and iii) weathering bedrock. A three-layered weathering profile has been  
observed in other till-covered areas of New Hampshire as well (Goldthwait and Kruger, 1938). We used these ideas  
340 to identify endmembers as described below.

Concentrations of sulfate in acid rain have declined over time in northeastern USA (Lynch et al., 2000;  
Lehmann et al., 2007). Of the three NMF-determined endmembers at Hubbard Brook, two of them show declining  
sulfate concentrations with time. We therefore attributed the first and second endmembers to acid rain (Fig. S1).

345 Only one endmember showed little to no decline in sulfate concentration over time, and we therefore  
attributed that endmember to deep weathering in water interacting with the underlying bedrock. The composition of  
the deep weathering endmember shows a strong correlation between [Mg<sup>2+</sup>]/[SO<sub>4</sub><sup>2-</sup>] and [K<sup>+</sup>]/[SO<sub>4</sub><sup>2-</sup>]. These  
compositions are similar to previous observations of weathering of metasedimentary rock piles where silicates  
(biotite and chlorite) are the first minerals to dissolve when sulfides oxidize (Moncur et al., 2009). Specifically,  
biotite (K(Si<sub>3</sub>Al)Mg<sub>2</sub>FeO<sub>10</sub>(OH)<sub>2</sub>) is known to release Mg<sup>2+</sup> and K<sup>+</sup> while chlorite releases Mg<sup>2+</sup> upon weathering.  
350 Moreover, the metamorphic conditions that produce pyrrhotite also produce biotite and chlorite, and those three  
minerals tend to be located together in schist foliations (Carpenter, 1974). Pyrrhotite oxidation at Hubbard Brook  
apparently causes dissolution of biotite ± chlorite because these are the most susceptible minerals in close proximity  
to the sulfide. Thus, several lines of evidence underlie our interpretation that component 3 is the deep weathering  
source of sulfate.

355 As summarized in Table 1, pyrrhotite can account for 29% of the total sulfate flux at Hubbard Brook. The  
schist and till contain essentially no carbonate; therefore, weathering is always a net sink for CO<sub>2</sub>. In this watershed,  
however, the story is complicated by the sulfuric acid from pyrrhotite oxidation and acid rain that dissolves silicate  
minerals. If we had assumed all of the base cations detected in Hubbard Brook were caused by CO<sub>2</sub>-weathering, we  
would have overestimated the net drawdown of CO<sub>2</sub> out of the atmosphere (Fig. 1). NMF deconvolutes this signal.

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**Figure 5.** Concentration of total sulfate (gray) and sulfide-derived sulfate (NMF-derived; yellow) in stream water plotted versus time at Shale Hills (A), East River (B), and Hubbard Brook (W-3 sub-catchment) (C). Shale Hills and East River are net neutral, while Hubbard Brook is a net sink ( $\kappa_{\text{stream}} < 0$ ) over the timescales studied, as shown by the  $\text{CO}_2$  sequestration coefficient ( $\kappa_{\text{stream}}$ ) for Shale Hills (D), East River, (E), and Hubbard Brook (F). The range (mean + 1s.d.) indicated in green to the right of D, E, and F represent  $\kappa_{\text{rock}}$ , the time integrated  $\text{CO}_2$  sequestration coefficient calculated from the rock chemistry (see text). At Shale Hills and Hubbard Brook, the discharge-weighted average  $\kappa_{\text{stream}}$  ( $\kappa_{\text{stream,Avg}}$ ; dashed red line) is larger than the average  $\kappa_{\text{rock}}$  because of acid rain, while at East River  $\kappa_{\text{stream}}$  is largely consistent with  $\kappa_{\text{rock}}$  during most of the year. The red shading on D, E, and F represents 1 s.d. from  $\kappa_{\text{stream,Avg}}$ . The long record at Hubbard Brook shows that  $\kappa_{\text{stream}}$  is approaching  $\kappa_{\text{rock}}$  as the watershed recovers from acid rain. Gaps in the time series for Shale Hills occur when the autosampler tubing or stream froze.

