Hydrologically Informed Machine Learning for Rainfall-Runoff Modelling: Towards Distributed Modelling

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Abstract. Despite showing a great success of applications in many commercial fields, machine learning and data science models generally show limited success in many scientific fields, including hydrology (Karpatne et al., 2017). The approach is often criticized for its lack of interpretability and physical consistency. This has led to the emergence of new modelling paradigms, such as Theory Guided Data Science (TGDS) and physics informed machine learning. The motivation behind such
10   approaches is to improve the physical meaningfulness of machine learning models by blending existing scientific knowledge with learning algorithms. Following the same principles in our prior work (Chadalawada et al., 2020), a new model induction framework was founded on Genetic Programming (GP), namely Machine Learning Rainfall-Runoff Model Induction Toolkit (ML-RR-MI). ML-RR-MI is capable of developing fully-fledged lumped conceptual rainfall-runoff models for a watershed of interest using the building blocks of two flexible rainfall-runoff modelling frameworks. In this study, we extend ML-RR-MI
15   towards inducing semi-distributed rainfall-runoff models. The meaningfulness and reliability of hydrological inferences gained from lumped models may tend to deteriorate within large catchments where the spatial heterogeneity of forcing variables and watershed properties is significant. This was the motivation behind developing our machine learning approach for distributed rainfall-runoff modelling titled Machine Induction Knowledge Augmented - System Hydrologique Asiatique (MIKA-SHA). MIKA-SHA captures spatial variabilities and automatically induces rainfall-runoff models for the catchment of interest without
20   any explicit user selections. Currently, MIKA-SHA learns models utilizing the model building components of two flexible modelling frameworks. However, the proposed framework can be coupled with any internally coherent collection of building blocks. MIKA-SHA's model induction capabilities have been tested on the Rappahannock River basin near Fredericksburg, Virginia, United States. MIKA-SHA builds and tests many model configurations using the model building components of the two flexible modelling frameworks and quantitatively identifies the optimal model for the watershed of concern. In this study,
25   MIKA-SHA is utilized to identify two optimal models (one from each flexible modelling framework) to capture the runoff dynamics of the Rappahannock River basin. Both optimal models achieve high-efficiency values in hydrograph predictions (both at catchment and subcatchment outlets) and good visual matches with the observed runoff response of the catchment. Further, the resulted model architectures are compatible with previously reported research findings and fieldwork insights of the watershed and are readily interpretable by hydrologists. MIKA-SHA-induced semi-distributed model performances were
30   compared against existing lumped model performances for the same basin. MIKA-SHA-induced optimal models outperform

the lumped models used in this study in terms of efficiency values while benefitting hydrologists with more meaningful hydrological inferences about runoff dynamics of the Rappahannock basin.

1 Introduction

Understanding the underlying environmental dynamics occurring within watersheds is an essential and fundamental task in hydrology. Hydrological models play a key role in capturing the discharge dynamics of watersheds. Irrespective of considerable advances over past decades, there is still some scope to advance state of the art in hydrological knowledge to fully describe the functioning of a watershed upon a rainfall event owing to the highly complex, interdependent, and non-linear behaviours of governing physical phenomena. So far, no hydrological model structure can perform equally well over the entire range of problems (Fenicia et al., 2011; Beven, 2012a). This leads to different research directions seeking different hydrological models based on different modelling strategies (Beven, 2012b). Hydrological models are expected not only to have good predictive power but also to be interpretable in capturing relationships among the forcing terms and catchment response which may lead to the advancement of scientific knowledge (Babovic, 2005, 2009; Karpatne et al., 2017). Ideally, the final goal of any successful hydrological model must be based on a physically meaningful model architecture along with a good predictive performance.

It is often observed that simple data-driven models outperform the theory-driven models, such as physics-based and conceptual models, in terms of prediction accuracy in many hydrological applications (Nearing et al., 2020). At the same time, the machine learning models are heavily criticized for the lack of interpretability of induced models (often referred to as the black-box paradigm). As a result of lack of interpretability, the contribution from data-driven models, such as machine learning models, towards scientific advancement is minimal. This hindered achieving the level of success machine learning models achieved in the commercial domain (Karpatne et al., 2017). Incorporating available scientific knowledge to guide learning algorithms to generate more physically reliable and consistent models will be an effective way to improve the explainability of machine learning models. This concept is presently recognized as a new modelling paradigm in the machine learning community as Physics Informed Machine Learning (Physics Informed Machine Learning Conference, 2016) or Theory Guided Data Science (Karpatne et al., 2017).

In this contribution, following the above-mentioned modelling paradigm, we introduce a novel model induction engine called Machine Induction Knowledge Augmented - System Hydrologique Asiatique (MIKA-SHA) for automatic induction of semi-distributed rainfall-runoff models for an area of concern. This work is motivated by the success of our previously introduced (Chadalawada et al., 2020) model induction toolkit titled Machine Learning Rainfall-Runoff Model Induction Toolkit (ML-RR-MI). ML-RR-MI is capable of inducing fully-fledged lumped conceptual rainfall-runoff models. We use the term "hydrologically informed machine learning" to refer that the existing body of hydrological knowledge is used to govern the machine learning algorithms to induce rainfall-runoff model configurations that are consistent with basic hydrological

understanding. The proposed framework uses Genetic Programming (GP) as its learning algorithm, whereas the model building modules of two flexible rainfall-runoff modelling frameworks, namely FUSE (Clark et al., 2008) and SUPERFLEX (Fenicia et al., 2011; Kavetski and Fenicia, 2011) represent the elements of existing hydrological knowledge.

65 By being a TGDS approach, the top priority of MIKA-SHA remains as the induction of readily interpretable rainfall-runoff models with high prediction accuracy. However, the specific objectives of the current study involve 1) Utilize GP for semi-distributed model induction by incorporating spatial heterogeneities of catchment properties and climate variables into the rainfall-runoff modelling, 2) Adopting a quantitative model selection approach to select an optimal model with appropriate complexity to represent runoff dynamics of the catchment of interest instead of the "simpler the better" paradigm used in ML-

70 RR-MI. The approach addresses common hydrological issues, such as equifinality, subjectivity, and uncertainty, in the context of semi-distributed modelling and machine learning. This study is a part of the larger ongoing research effort of using hydrologically informed machine learning for automatic model induction.

The following is how the rest of the text is organized. Section 1 provides a brief discussion on the background behind the development of the MIKA-SHA toolkit. The proposed model induction framework is introduced in Sect. 2. An application of

75 the proposed framework is given in Sect. 3, followed by a discussion on research findings in Sect. 4. The last section (Sect. 5) presents the conclusions of the current study. Additional details are given in the Appendix.

1.1 Uniqueness of the place

Considering the uniqueness of the place is an important aspect of hydrological modelling (Beven, 2020). The Spatio-temporal heterogeneity of landscape characteristics, such as topography, bedrock geology, soil types, land use and climate variables,

80 forces each watershed to behave uniquely. In general, this variability is scale-dependent. More heterogeneity can be observed in both surface and subsurface levels in higher scales, such as at the catchment scale. Namely, there is a possibility that macro-scale patterns of catchments are governed by heterogeneity (Nearing et al., 2020). The use of **flexible/ modular modelling frameworks** and **distributed modelling** concepts are two available toolsets to incorporate spatial heterogeneity into the model building phase.

85 The majority of hydrological models are developed using a generic model configuration that provides reasonable results across a relatively wide spectrum of catchments and meteorological conditions (known as fixed models). At the same time, it is quite improbable for a model to perform equally well in completely different climates and geological regions. In contrast to fixed models, modular modelling frameworks provide more flexibility in the model development by allowing the hydrologist to customize the model structure to suit the intended task. Instead of a single hypothesis available in fixed models, model building

90 components of these modular modelling frameworks can be structured diversely to evaluate multiple hypotheses on watershed functionings. The high degree of transferability of flexible modelling frameworks is an aiding factor in proceeding in the direction of a unified hydrological theory at a watershed level. Simultaneously due to the dynamic modularity and high level

of granularity of modular modelling frameworks, constructing a suitable model for the watershed of concern may require significant effort and expert knowledge. Hence, a hydrologist with novice knowledge would require to test many model structures before selecting an optimal model that is time demanding and computationally intensive. Consequently, it hinders the opportunity to use the flexible modelling frameworks to their full potential.

In addition to incorporating spatial heterogeneity in its modelling process, if the modeller's requirement lies within the catchment (e.g. discharge at a particular location within the catchment), then the only option would be to adopt a distributed model. At the early stages of distributed modelling, the approach (fully distributed modelling) was constrained due to the lack of data and computational power (Wood et al., 2011; Beven, 2012b; Fatichi et al., 2016). Hence, it was thought that this approach would gain success with the advancement of technology. However, until today, fully distributed models have not achieved the expected outcome (Beven, 2020). This points out that the problem lies not only in the lack of local information but also due to the issues in how processes are represented within the distributed model (Beven, 2020). An effective alternative for fully distributed models would be the semi-distributed models, where different conceptual models are allocated to functionally distinct catchment areas. In the semi-distributed modelling approach, each model operates individually with no dependencies or interconnections with others of the network (Boyle et al., 2001; Fenicia et al., 2016). This and using conceptual models rather than small-scale physics enable semi-distributed models to be several orders simpler than fully distributed models.

1.2 Choice of the model

There is an overwhelming number of hydrological models in practice. Selecting an optimal model from among suitable competing models is not a trivial matter. According to Wainwright and Mulligan (2013), the optimal model is defined as the model with enough complexity to explain the underlying physical phenomenon. Ideally, optimal model selection should be based on bias-variance tradeoff as the more complex models result in low bias and high variance, while simpler models result in low variance and high bias in their predictions (Hoge et al., 2018). However, there is no clear cut definition for model complexity, and existing definitions differ across different disciplines (Guthke, 2017). In the context of hydrology, model complexity is often defined based on the process complexity and spatial complexity of the model (Clark et al., 2016), where process complexity is a measure of the number of hydrological processes explicitly represented by the model and spatial complexity is a measure of the degree of model's spatial discretization and their connectivity.

As per the survey conducted by Baartman et al. (2019), most researchers believe selecting a model among competing models should be governed based on the question at hand (i.e. suitability of a model to achieve research objectives). However, Addor and Melsen (2018) have reported that the choice of the model in hydrological applications is often based on familiarity with the model (i.e. based on legacy rather than adequacy). The inherent model complexity is frequently assessed concerning either the number of model parameters, number of state variables, number of physical processes included or computational

complexity, and the choice of such matrix to measure complexity is often subjective (Baartman et al., 2019). One possible
125   alternative to measuring model complexity would be through the analysis of time series complexity of resulted output
signatures of the models based on information theory and pattern matching (Sivakumar and Singh, 2012). Regardless of the
matrix used to measure the model complexity, model parsimony should be a part of that as unwarranted complexity may lead
to overfitting and high uncertainty (Guthke, 2017).

1.3 Machine Learning in Water Resources

130   Machine learning, or data science in general, has become an irreplaceable tool, not only in commercials but also in many
scientific fields, with advancements in computing power and data acquisition through remote sensing and geographical
information systems (Yaseen et al., 2015). Especially within the last two decades, there is an increase in data science model
applications, such as machine learning models in hydrological modelling (Yaseen et al., 2015). Evolutionary Computation
(EC), Support Vector Machines (SVMs), Artificial Neural Networks (ANNs), Wavelet-Artificial Intelligence models (W-AI),
135   and Fuzzy set are the most popular data science techniques in hydrological modelling (Yaseen et al., 2015). Each of these
techniques has its strengths and weaknesses. The scope of this paper does not discuss different data-driven methods in detail.
Alternatively, interested readers may refer to the textbook by Hsieh (2009) and review articles by ASCE Task Committee
(2000), Oyebode and Adeyemo (2014), Yaseen et al. (2015), and Mehr et al. (2018). Machine learning models have shown
encouraging performances in a range of water resources applications because of their capability to handle noise complexity,
140   non-stationarity, non-linearity, and dynamism of data (Yaseen et al., 2015). Certainly, if we are only interested in better
forecasting results then, the machine learning models might be the preferred choice over the conceptual or physics-based
models (provided no data scarcity) due to their better predictive capability (Nearing et al., 2020). A machine learning model
also has the advantage of requiring much less human effort to design and train than a theory-based model (Nearing et al.,
2020).

145   Data-driven techniques have made it possible to develop implementable models with high prediction accuracy using the
available data with limited dependence on domain knowledge. At the same time, this very nature of data-driven models has
become the main point of criticism, especially in scientific fields, including hydrology. They are regularly quoted as black-
box models where the user has a limited understanding of how models generate their forecasts. There are two main reasons
for the limited success of data-driven models in scientific fields (Karpatne et al., 2017). The first reason is the data scarcity for
150   the model training, making it harder to extrapolate model predictions beyond the available labelled data. The second reason is
associated with the objectives of scientific discovery, where the final goal is not only to have actionable models but also to
convey a mechanistic awareness of underlying operations that may lead to the advancement of scientific knowledge. However,
data-driven models, like Deep Learning (DL) models, have demonstrated better hydrograph forecasts even in ungauged basins
(one of the most challenging tasks in hydrological modelling) over the conventional methods (Kratzert et al., 2019).

