



# Geophysically-based analysis of BTCs and ion exchange processes in soil

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**Abstract.** Breakthrough curves (BTCs) are a valuable tool for qualitative and quantitative examination of transport patterns in porous media. Although breakthrough (BT) experiments are simple, they often require extensive sampling and multi-component chemical analysis. In this work, we examine spectral induced polarization (SIP) signals measured along a soil column during a BT experiment in a homogeneous and heterogeneous soil profiles. Soil profiles were equilibrated with an  $NaCl$  background solution and then a constant flow of  $CaCl_2$  solution was applied. SIP signature was recorded, and complementary ion analysis was performed on the collected outflow samples. Our results confirm that changes to the pore-water composition, ion exchange processes and profile heterogeneity are detectable by SIP: the real part of the conductivity-based BTCs clearly indicated the BT of the non-reactive ions as well as the retarded BT of  $Ca^{2+}$ . The imaginary part of the conductivity-based curves reacted to the changes in ion mobility around the electrical double layer (EDL) and indicated the initiation and the termination of the  $Na^+ - Ca^{2+}$  exchange reaction. Finally, both the real and imaginary components of the complex conductivity reacted to the presence of a coarser textured layer in the heterogeneous profile.



## 1 Introduction

Breakthrough curves (BTCs) are a well accepted, convenient laboratory-scale method for evaluation of solute transport parameters in porous media. Arguably, these are the most important measurements needed for proper design of soil and groundwater remediation plan. Evaluation of advective velocity, dispersion coefficients and retardation factors using BTCs have been shown in multiple studies over the last decades (Cameron and Klute , 1977; Yamaguchi et al. , 1989; Vereecken et al. , 1999). The conventional laboratory setup for breakthrough (BT) experiments involves the injection of an inflow solution through a porous media profile; outflow samples are collected and analyzed for ionic composition. However, this conventional setup has drawbacks. Above all, since samples are taken only from the outflow, the obtained curves represents an integrated transport pattern of the solutes along the soil profile. This means that there is no consideration of soil heterogeneity. Additionally, in many cases, full outflow composition analysis requires the use of several analytical instruments and is time consuming and hence, it is often replaced by outflow electrical conductivity (EC) measurements.

The EC of a solution is a measure of its ability to carry an electrical charge and varies with the number and the type of ions present in the solution (Sawyer and McCarty , 1978). As a result, EC measurements provide a rapid estimate of the total dissolved species in water samples. Shackelford et al. (1999) investigated the factors affecting the applicability of EC-based BTCs as an indicator of chemical equilibrium between the effluent and inflow solution. Their findings showed that the shapes of EC-based BTC is a function of the flow rate, the solute retardation factor (that is primarily related to ion exchange processes), and to some extent the species of cation and anion in the inflow solution as well as the cations initially occupying the exchangeable component of the soil. They concluded that EC-based BTCs offer a simple, practical, and inexpensive method for determining chemical equilibrium in laboratory tests. However, since EC primarily reflects the amount of ions in the sample, it is insensitive to changes in ionic composition of the outflow when its overall ionic strength is not significantly altered. This may be a pitfall when exchange processes between the inflow cation and the adsorbed species are involved.

Hydrogeophysics is an emerging field of science that is looking for ways to infer hydrological properties and system states in a minimally invasive, minimally destructive fashion (Binley et al. , 2015). Induced polarization (IP) is of special interest to reactive transport, as it is sensitive to processes at the solid-liquid interface, as well as to the electrolyte properties. In the field of contaminant hydrology, a significant number of studies attempted to use IP methods to detect contamination in the field scale (Sogade et al. , 2006; Masi et al. , 2015). The geoelectrical signature is known to be a composite signature of the porous media itself, the chemical composition of the aqueous phase, the non-aqueous free phases, if such exist (e.g. air, oil) (Shefer et al. , 2013), exchange processes (Schwartz et al., 2012; Schwartz et al. , 2012b), degradation byproducts (Abdel Aal et al. , 2004, 2009, 2014; Schwartz et al. , 2014) and the soil microbial population (Abdel Aal et al. , 2010; Mellage et al. , 2018).

Five main mechanisms control the geophysical signature associated with IP in porous media. First is the conduction of charge by the electrolyte (the soil pore-water), which is often described by Archie's law (Archie et al. , 1942) or its derivatives. The



Electrical Double Layer (EDL) polarization mechanism is also relevant in the low range of frequencies characteristic to IP. The EDL polarization mechanism suggests that the polarization of the EDL in the presence of an external electric field is primarily the result of movement of ions in the stern layer. This suggests that the polarization is primarily affected by the grain size, grain electrical properties (e.g. site density, cation exchange capacity (CEC)), and the composition of the ions sorbed to the soil grain (Leroy et al. , 2009). The electrolyte conductivity and the EDL polarization are assumed to be the most relevant to this study. Other mechanisms include the membrane polarization, that is related to the formation of membrane-like features at bottlenecks between adjacent soil grains, the interfacial (or Maxwell-Wagner) polarization, that is related to charge accumulation at dielectric interfaces, and is typically relevant only in higher frequencies (e.g. above 1kHz), and the electroodic polarization that is relevant at the presence of metallic bodies (Ishai et al. , 2013).

