



1 **The added value of brightness temperature assimilation for the**
2 **SMAP Level-4 surface and root-zone soil moisture analysis over**
3 **mainland China**

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17 **Abstract.** The Soil Moisture Active Passive (SMAP) Level-4 Surface Soil Moisture and Root-Zone Soil Moisture (L4)
18 product provides global estimates of surface soil moisture (SSM) and root-zone soil moisture (RZSM) via the
19 assimilation of SMAP brightness temperature (Tb) observations into the Catchment Land Surface Model (CLSM).
20 Here, using in-situ measurements from 2474 sites in mainland China, we evaluate the performance of soil moisture
21 estimates from L4 and from a baseline “open-loop” (OL) simulation of CLSM without Tb assimilation. Using random
22 forest regression, the efficiency of the L4 ~~data assimilation~~ (DA) system (i.e., the performance improvement in L4
23 relative to OL) is attributed to 8 control factors related to the land surface modelling (LSM) and radiative transfer
24 modeling (RTM) components of the L4 system. Results show that 77% of the 2287 9-km EASE grid cells in mainland
25 China that contain at least one ground station exhibit an increase in the Spearman rank correlation skill (R) with in-
26 situ measurements for L4 SSM compared to that of OL, with an average R increase of approximately 14% ($\Delta R =$
27 0.056). RZSM skill is improved for about the same percentage of 9-km EASE grid cells, but the average R increase
28 for RZSM is only 7% ($\Delta R = 0.034$). Results further show that the SSM DA efficiency is most strongly related to the
29 error in Tb observation space, followed by the error in precipitation forcing and microwave soil roughness. For RZSM
30 DA efficiency, the three dominant control factors remain the same, although the importance of soil roughness exceeds
31 that of the Tb error. For the skill of the L4 and OL estimates themselves, the top control factors are the precipitation
32 error and the SSM-RZSM coupling strength error (in descending order of factor importance for R_{OL}), both of which
33 are related to the LSM component of the L4 system. Finally, we find that the L4 system can effectively filter out errors
34 in precipitation. Therefore, future development of the L4 system should focus on improving the characterization of the
35 SSM-RZSM coupling strength.

36

37 **Keywords.** SMAP Level 4, soil moisture, data assimilation, attribute analysis, random forest regression

38 1 Introduction

39 Soil moisture modulates water and energy feedbacks between the land surface and the lower atmosphere by
40 determining the partitioning of incoming net radiation into latent and sensible heat (Seneviratne et al., 2010, 2013).
41 High-quality, global-scale soil moisture products have become increasingly available in recent years (Gruber et al.,
42 2020). In particular, the L-band NASA Soil Moisture Active Passive (SMAP) satellite mission (Entekhabi et al., 2010;
43 Piepmeier et al., 2017) has significantly improved the skill of available, global-scale soil moisture products. However,
44 the SMAP observations contain temporal data gaps and are only representative of conditions within the top 5 cm of
45 the vertical soil moisture column. To address these limitations, the SMAP Level-4 Surface and Root-Zone Soil
46 Moisture (L4) algorithm assimilates SMAP brightness temperature (Tb) observations into the NASA Catchment Land
47 Surface Model (CLSM) to derive an analysis of surface (0–5 cm) and root-zone (0–100 cm) soil moisture estimates
48 with global, 3-hourly coverage (Reichle et al., 2017a; Reichle et al., 2017b; Reichle et al., 2019).



49 However, the performance of a land data assimilation (DA) system is sensitive to its parameterization and requires
50 careful assessment. For instance, Reichle et al. (2008) demonstrate that DA based on incorrect assumptions of modeling
51 and observation errors can degrade soil moisture estimates, compared with the case of not performing any DA.
52 Theoretically, the optimality of DA can be evaluated using so-called innovations, or observations-minus-forecast
53 residuals; however, an investigation of the innovations alone is often insufficient to determine if the soil moisture
54 analysis is optimal (Crow and Van Loon, 2006).

55 Recently, Dong et al. (2019a) proposed a novel statistical framework for evaluating the performance of a soil moisture
56 DA system. Specifically, they demonstrated that the relative skill of surface soil moisture (SSM) estimates acquired
57 with and without DA can be estimated using the ratio of their correlations with just one noisy but independent ancillary
58 remote sensing product. This approach was applied to the SMAP L4 system using ASCAT soil moisture retrievals.
59 Their results show that the added value of SMAP DA is closely related to both rain gauge and vegetation density.
60 However, due to the limited availability of independent root-zone soil moisture (RZSM) products for performing
61 statistical error estimation, this method is only applicable for SSM estimates.

62 Relative to SSM, the efficiency of assimilating land surface observations to improve RZSM is complicated by model
63 structural error that affects the ability of the DA to update unobserved model states. For instance, Kumar et al. (2009)
64 identified the surface–root zone coupling strength, which is the result of a model-dependent representation of processes
65 related to the partitioning of rainfall into infiltration, runoff, and evaporation components, as an important factor for
66 determining RZSM improvement associated with the assimilation of SSM retrievals. Their synthetic experiments
67 suggest that – faced with unknown true subsurface physics – overestimating the surface–root zone coupling in the land
68 model is a more robust strategy for obtaining skill improvements in the root zone than under-estimating the coupling.
69 Likewise, Chen et al. (2011) suggested that their Soil and Water Assessment Tool significantly under-predicts the
70 magnitude of vertical soil water coupling in the Cobb Creek Watershed in southwestern Oklahoma, USA, and this lack
71 of coupling impedes the ability of DA to effectively update deep-layer soil moisture, groundwater flow and surface
72 runoff. In the context of the present paper, the evaluation of L4 RZSM estimates has been limited to relatively few
73 SMAP core validation and sparse network sites (Reichle et al., 2017a; Reichle et al., 2017b; Reichle et al., 2019). With
74 such limited sample sizes, the RZSM skill of the L4 product at the global scale remains uncertain.

75 The primary objective of this study is to determine the DA efficiency, i.e., performance improvement in DA results
76 relative to the open-loop (OL) baseline of the L4 product, as a function of a variety of system aspects, including errors
77 in CLSM forcing (e.g., precipitation), errors in key CLSM parameters (e.g., relating to vegetation), mean errors in
78 CLSM structure (e.g., surface and root-zone coupling), and errors in the radiative transfer modeling (RTM) that links
79 the modeled soil moisture and temperature estimates to the observed T_b .

80 To this end, we first evaluate the performance of L4 SSM and RZSM estimates using a very large number ($n = 2474$)
81 of soil moisture profile measurement sites (generally acquired at sub-surface depths between 10 and 50 cm) within
82 mainland China. Next, the in-situ measurements are used to assess the DA efficiency of the L4 system, which is defined



83 as the skill difference between the L4 estimates and model-only estimates derived without SMAP Tb assimilation,
84 Additionally, we apply a machine-learning technique to quantify by how much various control factors drive the spatial
85 variations in the efficiency of the L4 system. In this way, we seek to prioritize future enhancements to the L4 system.

86 **2 Data and Methods**

87 This section briefly describes the SMAP L4 soil moisture product (Section 2.1), the extensive network of in-situ soil
88 moisture observations over mainland China (Section 2.2) and the ancillary data sources and metrics used in the skill
89 assessment (Sections 2.3 and 2.4). Next, we introduce the double instrumental variable (IVd) method employed to
90 determine the errors in control factors that cannot be determined using ground observations (Section 2.5). Finally, we
91 describe the random forest (RF) regression method used to identify the main factor(s) (out of the 8 control factors from
92 both CLSM and RTM aspects) that affect the spatial variations in SMAP L4 DA efficiency and L4 performance
93 (Section 2.6).

94 **2.1 SMAP L4 soil moisture product**

95 The SMAP L4 soil moisture product (version 4; Reichle et al., 2019) is generated by assimilating the SMAP L1C
96 Radiometer half-orbit 36 km EASE-Grid brightness temperature (Tb) observations (Version 4 SPL1CTB; Chan et al.,
97 2016) into the CLSM. The SMAP Tb observations are assimilated at 3-h intervals using a spatially distributed, 24-
98 member ensemble Kalman filter (Reichle et al. 2017b). The surface meteorological forcing data are from the global
99 Goddard Earth Observing System (GEOS) Forward Processing atmospheric analysis (Lucchesi, 2013), with
100 precipitation corrected using the daily, 0.5-degree, gauge-based Climate Prediction Center Unified (CPCU) product
101 (Xie et al. 2007). The L4 product provides global, 9-km, 3-hourly surface (0–5 cm) and root-zone (0–100 cm) soil
102 moisture estimates along with related land surface fields and analysis diagnostics. For the present study, we aggregated
103 all soil moisture estimates to daily-average (00:00 to 23:59 UTC) data. A baseline, model-only, ensemble CLSM
104 simulation without the assimilation of SMAP Tb observations (but using the same perturbations as in the L4 system)
105 is referred to as the “open-loop” (OL) run.

