



1	New isotope-based evapotranspiration partitioning method using the Keeling plot slope and direct-								
2	measured parameters								
3	Yusen Yuan ^{<i>a,b</i>} , Lixin Wang ^{<i>b</i>} *, Wenqing Lin ^{<i>a</i>} , Wenzhe Jiao ^{<i>b</i>} , Taisheng Du ^{<i>a</i>} *								
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5 6	^a Center for Agricultural Water Research in China, China Agricultural University, Beijing 100083, China								
7 8 9	^b Department of Earth Sciences, Indiana University–Purdue University Indianapolis, Indianapolis, Indiana 46202, USA								
10 11 12 13	* Corresponding author: Dr. Lixin Wang Fax: +1-1-317-274-7966; Tel: +1-317-274-7764 Email: lxwang@iupui.edu								
14 15 16 17	* Corresponding author: Dr. Taisheng Du Fax: +86-10-62737611; Tel: +86-10-62738398 Email: dutaisheng@cau.edu.cn								
18	Highlights:								
20 21 22 23 24 25 26	 A new method was developed to estimate the evapotranspiration partition using isotopes. Theoretical derivations were provided for the new method. Linear regression showed strong agreement between the new method and the traditional method. The new method eliminates high sensitivity contribution parameter δ_{ET}, and avoids the extrapolation of Keeling plot. 								
27									





28 Abstract

29	To better quantify water and energy cycles, numerous efforts to partition evapotranspiration (ET)
30	into evaporation (E) and transpiration (T) have been made over the recent half century. Various methods
31	such as direct measurements, analytical models and satellite-based estimations have been used to separate
32	ET across the field scale to the global scale. One of the analytical methods, isotopic approach, has been
33	often applied in terrestrial ecosystem ET partitioning. The isotopic composition of ET (δ_{ET}) is a crucial
34	parameter in the traditional isotope-based ET partition model, which however has considerable uncertainty.
35	Here we proposed a new method relying on Keeling plot slope (k), and relying on the direct measurements
36	of atmospheric vapor concentration (C_v) and isotopic composition of atmospheric vapor (δ_v), to avoid the
37	direct use of $\delta_{\text{ET}}.$ Mathematical derivation of the new method was provided, and field observations were
38	used to evaluate the new method. The T/ET results based on the new method agreed well with those using
39	the traditional isotopic method. The new method eliminates the high sensitivity contribution parameter $\delta_{\text{ET}}.$
40	In addition, the new method utilized directly measured values and regressive slope of Keeling plot instead
41	of using the interpolated Keeling plot intercept. Our study shows an analytical framework to estimate T/ET
42	based on the Keeling plot slope and direct-measured parameters. The new method potentially reduces the
43	uncertainty of isotope-based ET partition approach.
44	
45	Key words: ecohydrology, evaporation, evapotranspiration, Keeling plot, stable isotope; transpiration





54 1. Introduction

55 Evapotranspiration (ET) links water, energy, and carbon cycles on land surface (Jung et al., 2010), 56 consisting of evaporation (E) from soil (Sprenger et al., 2016) and open water (Gat et al., 1994), and 57 transpiration (T) from plants (Wang et al., 2012a; Wang et al., 2014). The processes and biological controls 58 of E and T are largely different: T is associated with physiological and biochemical reaction during plant 59 carbon sequestration, while E does not directly attribute to gross primary production and it is not directly 60 affected by biological processes (Scott et al., 2006; Wang et al., 2018; De Deurwaerder et al., 2020). Thus, 61 accurate quantification of T fraction in total ET is of great importance to understand water use efficiency 62 (WUE) from the canopy to the ecosystem scales (Zhou et al., 2014; Zhou et al., 2016). Besides, 63 implementing ET partition improves the comprehending of ecohydrological process, therefore benefits our 64 ability to quantify biological feedbacks on the hydrologic cycle (Newman et al., 2006). Moreover, ET and 65 its components have been used to interpret the vegetation control on ET (Wang et al., 2014) and surface 66 soil moisture control on ET (Cui et al., 2020), as well as to identify some inaccurate estimation of vegetation 67 and soil parameters in global climate model (GCM) (Lawrence et al., 2007; Peñuelas and Filella, 2009). 68 Therefore, ET partition is an important research topic in ecohydrological studies.

69 The attempt to separation E and T began at least in the 1970s (Ritchie, 1972), which initially rely on 70 direct measurements using micro-lysimeter measurements for E (Walker, 1984) and sap flow measurements 71 for T (Swanson and Whitfield, 1981). After Shuttleworth and Wallace (1985) first published ET partition 72 model, numerous analytical models including energy and water balance (ENWATBAL) model (Lascano et 73 al., 1987), soil water energy and transpiration (SWEAT) model (Daamen and Simmonds, 1996), two-source 74 energy balance (TSEB) model (Norman et al., 1995), FAO dual-Kc model (Allen et al., 1998) and isotope 75 model (Yepez et al., 2003) were developed to determine F_T at plot or field scales. Meanwhile, satellite-76 based estimations made it possible to determine F_T at regional or global scale (Wei et al., 2017; Martens et 77 al., 2017).

78

Hydrogen and oxygen isotopes are natural components of the hydrological cycle. E and T result in





79 different isotopic compositions due to the different isotopic fractionation process (Yepez et al., 2003). Using 80 the isotopic compositions of various ET components, the isotopic approach to estimate F_T has been widely 81 used in woodlands (Sun et al., 2014), grasslands (Cui et al., 2020), croplands (Wen et al., 2016; Lu et al., 82 2017), and drylands (Sun et al., 2019) ecosystems. Using the isotopic composition of E (δ_E), T (δ_T), and ET 83 (δ_{ET}) , F_T can be calculated theoretically based on mass balance (Yakir and Wang, 1996; Yakir and Sternberg, 84 2000). However, previous studies suggested δ_E , δ_T and δ_{ET} estimates are subject to large errors (Xiao et al., 85 2018), resulting in either over (Sutanto et al., 2012) or under (Wu et al., 2017) F_T estimations compared 86 with direct measurements and other analytical models. According to model sensitivity analysis, the errors 87 of δ_{ET} attributed the most to the potential errors in F_T (Cui et al., 2020). As a result, accurate quantification 88 of δ_{ET} is most crucial to obtain accurate F_T estimate using the isotopic approach.

89 Generally, δ_{ET} is estimated by Keeling plot method (Keeling, 1958; Yakir and Sternberg, 2000), flux-90 gradient method (Lee et al., 2007) and eddy covariance isotopic flux method (Griffis et al., 2008; Griffis et 91 al., 2010). However, disadvantages remain for all these three methods. Variation in the isotopic composition 92 of atmosphere vapor (δ_v) may be influenced by air masses advection rather than by ET (Lee et al., 2006), 93 which lead to less reliable δ_{ET} estimates using Keeling plot method over a long time period (Good et al., 94 2012). The representativeness of two heights in flux-gradient method is questionable (Good et al., 2012), 95 as the eddy diffusivity parameter may not be constant at the bottom of the boundary layer where vegetation 96 interacts with turbulent airflow, leading to variable vertical meteorological conditions (Monin and Obukhov, 97 1954). Eddy covariance isotopic flux method may induce many uncertainties when estimating the 98 covariance between isotopic ratios and vertical wind speed, as the information lost in the measured factors 99 (Good et al., 2012). In some case, the δ_{ET} may be underestimated by more than 20% for hydrogen, no matter 100 which method to be adopted (Good et al., 2012; Cui et al., 2020). Inevitably, reducing the uncertainty of 101 δ_{ET} estimate is critically needed.