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In this work, we use the sensitivity of spectral IP (SIP) to changes in pore-water electrolytic composition and charge storage in order to study transport patterns in a simple system, involving a non-reactive anion and two cations undergoing an exchange process. We aim to demonstrate the ability to accurately indicate the BT of the transported species and the initiation and termination of the cation exchange process using SIP. Additionally, we aim to show that profile's spatial heterogeneity (that wouldn't be inferred by chemical analysis) is easily detectable by SIP-based BTCs.

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## 2 Materials and Methods

### 2.1 Spectral Induced Polarization

In classic IP (time domain), an electrical current is injected into the soil profile through two electrodes, and the potential is measured between two other electrodes, focusing on the potential build-up after the initiation of the current (or its cease). In SIP (the method used here), an alternating current in wide range of frequencies is injected, and the phase and amplitude difference between the injected and induced potential is measured.

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The complex conductivity signal can be written as

$$\sigma^* = \frac{1}{\rho^*} = |\sigma^*| \exp(i\phi) = \sigma' + i\sigma'' \quad (1)$$

where  $\rho^*(\Omega m)$  is the complex electrical resistivity (i.e., the reciprocal of the conductivity),  $i^2 = -1$  is the imaginary unit,  $\phi(rad)$  is the phase shift, and  $\sigma'(S/m)$  and  $\sigma''(S/m)$  are the real and imaginary parts of the complex conductivity, respectively. Both the real and the imaginary parts of the complex conductivity are related to grain surface interactions; the real part is also related to the conductivity of the pore-water electrolyte composition. (Grunat et al. , 2013)

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$$\sigma^* = (\sigma'_{el} + \sigma'_{surf}) + i\sigma''_{surf} \quad (2)$$



75 where  $\sigma'_{el}(S/m)$  is the electrolyte conductivity,  $\sigma'_{surf}(S/m)$  and  $\sigma''_{surf}(S/m)$  represent the contribution of surface processes to the real and imaginary parts of the complex conductivity, respectively.

To link between surface processes (specifically, the characteristics of the EDL) during the SIP measurement and the complex conductivity signal, the Nernst-Planck equation should be solved, considering the influence of the external electric field expressed by Ohm's law. The resulting expression connects the mobility of ions in the stern layer to the complex surface conductivity (Leroy et al. , 2009).

$$\sigma_s^* = \frac{2}{r_0} (\Sigma_s + \Sigma_d) - \frac{2}{r_0} \frac{\Sigma_s}{1 + i\omega\tau_0} \quad (3)$$

where  $r_0(m)$  is the grain radius,  $\Sigma_s(S)$  is the conductance of the stern layer,  $\Sigma_d(S)$  represents the contribution of the diffuse layer,  $f(Hz)$  is the frequency,  $\omega = 2\pi f(rad/s)$  is the angular frequency of the current,  $\tau_0 = \frac{r_0^2}{2D}$  is the relaxation time constant ( $s$ ) and  $D(m^2/s)$  is the diffusion coefficient of the counter ion at the stern layer.

Both  $\Sigma_s$  and  $\Sigma_d$  are related to the mobility of ions in the EDL. Under the assumption that only one specie is adsorbed to the mineral surface (i.e. mono-ionic system), and that the electrolyte is composed of N species, the stern and diffuse layer conductance are given by

$$90 \quad \Sigma_s = e|z|\beta\Gamma_s \quad (4)$$

$$\Sigma_d = e\sum_{j=1}^N |z_j|\beta_j\Gamma_{j,d} \quad (5)$$

where  $e = 1.6 \times 10^{-19}C$  is the elementary charge,  $z$  is the valence of the ion,  $\beta(m^2/sV)$  is the ion mobility,  $\Gamma_s(1/m^2)$  and  $\Gamma_d(1/m^2)$  are the surface site densities of the stern and diffuse layer respectively.

## 95 2.2 Laboratory setup

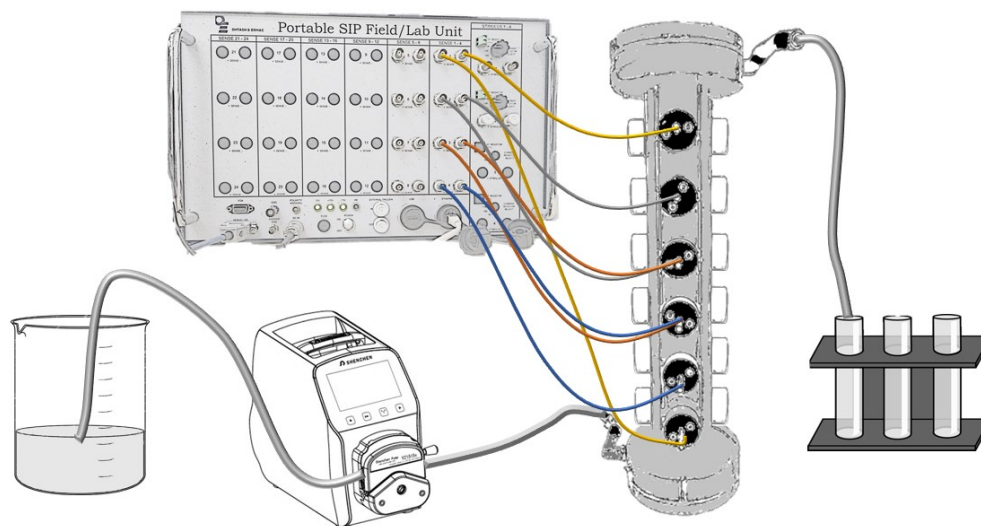
The laboratory setup included a Polycarbonate column (3 cm inner diameter, 32cm long) equipped with 6 brass electrodes at equal spacing of 4cm. The top and the bottom electrodes were used to inject the electrical current into the soil profile (and were fully penetrating the soil column), and the remaining four electrodes were used to measure the potential between each pair. The soil column was connected through the electrodes to a portable SIP device (Ontash and Ermac Inc., NJ) using alligator clips. Inflow solution entered the column through its bottom using a peristaltic pump to create saturated flow (a constant flow of 1.3mL/min) and outflow fractions were collected (see Fig.1).

