Comments on the Era of Infiltration

Editor

Dear Keith,
the three reviewers provided thoughtful, interesting and useful comments for which I like to thank them. Also thank you for your first level reply to these comments. Overall, the picture that is coming through from the reviews is very positive. Clearly, this paper will help the hydrological community to better understand the background to theories and practices we are using. The reviews also demonstrate that discussing this background reveal somewhat different perceptions that these theories hold in our science. If this paper would stimulated further that discussion, it would be a very good outcome of this special issue contribution.

What I propose is that you try in the discussion to reflect somehow this diversity of opinions, e.g. on if the era of infiltration is over or not and the general lack of verification of our theories as a reason for the over-reliance on infiltration theory. A few other suggestions have been made by the reviewers, I stimulate you to consider these.

I agree with Referee #3 that a restructure of the beginning of the paper could help digesting the structure of the paper easier. The paper now starts off as if it is obvious what the 'Infiltration theory of runoff' entails. I am afraid we cannot assume this. An initial short description of your understanding of this theory and how and in which section this will be further explained and discussed would go a long way in giving the reader some guidance.

Dear Okke,

I have produced a new version of the paper (added below) in response to the referee comments with a somewhat revised structure. Some of the discussion of Horton's 1933 paper has been moved to the beginning to provide a starting point and definition for the Era of Infiltration as requested.

Line 492 identified by Roger Smith has been corrected, along with some other minor corrections to spellings and grammar.

I am currently stuck in Switzerland without access to the original papers that the figures are based on. I cannot therefore produce better copies. Given the age of those papers I hope that the existing figure copies will suffice – they are perfectly legible.

In terms of more general points made by the referees, I make the following observations.

Roger Smith:

Appreciation of complexity of responses by hydrologists at the time: I think I do more than adequately cover this in the discussion, with the citations from Cook, Musgrave and references to Hursh and others.

Necessity for engineering approximations: I also think I make clear that this is the main reason for the rapid adoption and persistence of infiltration approaches.

Fred Ogden:

People not caring about infiltration: but is this not because they have "engineering approximation" models readily available? But which (for example in SWAT) infiltration excess is already included but just as another one or two parameters, so they do not have to

think too much about it. So it is treated as a sort of solved problem, rather than a misperception.

Lack of knowledge about subsurface processes and lack of alternatives to infiltration theory: Yes, but as already mentioned in the text, to use infiltration theory in such circumstances is delusional – and it is not as if other representations of subsurface flow do not exist at all. Two more references to lack of knowledge about subsurface processes have been included in the text.

Infiltration modelling remains an important need: Agreed, and now emphasised in the text where it might be appropriate (with reservations about scale issues). The Ogden et al. 2015 paper has now been cited.

Definitions of runoff processes: I have reviewed this discussion in the light of Fred's comments and my initial response but I think I stand by what I wrote in the original submission.

Lack of a verifiable theory: Well, yes – and how this impacts the application of hydrological models is the subject of a long and continuing debate (and a whole book on rainfall-runoff modelling on my part). I have added a reference to the recent Beven and Chappell 2020 paper in this context and some brief comments in the final discussion.

Referee 3.

Structure: The paper now starts with Horton's classic statement on infiltration.

Baseflow: not sure how this could really be made clearer. There is already a section on baseflow separation and I already discuss how the original hydrologists involved recognised that the separation of surface and subsurface flows was difficult. I also point out that ANY form of baseflow separation is ambiguous, particularly given tracer data.

Comparison of infiltration equations: I already give a number of citations where such comparisons are made. I do not think any further comparison is necessary here. As I note in my initial response, some might better fit a particular set of observations at a particular scale, and others a different set of observations.

Nomenclature: The ambiguity in symbols has been clarified by the use of different symbols or superscripts so as to avoid changing certain symbols in their traditional context.

Scale of infiltration observations: This was already mentioned but has been emphasised in several places.

Interactive comment on "The era of Infiltration" *by* Keith Beven

Roger Smith (Referee)

gromitroger@gmail.com
Received and published: 20 July 2020

The recommendations 1 and 2, above, are low because this is strictly not an original scientific paper but is a review paper.

Line 492 contains an awkward sentence, the word "data" needs to be relocated.

The author points to early efforts to describe the separation of rainfall into runoff and soil storage and characterises hydrologists 80 years ago in general as believing that the soil surface exhibited the dominant mechanism. It is in some ways a scientific cri- tique of methods largely engineering-oriented, and as such his critique is somewhat misdirected. Indeed, most of the early work he cites was done simply to try to de- scribe, parametrically, processes observed, rather than study them scientifically - I am sure Horton and Holtan, for example, were simply trying to describe the rainfall loss function, and were not trying to express a general soil water flow theory. Importantly, the end product was to have engineering application. Infiltration controlled by soil sur- face properties (infiltration theory) yet has its place in hydrology in several climates and soil conditions, but we know of course that it is not universal. The author believes that in the "era of infiltration" there was belief that this was general or universal. The processes on a catchment are of course varied, and moreover almost any catchment exhibits significant water flow variability both vertically and spatially. This reviewer is not convinced that early workers such as Holton did not appreciate this to some extent. But again, theirs was not a scientific objective. It is unclear in the end what is the au- thors point: Complexity and variability exist, infiltration by surface control also exists, a wide variety of paths from rainfall to the stream exist; we know these things. Applica- tion of scientific knowledge of flow proceesses to describe or predict a rainfall-caused hydrograph from any natural catchment simply requires more detailed soil and surface geology data than is practical to measure, and engineering approximations, such as the author cites, will continue to be required.

Interactive comment on Hydrol. Earth Syst. Sci. Discuss., https://doi.org/10.5194/hess-2020- 308, 2020.

Reply

Thanks for the comments Roger. Having looked into Horton's papers, I think he was really interested in the phenomenon and controls on infiltration as a scientist. The unpublished Monograph on Infiltration for example describes his experiments with large cores, his appreciation of the effects off air pressure and discusses the role of macroipores in water entry and air escape. There were, of course, other soil physicists working at the time to elaborate how water moves through soils, so the whole devel- opment of infiltration theory was being made within that context. But, as you point out, that was not the same as using infltration theory for practical applications. As I point out in the paper, this was convenient, as well as having a theoretical basis - so very marketable! But I do say that some of the people involved understood that it was not general or universal (the "unknown mix" of surface and subsurface flows) but the result was that it was widely applied where that theoretical basis was incorrect (and the real point is that it still is in the form of many models). So while I very much agree that engineering applications that simplify the complexity are required, I wish to push for methodologies that are more realistic in their assumptions.

Interactive comment on Hydrol. Earth Syst. Sci. Discuss., https://doi.org/10.5194/hess-2020- 308, 2020.

Interactive comment on "The era of Infiltration" *by* Keith Beven

Fred Ogden (Referee)

fred.ogden@noaa.gov
Received and published: 21 July 2020

My review is written from the perspective of a hydrologic model developer who devel- ops models to solve practical hydrograph prediction problems, firmly in the domain of "hydrologic engineering". From a practical standpoint, given that all models are falsifi- able, we seek models with the smallest number of parameters that predict hourly hydrographs reasonably well on a continuous basis when driven by reasonably accurate hourly forcing data. From the public safety and welfare standpoint, we are particularly interested in the peak discharge, its timing, and the total event runoff volume, especially for larger events.

In this paper Beven makes the point that for too long, modelers have overemphasized the role of infiltration on stormflow generation. I agree with this statement. Keith does his usual excellent deep dive into historical writings to illustrate that many contemporary research questions were well elucidated in the first half of the last century. I found the article an enjoyable read.

As a developer of several novel infiltration solutions, I would counter that the "era of infiltration" is largely over. Few people in hydrologic science today seem to care too much about infiltration. Outside the fields of soil physics and applied mathematics it is viewed as an esoteric topic. When my co-authors and I published the work describing the steps leading to the Soil Moisture Velocity Equation (Ogden et al. 2015, 2017) one of the reviewer comments was: "Most of the people who would care about this topic are deceased."

Beven concludes that over-reliance on falsified perceptual models related to the impor- tance of infiltration theory in runoff generation impedes progress. Rather, I see this a symptom of our lack of detailed knowledge, not the cause. Much of the field research effort expended in hydrologic science over the past 30+ years focused on highly uncer- tain subsurface processes and their role in runoff generation. Studies using inferences from light stable isotopic tracers and geochemistry to infer flow path and residence times in study after study provided site-specific results, and to date no common theory has arisen.

The reason for over-emphasis on infiltration theory or the persistent use of regression- based empirical approaches (e.g. CN) or other gross conceptualizations in runoff prediction lies squarely with the lack of a comprehensive and verifiable theory of runoff generation. As Beven correctly wrote, surface runoff is seldom seen in many hydrologic landscapes. In those cases, what is the alternative to infiltration theory? Catchment scale hydrographs remain flashy, even in the absence of observed surface runoff!

Nevertheless, accurate infiltration modeling remains an important need. Infiltration has a large effect on the catchment-scale water balance, particularly as it determines the store of water that is used by shallow-rooted plants through transpiration in many locations, at least during certain times of the year. Failure to correctly model this flux, or its omission, destroys the ability of a model to simulate an important hydrologic process, which renders models incapable of accurately closing the water and energy budgets.

Surface runoff, defined as water that enters the stream without having ever entered the subsurface, does occur; most commonly from areas of disturbed soils associated with agriculture, construction, and urbanization. As a flux, it frequently occurs in response to heavy to extreme rainfall, independent from runoff generation mechanism. I am not aware of a many instances where subsurface stormflow alone is responsible for flash flooding and its associated risks to life and property, except perhaps in situations where karst geology is involved.

In general, the specific terms: surface runoff, interflow, return flow, and groundwater flow or base flow describe useful concepts. They connote flow paths not mechanisms. I think when applied within the bounds of the WMO definitions, these terms are valid. Is it not reasonable to assert that stormflow consists of a superposition of surface runoff and interflow atop base flow? This definition remains valid if only one of these flow paths is non-zero.

Differentiation between flow path and runoff generation mechanism is important. The infiltration-excess and saturation-excess mechanisms have clear definitions, and might be considered well-behaved end-members that do occur in some catchments, even if only rarely, intermittently, and only under precisely defined conditions. When they are known to occur, these two mechanisms are highly predictable using models with a relatively small number of parameters.

However, there exists a vast state/parameter space lying between these two runoff gen- eration end members and it appears to be incomprehensibly complex. In this region heterogeneities dominate, as do uncertainties in processes, parameters, and difficult to identify, describe, quantify, and model unsteady bio-physiographic and anthropogenic phenomena. This complexity is bounded at the lower end by Occam's razor and the concept of model parsimony, with a nearly limitless upper bound occupied by parameter estimation schemes and the concept of equifinality.

I thank Keith Beven for writing this thought provoking paper. However, after reading it I have come to a different conclusion. I believe that the lack of a general, verifiable theory of runoff generation, hampered by our inability to

know what is truly going on in the subsurface is the problem. Over-reliance on infiltration theory and other empiricisms is merely a symptom caused our lack of this knowledge.

Cited Literature: Ogden, F.L., W. Lai, R.C. Steinke, J. Zhu, C.A. Talbot and J.L. Wilson, 2015. A new general 1-D vadose zone solution method. Water Resour. Res. 52, doi:10.1002/2015WR017126. Ogden, F.L., M.B. Allen, J. Zhu, W. Lai, C.C. Douglas and M. Seo, 2017, The soil moisture velocity equation. J. Adv. Model. Earth Syst. doi:10.1002/2017MS000931.

Interactive comment on Hydrol. Earth Syst. Sci. Discuss., https://doi.org/10.5194/hess-2020- 308, 2020.