106 The SMAP L4 assimilation system includes a zero-order “tau-omega” forward RTM (De Lannoy et al., 2013) that
107 converts SSM and surface soil temperature into L-band brightness temperature estimates. Selected parameters of the
108 L4 RTM, including microwave soil roughness parameters, a vegetation structure parameter, and the microwave
109 scattering albedo, were calibrated using multi-angular L-band brightness temperature observations from the Soil
110 Moisture Ocean Salinity (SMOS) mission (De Lannoy et al., 2014). The L4 RTM parameterizes microwave soil
111 roughness as a function of SSM (De Lannoy et al., 2013, their equation B1). Here, we used this parameterization to
112 compute the 2017–2018 time-averaged microwave soil roughness estimates as one potential indicator of DA efficiency
113 (Section 2.3). The necessary parameters were obtained from L4 “Land-Model-Constants” output Collection (last
114 access: 8 July 2020; DOI: <https://doi.org/10.5067/KGLC3UH4TMAQ>; Reichle et al., 2018a). The L4 “Analysis-
115 Update-Data” output Collection includes RTM predictions of Tb and the assimilated SMAP Tb observations (last
116 access: 8 July 2020; DOI: <https://doi.org/10.5067/60HB8VIP2T8W>; Reichle et al., 2018b).



117 To avoid the impact of seasonality, we performed our analysis using anomaly time series, derived by subtracting a
118 seasonally-varying (daily) climatology from each raw time series. The climatology of a given time series was obtained
119 by sampling the mean value of all soil moisture estimates that fall within a 31-day moving window centered on a
120 particular day-of-year. Moreover, L4 estimates of land latent heat flux (LE), land sensible heat flux (SH) and the
121 climatological LAI inputs to CLSM and the RTM, were obtained from the L4 “Geophysical-Data” output Collection
122 (last access: 6 April 2020; DOI: <https://doi.org/10.5067/KPJNN2G11DQR>; Reichle et al., 2018c). These datasets were
123 also used to compute control factors to explain spatial variations in the DA efficiency of the L4 system (Section 2.3).

124 **2.2 Soil moisture validation data**

125 In-situ soil moisture measurements during 2017 and 2018 were collected from a national network of Chinese
126 Automatic Soil Moisture Observation Stations (CASMOs) maintained by the Chinese Meteorological Administration
127 (CMA). In total, soil moisture measurements from 2474 separate stations arrayed across mainland China, and covering
128 different land use types, were collected. At each CASMO site, frequency domain reflectometry-based instruments
129 were used to record hourly volumetric soil moisture content within the following vertical depth ranges: 0–10, 10–20,
130 20–30, 30–40, and 40–50 cm below the surface. These hourly estimates (at multiple depths) were then aggregated into
131 daily values and linearly averaged (vertically) to produce 0–10 cm (SSM) and 0–50 cm (RZSM) in situ soil moisture
132 measurements – which were subsequently used to validate the L4 and OL SSM (0–5 cm) and RZSM (0–100 cm)
133 estimates. Note that Spearman correlation rather than Pearson correlation is used for L4 and OL validation, in order to
134 avoid impact of outliers in the time series and prior assumptions about soil moisture distributions.

135 Ground observations falling within the same 9-km EASE grid were averaged for comparisons against the collocated
136 9-km L4 and OL soil moisture estimates. A total of 2287 individual 9-km EASE grid cells within mainland China are
137 included in the analysis. Among them, 92.35% of grid cells contain one in-situ site, 7.26% contain two sites, 7 grid
138 cells contain three sites, and the remaining two grid cells contain four and five sites respectively.

139 **2.3 Explanatory data products**

140 As discussed above, our hypothesis is that the efficiency of the SMAP L4 system will be sensitive to the ability of the
141 ensemble-based L4 analysis in filtering errors that exist in the OL (that is, CLSM), in the model forecast T_b (that is,
142 the RTM), and in the SMAP T_b observations. We therefore considered two separate categories of factors that
143 potentially control spatial variations in DA efficiency. The factors are summarized in Table 1.

144 The first category represents a range of factors known to affect the skill of soil moisture estimates derived from LSM
145 (in this case, CLSM). The five control factors in this category are: i) the error in precipitation forcing, ii) the error in
146 (input) LAI, iii) the error in (output) LE, iv) the magnitude of mean error in CLSM SSM-RZSM coupling strength,
147 and v) the presence of vertical variability in soil properties (defined as the difference in clay fraction across the vertical
148 soil profile). Note that such variability represents a potential source of error because CLSM assumes that soil texture
149 and the associated soil parameters are vertically homogeneous within the soil column, with the exception of some



150 surface-layer moisture transport parameters. The soil texture information is from Harmonized World Soil Database
151 (HWSD) v1.2.

152 The second category contains three factors that affect radiative transfer modeling (RTM) and therefore DA updates.
153 These include: i) estimates of the joint error in SMAP Tb observations and RTM Tb simulations, ii) the magnitude of
154 microwave soil roughness, and iii) the magnitude of LAI (as a proxy for the vegetation optical depth at microwave
155 frequencies, which modulates the sensitivity of the observed Tb to SSM conditions).

156 The control factors take a variety of forms. Some factors are based on estimates of the errors fed into the L4 system as
157 (e.g., the error in CLSM rainfall forcing data). Other factors consist of the magnitude of the variable itself (e.g., the
158 vertical variability of clay fraction). Note that LAI is used in both ways: LAI error is used to predict OL performance
159 (because LAI is an important input into CLSM) while mean LAI is used to explain DA performance (because increased
160 LAI is associated with decreased soil moisture information content in microwave observations).

161 Note that the LAI used in the L4 system is a climatology derived from satellite observations of the Normalized
162 Difference Vegetation Index. Therefore, to indicate the magnitude by which each grid cell's LAI typically deviates
163 from its long-term climatology, we use the temporal standard deviation of anomaly time series of the benchmark LAI
164 (from SPOT VGT product) as a measure of the error in the LAI used in L4. Owing to the lack of reference Tb
165 observations at similar satellite overpass times and locations, Tb errors are gauged using the time series standard
166 deviation of the observation-minus-forecast (O-F) Tb residuals, which indicate the typical misfit between the model
167 forecast Tb and the (rescaled) SMAP Tb observations. This metric measures the total error in Tb observation space.
168 The exact data sets and the metrics utilized for evaluating these 8 control factors are summarized in Table 1.



Table 1 Benchmark data sets and metrics used for evaluating control factors of SMAP L4

Factor category	Control factor	Dataset/Benchmark	Temporal resolution	Spatial resolution	Data range	Metrics
LSM	Precipitation error	Rain gauge (CGDPA)	daily	0.25 °	2017-2018	Spearman's rank correlation <i>R</i>
	SSM-RZSM coupling strength error	CASMOS	daily	NA	2017-2018	Δ CP (see Section 2.4)
	Vertical variability of clay fraction	HWSD	NA	9 km	NA	Difference in clay fraction between topsoil (0-30 cm) and root-zone (0-100 cm) layers
RTM	SMAP L4 LAI error	SPOT LAI	10 d	1 km	2017-2018	Temporal standard deviation of SPOT VGT LAI anomaly
	LE error	FLUXCOM	daily	(1/120) °	2017-2018	IVd-based <i>R</i>
	Tb error	SMAP L4	daily	9 km	2017-2018	Temporal standard deviation of O-F Tb residuals
RTM	Microwave soil roughness	SMAP L4	daily	9 km	2017-2018	Temporal average based on De Lannoy et al. (2013)
	Annual mean LAI	MODIS/Geoland-based product	daily	9 km	2017-2018	Climatological mean



171 **2.3.1 Gauge-based precipitation gridded product**

172 Errors in the GEOS precipitation data used to force the CLSM within the SMAP L4 system were estimated via
173 Spearman's rank correlation with available rain-gauge observations. These network observations are based on an
174 analysis of ~2400 rain gauge stations distributed unevenly over mainland China. Recently, the China Gauge-based
175 Daily Precipitation Analysis (CGDPA) with a spatial resolution of $0.25^\circ \times 0.25^\circ$ based on this network was constructed
176 and has been made operational over mainland China. CGDPA uses a modified interpolation method of climatology-
177 based optimal interpolation (OI) with topographic correction proposed by Xie et al. (2007). In this process, daily
178 precipitation climatology over mainland China is optimized and is rebuilt using the 30-year average precipitation
179 observations from ~2400 gauges of the period 1971–2000 (Shen et al., 2010). CGDPA is shown to have smaller bias
180 and root mean square error than the CPCU product used in L4, which is based on fewer than 400 gauge sites over
181 mainland China (Shen et al., 2015).