102 In this paper, we proposed a new method to estimate F_T using a modified isotopic approach without 103 the need of δ_{ET} parameter. This new method relies on the identical instrumental setting for the classical 104 Keeling plot investigations. A detailed derivation of the new method was provided, and the new method





- 105 was evaluated by comparing the new method with traditional method using field observations. To further
- 106 assess the new method, a global sensitivity analysis was also conducted for model parameter evaluation.

107

- 108 2. Materials and Methods
- 109 2.1 Isotope-based ET partition methods
- 110 2.1.1 Traditional method
- 111 Traditionally, by measuring δ_{E} , δ_{T} and δ_{ET} , applying a two-source mixing model, F_{T} based on δ_{ET} 112 ($F_{T}(\delta_{ET})$ method) can be determined as

113
$$F_T(\delta_{ET}) = \frac{T}{ET} = \frac{\delta_{ET} - \delta_E}{\delta_T - \delta_E} , \qquad (1)$$

The relationships of δ_E and δ_T were demonstrated by an imaginary graph in **Fig. 1**, which was first proposed by Moreira et al. (1997). Line 1 is idealized Keeling plot line resulting from absolute evaporation, and line 2 is that of absolute transpiration. The dashed area between line1 and line 2 typifies all feasible Keeling plot lines mixed with E and T (i.e., ET). The intersection point of line 1 and line 2 indicated the source of ambient vapor. In other words, the y-axis of the intersection point stands for the isotopic composition of ambient vapor (δ_a), and the x-axis of the intersection point stands for the inverse of ambient water vapor concentration (1/C_a).

121 The Keeling plot method is often applied to simulate δ_{ET} (Keeling, 1958; Yakir and Sternberg, 2000). 122 Measured values and simulated values can be connected using an isotopic two-source mixture equation:

123
$$\delta_{\nu} = \frac{C_a(\delta_a - \delta_{ET})}{C_{\nu}} + \delta_{ET} , \qquad (2)$$

where C_a and C_v are the corresponding concentrations of ambient water vapor and directly measured atmospheric water vapor (i.e., the mixture of ambient water vapor and ET). For a given time, with multiple measurements of C_{vi} and δ_{vi} (the single measurement of the vapor concentration and isotopic composition of water vapor, respectively) collected at various heights during one observation period, the intercept δ_{ET} for this moment from ordinary least squares (OLS) of $1/C_{vi}$ and δ_{vi} is able to be estimated (Zhang et al.,





129 2011). Therefore, during one observation period, $\delta_v = \frac{1}{m} \sum_{i=1}^m \delta_{v_i}$ and $\frac{1}{c_v} = \frac{1}{m} \sum_{i=1}^m \frac{1}{c_{v_i}}$, where m is the

number of the single measurements (
$$\delta_{vi}$$
, 1/C_{vi}) used in Keeling plot relationship. The slope (k) of the linear

- 131 Keeling plot is defined as $k=C_a(\delta_a \delta_{ET})$.
- 132 δ_E is often calculated using the Craig–Gordon model (Craig and Gordon, 1965), which considering
- 133 both equilibrium fractionation and kinetic fractionation, and considering the diffusion of water vapor from
- 134 soil surface to the mixed boundary layer:

~

135
$$\delta_E = \frac{\frac{\delta_s}{\alpha} - h\delta_v - \varepsilon^* - (1 - h)\varepsilon_k}{(1 - h) + (1 - h)\frac{\varepsilon_K}{1000}},$$
(3)

where h is relative humidity, δ_s is the isotopic composition of soil liquid water at the evaporating front (0– 5 cm), ϵ^* and α are both the equilibrium fractionation factor from liquid water to vapor, which connected by the equation $\epsilon^*=1000(1-1/\alpha)$. α is estimated by Eq. (4) with soil temperature (T) (Majoube, 1971). The kinetic fractionation factor (ϵ_k) is specified by Eq. (5) (Gat, 1996; Wei et al., 2015).

140
$$\alpha(^{18}O) = \frac{1}{1000} \left(1.137 \times \frac{10^6}{T^2 - 0.4156 \times \frac{10^3}{T - 2.0667}} \right) + 1 , \qquad (4)$$

141
$$\varepsilon_k = n\left(1 - \frac{D_i}{D}\right) \times 10^3$$
, (5)

where n is isotopic enrichment factor of liquid water during evaporation with a value between 0.5 and 1 (Allison et al., 1985; Gat, 1996). We used a value of 0.67 for the farmland here, similar to what was used in Wei et al. (2015). D_i/D is the ratio of ${}^{1}H_{2}{}^{18}O$ molecular diffusion coefficients ratio of water vapor in dry air, with a value of 0.9691 for ${}^{18}O$ (Cappa et al., 2003).

146 δ_{T} can also be estimated by chamber method based on Keeling plots (Wang et al., 2010). Following 147 the basic gas exchange principle (Von Caemmerer and Farquhar, 1981; Song et al., 2015a), the chamber 148 method was further developed to measured δ_{T} directly as follows (Wang et al., 2012b):

149
$$\delta_T = \frac{C_m \delta_m - C_v \delta_v}{C_m - C_v} \quad , \tag{6}$$





- 150 where C_m and δ_m was the concentration and isotopic composition of the mixed vapor, respectively, which
- 151 is consisted of the vapor from ET and from the ambient atmosphere.
- 152 2.1.2 New ET partition method
- 153 In this study, we focus on the relationship between k and F_T . A simplified triangle graph was made
- 154 (Fig. 2) according to Fig. 1. $(1/C_x, \delta_x)$ is a random point on the Keeling plot. x, y and z represent the length
- 155 of the line segment ($\delta_{\rm T}$ $\delta_{\rm ET}$), the line segment ($\delta_{\rm ET}$ $\delta_{\rm E}$) and the line segment ($\delta_{\rm ET}$ $\delta_{\rm x}$), respectively, and
- 156 α , β and γ represent the intersectional angle of the line segment ($\delta_T \delta_{ET}$) and the line segment ($\delta_T \delta_x$), the
- 157 line segment (δ_{ET} - δ_E) and the line segment ($\delta_E \delta_x$) and the line segment (δ_{ET} - δ_E) and the line segment
- 158 $(\delta_{ET} \delta_x)$, respectively. Based on the law of sines, we have:

159
$$\frac{\sin(\gamma - \alpha)}{x} = \frac{\sin \alpha}{z} , \qquad (7)$$

160
$$\frac{\sin(\pi - \gamma - \beta)}{y} = \frac{\sin\beta}{z} .$$
 (8)