Reply

Thanks for the comments Fred and I am happy that you found it to be an interesting read!! Like Roger you point out the continuing requirement for methods for engineering applications, and that is actually why I do not agree that the era of infiltration is over. There are far too many models that are based on the idea that fast runoff production is produced by an infiltration excess mechanism (e.g all over a HRU in SWAT - perhaps the most widely used model in hydrology - based either on the CN or Green-Amp options with homogeneous parameters). I do think that this is worth pointing out as delusional - even if functionally such models can be calibrated to give "good fits" to hydrographs. But machine learning can do that too (indeed often somewhat better than hydrological models) so perhaps we should be moving more towards engineering methods that are more realistic in their process understanding. This was an opportunity to say so, given the often obvious misapplication of some infiltration based models. C1

Your final comment on the lack of a general hydrologic theory is clearly related to this. Given the detailed complexity of hydrological systems, and our lack of observational ca- pability in the subsurface, this is clearly challenging problem and one that I have strug- gled with throughout my career (including, as you know, all the work on the limitations of Darcy-Richards and trying to represent preferential flows). I suspect that this might also be solved by matching learning (see my recent commentary on Deep Learning in Hydrological Processes at https://onlinelibrary.wiley.com/doi/10.1002/hyp.13805). In the meantime, however, we should at least try and avoid applying misconceptions - even for engineering applications!

Interactive comment on Hydrol. Earth Syst. Sci. Discuss., https://doi.org/10.5194/hess-2020- 308, 2020.

Interactive comment on "The era of Infiltration" *by* Keith Beven

Anonymous Referee #3

Received and published: 12 August 2020

This is an interesting manuscript with a number of valuable references and thoughtful remarks. While I tend to agree with much that is being said, my feeling is that the text could have a larger impact if it would be better structured. As it is now, I am frankly not seeing such a structure. My suggestion would be to start with a description of the formulations for infiltration in the 'era of infiltration', followed by a discussion of what is wrong with this approach and how it has been misused (and still is?).

A question is how baseflow separation could/should be included. To me, this aspect is somewhat away from the main focus, but one could make that it is related to infiltration, just fro the other side of things (ie., the effect of infiltration on outflow composition). However, this link should be made clearer.

Table 1 is useful, also the description of the different formulae in the text. I especially found discussions such as the origin of the 0.2 in the CN approach interesting and valuable. Would a graphical comparison of the approaches be possible/useful? To which degree does the shape of infiltration over time differ? How flexible are the approaches? The table could be extended by some more information on the observational basis of each formula. Also in table 1 (and in the text), there are parameters that occur in differ- ent places. Sometimes these refer to the same thing (Ksat) but sometimes the same letter refers to very different parameters even with different units (e.g., 'alpha', 'n'). This should be clarified.

One issue that did not become fully clear to me is the scale of the infiltration equations. Often these have been derived from plot scale experiments but were then used at the catchment scale. I feel it would be valuable to discuss this aspect more.

Interactive comment on Hydrol. Earth Syst. Sci. Discuss., https://doi.org/10.5194/hess-2020- 308, 2020.

Reply

I will certainly think about improving the structure when preparing the revised manuscript but it is not clear that the referee has fully understood that this is a contribution to the special issue on the History of Hydrology. I therefore have not chosen to deal with the different performance of the infiltration models (but of course some might better fit a particular set of observations at a particular scale, and others a different set of observations) but rather the concepts and how they were developed. I do address the baseflow issue, because the difficult of differentiating surface and subsurface contributions to the hydrograph was understood at that time. I do discuss some of the methods that were used then (and later) but again do not feel it is necessary to compare performance (because there can no real right answer). There is already some discussion of scale issues but certainly that could be extended.

I am grateful to all the referees for their comments.

Interactive comment on Hydrol. Earth Syst. Sci. Discuss., https://doi.org/10.5194/hess-2020- 308, 2020.

The era of Infiltration

Keith Beven
Lancaster Environment Centre
Lancaster University
Lancaster, UK
k.beven@lancaster.ac.uk

Abstract

Inspired by a quotation from Howard Cook in 1946, this paper traces the evolution of the infiltration theory of runoff from the work of Robert Horton and LeRoy Sherman in the 1930s to the early digital computer models of the 1970s and 1980s. The reasons for the popularity of the infiltration theory are considered, as well as its impact on the way in which hydrological responses were perceived by several generations of hydrologists. Reconsideration of the perceptual model for many catchments, partly as a result of the greater appreciation of the contribution of subsurface flows to the hydrograph indicated by tracer studies, suggests a more precise utilisation of hydrological terms and, in particular, that the use of runoff and surface runoff should be avoided.

> *Some future historian of the development of scientific hydrology will probably be tempted to call the present period the "era of infiltration." At any rate, the preoccupation of contemporary hydrologists with "the infiltration theory of runoff," and the vast amount of energy they have expended in an effort to turn this concept to practical account, will certainly be put down as a distinctive feature of our times.*
>
> Howard L. Cook, 1946 (p.726)

The Background to the Era of Infiltration

This quotation from Howard L. Cook has stimulated this paper which has the aim of trying to understand why the "*infiltration theory of runoff*" came to have such an impact on hydrological understanding and analysis from the 1930s onwards, particularly in the work of American hydrologists such as Robert Elmer Horton[1], LeRoy Kempton Sherman[2], Waldo Smith[3], Cook himself and many others. In particular to consider the question of why, when in many parts of the United States overland flow is just not observed that often, the infiltration theory of runoff achieved such a widespread acceptance both in the US and elsewhere. The literature in relation to infiltration and surface runoff is, however, vast and a complete review is not possible. I hope to have brought out the most important points and references relevant to this question, particularly from some of the earlier publications.

Deleted: is

[1] (1875-1945), see http://www.history-of-hydrology.net/mediawiki/index.php?title=Horton,_Robert_Elmer
[2] (1869-1954), see http://www.history-of-hydrology.net/mediawiki/index.php?title=Sherman,_LeRoy_K.
[3] (1900-1994), Executive Director of AGU from 1944-1970, see https://honors.agu.org/waldo-e-smith-1900–1994/

We will take the start of the era of infiltration as the 1933 paper *On the role of infiltration in the hydrological cycle* in the Transactions of the American Geophysical Union by Robert Horton. That was not the start of infiltration studies in the United States. Before that there had been experimental studies of infiltration, particularly in relation to irrigation practices (e.g. Muntz et al., 1905) and at the plot scale (e.g. Houk, 1921) as well as the model of infiltration of Green and Ampt (1911). In the 1933 paper, however, Horton sets out a particular perceptual model of catchment response in an often-cited quotation.

> *"Infiltration divides rainfall into two parts, which thereafter pursue different courses through the hydrologic cycle. One part goes via overland flow and stream-channels to the sea as surface-runoff; the other goes initially into the soil and thence through ground-water flow again to the stream or else is returned to the air by evaporative processes. The soil therefore acts as a separating surface and the author believes that various hydrologic problems are simplified by starting at this surface and pursuing the subsequent course of each part of the rainfall as so divided, separately. This has not hitherto, in general, been undertaken."*
>
> Horton (1933, p.446/447)

This last sentence (not so often cited) suggests that this provides a good starting point. More than a decade later, the context of the Cook quotation was the report of the AGU Committee for Infiltration for 1946, chaired by G. W. Musgrave who worked in the Soil Conservation Service at that time. This committee had a number of sub-committees: on Infiltration and the Physics of Soil Moisture and of the Infiltration Process; on Infiltration in Relation to Ground Water; on Infiltration in Relation to Snow and Its Physical Properties; on Infiltration in Relation to Surface Runoff; on Infiltration in Relation to Irrigation; and on Infiltration in Relation to Evapo-transpiration and the Consumptive Use of Water. Infiltration was therefore considered to be both central and fundamental to hydrological understanding. The preface to the Cook article provided by Musgrave is pertinent to our question:

> *"In the early phases of the development of a new concept, it is common to find considerable diversity of thought among the workers in that field. Subsequently, through the exchange of ideas, and particularly through the development of factual evidence, abstract ideas are crystallized into specific entities. Progress in the development of the field is increased, and practical application of ideas that originally were abstract now proceeds with greater and greater success.*
>
> *The concept of infiltration as a factor modifying runoff phenomena is still relatively new. Discussions quite diverse in their conclusions abound in the literature. Is it not true that at least some of the diversity of thought is due to diverse interpretations of terms and definitions? Indeed, it would seem that there is need for re-examination of some of the very fundamentals of the problem.*
>
> *Many have realized during the past several years that there is great need for clarification of thought in this relatively new phase of hydrology. Many have realized that whatever may be done to promote thinking and expression in terms that are specific and are understood by all other workers is certain to result in improved research and improved application of research findings.*

Formatted: Font: Italic

Moved (insertion) [1]

Deleted: It is worth noting that well before the development of the infiltration theory in the US, there

Formatted: Indent: Left: 1.27 cm

Formatted: Font: (Default) +Body (Calibri), 12 pt, Italic

Formatted: Font: (Default) +Body (Calibri), 12 pt, Italic

Formatted: Font: Italic

Formatted: Font: (Default) +Body (Calibri), 12 pt, Italic

Formatted: Font: (Default) +Body (Calibri), 12 pt

Formatted: Normal, Right, Indent: Left: 1.27 cm, Don't adjust space between Latin and Asian text, Don't adjust space between Asian text and numbers

Deleted: T

Deleted: [4]

> *This paper should do much in the way of promoting unanimity in use of terms, of opinion as to their significance, and of clarity of concept."* (Musgrave, 1946a, p726)

The Sub-committee on Infiltration in Relation to Surface Runoff was chaired by Howard Cook, the other members being W. W. Horner, R. A. Hertzler, G. A. Hathaway, and Walter B. Langbein[5]. Cook had been one of the principal assistants of Robert Horton at the Horton Hydrologic Laboratory in Voorheesville, New York[6].

The popularity of the infiltration theory

Following the quotation at the head of this paper, Cook starts his outline of the subject by considering why the infiltration concept had become so popular:

> *"There have, of course, been logical reasons for this remarkable interest in the subject. As in all sciences, many have been attracted to it simply because of its newness. Another class—and the one that has participated most eagerly—is composed of those intrepid practicing engineers who are obliged to make the runoff estimates upon which depend the failure or success of costly flood control, water supply, and similar works. Still another group has been intrigued by a purely scientific interest, sharpened by the fact that the calculation of runoff is the central problem of the science of hydrology and involves all phases of the hydrologic cycle. Among these are scientists in the fields of soils, plants, and meteorology. As a result of these various motivations, vast amounts of labor have been expended - much of it misdirected - and many exaggerated claims have been made, to be countered, naturally, by the disparaging murmurs of the "old guard," and other important lines of investigation have been temporarily slighted. But real progress has been made. Better estimates of runoff are now possible than could be made previously. Problems that would not yield at all to earlier methods are now soluble, albeit the solutions are sometimes only rough approximations. The inescapable conclusion is that a tool of considerable practical value has been added to the equipment of the hydrologist."* (Cook, 1946, p727)

This quotation already reveals some quite modern elements of the sociology of an inexact science. The infiltration concept provided a new paradigm for thinking about runoff. It did so in a *rational* way *"simply by providing a physically correct concept of the runoff process"* (p.730), but which also provided the engineer with a tool that could be usefully applied to provide better estimates of runoff for design purposes (even if sometimes only *rough approximations*). I do wonder if any of that old guard were murmuring … but should you not be able to see the surface runoff occurring during storms to apply this type of analysis properly?

[5] (1907-1982), see http://www.history-of-hydrology.net/mediawiki/index.php?title=Langbein,_W

[6] Howard L. Cook graduated in Civil Engineering from the State University of Iowa in 1929 then worked at the Horton Hydrological Laboratory as assistant to Robert Horton from 1929 before moving to the Soil Conservation Service in 1934 where he was in charge of hydraulic research. He later worked as an engineer for the Department of the Army. I have not been able to find a full obituary of his life and career.

Surface and subsurface runoff

Cook, in fact, almost immediately recognises the difficulty of applying the concept in practice in a section on surface and subsurface runoff. He notes that:

> "*The runoff from an area is the water flowing from it over the surface of the Earth, either in streams or as overland flow. Part of this water has never been below the surface. This is called surface runoff. Another part has previously passed into the Earth and subsequently returned to the surface. This is called subsurface runoff…"* (op. cit. p.728).

