Minimizing the impact of vacating instream storage of a multi-reservoir system: a tradeoff study of water supply and empty flushing

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Abstract

Reservoir operator does not favor storage above a certain level in situations such as the pre-release operation prior to a flood, scheduled engineering constructions or mechanical excavations of sediments in the impoundments, drawdown and empty flushing, etc. This paper selects the last of which as the case study, and a method is presented to promote the feasibility of emptying reservoir storage. The impact of emptying reservoir on water supply is minimized through appropriate joint operation in a multi-reservoir system, where drawdown and empty flushing is carried out in a primary reservoir and the other reservoirs provides backup water for supply. This method prioritizes allocating the storage in the primary reservoir for water supply during specific periods prior to its empty. If the storage of every reservoir achieves its predefined conditions, drawdown of the primary reservoir is activated and followed by empty flushing. Previously preserved storage in the other reservoirs ensures adequate water supply during the periods of emptying the primary reservoir. Flushing of the primary reservoir is continued until either the accumulative released water exceeds the specified volume, storage in the backup reservoirs drops below the pre-defined threshold, or the inflow to the primary reservoir recedes from the flood peak to be below the releasing capacity of outlets. This behavior is simulated and linked with a nonlinear optimization algorithm to calibrate the

optimal parameters defining the activation and termination of empty flushing. The optimized strategy limits the incremental water shortage within the acceptable threshold and maximizes the expected benefits of emptying reservoir.

Keywords*:* water supply, joint operation of multiple reservoirs, drawdown of reservoir storage, empty flushing, reservoir desilting.

1. Introduction

Reservoirs intercept watercourses to store excessive water and regulate natural flow patterns into expected releases for different purposes. In contrast to conserve water, there are also circumstances in which storages above certain levels in reservoirs are not favored. These situations include when an imminent flood is anticipated, ~~an extraordinary water quality is measured,~~ engineering constructions or mechanical excavations of sediments within the impoundments are scheduled, and empty flushing operations. While the last of which is focused in this paper, the concept of minimizing the impact of vacating storages from reservoirs on the original purposes of water usage through careful management is general to all situations.

Empty flushing is the most effective method for removing deposited sediments from reservoirs (Fan and Morris, 1992; Morris and Fan, 1998; Shen, 1999). This process requires complete drawdown of reservoir storage to allow "inflows to pass through at riverine depths" (Atkinson, 1996). The drawdown of storage is usually carried out by releasing water through bottom outlets~~, such as sluiceways~~. During this process, the accelerated flow near the inlet may partially reactivate and scour out the depositions to generate a flushing cone in the vicinity of the inlet. By completely emptying the reservoir and maintaining the riverine flow condition, retrogressive erosion may be induced from the rim of the flushing cone extending to the upstream to create a flushing channel. The formation of the flushing channel usually leads to hyper sediment concentration of the bottom release and thus effectively recovers partial deposited capacity of the reservoir. This operation has been used to pursue sustainable utilization by many reservoirs worldwide (Atkinson, 1996; White, 2001; Chaudhry and Habib-ur-rehman, 2012), some examples of which are presented in Table 3 in the Appendix 1.

Because draining the storage of a reservoir counteracts its water supply function, empty flushing is generally limited to reservoirs that operate solely for hydropower generation, flood mitigation, or irrigation. These purposes usually do not require reservoir storage during certain

periods of the year, during which empty flushing can be implemented without impairing the original design function of the reservoir. However, for reservoirs with municipal or industrial end-users that rely on sufficient storage for steady water supply, the implementation of empty flushing is relatively rare.

The conflict between water supply and empty flushing has been addressed by Chang et al. (2003) and Khan and Tingsanchali (2009). Chang et al. (2003) developed the operating rule curves and empty flushing schedule for the Dapu Reservoir in central Taiwan. A genetic algorithm was used to optimize the rule curves by minimizing the shortage index for irrigation demand while empty flushing is implemented during prescribed periods. Khan and Tingsanchali (2009) applied a similar approach to the Tarbela Reservoir in Pakistan, the operating rule curves of which is optimized by maximizing the net benefit from irrigational water supply, hydropower generation, sedimentation evacuation and flood mitigation. However, these previous studies dealt only with single-reservoir. If there are additional reservoirs in the system that can act as backup water sources, it may be possible to elevate the feasibility of empty flushing by reducing its impact on water supply through appropriate joint operation. The ideal strategy may require utilizing the reservoir with the most excessive sediment deposition, referred to as the primary reservoir throughout the remainder of this paper, to supply demands while preserving the storage in the other reservoirs before empty flushing. This will lead to a lower water surface level (WSL) in the primary reservoir and a higher WSL in the others. Empty flushing in the primary reservoir can then be activated once favorable conditions are achieved, such as adequate storage distribution among reservoirs to ensure both high sediment flushing efficiency and steady backup water supply.

This study focused on a water resources system that contains two reservoirs, among which one primary reservoir is on-stream and requires empty flushing operation. The other with backup storage is off-stream and supplies demands jointly with the primary one. This specific

schematic protects the backup storage from the turbid release by the reservoir undergoing empty flushing thus ensuring uninterrupted water supply and could be the prototype for more complex system. The goal is to develop the optimal strategy, which maximizes the efficiency of empty flushing without significantly hindering water supply. In the following section, the case study system is introduced. Key factors influencing the efficiency of sediment flushing as well as the stability of water supply are then discussed, followed by developing the methodology to derive the strategy for joint water supply and empty flushing in the case study system. The results validate the efficacy of the proposed optimal strategy.

2 Case study area

The joint operating system of the serial Tsengwen and Wushanto Reservoirs is in southern Taiwan. Figures 1 and 2 show the location of these reservoirs and the network of the water resources system respectively. The Tsengwen Reservoir is in the upper section of the Tsengwen River, with a watershed area of 481.6 km^2. The original effective capacity with the WSL as the normal pool level El. 227 m was 631.2 million m^3 when the reservoir was completed in 1973. Operated by the Southern Regional Water Resources Office of Water Resources Agency (SRWRO), its purposes include agricultural and water supply, flood control, and hydropower generation. Located 6 km downstream of the Tsengwen Reservoir, the East Weir diverts the releases from the Tsengwen Reservoir to the Wushanto Reservoir through Wushan Hill Tunnel of 3.3 Km at a conveyance capacity of 56 m^3/s.

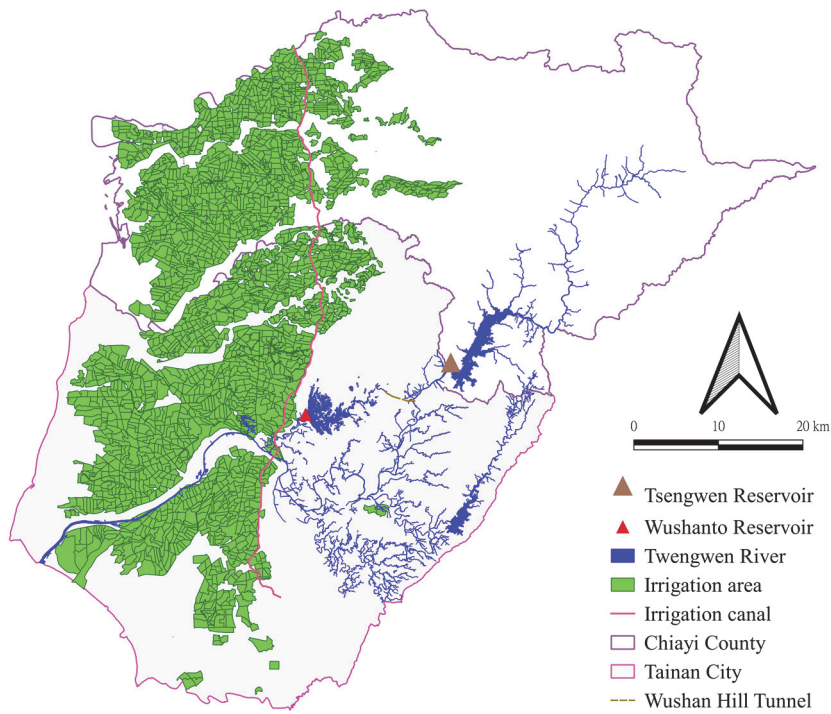
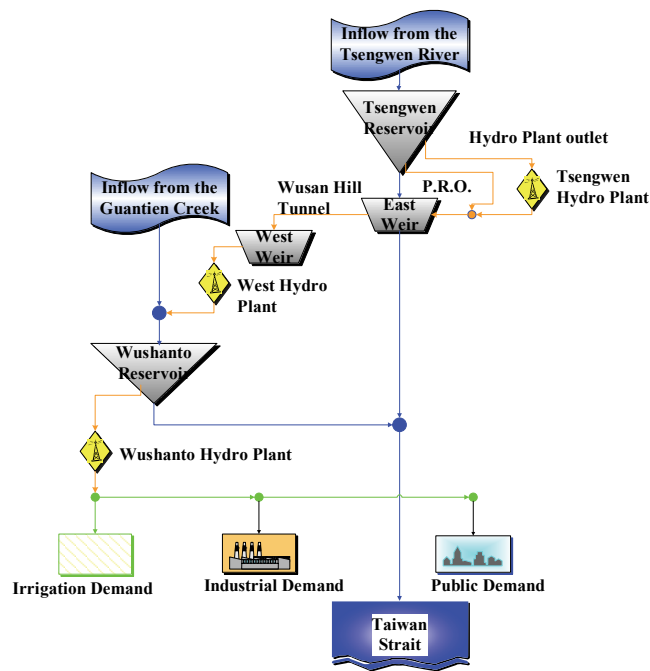



Fig. 1 The map of Tsengwen and Wushanto Reservoirs

5   **Fig. 2 Network of the joint operating system of Tsengwen and Wushanto Reservoirs**

The Wushanto Reservoir is situated to the southwest of the Tsengwen Reservoir in the

upper section of Guantien Creek, a tributary of Tsengwen River. The watershed area of the Wushanto Reservoir is only 60 km^2, which renders it conceptually off-stream. In 2015, its effective capacity was measured at 78.28 million m^3. The Chianan Irrigation Association manages the Wushanto Reservoir in coordination with the release from Tsengwen Reservoir, supplying irrigation water to over 70 thousand hectares of farmland in the Chianan Plain and providing the public and industrial water to the Tainan City and Chiayi County.

2.1 The rules of joint operation for water supply

Fig. 3 presents the joint operating rule curves for the Tsengwen and Wushanto Reservoirs. The rules stipulate that when the total storage of the two reservoirs is below the critical limit, only 80% of the public demand and 50% of the agricultural and industrial demands will be satisfied. When the total storage is between the lower and critical limits, the public demand should be fulfilled and 75% of the agricultural and industrial demands need to be satisfied. When the total storage is between the upper and lower limits, all demands should be fulfilled. In the event that the storage in the Tsengwen Reservoir exceeds the upper limit, extra water can provide excess supply or full loaded hydropower generation until the storage returns to the upper limit.

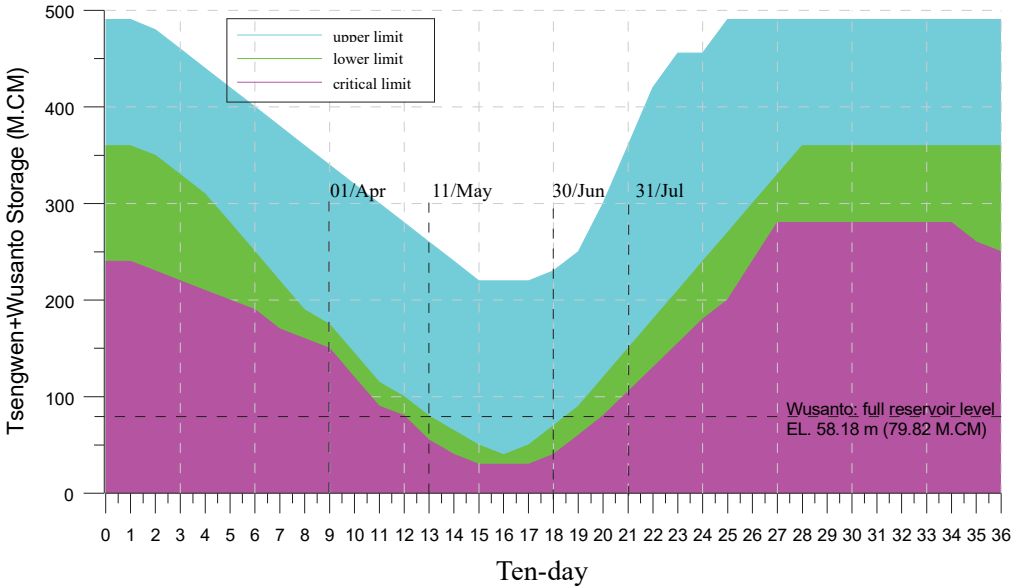



Fig. 3 Joint operating rule curves of the Tsengwen and Wushanto Reservoirs

In addition to the joint rule curves, the operators also prefer certain storage distribution among reservoirs to enhance the overall operating efficiency. The preference is represented by the form of storage balancing curves as shown by Fig. 4, which exhibits the storage preference for the two reservoirs in early April (SRWRO, 2012). The horizontal axis in the figure measures the total storage in the system, and the two curves represent the suggested desired storages for the respective reservoirs with regard to various total storage amounts. These curves vary during each ten-day period within a year to facilitate efficient storage allocation according to the pattern of water demands and reservoir inflow.