161 When combining Eq (7) and Eq (8), we will come up:

162
$$\frac{x}{y} = \frac{\sin(\gamma - \alpha)\sin\beta}{\sin(\gamma + \beta)\sin\alpha}$$
 (9)

163 Equation (9) can be transformed as:

164
$$\frac{x}{y} = \frac{\sin\beta\cos\alpha\sin\gamma - \sin\beta\sin\alpha\cos\gamma}{\sin\alpha\sin\beta\cos\gamma + \sin\alpha\cos\beta\sin\gamma}$$

165
$$= \frac{-\sin\alpha\sin\beta\cot\gamma - \sin\alpha\cos\beta + \sin\alpha\cos\beta + \sin\beta\cos\alpha}{\sin\alpha\sin\beta\cot\gamma + \sin\alpha\cos\beta}$$

166
$$= \frac{\sin(\alpha + \beta)}{\sin \alpha} \frac{1}{\sin \beta \cot \gamma + \cos \beta} - 1 , \qquad (10)$$

As k is the tangent value of the angle of Keeling plot line and x-axis positive direction, it is the minus tangent value of the angle of Keeling plot line and x-axis negative direction according to supplementary angles' property. As the angle of Keeling plot line and x-axis negative direction and angle γ are complementary angles, we have the relationship that k = - cot γ . When combining Eq (1) and Eq (10), we will get:





172
$$F_T = \frac{\delta_{ET} - \delta_E}{\delta_T - \delta_E} = \frac{y}{x + y} = \frac{1}{1 + \frac{x}{y}} = -\frac{\sin\alpha\sin\beta}{\sin(\alpha + \beta)}k + \frac{\sin\alpha\cos\beta}{\sin(\alpha + \beta)}, \quad (11)$$

173 where

174
$$\frac{\sin\alpha\sin\beta}{\sin(\alpha+\beta)} = \frac{1}{\frac{\sin\alpha\cos\beta + \cos\alpha\sin\beta}{\sin\alpha\sin\beta}} = \frac{1}{\cot\alpha + \cot\beta} = \frac{1}{C_x(\delta_T - \delta_E)} ,$$
(12)

175
$$\frac{\sin\alpha\cos\beta}{\sin(\alpha+\beta)} = \frac{\sin\alpha\cos\beta}{\sin\alpha\cos\beta + \sin\beta\cos\alpha} = \frac{1}{1 + \frac{\tan\beta}{\tan\alpha}} = \frac{\delta_x - \delta_E}{\delta_T - \delta_E} , \qquad (13)$$

176 As a result, F_T is able to be formed theoretically as

177
$$F_T(\delta_x) = -\frac{1}{C_x(\delta_T - \delta_E)}k + \frac{\delta_x - \delta_E}{\delta_T - \delta_E} , \qquad (14)$$

Because Keeling plot is based on the OLS using all the individual data points $(1/C_{vi}, \delta_{vi})$, the regression line passes through the mean values of the $1/C_{vi}$ $(1/C_v)$ and δ_{vi} (δ_v) based on the properties of the OLS line (Hogg et al., 2005). That is to say the mean values of $(1/C_v, \delta_v)$ during any observation period must locate on the Keeling plot line. As such, Eq. (14) can be expressed as the following form ((F_T(δ_v) method) during any observation period:

183
$$F_T(\delta_v) = -\frac{1}{C_v(\delta_T - \delta_E)}k + \frac{\delta_v - \delta_E}{\delta_T - \delta_E}$$
(15)

184 2.2 Field Evaluation

185 2.2.1 Experimental Site

Field Evaluation was conducted in Shiyanghe Experimental Station of China Agricultural University. It is located in Wuwei, Gansu Province, northwestern China (37°85'20"N, 102°85'10"E; altitude 1581m). The new method was tested in a maize field. The average yearly sunshine duration is more than 3,000 hours, and long-term average yearly temperature is around 8 °C. The region is suffered from water shortage. The groundwater table is more than 30m below the surface. The average yearly evaporation of 2,000 mm (from free water surfaces) against with average yearly precipitation of 164 mm perennially. The soil texture in the experimental site is loamy and sandy loam, with the field capacity of about 0.28 cm³ cm⁻³.





193 2.2.2 Field Experiment

194 Maize was sowed with row length of 40 cm and column width of 26 cm on 20 April in both 2017 195 and 2018, and harvested on 15 September in both 2017 and 2018. The total area was about 39 hectare, and 196 plant density was around 76,000 plants of maize per hectare. Maize is the primary crop cultivated in the 197 surrounding area. The soil temperature was monitored at 5cm depth. Relative humidity was measured at 2-198 meter-height with 10-min intervals. 199 The sampling of vapor (atmospheric vapor and mixed vapor) and soil water were conducted from 200 June to August 2017 and 2018 (sampling time points are shown in **Table 1**, which is specified hereinafter). 201 Vapor was collected by four gas traps, and was measured using a water vapor isotope analyzer (L2130-i, Picarro Inc., Sunnyvale, CA, USA) from 7:00 am to 7:00 pm with two hours interval. No.1-No.3 traps were 202 203 placed at just above the canopy, 2 m and 3 m respectively, which was used to collect the vapor of atmosphere 204 at different heights. While No.4 gas trap was used to collect the mixed vapor. To guarantee a thorough mix 205 of transpired vapor and ambient vapor, a long-term-operated van was fixed embedded of the chamber, 206 which followed the devise of Song et al. (2015b). The mixed vapor was derived from dynamic plant 207 chamber measurements (Fig. 3) at a flow rate of 500–1500cm³ min⁻¹. The structure of the chamber was 208 corresponding to the design of Pape et al. (2009). The theoretical basis of this design mainly follows the 209 gas exchange principles invited by Wang et al. (2012b). At each observation time point (last for 15 mins), 210 four times of independent measurements were taken corresponding to No.1-No. 4 sampling inlets. One 211 independent measurement lasted for 225 s. The switch process between two independent measurements 212 were self-acting. Since the analyzer record data every 0.9-1s, about 259-264 values for each inlet was 213 recorded within the circulation. For each 225 s measurement period, No. 195 to No. 253 data points were 214 selected to avoid residual issue and effect of transient pressure variation. As a result, 177 data points were used as $(1/C_{vi}, \delta_{vi})$ from No.1–No.3 traps, and the average values of 59 data points were used as C_m and δ_m 215 respectively from No. 4 gas trap. Vapor specifications ensure the precision of a measurement ranging from 216 1,000 to 50,000 ppm, the precision is 0.040^{\omega}-0.25^{\omega} for δ^{18} O (Zhao et al., 2019). Our vapor calibration 217

218 procedure was mainly corresponding to the study by Yuan et al. (2020). The volumes of the chamber was





40x60x180 cm³, which was made of acrylic glass. Artificial holes in the minor acrylic glass frame allow the device of inlet and outlet porthole. The soil samples were drilled by a soil auger at the depths of 0–5 cm. Pure soil liquid water was extracted by a cryogenic vacuum extraction system (LI-2000, LICA United Technology, China), and the extraction method is guided by Orlowski et al. (2013). The δ_s values were measured by the same isotope analyzer (L2130-i, Picarro Inc., Sunnyvale, CA, USA) in liquid water model. δ_s calibration process mainly obeyed the study by Wu et al. (2017). The isotopic compositions values relative to the Standard Mean Ocean Water (SMOW).