155 Not recognizing the potential of machine learning models in hydrological modelling has been identified as a danger to the hydrological modelling community (Nearing et al., 2020). Nearing et al. (2020) argue that machine learning models can identify catchment similarities by producing good performances even for the watersheds that were not utilized for training those models. This illustrates machine learning model capabilities in developing basin-scale theories that traditional models could not do so well. Further, the authors refuse the most frequent critique on machine learning models (difficulties in

160 interpretation) by arguing that even the accuracy of process representation in physics-based models is questionable owing to their poorer forecasting accuracies, criticizing only on machine learning models is unfair and meaningless. Despite having a huge potential within machine learning models, state-of-the-art machine learning capacities have not yet been thoroughly explored in hydrological modelling (Shen et al., 2018). Nearing et al. (2020) expect even distributed hydrological models are likely to establish primarily utilizing machine learning soon. Interestingly, recent studies like Nevo (2020), Xiang and Demir

165 (2020) have already explored the potential of DL in distributed streamflow and flood prediction, respectively. Beven (2020) emphasizes the significance of DL models' interpretability and proposes a more explicit integration of process information with DL models. Further, he highlights that machine learning models should also consider issues, such as equifinality, parameter and data uncertainties, common in conventional modelling approaches.

1.3.1 Genetic Programming (GP)

170 Genetic Programming is an EC algorithm (Koza, 1992) inspired through the basic principle of Darwin's evolution theory. The symbolic form of individual solution representation (known as parse trees) distinguishes GP from the other EC methods. GP is a form of supervised machine learning that allows computer programs to be generated automatically. The ability of GP to generate explicit mathematical expressions of input-output relationships distinguishes it from other machine learning techniques. As a result, GP is referred to as a grey-box data-driven mechanism and differentiates it from the other black box

175 data-driven approaches, like ANNs (Mehr et al., 2018). Other than that, GP has become a powerful machine learning approach due to its conceptual simplicity, parallel processing capability, and ability to obtain a near-global or global solution.

GP generates its solutions (GP individuals) by arranging mathematical functions, input variables, and random constants. These are known as the building blocks of the GP algorithm. The algorithm begins with a collection of randomly generated candidate solutions for the problem to be solved. The performance of each candidate is then assessed using a user-defined objective

180 function. Following that, genetic operators, including mutation and crossover, are performed on current generation GP individuals to produce offspring for the next generation. The procedure for selecting parent individuals for breeding guarantees that more fit individuals have a better chance of being chosen. The new set of offspring becomes the candidate solutions in the next generation. This process is repeated until the algorithm meets its termination criteria (usually a maximum number of generations). The candidate solutions evolve towards the global optimum when the GP algorithm curtails the error margin

185 between the simulated values of its individuals and measured observations (Babovic and Keijzer, 2000).

GP has been utilized extensively in water resources, including rainfall-runoff modelling (Babovic and Keijzer, 2002; Babovic et al., 2020), meteorological data analysis (Bautu and Bautu, 2006), streamflow forecasting (Meshgi et al., 2014, 2015; Karimi et al., 2016), soil moisture estimation (Elshorbagy and El-Baroudy, 2009), water quality simulations (Savic and Khu, 2005), sediment transport modelling (Babovic and Abbott, 1997; Safari and Mehr, 2018), reservoir operations (Giuliani et al., 2015), and groundwater simulations (Datta et al., 2014).

1.3.2 Physics Informed Machine Learning

While the community frequently admires theory-based models (physics-based and conceptual models) owing to their explainability, which may serve to understand watershed functioning better, they often experience poorer predictive power than data science models. At the same time, simplistic applications of data-driven models, which often result in higher prediction accuracy than theory-based models, may suffer serious difficulties with interpretation as they are unable to provide basic hydrological insights (Chadalawada et al., 2020). This dichotomy led to the evolution of two major communities in water resources engineering: those who work with theory-based modelling and those who deal with machine learning techniques, which appear to be working quite separately (Todini, 2007; Sellars, 2018).

One promising way to bridge the gap between theory-based and machine learning modelling communities would be to couple the current hydrological understanding to govern machine learning models (Babovic and Keijzer, 2002; Babovic, 2009). This recent paradigm is presently referred to as Physics Informed Machine Learning (Physics Informed Machine Learning Conference, 2016) or Theory Guided Data Science (TGDS) (Karpatne et al., 2017). This paradigm intends to simultaneously address the limitations of data science and physics-based models (primarily, lack of interpretability of data science models and poorer predictive capabilities of physics-based models) and to generate physically consistent and more generalizable models. According to the taxonomy presented by Karpatne et al. (2017), there are five different approaches to incorporating scientific knowledge into data science models. They are 1. theory-guided design of data science models, 2. theory-guided learning of data science models, 3. theory-guided refinement of data science outputs, 4. learning hybrid models of theory and data science, 5. augmenting theory-based models using data science. To bring together scientific knowledge and data science techniques, a typical physics informed data science model might use one or more of the approaches mentioned above. Only a few explainable artificial intelligence utilizations in hydrological modelling are reported in the past (Cannon and Mckendry, 2002; Keijzer and Babovic, 2002; Fleming, 2007). However, there is an increasing trend of adopting TGDS models for recent water resources applications (McGovern et al., 2019), such as hydroclimatic model building (Snauffer et al., 2018), automated model building (Chadalawada et al., 2020) and hydrologic process simulation (Solander et al., 2019).

Physics informed GP

While physics informed machine learning is a relatively new modelling paradigm, there have been attempts over the past two decades to blend the hydrological understanding with the basic GP framework to improve the physical consistency of induced models. Past research, such as Babovic and Keijzer (1999, 2002) and Keijzer and Babovic (2002), use the definitions of units of measurement to bias the search process of the GP algorithm to induce dimensionally correct expressions (a so-called dimensionally aware GP). The authors examined two different approaches, a coercion approach (i.e. a soft constraint on dimensional correctness) and a strongly-typed approach (i.e. a hard constraint on dimensional correctness) and found out that the coercion approach may be more appropriate for scientific discovery. More importantly, the dimensionally aware GP expressions were able to provide additional insights into the underlying problem. Babovic et al. (2001) utilized the dimensionally aware GP to derive hydraulic formulas from measured data and reported that GP induced expressions are quite similar to those identified by human experts with similar or improved accuracy. In a separate study (Baptist et al., 2007; Babovic, 2009), dimensionally aware GP was used to identify expressions to describe resistance induced by vegetation and found that GP induced expressions were superior to the expressions derived by domain experts.

Another augmented version of GP was used to identify predominant processes in hydrological system dynamics by Selle and Muttil (2011). A reservoir model, a cumulative sum and delay function, and a moving average operator were incorporated as basic hydrological insights into the GP function set by Havlicek et al. (2013) to develop a rainfall-runoff prediction programme called SORD. They achieved superior performances in prediction accuracy with SORD than with ANNs and GP without the above-mentioned special functions. GP was utilized by Chadalawada et al. (2017) to induce the most suitable reservoir configuration for a catchment of interest using a customized function set with conceptual modelling concepts extracted from the Sugawara Tank model architecture (Sugawara, 1979). Previously, we introduced (Chadalawada et al., 2020) an automated hydrologically informed lumped rainfall-runoff model induction toolkit based on GP titled Machine Learning Rainfall-Runoff Model Induction Toolkit.

2 Methodology

Chadalawada et al. (2020) introduced a new hydrologically informed rainfall-runoff model induction toolkit (ML-RR-MI) based on GP for developing lumped conceptual hydrological models utilizing model building components of FUSE and SUPERFLEX frameworks. The unique feature of ML-RR-MI is that it uses the existing body of hydrological knowledge to govern the GP algorithm to generate physically consistent models with high prediction accuracies. The building components of the two flexible modelling frameworks are used to incorporate hydrological knowledge with ML-RR-MI's learning algorithm. These building blocks are incorporated as purpose-built functions (named as FUSE and SUPERFLEX) into the function set of ML-RR-MI along with basic mathematical functions.

Successful applications of the ML-RR-MI toolkit motivated the present research to extend its modelling capabilities towards distributed hydrological modelling. Although applying the ML-RR-MI toolkit is more meaningful for small catchments due

to its lumped watershed representation, there is no strict catchment size limitation for using it. However, with the increase of basin sizes, the meaningfulness of the lumped values decreases. Hence, the inferences made on the basis of a lumped model may be accurate but not reasonable or realistic. Due to the limited success and higher-order complexity of fully distributed models, the semi-distributed modelling concept is used for the current study, where a network of functionally distinguishable conceptual models from flexible modelling frameworks is developed to represent the watershed dynamics. As a result of the higher granularity and flexibility provided by the flexible modelling frameworks, even with a lumped application, one can try thousands of possible model architectures for a catchment of interest. This may rise to millions of possible model combinations in the context of semi-distributed modelling, which makes it almost impossible to test them manually.

Further, selecting a model configuration without testing alternative model configurations would become highly subjective and require considerable expert knowledge and time. Upon review of 1500+ peer-reviewed articles, Addor and Melsen (2019) reported that selecting the hydrological model is frequently based on legacy factors such as prior experience, habit, easiness, the popularity of the model rather than adequacy factors like appropriateness of the model to achieve research objectives. A semi-distributed model choice based on a subjective model selection may introduce biased research findings. Therefore, we see a necessity to automate the model building phase to overcome these limitations. Henceforth, our machine learning approach for rainfall-runoff modelling titled Machine Induction Knowledge Augmented - System Hydrologique Asiatique (MIKA-SHA) captures spatial variabilities and automatically induces rainfall-runoff models for the catchment of interest without any explicit user selections.

GP has been selected as the machine learning technique here due to its ability to generate explicit mathematical relationships among independent (forcing) and dependent (response) variables. Therefore, incorporating hydrological knowledge can be done more explicitly with GP than other black-box type machine learning techniques. Yet, most state of the art GP utilizations in water resources (Oyebode and Adeyemo, 2014; Mehr et al., 2018), GP is still utilized as a short-term prediction mechanism that is analogous to ANN applications. In our contribution, we test the full potential of GP by developing fully-fledged rainfall-runoff models. As MIKA-SHA relies on GP, there is no requirement for pre-definition of a model structure (hypothesis on catchment runoff dynamics). Instead, identifying an appropriate model structure is part of the machine learning framework, meaning that GP simultaneously optimizes model structure and model parameters. Here hydrological insights are introduced through integrating process understanding by including model building components from existing flexible modelling frameworks into the function set of the GP algorithm. As per the classification presented by Karpatne et al. (2017), our framework falls under the hybrid TGDS category. Currently, MIKA-SHA learns models utilizing the model building components of two flexible modelling frameworks. However, the proposed framework can be coupled with any internally coherent collection of building blocks. R (R Core Team, 2018) programming language has been used to implement MIKA-SHA.

2.1 MIKA-SHA workflow

The workflow diagram of the MIKA-SHA is given in Fig. 1. Details about each module of MIKA-SHA (data preprocessing, model identification, model selection, and uncertainty analysis) are given in the sequel.