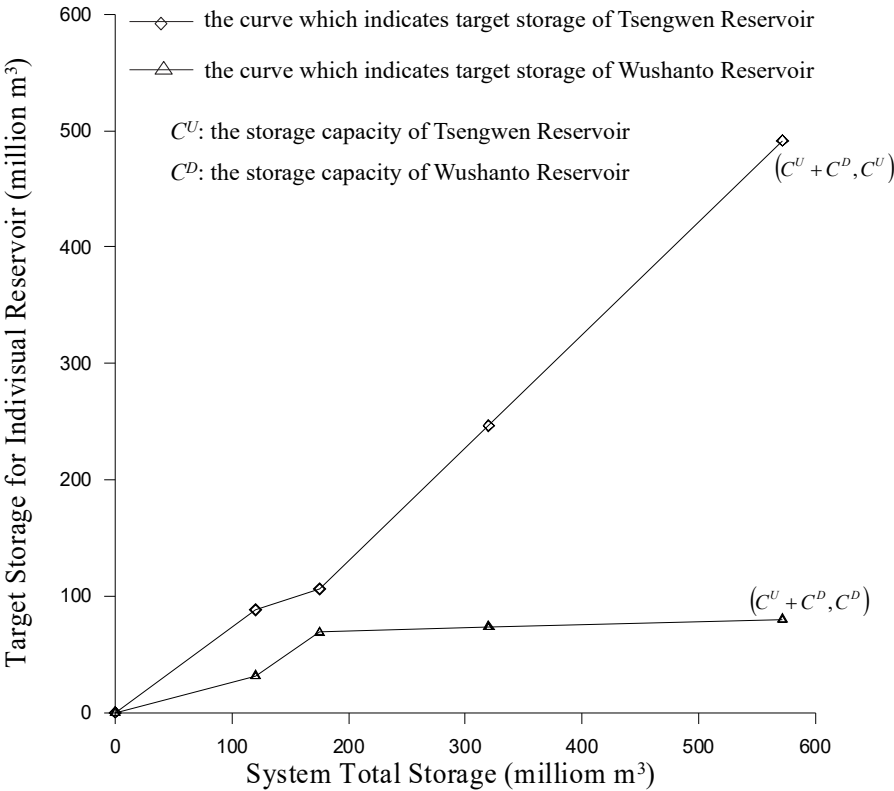



Fig. 4 Storage balancing curves for Tsengwen and Wushanto Reservoirs in the tenth ten-day period (early April)

Fig. 5 illustrates the whisker box of daily inflow discharge to the Tsengwen Reservoir in ten-day increments over a year. It shows a pattern of two peaks during the wet season, the first of which is induced by the front-induced plum rain between late May and early June and the

second is by typhoons mostly occurred in August. The average annual inflow volume of the reservoir is around 1.2 billion m^3. Water demand of this system is also included in Fig. 5, with an annual amount of 0.9 billion m^3 for two semiannual irrigations and 0.147 billion m^3 for public and industrial purposes with steady demand pattern.

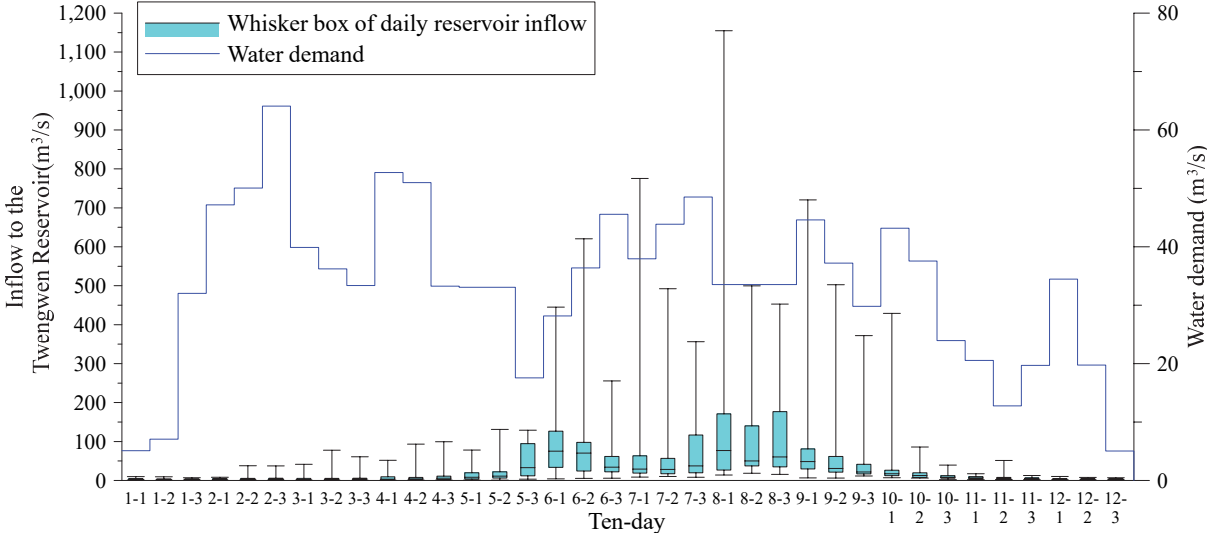



Fig. 5 Demand and inflow patterns of Tsengwen Reservoir of all ten-day periods throughout a year

2.2 The sedimentation of Tsengwen Reservoir and the adopted counteracts

10 From the beginning of operations in April 1973 until October 2017, the effective capacity of the Tsengwen Reservoir was reduced from 631.2 million m^3 to 453.7 million m^3. A major cause was Typhoon Morakot in 2009, which brought record-breaking rainfall to the reservoir watershed. The flood inflow of Tsengwen Reservoir peaked at 11,729 m^3/s, which is only slightly below the peak of its probable maximum flood as 12,430 m^3/s. Measurements at the

15 end of 2009 indicated that the sedimentation of Tsengwen reservoir had increased by a massive 91.08 million m^3 that year, which is 19.7 times that of the average annual sedimentation between 1973 and 2008. The average annual inflowing sediment volume was elevated to 5.6 million m^3.

In response to the substantial increase in sedimentation, the SRWRO increased the

releasing capacity of the permanent river outlet (PRO) to 177 m³/s and constructed a new desitling tunnel (DST) near the dam to enhance sediment venting during floods. The improvement of PRO includes replacing the Howell-Bunger valve by a jet flow gate with invert at 153.37 El. m. The design discharge and minimum operating WSL of the DST are 1,070 m³/s and 210 El.m respectively. The average annual sluicing volume of sediments through the PRO and DST is estimated as 1.6 million m³ by the SRWRO.

In addition to hydraulic sluicing, the master plan of desilting Tsengwen Reservoir counters the annual inflowing sediment by 3.0 million m³ through hydrosuction, 0.5 million m³ through sediment excavation and 0.5 million m³ through sediment yield reduction. This shows hydrosuction is the major approach adopted, due to its recent economic cost as 2.5 USD per desilted sediment volume (m³) and ability to continue desilting during non-flood periods. Several soil dikes were constructed in the river immediately downstream from the dam as temporary depositing area for the dredged slurries. The lump-sum volume of the depositing area, which constrains the annual dredging capacity, already reaches the available maximum as 3.5 million m³. For the other desilting measures, empty flushing could be a potential alternative due to the high cost of sediment excavation as 20 USD/m³ and uncertainties of effectiveness of sediment yield reduction. At present, the bed elevation in front of the Tsengwen Dam have been raised beyond 178 El. m. This level is higher than the invert of the PRO inlet which allows empty flushing.

3. ~~Material and Methods~~ Methodology

3.1 Qualitative analysis: Key factors for successful operations of empty flushing

Two major performance indices, expected desilting volume and the induced increments of water shortage, are used to evaluate an empty flushing strategy. An optimal strategy should maximize the desilting volume while maintaining the incremental shortage under an acceptable

threshold. According to the characteristics of the case study area and the other cases in Table 3, key factors for succeeding in these indices are identified as follows:

1. Qualitative conditions for water supply (~~QCWS~~ WS)

   (1) ~~QCWS 1~~ WS1F: Adequate water supply *during* empty flushing

   ~~In order to satisfy this condition, e~~Episodes between periods with heavy water supply pressure while backup water resources in the system is adequate can be utilized as windows of opportunity to implement empty flushing. ~~One example is the Dapu Reservoir in central Taiwan, which primarily provides agricultural and industrial water supply. Empty flushing of this reservoir is scheduled from May to July when irrigation demand is low and reservoir inflow is sufficient for demands. In contrast, reservoirs that provide water to the general public must maintain at stable supply level throughout the year. Empty flushing of such reservoirs would require backup water sources capable of ensuring a steady supply until the reservoirs can resume normal operations. One example is the Agongdian Reservoir in southern Taiwan which undergoes empty flushing from June to September annually, during which trans-basin diversion from an adjacent basin adequately supplements public and agricultural water supply.~~ As can be seen in Fig. 5, periods between late May and early June is when the irrigational water demand, which constitutes the majority of total demands, is lower. The first semiannual rice crop is harvested, and the second semiannual irrigation just begins. As shown in Fig. 2, between May 11 and June 30, the lower limit of joint operation rule curves of the two reservoirs is below the effective capacity of the Wushanto Reservoir. Even if the Tsengwen Reservoir is empty, as long as the Wushanto Reservoir is full, the total storage of the system would still exceed the lower limit and is generally adequate to fulfill demand.

   (2) ~~QCWS 2~~ WS2A: Adequate water supply *after* empty flushing

Satisfaction of this condition requires sufficient reservoir inflow following empty flushing to rapidly replenish the storage of the reservoir. Thus, the capacity of a reservoir undergoing empty flushing is usually relatively small compared to the volume of its inflow. Basson and Rooseboom (1997) indicated that empty flushing is more feasible for reservoirs with an effective capacity to annual inflow volume ratio (capacity-inflow ratio, CIR) of less than 0.03. Many of the reservoirs in Table 3 fulfill this criterion. The others that have a CIR greater than 0.03 are located in areas with uneven seasonal rainfall distributions, such that the abundance of inflow during flood seasons can effectively refill the storage soon after empty flushing. ~~One example is the Dapu Reservoir, which receives abundant rainfall and inflow from May to August every year. This particular reservoir can remain empty until early July without affecting the subsequent irrigational water supply.~~ The case study system with the CIR for the Tsengwen Reservoir as 0.38 shares the same characteristic of uneven rainfall distribution. The proper timing for terminating empty flushing should thus be carefully determined to ensure the remaining inflow during wet season satisfies this condition.

2. Qualitative conditions for flushing sediments (~~QCFS~~ FS)

Compliance with FS promotes efficiency of sediment flushing. The key is to take advantage of opportunities with both high inflow and low WSL of the primary reservoir to perform empty flushing.

(1) ~~QCFS1~~ FS1Q: High inflow during empty flushing

High inflow is required to more effectively scour and flush out the depositions of the reservoir. Atkinson (1996) and White (2001) indicated that empty flushing should only be initiated when the inflow is at least double the inflow in ordinary conditions. ~~The experience with flushing the Zemo Afchar Reservoir of the former USSR (Chaudhry and Habib-ur-rehman, 2012) suggests that empty flushing is most effective~~

~~with inflow between 400 to 500 m³/s, which is 2 to 2.5 times the average inflow (Bruk, 1985; Singh and McConkey Broeren, 1990). The operating experiences of Jianshanpi Reservoir in southern Taiwan also suggest that the efficiency of empty flushing peaks during heavy rainfall events when daily rainfall on the reservoir watershed is between 40 to 60 mm. This condition can also be artificially achieved. For instance, during the empty flushing of the Mangahao Reservoir in New Zealand, water was released from another upstream reservoir to enhance the scouring of depositions and thus maximize desilting volume (White, 2001).~~ For the Tsengwen Reservoir, wet season generally begins between late May and early June as the front-induced precipitation occurs. For floods during this period, the daily inflow discharge usually exceeds 100 m³/s, which is over 10 times of average inflow during January to April, and the hourly peak discharge could be beyond 1,000 m³/s.

(2) ~~QCFS2~~ FS2L: Low WSL *before* and *during* empty flushing

a. *Before* empty flushing is started: ~~operators could take advantage of periods when the reservoir WSL is low to perform drawdown and initiate empty flushing. In cases where the reservoir has outlets with sufficient capacities, timely drawdowns can be performed shortly prior to expected floods so that the flood inflow can effectively scour and flush out depositions. One example is the Dapu Reservoir, of which WSL is generally the lowest in mid-May. This timing is thus considered as the ideal time to empty the reservoir, with the expectation that subsequent abundant floodwater from May to August can also fulfill the QCWS 1, QCWS 2 and QCFS 1.~~ the operating records of Tengwen Reservoir over four decades shows its WSL is generally the lowest in mid-May, with average storage as 98.7 million m³ and median as 68.98 million m³. This means if the storage can be properly allocated to the Wushanto Reservoir then the Tsengwen Reservoir is likely to be nearly empty during these

periods. The capacity of PRO would also allow timely drawdown prior to expected flood so that the flood inflow can satisfy FS1Q.

b. *After* empty flushing is initiated: Once empty flushing operation is initiated, the reservoir should remain as close to empty as possible to maintain high flushing efficiency. However, if the inflow exceeds the capacity of PRO, then the WSL of the reservoir will arise. This leads to decreased flow velocity and reduced flushing efficiency in the reservoir. Atkinson (1996) suggested the use of the drawdown ratio (DDR) to measure the flushing efficiency. This index is defined as 1 minus the ratio between the depth of WSL during empty flushing and the depth of normal pool level of the reservoir. Atkinson (1996) and White (2001) defined incomplete drawdown flushing as situations in which DDR is less than 0.66, wherein the depth of the water during flushing is greater than one third of the maximum depth. ~~In such circumstances, the efficiency of empty flushing is significantly reduced and it is recommended to switch the operation to the regular mode of water supply~~. For the case of Tsengwen Reservoir, this threshold marks at the elevation of 185 El. m, which corresponds to an impoundment of 16.6 million m^3. In circumstances when the WSL exceeds this level, the efficiency of empty flushing is significantly reduced and it is recommended to switch the operation to regular mode of water supply.

The above analysis eventually leads to a conclusion that the meteorological and operating conditions during May and June are favorable for empty flushing of the Tsengwen Reservoir.

3.2 Quantitative derivation of the optimal empty flushing strategy

~~While the discussion of the previous subsection is generally applicable for any multi-reservoir systems, the proposed quantitative methodology as well as the following case study apply specifically to those without means to artificially generate flushing inflow to the primary~~

reservoir. In addition, we focus on event-based operation. This means that the timing and duration of empty flushing is flexible according to real-time hydrological and operational conditions. If these conditions are not favorable, the primary reservoir could resume regular operation of water supply. This feature distinguishes the present method from previous related studies (Chang et al., 2003; Khan and Tingsanchali, 2009), which mandatorily empty reservoir storage during predetermined periods within a year. This paper also assumed that the water demands in the system require constant supply, thus rendering empty flushing infeasible during parts of the year. To facilitate determination of feasible periods for empty flushing, the following criteria are provided:

1. Meeting QCWS 1 requires periods of low water demand during which backup reservoirs can provide adequate supply during empty flushing.