He continues:

> *"(1) Only surface runoff can be directly determined from Infiltration data. (2) When runoff contains subsurface flow, the gaged discharge cannot be used to derive infiltration data for the area unless the surface runoff can be separated from the total. (3) In general, there is no way of separating surface and subsurface runoff when only records of the rates of flow are available*." (op. cit. p.728)

There is also an interesting comment that:

> "*A normal stream. carries both surface and subsurface flow in proportions varying widely from time to time. During floods most of the water discharged from deep-soiled drainage basins is ordinarily made up of surface runoff. However, in areas of low storage capacity (such as thin-soiled basins) a large proportion of the flood water may consist of subsurface runoff."* (op. cit., p.728)

The reasoning behind this statement is not clear. It implies an expectation that catchments with thin soils and small storage capacities would be associated with higher infiltration capacities and higher downslope transmissivities such that there could be a greater contribution of subsurface stormflow. However, the reasoning might have run more along the lines that high storage capacity will mean a longer mean residence time so that any infiltrated water would simply not be able to contribute within the time scale of the hydrograph. Cook also notes later that in deeper soils when water tables are low in summer, infiltrating water may not actually reach the saturated zone.

In fact, the role of subsurface runoff production was being promoted more generally at this time. Charles R. (Chuck) Hursh[7], Director of the Coweeta watershed experiments in North Carolina, had long been promoting the idea that in places where overland flow was only rarely seen, such as in the forests of the Appalachians, the hydrograph was necessarily dominated by direct channel precipitation and subsurface flows, with only slow responses observed in boreholes (Hursh, 1936, 1944; Hursh and Brater, 1941). It is also not as if hydrologists did not realise that in different parts of the US there was less expectation of overland flow. In a national review of flood runoff published during the era of infiltration Hoyt and Langbein (1939) noted, with some surprise, that: "*To those who are acquainted*

[7] (1895-1988), see http://www.history-of-hydrology.net/mediawiki/index.php?title=Hursh,_Charles_R

with the flood-producing possibilities of isolated storms of from 10 to 12 inches [250-300mm] *in humid areas, the absence of flood-runoff under single storm-experiences of the same magnitude on steep mountain slopes of parts of the southern coast range* [in California] *is amazing*" (p.172). They continue:

> "*Although the small plots may indicate the absence of direct run-off and the differences between rainfall and runoff an absorption of between 15 and 20 inches, there is a rapid passage of a part of the infiltrated water into stream channels, either through the relatively shallow earth-mantel or through the upper parts of the shattered bedrock. To the extent that the observations and deductions are correct, the flood-hydrograph in these areas is composed largely of ground-water which has concentrated very quickly as to time superimposed on which is a small amount of direct runoff with irregularities closely following irregularities in the maximum rates of precipitation. This condition may also apply on other parts of the country where floods occur although studies on small areas indicate very high infiltration capacities.*" (Hoyt and Langbein, 1939, p.174)

That the infiltration concept was used much more widely however was undoubtedly due to a number of factors. The first was that it claimed to be *rational* or physically-based; the second was the simplicity of calculating amounts of runoff given information about rainfalls and infiltration capacities; the third was the strong and rather combative character of Robert Horton.

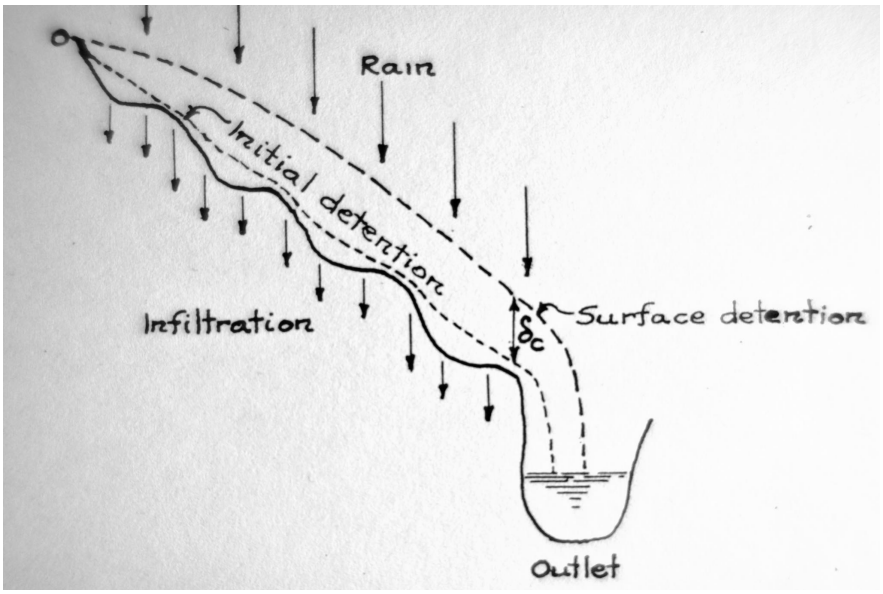

Figure 1. Half-Section of a Small Drainage Basin Illustrating Runoff Phenomena (Vertical Scale Greatly Exaggerated) (from Horton, 1935, with original caption)

Deleted: ¶
Horton's had earlier stated his view of the soil surface acting as a "*separating surface*" or "*sieve*" such that:¶
¶
"Infiltration divides rainfall into two parts, which thereafter pursue different courses through the hydrologic cycle. One part goes via overland flow and stream channels to the sea as surface runoff; the other goes initially into the soil and thence through ground-water again to the stream or else is returned to the air by evaporative¶ processes." (Horton, 1933 p.446)¶

In the 1933 paper Horton appears to buy in completely to the idea that storm hydrographs are produced by overland flow. This is also clear from his 1935 monograph on Surface Runoff Phenomena, from which Figure 1 is taken. This is perhaps an example of the pragmatics of applications outweighing the information from direct observations (Horton was working as a consultant by the 1930s). This is also evidenced in his paper on Remarks of Hydrologic Terminology later published in the Transactions of the AGU in 1942. He starts by saying that:

> *"When a science is advancing rapidly, as is hydrology today, especially when it is changing from an adolescent or qualitative to an adult or quantitative basis, new terms are needed in particular for the following two purposes: (1) To give expression to new ideas and concepts; (2) to give more definite, specific, quantitative meaning to terms and concepts heretofore chiefly qualitative."* (Horton, 1942, p.479)

However, in what follows it is clear that Horton's primary purpose is to favour his own terminology over that of others. There are a number of entries of this type (infiltration rate v. infiltration capacity; recharge v. accretion; plot v. plat[8]), but in the current context the one on subsurface runoff is of most interest. Thus:

> *"Subsurface and concealed-surface runoff*. Cases *arise where surface-runoff may take place in such a manner as not to be visible, as, for example, where it occurs through a layer of coarse material, sometimes through a thick matting of grass or mulch-cover; through a layer of plant roots close to the soil-surface and under forest-litter; or even, in some cases, (through a network of sun-cracks in the soil-surface. This has sometimes been called 'subsurface-runoff', sometimes 'ground-water flow'. The term 'subsurface-runoff' would not be objectionable were it not for the fact that it is likely to be confused with true ground-water flow. The term 'groundwater flow' applied to this class of flow is highly objectionable on several counts; flow occurring close to the surface in the manner described has little in common with true ground-water flow. It is mostly turbulent flow, while true ground-water flow is mostly laminar. It persists only during rainfall-excess or for a short time thereafter, measured in hours or at the most in days, whereas ground-water flow persists on perennial streams at all times. Furthermore, surface runoff follows the same laws and behaves in the same manner whether it actually occurs visibly on the ground surface, or is concealed and invisible, taking place just below the soil-surface where it is sustained by temporary detention below the soil-surface. Nevertheless, it may be desirable to distinguish between the two cases and, if so, flow which is essentially surface-runoff but which is concealed from view in some one of the ways described, may appropriately be called 'concealed-surface runoff.'"*
> (Horton, 1942, p.481)

Thus, by definition, water contributing to the hydrograph is allowed to be hidden from view and treated as surface runoff *as if* it was in excess of the infiltration capacity of the soil, at least if no longer a laminar flow. An example., taken from the boxes of Horton's papers in his analysis of downslope flow through sun-cracks (see Figure 2). Again, perhaps underlying this

[8] Horton argued that infiltration capacity, accretion and plat were to be preferred, citing Oxford English Dictionary definitions. In this at least, he has not got entirely his way in the long term.

Deleted: It is essentially in this statement that Horton laid the foundation of the infiltration theory concept.

Deleted: e

Deleted: w at this point

is an interpretation that laminar subsurface flow velocities were far too slow to allow significant contributions to the hydrograph (although, interestingly, observations from the Horton Hydrological Laboratory did show some examples of fast borehole responses, see Beven, 2004c).

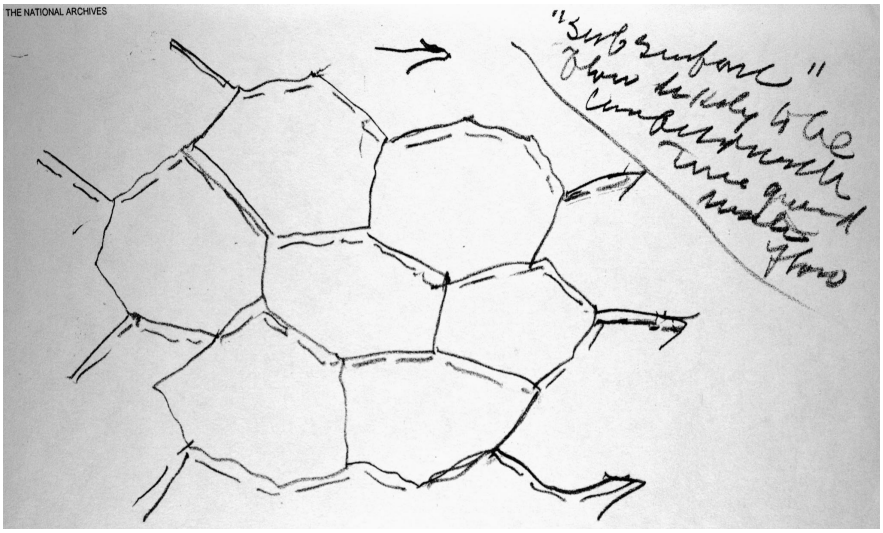

Figure 2. Figure explaining lateral "subsurface" flow in sun-cracks as concealed surface runoff (Drawing in Horton's hand from Box 71 of the Horton Papers in the National Archive)

We should remember that the tracer information that revealed that in many catchments hydrographs are composed largely of pre-event water was not available in the 1930s and 1940s, but Beven (2004a) shows that by comparing rainfall frequency data and Horton's own infiltration observations it is unlikely that he would have observed widespread overland flow on his own research catchment near Voorheesville more than 1 in 2 to 1 in 5 years (unless of course it was concealed!). Walter et al. (2003) had come to similar conclusions in an analysis of a number of sites in New York State.

The complexity of infiltration processes

Horton's perceptual model of the response of catchments was, however, much more sophisticated than he is generally given credit for. This was revealed in the 94 boxes of his papers that were classified by Walter Langbein (who had also worked with Horton) and deposited in the US National Archives in 1949 (see the discussions in Beven, 2004a,b,c). Horton argued, for example, that infiltration capacities would be primarily controlled at the soil surface by what he called extinction phenomena, such as compaction of the surface by rainsplash, and blocking of larger pores by displaced fine particles. It was these extinction phenomena that led to the gradual decline in infiltration capacities with time, as described by

his well-known infiltration equation that first appears in Horton (1939)[9]. He also recognised that bioturbation and agricultural practices would change the surface between events, resulting in a recovery of infiltration capacities. There could also be marked seasonal changes, something that he observed in his own infiltration observations, and strong variability in space. He recognised the role of macropores and surface microtopography in concentrating water and allowing the escape of air, which he had shown to be a control on infiltration by experiment (see Beven, 2004b). He also understood that while it was possible to make local predictions of infiltration excess on different land units (effectively producing a distributed model of surface runoff production), it was not possible to calculate the different contributions given only hydrograph contributions.