As our water vapor isotope analyzer was occupied due to maintenance and other experiments, twelve days were chosen to conduct ET partition observation. In each day, the observation started at 7:00 am and end up with 7:00 pm, conducting in 2 hours interval. Overall, we have 84 experimental data sets (**Table 1**). A quantity control filter was used on $F_T(\delta_{ET})$ and $F_T(\delta_v)$, which excluded the values beyond the range (0,1).

230 2.2.3 Global Sensitivity Analysis

231 A global sensitivity analysis was conducted for both two methods to determine the influence of a set 232 of parameters had on predicting $F_T(\delta_{ET})$ and $F_T(\delta_v)$. A Sobol-method-based (Zhang et al., 2015) software, 233 Crystal Ball (Oracle Inc., Redwood City, CA), was used to quantify the contribution of each input parameter 234 to the change of modeling results. The parameter interactions were considered in this approach. Running 235 the software, a Monte Carlo simulation (Bhat and Kumar, 2008) was implemented to supply random 236 variation data trials within the observed range. In the simulation, 10,000 trials were operated for each 237 parameter in both $F_T(\delta_{ET})$ method and $F_T(\delta_v)$ method, as well as 10,000 times subsampling input for each 238 parameter, represented by their mean values and standard deviations among all of the observation time points under an assumed normal distribution (Cui et al., 2020). After analyzing the pattern of these 10,000 239 240 trials of data derived from Monte Carlo simulation, a distribution of predicted $F_T(\delta_{ET})$ and $F_T(\delta_v)$ was able 241 to be shown. In this study, the mean standard deviation of predicted $F_T(\delta_{ET})$ and $F_T(\delta_v)$ was 0.02 both. Finally, 242 the software produced the contribution of each input parameter to the variability of results. The greater of 243 the percentage value, the more sensitive a model output variable is to that particular parameter.





244 **3. Results and Discussion**

245	3.1 Comparisons of the new method with the traditional method
246	Among all observation time points, the average δ_{ET} , δ_T , δ_E , δ_v and C_v values are -11.79±2.34‰, -8.50
247	±1.98‰, -28.75±6.96‰, -13.47±2.00‰ and 19284.02±5281.09 ppm, respectively (Table 1). After the
248	quality control (see section 2.2.2) to exclude the F_T values outside the range (0, 1), 94.0% and 96.4% of
249	$F_T(\delta_{ET})$ and $F_T(\delta_v)$ values remain. Finally, 79 data points overlapped between $F_T(\delta_{ET})$ and $F_T(\delta_v)$ methods.
250	The average $F_T(\delta_{ET})$ and $F_T(\delta_v)$ across all time points were 0.81±0.10 and 0.82±0.12. The F_T results from
251	the new method agreed well with the results using the traditional method (Fig. 4), which supports the
252	validity of the mathematical derivation of the new method using field observations.
253	3.2 The advantages of the new method compared with the traditional method
254	3.2.1 The elimination of high sensitivity contribution parameter δ_{ET}
255	Global sensitivity analysis was conducted for both $F_T(\delta_{ET})$ method (Fig. 5a) and $F_T(\delta_v)$ method (Fig.
256	5b). As for the traditional method, δ_{ET} contributed to 59% of the sensitivity of F_T , significantly larger than
257	those of δ_T and δ_E . The high sensitivity contribution of parameter δ_{ET} was also reported by a previous study
258	(Cui et al., 2020). Generally, great uncertainty of δ_{ET} was revealed in Keeling plot method, flux-gradient
259	method and eddy covariance isotopic flux method (Good et al., 2012), which resulted in large F_T uncertainty
260	when δ_{ET} was used in the traditional method on the basis of sensitivity analysis in our study and others'
261	research (Cui et al., 2020). While in the new method, the parameter with the largest sensitivity contribution
262	was k (46%). This result indicated that Keeling-plot-related parameters (δ_{ET} and k) brought most of the
263	uncertainty to estimate $F_{T}.$ At the same time, using k rather than δ_{ET} would diminish the uncertainty result
264	from Keeling plot since k can be directly calculated using observations without the need of extrapolation
265	to obtain the intercept $\delta_{\text{ET}}.$ The second largest sensitivity contribution in the new method was δ_v (27%), a
266	direct measured parameter instead of a simulated value in the traditional method. Meanwhile, the sensitivity
267	contributions of parameter δ_E and δ_T were reduced using the new method (7% and 18%) compared with the
268	traditional method (12% and 29%). It was thus favorable for $F_T(\delta_v)$ method for using a direct measured





- 269 parameter δ_v , and it will reduce the uncertainty of F_T .
- 270 3.2.2 The new method avoids extrapolation of Keeling plot

271 One of the limitations of the Keeling plot is that it requires extrapolation far beyond the measured 272 range of data points to the y-axis to obtain the intercept δ_{ET} (Pataki et al., 2003). Geometrically, data points 273 $(1/C_{vi}, \delta_{vi})$ are always assembled in a restricted area, which is distant to the potential intercept point of the 274 Keeling plot. In some cases, the extrapolation distance will be 8-10 times of original $1/C_{vi}$ range (Quade et 275 al., 2018), such that small uncertainties in the OLS regression slope result in large uncertainties in the 276 intercept δ_{ET} (Tans, 1998). Our result of high sensitivity of δ_{ET} also supports this point. To make matters 277 worse, to meet the assumption of Keeling plot of constant slope and intercept (Wang et al., 2013), one of 278 the principles is to shorten the observation period to obtain data points $(1/C_{vi}, \delta_{vi})$ in a relatively short 279 interval, such as 30 minutes (Good et al., 2012; Xiao et al., 2018). However, short interval data points (1/Cvi, δ_{vi}) may also shorten the $1/C_{vi}$ range, which further increases the extrapolation distance to the y-axis. In 280 281 such cases, it is more dependable to use parameters derived from nearby data point $(1/C_{vi}, \delta_{vi})$ than an 282 interpolated intercept.

283 4. Conclusions

284 In this study, we established a new isotopic based method to quantify $F_T(F_T(\delta_v))$. The $F_T(\delta_v)$ method 285 was derived based on the law of sines. The new method estimated F_T using the modeled parameter k derived 286 from Keeling plot relationship, and direct measured parameters C_v and δ_v . Evaluated by observation data, 287 the linear regression showed the new $F_{T}(\delta_{v})$ method results agreed well with the results from the traditional 288 $F_T(\delta_{ET})$ method. The new method avoids the use of high sensitivity contribution parameter δ_{ET} . A direct 289 measured parameter δ_v in $F_T(\delta_v)$ method would reduce the uncertainty of F_T simulation. Using the 290 parameters derived from direct measurements rather than extrapolation in Keeling plots, the new method 291 should be more dependable. This study provides an analytical framework to estimate F_T using a novel 292 method based on existing Keeling plot instrumentations. The new method potentially reduces the 293 uncertainty of isotope-based ET partition approach.