2. QCFS 2 dictates that the most opportune time to begin empty flushing is at the end of the dry season. At this time the storages of reservoirs are usually at their lowest levels of the year. This ensures that storage can be effectively and efficiently drained by drawdown flushing through the capacitated bottom outlets of the primary reservoir.

3. Meeting QCFS 1 requires that the feasible duration for empty flushing should be extended into the wet season to ensure adequate inflow for scouring depositions.

Meeting QCWS 2 requires that the feasible duration for empty flushing should be ended before the end of the wet season to ensure adequate replenishment of reservoir storage after the flushing operation.

The ~~following~~ proposed method adopts the simulation-optimization linkage approach for deriving optimal strategy. It requires simulating the operations of water supply and empty flushing, thus allowing for quantifying the desilting volume as well as the incremental water shortage generated by a given strategy. The process of water supply is simulated according to a set of joint operating rules as presented in subsection 3.2.1. When specific quantitative

conditions presented in subsection 3.2.2 are achieved, empty flushing in the primary reservoir is activated and the approach in subsection 3.2.3 is employed to estimate the desilting volume. The empty flushing terminates when the conditions presented in subsection 3.2.4 are reached, and the simulation is switched to regular water supply operation until the next time activation conditions are satisfied. The simulation model is linked to an optimization algorithm to calibrate optimal parameters in the activation and termination conditions, according to the formulation presented in subsection 3.2.5. Fig. 6 depicts a flowchart of the analyzing procedure.

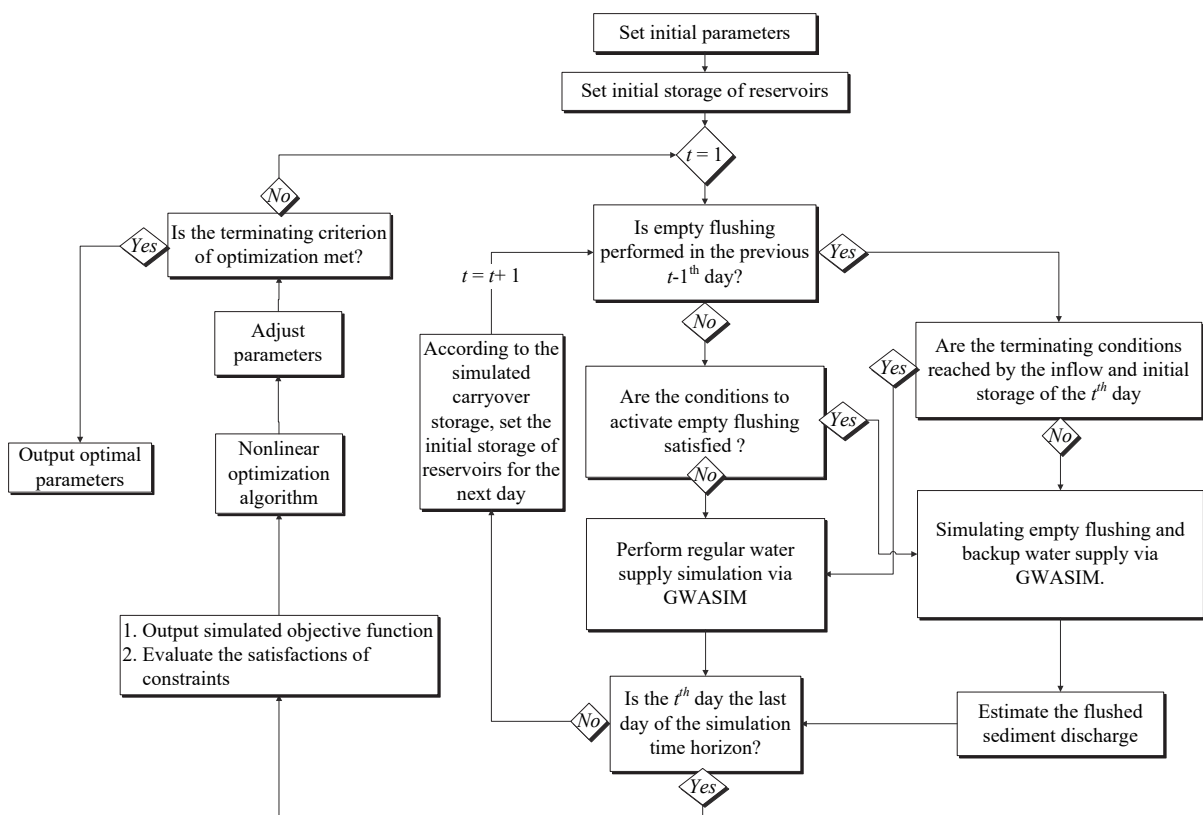



Fig. 6 The procedure to derive the optimal empty flushing strategy

3.2.1 Joint operating rules for a multi-reservoir system

According to Oliveria and Loucks (1997), the rules to jointly operate multiple reservoirs for water supply include the following two phases:

1. Determination of total water supply: The total amount of water supply is determined based on the total storage of reservoirs and the system-wide release rule. The rule stipulates that

if the total storage does not suffice, a discount of total water supply may be applied, such as the joint rule curves shown in Fig. 2 and the water rationing mechanism described in section 2. by the system-wide release rule. Fig. 2 presents the joint operating rule curves, a form of the system-wide release rule, for the Tsengwen and Wushanto Reservoirs in southern Taiwan. The location and associated water resources system of these reservoirs are depicted in Figs. 4 and 6 in the case study section. The release rules stipulate that when the total storage of the two reservoirs is below the critical limit, only 80% of the public demand and 50% of the agricultural and industrial demands will be satisfied. When the total storage is between the lower and critical limits, the public demand should be fulfilled and 75% of the agricultural and industrial demands need to be satisfied. When the total storage is between the upper and lower limits, all demands should be fulfilled. In the event that the storage in the Tsengwen Reservoir exceeds the upper limit, extra water can provide excess supply or full loaded hydropower generation until the storage returns to the upper limit.

2. Distributing storage to individual reservoirs: Based on the calculated total water supply, the total end-of-period storage in the system can be estimated with the expected reservoir inflow during one single operating period. The release from each individual reservoir can then be determined by applying an individual reservoir storage balancing function, such as the storage balancing curves depicted in Fig. 4. Fig. 3 exhibits the storage balancing curves for the Tsengwen and Wushanto Reservoirs in early April (Southern Regional Water Resources Office, SRWRO, 2012). The horizontal axis in the figure measures the total storage in the system, and the two curves represent the suggested target storages for the respective reservoirs with regard to various total storage amounts. These curves vary during each ten-day period within a year to facilitate efficient storage allocation according to the pattern of water demands and reservoir inflow.

Fig. 4 was designed to ensure efficient utilization of water resources, without any

consideration of empty flushing. It was derived initially based on field operating experiences and revised through trial and error process. The first part of the proposed method requires appropriate adjustment of the storage balancing curves before and during the periods feasible for empty flushing. This adjustment prioritizes the water released from the primary Tsengwen Reservoir while preserving storage in the Wushanto Reservoir. This complies with the aforementioned WS1F and FS2L, and creates a favorable initial condition for empty flushing. Fig. 7 depicts the balancing curves updated from the original Fig. 4.

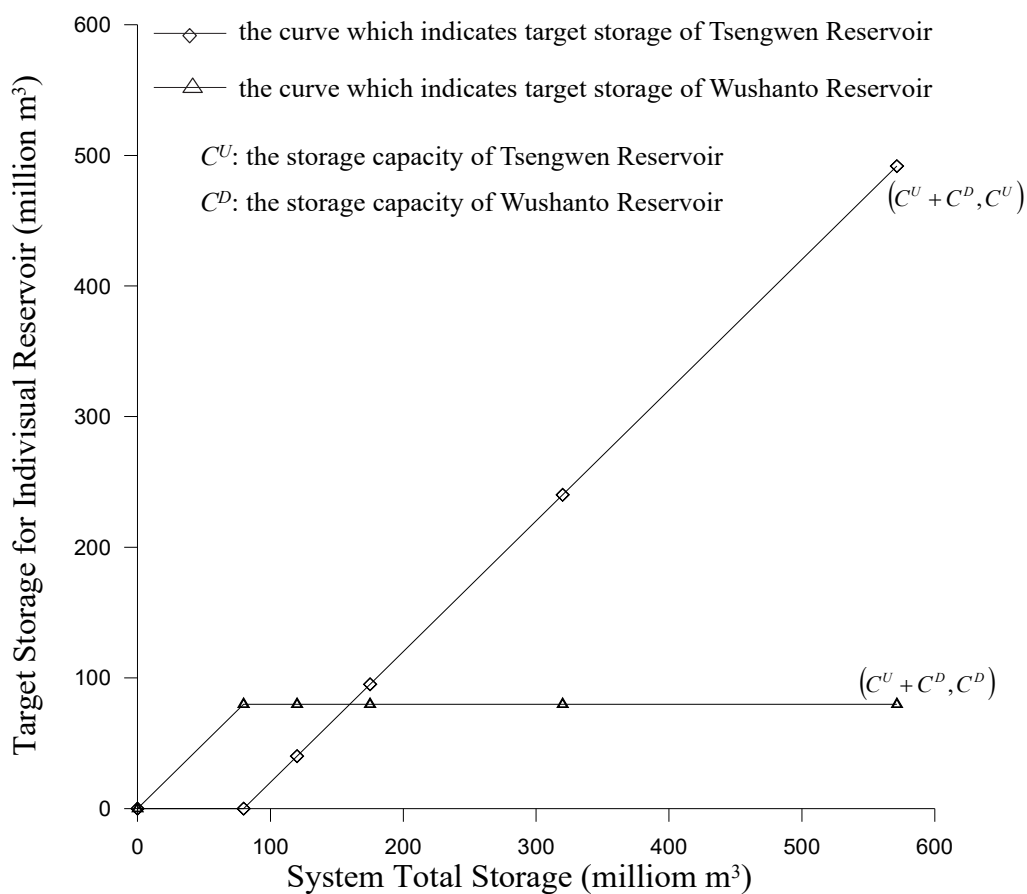



Fig. 7 Modified storage balancing curves using Tsengwen Reservoir as primary source to satisfy water demand

3.2.2 Conditions for initiation of an empty flushing operation

Water supply simulation of historical daily reservoir inflow records is sequentially performed according to the joint operating rules. During the simulation, empty flushing

operation is activated when *all* of the following conditions are satisfied:

1. The current simulating date falls within the pre-evaluated feasible timeframe for empty flushing.

2. The storage of the primary reservoir is lower than a threshold T^U. This ensures the satisfaction of FS2L. A higher value of T^U allows initiating drawdown flushing at higher primary reservoir storage, thus increasing the range of opportunities for empty flushing. Nonetheless, a higher T^U incurs the risk that, if subsequent reservoir inflow falls short of predicted values, the emptied storage may not be replenished.

3. The total storage in the backup reservoir is greater than a threshold T^D. This ensures meeting WS1F. A higher value of T^D elevates the stability of water supply during empty flushing. In cases where either this or the above condition has not been met, demand should be supplied from the primary reservoir as much as possible, or storage should be diverted from the primary reservoir to the other. However, this storage reallocation may be limited by the water transmitting capacity between reservoirs. Such that the conditions for initiating empty flushing may not be met within the pre-specified feasible period for flushing. Therefore, a higher T^D may reduce the opportunities to perform empty flushing.

3.2.3 Estimation of the flushed sediment discharge

Once the activation conditions are met, the gates of the PRO of Tsengwen Reservoir are fully opened to empty the storage and route the inflowing water and sediments. The release from the primary reservoir would cause blockages of the downstream water diversion or water treatment facilities due to its high sediment concentration. Thus the water supply relies solely on the storage preserved in the Wushanto Reservoir. During empty flushing, the inflow, outflow and WSL of the primary reservoir are used to estimate the volume of flushed sediments. The estimation can be based on either numerical simulation or empirical formula, the second of

which is adopted by this paper due to its simplicity and easy incorporation with the proposed optimization framework. After the optimized strategy identifies feasible events of empty flushing, numerical simulation is then used to verify the effectiveness of the empirical formula, as presented in Appendix 3.

5   The empirical formula developed by the International Research and Training Center on Erosion and Sediment (IRTCES) in Tsinghua University, Beijing (IRTCES, 1985) is employed for the estimation of releasing sediment discharge from the primary reservoir. The formula is based on measurements from 14 reservoirs in China:

$$QC_t = \psi \frac{Q_t^{1.6} S_f^{1.2}}{W^{0.6}}$$
(1)

10   where QC_t and Q_t denote the sediment discharge (T/s) and water discharge (m³/s) flushed from the primary reservoir during the t-th simulating day, respectively; S_f represents the energy slope associated with the flow in the primary reservoir during empty flushing; W is the width of the flushing channel (m), which can be estimated using the empirical formula $W = 12.8 \cdot Q^{0.5}$ (Atkinson, 1996), and ψ is the flushing coefficient, associated with the characteristics of the 15   sediment and topography of the reservoir.

For the current case study area, the value of ψ is set as 60 when the reservoir storage remains nearly empty, as suggested by Atkinson (1996) for cases with limited-capacity bottom outlets. To prevent overestimating the effectiveness of empty flushing, it is assumed that if a flood raises the WSL of the Tsengwen Reservoir to exceed 185 El. m, which is about 30 % of 20   its maximum depth, then the flushed sediment volume from the PRO is set to be 0. This setting is supported by field measurements of Tsengwen Reservoir and other adjacent reservoirs which regularly undergo empty flushing in southern Taiwan. These measurements are reported in Appendix 2.

3.2.4 Conditions for termination of empty flushing operation

Empty flushing should be terminated if *one* of the following circumstances occurs:

1. The accumulative released water volume from the primary reservoir exceeding a certain threshold T^V would halt the flushing of the year. Empty flushing consumes water originally stored in the reservoir for water supply. This consumption is expected to be compensated by subsequent floods which refill the reservoir and induce spillage. Nonetheless, if the floods are not significant enough following the flushing, the impacts of excess releasing will be carried on to the next dry season and increase water shortage. The threshold T^V alleviates this impact by restraining the water consumption volume of empty flushing.