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### 3.6 Predicting $\text{CO}_2$ release or drawdown from rock chemistry

From the stream chemistry, we found that Shale Hills and East River are net neutral with respect to  $\text{CO}_2$ , and Hubbard Brook is a net sink (Table 1; Figure 5). In Table 1, the weathering fluxes are simply summarized as  $\text{CO}_2$  fluxes (see SM section 2.2), but the NMF results can also be used to calculate weathering losses for each mineral or for sulfate-driven weathering as described in SM 2.5 (Table S5). Although we do not explicitly discuss each of these additional fluxes learned from NMF, we note that the fluxes have resulted in losses of minerals from protolith as soil formed over time and we can use soil chemistry therefore as an additional test of  $\kappa_{\text{stream}}$ : specifically, we compare  $\kappa_{\text{stream}}$  to the  $\text{CO}_2$  flux recorded in the weathered profile as solid-phase chemistry. To do this, we calculate a  $\text{CO}_2$  sequestration coefficient analogous to  $\kappa_{\text{stream}}$  but instead based on rock chemistry,  $\kappa_{\text{rock}}$ , by assessing soil and taking

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into account the fraction of base cations weathered, the fraction of base cations from carbonates, and the capacity of the bedrock to produce  $\text{H}_2\text{SO}_4$ :

$$\kappa_{rock} = \frac{1}{2}(\tau + \gamma_{rock} + \zeta_{rock}), \quad (3)$$

Here,  $\kappa_{rock}$  is the time-integrated  $\text{CO}_2$  sequestration coefficient determined from the solid phase weathering products in units of meq  $\text{CO}_2$ /meq base cation,  $\tau$  is the mass transfer coefficient for base cations at the land surface (where  $1-\tau$  equals the fraction of cations present in original parent rock that remain in topsoil at land surface),  $\gamma_{rock}$  is the proportion of base cations in the bedrock associated with carbonate minerals, and  $\zeta_{rock}$  is the acid generation capacity of the rock. The derivation of eq. 3 and description of each variable is more fully summarized in SM section 2.3. Briefly,  $\gamma_{rock}$  expresses the proportion of base cations in the parent rock that are associated with carbonate minerals (varies from 0 to 1 for 100% silicate protolith to 100% carbonate protolith).  $\zeta_{rock}$  expresses the relative amount of (acid-generating) pyrite to base cations in the rock (varies from 0 to 1.5 for catchments where 100% of weathering is  $\text{CO}_2$ -driven to catchments where 100% of weathering is  $\text{H}_2\text{SO}_4$ -driven, respectively).  $\tau$  expresses the fraction of cations that have not dissolved away upon exposure at the land surface (varies from -1 to 0 for 0% cations remaining at land surface to 100% cations remaining, respectively). Negative  $\kappa_{rock}$  is a lithology that has been net sequestering  $\text{CO}_2$  over the duration of weathering, whereas positive  $\kappa_{rock}$  has been net releasing  $\text{CO}_2$ . Based on the chemistry of the bedrock and topsoil at each watershed,  $\kappa_{rock}$  is  $-0.08 \pm 0.11$ ,  $0.08 \pm 0.17$ , and  $-0.19 \pm 0.11$  for Shale Hills, East River, and Hubbard Brook, respectively (Tables 1, S3). Based on these values from observations of the solid weathering phases, Shale Hills and East River on net are  $\text{CO}_2$  neutral (i.e., within error of 0), but Hubbard Brook has acted as a long-term  $\text{CO}_2$  sink.