294 5. Acknowledgements

- 295 We acknowledge support from the National Natural Science Foundation of China (51725904,
- 296 51621061, 51861125103), the National Key Research Program (2016YFC0400207), the Discipline
- 297 Innovative Engineering Plan (111 Program, B14002), the Research Innovation Fund for Graduate Students
- of CAU (2020XYZC39A), and the President's International Research Awards from Indiana University and
- 299 the Division of Earth Sciences of National Science Foundation (EAR-1554894).

300 6. Code and Data Availability

301 Code and data are available on request.

302 7. Author Contribution

- 303 YY, LW and TD conceptualized the main research questions. YY and WL collected the data. YY
- 304 performed the data analyses. YY and LW wrote the first draft. WJ contributed to additional analyses on the
- new method. All the authors contributed ideas and edited the manuscript.
- 306 8. Competing Interests
- 307 There authors declare no competing interests.

308 9. References

- Allen, R. G., Pereira, L. S., Raes, D., and Smith, M.: Crop evapotranspiration-Guidelines for computing crop water requirements-FAO Irrigation and drainage paper 56, **Fao, Rome**, 300, D05109, 1998.
- Allison, G., Gat, J. R., and Leaney, F. W.: The relationship between deuterium and oxygen-18 delta values
 in leaf water, Chemical Geology: Isotope Geoscience Section, 58, 145-156, 1985.
- Bhat, A., and Kumar, A.: Application of the Crystal Ball® software for uncertainty and sensitivity analyses
 for predicted concentration and risk levels, Environmental Progress, 27, 289-294, 2008.
- Cappa, C. D., Hendricks, M. B., DePaolo, D. J., and Cohen, R. C.: Isotopic fractionation of water during
 evaporation, Journal of Geophysical Research: Atmospheres, 108, 4525, 2003.
- Craig, H., and Gordon, L. I.: Deuterium and oxygen 18 variations in the ocean and the marine atmosphere,
 9, 1965.
- Cui, J., Tian, L., Wei, Z., Huntingford, C., Wang, P., Cai, Z., Ma, N., and Wang, L.: Quantifying the controls
 on evapotranspiration partitioning in the highest alpine meadow ecosystem, Water Resources
 Research, 56, e2019WR024815, 2020.
- Daamen, C. C., and Simmonds, L. P.: Measurement of evaporation from bare soil and its estimation using
 surface resistance, Water Resources Research, 32, 1393-1402, 1996.
- De Deurwaerder, H., Visser, M. D., Detto, M., Boeckx, P., Meunier, F., Zhao, L., Wang, L., and Verbeeck,
 H.: Diurnal variation in the isotope composition of plant xylem water biases the depth of root-water
 uptake estimates, **Biogeosciences Discussions**, 1-48, 2020.





- Gat, J. R., Bowser, C. J., and Kendall, C.: The contribution of evaporation from the Great Lakes to the
 continental atmosphere: estimate based on stable isotope data, Geophysical Research Letters, 21,
 557-560, 1994.
- Gat, J. R.: Oxygen and hydrogen isotopes in the hydrologic cycle, Annual Review of Earth and Planetary
 Sciences, 24, 225-262, 1996.
- Good, S. P., Soderberg, K., Wang, L., and Caylor, K. K.: Uncertainties in the assessment of the isotopic
 composition of surface fluxes: A direct comparison of techniques using laser-based water vapor
 isotope analyzers, Journal of Geophysical Research: Atmospheres, 117, D15301, 2012.
- Griffis, T. J., Sargent, S., Baker, J., Lee, X., Tanner, B., Greene, J., Swiatek, E., and Billmark, K.: Direct
 measurement of biosphere-atmosphere isotopic CO₂ exchange using the eddy covariance technique,
 Journal of Geophysical Research: Atmospheres, 113, D08304, 2008.
- Griffis, T. J., Sargent, S., Lee, X., Baker, J., Greene, J., Erickson, M., Zhang, X., Billmark, K., Schultz, N.,
 and Xiao, W.: Determining the oxygen isotope composition of evapotranspiration using eddy
 covariance, Boundary-layer Meteorology, 137, 307-326, 2010.
- 341 Hogg, R. V., McKean, J., and Craig, A. T.: Introduction to mathematical statistics, Pearson Education, 2005.
- Jung, M., Reichstein, M., Ciais, P., Seneviratne, S. I., Sheffield, J., Goulden, M. L., Bonan, G., Cescatti, A.,
 Chen, J., and De Jeu, R.: Recent decline in the global land evapotranspiration trend due to limited
 moisture supply, Nature, 467, 951-954, 2010.
- Keeling, C. D.: The concentration and isotopic abundances of atmospheric carbon dioxide in rural areas,
 Geochimica et Cosmochimica Acta, 13, 322-334, 1958.
- Lascano, R., Van Bavel, C., Hatfield, J., and Upchurch, D.: Energy and Water Balance of a Sparse Crop:
 Simulated and Measured Soil and Crop Evaporation 1, Soil Science Society of America Journal,
 51, 1113-1121, 1987.
- Lawrence, D. M., Thornton, P. E., Oleson, K. W., and Bonan, G. B.: The partitioning of evapotranspiration
 into transpiration, soil evaporation, and canopy evaporation in a GCM: Impacts on land–atmosphere
 interaction, Journal of Hydrometeorology, 8, 862-880, 2007.
- Lee, X., Smith, R., and Williams, J.: Water vapour ¹⁸O/¹⁶O isotope ratio in surface air in New England,
 USA, Tellus B: Chemical and Physical Meteorology, 58, 293-304, 2006.
- Lee, X., Kim, K., and Smith, R.: Temporal variations of the ¹⁸O/¹⁶O signal of the whole canopy transpiration in a temperate forest, **Global Biogeochemical Cycles**, 21, GB3013, 2007.
- Lu, X., Liang, L. L., Wang, L., Jenerette, G. D., McCabe, M. F., and Grantz, D. A.: Partitioning of
 evapotranspiration using a stable isotope technique in an arid and high temperature agricultural
 production system, Agricultural Water Management, 179, 103-109, 2017.
- Majoube, M.: Fractionnement en oxygene 18 et en deuterium entre l'eau et sa vapeur, Journal de Chimie
 Physique, 68, 1423-1436, 1971.
- Martens, B., Gonzalez Miralles, D., Lievens, H., Van Der Schalie, R., De Jeu, R. A., Fernández-Prieto, D.,
 Beck, H. E., Dorigo, W., and Verhoest, N.: GLEAM v3: Satellite-based land evaporation and root zone soil moisture, Geoscientific Model Development, 10, 1903-1925, 2017.
- Monin, A. S., and Obukhov, A. M.: Basic laws of turbulent mixing in the surface layer of the atmosphere,
 Contrib. Geophys. Inst. Acad. Sci. USSR, 151, e187, 1954.
- Moreira, M., Sternberg, L., Martinelli, L., Victoria, R., Barbosa, E., Bonates, L., and Nepstad, D.:
 Contribution of transpiration to forest ambient vapour based on isotopic measurements, Global
 Change Biology, 3, 439-450, 1997.
- Newman, B. D., Wilcox, B. P., Archer, S. R., Breshears, D. D., Dahm, C. N., Duffy, C. J., McDowell, N.
 G., Phillips, F. M., Scanlon, B. R., and Vivoni, E. R.: Ecohydrology of water-limited environments:
- 372 A scientific vision, Water Resources Research, 42, W06302, 2006.
- Norman, J. M., Kustas, W. P., and Humes, K. S.: Source approach for estimating soil and vegetation energy
 fluxes in observations of directional radiometric surface temperature, Agricultural and Forest
 Meteorology, 77, 263-293, 1995.
- 376 Orlowski, N., Frede, H.-G., Brüggemann, N., and Breuer, L.: Validation and application of a cryogenic