182 **2.3.2 FLUXCOM LE estimates**

183 The FLUXCOM ensemble of global land-atmosphere energy fluxes was used to evaluate the error of the L4 LE
184 estimates. This ensemble merges energy flux measurements from FLUXNET eddy covariance towers with remote
185 sensing and meteorological data based on a machine learning method to estimate global gridded net radiation, latent
186 and sensible heat and their related uncertainties (Jung et al., 2019). The resulting FLUXCOM database has a 0.0833°
187 spatial resolution when applied using MODIS remote sensing data. The monthly energy flux data of all ensemble
188 members, as well as the ensemble estimates from the FLUXCOM initiative, are freely available (CC4.0 BY license)
189 from the Data Portal (<http://fluxcom.org/>), while the daily- and 8-day FLUXCOM products are available upon request
190 from dataset provider Martin Jung. To calculate the LE error, we've collected the daily, high spatial resolution
191 FLUXCOM product and extracted the estimates where in-situ soil moisture sites located.

192 **2.3.3 SPOT VGT LAI**

193 The data set used as a benchmark for assessing leaf area index (LAI) errors present in the SMAP L4 analysis was
194 derived from SPOT/VEGETATION and PROBA-V LAI products (version 2) that are generated every 10 days at
195 spatial resolution of 1 km. The SPOT LAI version 2 product capitalizes on the development and validation of already
196 existing products: CYCLOPES version 3.1 and MODIS collection 5 and the use of neural networks (Baret et al., 2013;
197 Verger et al., 2008). The version 2 products are derived from top of canopy daily (S1-TOC) reflectances instead of
198 normalized top of canopy 30-day composited reflectances as in the version 1. Compared to version 1, the compositing
199 step is performed at the biophysical variable level instead of reflectance level. This ensures reduced sensitivity to
200 missing observations and avoids the need for a BRDF model.

201 **2.3.4 HWSO soil texture**

202 The HWSO attribute database (v1.2) is a 30 arc-second raster database with 15773 different soil-mapping units. It
203 provides information on the standardized soil parameters for topsoil (0–30cm) and subsoil (30–100 cm) separately. In



204 this study, we use the difference of clay fractions between topsoil (0-30cm) and the aggregated 0-100cm layer to
205 measure the vertical clay fraction variation at each 9-km grid cell.

206 **2.4 Vertical coupling metric**

207 The RZSM time series generally show decreased temporal dynamics relative to SSM. As a result, overestimated SSM-
208 RZSM coupling tends to spuriously increase the (correlation-based) similarity of SSM and RZSM time series, and
209 thereby, overestimate RZSM temporal variability. Therefore, analogous to Kling-Gupta efficiency (Gupta et al., 2009),
210 we defined the SSM-RZSM coupling strength (CP) as:

$$CP = 1 - \sqrt{(R-1)^2 + (\alpha-1)^2} \quad (1)$$

211 where R is the Spearman's rank correlation between SSM and RZSM, and α is the ratio of temporal standard deviation
212 of SSM to that of RZSM. A CP value of one represents the extreme case where RZSM is identical to SSM, i.e., a
213 strongly coupled case. Likewise, a CP of zero represents the opposing case of completely uncoupled time series. Cases
214 with negative CP do not exist.

215 Observed CP (CP_{obs}) was based on comparisons between 0-10 cm "surface" estimates and 0-50 cm "root-zone" in situ
216 observations and used as a benchmark. In contrast, SMAP L4 CP estimates (CP_{OL}) was based on the comparison of 0-
217 5 cm "surface" estimates and 0-100 cm "root-zone" estimates. Therefore, the surface versus root-zone storage contrast
218 in the observation time series is less than that of the L4 estimates. This will likely cause the observed correlation
219 between surface and root-zone time series to be systematically higher than the analogous vertical correlation
220 calculation for L4 estimates. However, this bias is partially corrected for by the second term in Eq. (1) – since the
221 observed α ratio will, by the same token, tend to be smaller (i.e. closer to one) than α sampled from the L4 analysis.
222 Such ability to compensate for vertical depth differences is a key reason we apply CP, rather than *simple correlation*,
223 as a vertical coupling strength metric. Nevertheless, it should be noted that our main interest here lies in describing
224 spatial variations in ($CP_{OL} - CP_{obs}$) and care should be taken when interpreting raw ($CP_{OL} - CP_{obs}$) differences as an
225 *absolute* measure of L4 vertical coupling bias.

226 **2.5 Double instrumental variable (IVd) method**

227 The benchmark data set of FLUXCOM LE described above contains error that is (likely) of a similar order of
228 magnitude as the L4 LE dataset it is applied to evaluate. Therefore, in an attempt to correct for the impact of this error,
229 the LE error used here as a control factor is obtained via a double instrumental variable (IVd; Dong et al., 2019b)
230 analysis approach that minimizes the spurious impact of random errors in benchmark data sets. As shown in Dong et
231 al. (2019b), for the evaluation of two time series with auto-correlation in both of them, IVd is more robust than single
232 instrumental variable based algorithm, therefore we apply IVd to evaluate the LE error.



233 IVd is a modified version of triple collocation (TC) analysis. In TC analysis (McColl et al., 2014), geophysical
234 variables obtained from three independent sources (x , y and z) are assumed to be linearly related to the true signal P
235 as:

$$x = \alpha_x P + B_x + \varepsilon_x \quad (2)$$

236 where the α_x is a scaling factor; B_x is a temporal constant bias and ε_x is zero-mean random error.

237 As opposed to the TC method, IVd uses only two independent products (x , y) to characterize geophysical data product
238 errors. This method introduces two instrumental variables (I and J , i.e., $I_t = \alpha_x P_{t-1} + B_x + \varepsilon_{xt-1}$, $J_t = \alpha_y P_{t-1} + B_y + \varepsilon_{yt-1}$),
239 which are based on the lag-1 (day) time series (at day t) of x and y , respectively. Therefore, assuming that the errors of
240 two independent products are serially white, the covariance between instrumental variables and products can be written
241 as follows:

$$C_{Ix} = \alpha_x^2 L_{PP} \quad (3)$$

$$C_{Jy} = \alpha_y^2 L_{PP} \quad (4)$$

242 where C represents the covariance of the subscript products. For instance, C_{Ix} represents the covariance of x and its
243 instrumental variable I . Variable L_{PP} is the lag-1 auto-covariance of the true signal. Combining Eqs. (3) and (4), the
244 scaling ratio s_{ivd} of the two products x and y can be written as:

$$s_{ivd} = \sqrt{\frac{C_{Ix}}{C_{Jy}}} \quad (5)$$

245 Based on Eq. (5), their correlation with truth can be estimated as:

$$R_{Px}^2 = \frac{C_{xy} s_{ivd}}{C_{xx}} \quad (6)$$

$$R_{Py}^2 = \frac{C_{xy}}{C_{yy} s_{ivd}} \quad (7)$$

246 In this way, the error in the L4 LE (measured by IVd-based correlation with truth) can be estimated robustly using the
247 FLUXCOM LE product described in Section 2.3.2.