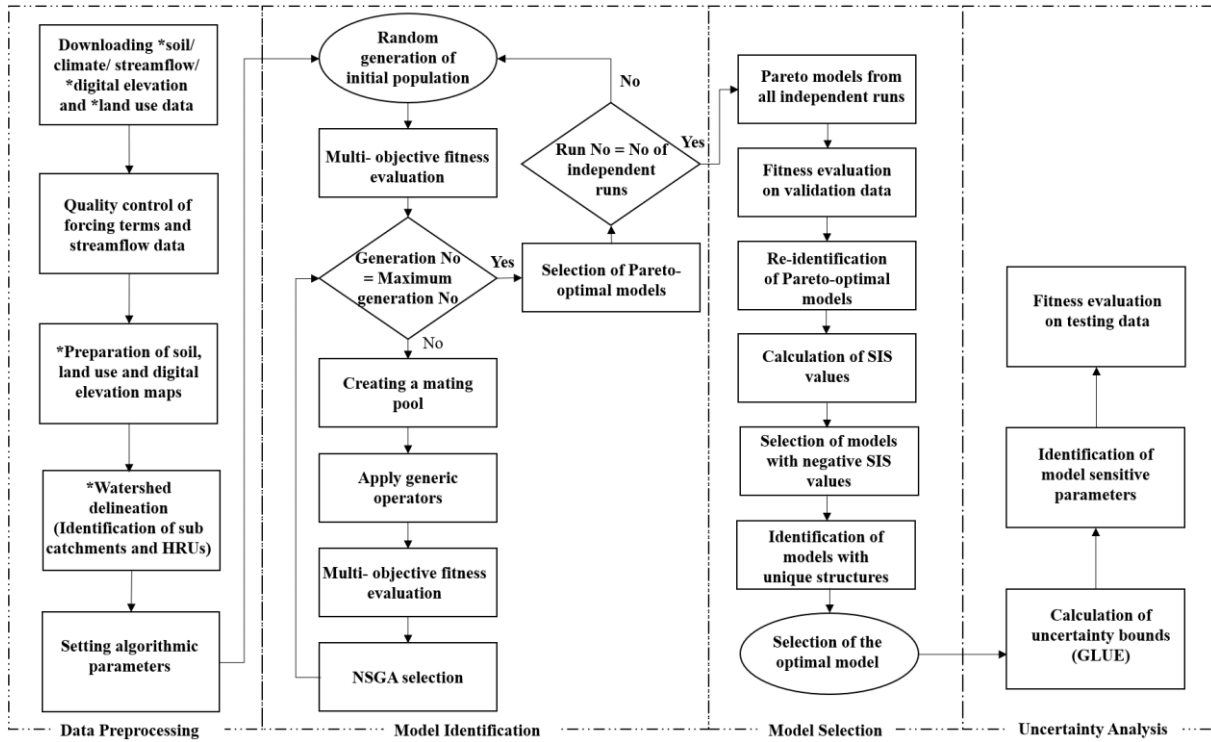



Figure 1: Workflow diagram of MIKA-SHA

2.1.1 Data Preprocessing

The data preprocessing stage includes quality checking of forcing terms (precipitation, potential evaporation, temperature) and runoff data, identification of subcatchments and Hydrological Response Units (HRUs) through watershed delineation, preparation of subcatchment averaged forcing terms vectors and setting algorithmic parameters (e.g. number of generations, population size, number of independent runs, etc.). In general, there are no specific rules to select the appropriate algorithmic settings. However, the chosen settings eventually decide the computational time and demand. MIKA-SHA uses QGIS software (QGIS, 2020) to prepare the required Digital Elevation Maps (DEM), land use maps, geological maps and soil maps for watershed delineation. Then, the SWAT+ plugin of QGIS software is used for the watershed delineation. HRUs can either be identified based on the topography, soil type, land use, geology or combination of different landscape types of the catchment of interest.

2.1.2 Model Identification

At the model identification stage, GP based machine learning framework of MIKA-SHA optimizes both model structure and parameter values of candidate solutions which involves the following steps.

Step 1: A set of candidate model structures (semi-distributed model structures made from the purpose-built functions, basic mathematical functions and random constants) are randomly generated to capture the watershed's runoff dynamics (known as the initial population). These model structures (GP individuals) may differ from each other in terms of model structural components and parameter values. MIKA-SHA consists of three different initialization procedures. (i) Full method (all individuals have the maximum allowable initial tree depth), (ii) Grow method (individuals of different tree depths up to the maximum allowable initial tree depth are possible), (iii) Ramped half-and-half method (individuals are generated both using the full method and grow method in equal proportions).

Step 2: The performance of each candidate model structure is evaluated on a user-defined multi-objective criterion. Non-dominated Sorting Genetic Algorithm-II (NSGA-II) (Deb et al., 2002) is used to found the multi-objective optimization scheme of MIKA-SHA. Each individual in the population is evaluated on each objective function separately. MIKA-SHA utilizes parallel computation at this stage to reduce computational time.

Step 3: Each individual is assigned a non-domination rank and a crowding distance value based on the objective function values. The ranks are identified based on the Pareto-optimality concept. For example, all the individuals with non-domination rank two are dominated by individuals with rank one. However, individuals with rank two are not dominated by any other individuals with a higher rank (lower the rank, better the individual). On the other hand, crowding distance measures how an individual located relative to the other individuals of the same rank (more the distance better the individual – more diversity).

Step 4: Individuals are selected for a mating pool to create offsprings using the tournament selection mechanism (a user-defined number of individuals are chosen randomly. If they have different ranks, the individual with the lowest rank is selected. If all of them have the same rank, then the individual with the highest crowding distance is selected). The selection mechanism ensures that individuals with higher performance values in terms of the objective functions used have a higher chance of selection.

Step 5: Genetic operators, mainly crossover (two parent individuals are divided and recombined to form two offsprings) and mutation (sub-tree of a parent individual is randomly substituted with another sub-tree), are applied to parent individuals to create the child population. Then, Step 2 is followed for the child population.

Step 6: Both parent population and child population are combined, and Step 3 is followed. Individuals are selected for the next parent population from the combined population using non-domination ranks and crowding distance values (e.g. individuals with lower ranks proceed first into the next generation until the population size reaches).

Step 7: Step 2 to Step 6 are repeated until the algorithm reaches the maximum number of generations. Rank one individuals of the final generation are saved into a different file.

Step 8: Step 1 to Step 7 are repeated for a user-defined number of independent runs to cover the solution space to a greater extent. The model identification stage's output consists of a set of non-dominated models (Pareto-optimal models) based on the selected objective criteria.

2.1.3 Model Selection

By nature, the GP algorithm drives its total population towards the global or near-global solution, which results in a set of possible solutions instead of one solution. In the context of rainfall-runoff model induction, such possible solutions may represent different model structures (different hypotheses about catchment dynamics). Identifying the best performing model from Pareto front of non-dominated solutions for a watershed of interest is not a trivial matter. Hence, it is often required to use a model selection scheme to select the optimal model from the competing models. The model selection stage of MIKA-SHA starts with the best models of each independent run derived through the GP framework at the model identification stage. The quantitative optimal model selection process is streamlined as follows.

Step 1: Performance evaluation using the same multi-objective criterion on validation data for all identified models from the model identification stage.

Step 2: Re-identification of Pareto-optimal models based on calibration and validation fitness performances.

Step 3: Calculation of Standardized Signature Index Sum (SIS) of each Pareto-optimal model.

- *Standardized Signature Index Sum (SIS)*

The SIS value is a comparative performance metric that quantifies a model's capability in capturing the observed Flow Duration Curve (FDC) relative to other competitive models (Ley et al., 2016). A model with a negative SIS value indicates over average capability in capturing observed FDC and vice versa. In SIS calculation, both observed and simulated FDCs are divided into four flow regimes based on flow exceeding probabilities and calculate the absolute difference in observed and simulated cumulative discharges in each region. Then, four separate Z-score values (representing four regions) are assigned to each model based on the standard deviation and mean of all models considered. The algebraic sum of those four Z-score values becomes the SIS value of the model.

$$Z_{sa} = \frac{|x_{sa}| - \overline{x_a}}{\sigma_a} \tag{1}$$

$$SIS_a = Z_{sFHV} + Z_{sFMV} + Z_{sFMS} + Z_{sFLV} \tag{2}$$

where $|x_{sa}|$: modulus of the signature index where, s: model, a: FDC signature based on Flow Exceeding Probability (FEP) (FHV: FEP less than 2%, FMV: FEP between 2% and 20%, FMS: FEP between 20% and 70%, FLV: FEP greater than 70%) and x: value, Z: standard score, $\overline{x_a}$ and σ_a : average and standard deviation of $|x_{sa}|$.

Step 4: Selection of Pareto-optimal models with SIS scores below zero over the calibration and validation periods.

Step 5: Identify unique model structures (referred to as competitive models) from the models in Step 4. If there is more than one model with the same model structure, the model with the most negative SIS value is selected.

Step 6: Competitive models are ranked separately according to three relative measures: Cross sample entropy value (Cross-SampEn), Dynamic Time Warping (DTW) distance and model parsimony (lower the value better the performance, lower the rank). The model with the lowest sum up rank is identified as the optimal model for the catchment in consideration.

- *Cross sample entropy value (Cross-SampEn)*

Cross-SampEn value is a derivation from the commonly used Sample Entropy value (Richman and Moorman, 2000). Sample Entropy is a complexity measure of data series which has its origin in information theory. Sample Entropy value gives an idea about the complexity of the data series based on the information content in a mathematical way. Cross-SampEn value also follows the same concept but is used to measure the correlation between two series by matching patterns from one series with another. A low Cross-SampEn value indicates that the two series are more similar to each other. More details about Cross-SampEn can be found in Delgado-Bonal and Marshak (2019).

- *Dynamic Time Warping (DTW) distance*

DTW distance (Sakoe and Chiba, 1978) is a similarity measure between two time series, including warping of their time axes to find the optimal temporal alignment between the two. DTW distance is derived as an alternative to the commonly used Euclidean distance. Two identical time series with a small-time shift may ending up with a large Euclidean distance and may consider them as two dissimilar time series. The DTW method captures them as two similar time series as it ignores the shift in the time axes. A low DTW distance indicates more similarity between the two time series compared. Details and applications of the DTW method can be found in Salvador and Chan (2007), Giorgino (2009) and Vitolo (2015).

375 - *Model parsimony*

Here, the model parsimony is evaluated in terms of each model's number of associated model parameters. One model is considered more parsimonious than another model if the number of model parameters of the former is lower than the latter.

2.1.4 Uncertainty Analysis

Once the optimal model is identified for the catchment of interest, the Generalized Likelihood Uncertainty Estimation (GLUE)
380 approach (Beven and Binley, 1992) is used to perform its sensitivity and uncertainty analysis as described below.

Step 1: A random subset of model parameters of the identified optimal model structure is uniformly changed within their parameter range (in this case, between 0 and 1 as all parameter ranges are normalized within the MIKA-SHA framework) while keeping the remaining model parameters at their calibrated values (parameter values determined in the model identification stage). Then, the performance of the parameter set is evaluated using a user-defined objective function
385 (likelihood estimator). If the model parameter set provides an objective function value greater than the likelihood threshold, the parameter set (known as a behavioural model), its objective function value and the simulated discharge are recorded.

Step 2: Repeat the above step until the number of behavioural models reaches a user-defined value. Each time the number of parameters to change and which parameters to change are randomly chosen from a uniform distribution.

Step 3: For each time step, simulated discharge values of all behavioural models are sorted in ascending order. Then, a weight
390 is assigned to each model (objective function value itself can be used as the weight). Finally, the Cumulative Probability Distribution Function (CDF) of the weights is calculated at each time step.

Step 4: For each time step, a relationship diagram is obtained by taking CDF as the x-axis and simulated discharge at the y-axis. From the diagram, corresponding simulated discharge values of 95% and 5% quantile of CDF are selected as the upper and lower bounds of the 90% confidence band.

395 **Step 5:** Percentage of measured streamflows of the calibration period, which fall inside the 90% confidence band, is used to measure the uncertainty estimation capability of the selected optimal model (i.e., check whether the chosen model's parameter uncertainty is capable or not to account for total output uncertainty).

Step 6: If the uncertainty estimation capability is satisfactory (above a user-defined % value), the model performance of the optimal model is tested for an independent time frame (testing period) which is not used in model selection or identification
400 stages. If the uncertainty estimation is not satisfactory, then all the above steps will be repeated with the next best competitive model.

Step 7: Sensitivity scatter plot diagrams are constructed for every model parameter using the parameter values of behavioural models. The shape of the scatter plot (the x-axis – normalized parameter range, the y-axis – objective function values) is used to identify the degree of sensitivity of each model parameter.

MIKA-SHA has been developed by following good practices to handle general modelling issues related to both hydrological modelling and machine learning. Multi-objective optimization is used to ensure the selected models perform better in many flow characteristics instead of fitting to a particular segment of measured flow. The automated and quantitative approach of the toolkit ensures no direct human involvement (no subjectivity in model induction or selection except setting algorithmic parameters). Model performance is evaluated on different absolute and relative performance measures. A model performing well in many performance measures may suffer less from equifinality (model performs for the right reasons). To prevent overfitting, the optimal model selection process considers performances of both calibration and validation periods. Further, model parsimony is considered in the model selection stage as more complex models are more susceptible to overfitting and over-parameterization. Parallel computing significantly reduces overall computation time since purpose-built functions take much longer to compute than basic mathematical functions. The more stable fixed-step implicit Euler's method is used to solve partial differential equations.

2.2 Purpose-built functions

Incorporating existing hydrological knowledge is done by adding purpose-built functions into the function set of the GP-based optimization framework (model identification stage) of the MIKA-SHA toolkit. At present, there are two different model building block libraries in MIKA-SHA, SUPERFLEX library and FUSE library. Functional argument values of purpose-built functions decide the structure and corresponding parameter values of induced rainfall-runoff models.

2.2.1 SUPERFLEX Library

SUPERFLEX library of MIKA-SHA includes model building components of popular SUPERFLEX (Fenicia et al., 2011; Kavetski and Fenicia, 2011) flexible rainfall-runoff modelling framework. SUPERFLEX framework facilitates hydrologists to test many different hypotheses about the functioning of the watershed of interest using the model building components (reservoirs, junctions, and lag functions) available in the framework. The water storages within the catchment, such as soil moisture, interception, groundwater, snow, and their release of water, are represented through reservoir units. Junction elements conceptualize the merging and splitting different fluxes in catchment dynamics (e.g. Hortonian flow, evaporation). Channel routing (delays in flow transmission) is described using lag functions. A number of constitutive functions are available to describe lag function characteristics and storage-discharge relationships of storage units (reservoirs). SUPERFLEX applications in rainfall-runoff modelling are found in van Esse et al. (2013), Fenicia et al. (2014, 2016), and Molin et al. (2020). Within MIKA-SHA, a purpose-built function named SUPERFLEX assembles these generic components in a meaningful and guided manner to induce different rainfall-runoff model structures.