2. Providing the accumulative release volume is still under T^V, the flushing should be terminated when the flood flow has raised the WSL of the primary reservoir and daily inflow subsequently recedes to be below the capacity of associated bottom outlets. This situation indicates that the operation has been successfully timed to encounter a flood and should thus be ended when the flood ends.

3. The flushing should be ended when the storage of backup reservoirs decreases to below a threshold T^d. This condition prevents short-term water shortages following flushing operations resulting from insufficient storage. During the empty of the primary reservoir, providing water supply will gradually reduce available storage in the other reservoir. A higher value of T^d will cause the storage below threshold more quickly, thus reducing the window of operation for empty flushing. Nonetheless, adequate reservoir inflow and proper storage reallocation after an earlier termination of one flushing operation will facilitate the re-initiation of a subsequent operation during the feasible period for empty flushing. Thus, under conditions of a higher T^d value, the pattern of empty flushing may be transformed

from a few operations of longer duration into multiple intermittent operations of shorter durations.

A generalized water allocation simulation model (GWASIM) developed by Chou and Wu (2010) is used to simulate the alternating operations of empty flushing and joint water supply according to the aforementioned rules and conditions. The simulation is designed to evaluate the performance of the water resources system under specific storage volume, water demand and operating rules. It requires sequential daily routing of system operation for several decades of inflow series to reflect the long-term hydrological variation. GWASIM has already been implemented in the planning and management studies of all water resources systems of western Taiwan. Details of its simulations regarding the operations of multi-reservoir systems can be found in Chou *et al*. (2006) and Chou and Wu (2014).

3.2.5 Evaluation of optimal empty flushing strategies

The thresholds for activating and terminating an empty flushing operation as described in subsections 3.2.2 and 3.2.4 are regarded as decision variables. They are calibrated to maximize the total desilting volume without inducing both short- and long-term intolerable water shortage scenarios. The short-term scenario relies on the occurrence of subsequent floods to induce spillage and fully compensate for the impact of emptying reservoir. Thus the incremental shortage following empty flushing is concentrated in a few months before the consequent floods, during each of which the monthly shortage increment and ratio is calculated respectively:

$$d_{n,m}^{I} = d_{n,m} - d_{n,m}^{0}, \quad m = 0,1,2,...,n^{m}, \ n = 1,2,...,n^{y} \quad (2)$$

$$d_{n,m}^{R} = \frac{d_{n,m}}{D_{m}}, \quad m = 0,1,...,n^{m}, \ n = 1,2,...,n^{y} \quad (3)$$

where $d^I_{n,m}$ and $d^R_{n,m}$ represent the water shortage increment and ratio during the *m*-th month following the feasible period of empty flushing in the *n*-th simulating year; D_m denotes the water demand during the *m*-th month following empty flushing; $d_{n,m}$ and $d^0_{n,m}$ represent simulated water shortages under conditions with and without empty flushing operations. $d^0_{n,m}$ is from simulating the default regular water supply process using the GWASIM and $d_{n,m}$ is obtained by incorporating empty flushing operations according to the activating and terminating conditions defined by the decision variables. n^m is the number of months within which the impact of empty flushing on water supply is carried over; and n^y is the number of simulating years.

The long-term shortage scenario aims at situations that subsequent floods are not significant enough to induce reservoir spillage. Thus the incremented shortage extends into the next dry season, of which shortage ratios with or without empty flushing are expressed as below:

$$d^{R,0}_{n,dry} = \frac{d^0_{n,dry}}{D_{dry}}, \quad n = 1, 2, ..., n^y \tag{4}$$

$$d^R_{n,dry} = \frac{d_{n,dry}}{D_{dry}}, \quad n = 1, 2, ..., n^y \tag{5}$$

where D_{dry} represents the total demand during the dry season, $d^0_{n,dry}, d_{n,dry}, d^{R,0}_{n,dry}$ and $d^R_{n,dry}$ are the water shortage volumes and ratios with and without executing empty operation during the dry season, respectively.

The formulation of the optimization problem is as follows:

$$\textit{Maximize} \quad \sum_{t=1}^{n^t} QC_t \tag{6}$$

subject to

$$d_{\max}^{R} = \max_{n,m}(d_{n,m}^{R} | d_{n,m}^{I} > 0) \le \alpha \quad m = 0,1,2,...,n^{m}, n = 1,...,n^{y} \qquad (7)$$

$$d_{\max,dry}^{R} = \max_{n=1,...,n^{y}}(d_{n,dry}^{R} | d_{n,dry}^{R,0} \le \beta) \le \beta \qquad (8)$$

where n^{t} is the total number of days within the simulating horizon; QC_{t} is the simulated
sediment discharge from the primary reservoir by empty flushing on the t-th day. It is
determined by substituting the release of the primary reservoir during the flushing period into
Eq. (1). The left hand side (LHS) of Eq. (7), $d_{\max}^{R}$, represents the maximum monthly water
shortage ratio from the n^{y} simulating years given that the short-term shortage is induced by
empty flushing. The right hand side (RHS) of Eq. (7), α, is the maximum acceptable value for
$d_{\max}^{R}$. The LHS of Eq. (8), $d_{\max,dry}^{R}$, represents the maximum shortage ratio during the dry season
following empty flushing, given that the original shortage ratio of the same periods without
flushing is less than a failure threshold. The failure threshold of shortage ratio β usually means
the irrigation for majority areas needs to be suspended to ensure steady public water supply in
Taiwan. Eq. (8) thus avoids inducing additional failure events of water supply in the dry season
following empty flushing.

The BOBYQA, a nonlinear optimization algorithm of Powell (2009), is used to solve the
problem. The details of BOBYQA can be found in Powell (2009) and the barrier function
approach to handle the constraint of Eqs. (7) and (8) can be found in Chou and Wu (2015).

4. ~~Result and discussion~~ Analysis, results and discussion

4.1 The base scenario with default operating rules ~~Determination of the feasible period for empty flushing~~

In the base scenario, sequential water supply simulation in the absence of empty flushing is performed using the daily inflow records of the reservoirs from 1975 to 2009 and the joint operating rules as described in section 2. It generates the default water supply condition, i.e. $d_{n,m}^0$, $d_{n,dry}^0$ and $d_{n,dry}^{R,0}$ in Eqs. (2) and (4), and provides a basis to evaluate the incremental shortage induced by empty flushing.

Based on the simulated results, the probability that the storage in the Tsengwen Reservoir drops below 20 million m^3 for preparing empty flushing timely in a given month while the Wushanto Reservoir storage simultaneously exceeds the lower limit of the rule curves is calculated. The results are displayed in the "Balancing curves I" rows of Table 1. The results show that in May, there is a 52 % probability that the storage of the Tsengwen Reservoir will drop below 20 million m^3 and an 8 % probability that the Tsengwen Reservoir storage drops below 20 million m^3 while the Wushanto Reservoir storage simultaneously exceeds the lower limit. In June, the two probabilities are 31 % and 14 %, respectively. These two months with the highest probabilities of desired storage distribution within a year are most promising for empty flushing. The respective storage of the Tsengwen and Wushanto Reservoirs each satisfies the abovementioned conditions only between May 11 and June 20, which is selected as the feasible period for empty flushing in the Tsengwen Reservoir.

4.2 Schemes for the modification of storage balancing curves

Based on the base scenario, three additional simulations are conducted in which the modified storage balancing curves as Fig. 7 are applied during (1) May 1 to June 20, (2) April 1 to June 20, and (3) March 1 to June 20. The simulated results are summarized in Table 1. It demonstrates that the probability of favorable storage distribution for empty flushing during May and June can be effectively elevated by modifying storage balancing curves in April. The trade-off of creating this favorable initial condition is that preserving the storage of Wushanto

Reservoir before and during empty flushing might cause unnecessary spillage while the full reservoir cannot store the inflow from Guantien Creek. Also, allocating storage between reservoirs through the Wushan Hill Tunnel will induce more transmitting loss of water. Nonetheless, the shortage ratios generated by the modified balancing curves are no more than 0.01 higher than those from the original balancing curves, which means that the modification has only a trivial impact on the efficiency of water resources utilization.

The results also indicate that the average water shortage ratio during the wet season drops considerably after July. This is because the first typhoon of the wet season generally occurs in July or early August, bringing substantial inflow to the reservoirs. Thus in the following evaluation of empty flushing strategies, the water shortage scenarios through the end of July are selected to represent the impact of empty flushing on short-term water supply, i.e. n^m in Eqs. (3) and (7) is set as 1. For the long-term impact, the shortage ratio during the next dry season, from January to May of the next year, are considered, referring to $d_{n,dry}$, $d_{n,dry}^R$ and $d_{\max,dry}^R$ in Eqs. (4) and (8).

Table 1 Monthly probabilities of Tsengwen Reservoir storage dropping below 20 million

m³ under various strategies of storage allocation

Month	Jan	Feb	Mar	Apr	May	June	Jul	Aug	Sep	Oct	Nov	Dec
Strategy ＼ Index	Monthly probabilities of Tsengwen Reservoir storage dropping below 20 million m³											
Balancing curves I	0.01	0.04	0.13	0.13	0.52	0.31	0.12	0.02	0.00	0.00	0.00	0.00
Balancing curves II	0.03	0.04	0.13	0.13	0.64	0.33	0.13	0.03	0.00	0.00	0.00	0.01
Balancing curves III	0.03	0.04	0.13	0.34	0.78	0.33	0.13	0.02	0.00	0.00	0.00	0.01
Balancing curves IV	0.03	0.04	0.13	0.45	0.78	0.33	0.13	0.02	0.00	0.00	0.00	0.01
Strategy ＼ Index	Monthly probabilities of storage in Tsengwen Reservoir dropping below 20 million m³ with storage in Wushanto Reservoir exceeding the lower limit											
Balancing curves I	0.00	0.00	0.00	0.00	0.08	0.14	0.00	0.00	0.00	0.00	0.00	0.00
Balancing curves II	0.00	0.00	0.00	0.00	0.11	0.16	0.00	0.00	0.00	0.00	0.00	0.00
Balancing curves III	0.00	0.00	0.00	0.00	0.14	0.16	0.00	0.00	0.00	0.00	0.00	0.00
Balancing curves IV	0.00	0.00	0.00	0.01	0.14	0.16	0.00	0.00	0.00	0.00	0.00	0.00
Strategy ＼ Index	Average monthly water shortage ratio											
Balancing curves I	0.10	0.17	0.23	0.29	0.22	0.07	0.10	0.06	0.06	0.09	0.09	0.11
Balancing curves II	0.11	0.18	0.24	0.30	0.23	0.07	0.10	0.06	0.07	0.09	0.09	0.12
Balancing curves III	0.11	0.18	0.24	0.31	0.23	0.07	0.10	0.06	0.07	0.09	0.09	0.12
Balancing curves IV	0.11	0.18	0.24	0.31	0.23	0.07	0.10	0.06	0.07	0.09	0.09	0.12

Balancing curves I: the original storage balancing curves as shown in Fig. 4.
Balancing curves II: adopting the modified curves as in Fig. 7 from May 1 to June 20.
Balancing curves III: adopting the modified curves as in Fig. 7 from April 1 to June 20.
Balancing curves IV: adopting the modified curves as in Fig. 7 from March 1 to June 20.

4.3 Preliminary simulations and assessment of empty flushing strategies

The thresholds to activate and terminate an empty flushing operation, i.e. T^U for the Tsengwen Reservoir, T^D and T^d for the Wushanto Reservoir, and T^V for the maximum accumulative releasing volume are parameters to be optimized. Except T^V, the other parameters are allowed to vary during different ten-day periods from May 11 to June 20 to promote the performance of desilting and backup water supply. Before actually optimizing these parameters, preliminary simulations are performed with constant storage thresholds throughout May 11 to June 20. This process facilitates determination of a good initial solution as well as a basis for

comparison to measure the effects of optimization. The preliminary simulations consider seven different T^U values, ranging from 0 to 60 million m^3 with a constant interval of 10 million m^3, for the Tsengwen Reservoir. Six values (including 55, 60, 65, 70, 75 and 78 million m^3) for T^D and nine values (including 30 to 70 million m^3 with a constant interval as 5 million m^3) for T^d are considered. The value T^V is set as an extremely high value, thus imposing no constraint on the water releasing volume of empty flushing as well as the long-term water supply. All these values contribute to a total of 308 combinations of empty flushing strategies in which T^d is less than T^D. Simulations of the 308 combinations are performed using the original storage balancing curves. The resulting average annual desilting volume and maximum short-term monthly water shortage ratio induced by empty flushing are then calculated. The results are presented in Fig. 8, in which the desilting volume is converted from the estimated flushing discharge by Eq. (1) with bulk density as 1.56 T/m^3 (Water Resources Agency, 2010). The simulations are then repeated by applying the modified storage balancing curves in Fig. 7 to the period between April and June, the results of which are displayed in Fig. 9. A comparison of Figs. 8 and 9 shows that the modified storage balancing curves effectively enhance the effectiveness of desilting. For instance, strategies with d^R_{max} between 0.17 and 0.23 correspond to a maximum annual desilting volume of 0.06 million m^3/year in Fig. 8, whereas the same strategies in Fig. 9 result in an increase of desilting volume reaching 0.54 million m^3/year.