248 2.6 Random forest regression

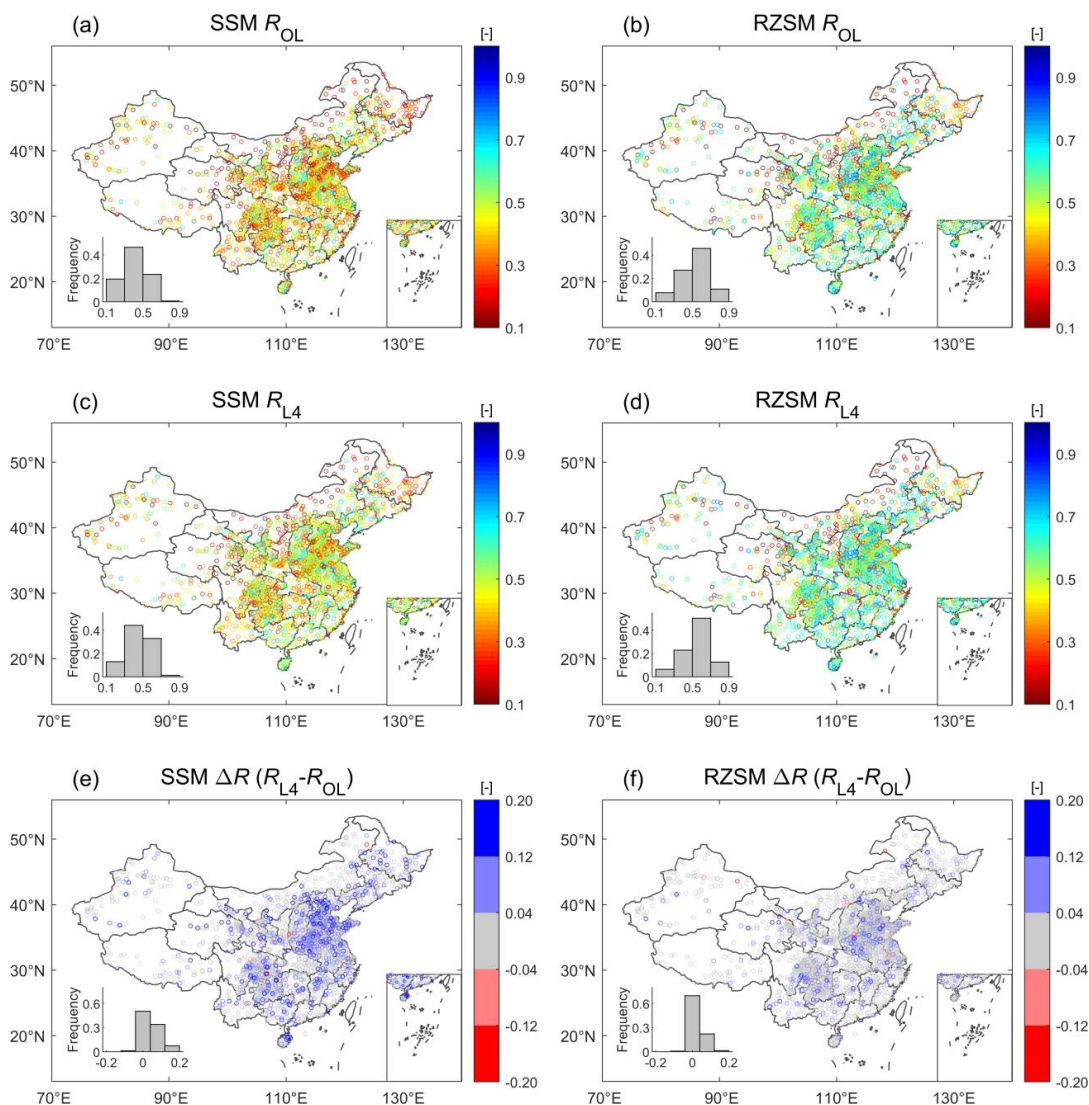
249 A random forest (RF) regression approach was used to rank and quantify the importance of the 8 control factors
250 introduced above (Table 1) for describing spatial patterns in DA efficiency for both SSM and RZSM estimates. The
251 RF method is a supervised learning algorithm based on an averaged ensemble of decision trees (Breiman, 2001). Unlike
252 linear regression approaches, RF can capture non-linear interactions between the features and the target. In addition,
253 the normalization (or scaling) of data is not necessary in RF application. Another advantage of the RF algorithm is that
254 it can readily measure the relative importance of each feature on the estimates, which makes it highly suitable for an
255 attribution analysis. Therefore, based on the output of RF, key control factors determining the efficiency of SMAP
256 DA were evaluated and ranked. The RF estimates are based on a 10-fold cross-validation approach.

257 3 Results

258 3.1 Validation of SMAP L4 and OL estimates of SSM and RZSM anomalies

259 Figure 1 maps validation results (i.e., anomaly Spearman's rank correlation with in-situ observations, R) for SMAP L4
260 and associated OL soil moisture estimates. The skill patterns for OL and L4 are, in general, quite spatially consistent.
261 Both are characterized by an increasing trend of SSM estimation skill moving from northwest to southeast China (Fig.
262 1a and 1b). In relative terms, the L4 product surpasses the baseline OL's SSM skill within 77% of the 2287 9-km
263 EASE grid cells containing ground observations – with a mean R increase of $\Delta R = 0.056$ [-] and mean relative
264 improvement versus R_{OL} of 14%.

265 Similar spatial patterns are observed for RZSM skill. As with SSM, generally higher consistency with in-situ RZSM
266 measurements is found in southeast China relative to northern China. However, relative to SSM, the added value of
267 SMAP data assimilation (i.e. L4) is reduced for RZSM and the mean relative R improvement falls to 7% ($\Delta R = 0.034$
268 [-]) (compare Fig. 1e and 1f). This is not surprising since assimilated SMAP Tbs are primarily sensitive to soil moisture
269 conditions in the surface (0-5 cm) layer.



270

271 **Figure 1:** OL (a, b) and L4 (c, d) skills (R values) for SSM (left column) and RZSM (right column). DA efficiency ($\Delta R = R_{L4}$
 272 $- R_{OL}$) for (e) SSM and (f) RZSM. Blue (red) colors in (e) and (f) indicate grid cells where L4 estimates are better (worse)
 273 than OL. Non-significant differences (based on a 1000-member bootstrapping analysis) are colored grey. The lower left inset
 274 in each subplot indicates the frequency of binned R -values across all 9-km EASE grid cells containing ground observations.

275

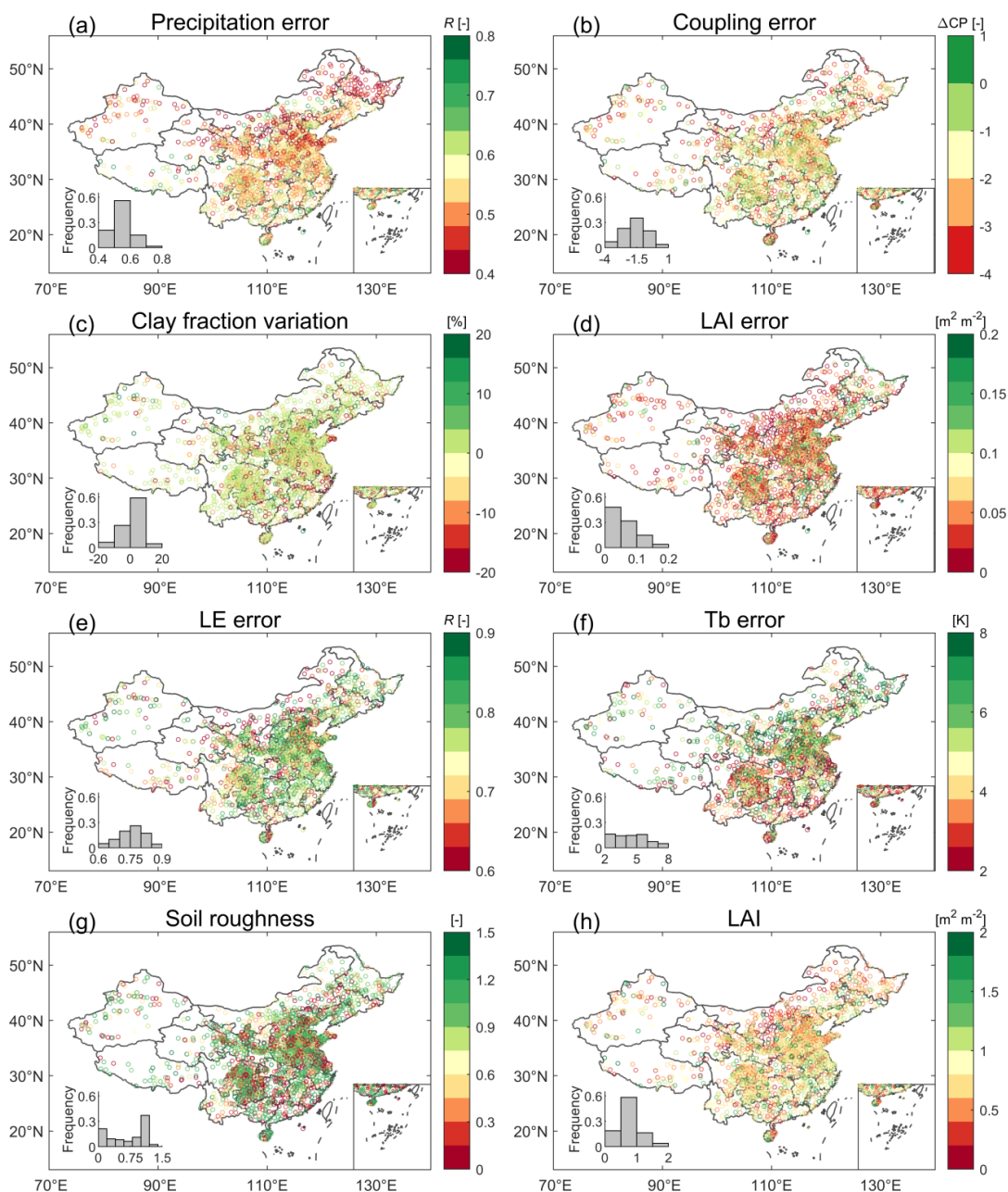
276 3.2 Spatial distribution of potential factors controlling SMAP L4 DA performance