2.2.2 FUSE Library

FUSE library of MIKA-SHA consists of model building components of Framework for Understanding Structural Errors (FUSE) (Clark et al., 2008) modular rainfall-runoff modelling framework. FUSE was developed to examine the effect of model structural differences on rainfall-runoff modelling. FUSE conceptualizes the functioning of a catchment using a two-zone model architecture: an unsaturated zone (upper soil layer) and a saturated zone (lower soil layer). The model building modules of FUSE involve the choice of upper and lower soil configurations and parameterization for different hydrological processes, such as evaporation, percolation, interflow, surface runoff, and baseflow. The modeller has the freedom of selecting these model building modules from four rainfall-runoff models (TOPMODEL, ARNO/VIC, SACRAMENTO, and PRMS), which are known as FUSE parent models. For more details and applications of FUSE, please refer to Clark et al. (2011) and Vitolo (2015). Inside the MIKA-SHA FUSE library, a purpose-built function named FUSE integrates model building decisions of the FUSE framework to develop different rainfall-runoff model configurations.

In the present contribution, a new function called DISTRIBUTED has been incorporated into the GP function set along with FUSE, SUPERFLEX and other mathematical functions. The DISTRIBUTED function represents the induced semi-distributed models (GP individuals) within the framework. The parse tree demonstration of the DISTRIBUTED function is shown in Fig. 2. As it can be seen, the DISTRIBUTED function uses either FUSE or SUPERFLEX functions as its function arguments depending on the selected model inventory library by the user. The length of the function arguments of DISTRIBUTED function relies on the count of HRUs within the watershed. The DISTRIBUTED function assigns separate model structures to each HRU, and HRUs within the same subcatchment share the same forcing variables. The last two arguments of the DISTRIBUTED function are the lag parameters used to route HRU outflows into the subcatchment outlets (Lag_HRU) and subcatchment outflows into the catchment outlet (Lag_Sub). Here, the routing module is based on two-parameter gamma distribution with the shape parameter equals 3 (Clark et al., 2008). Nodes from depth = 2 to depth = maximum allowable tree depth are the function arguments of either FUSE or SUPERFLEX functions. For more details on FUSE and SUPERFLEX functions, such as function arguments and parse tree representations, please refer to Chadalawada et al. (2020).

2.3 Performance Measures

MIKA-SHA consists of a performance measures library, including the most widely adopted performance matrices. The explanatory power of the performance measure used to assess the prediction accuracy of model simulations has a direct impact on the optimal model selection (Chadalawada and Babovic, 2017). In the present study, we have selected four absolute performance measures, namely volumetric efficiency (Criss and Winston, 2008), Kling-Gupta efficiency (Gupta et al., 2009), Nash-Sutcliffe efficiency (Nash and Sutcliffe, 1970) and log Nash-Sutcliffe efficiency (Krause et al., 2005) from the MIKA-SHA's performance measures library to evaluate the simulated discharge values against the measured discharge values. The four selected objective functions are sensitive to different regions of measured and simulated runoff signatures, and their details are given in Table 1. The four selected objective functions are used in the multi-objective optimization scheme of MIKA-SHA.

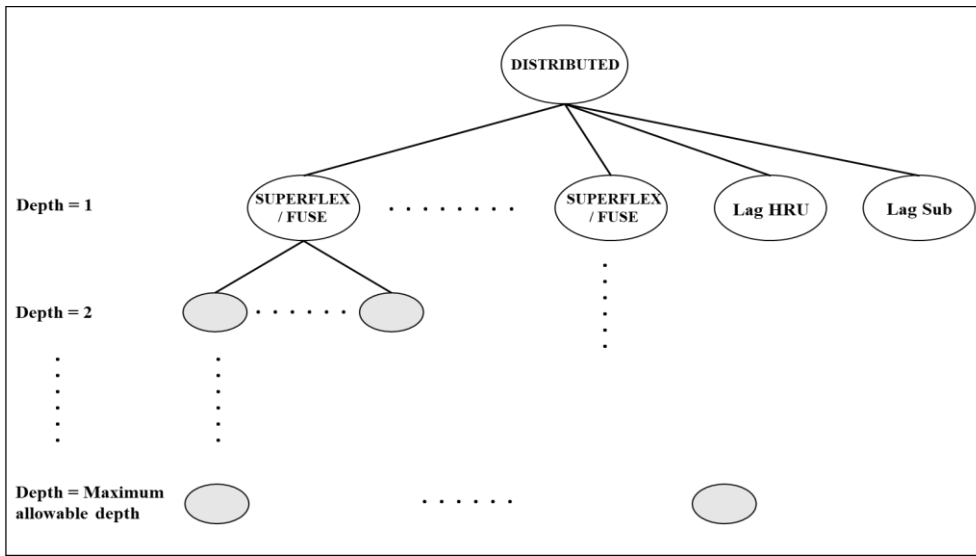



Figure 2: Parse tree representation of the DISTRIBUTED function of MIKA-SHA

Table 1: Absolute performance measures used in the current study

Name	Equation	Sensitivity	Optimum
Volumetric Efficiency (VE)	$VE = 1 - \dfrac{\left|\sum_{t=1}^{N}(Q_{ot} - Q_{st})\right|}{\sum_{t=1}^{N} Q_{ot}}$ N: Time steps, Q_{ot}: Observed streamflow, Q_{st}: Simulated streamflow	Water balance	1
Kling-Gupta Efficiency (KGE)	$KGE = 1 - \sqrt{(r-1)^2 + (\alpha-1)^2 + (\beta-1)^2}$ r: Linear correlation coefficient, $\alpha = \dfrac{\sigma_s}{\sigma_o}$, $\beta = \dfrac{\mu_s}{\mu_o}$, σ: Standard deviation, μ: Mean	Flow variability	1
Nash-Sutcliffe Efficiency (NSE)	$NSE = 1 - \dfrac{\sum_{t=1}^{N}(Q_{ot} - Q_{st})^2}{\sum_{t=1}^{N}(Q_{ot} - \overline{Q_{ot}})^2}$ $\overline{Q_{ot}}$: Average of measured discharge values	High flows	1
Log Nash-Sutcliffe Efficiency (logNSE)	$logNSE = 1 - \dfrac{\sum_{t=1}^{N}(logQ_{ot} - logQ_{st})^2}{\sum_{t=1}^{N}(logQ_{ot} - log\overline{Q_{ot}})^2}$ log: Natural logarithm	Low flows	1

3 Application of MIKA-SHA

This section aims to demonstrate how MIKA-SHA works through a one case study using a watershed in the United States. MIKA-SHA was applied to induce two optimal semi-distributed models for the watershed using SUPERFLEX and FUSE model inventory libraries independently.

3.1 Study Area

The Rappahannock River basin at Fredericksburg, Virginia (Fig. 3) was selected to test the semi-distributed model induction capabilities of MIKA-SHA. Rappahannock River basin is an Intermediate Scale Area (ISA) river basin with a drainage area of 4134 km^2 located in the southeastern quadrant of the United States. Basin details are summarized in Table 2. Digital Elevation Data (DEM) of the Rappahannock River basin at 30 m resolution were obtained from the United States Geological Survey (USGS) EarthExplorer's Shuttle Radar Topography Mission (SRTM) data (USGS EarthExplorer, 2020). The entire basin was split into three subcatchments for the current application. The topography of the region was used to identify HRUs, and three HRUs, namely, Hill (slope band % > 10), Floodplain (slope position threshold = 0.1), and plateau (slope band % < 10), were selected. The HRU details are given in Table 3.

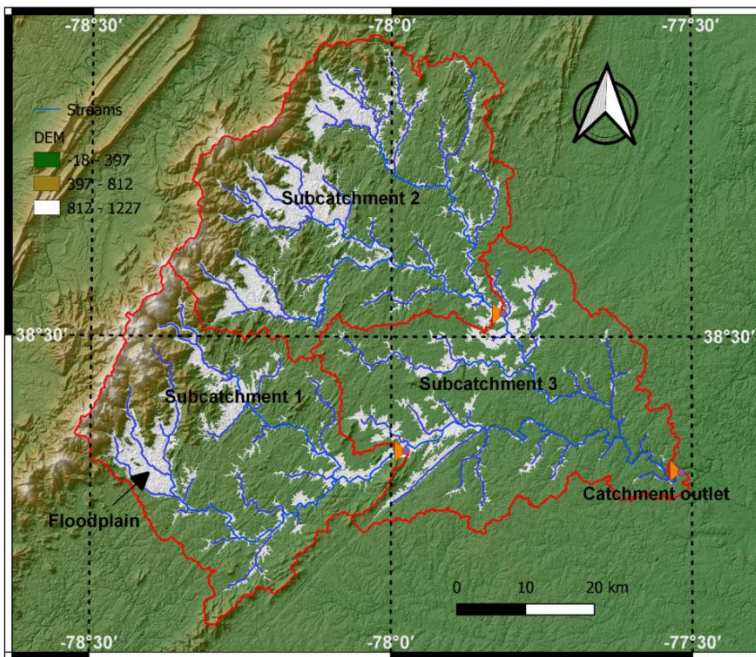



Figure 3: Rappahannock River basin at Fredericksburg, Virginia, United States (map was generated through SWAT+ plugin in QGIS software using USGS EarthExplorer's Shuttle Radar Topography Mission DEM data)

Fifteen years (1 January 1987 to 31 December 2001) of forcing terms and discharge data of Rappahannock River basin were utilized for model spin-up (1 January 1987 – 31 December 1987), calibration (1 January 1988 – 31 December 1992), validation (1 January 1993 – 31 December 1997) and testing (1 January 1998 – 31 December 2001). Daily catchment average potential evaporation, temperature, and streamflow data were downloaded from the MOPEX dataset (USGS ID: 1668000) (MOPEX, 2021). The spatial distribution of daily precipitation data was taken into account and lumped at the subcatchment scale. Precipitation data were downloaded from the Dayment dataset (Dayment, 2020), which provides daily weather parameters (resolution: 1 km x 1 km) over North America. The time series diagrams of precipitation, potential evaporation, temperature, and streamflow of the Rappahannock River basin are displayed in Fig. 4. Additionally, hydrometeorological data of subcatchment 1 and 2 are available in the CAMELS dataset (USGS ID: 1667500 and 1664000, respectively) (Newman et al., 2015). Even though MIKA-SHA only utilizes runoff at the catchment outlet for model training (calibration period), it can predict runoff at every subcatchment outlet. Therefore, once MIKA-SHA identifies the optimal models, their internal prediction capabilities are assessed using observed runoff data of subcatchment 1 and 2. Once the relevant data are processed, the user can set the algorithmic parameters of MIKA-SHA. Table 4 summarizes the algorithmic setting of MIKA-SHA used in the current study.