Two experiments were performed: the first included a homogeneous loam profile (calcareous loamy sand) and the second was a layered profile that included the same soil, but had a 3cm sand layer in the middle. Throughout the experiments, the SIP signal was recorded at frequencies of 0.1 – 10,000Hz. The impedance and phase shift data were used to calculate the real and



105 imaginary conductivity. Additional information regarding the soil composition and column packing is in the supplementary material.

Experiments started with the injection of a background solution into the column ( $NaCl$   $200\text{ mg/L}$ ,  $EC \approx 580 \mu\text{S/cm}$ ). The background solution injection proceeded until equilibrium between the inlet and the outlet EC was obtained. Subsequently to the EC stabilization, the inflow background solution was replaced by a  $CaCl_2$  solution ( $360 \text{ mg/L}$ ,  $EC \approx 1080 \mu\text{S/cm}$ ).



**Figure 1.** Laboratory setup: the inflow solution is pumped into the column from its bottom and the outflow is collected in fractions. SIP signal is measured between three sets of potential electrodes: channel 1 (blue), channel 2 (orange) and channel 3 (grey). The current is injected between the top and bottom electrodes (yellow).

### 110 2.3 Complementary analysis

The outflow solution was collected in equal-volume fractions. Immediately after the collection of each sample, its EC was measured using an EC meter (Eutech con 700). Each sample was then passed through a  $0.22\mu\text{m}$  cellulose filter and analyzed for  $Cl^-$  using an Ion Chromatograph (881 compact IC pro, Metrohm) and for  $Na^+$  and  $Ca^{2+}$  by inductively coupled plasma (ICP OES; iCAP 6000).

### 115 2.4 Modeling

A simple solute transport model was constructed based on the HYDRUS 1D platform (Simunek et al. , 1998). Hydrus 1D is a computer software for numerical modeling of water flow and solute transport in porous media. The inverse tool of Hydrus 1D was applied to fit model parameters to experimental results, based on the Levenberg-Marquardt nonlinear minimization



method (Marquardt , 1963). The appropriate mass balance equation for this application is given by the advection-dispersion  
120 equation (ADE)

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial l} \left( D \frac{\partial C}{\partial l} \right) - \frac{\partial}{\partial l} (vC) \quad (6)$$

where  $l(cm)$  is the vertical coordinate,  $v(cm/h)$  is the water velocity,  $D(cm^2/h)$  is the hydrodynamic dispersion coefficient and  $t(h)$  is time.

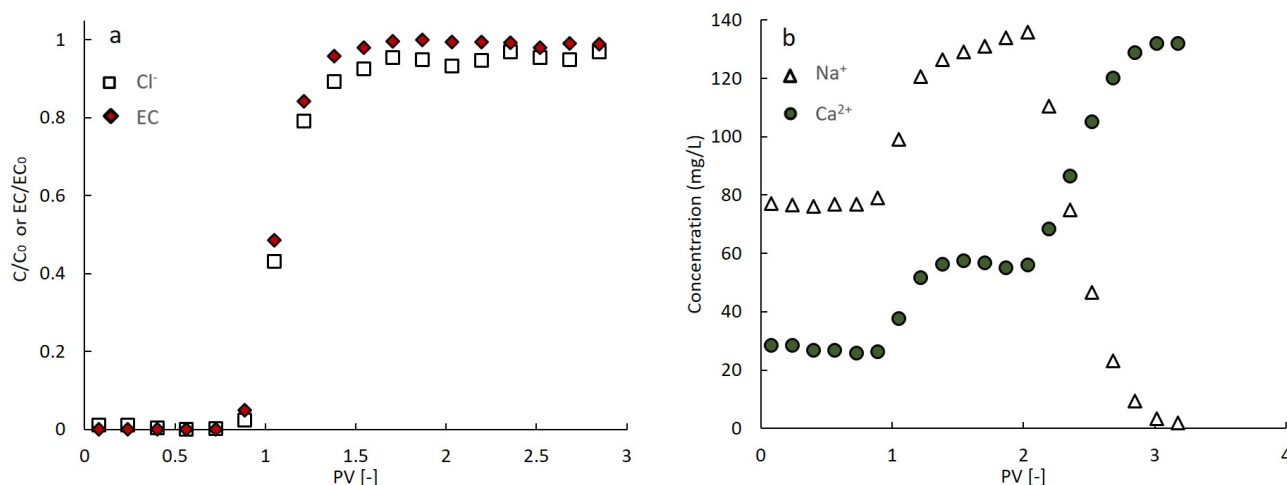
125 Here, the boundary flux was determined based on the measured flow and column cross-section. The hydrodynamic dispersion coefficient ( $D$ ), the soil porosity ( $n$ ) and saturated hydraulic conductivity ( $K_s$ ) were fitted using the inverse tool.