277 As described in Section 2.3, we selected 8 control factors that potentially influence the skill of SMAP L4 soil moisture
 278 estimates. Using the attribution analysis described in Section 2.6, these factors will be used to explain the spatial



279 variations in skill and DA efficiency seen in Fig. 1. As a first step, this section examines the spatial patterns inherent
280 in the 8 control factors. Errors in the CLSM precipitation forcing are relatively higher in northern and northwestern
281 areas of China (Fig. 2a), where the gauge density is generally more sparse than southern China. Among the factors
282 representing CLSM structural errors, a pre-dominantly negative bias is observed in SSM-RZSM coupling strength
283 generally across China (i.e., lower CP_{OL} compared to CP_{obs}), while a very small number of grid cells show a positive
284 coupling strength bias in eastern China (dark green dots in Fig. 2b). This is expected since at the coarse resolution, the
285 model's vertical coupling strength should be much less than at any single point. In addition, this may be partly
286 attributed to the layer depths differences, since CLSM represents surface and root-zone depths of 0-5 cm and 0-100
287 cm, whereas the corresponding in-situ observations represent the 0-10 cm and 0-50 cm layers, and it can be expected
288 that CP_{OL} should thus be smaller than CP_{obs} . In addition, the vertical variability of the clay fraction seems to show little
289 spatial variation across mainland China (Fig. 2c). With respect to CLSM LAI error, regions in southern China that
290 have generally higher LAI show larger standard deviation in SPOT LAI time series (Fig. 2d and 2h). The IVd-based
291 estimates of SMAP L4 LE error, which represent a potential control factor for water-balance errors in CLSM, generally
292 show low-level of error across mainland China (Fig. 2e).

293 For O-F Tb residuals describing RTM-related error, a higher standard deviation of O-F Tb residuals is observed in the
294 North China Plain (Fig. 2f), which is very consistent in spatial distribution with areas displaying the highest and most
295 significant SSM prediction improvement (Fig. 1c). This is expected, as mentioned above, because O-F Tb residuals
296 are the basis for the soil moisture corrections (or increments) that are applied in the DA system as part of the L4
297 analysis. The 2017-2018 mean of soil roughness and the 2017-2018 mean LAI show higher values in southwest and
298 southeast China (Fig. 2g-h).



299

300 **Figure 2: Factors potentially influencing SMAP L4 performance over mainland China: (a) CLSM precipitation error**
 301 **measured by the Spearman's rank correlation between CLSM precipitation and ground observations; (b) SSM-RZSM**
 302 **coupling strength error (CP_{OL} minus CP_{obs}); (c) clay fraction variation (difference) across the soil profile; (d) error in LAI**
 303 **input to L4; (e) IVD-based error of LE from L4; (f) Tb error; (g) L4 microwave soil roughness; (h) climatology mean of LAI**
 304 **input to L4.**



305

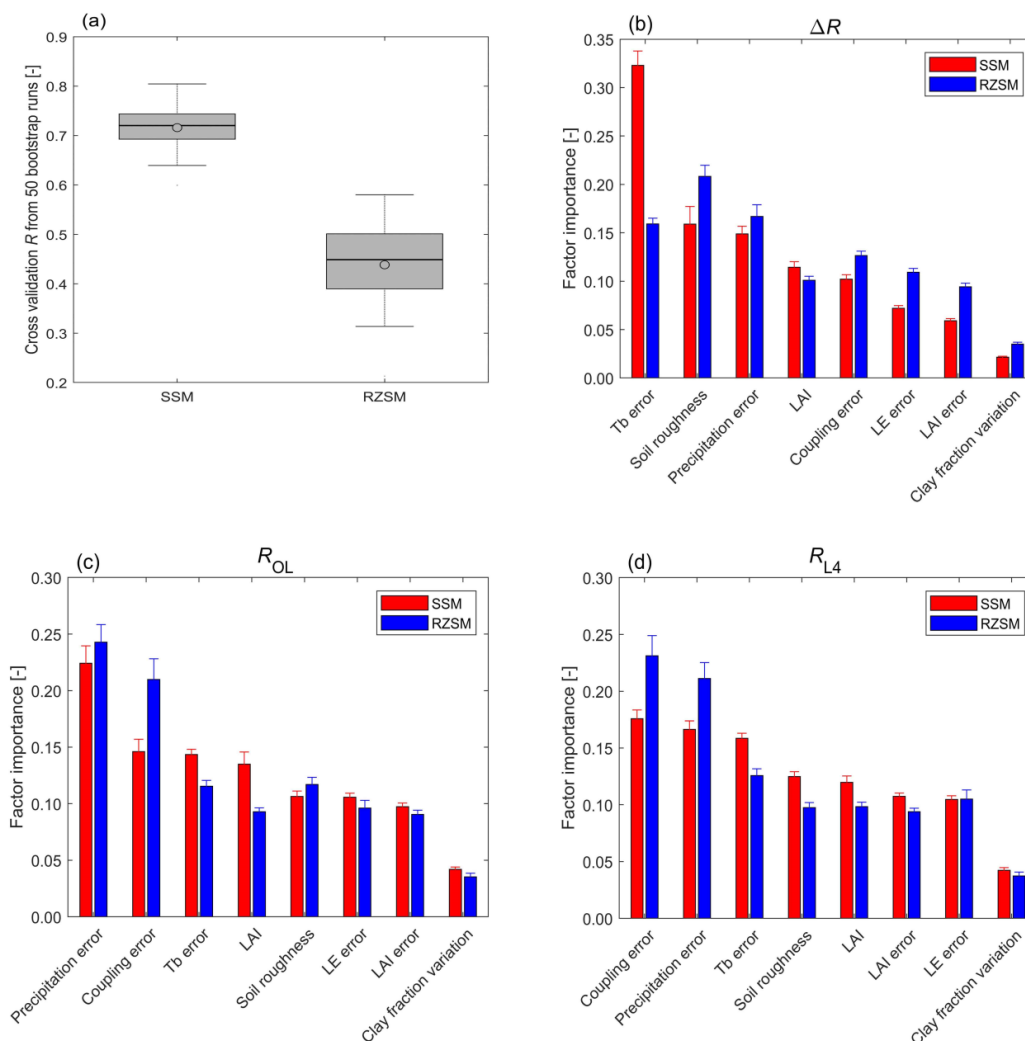
306 **3.3 Attribution of SMAP L4 versus OL performance to control factors**

307 **3.3.1 Attribution using random forest regression**

308 As mentioned above, RF regression was used to identify the relative importance of our 8 control factors for determining
309 the efficiency of SMAP L4 DA (i.e., $\Delta R = R_{L4} - R_{OL}$), and also L4 (R_{L4}) and OL performances (R_{OL}). To start, we first
310 investigate the robustness of RF for predicting ΔR . To estimate the magnitude of randomness in the RF algorithm, we
311 use 50 bootstrap runs. As shown in Fig. 3a, the 10-fold cross-validation test (228 validation samples) shows that the
312 predicted and in-situ-based ΔR have a mean correlation of 0.72 and 0.46 for SSM and RZSM, respectively.