Table 2: Basin details

Parameter	Details
Drainage area	4134 km^2
Outlet coordinates	38.3222º, -77.5181º
Sub catchment area %	Sub 1 – 29.2%, Sub 2 – 38.8%, Sub 3 – 32.0%
Floodplain/ Upslope	20.3% / 79.7%
Annual average discharge	378 mm/year
Annual average potential evaporation	921 mm/year
Annual average temperature	12.46 ^{0}C
Annual average precipitation	1030 mm/year
Average slope	0.03035
Average elevation	198.9 m
Length from subcatchment outlet to catchment outlet along the main river	Sub 1 – 60.6 km, Sub 2 – 47.8 km, Sub 3 – 0 km
Vegetation type/ Soil type	Mixed forest/ Silt loam and clay loam

500

Table 3: Area percentages of topography-based HRUs

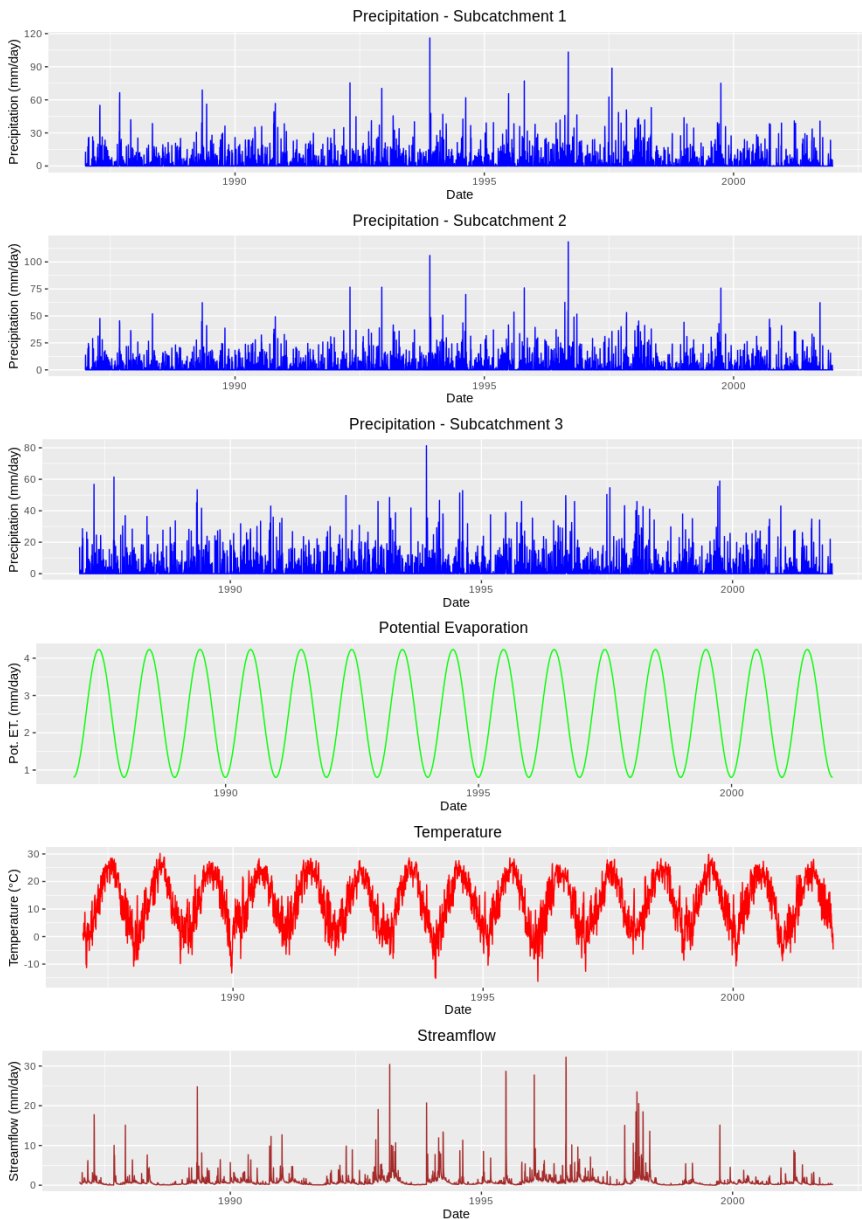
Subcatchment	Hill (%)	Floodplain (%)	Plateau (%)
1	45.2	20.6	34.2
2	44.6	23.9	31.5
3	19.0	15.6	65.4

505   **Figure 4: Forcing terms and streamflow data of Rappahannock River basin**

Table 4: Algorithmic settings of MIKA-SHA used in the current study

Option	Setting
Number of independent Runs	40
Size of population	2000
Termination criteria	Generation number = 50
The randomized method used for initialization	Ramped half-and-half
Purpose built functions/ Mathematical functions	SUPERFLEX, FUSE, DISTRIBUTED/ +, -, /, *
Input variables – SUPERFLEX	Precipitation, temperature, potential evaporation
Input variables – FUSE	Precipitation, potential evaporation
Dependent variable	Streamflow
Objective functions used	NSE, VE, logNSE, KGE
Normalized range of random constants	0 to 1
Depth of parse trees- initial/ maximum	SUPERFLEX – 3/5, FUSE – 2/5
The mating pool selection strategy	Tournament selection with four competitors at once
Genetic operator probability: mutation	
Constant/ Tree/ Separation/ Node	0.5/0.5/0.3/0.3
Genetic operator probability: crossover	0.7
Count of CPUs used for parallel computation	40 units
Level of parallel computation	Performance evaluation level
Likelihood threshold – GLUE	Nash Sutcliffe efficiency = 0.6 (Beven and Free, 2001)
Behavioural models – GLUE	5000
Satisfactory uncertainty estimation threshold	60%

3.2 Results

3.2.1 MIKA-SHA models induced using SUPERFLEX Library

Adhering to the methodology given in Sect. 2, the model architecture presented in Fig. 5 (hereinafter referred to as MIKA-
510 SHA_SUPERFLEX) was identified to capture the runoff response of the Rappahannock River basin. The hillside structure of the MIKA-SHA_SUPERFLEX consists of four reservoirs: a fast-reacting reservoir (FR), an unsaturated reservoir (UR), a slow-reacting reservoir (SR), and a riparian reservoir (RR). The hillside model structure also includes a half-triangular delay function associated with SR. The discharge of the UR incorporates a modified logistic curve function relationship with its storage. The storage-discharge relationships of both RR and SR are linear, while FR has a power function relationship. The
515 model structure representing the floodplain consists of only a UR with a power function storage-discharge relationship. The second link from the top of the floodplain model structure represents the runoff generation through infiltration excess overland

flow. The Plateau area model structure of MIKA-SHA_SUPERFLEX is based on a three-reservoir configuration with a UR, an FR, and an SR. The power function governs the storage-discharge relationships of both UR and FR of the plateau area model structure, while the storage-discharge relationship of SR is linear.

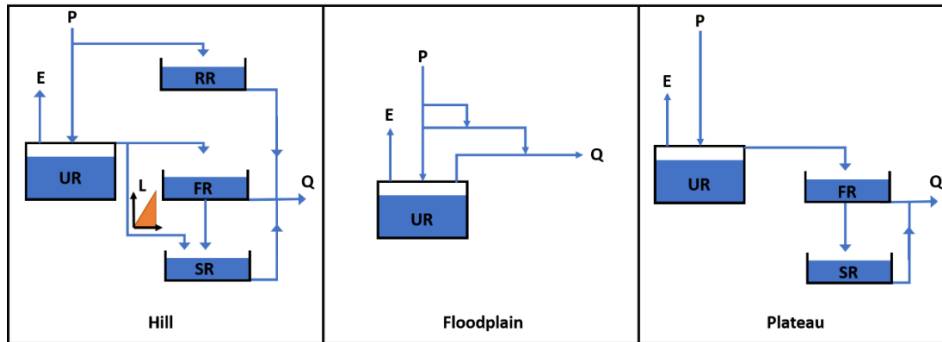



Figure 5: MIKA-SHA_SUPERFLEX model configuration (P: precipitation, E: evaporation, Q: total discharge, RR: riparian reservoir, SR: slow-reacting reservoir, FR: fast-reacting reservoir, UR: unsaturated reservoir, L: half-triangular lag function)

The performance matrix over calibration, validation and testing phases of MIKA-SHA_SUPERFLEX is given in Table 5. The high-efficiency values of all four absolute performance measures suggest that MIKA-SHA_SUPERFLEX is competent in capturing the catchment dynamics of the Rappahannock River basin. More importantly, MIKA-SHA_SUPERFLEX is capable of predicting discharge at two subcatchment outlets satisfactorily. Throughout the calibration, validation, and testing phases, the model behaves consistently. As a result, we may anticipate no overfitting problems with training data (calibration data). Figure 6 illustrates the simulated hydrograph of MIKA-SHA_SUPERFLEX along with the observed hydrograph of the watershed. As can be seen, the simulated discharge signature matches the observed discharge signature reasonably well. It is noteworthy that MIKA-SHA_SUPERFLEX underestimates the peak discharges in some instances. Figure 7 illustrates the observed FDCs of the watershed and the simulated FDCs of MIKA-SHA_SUPERFLEX for calibration, validation, and testing periods. Modelled FDCs nearly follow the measured FDCs both in medium and high flow regimes but diverge slightly at low flow regimes.

Uncertainty analysis reveals that 60.2% of the measured streamflow data of the calibration period lie inside the 90% uncertainty bands of MIKA-SHA_SUPERFLEX, which is higher than the threshold set for the current study (60%). Hence, it is assumed that the MIKA-SHA_SUPERFLEX's parameter uncertainty alone sufficiently estimates the total output uncertainty. Out of the 37 model parameters included in MIKA-SHA_SUPERFLEX, 13 model-sensitive parameters can be recognized by analyzing the shapes of sensitivity scatterplots. Five of them are associated with the hillside model structure (D_R, D_F, Ce, Tlag, and Beta_Qq_UR). The Floodplain model structure consists of two model-sensitive parameters (Ce and D_S), while the plateau area model structure includes four model-sensitive parameters (Beta_Qq_UR, Ce, Smax_UR, and K_Qb_FR). Further, the two lag parameters of the DISTRIBUTED function are also identified as model-sensitive parameters (lag_HRU and

lag_Sub). The sensitivity scatterplots and the model parameters details of MIKA-SHA_SUPERFLEX are provided in the Appendix.

545 **Table 5: Performance matrix of MIKA-SHA_SUPERFLEX**

Outlet	Efficiency (Calibration/ Validation/ Testing)			
	KGE	NSE	logNSE	VE
Catchment	0.83/ 0.82/ 0.83	0.74/ 0.66/ 0.82	0.76/ 0.73/ 0.74	0.65/ 0.57/ 0.61
Subcatchment 1	0.73/ 0.69/ 0.89	0.55/ 0.55/ 0.79	0.67/ 0.67/ 0.73	0.60/ 0.53/ 0.59
Subcatchment 2	0.72/ 0.72/ 0.86	0.60/ 0.44/ 0.74	0.68/ 0.67/ 0.70	0.57/ 0.51/ 0.56

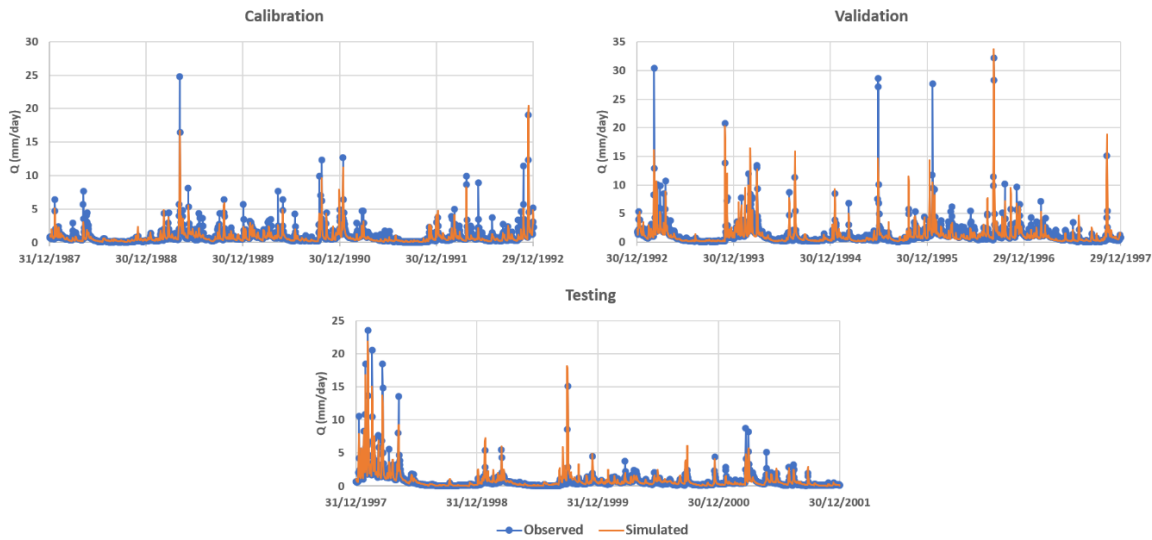



Figure 6: Simulated hydrograph of MIKA-SHA_SUPERFLEX with the observed hydrograph of the basin

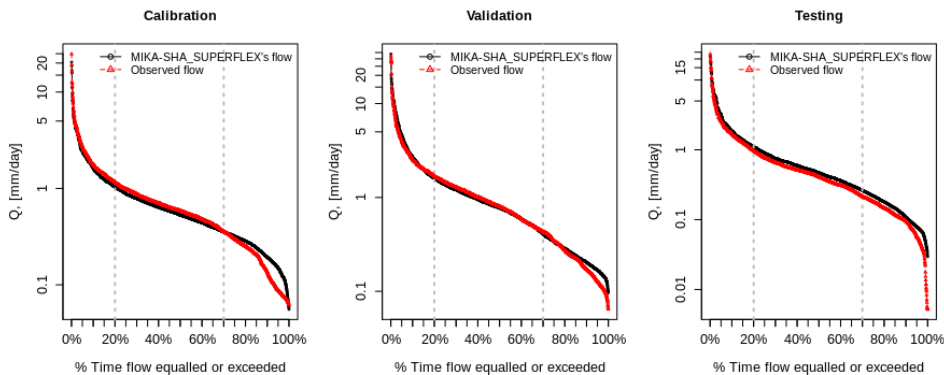



Figure 7: Simulated FDCs of MIKA-SHA_SUPERFLEX with the observed FDCs of the basin

3.2.2 MIKA-SHA models induced using FUSE Library

The identified optimal semi-distributed model for the Rappahannock River basin using the FUSE library of MIKA-SHA is shown in Fig. 8 (hereinafter referred to as MIKA-SHA_FUSE). Hillside, floodplain, and plateau area model structures of MIKA-SHA_FUSE, consisting of the same upper-zone configuration identical to FUSE parent model ARNO-VIC/ TOPMODEL, a single state soil reservoir. Like in the FUSE parent model SACRAMENTO, the lower-layer architecture of the hillside model structure has a tension reservoir with two parallel tanks. The Floodplain model structure incorporates a lower zone configuration like the FUSE parent model TOPMODEL with an unlimited size reservoir with power recession. In comparison, the lower zone configuration of the plateau area model structure consists of single fixed-size storage similar to the ARNO-VIC model. Surface flow from all three model structures is developed as saturation-excess overland flow and described using the flux equations in the FUSE parent model TOPMODEL. Both hillside and plateau area model structures have the same percolation mechanism, allowing water to percolate from the field capacity to saturation, and is described using the flux equations of the FUSE parent model PRMS/ TOPMODEL. In contrast, percolation in the plateau area is controlled by the saturated zone's moisture amount as in the SACRAMENTO model. A root weighting evaporation model is used in hillside and floodplain model structures, while a sequential evaporation model is used in plateau area model structure. Interflow and routing are not allowed in any model structure of MIKA-SHA_FUSE.