- vacuum extraction system for soil and plant water extraction for isotope analysis, Journal of Sensors
 and Sensor Systems, 2, 179-193, 2013.
- Pape, L., Ammann, C., Nyfeler-Brunner, A., Spirig, C., Hens, K., and Meixner, F.: An automated dynamic
 chamber system for surface exchange measurement of non-reactive and reactive trace gases of
 grassland ecosystems, **Biogeosciences**, 6, 405-429, 2009.
- Pataki, D., Ehleringer, J., Flanagan, L., Yakir, D., Bowling, D., Still, C., Buchmann, N., Kaplan, J., and
 Berry, J.: The application and interpretation of Keeling plots in terrestrial carbon cycle research,
 Global Biogeochemical Cycles, 17, 1022, 2003.
- 385 Peñuelas, J., and Filella, I.: Phenology feedbacks on climate change, Science, 324, 887-888, 2009.
- Quade, M., Brüggemann, N., Graf, A., Vanderborght, J., Vereecken, H., and Rothfuss, Y.: Investigation of
 kinetic isotopic fractionation of water during bare soil evaporation, Water Resources Research, 54,
 6909-6928, 2018.
- Ritchie, J. T.: Model for predicting evaporation from a row crop with incomplete cover, Water Resources
 Research, 8, 1204-1213, 1972.
- Scott, R. L., Huxman, T. E., Cable, W. L., and Emmerich, W. E.: Partitioning of evapotranspiration and its relation to carbon dioxide exchange in a Chihuahuan Desert shrubland, Hydrological Processes, 20, 3227-3243, 2006.
- Shuttleworth, W. J., and Wallace, J.: Evaporation from sparse crops an energy combination theory,
 Quarterly Journal of the Royal Meteorological Society, 111, 839-855, 1985.
- Song, X., Loucos, K. E., Simonin, K. A., Farquhar, G. D., and Barbour, M. M.: Measurements of
 transpiration isotopologues and leaf water to assess enrichment models in cotton, New Phytologist,
 206, 637-646, 2015a.
- Song, X., Simonin, K. A., Loucos, K. E., and Barbour, M. M.: Modelling non-steady-state isotope
 enrichment of leaf water in a gas-exchange cuvette environment, Plant, Cell & Environment, 38,
 2618-2628, 2015b.
- Sprenger, M., Leistert, H., Gimbel, K., and Weiler, M.: Illuminating hydrological processes at the soil vegetation-atmosphere interface with water stable isotopes, **Reviews of Geophysics**, 54, 674-704,
 2016.
- Sun, S., Meng, P., Zhang, J., Wan, X., Zheng, N., and He, C.: Partitioning oak woodland evapotranspiration
 in the rocky mountainous area of North China was disturbed by foreign vapor, as estimated based on
 non-steady-state ¹⁸O isotopic composition, Agricultural and Forest Meteorology, 184, 36-47, 2014.
- Sun, X., Wilcox, B. P., and Zou, C. B.: Evapotranspiration partitioning in dryland ecosystems: A global
 meta-analysis of in situ studies, Journal of Hydrology, 576, 123-136, 2019.
- Sutanto, S., Wenninger, J., Coenders-Gerrits, A., and Uhlenbrook, S.: Partitioning of evaporation into
 transpiration, soil evaporation and interception: a comparison between isotope measurements and a
 HYDRUS-1D model, Hydrology and Earth System Sciences, 16, 2605–2616, 2012.
- Swanson, R., and Whitfield, D.: A numerical analysis of heat pulse velocity theory and practice, Journal
 of Experimental Botany, 32, 221-239, 1981.
- Tans, P. P.: Oxygen isotopic equilibrium between carbon dioxide and water in soils, Tellus B, 50, 163-178,
 1998.
- Von Caemmerer, S. V., and Farquhar, G. D.: Some relationships between the biochemistry of photosynthesis
 and the gas exchange of leaves, **Planta**, 153, 376-387, 1981.
- Walker, G.: Evaporation from wet soil surfaces beneath plant canopies, Agricultural and Forest
 Meteorology, 33, 259-264, 1984.
- Wang, L., Caylor, K. K., Villegas, J. C., Barron-Gafford, G. A., Breshears, D. D., and Huxman, T. E.:
 Partitioning evapotranspiration across gradients of woody plant cover: Assessment of a stable isotope
 technique, Geophysical Research Letters, 37, L09401, 2010.
- Wang, L., d'Odorico, P., Evans, J., Eldridge, D., McCabe, M., Caylor, K., and King, E.: Dryland
 ecohydrology and climate change: critical issues and technical advances, Hydrology and Earth
 System Sciences, 16, 2585-2603, 2012a.