Horton was also not alone in recognising the complexity of infiltration processes in this period. In the discussion of a physics-based paper on infiltration by Willard Gardner (1946), G. W. Musgrave commented:

> "*However, we have before us a type of problem which particularly requires caution in extending and applying laboratory-findings to natural field-soils. At least insofar as the structure of the laboratory-sample differs from that of the natural soil, caution is warranted. Most soils of natural structure contain crevices, channels, and openings that transmit free water rather rapidly, though locally, to some depth. It appears from many observations in the field that in some cases at least, a very large portion of the infiltrating water is thus transmitted. Where a dye is used and the soil-profile is dissected following application, the highly irregular nature of the downward moving water becomes evident. Dry "islands" are bypassed and left with their air-water interfaces intact, at least temporarily. The channels conducting free water act as feeders laterally for capillary water, often for a considerable time. The forces of gravity and capillarity are not always acting in conjunction. One wonders whether other forces such as thermal gradients are involved, and if so, to what extent they are effective*."
>
> G. W. Musgrave (1946b, p.135)

Surface runoff and baseflow separation

This then created a problem for the infiltration theory of runoff because, as noted earlier, Cook points out there was no way of separating surface runoff and subsurface contributions to the hydrograph. But in order to derive the apparent infiltration characteristics from hydrographs and pluviographs it was necessary to do so. The concept of baseflow separation and recession analysis has continued to exercise hydrologists ever since (see Hall, 1968; Tallaksen, 1995; Beven, 1991; Arnold et al., 1995; Chapman, 1999; Eckhardt, 2005), right to the present day (Ladson et al., 2013; Lott and Stewart, 2016; He et al., 2016; Duncan, 2019). Some of these methods allowed for an increase in baseflow during an event, arguing that there would be some accretion to the water table during the time scale of the event (e.g. Horton, 1935; Hursh and Brater, 1941, as based on borehole observations at Coweeta; Hewlett and Hibbert, 1967; or the digital filters of Nathan and McMahon, 1990; Furey and Gupta, 2001; and Aksoy et al., 2009).

[9] It is commonly cited to Horton (1933) but does not appear there. It also does not appear in Horton's Monograph on Surface Runoff Phenomena of 1935.

Both Horton (1935) and Cook (1946) suggests the strategy of continuing the past groundwater depletion or recession curve as an indicator of baseflow, with all the flow above that curve being treated as if it was infiltration excess surface runoff but only for "*the special case when the subsurface flow is derived entirely from the zone below the permanent groundwater, table, and no groundwater accretion occurs, a satisfactory estimate of subsurface flow can be made simply by extending the groundwater depletion curve*." (Cook, op.cit. p728).

But simply continuing the recession curve results in a problem for the method in calculating the volume of surface runoff for an event, since the previous recession will always be below the recession of the current event. Thus, there was also a pragmatic need to allow for a "baseflow" contribution to rise to meet the falling recession limb of an event. Horton (1935) had earlier wanted to allow for the accretion of groundwater due to infiltration and specifies a method for deciding when the field moisture deficit of the soil has been satisfied, after which a line can be drawn to where the form of the recession matches the groundwater depletion curve. He notes that this might occur above or below the point of initial hydrograph rise (Figure 3). Hewlett and Hibbert (1967) suggested using a standard slope for this rise of 0.05 cfs/mi^2/hr (or 0.0567 ls^{-1}/km^2/hr), starting from beneath the hydrograph peak, but this was based only on discharge and borehole data from some small catchments at Coweeta. Somehow, it became a standard that was used around the world, regardless of soils, vegetation or geology. Others suggested that the end of surface runoff would be marked by a break between straight line segments on a semi-logarithmic plot of the recession, indicating a transition to a process with a slower time constant[10]. In essence Cook was correct, there is no satisfactory way of separating surface from subsurface flow in this way (see also the discussion in Beven, 1991[11]).

Deleted: peci

[10] Barnes (1939, 1944) recognised three such components, overland-flow, ground-water flow, and what he called secondary base-flow, and later storm-seepage or interflow; while Kunkle (1962) distinguished baseflow from the effects of bank storage.

[11] Beven (1991) includes a section headed "Choosing a baseflow separation method" that consists only of the one word "Don't".

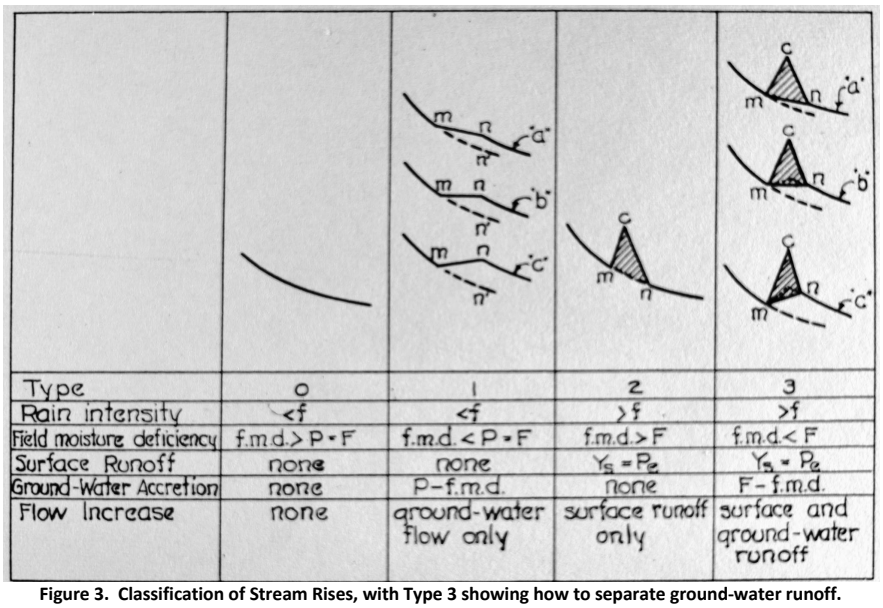

Figure 3. Classification of Stream Rises, with Type 3 showing how to separate ground-water runoff.

Derivation of infiltration indices from the hydrograph

Both Horton and Cook recognised that there was a difference between predicting surface runoff locally given information about rainfall and infiltration capacity curves for a soil and deriving apparent infiltration information from rainfalls and an estimate of "surface runoff". In the first case, the local variability of soils, vegetation and management practices could be taken into account (given the infiltration characteristics of each) on what Cook calls soil-cover *complexes*; the equivalent of modern-day hydrological response units. Such an approach can, in principle, also allow for the type of time variability of observed infiltration rates described by Horton (1940). However, I have found no real recognition at that time of the difference in scale between the point and plot scale at which observations are possible, and the soil-cover complex scale at which the calculations might be applied.

The second case is more challenging in that it is not possible to obtain more than an index of catchment-wide apparent infiltration. Cook gives two examples of such indices that can be obtained by matching the observed volume of surface runoff to the observed pattern of rainfall, both of which still appear in texts today. The first is based on assuming an average declining infiltration capacity to produce an average infiltration capacity (the f_{av} or W index) with a special case after significant wetting equivalent to a final constant infiltration capacity W_{min}. The second is assuming a constant infiltration capacity (the ø index). He demonstrates that for this latter index a dependence on rainfall intensity should be expected where there are multiple soil-cover complexes in a catchment "*because the higher the intensity the greater the proportion of the area producing runoff throughout the rain, not because infiltration capacity increases with intensity of rainfall.*" (Cook, op.cit. p.738). He therefore already

Deleted:

Deleted: The second case

Deleted: He

Deleted: rate

Deleted: rate

Deleted: rate

recognises the possibility of partial contributing areas of runoff production (but again, not how scale issues might affect the outcome).

Further problems arise when there is intermittent rainfall, or where rainfall intensity intermittently falls below the infiltration capacity of the soil and there might be the possibility of some recovery of infiltration capacities between bursts of rainfall. He goes into some detail to explain how different cases might be handled. He does not include, however, the suggestion of using *time condensation* (now more commonly known as the *time compression assumption*). This had been introduced 3 years earlier by Leroy Sherman (1943) and then modified by Heggie Nordahl Holtan[12] (1945). Holtan (1961) was also the first person to suggest an infiltration equation that was expressed directly in terms of cumulative infiltrated water, thereby implicitly incorporating a time compression assumption.

Infiltration equations

Application of the infiltration theory is easiest on a single soil-cover complex given rainfall and information about infiltration capacities of the soil. Quantitative estimation of runoff is easier if the infiltration capacities can be represented as a mathematical function (although in the 1930s and 1940s when the calculations were made by hand, it could actually be faster to read values off of a graph or from a table than to do the calculation, and many papers of the time give examples of hand-worked calculations, e.g. Sherman, 1936, 1943).

The Green and Ampt (1911) infiltration equation (Table 1), based on a piston-like wetting front approximation to Darcy's law had been available for some time. Horton (1939, 1940) developed his own form of equation[13]. As noted earlier, he argued that this represented surface controls rather than profile controls on the infiltration capacity. Cook mentions only the Horton equation in his exposition of the infiltration theory but there were other empirical infiltration equations suggested such as the power law form suggested independently by A. N. Kostiakov (1932) and Mortimer Reed Lewis (published in 1937 but according to Swarzendruber, 1993, proposed in 1926), the Soil Conservation Service (SCS) curve number method that first appeared in 1954 (SCS, 1954), and later that of Holtan (1961). The idea of solving the Darcy-Richards equation was picked up again in the 1950s, most notably by John Philip[14] (1954) and then in a series of papers for the infiltration problem (Philip, 1957). Given the nonlinearity of the governing equation this was a mathematical challenge for soil physicists and set off a variety of solutions for different types of diffusivity function and boundary conditions, that continued into the 21st Century (e.g. Ogden et al., 2015). A summary of some of these infiltration equations is given in Table 1. Comparison of the behaviours of different equations have been given by, for example, Wilson et al. (1982), Davidoff and Selim (1986), Mishra et al. (2003) and Chahinian et al. (2005).

Deleted: T

The SCS curve number method is of particular interest in terms of its common interpretation as an infiltration equation. Horton frequently clashed with the SCS and seems to have had a low opinion of their engineers (the SCS insisted on interpreting infiltration capacity as a

[12] (1909-2006), see http://www.history-of-hydrology.net/mediawiki/index.php?title=Holtan,_H._N.
[13] Note that Philip (1954) suggests that this equation was first suggested by Gardner and Widtsoe (1921), but Horton (1939, 1940) does not refer back to that earlier paper.
[14] (1927-1999), see http://www.history-of-hydrology.net/mediawiki/index.php?title=Philip,_John_R

volume rather than as a rate, for example[15]). This originally derives from the work of Mockus (1949) who plotted estimates of storm rainfall against the volume of surface runoff, as previously suggested by Sherman (1943). From this analysis Mockus suggests a relationship between them of the form

$$Q = P[1 - (10)^{-bP}]$$

with a multiple regression used to estimate the coefficient *b* based on data for 50 storms collected from catchments "*of field size or larger*" (p.41). The soil, crop, season, and antecedent precipitation indices used in the regression were derived by an analysis of data from nine USDA research stations. Nowhere does he specify how the amounts of surface runoff were derived. The resulting surface runoff was routed through a dimensionless unit hydrograph to derive hydrograph peaks (Mockus also mentions how a triangular unit hydrograph could be used to approximate the dimensionless unit hydrograph).

The methods were tested "*by estimating total runoff for storms on single- and mixed-cover watersheds",* by which he seems to mean the total volume of surface runoff. The results were better for large storms than small storms and for mixed-cover rather than single cover catchments. Better results were obtained by breaking long duration storms into parts. He notes that rainfall spatial variability and direction of movement might be important in getting better estimates.