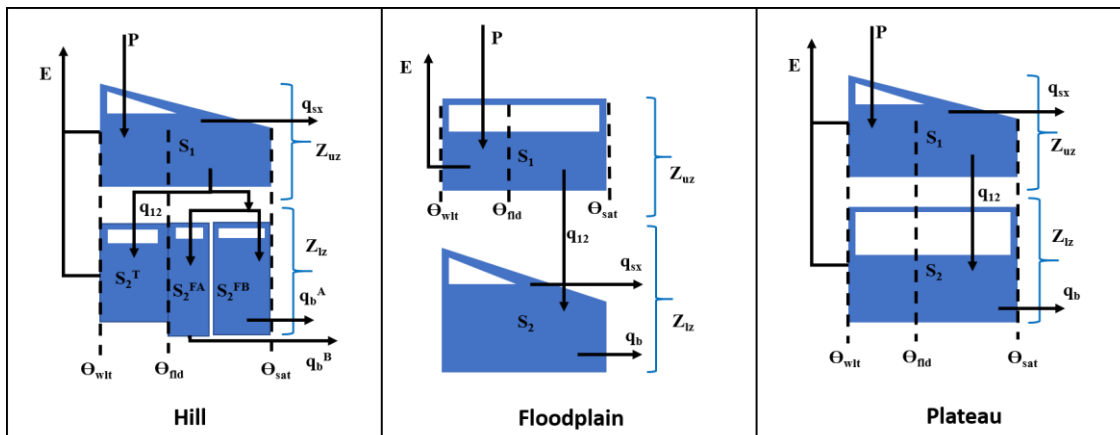



Figure 8: MIKA-SHA_FUSE model configuration (P: precipitation, E: evaporation, q_b: base flow, q_{sx}: surface flow, q_{12}: percolation, Z_{uz}, and Z_{lz}: depth of unsaturated zone and saturated zone, S_1, S_2: unsaturated zone and saturated zone water content, S_2^T: tension water content, $S_2^{FA,}$ and S_2^{FB}: free water content in the primary and secondary baseflow storages, q_b^A and q_b^B: baseflow from the primary and secondary baseflow storages, Θ_{wlt}, Θ_{fld}, Θ_{sat}: soil moisture at wilting point, field capacity and saturation)

The performance matrix of MIKA-SHA_FUSE is presented in Table 6. According to the high-efficiencies, the simulated discharge of MIKA-SHA_FUSE shows a good match with the observed discharge data. Further, MIKA-SHA_FUSE performs

consistently over the calibration, validation, and testing periods. MIKA-SHA_FUSE also demonstrates reasonable prediction accuracy for the two subcatchment outlets. Further, the simulated hydrograph (Fig. 9) of MIKA-SHA_FUSE can reasonably well capture the observed flow signature of the watershed. Simulated FDCs of MIKA-SHA_FUSE are presented in Fig. 10, along with the observed FDCs of the catchment. The simulated FDC at the calibration stage nearly follows the observed FDC and deviates slightly in validation and testing periods. According to the uncertainty analysis, 82.1% of the measured streamflows of the calibration period lie between the 90% uncertainty bands of MIKA-SHA_FUSE. This high percentage value suggests that the parameter uncertainty of MIKA-SHA_FUSE alone sufficiently estimates the total output uncertainty. Out of the total 34 model parameters of MIKA-SHA_FUSE, 11 model-sensitive parameters can be identified. Among them, four are related to hillside model structure (fracten, rtfrac1, percexp, and percfrac), three are related to floodplain model structure (maxwatr_1, rtfrac1, and loglamb), and two are associated with the plateau area model structure (fracten and maxwatr_2). The two lag parameters (lag_HRU and lag_Sub) are the remaining two model-sensitive parameters. Please refer to the Appendix for Sensitivity scatterplots and model parameter details of MIKA-SHA_FUSE.

Table 6: Performance matrix of MIKA-SHA_FUSE

Outlet	Efficiency (Calibration/ Validation/ Testing)			
	KGE	NSE	logNSE	VE
Catchment	0.87/ 0.79/ 0.79	0.77/ 0.66/ 0.76	0.81/ 0.78/ 0.77	0.68/ 0.60/ 0.58
Subcatchment 1	0.73/ 0.71/ 0.86	0.61/ 0.54/ 0.80	0.73/ 0.77/ 0.79	0.64/ 0.58/ 0.64
Subcatchment 2	0.81/ 0.74/ 0.80	0.68/ 0.47/ 0.72	0.77/ 0.78/ 0.77	0.62/ 0.57/ 0.58

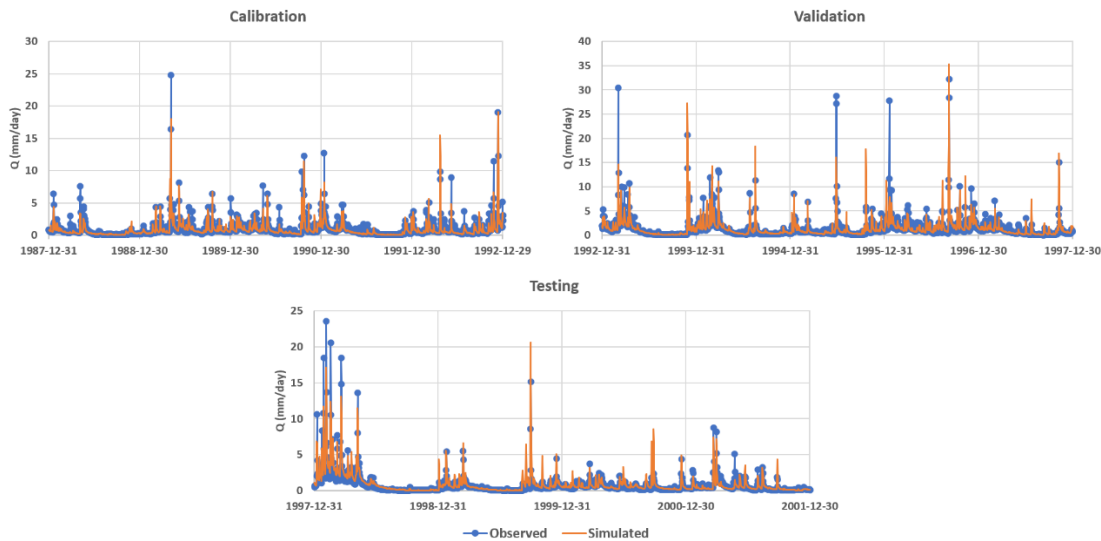



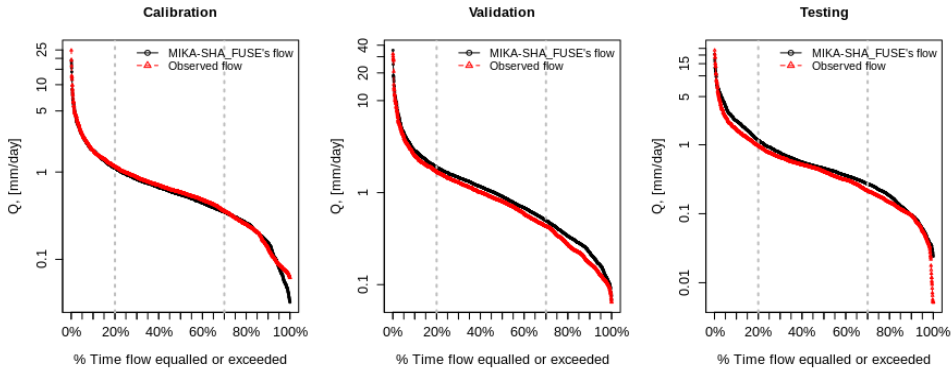
Figure 9: Simulated hydrograph of MIKA-SHA_FUSE with the observed hydrograph of the basin

590

Figure 10: Simulated FDCs of MIKA-SHA_FUSE with the observed FDCs of the basin

3.2.3 Lumped vs. Distributed

This section compares the optimal semi-distributed models identified by MIKA-SHA (MIKA-SHA_SUPERFLEX & MIKA-SHA_FUSE) with lumped models calibrated/ induced for the same Rappahannock River basin. First, two widely used
595 conceptual rainfall-runoff models, the XINANJIANG model (Zhao, 1992) and the HyMOD model (Wagener et al., 2001), are calibrated in the lumped setting (catchment averaged forcing terms from the MOPEX dataset are used) to predict the basin's catchment outflow using a non-machine learning approach. Model codes of both XINANJIANG and HyMOD models were obtained from the MARRMoT framework (Knoben et al., 2019), where model codes of 46 existing hydrological models are provided. Two hydrological models were calibrated using Dynamically Dimensioned Search (DDS) algorithm (Tolson and
600 Shoemaker, 2007) with the same model spin-up and calibration periods. DDS is a single-objective global search optimization algorithm that has been used in many hydrological modelling studies (Shafii and Tolson, 2015; Becker et al., 2019; Spieler et al., 2020). In this study, the DDS algorithm was used with NSE as the objective function. Ten iterations of the DDS algorithm with 5000 model evaluations per one iteration were utilized with each model. The parameter set which gives the highest NSE over the calibration period was identified as the optimum parameter set. For the comparison purpose, VE, KGE, and logNSE
605 values of each model (using the optimum parameter set identified with NSE) were also calculated. The performance matrix of two calibrated models is presented in Table 7. According to the efficiency values, both the XINANJIANG and HyMOD models perform poorly for the Rappahannock basin compared to MIKA-SHA-induced semi-distributed models.

Table 7: Performance matrix of XINANJIANG model and HyMOD model

Model	Efficiency (Calibration/ Validation/ Testing)			
	KGE	NSE	logNSE	VE
XINANJIANG	0.55/ 0.51/ 0.61	0.49/ 0.42/ 0.56	0.70/ 0.68/ 0.65	0.57/ 0.51/ 0.44
HyMOD	0.65/ 0.60/ 0.65	0.57/ 0.52/ 0.63	0.39/ 0.51/ 0.36	0.50/ 0.47/ 0.36

Next, our priorly introduced GP-based ML-RR-MI toolkit was used to induce optimal lumped models for the same Rappahannock River basin using SUPERFLEX and FUSE libraries. ML-RR-MI was run using the same settings given in Table 4. In contrast to the MIKA-SHA, once the ML-RR-MI identifies the competitive models, the most parsimonious model in terms of the number of model parameters is recognized as the optimal model. The model configurations of the two optimal models identified by ML-RR-MI with SUPERFLEX library (hereinafter referred to as ML-RR-MI_SUPERFLEX) and FUSE library (hereinafter referred to as ML-RR-MI_FUSE) are shown in Fig. 11. ML-RR-MI_SUPERFLEX is similar to the plateau area model structure of MIKA-SHA_SUPERFLEX regarding the reservoir units and storage-discharge relationships. Additionally, ML-RR-MI_SUPERFLEX consists of a half-triangular lag function with SR. Interestingly, ML-RR-MI_FUSE's upper- and lower-layer architectures and percolation mechanism are similar to the plateau area model structure of MIKA-SHA_FUSE. In contrast, surface runoff of ML-RR-MI_FUSE is controlled by the upper layer, and the evaporation module is root weighting as in FUSE parent model ARNO-VIC. Further, routing is also allowed in ML-RR-MI_FUSE.