313 Given the sampling errors of ΔR , which is based on a two-year validation period, and the relatively low spatial
314 variability in RZSM skill (Figs. 1f), the performance of RF is acceptable. In addition, ground-measurement upscaling
315 error is likely a significant contributor to unexplainable spatial variability for ΔR in Fig. 1. In fact, Chen et al. (2016)
316 found large spatial variability in the ability of point-scale SSM ground observations to describe grid cell-scale SSM
317 dynamics. In-situ observations sites associated with larger upscaling errors will introduce a spurious low bias into
318 sampled estimates of ΔR values (see Appendix B in Dong et al., 2020). Therefore, some of the ΔR spatial variability
319 observed in Fig. 1 is unrelated to any aspect of the L4 system and is therefore unexplainable via the 8 control factors
320 we have selected.

321



322

323 **Figure 3: Attribution analysis of SMAP L4 DA efficiency: (a) Cross-validation of RF regression method in predicting DA**
 324 **efficiency $\Delta R = R_{L4} - R_{OL}$ based on our 8 control factors (Table 1). Relative importance of 8 control factors determining**
 325 **spatial patterns in (b) DA efficiency (ΔR), (c) OL performance (R_{OL}), and (d) L4 performance (R_{L4}). Red (blue) bars**
 326 **represent predictor importance for SSM (RZSM). Error bars reflect the standard deviation from 50-member bootstrapping**
 327 **of the RF importance estimates.**

328

329 Based on the RF results, the Tb error is quantified as the most prominent factor in determining DA efficiency (i.e., ΔR)
 330 = $R_{L4} - R_{OL}$) – followed by precipitation error and microwave soil roughness (Fig. 3b). The RF-derived ranking of
 331 control-factor importance for RZSM is similar to that of SSM in that the same three factors are still the most



332 explanatory. However, in contrast to SSM, the importance of Tb error for RZSM decreased dramatically from >30%
333 to ~15%. Other modeling error sources (e.g., the vertical variability of soil properties) have only very limited impact
334 on SMAP DA improvement.

335 As seen in Fig. 3c, for the OL performance (R_{OL}), the most important factors identified by RF include precipitation
336 error, SSM-RZSM coupling error, and Tb error (microwave soil roughness) for SSM (RZSM). Note that although the
337 Tb error is identified as third important factor for R_{OL} in SSM skill, this is an instance where there is correlation (poorer
338 skill happens to coincide with higher Tb error), but this does not imply a causal relationship. Specifically, it is normal
339 that Tb (O-F) errors are higher where the OL performs worse, but a high Tb error is not the cause of a low OL
340 performance. The same applies to the relationship between microwave soil roughness and OL skill for RZSM
341 estimation. The SMAP L4 system is able to reduce the predominant impact of precipitation errors on both SSM and
342 RZSM estimation skill, rendering SSM-RZSM coupling error the most important factor for R_{L4} (Fig. 3d). In addition,
343 in the L4 system, the high vegetation density effect on SSM and RZSM estimation is clearly reduced, as the fourth
344 most important factor of LAI is replaced by Tb error.

345 The qualitative rankings provided by the RF analysis in Fig. 3 are relatively robust to our particular choice of
346 benchmark data set to define the ‘error’ of various control variables. For instance, we replaced the CGDPA
347 precipitation benchmark with the CMORPH-merge product (Version 1, last access: 6 April 2020; DOI:
348 <https://doi.org/10.25921/w9va-q159>; Xie et al., 2019), which is the 0.1 degree merging product of CMORPH and
349 observations from more than 30,000 automatic weather stations in mainland China. For this case, the predictive power
350 of the regression model established by the RF is not affected (similar to Fig. 3a), and the qualitative rankings of the
351 precipitation error in R_{OL} and R_{L4} are not impacted (similar to Fig. 3c-d).

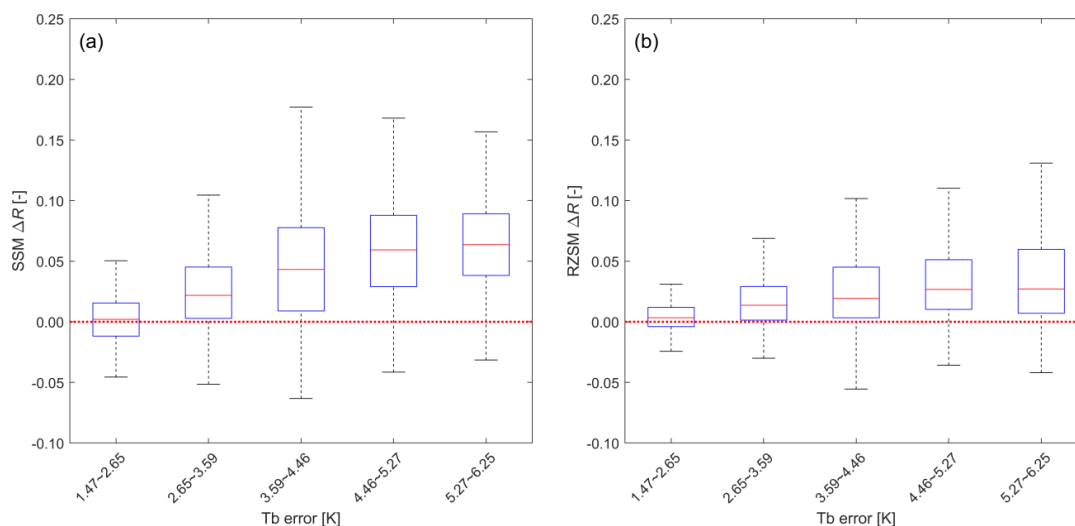
352

353 3.3.2 Attribution using box plot comparisons

354 As stated in Section 2.5, the RF method is adept at summarizing the impact of multiple (co-varying) control factors
355 simultaneously in the established regression model and thus provides more comprehensive insights than the
356 examination of how the target variable (DA improvement) fluctuates with each individual control factor. However, it
357 does not allow the investigation of the sign of the relationship between DA improvement and each control factor –
358 which is important for understanding exactly how each factor influences the DA system. In addition, since the net
359 impact of various factors can enhance DA efficiency by either degrading the OL or enhancing the ability of DA to add
360 more value, it is important to decompose the source of variations in ΔR . Therefore, in addition to examining how
361 SMAP DA efficiency, i.e., $\Delta R = R_{L4} - R_{OL}$, varies as a function of the most prominent control factors identified in the
362 above Section 3.3.1 (i.e., Tb error, precipitation forcing, and microwave soil roughness), we also examine how
363 precipitation error as a control factor affects the OL performance, i.e., R_{OL} .



364 To minimize the uncertainty caused by large errors in each of the control factors, we exclude samples with errors
365 (separately for each control factor) ranking above the 80th percentile in the following analysis. The relationship
366 between Tb errors and L4 DA efficiency is straightforward: higher Tb errors are associated with higher ΔR , with ΔR
367 generally larger for SSM than for RZSM (Fig. 4a-b).