The SCS curve number method took the data of Mockus and also a large number of infiltration capacity measurements on different soil types and land covers in the US, and postulated a proportionality between retention and runoff such that:

$$\frac{F}{S} = \frac{P - Q}{S} = \frac{Q}{P}$$

where *F* is the cumulative infiltration, *S* is the storage capacity of the soil, *Q* is the total runoff and *P* is the total precipitation for an event. According to an interview with Vic Mockus, he had fixed on this functional relationship after dinner one evening, having tried many others, because it best fit the data (Ponce, 1996). An initial abstraction loss, I_a, was also introduced which, on the basis of data from catchments of 10 acres or less, was made proportional to *S* as $I_a = \lambda S$. While 50% of these observations showed values of λ in the range 0.095 to 0.38, a value of 0.2 was chosen as being at the centre of the data (though Mockus allows that other values might be valid). Combining these equations an expression for *Q* can be derived as

$$Q = \frac{(P - 0.2S)^2}{P + 0.8S}$$

with only the one parameter *S*. For convenience in engineering applications, this was then scaled to a non-dimensional curve number *CN* such that (for *S* in units of inches)

[15] Beven (2004b) reports that in a letter to a Mr. Ramser of the SCS Horton wrote "In reading this discussion I am reminded of the adage that you can lead a horse and some other related animals to water but you can't make them think." [Horton papers Box 2: copy of letter dated June 7, 1943]

Deleted: ¶

$$S = \frac{1000}{CN} + 10$$

where *CN* has the range of 0 to 100 and is tabulated for different soil classes, land covers and antecedent conditions. The soils information was simplified to only 4 classes for simplicity of use by G. W. Musgrave (Ponce, 1996). It is clear from the literature associated with the curve number methodology that the SCS interpreted the output *Q* as a volume of surface runoff in excess of the infiltration capacity of the soil (Table 1). Thus, in Module 103 of the SCS-CN Training Manual it is stated that: "*Runoff is that part of the precipitation that makes is way towards stream channels, lakes or oceans as surface flow*" (p1). The Manual also provides definitions of interflow and baseflow as subsurface contributions to streams but suggests that interflow "*is not usually considered in SCS methods of estimating runoff*" (p.3).

There have since been many other interpretations of the SCS Curve Number relationships. Chen (1982) showed how the SCS curve number method could be related to the Holtan infiltration equation, which also allows for a maximum storage capacity, while Mishra and Singh (1999, 2002, 2003) showed how the Mockus relationship could be analytically related to the SCS Curve Number equation and also to the Horton infiltration equation (for the case where the long time infiltration capacity f_c can be assumed negligible). They refer to what is being estimated as *direct surface runoff*. It seems, given the relationship to infiltration equations they derive, they mean by this overland flow to the stream. Steenhuis et al. (1995) suggested that the method could also be interpreted as a saturation excess variable contributing area function, with later verification by Dahlke et al. (2006), while Yu (1998) suggested that it was equivalent to the partial area surface runoff that would be generated on a statistical distribution of soil infiltration characteristics. In all these cases, however, it retains the preconception of representing surface runoff as overland flow. It is important to note, however, that this may not have been the case for the original small catchment observations from which the method was derived (see also the results from Horton's runoff plat experiment reported in Beven, 2004a, where runoff rate was significantly higher than the observed rainfall intensity). More recently, Ogden et al. (2017) suggest it is really time to move beyond the curve number method suggesting that "*sixty-five years of use and multiple reinterpretations have not resulted in improved predictability using the method".*

Deleted:

Surface detention, channel storage and the unit-graph

Horton and others in the era of infiltration recognised that in both analysis and prediction it was not enough to simply calculate the excess of precipitation over the infiltration capacity of the soil. As Horton (1935) put it: "*A striking fact about surface runoff is the manner in which a jagged, irregular rain intensity graph is often transformed into a smoothly rounded runoff graph…. This is the result of regulation by surface detention and channel storage"* (Horton, 1935, p.1). By thinking in terms of a unit strip of hillslope (for which he credits a suggestion of LeRoy Sherman) Horton (1935) analyses the velocities expected for both laminar and turbulent sheet flow, with hydraulic radius assumed equal to the flow depth for a shallow flow, in terms of the Hagan power law equation:

$$q = k_H \delta_c{}^m S^n$$

Deleted: K

Deleted: M

Deleted: S

Deleted: N

where q is the flow per unit width, δ_c is the depth of flow averaged across the width of the slope segment, s is the slope of the surface and k_H, m, and n are parameters. Horton notes the theoretical values of m and n for laminar and turbulent flows, but also gives analyses of flume data provided by Lewis and Neal of the Idaho State Agricultural Experiment Station that suggest values of m of 0.85 and n of 0.74, suggesting mixed laminar and turbulent flow. He also uses this to derive a profile of overland flow depths under a steady distributed input rate equal to the rainfall rate – a constant infiltration capacity (essentially making the kinematic wave assumption).

He also recognised the effect of routing through channel storage, both in predicting hydrographs and in the analysis of observed hydrographs to derive infiltration parameters. He suggested a method of routing through a nonlinear (power law) storage based on the storage-discharge curve for the channels, but noting that "*in applying this method for correction for channel storage it is important that ground-water flow, if any exists, should be eliminated from the hydrograph in advance*" (Horton, 1935, p.41).

It might be that Horton felt compelled to provide a method of routing runoff because a few years earlier LeRoy Sherman (1932) had already proposed a more general method as an abstraction of the time-area approach that he called the unit-graph method (see the discussion of Beven, 2020). This was then developed into the unit hydrograph theory, with its many variants in terms of mathematical representation, methods of fitting, and parameters related to catchment characteristics. In its classical form the unit hydrograph is used to route estimates of the water contributing to the storm hydrograph after baseflow separation as appropriate (although modern transfer function methods can also be used to predict the complete hydrograph, e.g. Young, 2013). It was thus easy to combine the unit-hydrograph with the infiltration theory *as if* all that water was overland flow in excess of the infiltration capacity of the soil. This provided a convenient engineering procedure that is still in widespread use in many countries.

Surface Runoff, Direct Runoff and Stormflow

The infiltration theory essentially defines that proportion of the rainfall that will produce surface runoff and contribute to the storm hydrograph. But part of the problem here is what is actually meant by surface runoff. Even going back to the original definitions of Horton and Cook we have seen how surface runoff is what is measured in a stream hydrograph, but that might have reached the stream as either overland flow or subsurface stormflow. We have seen already how Robert Horton suggested that some of this contribution might be *concealed surface runoff* and how Howard Cook allowed that effective infiltration rates could not be inferred if there was a significant contribution to the hydrograph from subsurface flows.

It is also clear that the runoff data analysed by Mockus (1949) and that was used in evolving the SCS-CN model was not necessarily produced entirely by overland flow, despite the common interpretation of the SCS-CN function as an infiltration model. Yet, in setting out the definitions for his analysis, Mockus defines surface runoff as overland flow. He distinguishes between surface runoff, subsurface flow contributing to the hydrograph but which will quickly cease to contribute to streamflow, and groundwater flow which "*may first appear in the stream channels during or after the storm, and may continue for a relatively long time"* (p.2).

Deleted: *S*
Deleted: *K*
Deleted: *M*
Deleted: *N*
Deleted: *M*
Deleted: *N*
Deleted: data
Deleted: *M*
Deleted: *N*

He then defines the term *Direct Runoff* as the sum of surface runoff and subsurface flow *"combined in unknown proportions".* However, having set out these definitions he proceeds to outline methodologies for estimating surface runoff alone based on nomograms that allow for soil, crop, antecedent conditions, storm duration and seasonal effects. In his use of *Direct Runoff*, Mockus was following Franklin F. Snyder a decade earlier who, in a glossary of terms associated with his *Conception of Runoff-Phenomena* defines *surface-runoff* as:

> "*Usually defined as the runoff reaching the surface drainage-channels without penetrating the ground-surface. As actually used, surface-runoff usually includes considerable subsurface storm-flow and might be better termed direct runoff, since it consists of the discharge in excess of a base or ground-water flow which passes a gaging station within a rational period of time subsequent to the storm causing the rise".* (Snyder, 1939, p.736).

Note how this differs from the definition cited earlier in SCS Training Module 103. Later usage was also mixed, and there does not seem to have been a real history of development in the use of the different terms for runoff. To give just a few examples, Leach et al. (1933) use both storm-flow and surface-runoff; Langbein (1940) uses direct runoff, as do Hursh and Brater (1941) who specifically say that storm-runoff as overland-flow has not been observed on the study watershed at Coweeta and give examples of hydrographs dominated by channel precipitation. Hoover and Hursh (1943), however, revert to using storm-runoff. Marston (1952) equates storm runoff to overland flow but Reinhart (1964) includes subsurface stormflow in storm runoff, and in the study of Whipkey (1969) essentially all the storm runoff is subsurface stormflow. Hamon (1963) refers to direct runoff in relation to that predicted by the SCS curve number method, whereas others have continued to use storm runoff as equivalent to overland flow, especially in semi-arid catchments (e.g. Fogel and Duckstein, 1970).

If we turn to the latest issue of the WMO International Glossary of Hydrology (2012) we find *runoff* defined as that part of the precipitation which flows towards a river on the ground surface (*surface runoff*) or within the soil (*subsurface runoff* or *interflow*). *Direct runoff* (or direct flow or storm runoff) is defined simply as water that enters a watercourse without delay (and without any process interpretation). *Infiltration index*, however, is defined as an average rate of infiltration such that precipitation in excess of that value equals the volume of *storm runoff* (implying that the infiltration theory concept still persists, if only in an index form). In the Glossary for *Hillslope Hydrology,* Chorley (1978) also defines *direct runoff* with respect to time, adding that it comprises the sum of channel precipitation, overland flow and subsurface stormflow. His definition of *surface runoff* is limited to flow over the soil surface, and for *quickflow*, *storm runoff,* and *stormflow* he says "*see direct runoff"*.

There is thus some continuing ambiguity about the use of these terms, particularly surface runoff. This is in part a process issue because, however water flows into a stream by either surface or subsurface flow processes, once in the stream it is measured as a surface runoff (as was the case for the fields and small catchments in the data used by Mockus). The problem is that the word runoff still induces a perception of an overland flow, as in running off over the land surface. This is reinforced by the use of *surface* runoff even if the ambiguity recognised by Snyder, Cook and Mockus of the unknown mix of surface and subsurface

Formatted: Font: Italic, Underline

contributions to the hydrograph cannot be easily resolved. This mix, defined by them as *direct runoff* (and now sometimes referred to as *storm runoff* or *stormflow* or *quickflow*) is more commonly what is estimated by the use of hydrograph separation, but it should not then be interpreted as runoff in excess of the infiltration capacity of the soil. That is, perhaps, why the WMO Glossary refers to an infiltration ***index*** to match the volume of *storm runoff*, even if this perpetuates the perception of runoff as an overland flow. On the other hand, the convenient alliteration of *rainfall-runoff modelling* is generally used to indicate a mix of surface and subsurface processes (except in models that are still limited to predicting only overland flows).

Formatted: Underline

Given these ambiguities, it might be better to avoid the use of the terms runoff and surface runoff (and concealed surface runoff) altogether and instead refer to *stormflow* or *storm discharge* when no process interpretation is inferred, and refer explicitly to overland flow and subsurface stormflow when there is evidence for making a process interpretation[16]. There is also no reason why the general term *hydrological model* should not replace the ambiguity of rainfall-runoff model. This might (just perhaps) lead to a greater appreciation and greater thought about the perceptual model of hydrological processes relevant to particular catchments of interest (Beven, 2001; Beven and Chappell, 2020).

Persistence of the era of infiltration and perceptual model failures

When Cook was writing in 1946, he noted that the infiltration theory of surface runoff was still young and needed to be developed further, such that "*before it can be generally employed, many problems must be solved and large quantities of data published"* (op. cit. p.743). He notes in particular, that it would only be valid for cases where subsurface runoff could be neglected, and that infiltration indices derived from hydrograph data would only be satisfactory if there was only one soil-cover complex, otherwise, "*the physical significance is obscure"* (p.743). His final statement is to suggest that because of these issues all infiltration data should be accompanied by a statement of how they were derived, so that they would not be misused. It can be said, therefore, that Howard Cook had a rather realistic understanding of the limitations of the infiltration theory.

It seems that in the years following, however, the pragmatic utility of the methodology to provide estimates of the volume of storm discharge dominated any concerns about the validity of the assumptions. That volume could be combined with the time distribution of the Sherman (1932) unit-graph (and later representations of the unit hydrograph) to allow the prediction of hydrographs, and of hydrograph peaks for design applications. The methodology came to dominate hydrological practice, even well into the computer age, when there were many models essentially based on predicting and routing *effective* or *excess* rainfall based on infiltration equations (see, for example, Beven, 2012).