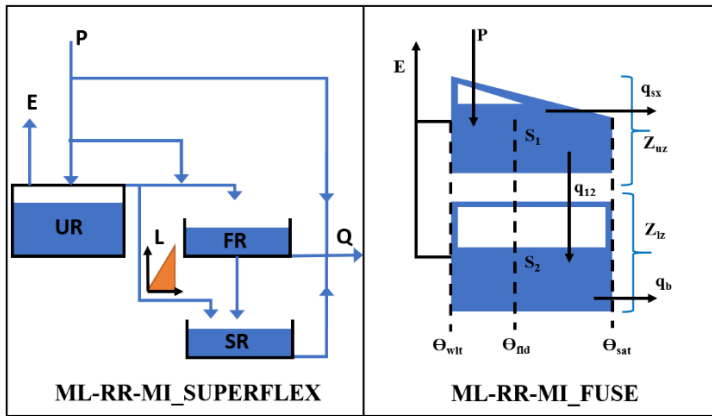



Figure 11: ML-RR-MI_SUPERFLEX and ML-RR-MI_FUSE model configurations (P: precipitation, E: evaporation, Q: total discharge, SR: slow-reacting reservoir, FR: fast-reacting reservoir, UR: unsaturated reservoir, L: half-triangular lag function, q_b: base flow, q_{sx}: surface flow, q_{12}: percolation, Z_{uz}, and Z_{lz}: depth of unsaturated zone and saturated zone, S_1 and S_2: unsaturated zone and saturated zone water content, Θ_{wlt}, Θ_{fld}, Θ_{sat}: soil moisture at wilting point, field capacity and saturation)

The performance matrix of ML-RR-MI_SUPERFLEX and ML-RR-MI_FUSE is given in Table 8. In contrast to the two fixed conceptual models (XINANJIANG & HyMOD), two optimal lumped models identified by ML-RR-MI demonstrate higher prediction capabilities. MIKA-SHA_FUSE model outperforms the ML-RR-MI_FUSE model in all four objective functions over the calibration, validation, and testing periods. However, the ML-RR-MI_SUPERFLEX model outperforms/ equally performs the MIKA-SHA_SUPERFLEX model in the calibration and validation periods. Yet, the MIKA-SHA_SUPERFLEX model outperforms ML-RR-MI_SUPERFLEX in all objective functions over the testing period. As per the workflow of both

MIKA-SHA & ML-RR-MI, calibration and validation periods are used in the optimal model identification process. Therefore, the performance in the testing period demonstrates the out-of-sample performance of induced models.

Table 8: Performance matrix of ML-RR-MI_SUPERFLEX and ML-RR-MI_FUSE

Model	Efficiency (Calibration/ Validation/ Testing)			
	KGE	NSE	logNSE	VE
ML-RR-MI_SUPERFLEX	0.88/ 0.82/ 0.65	0.77/ 0.66/ 0.76	0.80/ 0.77/ 0.67	0.68/ 0.60/ 0.54
ML-RR-MI_FUSE	0.82/ 0.78/ 0.69	0.67/ 0.60/ 0.67	0.78/ 0.77/ 0.75	0.63/ 0.58/ 0.51

4 Discussion

4.1 MIKA-SHA_SUPERFLEX

Among the three model structures of MIKA-SHA_SUPERFLEX, the hillside model structure has the most complex configuration in terms of reservoir units and model parameters. Further, the hillside model structure is correlated with the majority of model-sensitive parameters, and runoff per unit area is also highest in the hillside model structure. Therefore, runoff generation from the hillside structure is a significant component of the total runoff of MIKA-SHA_SUPERFLEX. This is quite meaningful due to the higher topographic gradients in upper subcatchments (subcatchment 1: 23.4 m km^{-1} and subcatchment 2: 30.3 m km^{-1}) of the Rappahannock basin.

On the other hand, the plateau area model structure has the lowest runoff generation per unit area (i.e., highest storage). We find this behaviour of plateau area model structure reasonable as more subsurface oriented delayed response may expect in plateau area due to milder slopes which may result in higher resident times (water may have more time to reach deeper soil layers). Further, most of the catchment area of the Rappahannock basin consists of moderately permeable silty loam and clay loam soils which may also encourage vertical drainage. Conceptually, SRs are used to represent the slow runoff components like groundwater flow. SRs in both hillside and plateau area model structures have linear storage-discharge relationships. Interestingly, it is reported that (Fenicia et al., 2006) linear reservoirs best describe the slow flow dynamics of groundwater movement. Further, the inclusion of stable baseflow components (SRs in both hillside and plateau area model structures) in the model configuration of MIKA-SHA_SUPERFLEX is reasonable because the main river channel of the basin can be categorized as a perennial river where a continuous groundwater supply is required to sustain water throughout the year.

The floodplain model structure of MIKA-SHA_SUPERFLEX has a relatively simple model architecture with only one reservoir. The floodplain area is expected to be saturated or nearly saturated and continuously connected with the stream. In earlier FLEX and SUPERFLEX applications (Savenije, 2010; Fenicia et al., 2016), where the model selection for each HRU was based on expert judgement, a simple linear reservoir model was identified as sufficient enough to represent quick runoff

responses of riparian zones. Consistent with this in the current application, MIKA-SHA also identified a simpler model with one reservoir to capture the runoff dynamics of floodplains. However, the UR in the floodplain model structure has a power function relationship between its discharge and storage. As mentioned earlier, infiltration excess overland flow is included as

660 a runoff component of the floodplain model structure. Often floodplains consist of soil types with poor permeabilities and hence may cause quick runoff generation mechanisms like infiltration excess overland flow. The constitutive functions of FRs and URs in MIKA-SHA_SUPERFLEX are non-linear, which may help capture the non-linear and threshold-like response of runoff generation.

4.2 MIKA-SHA_FUSE

665 The hillside model structure of MIKA-SHA_FUSE has the highest runoff generation per unit area (approximately 2.1 x plateau area runoff generation), followed by the floodplain model structure (about 1.6 x plateau area runoff generation). Interestingly, a similar order was observed with MIKA-SHA_SUPERFLEX. Similar to the hillside model structure of MIKA-SHA_SUPERFLEX, the hillside model structure of MIKA-SHA_FUSE has the most complex model configuration in terms of the number of model parameters and is associated with most of the model-sensitive parameters. Hence, it is clear that runoff

670 generation from the hillside model structure dominates the total runoff generation of MIKA-SHA_FUSE, which is logical due to the high topographic relief of the basin. Further, a high runoff generation in floodplain model structure is meaningful due to high water table levels in floodplains, resulting in quick runoff generation mechanisms like saturation excess overland flow. Comparatively, lower percolation can be expected in floodplain model structure as its percolation is controlled by the moisture content in the lower zone (percolation is higher when the lower zone is dry). This goes in line with the characteristics of

675 floodplains, where most of the time remain saturated or nearly saturated.

On the other hand, a comparatively lower runoff contribution from the plateau area model structure is reasonable as more vertical drainage can be expected than lateral drainage in plateau areas due to milder slopes and moderately permeable soil types. As per the calibrated model parameters and model-sensitive parameters, runoff from the plateau area model structure is dominated by the subsurface flow component. Lower-layer reservoirs of both floodplain and plateau area model structures

680 consist of non-linear storage-discharge relationships (baseflow), which may help them capture the non-linear runoff response of the Rappahannock basin. In contrast, baseflow from the hillside model structure is generated through two parallel linear reservoirs.

4.3 Model induction capability of MIKA-SHA

The proposed MIKA-SHA toolkit incorporates spatial heterogeneity in catchment properties and forcing terms into the model

685 building phase and induces representative semi-distributed rainfall-runoff models based on measured data to capture the discharge response of watershed of interest. In comparison to the lumped model performances presented in Sect. 3.2.3, two optimal semi-distributed models identified by MIKA-SHA with FUSE and SUPERFLEX libraries achieve higher efficiency

values, especially for the testing period. The difference in efficiency values is significant between MIKA-SHA-induced semi-distributed models and two fixed lumped hydrological models (XINANJIANG and HyMOD). MIKA-SHA-induced semi-distributed models may achieve high-efficiency values than fixed hydrological models used in this study due to (i) flexibility offered by modular modelling frameworks to customize the model structure in contrast to the single model structure in fixed hydrological models, (ii) incorporation of spatial heterogeneity in catchment properties and climate variables, (iii) capability of GP based machine learning framework to optimize both model structure and parameters over non-machine learning method.

Even though the two fixed lumped models could not achieve satisfactory performance, two lumped models induced by our priorly introduced ML-RR-MI toolkit performed well in capturing the Rappahannock River basin runoff response. This demonstrates the capability of lumped models to perform satisfactorily, even for large catchments with substantial spatial heterogeneities. However, the inferences gain through a lumped model for a large watershed may be limited, and the lumped representation may not reflect the physical reality in runoff generation. As seen with MIKA-SHA_SUPERFLEX and MIKA-SHA_FUSE, the inferences made through the semi-distributed models are much meaningful and compatible with catchment characteristics. On top of that, MIKA-SHA-induced models have a unique advantage over the lumped models of predicting discharge inside the watershed (at subcatchment outlets).

In this study, spatial heterogeneity of the catchment was incorporated into the model building process based on the topography (i.e., three HRUs, namely hills, floodplain, and plateau, were identified based on the topography of the area). The results obtained based on topography-based HRUs, such as achieving high-efficiency values for the absolute performance measures and obtaining a good visual equivalent between measured and modelled hydrographs, suggest that topography of the catchment may have a strong impact on runoff generation. This illustrates another potential utilization of the MIKA-SHA to use the toolkit to identify the runoff drivers of a catchment of interest. For example, one can also define the HRUs based on either geology or soil type of the catchment of interest and use MIKA-SHA to identify optimal model configurations. This way, one can determine the relative dominance of runoff drivers towards the total catchment runoff response.

One of the major issues with machine learning models is the overfitting of the model to its training dataset. However, the optimal model selection strategy used in MIKA-SHA, which considers both calibration and validation model performances, ensures the selected optimal model performs satisfactorily not only in the training period (more generalizability). Deterministic semi-distributed modelling would require/ rely on a large number of model parameters, by comparison, a smaller number of model parameters are sensitive towards the total model performance. Further, the values of two lag parameters associated with the DISTRIBUTED function (lag_HRU and lag_Sub) were found to be crucial in achieving high model performances. As the research findings of MIKA-SHA demonstrate a logical match with previously reported research findings and fieldwork insights, it may be safe to assume that MIKA-SHA is capable of handling equifinality phenomenon satisfactorily (i.e., selected optimal models perform for the right reasons). Additionally, the quantitative model selection scheme of MIKA-SHA ensures

the selected optimal model has the appropriate complexity to describe the dominant runoff generation processes of the catchment instead of selecting an optimal model only based on model parsimony.

More importantly, both MIKA-SHA_SUPERFLEX and MIKA-SHA_FUSE share similarities among their model configurations, such as model outflows dominated by the runoff generated through hillside model structures, having the most complex configurations for hillside model structures, demonstration of more subsurface type delayed responses by plateau area model structures. Further, finding a reasonable match between the model structural components of optimal models and the catchment characteristics was possible. This consistency and compatibility demonstrated by the MIKA-SHA in capturing similar runoff dynamics across different model inventories show that the toolkit is capable of extracting information from data, making it feasible to depend on the derived model configurations beyond just statistical confidence.

5 Conclusions

In this contribution, we introduce Model Induction Knowledge Augmented-System Hydrologique Asiatique (MIKA-SHA) for learning semi-distributed models where the spatial distributions of catchment properties and climate variables are taken into account. MIKA-SHA utilizes the existing hydrological knowledge to guide the machine learning algorithm, which eventually results in physically meaningful hydrological models that can be readily interpretable by domain specialists. In the current study, background hydrological knowledge is blended with the machine learning algorithm through the model building components of flexible rainfall-runoff modelling frameworks.

Results of this study indicate that the consideration of spatial distributions of forcing data and catchment properties gives more meaningful insights regarding the environmental dynamics occurring within the watershed. MIKA-SHA's unique and distinct feature is that it can be combined with any internally coherent set of building blocks reflecting the hydrological knowledge elements. Further, it uses genetic programming to optimize both model architecture and model parameters simultaneously. This approach enables hydrologists to utilize flexible modelling frameworks to their full potential by trying many hypotheses before selecting an optimal model. By automatically identifying optimal model structures for a catchment of interest relying on adequacy in place of legacy, MIKA-SHA can serve as an alternative to the conventional subjective model selection. MIKA-SHA is expected to be most valuable in circumstances where there may be a lack of experimental insights regarding the catchment of interest or human expert's knowledge.

We see machine learning algorithms as having great potential in hydrological modelling. However, simplistic black-box type data-driven models may contribute to developing accurate models with severe interpretation difficulties that may not advance hydrological understanding. Thus, the most promising way forward would be to integrate current hydrological understanding with learning algorithms to generate physically consistent and more generalizable models. This was the driving force behind the proposed MIKA-SHA framework's development, which has been founded on both machine learning and hydrological

theories. As a result, we anticipate that current research will reinforce the connection between two important but traditionally separate communities in water resources: those operating with machine learning and those dealing with theory-based modelling. Lastly, we foresee that more theory-guided machine learning research in hydrological modelling will be geared towards automated model building and knowledge discovery.