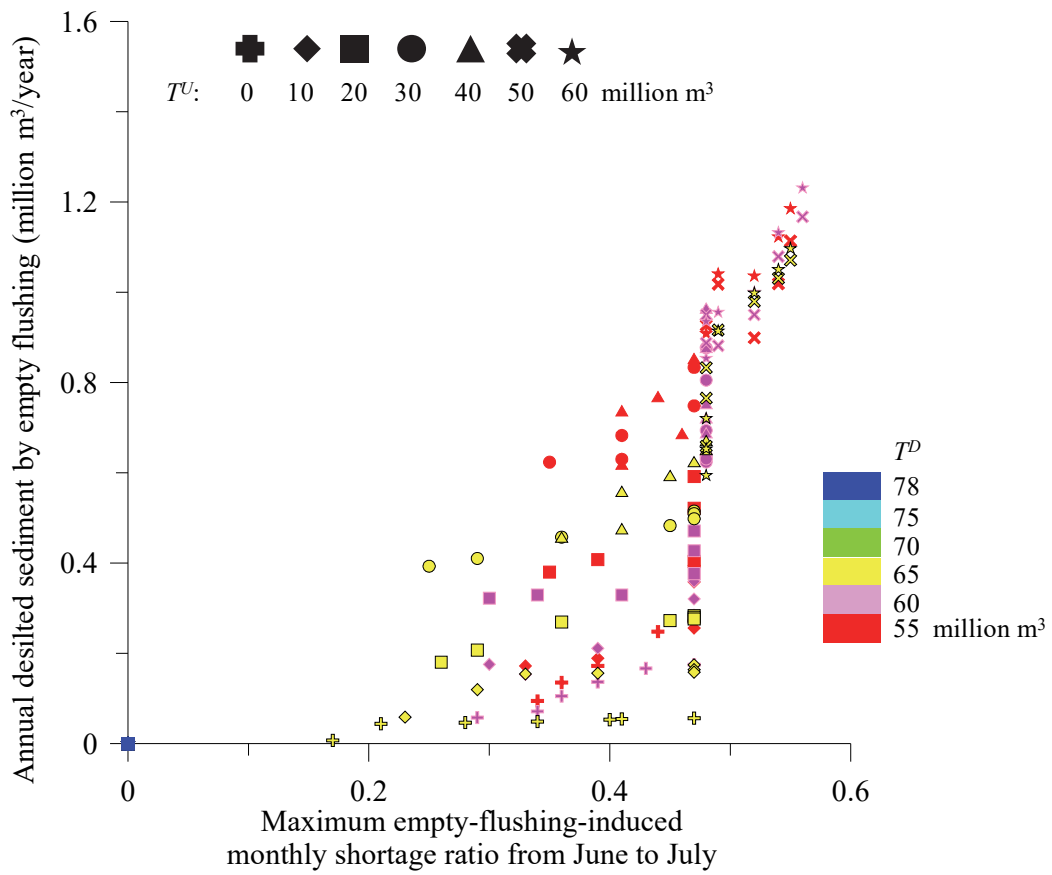



Fig. 8 Simulation results of various empty flushing strategies using the original storage balancing curves

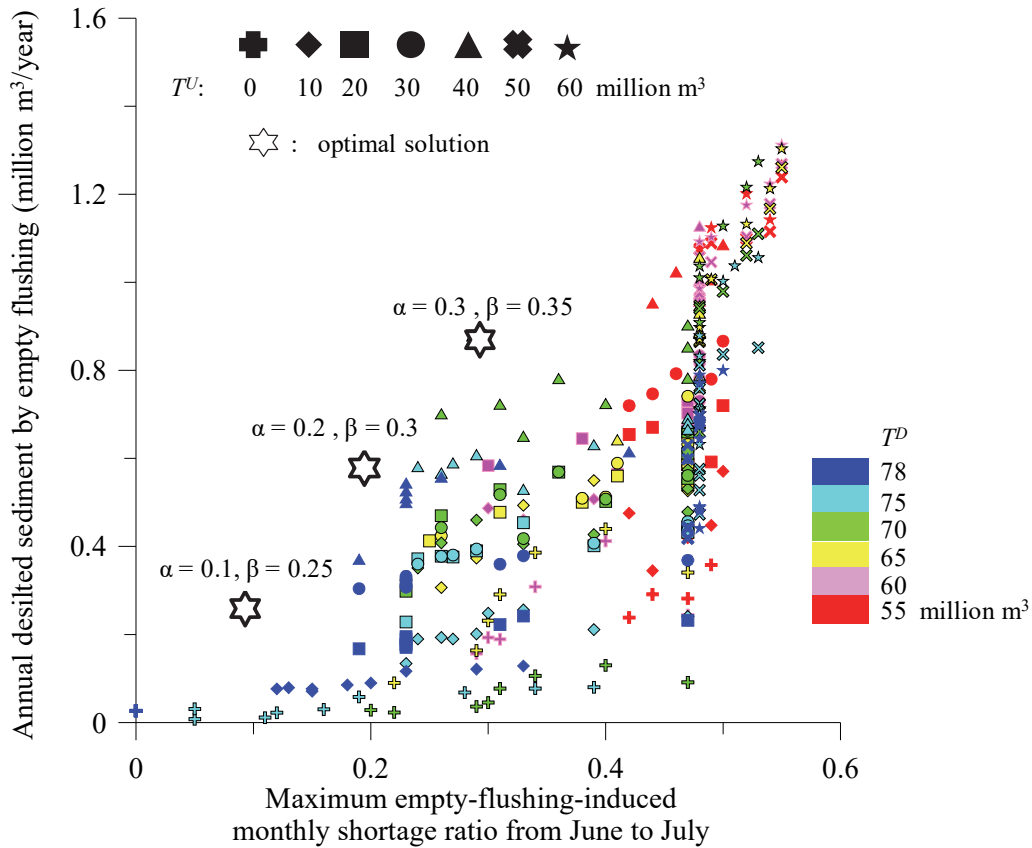



Fig. 9 Simulation results of various empty flushing strategies using modified storage balancing curves from April to June

4.4 Optimization of empty flushing strategies

Coupling GWASIM which simulates the water supply and empty flushing process from 1975 to 2009 with the optimization algorithm leads to an optimal solution of Eqs. (6), (7) and (8) under specific values of α and β. Three sets of α and β are tested, which are (0.1, 0.25), (0.2, 0.30) and (0.3, 0.35) respectively. The corresponding optimized results are presented in Table 2. The average annual desilting volume and maximum monthly shortage ratio induced by empty flushing are also marked in Fig. 9. The abovementioned desilting volumes are calculated using Eq. (1) with the setting of ψ described in sub-section 3.2.3. To validate this estimation, numerical simulations of sediment flushing process by the SRH-2D model of U.S. Bureau of Reclamation (Lai, 2008) are carried out for the major flushing events identified in

the optimal strategy associated with α=0.1 and β=0.25. The result shows great agreement between the empirical estimation and numerical simulation and is reported in Appendix 3. Sensitivity analysis of the flushing coefficient in the scenario of (α=0.1, β=0.25) is also performed to inspect its impact on the optimization. The result is presented in Appendix 4, which shows that the optimal strategy is dominated by the shortage constraints and insensitive to the value of ψ.

Fig. 10 depicts the historical accumulative sedimentation record of Tsengwen Reservoir, as well as the updated progress by imposing the suggested empty flushing events and subtracting the generated desilting volume from the actual sedimentation. Some features can be observed as following:

1. The Typhoon Morakot in 2009 represents an outlier and boosts the average annual sedimentation and inflowing sediment by over 2 million m^3 per year. The newly constructed DST aims for this kind of extreme floods and allow nearly 40% of sediments of density current and turbid storage passing through the reservoir along with the updated PRO. Most of the remaining detained sediments are expected to be removed by the cost-effective perennial hydrosuction. Nonetheless, its annual capacity has reached a maximum while no convenient downstream deposition area is currently available for further expansion.

2. Empty flushing serves as an alternative for more expensive or uncertain desilting measures other than hydraulic sluicing and hydrosuction, to achieve long-term balance between the incoming and outgoing sediment of a reservoir. The estimated net benefits by empty flushing are also included in Table 2. The referred benefit of flushing is the alternative cost by mechanical excavation as USD\$ 20 per unit volume (m^3) of sediment. The induced cost is from the water transferring fee, USD\$0.15 per m^3 of water, for compensating the agricultural purpose and enhancing irrigation management. The results reveal the economic superiority of empty flushing over mechanical excavation, as long as it does not induce

unmanageable water shortage and create additional large-scale suspensions of irrigation.

3. The hydrological characteristic of the case study system allows empty flushing only feasible in less than 40% of the simulating years. During the other years the reservoir storage is inadequate, i.e. either the storage of Wushanto Reservoir is lower than T^D or Tsengwen Reservoir is higher than T^U between May 11 to June 20. A trend of increasing frequency of empty flushing in recent years can also be observed in the figure. This might be the result of climate change which increases the variance of flood magnitude and more frequently lead to lower but adequate reservoir storage in the end of dry season in the case study area.

4. Due to the frequency of drought and high pressure of water supply in this system, the optimal strategy associated with α =0.1 and β =0.25 is selected for further scrutiny. Table 3 displays the simulated events of empty flushing based on this calibrated strategy.

Table 2 Optimal empty flushing strategies based on acceptable water shortage rates following the completion of empty flushing operations

Maximum allowable short- and long-term shortage scenarios	Optimized decision variables defining the rules for activation and termination of empty flushing													Performance indices					
	Tsengwen Reservoir flushing initiation condition T^U (million m³)				Wushanto Reservoir flushing initiation condition T^D (million m³)				Wushanto Reservoir flushing termination condition T^d (million m³)				Maximum allowable water volume consumed by empty flushing (million m³)	Water shortage increment (million m³/year)		Desilting volume (million m³/year)		Net benefits (million USD/year)	
	Ten-day period				Ten-day period				Ten-day period					1975 ~ 2009	1975 ~ 2018	1975 ~ 2009	1975 ~ 2018	1975 ~ 2009	1975 ~ 2018
	14th	15th	16th	17th	14th	15th	16th	17th	14th	15th	16th	17th							
$\alpha=0.1$, $\beta=0.25$	0.2	40.0	40.0	0.0	75.0	70.0	68.5	79.8	73.9	51.0	60.0	76.0	76.0	5.48	7.27	0.25	0.27	4.2	4.3
$\alpha=0.2$, $\beta=0.30$	60.0	40.0	44.0	30.0	75.0	61.0	67.5	79.8	55.0	40.0	44.0	60.0	132.0	8.95	11.86	0.59	0.69	10.5	12.0
$\alpha=0.3$, $\beta=0.35$	80.0	40.0	40.0	30.0	75.0	57.0	67.5	79.8	51.1	40.0	39.2	60.0	199.0	11.77	14.85	0.88	0.97	15.8	17.2

Table 3 Simulated empty flushing events based on the optimal strategy with α=0.1, β=0.25

Year	Duration	Inflow volume to T. Reservoir (M.m³)	Reservoir storage at initiation (M.m³) T.	W.	Reservoir storage at termination (M.m³) T.	W.	Water shortage until June increment (M.m³)	ratio (%)	Water shortage in July increment (M.m³)	ratio (%)	Water shortage ratio during the next dry season (%) w.o./e.f.	w./e.f.	Bottom release volume from T. Reservoir (M.m³)	De-silting volume (M.m³)	Ave. concentration (ppm)	Down-stream lateral flow during e.f. (M.m³)	Total Inflow to T. reservoir during the wet season (M.m³)	Spillage of T Reservoir in the wet season (M.m³)
1979	6/10	25.03	11.60	69.10	21.06	69.07	0.00	0.00	0.00	0.00	17.0	17.0	11.12	0.40	36,291	7.67	1,109	155.80
1984	5/13~5/14	2.21	0.00	78.53	0.00	72.97	0.00	0.00	0.00	0.00	45.0	49.0	2.21	0.04	18,194	1.32	676	--
	5/21~5/31	121.55	0.00	70.26	42.68	62.45							65.27	1.26	19,344	30.51		
1986	5/21~5/29	91.44	11.61	71.93	8.31	64.96	0.00	0.00	0.00	0.00	12.0	25.0	77.50	2.63	33,909	18.31	843	--
1989	5/14~5/15	1.78	0.00	78.83	0.00	73.24	0.00	10.00	0.00	41.00	1.0	1.0	1.78	0.03	17,010	0.35	1,006	121.60
1997	6/07~6/10	31.99	5.58	71.08	0.00	64.45	0.00	0.00	0.00	0.00	5.0	5.0	33.25	1.11	33,381	2.84	941	23.51
2006	5/25~6/05	127.63	6.71	72.66	25.62	62.40	0.00	0.00	0.00	0.00	20.0	21.0	86.26	2.43	28,115	17.06	1,657	503.86
2008	6/09~6/10	7.59	28.72	68.54	51.22	64.41	0.00	0.00	8.71	7.00	1.0	2.0	22.28	0.81	36,311	1.22	1,930	858.88
2009	5/11~5/12	1.36	0.00	77.86	0.00	72.24	0.28	2.00	0.00	41.00	28.0	28.0	1.36	0.02	18,001	0.03	1,554	744.37
2010	6/04-6/08	11.61	21.02	69.74	0.00	58.70	0.00	0.00	7.53	18.00	2.0	4.0	23.85	0.74	30,992	0.53	927	--
2013	5/11	1.47	0.00	75.56	0.00	72.81	0.00	0.00	0.00	0.00	20.0	20.0	1.47	0.03	19,767	0.63	1,347	402.24
	5/21-5/31	64.37	19.91	70.71	0.00	58.72							66.59	2.12	31,906			
2014	6/06	6.85	23.25	68.86	14.45	67.09	0.00	0.00	23.04	21.00	47.0	54.0	11.19	0.41	36,351	6.52	683	--

1. T. and W. represent Tsengwen and Wushanto Reservoirs respectively.
2. E.f. is the abbreviation of empty flushing.
3. The monthly shortage ratio in July following the empty flushing operations in 1989 and 2009 both reach 0.41. However, the corresponding shortage increments are both 0; therefore, they did not violate the constraints of Eqs. (12) and (13). For these events, the Tsengwen Reservoir is nearly empty and the Wushanto Reservoir is nearly full before the initiation of empty flushing operations. Thus, the empty flushing operations only consume the inflow of Tsengwen Reservoir during a 2 days period. These water consumption volumes are too insignificant to induce the subsequent water shortage seen in July. The primary reason for the delayed arrival of the first typhoon in late July or early August, by which time the total storage falls below the critical limit of the joint operating rule curves and water rationing is applied. Following the arrival of the typhoons, however, the total reservoir storage exceeds the lower limit and even the upper limit of rule curves, thereby alleviating the water shortage.