However, from the late 1960s onwards, the general applicability of the infiltration theory started to be questioned. Cappus (1960) and Moldenhauer et al. (1960) suggested that not all of a catchment would contribute surface runoff, while Betson (1964) concluded that the

[16] Note that Beven and Young (2013) also suggest some clarifications to the language used in hydrological modelling.

generally wetter conditions at the base of hillslopes would result in a relatively consistent partial contributing area (see also the consequent partial area model of Betson and Marius, 1969). Hewlett and Hibbert (1967) proposed that the contributing area would be dynamic, varying with antecedent conditions and storm rainfalls (see also Dickinson and Whitely, 1970).

However, particularly after the geochemical hydrograph separation of Pinder and Jones (1969) and the environmental isotope hydrograph separation of Sklash and Farvolden (1979), there was a more general realisation that subsurface processes were necessarily important in storm flow generation in many catchments because of the high proportion of pre-event water that appeared to be displaced in the event (something that was later called a double paradox by Kirchner, 2003). Thus, even if there was some overland flow, much of the water in the hydrograph had to be displaced from the soil or deeper layers (Sklash and Farvolden reported that at one site samples of overland flow were indicative of event water in one sampled storm and pre-event water in another). Thus new concepts of runoff generation were required. At Coweeta, where overland flow is rare except in the immediate riparian area (but runoff coefficients can be small), John Hewlett[17] had continued the work of Hursh in trying to understand the role of subsurface flow in hydrograph generation. The idea of runoff and return flow to dynamic saturated areas had appeared in the work of Dunne and Black (1970), a concept later claimed by Hewlett (1974). However, at around the same time, computer models such as the Huggins and Monke (1968) model; the KINEROS model that developed from Smith and Woolhiser (1971); the partial area Quasi-Physically-Based Rainfall-Runoff Model (QPBRRM) model of Engman and Rogowski (1974) also included in the study of Loague and Freeze (1985)[18]; and the CASC2D model of Downer et al. (2004); were all based on the infiltration theory (and there were many others). Of course, there are still catchments where the infiltration theory might indeed match the perceptual model of overland flow as the dominant process, but it still took time for the perceptual model of how catchments function to recognise the important contribution of subsurface water to stormflow in many catchments.

A really instructive case in this respect is the history of modelling the R5 catchment at Coshocton by Keith Loague and his colleagues. This is only a small catchment area (0.1 km^2) and started out as a study of effect of the variability of infiltration rates in space on runoff generation, making use of the extensive database of infiltration measurements collected by Sharma et al. (1980). It was included in the study of Loague and Freeze (1985) using the QPBRRM computer model. Loague and Gander (1990) added a further 247 infiltration measurements, and Loague and Kyriakidis (1997) used kriging interpolation to produce a fully distributed spatial pattern of infiltration characteristics. Using this information, however, produced less satisfactory hydrograph simulations than the original Loague and Freeze (1985) calibrated model. Various things were tried to improve the results, including allowing for temperature effects in the original infiltration measurements, and taking averages over stochastic fields of parameters consistent with the kriging estimates. It was suggested that

[17] (1922-2004), see http://www.history-of-hydrology.net/mediawiki/index.php?title=Hewlett,_J_D

[18] In Beven (1989) I criticised the paper of Keith Loague and Al Freeze (1985) because they had applied such the QPBRRM model to the Hubbard Brook catchment where surface runoff would be rarely observed. I suggested that was simply poor hydrological practice. Loague (1990) replied that they had made the choice of applying a model that was widely used in practice, and that such models might well be used in practice where the assumptions were not valid.

Deleted: runoff

Deleted: Keith

Deleted: replied

Deleted: pers.comm.

Deleted: ,

Deleted: these

there were still limitations of resolution in representing the surface runoff pathways and effects of run-on and reinfiltration. However, improvements in predictions of the peak and time to peak came with a change of model to the finite element based Integrated Hydrological Model (InHM) that included the effects of subsurface flow pathways (VanderKwaak and Loague, 2001; Loague et al., 2005). Following this change of perceptual model from a simple infiltration theory concept, R5 has continued to be used as a case study for the application of integrated models (Heppner et al., 2007; Mirus et al., 2011; Mirus and Loague, 2013).

Another case is reported in Beven (2002). I was a visiting scientist at the ARS laboratory in Fort Collins, Colorado working with Dave Woolhiser and Roger Smith and helped in an experiment to look at runoff generation on shallow restored soils over mine tailings near Steamboat Springs, Colorado in 1981. The perceptual model in designing the experiment was that the runoff generation would be produced by an infiltration excess mechanism. Thus many dual ring infiltrometer measurements were done, and replicate 25m by 5m sloping plots were watered using a sprinkler system supplied from a large impermeable container of rubberised fabric. Unfortunately, during the experiment the supply started to be limited by movement of the container as it emptied, but some overland flow was generated and collected. It was, however, localised on the surface, and rapidly fell to zero. Meanwhile, in the shallow trench that had been dug to take the collected overland flow from the measurement flume to a small channel, subsurface flow from beneath the collectors continued for some 90 minutes, and at the bankside of the channel there were two outflows from preferential flow pathways through otherwise unsaturated soil. It appeared as if there had been a form of percolation excess process taking place at the boundary between the mine tailings and topsoil, and that the resulting subsurface flow was somehow being channelled within the soil that had been replaced over the mine waste. The volumes of subsurface flow were not measured but were clearly much greater than the surface runoff collected. This was also an instructive case where the perceptual model based on the infiltration theory used in designing the experiment was clearly not correct and needed to be revised.

There is, therefore, no doubt that the infiltration theory concept led to many misconceptions or perceptual model failures of how the response of particular catchments was dominated by surface flow. There were, of course, many other catchments where subsurface contributions to the hydrograph have been studied in more detail and qualitative perceptual models developed, such as Hursh, Hewlett and others at Coweeta, North Carolina, as mentioned above, and Mosley (1982) and McDonnell (1990) at Maimai, New Zealand, with later additions by Brammer and McDonnell (2003) and McGlynn et al. (2010). These more complete perceptual models, however, tend to be complex and subject to limitations of knowledge of hydrological processes in the subsurface. In addition, there remains a need to simplify in applying quantitative predictive models in practice (Beven and Chappell, 2020). In that respect, infiltration theory still provides an approximate engineering solution that is simple to apply, as already recognised in the "*rough approximations*" of Cook (1946).

Deleted: and

Deleted:

This is perhaps the main explanation of the question posed at the beginning of this paper as to why the infiltration theory of runoff concept has persisted so widely in applications. It still underlies many current hydrological models in one form of another, including the SCS-CN or alternative Green-Ampt methods for estimating direct flow in the Soil Water Assessment Tool (SWAT). In this way, the era of infiltration theory continues, in part because of the

convenience of applying the SCS-CN method for practical applications without thinking too much about whether that is appropriate in any particular catchment. In fact, since we do not know too much about the processes in the catchments on which the analysis of Mockus (1949) that led to the SCS-CN method were based, that approach be more defensible (if only for the range of conditions for which the data were available) as a predictor of total direct runoff at the scale of interest than the use of point infiltration equations to predict purely overland flow (especially if heterogeneity of soil characteristics, the commensurability issues of scale of infiltration measurements against scale of applications, and run-on effects are neglected).

It does seem surprising, however, that more than 70 years after Howard Cook announced the era of infiltration, and 50 years after tracer information showed that hydrographs could be dominated by pre-event water, we should still be left with so much ambiguity about how to describe what is actually being observed and estimated in catchment hydrographs. Cook's observation that it is impossible to separate surface and subsurface contributions to the hydrograph when only records of the rates of flow are available still holds. Learning from tracer separations is not yet standard practice and does not provide unambiguous information about flow pathways. Yes, we understand that there are limitations on the knowability of what goes on in the subsurface but such ambiguity means that there have been no real attempts to define the limits of validity of the infiltration theory, and much confusion about its use. It seems that some of the old guard might still have reason to grumble.

Deleted: might

Deleted: so confused

Deleted: The resulting

Acknowledgements
My thanks to Nick Chappell for his useful comments on an earlier version of this paper.

References

Ahuja, L.R. and Tsuji, G.Y., Use of the Green-Ampt Equation with Variable Conductivity. *Soil Science Society of America Journal*, 40(4), 619-622, 1976.

Aksoy, H., Kurt, I. and Eris, E., Filtered smoothed minima baseflow separation method. *Journal of Hydrology*, *372*(1-4), 94-101, 2009.

Arnold, J.G., Allen, P.M., Muttiah, R. and Bernhardt, G., Automated base flow separation and recession analysis techniques. *Groundwater*, *33*(6), 1010-1018, 1995.

Barnes, B. S., The structure of discharge-recession curves, *Trans. Amer. Geophys. Un.* 20, 721-725, 1939

Barnes, B.S., Subsurface-Flow. *Transactions American Geophysical Union*, *25*(5), 746-746, 1944.

Betson, R. P., What is watershed runoff? *J. Geophys. Res.*, 69(8), 1541-1552, 1964.

Betson, R. P., and Marius, J. B., Source areas of storm runoff, *Water Resour. Res.* 5(3), 574-582, 1969.

Beven, K.J. Infiltration into a class of vertically non-uniform soils, *Hydrological Sciences J.*, 29(4), 425-434, 1984.

Beven, K.J. Changing ideas in hydrology: the case of physically based models. *J. Hydrology*, 105, 157-172, 1989.

Beven, K.J. Hydrograph Separation? Proc.BHS Third National Hydrology Symposium, Institute of Hydrology, Wallingford, 3.1-3.8, 1991.

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Beven, K.J., *Rainfall-Runoff Modelling – the Primer*, 1st edition, John Wiley and Sons: Chichester, 2001.

Beven, K.J., Runoff production in semi-arid areas, in M J Kirkby and L Bull (Eds.), *Dryland Rivers,* Wiley, Chichester, 57-105, 2002.

Beven, K.J., Surface runoff at the Horton Hydrologic Laboratory (or not?), *J. Hydrology,* 293, 219-234, 2004a.

Beven, K.J., Robert Horton's perceptual model of infiltration, *Hydrological Processes*, 18, 3447-3460, 2004b.

Beven, K.J., Robert Horton and abrupt rises of groundwater, *Hydrological Processes,* 18, 3687-3696, 2004c.

Beven, K.J., A history of the time of concentration concept, *Hydrology and Earth System Sciences*, https://doi.org/10.5194/hess-2019-588, 2020.

Beven, K.J. and Chappell, N. A., Perceptual perplexity and parameter parsimony, *WIRES Water*, in press, 2020.

Beven, K. J., and Young, P.C. A guide to good practice in modeling semantics for authors and referees, Water Resour.Res., 49, 5092–5098, doi:10.1002/wrcr.20393, 2013.

Brammer, D.D. and McDonnell, J.J., An evolving perceptual model of hillslope flow at the Maimai catchment. *Advances in hillslope processes*, 1, 35-60, 1996.

Cappus, P., Bassin versant experimental d'Alrance: études des lois de l'écoulement. Application au calcul et à la prévision des debits, *La Houille Blanche* A, 15, 493-520, 1960

Chahinian, N., Moussa, R., Andrieux, P. and Voltz, M., Comparison of infiltration models to simulate flood events at the field scale. *Journal of Hydrology*, *306*(1-4), 191-214, 2005.

Chapman, T., A comparison of algorithms for stream flow recession and baseflow separation. *Hydrological Processes*, *13*(5), 701-714, 1999.

Chen, C.-L.. An evaluation of the mathematics and physical significance of the Soil Conservation Service curve number procedure for estimating runoff volume. *Proc., Int. Symp. on Rainfall-Runoff Modeling*, Water Resources Publications, Littleton, Colo., 387-418, 1982.

Chorley, R. J., Glossary of Terms, in M. J. Kirkby (Ed.) *Hillslope Hydrology*, John Wiley and Sons: Chichester, 1978.

Collis-George, N., Infiltration equations for simple soil systems. *Water Resources Research*, *13*(2), 395-403, 1977.