427	Wang, L., Good, S. P., Caylor, K. K., and Cernusak, L. A.: Direct quantification of leaf transpiration isotopic
428	composition, Agricultural and Forest Meteorology, 154, 127-155, 2012b.
429	wang, L., Niu, S., Good, S. P., Soderberg, K., McCabe, M. F., Sherry, K. A., Luo, T., Zhou, A., Ala, J., and
430	Caylor, K. K.: The effect of warming on grassland evapotranspiration partitioning using laser-based
431	isotope monitoring techniques, Geochimica et Cosmochimica Acta, 111, 28-38, 2013.
432	Wang, L., Good, S. P., and Caylor, K. K.: Global synthesis of vegetation control on evapotranspiration
433	partitioning, Geophysical Research Letters, 41, 6/53-6/5/, 2014.
434	Wang, P., Li, X. Y., Wang, L., Wu, X., Hu, X., Fan, Y., and Tong, Y.: Divergent evapotranspiration partition
435	dynamics between shrubs and grasses in a shrub-encroached steppe ecosystem, New Phytologist,
436	219, 1325-1337, 2018.
437	Wei, Z., Yoshimura, K., Okazaki, A., Kim, W., Liu, Z., and Yokoi, M.: Partitioning of evapotranspiration
438	using high-frequency water vapor isotopic measurement over a rice paddy field, Water Resources
439	Research , 51, 3716-3729, 2015.
440	Wei, Z., Yoshimura, K., Wang, L., Miralles, D. G., Jasechko, S., and Lee, X.: Revisiting the contribution of
441	transpiration to global terrestrial evapotranspiration, Geophysical Research Letters, 44, 2792-2801,
442	2017.
443	Wen, X., Yang, B., Sun, X., and Lee, X.: Evapotranspiration partitioning through in-situ oxygen isotope
444	measurements in an oasis cropland, Agricultural and Forest Meteorology, 230, 89-96, 2016.
445	Wu, Y., Du, T., Ding, R., Tong, L., Li, S., and Wang, L.: Multiple methods to partition evapotranspiration
446	in a maize field, Journal of Hydrometeorology, 18, 139-149, 2017.
447	Xiao, W., Wei, Z., and Wen, X.: Evapotranspiration partitioning at the ecosystem scale using the stable
448	isotope method—A review, Agricultural and Forest Meteorology, 263, 346-361, 2018.
449	Yakir, D., and Wang, XF.: Fluxes of CO2 and water between terrestrial vegetation and the atmosphere
450	estimated from isotope measurements, Nature, 380, 515-517, 1996.
451	Yakir, D., and Sternberg, L.: The use of stable isotopes to study ecosystem gas exchange, Oecologia, 123,
452	297-311, 2000.
453	Yepez, E. A., Williams, D. G., Scott, R. L., and Lin, G.: Partitioning overstory and understory
454	evapotranspiration in a semiarid savanna woodland from the isotopic composition of water vapor,
455	Agricultural and Forest Meteorology, 119, 53-68, 2003.
456	Yuan, Y., Du, T., Wang, H., and Wang, L.: Novel Keeling-plot-based methods to estimate the isotopic
457	composition of ambient water vapor, Hydrology and Earth System Sciences, 24, 4491-4501, 2020.
458	Zhang, X. Y., Trame, M., Lesko, L., and Schmidt, S.: Sobol sensitivity analysis: a tool to guide the
459	development and evaluation of systems pharmacology models, CPT: Pharmacometrics & Systems
460	Pharmacology , 4, 69-79, 2015.
461	Zhang, Y., Shen, Y., Sun, H., and Gates, J. B.: Evapotranspiration and its partitioning in an irrigated winter
462	wheat field: A combined isotopic and micrometeorologic approach, Journal of Hydrology, 408,
463	203-211, 2011.
464	Zhao, L., Liu, X., Wang, N., Kong, Y., Song, Y., He, Z., Liu, Q., and Wang, L.: Contribution of recycled
465	moisture to local precipitation in the inland Heihe River Basin, Agricultural and Forest
466	Meteorology, 271, 316-335, 2019.
467	Zhou, S., Yu, B., Huang, Y., and Wang, G.: The effect of vapor pressure deficit on water use efficiency at
468	the subdaily time scale, Geophysical Research Letters, 41, 5005-5013, 2014.
469	Zhou, S., Yu, B., Zhang, Y., Huang, Y., and Wang, G.: Partitioning evapotranspiration based on the concept
470	of underlying water use efficiency, Water Resources Research, 52, 1160-1175, 2016.
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- 475 Table 1. Parameters used to estimate the transpiration to evapotranspiration ratio by $F_T(\delta_{ET})$ method and
- 476 $F_T(\delta_v)$ method. The underlined data was expurgated because they are outside the possible range of
- 477 transpiration to evapotranspiration ratio (i.e., >1).