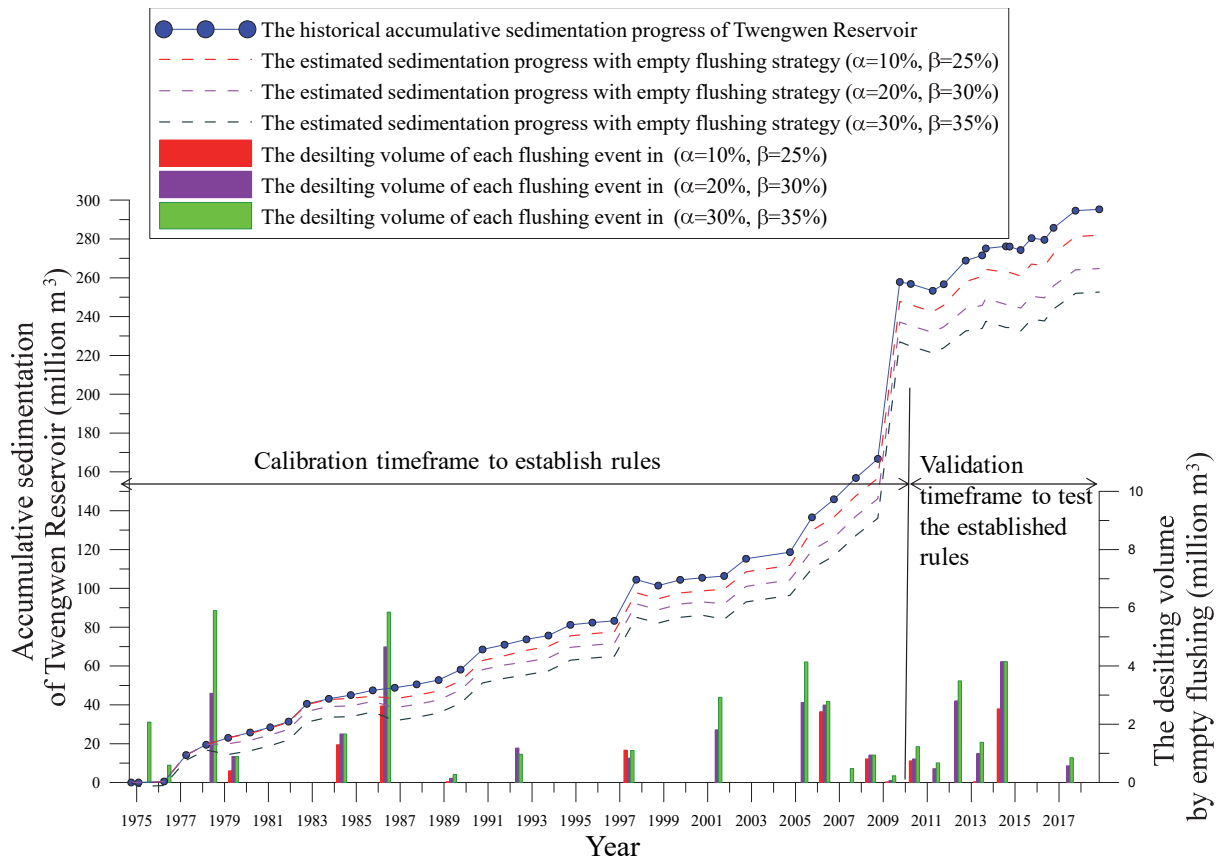



Fig. 10 The sedimentation progress of Tsengwen Reservoir with and without empty flushing

4.5 Validation of the optimal strategies

The optimal strategies in Table 2 are derived according to the records of daily reservoir inflow between 1975 and 2009. In other words, their average performances regarding Eqs. (6), (7) and (8) are boosted and customized against the hydrological conditions during this calibration time period. Following which, the records through the end of 2018 are used to verify the effectiveness of the established strategy. The validation tests the strategy with inflow series outside of the calibration timeframe to check its validity for general conditions. The results indicate that four additional flushing operations could have been conducted, two of which occur in 2010 and 2013 respectively and the others in 2014. The last four rows in Table 3 summarize these events. In addition to the case of 2013 which imposes no impact on water supply, the empty flushing operations in the other years are depicted in Figs. 11 and 12 and discussed as

below:

1. Following the empty flushing in early June of 2010, the monthly water shortage ratio during July is 0.18, which is higher than the 0.12 that would have been the case without empty flushing. The increased shortage ratio is induced by drawdown and empty flushing, which causes the total storage to fall below the critical limit of rule curve earlier in July. Empty flushing thus necessitates a slightly longer water rationing period. Nonetheless, torrential rains in late July elevate the storage to exceed the lower limit, thereby resolving the shortage crisis. The major impact of water shortage during this period is on the second semiannual irrigation operation, which requires large quantities of water during July. One of the mitigation measures have been adopted in field is to postpone the beginning of irrigation schedule no later than August 10. For example, in June of 2004, the total storage in the two reservoirs fell below the critical limit, which delayed the second semiannual irrigation from the originally planned June 6 to July 17 when Typhoon Mindulle invaded and elevated the storage above the upper limit in one day of early July.

2. In 2014, over 40% of the wet season inflow of Tsengwen Reservoir occurred in May and June, which means the front-induced inflow in the early flood season is abundant and only one typhoon invaded Taiwan for the remaining 5 months. The unexpected lack of subsequent floods leads to partial recovery of reservoir storage. The impact is alleviated through water rationing during the wet season to allow carrying out the second semiannual irrigation. For the following drought occurred at the dry season in 2015, it inevitably leads to large scale suspension of the first semiannual irrigation to reduce the agricultural demand to nearly 0, whether empty flushing in the previous year is performed or not. With or without empty flushing, the water originally supplied to the first semiannual irrigation, the volume of which ranges between 0.2~0.3 billion m^3, will be kept to secure public water supply. The annual demand of public and industrial purposes of this system is only 0.147 billion m^3 and

every empty flushing practice consumes water no more than 0.09 billion m³ according to Table 3. The demand magnitude and water transfer mechanism guarantee that the risk of increased shortage induced by empty flushing for this particular situation will be completely offset in reality.

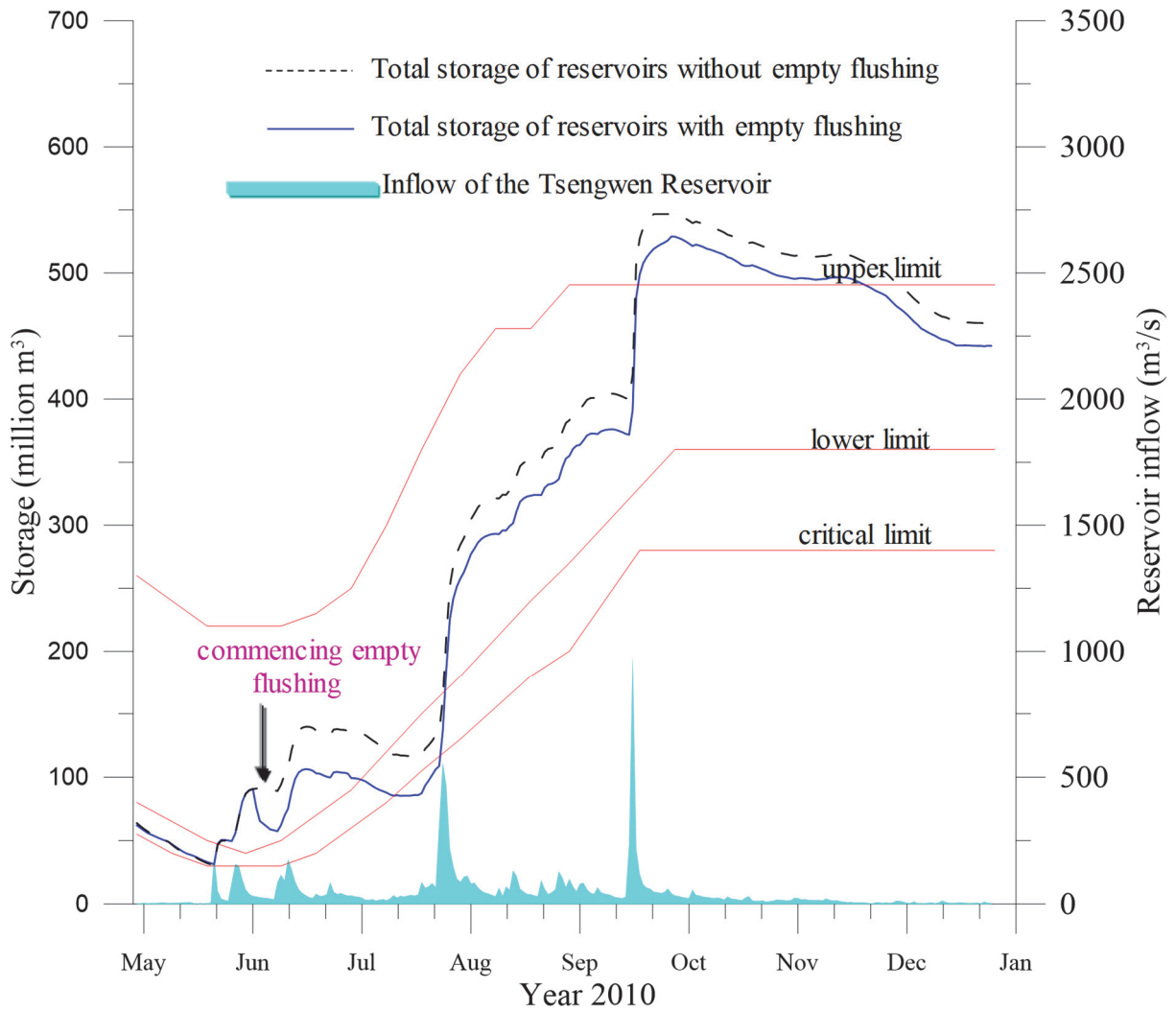



Fig. 11 Reservoir inflow and storage throughout 2010

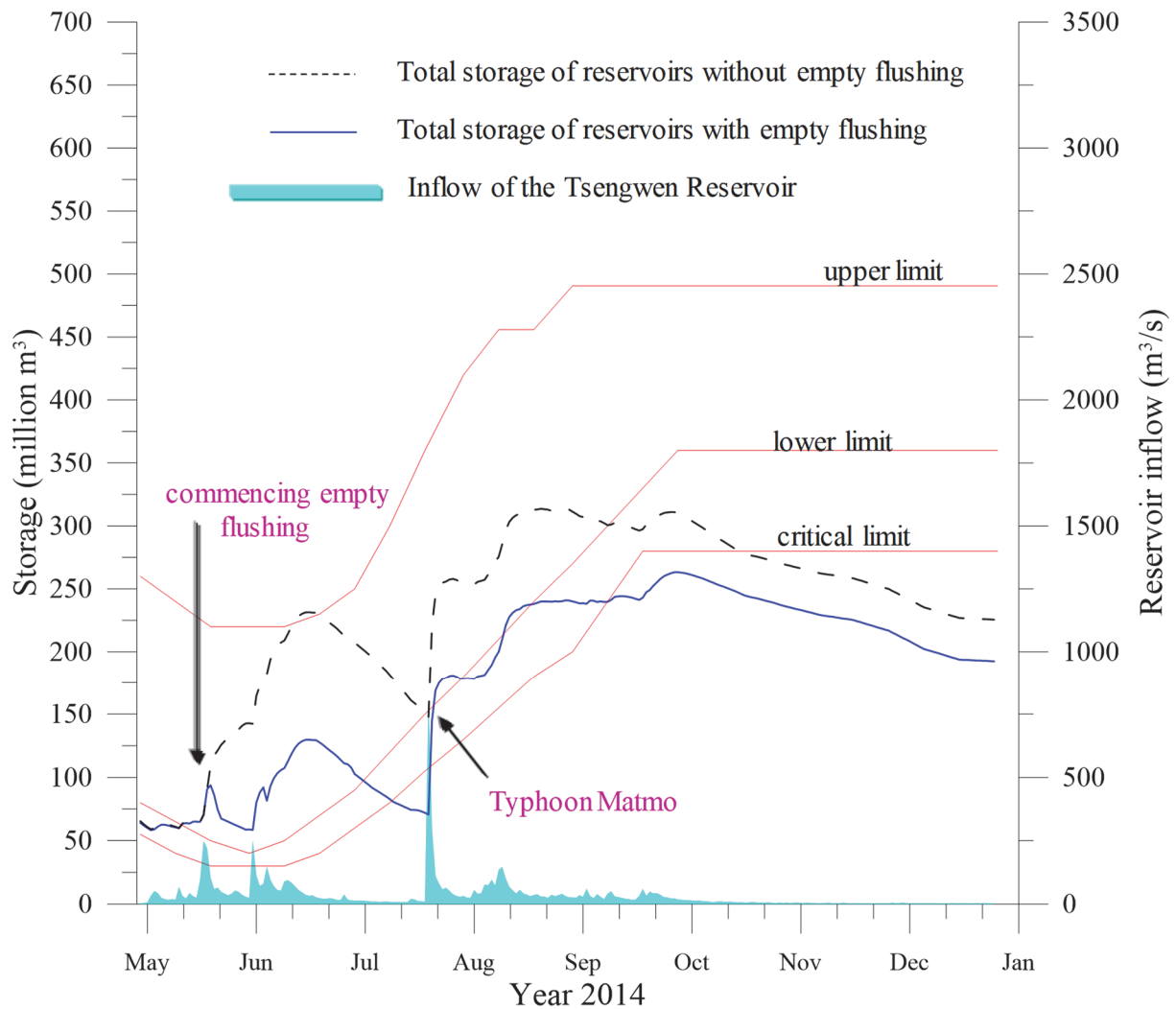



Fig. 12 Reservoir inflow and storage throughout 2014

5. The impacts on downstream environment and potential extensions of the proposed method

In addition to induce incremental water shortage, potential adverse impacts on the downstream environment may appear due to flushing. They originate from the high sediment concentration of flushing release in the absence of a simultaneous downstream flood, which may significantly reduce dissolved oxygen in the river, smother stream benthos, clog gravels thus endangering spawn sites and habitat, impairing river functions such as flood conveyance, navigation or recreation, etc (Morris, 2014). Some measures to minimize these impacts by

carefully determining the timing, duration and frequency of flushing and controlling the releasing discharge and concentration can be found in Morris (2014), Moridi and Yazdi (2017), Espa *et al.*(2019) and Cattanéo *et al.*(2021). ~~To minimize these impacts, Morris (2014) suggests to carefully determining the timing, duration and frequency of empty flushing. The general principle is to limit the volume and duration of the flushed sediments detained on the downstream river bed. This leads to the following measures:~~

~~1. To identify and avoid periods during which stream creatures are sensitive to water quality.~~

~~2. To schedule the empty flushing while natural floods downstream or releases from other reservoirs are available during the same storm to dilute and transport sediments.~~

~~3. To ensure that subsequent high-streamflow, either from tributaries or reservoir releases, is available to clear the accumulated sediments from previous flushing events.~~

~~4. Adopting more frequent, periodical and short period of flushing to attenuate the release concentration in each operation.~~

~~This paper focuses on balancing water supply and empty flushing of sediment through proper joint operation of reservoirs.~~ The theme of this paper, to secure water supply while enhancing desilting, acts similarly as mitigating environmental impacts, since they both need to restrain the effectiveness of empty flushing. ~~The impacts to these two purposes are addressed as below~~ The conjunctions include:

1. Meeting WS1F ~~QCWS1~~ and FS1Q ~~QCFS1~~ suggests the flushing periods to coincide with the first flood of wet season, while subsequent typhoon-induced floods satisfy ~~QCWS2~~ WS2A. These conditions prompt adequate water during and following flushing for dilution and transportation of sediments downstream. ~~These conditions conform to the principles of limiting environmental impacts, since they prompt adequate water during and following flushing for dilution and transportation of sediments downstream.~~

2. The second termination condition in subsection 3.2.4 allows empty flushing until the inflow

recedes below the capacity of PRO. The release during the recession limb of flood inflow with lower concentration and higher WSL of reservoir partially offsets the impact immediately following the empty flushing.