### 3 Results and discussion

Figure 2a presents the measured outflow  $Cl^-$  concentrations and EC values versus pore-volume ( $PV[-]$ ; one pore-volume is equivalent to  $\sim 82$  minutes). Both the  $Cl^-$  and EC outflow values along time fit the expected BT pattern of a non-reactive solute:  
130 the ratio of solute concentration ( $C$ ) to its inflow concentration ( $C_0$ ) is equal to  $\frac{1}{2}$  approximately after  $1PV$  ( $PV(\frac{C}{C_0} = \frac{1}{2}) \approx 1$ ).  $Na^+$  and  $Ca^{2+}$  dynamics during the  $CaCl_2$  injection are described in Fig. 2b.  $Na^+$  outflow concentrations increased in parallel to the increase in outflow  $Cl^-$ . This observation is explained by the fact that the injection of the  $CaCl_2$  solution started after an equilibrium between the background solution and the soil was reached. At this point, the  $Na^+$  concentration in the pore water was already equal to its concentration in the inflow solution ( $\frac{C}{C_0} = 1$ ) and therefore  $Na^+$  behaved as an inert solute. As  
135 the  $CaCl_2$  solution entered the column, adsorbed  $Na^+$  ions were replaced by  $Ca^{2+}$  and hence the  $Na^+$  outflow concentration increased further. In parallel to the increase in outflow  $Na^+$ , a moderate increase in outflow  $Ca^{2+}$  was observed. This early increase in outflow  $Ca^{2+}$  represents the fraction of the inflow  $Ca^{2+}$  ions that did not participate in the  $Na^+ - Ca^{2+}$  exchange reaction (note the timing at  $\sim 1.1PVs$ ). Subsequently to the completion of the  $Na^+ - Ca^{2+}$  exchange, a decrease in outflow  $Na^+$  concentrations was observed while outflow  $Ca^{2+}$  increased and reached its inflow concentration.

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Outflow EC values (Fig.2a) increased in a similar pattern to the  $Cl^-$  ions and reached their maximal value after  $\sim 1.1PVs$ . The major changes in the ionic composition of the outflow during the  $Na^+ - Ca^{2+}$  exchange reaction (see Fig.2b) were not reflected in the EC measurements. This observation is consistent with the findings of Shackelford et al. (1999); in their study, they combined experimental observations and theoretical approach to investigate EC-based BTCs. They used a sodium-saturated  
145 clay soil (sodium bentonite) and a  $CaCl_2$  solution as the inflow solution. Their results showed that while the EC-based BTC matched the  $Cl^-$  BT pattern, reaching its maximal value after  $\sim 1.5PVs$ , it stayed stable afterwards and did not reflect the subsequent decrease in outflow  $Na^+$  and increase in outflow  $Ca^{2+}$ , similarly to the presented here.



**Figure 2.** Outflow values along time of (a) Measured  $Cl^-$  and EC (empty rectangles and red rhombi), and (b)  $Na^+$  and  $Ca^{2+}$  ions (empty triangles and green circles).

Figure 3a presents the real component of the complex conductivity at 1Hz versus time at three locations denoted as channel 1, channel 2 and channel 3, for the homogeneous loam profile (raw SIP spectra are presented in the supplementary material). The values of the real conductivity along time depicted the general shape of a BTC: a gradual increase in  $\sigma'$  was followed by stabilization of the signal around its maximal value. The  $\sigma'$ -based BT pattern at the different channels was consistent with the location of the electrode pairs: BT was first observed at channel 1 (blue), which is the closest to the inlet, then at channel 2 (orange) and lastly at channel 3 (grey). Further, the values of  $\sigma'$  along time are in agreement with the measured EC values presented in Fig.2a. In all three channels, the signal was initially stable at around  $580 \mu S/cm$  and stabilized on its maximal value ( $\sigma'_0$ ) at  $\sim 1055 \mu S/cm$  ( $\frac{\sigma'}{\sigma'_0} = 0.976$ ).

As discussed above,  $Cl^-$  BT was observed at around 1.1PV (equivalent to around 1.5h; see Fig 2a). A HYDRUS 1D-based model was used in order to evaluate the similarity between the obtained  $\sigma'$ -based curves (between 0 – 1.5h) and the expected transport pattern of  $Cl^-$  through the profile. In the model fitting process, the  $\sigma'$  time series were used as a proxy for concentration. This approach was used before; Moreno et al. (2015) used electrical resistivity tomography (ERT) to monitor the water dynamics under a drip-irrigated citrus orchard. They presented a coupled flow and transport model that was calibrated using electrical conductivity measurements with the pore-water electrical conductivity serving as a pseudo-solute.