If the streams at each site today are acting just like the weathering recorded over the last tens of thousands of years in the solid-phase material,  $\kappa_{rock}$  should equal  $\kappa_{stream}$ . Here, we find that  $\kappa_{stream}$  (discharge-weighted average) for Shale Hills, East River, and Hubbard Brook are  $0.01 \pm 0.03$ ,  $-0.03 \pm 0.11$ , and  $-0.14 \pm 0.06$  respectively (Table 1). In Figure 5 we compare  $\kappa_{stream}$  for each sample to  $\kappa_{rock}$ , i.e., the time-integrated  $\text{CO}_2$  (sequestered or released) per base cation in the parent rock. For all sites, the stream chemistry shows similar values of  $\text{CO}_2$  sequestration coefficient for the modern (stream timescale) compared to the time-integrated (soil timescale), i.e.,  $\kappa_{stream} \approx \kappa_{rock}$ , consistent with Shale Hills and East River acting as  $\text{CO}_2$  net neutral but Hubbard Brook as a  $\text{CO}_2$  sink. In addition, at Hubbard Brook, it can be seen that acid rain has competed with  $\text{CO}_2$  in weathering minerals, lowering the capacity of the rock to sequester atmospheric  $\text{CO}_2$ , only moving back to equivalency between the rock and stream record in recent years (2013-2016; Fig. 5F) as the system recovers from acid rain.

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#### 4 Conclusions

By not requiring a priori assignments of endmembers, a new machine learning technique not only successfully reproduced source apportionments made in more traditional endmember analysis for streams, but it also revealed new information about how watersheds work. At the same time, the method also solved some issues related to source apportionment for streams with time variations of large acid rain inputs. The approach documented that two

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carbonate-containing shale watersheds (Shale Hills, East River) act intermittently as sources or sinks of CO<sub>2</sub> to the atmosphere but on net are neutral with respect to CO<sub>2</sub>. In contrast, because it has no carbonate minerals, Hubbard Brook is a constant sink for CO<sub>2</sub> (Fig. 5). These observations were compared and confirmed by comparing stream chemistry to rock chemistry.

420 NMF also emphasized the importance of different water flowpaths in determining endmembers: the endmembers were not strictly defined by mineralogy but by patterns of subsurface flow. These flowpaths lead to patterns in stream water chemistry that were easily deciphered by our newly developed machine learning-based mixing model. In particular, for three streams, signals in the chemical variations were observed to reveal dissolution of the most reactive mineral in proximity to sulfide oxidation. Many watersheds have flowpaths distinguished by  
425 geochemical signatures from mineral reactions (Brantley et al., 2017) but we do not know these paths a priori when we investigate stream chemistry. Machine learning will be useful to model mineral reactions on broader spatial scales and will help constrain global weathering-related CO<sub>2</sub> dynamics because it can delineate endmembers without a priori assumptions.

Beyond these attributes, the machine learning approach also revealed other new attributes of weathering. In  
430 Shale Hills, we discovered that sulfate inputs from acid rain are not exported completely for two decades, which impacts mass balance and weathering-related CO<sub>2</sub> dynamics. Although not discussed explicitly here, this decadal time-lag was also observed at Hubbard Brook. NMF also showed that Hubbard Brook, recovering from the impacts of acid rain, is only recently returning to its full potential as a CO<sub>2</sub>-sequestering rock system. In other words, prior to acid rain, Hubbard Brook sequestered more CO<sub>2</sub> per mole of weathered bedrock than it does today. But acid rain  
435 dissolved some of the silicates with H<sub>2</sub>SO<sub>4</sub>, lowering the CO<sub>2</sub> sequestration capability of the watershed. NMF led us to discover this new attribute of acid rain, namely that it diminishes the capacity of a rock to sequester CO<sub>2</sub> at millennial timescales (Figure 1) by replacement of CO<sub>2</sub> by H<sub>2</sub>SO<sub>4</sub> as a weathering agent. Regardless of the net CO<sub>2</sub> dynamic, we discovered that without considering sulfide oxidation or acid rain, the CO<sub>2</sub> weathering sink considered over millennial timescales is always overestimated.

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### Data Availability

Data used in analysis for this work can be found at the Susquehanna Shale Hills Critical Zone website

455 (<https://criticalzone.org/shale-hills/data>), the Hubbard Brook data catalog (<https://hubbardbrook.org/d/hubbard-brook-data-catalog>), and in Wan et al. (2019) and in Winnick et al. (2017). Codes used in the modeling are available upon request.

### Author Contributions

460 SLB, TW, and ARS conceived the project. TW and ARS developed the codes for the model. SLB, XG, and ARS interpreted the data and model outputs. All authors contributed in the preparation of the manuscript.

### Competing Interests

The authors declare that they have no conflict of interest.

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