Appendix A

Table A1: Model parameter details of ML-RR-MI_SUPERFLEX & MIKA-SHA_SUPERFLEX

Model parameter (Unit/ Range/ Symbol)	ML-RR-MI SUPERFLEX	MIKA-SHA_SUPERFLEX		
		Hill	Flood	Plateau
K in $Q = K*(S)$ from RR (t^{-1}/ 0.05 – 4/ K_Qq_RR)	-	0.476	-	-
Fraction of inflow to RR (No units/ 0 – 1/ D_R)	0.003	0.083	-	-
K in $Q = K * S^{\alpha}$ of FR ($mm^{\alpha}\ t^{-1}$/ 0.0001 – 10/ K_Qq_FR)	10	1.790	-	1.084
K in $Q = K*S$ from FR to SR (t^{-1}/ 0 – 4/ K_Qb_FR)	1.86	4	-	4
Smoothing parameter for E of FR (No units/ 0.01- 2/ m_E_FR)	1.679	0.815	-	0.262
α in $Q = K * S^{a}$ of FR (No units/ 0.1 – 10/ α_Qq_FR)	9.745	7.394	-	7.394
Portion of inflow from Q_{UR} to SR (No units/ 0 – 1/ D_F)	0.273	0.093	0	0
Evaporation multiplying parameter (No units/ 0.1 – 2/ Ce)	0.795	2	0.935	1.015
Base of rising limb of half triangular lag (t/ 1 – 10/ Tlag)	2.415	2.368	-	-
Portion of rainfall to FR (No units/ 0 – 1/ D_S)	0.09	-	0.02	-
Runoff coefficient parameter of UR (No units/ 0.001 – 10/ β_Qq_UR)	2.942	4.559	10	5.989
Maximum reservoir capacity (mm/ 0.1 – 1000/ Smax_UR)	159.7	114.8	159.3	191.8
Smoothing parameter for E of UR (No units/ 0.01 – 5/ Beta_E_UR)	0.010	0.138	0.355	0.201
State initial factor (No units/ 0 - 0.1/ SiniFR_UR)	0.073	0.046	0.062	0.072
Parameter of modified logistic curve (No units/ 0.1 – 0.2/ mu_Qq_UR)	-	0.155	-	-
K in $Q = K * S^{\alpha}$ of SR ($mm^{\alpha}\ t^{-1}$/ 1e-7 - 0.6/ K_Qq_SR)	0.146	0.046	-	0.060
Smoothing parameter E of SR (No units/ 0.001 – 1/ m_E_SR)	0.193	0.001	-	0.192
Infiltration excess threshold (mm t^{-1}/ 0.1 - 1e7/ P_ED_max)	-	-	0.1	-
Infiltration excess flow smoothing factor (mm t^{-1}/ 0.001 – 10/ m_P_ED)	-	-	10	-
Time delay-HRU to subcatchment outlet (t/ 0.01 – 5/ lag_HRU)	-	1.570		
Time delay-Subcatchment to catchment outlet (t/ 0.01 – 5/ lag_Sub)	-	0.404		

* For more details, please refer to Fenicia et al. (2016)

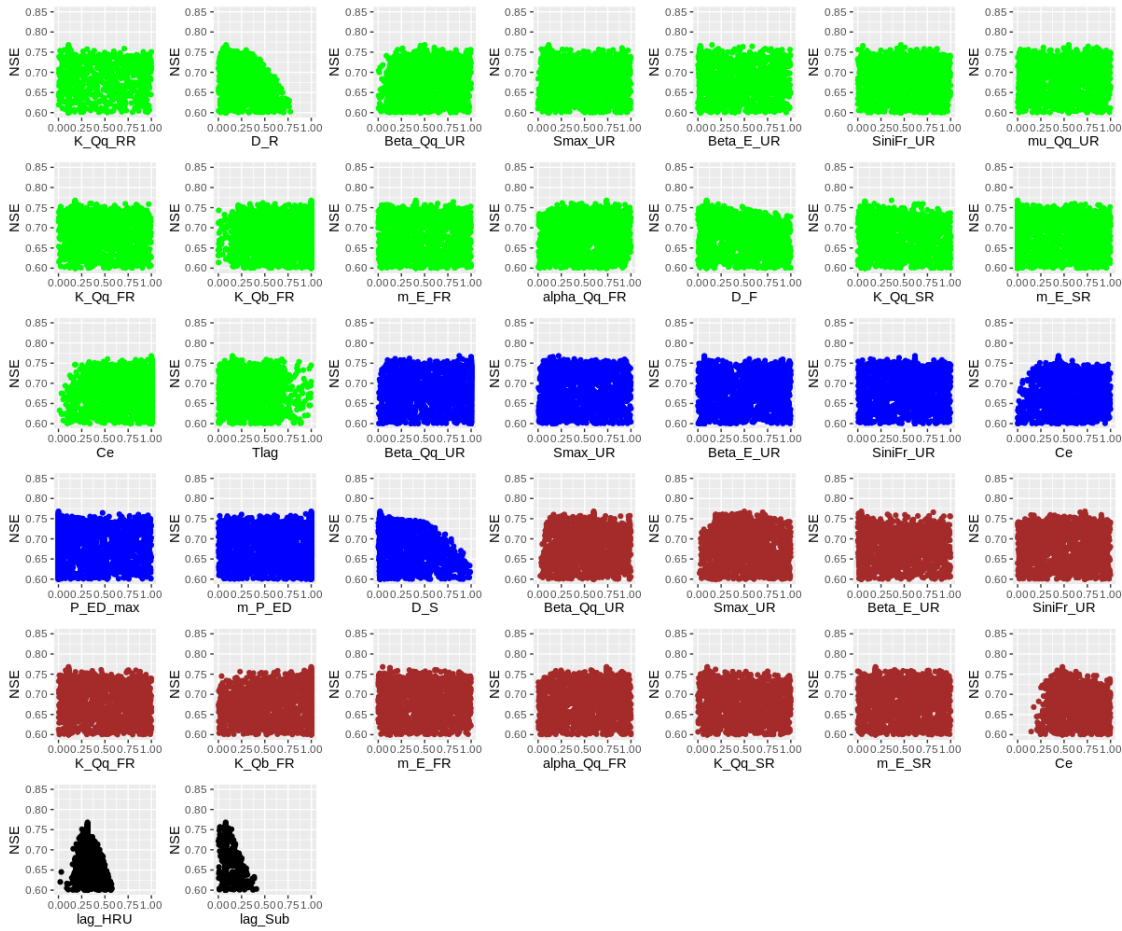



Figure A1: Sensitivity scatter plots of MIKA-SHA_SUPERFLEX

Table A2: Model parameter details of ML-RR-MI_FUSE & MIKA-SHA_FUSE

Model parameter (Unit/ Range/ Symbol)	ML-RR-MI _FUSE	MIKA-SHA_FUSE		
		Hill	Flood	Plat.
Maximum total storage in upper soil layer (mm/ 25 – 500/ maxwatr_1)	142.6	165.1	250.5	121.0
Maximum total storage in lower soil layer (mm/ 50 – 5000/ maxwatr_2)	745.7	2399.4	3739.5	995.5
Fraction total storage as tension storage (No units/ 0.05 - 0.95/ fracten)	0.467	0.685	0.495	0.573
Fraction storage in 1st baseflow reservoir (No units/ 0.05 - 0.95/ fprimqb)	-	0.95	-	-
Percolation rate (mm day^{-1}/ 0.01 - 1000/ percrte)	94.8	214.2	-	192.1
Percolation exponent (No units/ 1 – 20/ percexp)	16.52	11.05	-	11.10
Fraction of percolation to tension storage (No units/ 0.05 - 0.95/ percfrac)	-	0.858	-	-
Range of the baseflow rate (No units/ 0.001 – 1000/ baserte)	662.1	-	380.2	139.9

Baseflow exponent (No units/ 1 – 10/ qb_powr)	4.753	7.708	3.785	7.205
Baseflow depletion rate 1st reservoir (day^{-1}/ 0.001 - 0.25/ qbrate_2a)	-	0.002	-	-
Baseflow depletion rate 2nd reservoir (day^{-1}/ 0.001 - 0.25/ qbrate_2b)	-	0.223	-	-
Mean value:log-transformed topographic index (m/ 5 – 10/ loglamb)	6.129	8.957	9.176	6.418
Shape para: topo index gamma distribution (No units/ 2 – 5/ tishape)	2.284	2.134	3.201	3.621
Range of the fraction of roots in the upper layer (No units/ 0.05 - 0.95/ rtfrac1)	0.721	0.634	0.878	-
SAC percolation multiplier for dry soil layer (No units/ 1 – 250/ sacpmlt)	-	-	71.6	-
SAC percolation exponent for dry soil layer (No units/ 1 – 5/ sacpexp)	-	-	4.193	-
Time delay in runoff (day/ 0.01 – 5/ timedelay)	2.548	-	-	-
ARNO/VIC model "b" exponent (No units/ 0.001 – 3/ axv_bexp)	0.048	-	-	-
Time delay-HRU to subcatchment outlet (day/ 0.01 – 5/ lag_HRU)	-	1.332		
Time delay-Subcatchment to catchment outlet (day/ 0.01 – 5/ lag_Sub)	-	0.207		

* For more details, please refer to Clark et al. (2008, 2011)

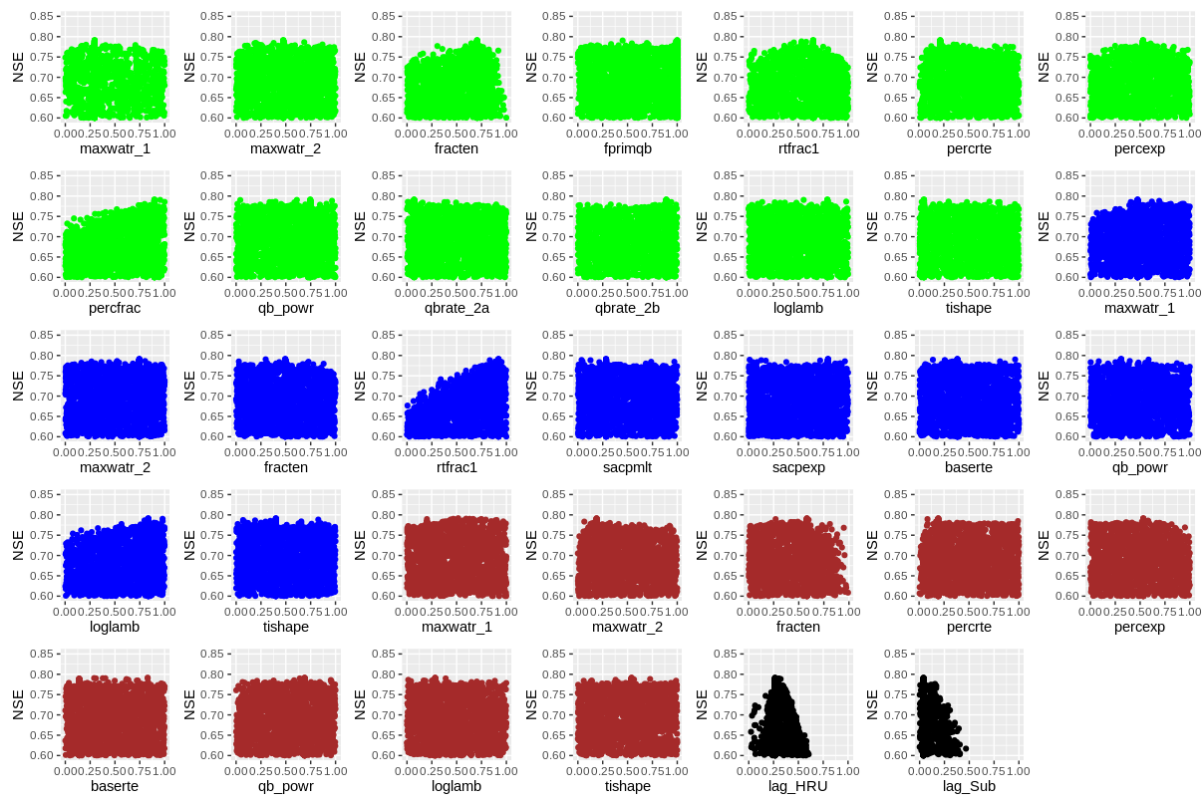



Figure A2: Sensitivity scatter plots of MIKA-SHA_FUSE

Data Availability

The data sets used in this study are publicly available through the references given in the manuscript.

Author Contribution

H. M. V. Vidura Herath: Conceptualization, Formal Analysis, Methodology, Software, Visualization, Writing – original draft

Jayashree Chadalawada: Conceptualization, Methodology, Software

Vladan Babovic: Conceptualization, Project administration, Supervision, Writing – review & editing

Competing Interests

The authors declare that they have no conflict of interest.

Acknowledgements

We greatly appreciate the support given by Dr. Vojtech Havlicek in R programming. Further, we acknowledge Dr. Fabrizio Fenicia for his assistance in SUPERFLEX framework.

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