Here, the  $\sigma'$ -based BTCs of all three channels were normalized to a scale of 0 to 1 and the HYDRUS inverse tool was used to fit the model parameters. The obtained dispersion coefficient, porosity and saturated hydraulic conductivity were  $15(cm^2/h)$ , 47% and  $11.38(cm/h)$ , respectively.

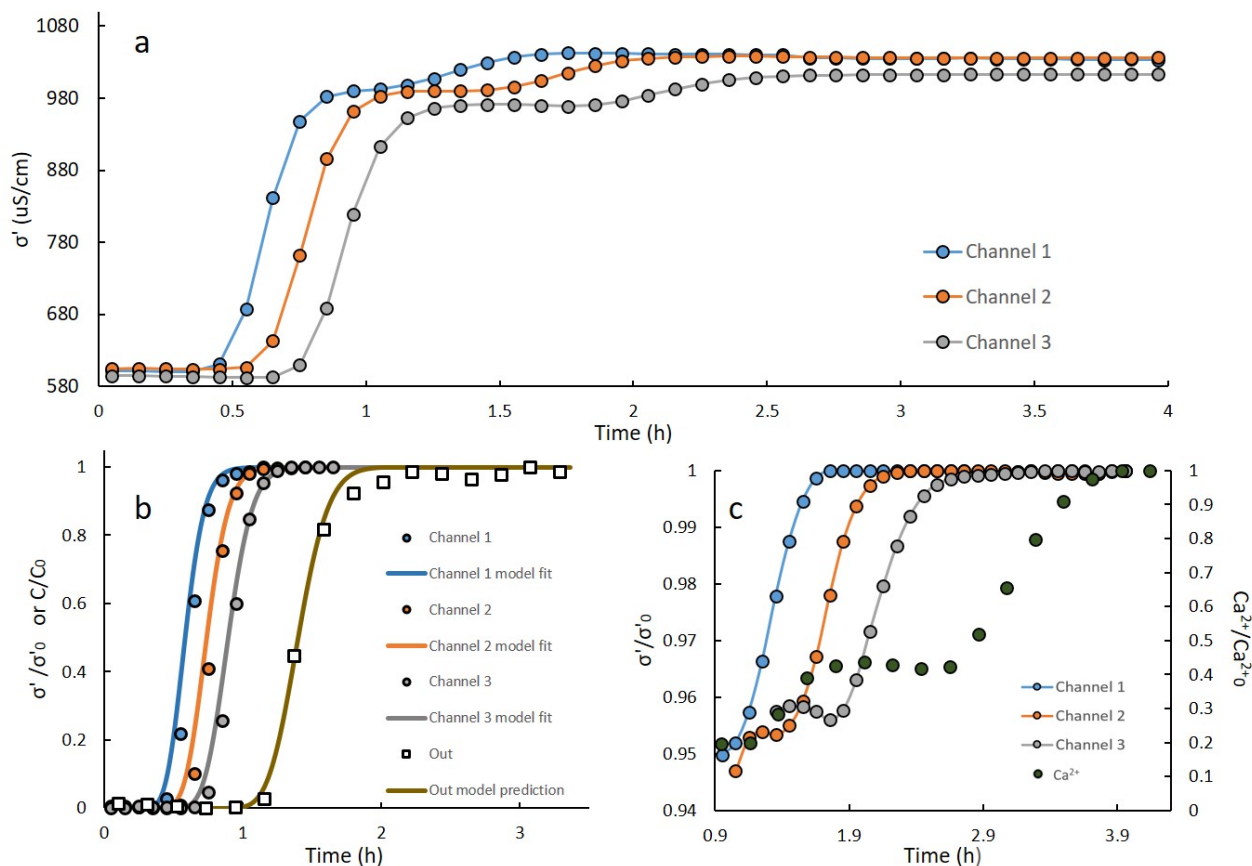
Figure 3b presents the normalized  $\sigma'$ -based time series (blue, orange and grey markers) and their model fit (blue, orange and grey continuous lines). Using the obtained model parameters, outflow  $Cl^-$  concentrations were predicted (brown continuous line) and compared to the measured  $Cl^-$  concentrations (clear rectangles). Both the model fit and the predicted outflow con-



170 centration presents an excellent fit to the measured data ( $R^2$  is 0.991 and 0.972 respectively). The ability to accurately predict  
the BT pattern of the  $Cl^-$  using a simple, HYDRUS-based numerical model suggests that the electrical measurement can  
replace outflow sampling and chemical analysis. Clearly, in more complex systems that involve multiple ions (either in the in-  
flow solution or adsorbed to the soil), some sampling and chemical analysis may be required in addition to the SIP monitoring.  
However, even for such systems, the use of electrical monitoring may allow to drastically reduce the sampling frequency and  
175 simplify the analysis performed on the outflow samples.