Date	Time	δ _{ET} (‰)	δ _T (‰)	δ _E (‰)	k(ppm*‰)	δ _v (‰)	C _v (ppm)	$F_T(\delta_{ET})$	$F_T(\delta_v)$
	7:00	-13.92	-8.06	-28.82	-23593.40	-15.95	14229.25	0.72	0.70
	9:00	-13.70	-7.66	-30.06	-25525.94	-15.26	13062.02	0.73	0.75
	11:00	-13.24	-7.43	-29.22	-33109.69	-15.13	17816.22	0.73	0.73
2017/6/19	13:00	-12.07	-7.57	-29.11	-68684.16	-14.65	20298.32	0.79	0.83
	15:00	-12.03	-7.17	-27.94	-55539.52	-16.30	16264.75	0.77	0.72
	17:00	-12.12	-7.77	-27.75	-74334.03	-17.11	12113.71	0.78	0.84
	19:00	-12.87	-8.65	-28.20	-58488.12	-18.68	9569.86	0.78	0.80
	7:00	-16.14	-8.26	-31.90	43614.44	-15.24	14410.06	0.67	0.58
	9:00	-13.76	-7.66	-30.18	-55954.42	-15.53	15795.70	0.73	0.81
	11:00	-13.11	-7.43	-30.57	-68576.56	-15.31	16896.24	0.75	0.83
2017/6/25	13:00	-13.44	-6.57	-32.25	-50147.02	-15.20	17584.07	0.73	0.78
	15:00	-11.28	-6.17	-31.95	-86993.84	-15.29	19003.64	0.80	0.82
	17:00	-12.20	-7.47	-30.51	-65906.59	-15.58	17323.40	0.79	0.81
	19:00	-10.26	-7.85	-29.58	-86035.77	-15.43	12445.80	0.89	0.97
	7:00	-12.50	-8.66	-34.08	-34129.27	-12.50	13197.35	0.85	0.95
	9:00	-12.49	-8.26	-30.44	-46750.79	-13.67	17075.91	0.81	0.88
	11:00	-11.24	-7.47	-30.02	-71075.34	-13.61	22314.74	0.83	0.87
2017/7/6	13:00	-9.78	-6.08	-28.85	-86554.42	-13.63	25873.61	0.84	0.82
	15:00	-8.14	-5.98	-29.89	-133581.89	-12.54	24659.11	0.91	0.95
	17:00	-9.55	-4.15	-28.85	-24038.31	-12.10	19541.53	0.78	0.73
	19:00	-9.85	-6.57	-29.87	-84465.09	-12.95	20679.12	0.86	0.90
	7:00	-11.26	-7.97	-36.83	-10515.44	-11.60	14008.84	0.89	0.90
	9:00	-10.90	-7.50	-33.55	-16700.50	-12.10	16149.08	0.87	0.86
	11:00	-9.31	-6.47	-29.87	-24921.96	-11.19	18048.50	0.88	0.86
2017/7/15	13:00	-7.46	-5.76	-27.92	-54441.51	-10.20	25313.63	0.92	0.90
	15:00	-8.83	-4.23	-29.03	27456.88	-9.86	26911.28	0.81	0.73
	17:00	-8.89	-4.17	-28.07	64236.29	-8.14	22845.26	0.80	0.72
	19:00	-9.04	-7.16	-28.33	-36304.58	-10.00	23204.34	0.91	0.94
	7:00	-3.82	-9.66	-63.48	-77049.20	-14.99	15582.36	1.11	0.99
	9:00	-12.11	-10.10	-43.83	-45814.72	-14.71	16621.78	0.94	0.94
	11:00	-20.74	-8.61	-37.03	171634.91	-14.46	26197.73	0.57	0.56
2017/8/2	13:00	-11.96	-8.17	-36.00	18843.93	-11.56	25519.20	0.86	0.85
	15:00	-11.55	-7.60	-31.83	-5444.14	-11.65	28032.11	0.84	0.84
	17:00	-10.36	-8.34	-30.89	-63514.27	-12.43	23523.91	0.91	0.94
	19:00	-9.70	-8.29	-34.12	-101072.20	-13.58	22204.88	0.95	0.97
	7:00	-14.56	-9.62	-32.98	7022.82	-15.46	15810.78	0.79	0.73
	9:00	-13.47	-9.34	-34.58	-31496.84	-15.28	18125.23	0.84	0.83
	11:00	-12.69	-8.99	-32.19	-49740.56	-15.15	23377.49	0.84	0.83
2017/8/13	13:00	-9.87	-9.49	-29.73	-149355.24	-16.17	23653.76	0.98	0.98
	15:00	-10.01	-6.87	-28.76	-170549.90	-17.28	25081.47	0.86	0.84
	17:00	-10.82	-8.98	-29.11	-147630.72	-17.46	21800.46	0.91	0.92
	19:00	-11.07	-8.42	-29.76	-104132.77	-16.72	17897.72	0.88	0.88
	7:00	-11.55	-7.66	-42.21	-46373.17	-12.91	12350.75	0.89	0.96
	9:00	-11.57	-7.39	-37.36	-29525.94	-12.62	13438.87	0.86	0.90
	11:00	-15.05	-7.79	-29.30	3109.69	-14.81	13941.85	0.66	0.66
2018/6/19	13:00	-14.12	-8.57	-29.44	-8684.16	-14.72	15936.65	0.73	0.73
	15:00	-10.81	-7.17	-29.72	-36539.52	-13.28	14946.74	0.84	0.84
	17:00	-13.09	-6.47	-28.36	-14334.03	-14.36	14842.84	0.70	0.68
	19:00	-9.89	-6.65	-27.47	-48488.12	-15.26	12663.53	0.84	0.77
	7:00	-12.38	-8.61	-7.55	-8171.10	-12.59	14702.98	4.54	4.22
	9:00	-12.94	-8.45	-28.94	7900.05	-12.69	13414.94	0.78	0.76
	11:00	-12.10	-8.30	-29.18	-14964.90	-12.30	19508.19	0.82	0.85
2018/7/4	13:00	-12.20	-8.89	-20.65	11520.51	-11.96	22917.28	0.72	0.70
	15:00	-11.42	-7.77	-24.37	-5545.77	-12.70	21721.97	0.78	0.72
	17:00	-11.64	-8.48	-20.83	-5165.10	-12.90	18580.88	0.74	0.66
	19:00	-11.61	-8.47	-26.37	-16382.76	-12.43	17932.02	0.82	0.83
	7:00	-7.33	-7.97	-27.66	-67353.64	-11.14	18518.09	1.03	1.02
	9:00	-7.72	-7.50	-22.96	-56621.94	-11.14	19975.82	0.99	0.95
	11:00	-8.82	-7.47	-32.13	-50553.49	-10.50	24384.42	0.95	0.96
2018/7/13	13:00	-10.13	-6.76	-30.15	-30834.35	-10.70	28806.53	0.86	0.88
	15:00	-9.93	-9.23	-32.28	-38742.43	-10.66	29499.65	0.97	0.99
	17:00	-9.84	-8.17	-31.84	-19777.39	-10.20	19535.72	0.93	0.96
	19:00	-10.22	-7.16	-28.08	-9873.97	-10.46	15464.54	0.85	0.87
	7:00	-11.47	-11.66	-23.34	-88769.20	-13.80	16165.60	1.02	1.29
	9:00	-11.17	-11.26	-22.70	-46040.00	-13.93	20925.90	1.01	0.96
2010 201	11:00	-12.21	-11.42	-23.03	-32807.57	-13.84	23942.07	0.93	0.91
2018/7/16	13:00	-12.52	-11.09	-23.71	-30703.45	-14.22	29293.09	0.89	0.83
	15:00	-12.21	-9.97	-23.69	3374.13	-12.16	30129.54	0.84	0.83
	17:00	-12.89	-9.11	-20.58	16937.64	-12.34	19370.21	0.67	0.64
	19:00	-10.89	-7.51	-22.44	-14501.33	-12.75	13719.02	0.77	0.72
	7:00	-12.58	-11.26	-20.25	-9352.71	-12.96	21818.45	0.85	0.86
	9:00	-13.69	-12.06	-22.55	-6214.77	-14.03	24953.63	0.84	0.84
	11:00	-12.33	-11.60	-21.72	-34072.08	-13.43	28033.17	0.93	0.94
2018/7/25	13:00	-11.75	-11.10	-19.17	-60112.52	-13.59	33955.04	0.92	0.91
	15:00	-14.90	-11.71	-21.88	18324.12	-12.92	25485.05	0.69	0.81
	17:00	-13.66	-11.27	-30.74	-14127.35	-12.37	22556.53	0.88	0.98
	19:00	-15.95	-10.92	-36.17	31405.77	-10.05	19852.51	0.80	0.97
	7:00	-10.93	-7.49	-39.11	-11535.26	-12.92	16509.69	0.89	0.85
	9:00	-11.99	-8.58	-24.23	869.56	-12.81	14106.31	0.78	0.73
2010	11:00	-14.72	-10.30	-21.46	15267.54	-14.46	13635.30	0.60	0.53
2018/8/19	13:00	-15.75	-14.69	-16.68	10632.60	-15.18	14099.66	0.47	0.37
	15:00	-14.70	-14.14	-15.44	7750.78	-14.15	14595.20	0.57	0.58
	17:00	-14.51	-11.67	-20.90	70.99	-14.52	12306.90	0.69	0.69
	19:00	-13.39	-11.32	-20.52	3667.42	-12.89	11256.45	0.77	0.79







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Inverse of $C_{\rm v}$

480 Fig. 1 Hypothetical graph of the Keeling plot of the isotopic composition of evaporation vapor (δ_E) line

- 481 (line 1), the isotopic composition of transpiration vapor (δ_T) line (line 2) and the possible area (shaded area)
- 482 of the Keeling plot lines.





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Fig. 2 A simplified triangle graph of the Keeling plot. Where x, y and z represent the length of the line segment ($\delta_T - \delta_{ET}$), the line segment ($\delta_{ET} - \delta_E$) and the line segment ($\delta_{ET} - \delta_x$), respectively, and α , β and γ represent the angle of the line segment ($\delta_T - \delta_{ET}$) and the line segment ($\delta_T - \delta_x$), the line segment ($\delta_{ET} - \delta_E$) and the line segment ($\delta_E - \delta_x$) and the line segment ($\delta_{ET} - \delta_E$) and the line segment ($\delta_{ET} - \delta_x$), respectively. 489





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Fig. 3 Schematic of the plant transpiration chamber system. The system is made up of (a) suction port which
absorbs the atmosphere vapor, (b) acrylic glass chamber with volumes of 40x60x180 cm³, and (c) Teflon

495 tube which connects to the suction port or the chamber with water vapor isotope analyzer.





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499 Fig. 4 Comparison of transpiration fraction in the total evapotranspiration between traditional $F_T(\delta_{ET})$ 500 method and the new $F_T(\delta_v)$ method.







503 Fig. 5 Sensitivity contribution of each parameter based on $F_T(\delta_{ET})$ method (a) and $F_T(\delta_v)$ (b) method,

504 respectively.