3. The strict requirement on the stability of water supply leads to a higher T^d for the third termination condition, the threshold backup storage to stop an empty flushing operation. In the absence of a flood, this induces an earlier termination and increases the opportunities of re-activation of another flushing operation. This results in more frequent flushing with shorter duration, which is considered as more favorable to mitigate downstream impacts (Morris, 2014; Sumi and Kantoush, 2010; Crosa *et al*., 2010).

~~Some characteristics of the case study area regarding the impact from empty flushing on downstream environment are addressed as below:~~ Some characteristics of the case study area to temper the impact on environment include:

1. The capacity of PRO of the Tsengwen Reservoir when the storage is nearly empty is around 130 m^3/s. This flushing discharge is relatively insignificant comparing to the magnitudes of spillway releases and downstream lateral flow during a moderate flood. ~~The bottom outlet available for empty flushing of the primary reservoir, Twengwen Reservoir, is its permanent river outlet (PRO) with design capacity as 177 m³/s. Its actual capacity when the storage is nearly empty decreases to around 130 m³/s. According to the operating guidelines of Twengwen Reservoir, the minimum operating spillway release is 300 m³/s and a release under 2,250 m³/s is considered as free of inducing downstream flooding damage. It shows that release from empty flushing is relatively insignificant comparing to the magnitudes of spillway releases and downstream lateral flow during a moderate flood.~~

2. ~~The current operators adopt dredging, or more precisely hydrosuction, as the major approach to desilt the Twengwen Reservoir. Several soil dikes were constructed in the river immediately downstream from the dam as temporary depositing area for the dredged~~

slurries. The lump-sum volume of the depositing area which defines the annual dredging capacity is currently 2.8 million m³ and to be expanded to 3.5 million m³ in the future. The artificially deposited sediments as well as the soil dikes are expected to be flushed out by the spillway release during typhoons to allow continuation of hydrosuction in the next year. The required volume from the reservoir release to vacate downstream depositions and soil dikes is estimated as 40 million m³ (900 m³/s times 12 hours) based on field operating experiences. Previous surveys (Water Resources Agency, 2018) showed that these operations have limited impacts on the flood conveyance function as well as the weighted usable area of a major interested benthos specie in the downstream river. It is expected the sediments from empty flushing during the first flood can be partially detained in the depositing area, and then carried downstream along with the dredging depositions by the subsequent flood operation during typhoons in the rest of wet season.

3. The downstream major benthos specie of interest is Sinogastromyzon nantaiensis (Chen *et al.*, 2002), with spawning season from June to September and habitation site within the first downstream reach from the Tsengwen Dam. The most threat for the benthos is the fine suspended or even wash loads from either hydrosuction, flushing or sluicing operations, which may fill up the voids of river bed and destroy its spawning sites. The empty flushing is limited before mid-June to minimize the concurrence periods of the spawning season. The first river reach downstream from the dam has a moderate slope as 0.0036 and short distance as 20.5 km. These prompt transportation of sediments by the typhoon-induced reservoir spillage.

4. The spillway release during typhoon is expected to flush out the artificially deposited sediments as well as the soil dikes in the downstream river reach to allow continuation of hydrosuction. The required volume from the reservoir release to vacate downstream depositions and soil dikes is estimated as 40 million m³ (900 m³/s times 12 hours) based on

field experiences. It is expected the sediments from empty flushing can be partially detained in the depositing area, and then carried downstream along with the dredging depositions by the subsequent reservoir spillage. The impact by empty flushing is thus limited within the already existed deposition area.

5. From Table 6, either the bottom release during empty flushing or the spillage during the rest of the year in almost every identified event exceeds 40 million m^3 to effectively transport downstream depositions. The only two exceptions are the events of 1977 and 2010. To manage these years, the reservoir may need to deliberately release water before the end of wet season to vacate downstream depositions. This will increase the shortage situation in the dry season of next year by 40 million m^3, which is about 10% of the first semiannual irrigation demand. For these two years, this shortage increment can still be managed by regular water saving measures without inducing suspension of irrigation.

Some suggestions for future extension of the current study are provided as below:

1. To incorporate short-term forecasting of reservoir inflow in determining the activation or termination of an empty flushing operation. If the forecast is reliable, a certain amount of storage can be kept in the primary reservoir and pre-emptied shortly before an expected flood. The forecast uncertainty should be incorporated to avoid inducing intolerable water shortage in case the flood does not occur after empting the reservoir.

2. To test the established rules with synthetically generated hydrological series containing more years with unexpected lacks of floods. This would allow a more comprehensive evaluation of the potential risk of water shortage especially under the impact of climate change. To facilitate this extension, the correlation across daily inflows of different sites in a multi-reservoir system should be properly modeled to correctly represent the temporal and spatial stochastic hydrological nature.

3. The case study specifically discusses a system with an upstream online reservoir requiring

empty flushing and a downstream offline reservoir which provides backup water supply. Implementations for other systems with different schematics may require more complex optimization formulations with additional parameters. For example, if an additional reservoir is available upstream from the primary reservoir, its storage could serve to generate artificial flushing discharge. The flushing operation may start from emptying the downstream reservoir, and then drawing down the storage of the upstream reservoir and allowing the drawdown release to scour and pass through the downstream reservoir. The timing to start and terminate the joint flushing operation may be guided by the joint operating rule curves. The joint rule curves can also be included as parameters to be optimized to promote the performance of empty flushing without inducing significant water shortage. Similar study can be found in Chou and Wu (2017).

4. Numerical modeling may be directly integrated into the optimization framework for a more accurate estimation of the desilting volume. The transportation of flushed sediments in the downstream river could also be simulated to more comprehensively evaluate of the impacts of empty flushing on environment and incorporate the threshold concentration as constraints into the optimization problem.

6. Conclusions

This study optimizes the performance of empty flushing of one primary reservoir within a multi-reservoir system. Prior to empty flushing, the total available storage in a system is allocated from the primary reservoir to the others to create favorable initial conditions and prepare backup water to be supplied during empty flushing. The activation and termination conditions of an empty flushing operation are determined according to whether storage in the primary and auxiliary reservoirs satisfies applicable thresholds. Optimization analysis calibrates these storage thresholds to maximize the desilting volume without inducing

intolerable water shortage. The case study of the water resources system of the Tsengwen and Wushanto Reservoirs of southern Taiwan verifies the effectiveness of the derived optimal strategy.

Integrating reservoir desilting considerations with water supply operation creates more facets into the multi-objective water resources management. In addition to irrigation, municipal, industrial and hydropower purposes, the competition of water extends to include sediment flushing, sluicing, vacating previous dredged and deposited sediments, and alleviating their impacts on downstream environment. The high risk of water shortage in the case study area currently dictates the operating objective to solely focus on reliable water supply. This restricts the feasibility of not only empty flushing, but any other operations may cause additional consumption of reservoir storage, and leads to great reliance on hydrosuction to reservoir desilt, degradation of downstream environment and inefficient utilization of water resources. This paper elaborately creates an opportune chance for potential empty flushing under such high-pressure of water supply. If this pressure can be somehow relieved, the practical benefits of the proposed method could be more evident, since all the problems stem from the same core: insufficiency of available water with acceptable quality for all purposes. While the operators are forced to myopically prevent the imminent water shortage risks, reservoir sedimentation also imposes an equivalent and long-term threat to the degeneration of water supply yield. The urgent needs of both desilting and water supply may also endow a new role to the conventional projects of water resources development. In addition to elevating the yield of water supply, it may exploit more water to allow recovery and enhanced desilting of existing reservoirs, thus allowing the entire system to advance toward the goal of sustainability.

Data availability

The data used in this study, including 46 years of daily hydrological series, simulated

water allocation process, as well as hundreds of input and output files of the GWASIM and SRH-2D models, are available from the authors upon requests (chiawenwu1977@gmail.com). The executive file of SRH-2D model and the associated manuals are available on the website of U.S. Bureau of Reclamation.

5 (https://www.usbr.gov/tsc/techreferences/computer%20software/models/srh2d/index.html).

Author contribution

The study was initiated by FNFC, who also got the funds. FNFC and CWW both contribute to the methodological development of simulation and optimization models. CWW

10 carried out the contents of most analysis in the case study. The numerical simulation of SRH 2D was performed by FZL. The manuscript was jointly drafted by CWW and FNFC.

Competing interests

The authors declare that they have no conflict of interest.

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Appendix I. Cases of reservoirs adopting empty flushing in the world

Table 3 Cases of empty flushing

Reservoir	Country	Effective capacity (Mm3)	Major Purpose	Number of flushing days per operation	Reservoir system	Watershed sediment yield (M.ton/year)	Capacity-inflow ratio (CIR)	Annual flushing periods	Backup water supply during flushing	Flushing facilities	Flushing experiences	Literature source
Akung-ten	Taiwan	16.47	FC IR	100 days	S	0.55	0.71	June to September	Trans-basin diversion from an adjacent river	morning glory with capacity of 85 m³/s	Flushing out 5% to 54% of the inflowing sediments during floods between 2009 to 2013	Southern Water Resources Office, 2013
Baira	India	2.40	HP	1 to 2 days	S	0.3 (from siltation after 18 months)	0.001	April to May	Halting hydro-power generation	low–level diversion tunnel with capacity of 44 m3/s	The first operation in Aug of 1983, lasting for 40 hours with discharge of 44 m3/s, flushed out 85% of the deposited sediments. Afterwards the empty flushing is suggested to be annually performed during April to May.	Jaggi and Kashyap, 1984; Atkinson, 1996; Chaudhry and Habib-ur-rehman, 2012
Cachi	Costa Rica	54.0	HP	2 to 3 days	S	0.81	0.016	May (the beginning of wet season)	Halting hydro-power generation	Bottom outlet	On average flushing out 0.25 million m3/year of sediments annually.	Brandt and Swenning, 1999; Jansson and Erlingsson, 2000; Chaudhry and Habib-ur-rehman, 2012;
Dapu	Taiwan	5.29	IR ID	50 days	S	0.40	0.04	May to July	Halting irrigational supply. Industrial demand is supplied by reservoir inflow	Sluiceway with capacity of 325 m3/s	On average flushing out 0.20 million m3/year of sediments annually.	Chang et al, 2003; Water Resources Agency, 2010
Gebi-dem	Switzer-land	9.0	HP	2 to 4 days	S	0.50	0.02	May to June	Halting hydro-power generation	Bottom outlet with flushing discharge of 10 m3/s	Since 1992, the annual volume of flushed sediments is between 0.2 to 0.5 million m3 per year.	Atkinson, 1996; Chaudhry and Habib-ur-rehman, 2012; Meile et al., 2014

HP: hydropower generation, FC: flood control, IR: irrigation, ID: industrial water supply, S: single reservoir system, M: multi-reservoir system, Capacity-inflow ratio: the ratio between the effective capacity and the annual inflow volume of the reservoir;

Table 3 Cases of empty flushing (continued)

Reservoir	Country	Effective capacity (Mm3)	Major Purpose	Number of flushing days per operation	Reservoir system	Watershed sediment yield (M.ton/year)	Capacity-inflow ratio (CIR)	Annual flushing periods	Backup water supply during flushing	Flushing facilities	Flushing experiences	Literature source
Heng-shan	China	13.30	FC IR	10 to 20 days	S	1.18	0.84	June to September	Diverting turbid release to provide irrigational demand.	Bottom outlet with capacity of 17 m³/s at full impounding level and 2 m³/s during empty flushing	The first operation in 1974 lasted for 37 days and flushed out 0.8 million m³ of sediments. The second operation in 1979 lasted for 52 days and flushed out 1.03 million m³ of sediments.	Atkinson, 1996; Chaudhry and Habib-ur-rehman, 2012
Jensan-pei	Taiwan	1.51	IR	53 days	S	0.28	0.80	May to June	Halting water supply	Sluiceway with capacity of 12.2 m³/s	On average flushing out 0.33 million m³/year of sediments annually.	Water Resources Planning Institute, 2010
Mang a-hao	New Zealand	2.39	HP	30 days	M	—	—	May	Halting hydro-power generation	low –level diversion tunnel	During the total duration of one month of flushing in 1969, 0.8 million m³ of sediment has flushed from the reservoir, which equals to the 75% of sediment that had accumulated since 1924	Jowett, 1984; Atkinson, 1996; White, 2001; Chaudhry and Habib-ur-rehman, 2012
Nan-qin	China	10.20	IR FC	4 days every 3–4 years	S	0.53	0.08	The end of the flood season	---	Sluiceway with flushing discharge of 14 m³/s	The first operation in 1984 flushed out all inflow sediments in 1984, along with 0.72 million m3 that had deposited in the earlier years.	Chen and Zhao, 1992; Chaudhry and Habib-ur-rehman, 2012
Santo Domi ngo	Vene-zuela	3.00	HP	3 to 4 days	S	0.20	0.01	May	Halting hydro-power generation	Three bottom outlets with capacity of 13 m³/s	The first operation in May of 1978 lasted for 4 days and flushed out 50~60% of the deposited sediments. Afterwards mechanical excavation was used to disperse the consolidated deposits and empty flushing is again performed for three weeks to fully restore the deposited capacity.	Krumdieck and Chamot, 1979; Atkinson, 1996