Interestingly, a secondary BT pattern was detected in the  $\sigma'$ -based curves between 0.9 and 2.5h (Fig.3c is an enlarged version of  
Fig.3a for the relevant times). The temporal location of this BT pattern suggests that the real part of the complex conductivity  
responded to the increased pore-water  $Ca^{2+}$  concentrations after the  $Na^+ - Ca^{2+}$  exchange reaction reached equilibrium.  
180 This increase, however, occurred simultaneously to the decrease in  $Na^+$  concentrations in the pore-water and hence did not  
have a major effect on the ionic strength of the outflow and was not detected by the EC measurements (see Fig.2a).





**Figure 3.** (a) Real conductivity at 1Hz versus time at three locations, (b) model fit to the  $\sigma'$ -based curves and model prediction for outflow  $\text{Cl}^-$  compared to measured  $\text{Cl}^-$ , (c) an enlarged version of (a), between 0.9 – 4 h, presented as normalized values and compared to outflow  $\text{Ca}^{2+} / \text{Ca}_0^{2+}$  (right vertical axis).

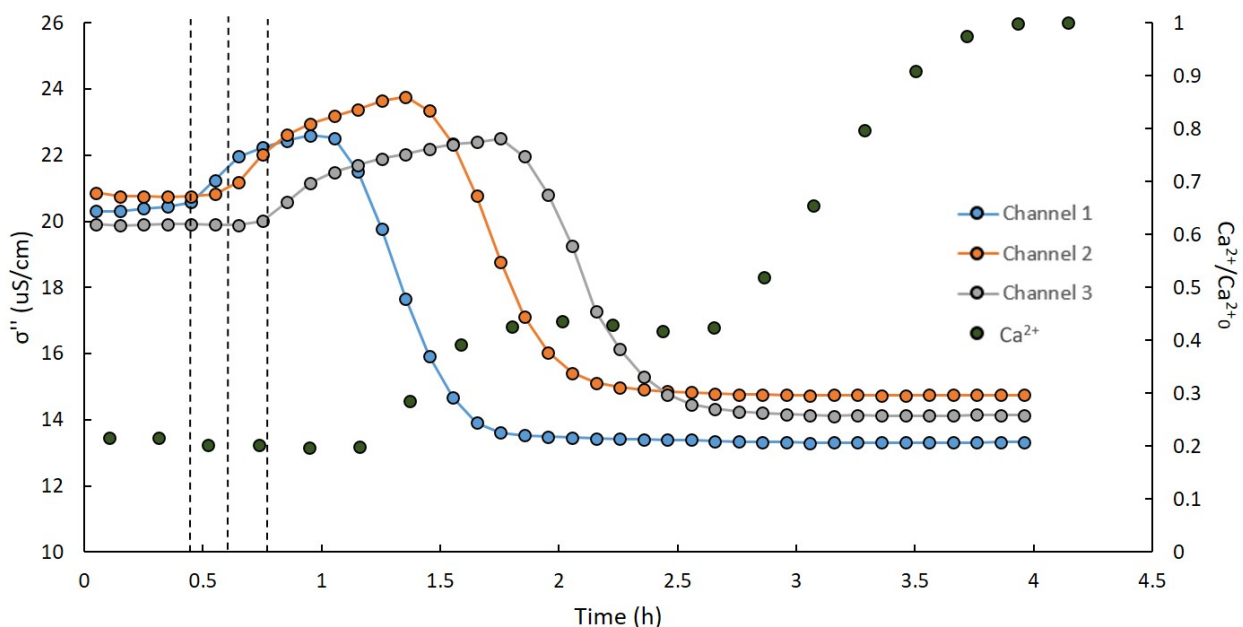
The imaginary conductivity along time (Fig.4) provides a clear indication for the scope of the  $\text{Na}^+ - \text{Ca}^{2+}$  exchange reaction. The signal increased initially in all channels, but decreased and stabilized after reaching its maximal value. The observed decrease in  $\sigma''$  that was followed by the BT of  $\text{Ca}^{2+}$  at the outflow, is related to the altered composition of the stern layer after the exchange reaction. Imaginary conductivity changes have been shown to be related to the mobility of ions in the stern layer (Vaudelet et al., 2011; Schwartz et al., 2012). Specifically, adsorbed  $\text{Na}^+$  ions maintain their hydration shell and hence, are weakly adsorbed to the soil and are more mobile compared to  $\text{Ca}^{2+}$ . During the  $\text{Na}^+ - \text{Ca}^{2+}$  exchange, the less mobile  $\text{Ca}^{2+}$  ions occupied the stern layer and caused the decrease in  $\sigma''$ . These observations are consistent with earlier studies. Shefer (2015) examined the SIP signature of loam and loess soils; the soil profiles were treated with high concentrations of  $\text{NaCl}$  or  $\text{CaCl}_2$  solution to alter the ionic composition of the stern layer. The results showed that the imaginary conductivity of the soil profile increased inversely to the mobility of the adsorbed ion. Vaudelet et al. (2011) observed similar results comparing the SIP signal of a saturated sand profile adsorbed with  $\text{Cu}^{2+}$  and  $\text{Na}^+$ . The  $\text{Cu}^{2+}$  ions are adsorbed to the soil mainly as an



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inner sphere (less mobile) species and hence the  $Na^+ - Cu^{2+}$  exchange reduced the overall ion mobility in the stern layer, similarly to the  $Na^+ - Ca^{2+}$  exchange considered here.