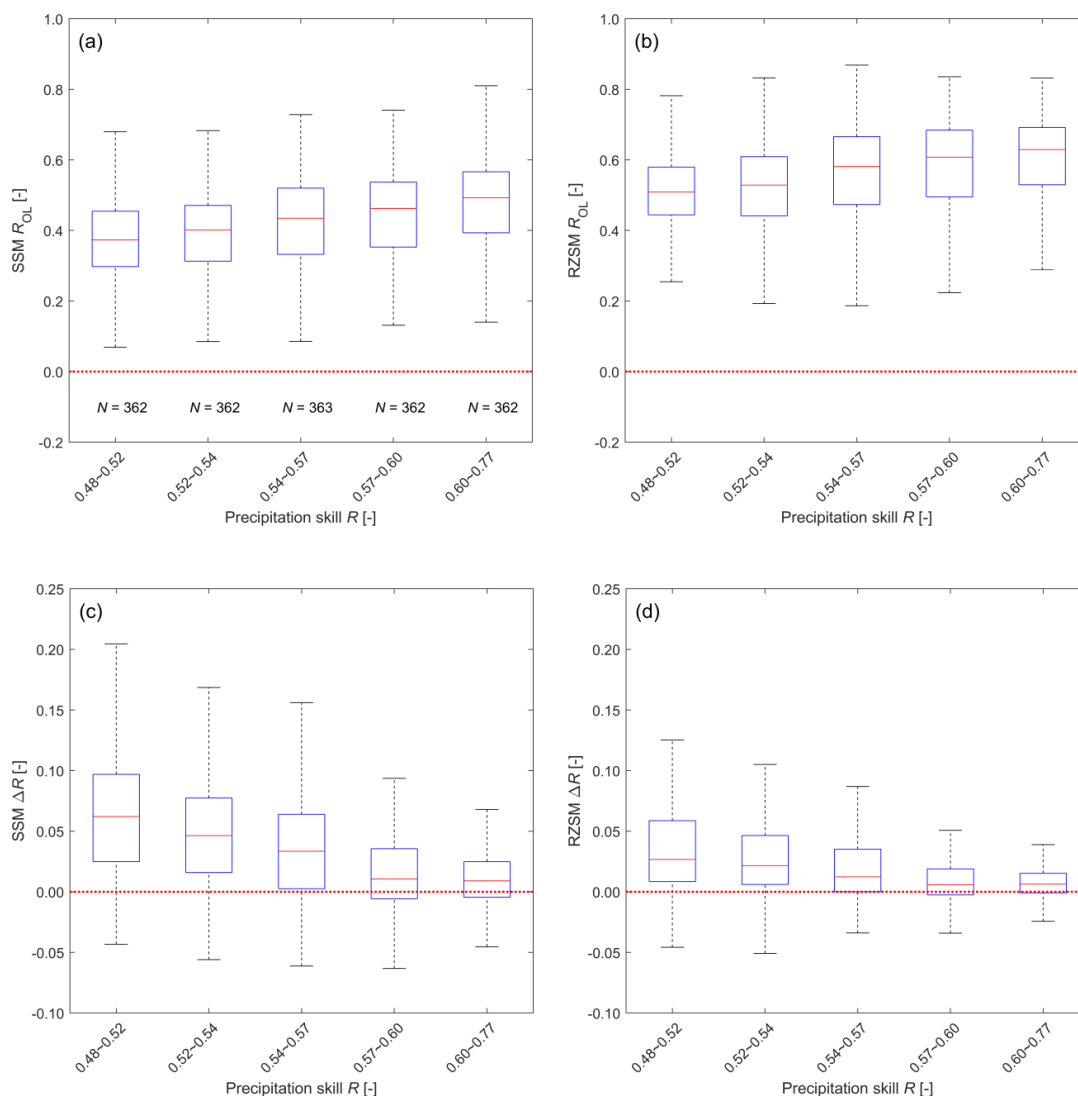


368

369 **Figure 4: SMAP L4 DA efficiency ($\Delta R = R_{L4} - R_{OL}$) as a function of Tb error for (a) SSM and (b) RZSM. Samples with Tb**
370 **error ranking above the 80th percentile are excluded from the analysis.**

371

372 For precipitation, this decomposition is illustrated in Fig. 5. Note that, as expected, low-quality precipitation tends to
373 degrade the skill (i.e., correlation versus ground observations) of OL SSM and RZSM estimates (see Fig. 5a-b). This
374 degradation provides an enhanced opportunity for SMAP L4 DA to provide added value. As a result, ΔR tends to be a
375 proportional function of precipitation skill (i.e., higher precipitation skill leads to lower ΔR , see Fig. 5c-d). This inverse
376 relationship is a well-known tendency for land data assimilation systems (Liu et al., 2011; Bolten and Crow, 2012;
377 Dong et al., 2019a). Precipitation quality has a diminished impact on RZSM estimation skill compared to SSM
378 estimation skill. This is expected since RZSM is (essentially) the result of applying a low-pass time series filter to
379 precipitation. As such, it is less sensitive to high-frequency errors in precipitation products than SSM is.



380

381

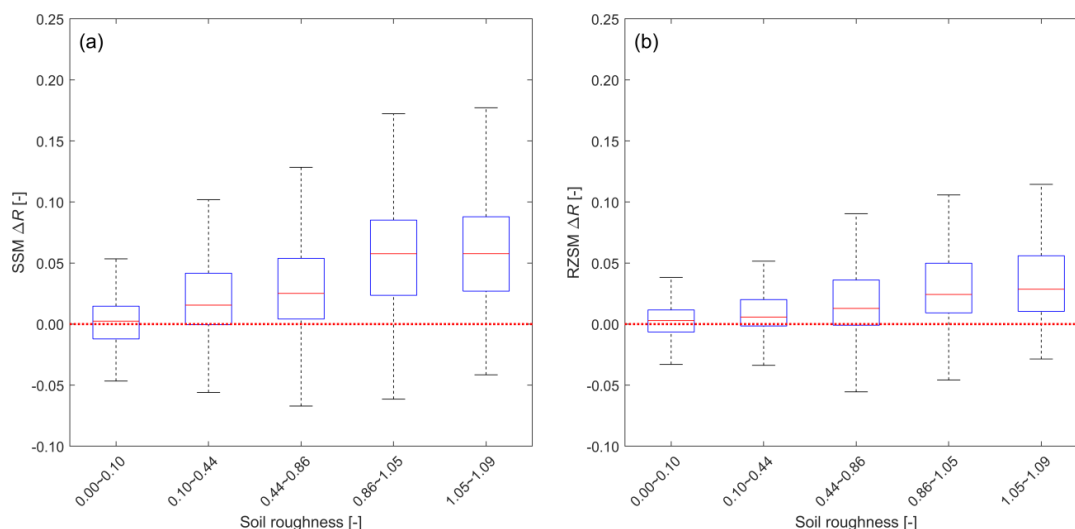
382 **Figure 5: OL performance (R_{OL}) as a function of precipitation forcing skill R for (a) SSM and (b) RZSM. SMAP L4 DA**
383 **efficiency ($\Delta R = R_{L4} - R_{OL}$) as a function of precipitation skill for (c) SSM and (d) RZSM. Samples with precipitation skill**
384 **ranking below the 20th percentile are excluded from the analysis.**

385

386 Figure 6 is analogous to Fig. 4 but shows skill differences ΔR as a function of microwave soil roughness. Similar to
387 Tb errors, it is as expected that this control factor of microwave soil roughness has little impact on the OL performance,
388 except that R_{OL} shows slight decreasing tendency with increasing soil roughness (not shown). Given the fact that the



389 OL does get worse with increasing roughness, there is more room for improvement as the roughness increases, which
390 makes it plausible that ΔR increases with increasing soil roughness (see Fig. 6a-b).