Cook, H.L., The infiltration approach to the calculation of surface runoff. *Trans. Amer. Geophys. Union*, 27, 726–743, 1946.

Dahlke, H. E., Easton, Z. M., Walter, M., and Steenhuis, T.S., Field Test of the Variable Source Area Interpretation of the Curve Number Rainfall-Runoff Equation, *Journal of Irrigation and Drainage Engineering, ASCE*, 138(3), 235-244, 2012.

Davidoff, B. and Selim, H.M., Goodness of fit for eight water infiltration models. *Soil Science Society of America Journal*, *50*(3), 759-764, 1986.

Dickinson, W.T. and Whiteley, H. Watershed areas contributing to runoff. *Int. Assoc. Sci. Hydrol. Pubn*. 96, 12-26, 1970.

Deleted: :

Formatted: Font: Italic

Formatted: Font: Italic

Deleted: :

Deleted: pp.

Deleted: :

Downer, C.W., Ogden, F.L., Martin, W.D. and Harmon, R.S., Theory, development, and applicability of the surface water hydrologic model CASC2D. *Hydrological Processes*, 16(2), 255-275, 2002.

Duncan, H.P. Baseflow separation–A practical approach. *Journal of Hydrology*, 575, 308-313, 2019.

Dunne, T., and Black, R. D. Partial area contributions to storm runoff in a small New England watershed, *Water Resour. Res.,* 6(5), 1296–1311, 1970.

Eckhardt, K., How to construct recursive digital filters for baseflow separation. *Hydrological Processes*, 19(2), 507-515, 2005.

Engman, E. T. and Rogowski, A. S., A partial area model for storm flow synthesis, *Water Resour. Res.,* 10, 464-472, 1974.

Fogel, M.M. and Duckstein, L., Prediction of convective storm runoff in semi-arid regions. *Int. Assoc. Sci. Hydrol. Pubn*. 96, 465-478, 1970.

Furey, P.R. and Gupta, V.K., Tests of two physically based filters for base flow separation. *Water Resources Research*, *39*(10), W1297, 2003.

Gardner, W. and J. A. Widtsoe, The measurement of soil moisture, *Soil Science*, 11, 215-232, 1921.

Gardner, W. Infiltration.*Transactions American Geophysical Union* 27(1), 126-138, 1946.

Green, W. H. and Ampt, G. A., Studies in soil physics. I. The flow of air and water through soils, *J. Agric. Sci.*, 4(1), 1-24, 1911.

Hall, F. R., Baseflow recession – a review, *Water Resour. Res.*, 4(5), 973-983,1968.

Hamon, W. R. Direct Runoff using SCS function. Computation of direct runoff amounts from storm rainfall, *Int. Assoc. Sci. Hydrol. Pubn*., 63, 52-62, 1963

He, S., Li, S., Xie, R. and Lu, J., Baseflow separation based on a meteorology-corrected nonlinear reservoir algorithm in a typical rainy agricultural watershed. *Journal of Hydrology*, 535, 418-428, 2016.

Heppner, C.S., Loague, K. and VanderKwaak, J.E. Long-term InHM simulations of hydrologic response and sediment transport for the R-5 catchment. *Earth Surface Processes and Landforms*, *32*(9), 1273-1292, 2007.

Hewlett, J. D., Comments on letters relating to the 'Role of subsurface flow in generating surface runoff. 2. Upstream source areas' by R. Allen Freeze, *Water Resour. Res.,* 10, 605-607, 1974

Hewlett, J. D. and Hibbert, A. R., Factors affecting the response of small watersheds to precipitation in humid areas, in: W.E. Sopper and H.W. Lull (Eds.), *International Symposium on Forest Hydrology*, Pergamon: New York, 275-290, 1967.

Holtan, H.N.,Time-condensation in hydrograph-analysis. *Eos, Transactions American Geophysical Union*, 26(3), 407-413, 1945.

Holtan, H. N., A concept for infiltration estimates in watershed engineering. USDA, Agricultural Research Service Publication 41-51, USDA, Washington, DC, 1961.

Hoover, M.D. and Hursh, C.R., Influence of topography and soil-depth on runoff from forest land. *Eos, Trans. Amer. Geophys. Un.*, 24(2), 693-698, 1943.

Horton, R. E., The role of infiltration in the hydrologic cycle, *Trans. Amer. Geophys. Un*., 14, 446-460, 1933.

Deleted: :

Deleted: :

Formatted: Font: Not Italic

Deleted: *s: An International Journal*,

Deleted: :

Formatted: Font: Not Italic

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Formatted: Font: Not Italic

Deleted: ., 2007

Deleted: pp.

Deleted: :

Formatted: Font: Not Italic

Deleted: :

Deleted: *Transactions American Geophysical Union*

Formatted: Font: Not Italic

Deleted: :

Deleted: :

Horton, R. E., Surface Runoff Phenomena. Part I – Analysis of the hydrograph, *Publication 101*, Horton Hydrological Laboratory: Voorheesville, NY, 1935.

Horton R.E., Analysis of runoff-plat experiments with varying infiltration capacity. *Trans. Amer. Geophys. Un.*, 20, 693–711, 1939.

Horton, R. E., An approach towards a physical interpretation of infiltration rate, *Soil Sci. Soc. Amer. Proc.*, 5, 399-417, 1940.

Horton, R. E., Remarks on hydrologic terminology, *Trans. Amer. Geophys. Un.*, 23, 479-482, 1942.

Houk, I. E., Rainfall and runoff in the Miami Valley. State of Ohio, Miami Conservancy District, Tech. Rept., 8p, 1921.

Hoyt, W. G. and W. B. Langbein, Some general observations of physiographic and climatic influences on floods, *Trans. Amer. Geophys. Un.*, 20(2), 166-174, 1939.

Huggins, L. F. and Monke, E. J., A mathematical model for simulating the hydrologic response of a watershed, *Water Resour. Res.*, 4, 529-539, 1968.

Hursh, C. R., Storm water and adsorption, *Trans. Amer. Geophys. Un.*, 17, 301-302, 1936

Hursh C. R., Subsurface-flow. *Trans. Amer. Geophys. Un.*, 25, 743–746, 1944.

Hursh, C. R. and Brater, E. F., Separating storm-hydrographs from small drainage-areas into surface- and subsurface-flow, *Trans. Amer. Geophys. Un.*, 22, 863-870, 1941

Kirchner, J.W., A double paradox in catchment hydrology and geochemistry. *Hydrological Processes*, 17(4), 871-874, 2003.

Kostiakov, A. N., On the dynamics of the coefficient of water-percolation in soils and on the necessity of studying it from a dynamic point of view for purposes of amelioration. *Trans. 6th Comm. Intl. Soil Science Society* Part A, 17-21, 1932.

Kunkle, G. R., The baseflow-duration curve: a technique for the study of groundwater discharge from a drainage basin, *J. Geophys. Res.* 67(4), 1543-1554, 1962.

Ladson, A.R., Brown, R., Neal, B. and Nathan, R., A standard approach to baseflow separation using the Lyne and Hollick filter. *Australasian Journal of Water Resources*, 17(1), 25-34, 2013.

Langbein, W.B., Channel-storage and unit-hydrograph studies. *Trans. Amer. Geophys. Un.*, 21(2), 620-627, 1940.

Leach, H.R., H.L. Cook and R.E. Horton, Storm-flow prediction, *Trans. American Geophysical Union,* 14(1), 435-446, 1933

Lewis, M. R. The rate of infiltration of water in irrigation practice. *Trans., American Geophysical Union,* 18, 361-368, 1937.

Loague, K. Changing ideas in hydrology—The case of physically based models—Comment. *Journal of Hydrology*, 120(1-4), 405-407, 1990.

Loague, K. and Freeze, R. A., A comparison of rainfall-runoff modelling techniques on small upland catchments, *Water Resour. Res.*, 21, 229-248, 1985.

Loague, K. and Gander, G. A., R-5 revisited: spatial variability of infiltration on a small rangeland watershed, *Water Respour. Res.*, 26, 957-971, 1990.

Deleted: *Transactions, American Geophysical Union*

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: *Transactions, American Geophysical Union*

Deleted: :

Deleted: :

Formatted: Font: Not Italic

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Formatted: Font: Not Italic

Deleted: *Transactions American Geophysical Union*

Deleted: :

Deleted: ,

Deleted:

Deleted: :

Formatted: Font: (Default) +Body (Calibri)

Formatted: Normal

Formatted: Font: (Default) +Body (Calibri)

Formatted: Font: (Default) +Body (Calibri), Not Italic

Formatted: Font: (Default) +Body (Calibri)

Formatted: Font: (Default) +Body (Calibri)

Formatted: Font: 12 pt

Deleted: :

Deleted: :

Loague, K. and Kyriakidis, P. C., Spatial and temporal variability in the R-5 infiltration data set: déjà vu and rainfall-runoff simulations, *Water Resour. Res.*, 33, 2883-2896, 1997.

Loague, K., Heppner, C.S., Abrams, R.H., Carr, A.E., VanderKwaak, J.E. and Ebel, B.A., Further testing of the Integrated Hydrology Model (InHM): Event-based simulations for a small rangeland catchment located near Chickasha, Oklahoma. *Hydrological Processes*, 19(7), 1373-1398, 2005.

Lott, D.A. and Stewart, M.T., Base flow separation: A comparison of analytical and mass balance methods. *Journal of Hydrology*, 535, 525-533, 2016.

Marston, R. B., Ground cover requirements for summer storm runoff control on aspen sites in Northern Utah, J. Forestry 50(4), 303-307, 1952

McDonnell, J.J., A rationale for old water discharge through macropores in a steep, humid catchment. *Water Resources Research*, *26*(11), 2821-2832, 1990.

McGlynn, B.L., McDonneli, J.J. and Brammer, D.D., A review of the evolving perceptual model of hillslope flowpaths at the Maimai catchments, New Zealand. *Journal of Hydrology*, 257(1-4), 1-26. 2002.

Mein, R.G. and Larson, C.L., Modeling infiltration during a steady rain. *Water resources research*, 9(2), 384-394, 1973.

Mezencev,V.S., Theory of the formation of the surfacerunoff on the slope. Meteorol. Gidrol., 3, 33—40, 1948 (in Russian)

Minshall, N.E., Predicting storm runoff on small experimental watersheds*, J. Hydraul. Div. ASCE*, 86(8), 17-38, 1960.

Mirus, B. B. and Loague, K., How runoff begins (and ends): Characterizing hydrologic response at the catchments scale, *Water Resources Research*, 49(5), 2987-3006, 2013

Mirus, B. B., Ebel, B. A., Heppner, C. S and Loague, K., Assessing the detail needed to capture rainfall-runoff dynamics with physics-based hydrologic response simulation, *Water Resources Research,* 47(3), W00H10, doi: 10.1029/2010WR009906, 2011.

Mishra, S. K. and Singh, V. P., Another look at SCS-CN method, *J. Hydrologic Engineering, ASCE*, 4, 257-264, 1999.

Mishra, S.K. and Singh, V.P., SCS-CN method. Part I: derivation of SCS-CN-based models. *Acta Geophysica Polonica* 50(3), 457-477, 2002.

Mishra, S.K. and Singh, V.P., SCS-CN method. Part II: analytical treatment, *Acta Geophysica Polonica,* 51(1), 108-123, 2003

Mishra, S.K., Tyagi, J.V. and Singh, V.P., Comparison of infiltration models. *Hydrological Processes*, 17(13), 2629-2652, 2003.

Mockus, V., Estimation of total and peak rates of surface runoff for individual storms. Exhibit A, Appendix B, Interim Survey Report, Grand (Neosho) River Watershed, US Department of Agriculture: Washington D.D., 1949.

Moldenhauer, W.C., W.C. Barrows, and D. Swartzendruber, Influence of rainstorm characteristics on infiltration measure- ments, *Trans. Int. Cong. Soil Sci*., 7, 426-432, 1960.

Mosley, M.P., Subsurface flow velocities through selected forest soils, South Island, New Zealand. *Journal of Hydrology* 55, 65-92, 1982.