The increase in  $\sigma''$  begun in all channels before  $PV = 1$  was reached (see dashed vertical lines in Fig. 4) and hence, might be related to the progression of the  $Cl^-$  front and increase in EC during the  $CaCl_2$  injection. However, the imaginary conductivity is only marginally influenced by the conductivity of the pore-water. Moreover, the signal continued to increase in all channels after the stabilization of the outflow EC. This may imply that the increase in  $\sigma''$  is related to the  $Na^+ - Ca^{2+}$  exchange reaction. As  $CaCl_2$  entered the column,  $Na^+$  ions were detached from the grain surface and replaced by  $Ca^{2+}$ . We hypothesize that this decreased stability of the EDL during the exchange reaction (i.e increased ion mobility around the stern layer) is the cause of the observed increase in  $\sigma''$ . This suggests that the beginning of the  $\sigma''$  increase indicates the initiation of the exchange reaction at each location, while the steep decrease and following stabilization of the signal on its minimal value marks the end of the exchange. The secondary BT pattern observed in the  $\sigma'$  signal (see Fig.3b) supports our hypothesis: the minimal  $\sigma''$  values (indicating the end of the  $Na^+ - Ca^{2+}$  exchange) were observed at the same time as the stabilization of the  $\sigma'$  signal on its maximal value (suggesting the presence of  $Ca^{2+}$  at its inflow concentration in the pore-water).



**Figure 4.** Imaginary conductivity at 1Hz versus time at three locations (left vertical axis) and outflow  $Ca^{2+}/Ca_0^{2+}$  versus time (right vertical axis). The vertical dashed lines represent the beginning of the increase in  $\sigma''$  at each of the channels.

A comparison of  $Ca^{2+}$ ,  $Na^+$ ,  $Cl^-$  concentrations and EC values at the outflow samples collected during the heterogeneous and homogeneous experiments revealed no significant difference (t-test,  $\alpha=0.01$ ; see Fig.S1 in the supplementary material). This may be due to a combination of several different reasons: first, the loamy soil used here contained >90% sand, and

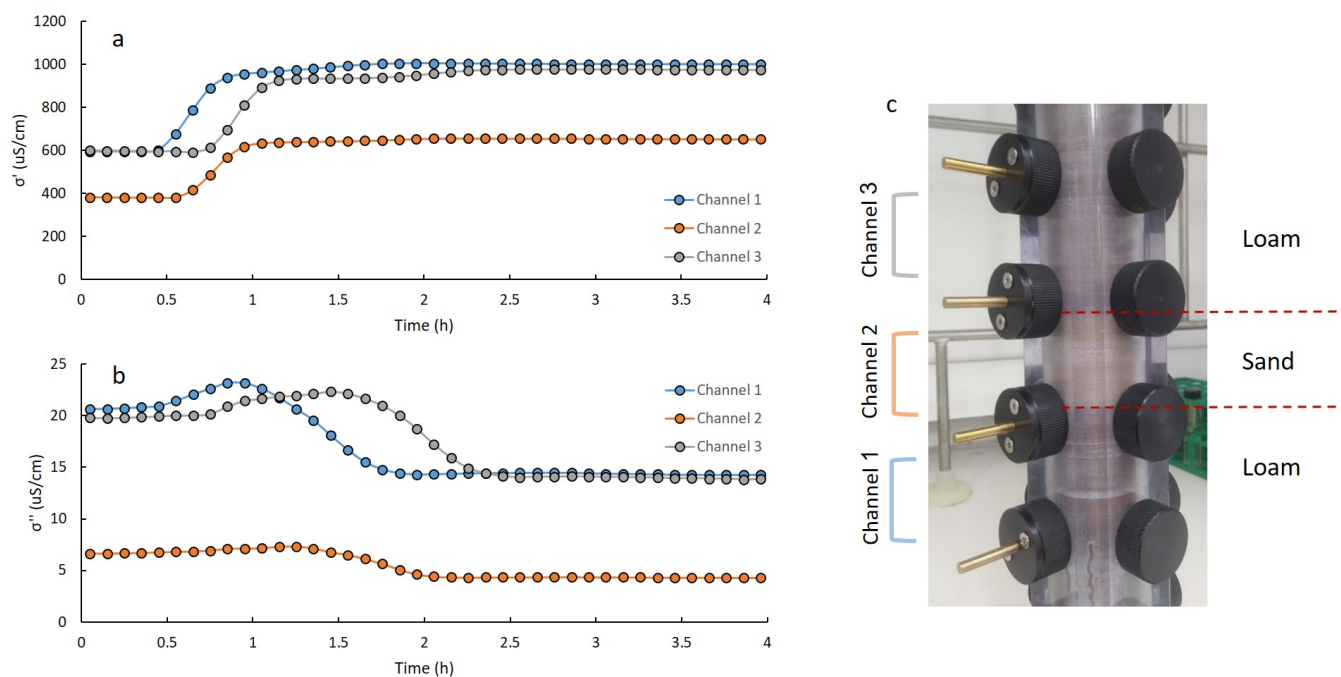


210 hence the overall difference in CEC between the profiles was minor. Further, the sand layer was relatively thin at one-tenth the profile's total volume (see Fig. 5c). Since the chemical measurements were conventionally performed on outflow samples, the obtained transport patterns of the different ions along time represent a spatial average and hence the implications of the heterogeneity were not detected by the chemical analysis.