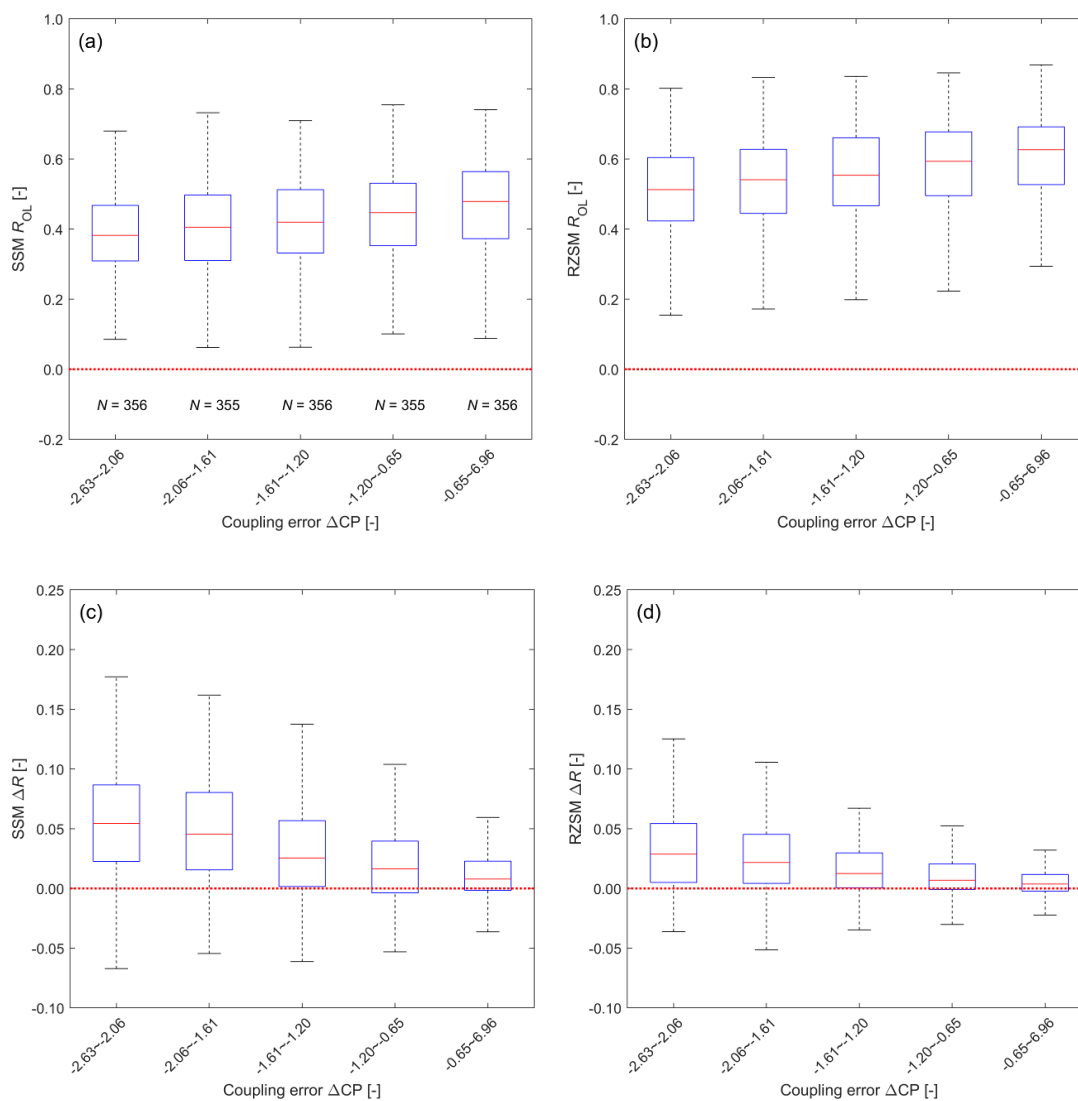
391

392 **Figure 6:** As in Fig. 4 but for ΔR as a function of microwave soil roughness.

393

394 Besides the above three control factors that dominate the DA efficiency, we also examine the top factor that affects
395 SMAP L4 performance, i.e., vertical-coupling errors (Fig. 7). As expected, larger (absolute) bias in SSM-RZSM
396 coupling in CLSM tends to be associated with degraded OL estimates of both SSM and RZSM (see Figs. 7a-b),
397 although the analysis does not prove such a causal relationship. Similar to precipitation errors above, decreased OL
398 skill (seen on the left-hand-side of the figures) provides an opportunity for increased DA efficiency – which is clearly
399 seen in Fig. 7. However, such increases are much larger for SSM than for RZSM.

400 For RZSM, SSM-RZSM coupling bias represents a double-edged sword. While such bias leads to an enhanced
401 opportunity to improve upon a degraded OL, it should also hamper the ability of DA to transfer SSM increments into
402 the root-zone – particularly when, like here, the bias reflects the lack of vertical coupling in the model (Kumar et al.,
403 2009). This means that some of the opportunity presented by the larger OL RZSM errors is squandered by sub-optimal
404 DA. As a result, the increase in RZSM DA efficiency associated with biased SSM-RZSM coupling (Fig. 7d) is smaller
405 than the analogous increase in SSM DA efficiency (Fig. 7c).



406

407

408 **Figure 7:** As in Fig. 5 but for R_{OL} and ΔR as a function of SSM-RZSM coupling error indicated by the CP difference (ΔCP
 409 = $CP_{OL} - CP_{obs}$).

410

411 For the three strongest control factors that determine DA efficiency ΔR , i.e., Tb error, precipitation error and
 412 microwave soil roughness, we further conducted paired one-way analysis of variance (not shown). Results indicates
 413 that for each of the five binned groups separated by each of the above-mentioned three control factors, the inter-group
 414 difference in ΔR caused by each control factor is significant ($p < 0.01$) for both SSM and RZSM. In addition, except for



415 the groups with lowest mean ΔR in Fig. 4a and Fig. 6a, the averages of ΔR from all groups are significantly higher
416 than 0 ($p < 0.01$).

417 As expected, precipitation error is the dominant factor for explaining the skill of the OL estimates. In contrast, the
418 SSM-RZSM coupling error is the dominant factor for explaining the skill of the L4 results, which shows DA is able to
419 correct for precipitation errors.

420 **4 Conclusions**

421 The SMAP L4 algorithm assimilates L-band Tb observations into the Catchment Land Surface Model, to provide
422 surface and root-zone soil moisture estimates (i.e., SSM, RZSM) with global, 3-hourly coverage at 9-km resolution.
423 The performance of the L4 soil moisture estimates compared to a baseline model-only simulation (OL) is influenced
424 by multiple control factors associated with the land surface modelling (LSM) and radiative transfer modeling (RTM)
425 components of the L4 system. In this study, we assess the performance of SMAP L4 DA system using the 2 years of
426 in-situ soil moisture profile observations at 2474 sites across mainland China. We apply a random forest (RF)
427 regression to identify the dominant factors that control the spatial distribution of the DA efficiency (defined as the skill
428 difference between the L4 and OL estimates of SSM and RZSM as measured by their Spearman rank correlation with
429 in-situ measurements). Results show that L4 improves SSM prediction skill by 14% on average, with over 77% of the
430 2287 9-km EASE grid cells showing an increase in Spearman's rank correlation with in-situ observations. Similarly
431 widespread but smaller improvements are also observed in RZSM, with averaged R improvement of 7%.

432 Based on the RF regression analysis, the added value of SMAP L4 DA for SSM is primarily determined by Tb error
433 (measured by standard deviation of O-F Tb residuals), followed by microwave soil roughness and daily precipitation
434 error. These three factors are also the most prominent factors controlling SMAP DA improvement for RZSM, albeit
435 with the Tb error being the least important of these three factors for RZSM DA efficiency.

436 Generally, the OL performance clearly decreases with increasing precipitation error, whereas for L4 performance
437 precipitation error is not identified as the most dominant control factor. This indicates that the L4 system is able to
438 correct for errors in precipitation forcing. In addition, our results demonstrate that SMAP DA contributes the most
439 added value for cases where CLSM underestimates SSM-RZSM vertical coupling strength. However, due to the
440 difference in top-layer soil depth between the in-situ observations (10 cm) and the L4 analysis (5 cm), it is unclear
441 whether or not the observed SSM-RZSM coupling strength biases are real in an absolute sense – or simply reflect
442 inconsistencies in the depth of modelled versus observed SSM and RZSM time series. Nevertheless, it is worth
443 stressing that, despite the ambiguity with regards to their absolute magnitude/sign, relative variations in apparent SSM-
444 RZSM coupling biases explain a significant amount of the observed spatial variation in L4 performance. Therefore,
445 this finding clearly underpins the importance of properly specifying SSM-RZSM coupling strength in CLSM as a way
446 to improve the SMAP L4 product.



447 For SMAP L4 SSM skill, the next-most important factors (after SSM-RZSM coupling) are the precipitation error, the
448 Tb error and microwave soil roughness (Fig. 3d). For L4 RZSM skill, the next-most important factors (after SSM-
449 RZSM coupling) are the precipitation error, the Tb error and the LE error, with the latter two factors of comparable
450 importance (Fig. 3d). To enhance the L4 performance, additional focus should thus be placed on improving the model's
451 characterization of the partitioning of the available energy into latent and sensible heat (LE error) and the microwave
452 radiative transfer modeling (Tb error).

453 **Data availability**

454 The SMAP L4 datasets are available from <https://nsidc.org/data/SPL4SMAU/versions/4>. Gauge-based precipitation
455 dataset CGDPA is from http://data.cma.cn/data/cdcdetail/dataCode/SEVP_CLI_CHN_PRE_DAY_GRID_0.25.html.
456 The availabilities of other datasets are stated in their corresponding subsections.

457 **Author contributions**

458 Jianxiu Qiu and Jianzhi Dong conceptualized the study. Jianxiu Qiu carried out the analysis and wrote the first draft
459 manuscript, Wade Crow refined the work, Jianzhi Dong, Rolf Reichle, and Gabrielle De Lannoy helped with the analysis.
460 All authors contributed to the analysis, interpretation of the results and writing.

461 **Competing interests**

462 The authors declare that they have no conflict of interest.

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