Deleted: :

Formatted: Font: Not Italic

Deleted: :

Formatted: Font: Not Italic

Deleted: :

Deleted: :

Deleted: :

Formatted: Font: Not Italic

Formatted: Font: Not Italic

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: 2011,

Deleted: :

Deleted: :

Deleted: :

Formatted: Font: Not Italic

Deleted: :

Deleted: :

Muntz, M. A., Fauré, M. L., Lain, M. E., Etudes sur la perméabilité des terres faites en vue de l'arrosage, Min. de l'Agr., Dir. Gén. Eaux et Forêts, Ann. Forêts-Hydraulique, 36, 45-96, 1905.

Musgrave, G. W., Report of the Committee on Infiltration 1956-46, *Trans. Amer. Geophys. Un.*, 27(5), 726, 1946a.

Musgrave, G. W., Comment on Infiltration by Willard Gardner, *Transactions American Geophysical Union* 27(1), 135, 1946b.

Nathan, R. J. and MacMahon, A. A. Evaluation of automated techniques for base flow and recession analyses. *Water Resources Research*, 26(7), 1465-1473, 1990.

Ogden, F.L., W. Lai, R.C. Steinke, J. Zhu, C.A. Talbot and J.L. Wilson. A new general 1-D vadose zone solution method. *Water Resources Research*, 52(6), 4282-4300, doi:10.1002/2015WR017126, 2015.

Ogden, F.L., Hawkins, R.P., Walter, M.T. and Goodrich, D.C., Comment on "Beyond the SCS-CN method: A theoretical framework for spatially lumped rainfall-runoff response" by MS Bartlett et al. *Water Resources Research*, 53(7), 6345-6350, 2017.

Philip, J.R., An infiltration equation with physical significance. *Soil Science*, 77(2), 153-158, 1954.

Philip, J. R., The theory of infiltration: 1. The infiltration equation and its solution, *Soil Science*, 83, 345-357, 1957

Pinder, G.F. and Jones, J.F., Determination of the ground-water component of peak discharge from the chemistry of total runoff. *Water Resources Research*, *5*(2), 438-445, 1969.

Ponce VM. Notes of my conversation with Vic Mockus, 1996. Available at http://mockus.sdsu.edu/ (last accessed 8 June 2020).

Reinhart, K. G., Effect of commercial clearcutting in West Virginia on Overland Flow and Storm Runoff, J. Forestry 62(3), 167-171, 1964.

SCS, Hydrology guide for use in watershed planning, Soil Conservation Service, USDA, Washington, D.C., 1954.

SCS, Engineering Hydrology Training Series, Module 103: Runoff Concepts, US Department of Agriculture, Washington DC, 1989.

Sharma, M.L., Gander, G.A. and Hunt, C.G., Spatial variability of infiltration in a watershed. *Journal of Hydrology*, *45*(1-2), 101-122, 1980.

Sherman, L. K., Streamflow from rainfall by unit-graph method, *Engineering News Record,* 108, 501-505, 1932.

Sherman, L.K., Appendix C—The Horton method for determination of infiltration-rates. *Transactions American Geophysical Union*, 17(2), 312-314, 1936.

Sherman, L. K., Comparison of *f* curves derived by the methods of Sharp and Holtan and of Sherman and Mayer, *Transactions American Geophysical Union*, 24, 465-467, 1943.

Singh, V.P. and Yu, F.X., Derivation of infiltration equation using systems approach. *Journal of Irrigation and Drainage Engineering*, 116(6), 837-858, 1990.

Sklash, M.G., Farvolden, R.N., The role of groundwater in storm runoff. *J. Hydrol.* 43, 45-65, 1979.

Smith RE. The infiltration envelope: results from a theoretical infiltrometer. *J. Hydrol*, 17, 1–21, 1972.

Deleted: :

Deleted: Trans. A,er. Geophys. Un

Deleted: :

Deleted: :

Formatted: Font: (Default) +Body (Calibri), 10 pt

Formatted: Font: (Default) +Body (Calibri), 10 pt, Italic

Formatted: Font: Italic

Formatted: Font: (Default) +Body (Calibri), 10 pt, Italic

Formatted: Font: Italic

Formatted: Font: (Default) +Body (Calibri), 10 pt

Formatted: Font: (Default) +Body (Calibri), 10 pt

Formatted: Font: (Default) +Body (Calibri)

Formatted: Font: (Default) +Body (Calibri), 10 pt

Formatted: Font: Not Italic

Deleted: :

Formatted: Font: Not Italic

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Formatted: Font: Not Italic

Deleted: :

Deleted: :

Formatted: Font: Not Italic

Deleted: :

Deleted: *Journal of*

Deleted: *ogy*

Deleted: :

Smith, R. E., and Parlange, J.-Y., A parameter-efficient hydrologic infiltration model, *Water Resour. Res.*, 14(3), 533-538, 1978.

Smith, R.E. and Woolhiser, D.A., Overland flow on an infiltrating surface. *Water Resour. Res.*, 7(4), 899-913, 1971.

Snyder, F. F., A conception of runoff-phenomena, *Trans. Amer. Geophys. Un.*, 20, 725-736, 1939.

Steenhuis, T.S., Winchell, M., Rossing, J., Zollweg, J. A. and Walter, M. F., SCS runoff equation revisited for variable source runoff areas, *J. Irrig. Drain. Div. ASCE,* 121, 234-238, 1995.

Swartzendruber, D., Revised attribution of the power form infiltration equation. *Water Resources Research*, 29(7), 2455-2456, 1993.

Tallaksen, L.M., A review of baseflow recession analysis. *Journal of Hydrology*, 165(1-4), 349-370, 1995.

Talsma, T. and Parlange, J.-Y., One-dimensional vertical infiltrations, *Aus. J. Soil Res.*, 10, 143-150, 1972.

VanderKwaak, J.E. and Loague, K., Hydrologic-response simulations for the R-5 catchment with a comprehensive physics-based model. *Water Resources Research*, *37*(4), 999-1013, 2001.

Walter, M.T., Mehta, V.K., Marrone, A.M., Boll, J., Gerard-Marchant, P., Steenhuis, T., Walter, M.F., Simple estimation of prevalence of Hortonian flow in New York City watersheds. *J. Hydrol. Eng., ASCE* 8(4), 214–218, 2003.

Whipkey, R. Z., Storm runoff from forested catchments by subsurface routes, *Int. Assoc. Sci. Hydrol. Pubn*. 85, 773-779, 1969.

Wilson B.N., Slack D.C., Young R.A. A comparison of three infiltration models. *Trans. Amer, Soc. Aric. Engrs*. 25, 349–356, 1982.

WMO, *International Glossary of Hydrology*, Report WMO-No.385, WMO: Geneva, 2012.

Young, P.C., Hypothetico-inductive data-based mechanistic modeling of hydrological systems. *Water Resources Research*, *49*(2), 915-935, 2013.

Yu, B., Theoretical justification of SCS method for runoff estimation, *J. Irrig. Drain. Div., ASCE,* 124, 306-309, 1998.

Deleted: :

Deleted: *ces*

Deleted: *earch*

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Formatted: Font: Not Italic

Deleted: *h*

Formatted: Font: Not Italic

Deleted: :

Deleted: :

Deleted: *r*

Deleted: *r*

Deleted: :

Deleted: *gng*

Deleted: :

Deleted: :

Deleted: :

Deleted: :

Table 1. Selected 20th Century infiltration equations with *f(t)* as infiltration capacity, *F(t)* as cumulative infiltration, and K_s as saturated hydraulic conductivity (other symbols defined under Comments)

Source	Equation	Comments
Green and Ampt (1911)	$f(t) = K_s\left(\frac{\lvert\psi_f\rvert}{z_f} + 1\right)$	Based on Darcy's law with piston-like wetting front from initial moisture content to saturation. ψ_f is capillary pressure change across wetting front, z_f is current depth to wetting front
Kostiakov (1932), Lewis (1937)	$f(t) = Kt^N$	Empirical, with *K* and *N* as parameters
Horton (1939, 1940)	$f(t) = (f_o - f_c)e^{-kt} + f_c$	Empirical, with *k* as a time scale parameter. Allows for an initial f_o and final f_c infiltration capacities. Argues that it represents rate equation for extinction phenomena at the soil surface
Mezencev (1948) and later Smith (1972)	$f(t) = Kt^N + f_c$	Extension of the Kostikov-Lewis equation to include a final infiltration capacity
SCS-CN (1954)	$F = P - \frac{(P - 0.2S_{CN})^2}{P + 0.8S}$ $S_{CN} = \frac{1000}{CN} - 10$	Origins lie in estimation of direct flow rather than overland flow, but often interpreted as an infiltration equation. *P* is event precipitation, S_{CN} is storage capacity of the soil associated with the Curve Number, *CN*
Philip (1957)	$f(t) = \frac{St^{-1/2}}{2} + A$	First two terms of series solution to Darcy-Richards equation assuming constant diffusivity. *S* is the *sorptivity* of the soil, *A* is a parameter likely to be somewhat smaller than the saturated conductivity of the soil.
Holtan (1961)	$f(t) = f_o + \alpha(S_o - F)e^{\eta}$	Empirical with α and η as parameters. Makes infiltration capacity dependent on initial value f_o, cumulative volume already infiltrated F and initial storage capacity of the soil S_o which also provides an upper limit for infiltration
Talsma and Parlange (1972)	$f(t) = St^{1/2} + \frac{K_s t}{3} + \frac{{K_s}^2 t^{3/2}}{9S}$	Assumes diffusivity is proportional to rate of change of conductivity with θ. K_s is saturated hydraulic conductivity and *S* sorptivity
Morel-Seytous and Khanji (1974)	$f(t) = \frac{K_s}{B}\left[\frac{h_o(\theta_s - \theta_i) + C_d}{z_f(\theta_s - \theta_i)} + 1\right]$	Extension of the Green-Ampt equation with C_d as the capillary drive, h_o as depth of

Deleted: *n*

Deleted: *S*

Deleted: is the curve number

Deleted: *r*

Deleted: *α*

Deleted: *n*

Formatted: Font: Not Italic

Formatted: Font: Not Italic

Deleted: and

		surface ponding and B as a scaling parameter allowing for lack of complete wetting.
Ahuja and Tsuji (1976)	$F(t) = K_s t + \frac{K_s - a}{b}[e^{-bt} - 1] + z_f(\theta_s - \theta_i)\ln[1 + F(t)/z_f(\theta_s - \theta_i)]$	Extension of the Green-Ampt equation to have an exponential time variable hydraulic conductivity function, with parameters a, and b, based on comparison with the Philip equation. Claim better fit to observations.
Collis-George (1977)	$F(t) = S(t_c)^{1/2}\left(\tanh\frac{t}{t_c}\right)^{1/2} + f_c t$	Empirical but argues that it provides a better fit to data than Green-Ampt, Horton or Philip equations. *S* is the sorptivity, t_c a time scale parameter, and f_c a final infiltration capacity
Smith and Parlange (1978)	$f(t) = K_s\left[\frac{expF(t)/C_D}{expF(t)/C_D - 1}\right]$	Solution of Darcy-Richards assuming an exponential diffusivity function. Useful when rainfall rates vary, as *f(t)* is a function of cumulative inlftration *F(t).*
Beven (1984)	$\frac{dF(t)}{dt} = \frac{K_o\beta[\lvert\psi_f\rvert + F/(\theta_s - \theta_i)]}{1 - e^{-\beta F/(\theta_s - \theta_i)}}$	Extension of Green-Ampt for case of exponential decline of saturated conductivity with depth as $K_s(z) = K_o e^{-\beta z}$. Has an implicit solution for *F*
Singh and Yu (1990)	$f(t) = f_c + \frac{a[S_o - F(t)]^M}{[F(t)]^N}$	Made infiltration dependent on initial storage available and powers of cumulative infiltration and remaining storage. M, N and a, are parameters

Formatted: Font: Not Italic

Deleted: *A*

Deleted: *B*

Deleted: and

Deleted: α

Deleted: α

Deleted: K

Deleted: α

Deleted: a

Deleted: M

Deleted: N

Deleted: M

Deleted: N

Deleted: a