215 Figure 5 presents the real (5a) and imaginary (5b) components of the complex conductivity at 1Hz versus time for the heterogeneous profile. Similarly to the homogeneous experiment, the  $\sigma'$ -based BT pattern observed between 0.5 and 1.2 h appeared at the different channels according to the geometrical hierarchy. The general shape of the secondary increase in  $\sigma'$  (between 0.9 and 2.5 h) and the imaginary conductivity curves are also consistent with the homogeneous case. However, for both components of the complex conductivity, the signal recorded in the middle channel (channel 2, measuring over the sand portion of the  
220 column) was notably lower compared to the other two channels.  $\sigma'$  values ranged between 600 – 1055  $\mu S/cm$  in the loam but were between 400 – 600  $\mu S/cm$  in the sandy layer. Similarly,  $\sigma''$  values ranged between 15 – 24  $\mu S/cm$  in the loam compared to 4 – 7  $\mu S/cm$  in the sandy layer. This observation indicates that the SIP-based BTC can characterize system heterogeneity, which is a major advantage over the conventional outflow analysis method.

225 The sensitivity of the complex conductivity to the geometry of the porous media and its surface charge means that differences in soil grain size, porosity, and CEC are likely to be reflected in the obtained signal. Geoelectrical studies of porous media characteristics mostly focused on physical aspects, rather than chemical aspects. The effect of soil hydraulic characteristics on its SIP signature have been studied before (e.g. (Kruschwitz et al. , 2010; Breede et al. , 2012; Nordsiek et al. , 2016)). For example, Kruschwitz et al. (2010) examined the low-frequency electrical spectra of a range of natural and artificial porous  
230 media in the aim to link the electrical signature to the physical properties of the examined media. They confirmed a significant positive correlation between the electrical polarization and the surface area to pore-volume ratio. Breede et al. (2012) investigated the SIP signature of sand and sand-clay mixtures (5, 10 and 20 % clay) under different saturation levels. Their results showed that the magnitude of both  $\sigma'$  and  $\sigma''$  were lower in sand compared to sand-clay mixtures for saturated conditions. The distinct values of  $\sigma'$  and  $\sigma''$  measured in channel 2 suggest that this area has different hydraulic characteristics compared to  
235 the rest of the profile. Specifically, it is consistent with the presence of a coarser textured soil, characterized by larger average grain size and lower CEC compared to the loamy soil that was measures by channels 1 and 3.

Analysis of the magnitude of the initial increase in  $\sigma''$  at the different channels (between 0.5 and 1.6 hours) for the heteroge-  
neous case showed that it was lower in the sandy layer (channel 2) compared to the loam (channels 1 and 3) by  $\sim 15\%$ . This  
240 observation can be explained by the difference in CEC between the different soil types. Isomorphic exchange in the mineral structure are less substantial in sand, which in combination with its smaller specific surface area, leads to lower CEC. Hence, the changes to the stern layer composition resulting from the  $Na^+ - Ca^{2+}$  exchange were less prominent in the sand.



**Figure 5.** The real (a) and imaginary (b) components of the complex conductivity at 1Hz versus time, for the heterogeneous profile. (c) shows the heterogeneous profile: a sandy layer was packed between the two middle electrodes (channel 2).

#### 4 Summary and conclusions

The main objective of this study was to investigate the ability of SIP measurements to depict BT patterns, ion exchange  
 245 processes and profile heterogeneity in a simple system. The presented laboratory setup for  $\text{Na}^+ - \text{Ca}^{2+}$  exchange combined  
 geo-electrical measurements backed by standard outflow ion and EC analysis. Our results led us to the following conclusions:  
 (1) SIP may serve as an alternative or supplementary tool for the monitoring of solute transport patterns through porous media,  
 requiring no outflow sampling. (2) In addition to the changes in outflow EC, the SIP measurement also indicated the initiation  
 and the end of the  $\text{Na}^+ - \text{Ca}^{2+}$  exchange in the soil column and following it, the delayed BT of  $\text{Ca}^{2+}$  ions. (3) SIP-based  
 250 BTC analysis is superior over conventional outflow analysis as it can characterize system heterogeneity, and is superior over  
 EC-based analysis as it is capable of distinction between the adsorption end-members. Clearly, in more complex systems that  
 involve multiple ions (either in the inflow solution or initially adsorbed to the soil), some sampling and chemical analysis may  
 be required. However, even for such systems, the use of electrical monitoring may allow to reduce the sampling frequency and  
 types of analysis performed on the outflow samples.



255 *Author contributions.* PK and DE performed preliminary experimental work, SBM and AF designed the the experiments. SBM performed the experiments, analyzed the data and drafted the paper. All authors edited the paper.

*Competing interests.* The authors declare that they have no conflict of interests

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