HP: hydropower generation, FC: flood control, IR: irrigation, ID: industrial water supply, S: single reservoir system, M: multi-reservoir system,

Capacity-inflow ratio: the ratio between the effective capacity and the annual inflow volume of the reservoir,

Table 3 Cases of empty flushing (continued)

Reservoir	Country	Effective capacity (Mm3)	Major Purpose	Number of flushing days per operation	Reservoir system	Watershed sediment yield (M.ton/year)	Capacity-inflow ratio (CIR)	Annual flushing periods	Backup water supply during flushing	Flushing facilities	Flushing experiences	Literature source
Sefid-Rud	Iran	1760	IR HP	4 months	S	50	0.36	October to February	No requirement for irrigational water supply	Bottom outlets with flushing discharge of 100 m³/s	Empty flushing during non-irrigational periods removes approximately 28.4 million T of sediments per year.	Atkinson, 1996; Taklimy and Tolouie, 2005
Zemo-Afchar	Former USSR	--	HP	1 to 3 days	S	Suspended load 4 Mm³	--	April, May or November	Halting hydro-power generation	Bottom outlets with flushing discharge of 450 m³/s	Implemented from 1939, with full drawdown. Removing about 1.0 million m³ (from 0.5 to 2 million m³) per year	Bruk, 1985; Chaudhry and Habib-ur-rehman, 2012;
Dashidaira	Japan	1.657	HP FC	1 to 2 days	M	0.62	0.00674	June to August	Halting hydro-power generation	Bottom outlets with flushing discharge between 200~300 m³/s	When inflow at the upstream Dashidaira Dam exceeds 300 m³/s at the first time of the year during June to August, a coordinate flushing is performed. The average annual flushed volume between 2001 to 2007 is 0.27 million m³/year	Sumi, 2008; Sumi et al., 2009
Unazuki		12.70				0.96	0.014					
Verbois	Switzerland	12.00	HP	1 to 2 days every 3 years	M	0.33	0.00144	May to June	Halting hydro-power generation	Bottom outlets with flushing discharge of 600 m³/s	Flushing is performed in every 3 years. The volumetric flushed sediments per event is around 0.6 and 1.1 million m³ for Verbois Reservoir and 0.1 and 0.4 million m3 for Genissiat Reservoir according to Sumi (2008)	Sumi, 2008
Genissiat	France	18.00				0.73	0.00467					

HP: hydropower generation, FC: flood control, IR: irrigation, ID: industrial water supply, S: single reservoir system, M: multi-reservoir system,

Capacity-inflow ratio: the ratio between the effective capacity and the annual inflow volume of the reservoir,

Appendix 2 Cases of other reservoirs adopting empty flushing in southern Taiwan

Exact data from flushing in Tsengwen Reservoir does not exist since the reservoir has never been gone through such operations. The operators have constantly maintained the reservoir at high WSL to ensure stable water supply. The only experience for the reservoir drawing nearly to empty was in the beginning of wet seasons in 2004 before the Typhoon Mindulle invaded, during which the reservoir did not release water at all. Fig. 8 includes the data of the reservoir WSL, inflowing discharge and measured sediment concentration in front of the dam in a few hours of the rising periods of Typhoon-Mindulle-flood, during which the WSL had yet been raised beyond El. 190 m. It shows the corresponding value of ψ ranges from 20 to 160, surrounding the value of 60 suggested by Atkinson (1996) for cases with limited-capacity bottom outlets. To prevent overestimating the effectiveness of empty flushing, it is assumed that if a flood raises the WSL of the Tsengwen Reservoir to exceed 185 El. m, then the flushed sediment volume from the PRO is set to be 0, otherwise the ψ is set as 60.

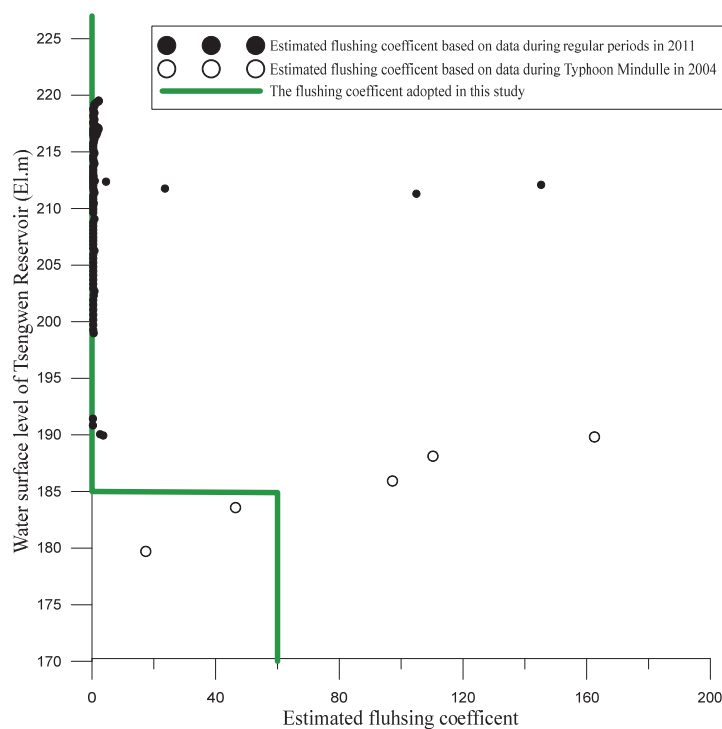



Fig. 13 Relationship between the flushing coefficient and WSL of Tsengwen Reservoir

It should be noted that similar setting of ψ has been applied and validated in other reservoirs in adjacent basins of southern Taiwan (SWRO, 2015). One of which is the Akungten reservoir, which annually undergoes empty flushing between 1st May to 10th September. The estimated volumes of flushed sediments during several floods appears to be in the same order to the measurements as shown by Table 4. Substituting the above setting of ψ and a full-capacity discharge of PRO of Tswengwen Reservoir into Eq. (1) will lead to a volumetric sediment concentration as 39,928 ppm. Another adjacent Jensanpei Reservoir in southern Taiwan recorded the volumetric sediment concentration from its historical empty flushing operations ranging between 54,014 to 446,182 ppm, and averaged at 105,478 ppm (Water Resources Planning Institute, 2010). This shows the conservativeness of the adopted setting of ψ in the current study.

Table 4 The operating records of Akungten Reservoir during its empty flushing periods (SWRO, 2015)

Typhoon event	Duration	Total rainfall (mm)	Peak inflow (m³/s)	Total desilting mass (thousand ton)	
				Measurement	Estimation
Morakot	2009/08/06~08/11	836.5	303.2	67.0	51.0
Fanapi	2010/09/18~09/21	589.0	673.9	16.0	20.6
Nanmadol	2011/08/27~08/31	353.0	95.4	32.0	41.4
Torrential Rain	2012/06/09~06/16	593.0	248.8	48.0	47.4
Talim	2012/06/18~06/25	348.0	164.7	14.0	5.2
Trami	2013/08/21~08/24	225.0	127.0	6.0	14.3
Kong-Rey	2013/08/29~09/03	546.5	216.7	3.0	15.9
			Average	26.6	28.0

Appendix 3 Numerical simulation of the empty flushing process

Flow in reservoir during empty flushing is relatively shallow and the effect of vertical motions is negligible. The 3D Navier-Stokes equations coupled with sediment transport formulas may be vertically averaged to obtain a set of depth averaged 2D equations. A

numerical model solving these equations, SRH-2D, is applied to validate the releasing sediment discharge under the condition of empty flushing. An extensive list of SRH-2D calibrations, verifications and applications had been carried out (Lai, 2008, 2010). The model can be downloaded from the website of the U.S. Bureau of Reclamation.

The flushing events in 1984, 1986, 1997 and 2006 listed in Table 6 are selected for numerical investigation. The Dirichlet boundary conditions are given at upstream and downstream simulation grids. Sediment transport equation of Engelund-Hansen (1967) is adopted to simulate sediment discharge. The particle size of sediment deposited on the reservoir bottom is given from field survey. Fig. 14(a) shows the simulated bottom variation of the event in 2006. It shows that the erosion mechanism dominates the reservoir bed changing due to low water level. A flushing channel is created from the inlet of sluiceway toward the midstream of the reservoir. The flushing process, including discharges of reservoir inflow and release, storage, sediment concentration of release and accumulative desilting volume during this event is also depicted in Fig. 14(b). The entire process consists of two stages of drawdown, empty and refill phases regarding reservoir storage. The release concentration peaks around 50,000 mg/l while the reservoir is empty and the flushing channel is formed. The release with lower concentration during the two refill phases also facilitates alleviating the impacts on downstream environment. Figure 14(c) reveals that the simulated desilting volumes by SRH-2D agree well with the estimated values from Eq. (1). This validates the acceptability of the adopted empirical formula.

(a) Reservoir bed erosion and deposition in the 2006 event

(c) Comparison of total desilting volume from numerical simulation and empirical formula

(b) Reservoir inflow, release discharges, storage, sediment concentration of release, and accumulative desilting volume of the 2006 event

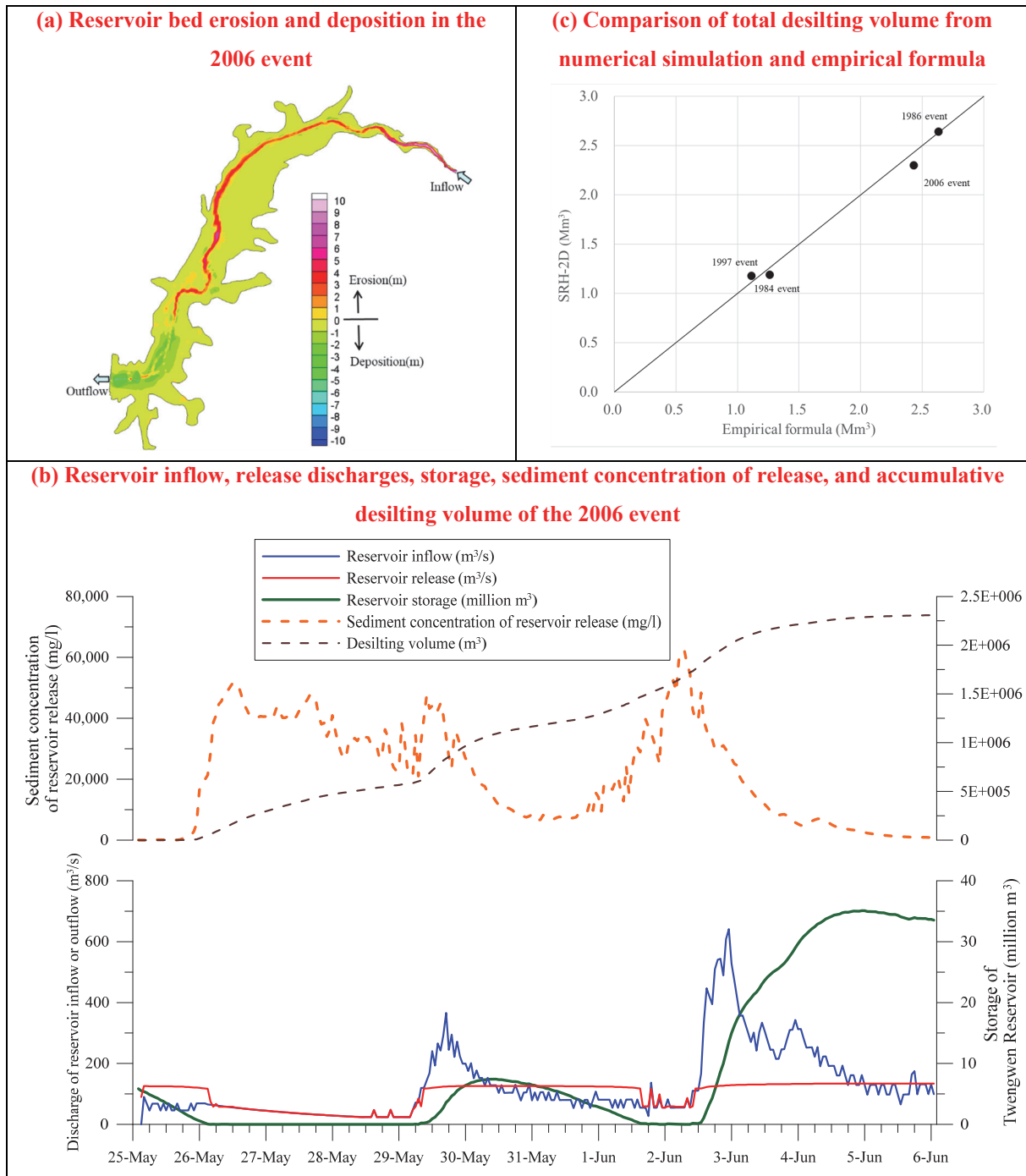
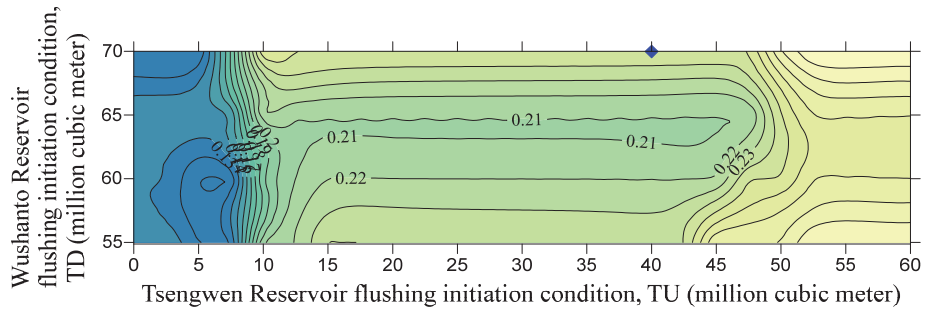
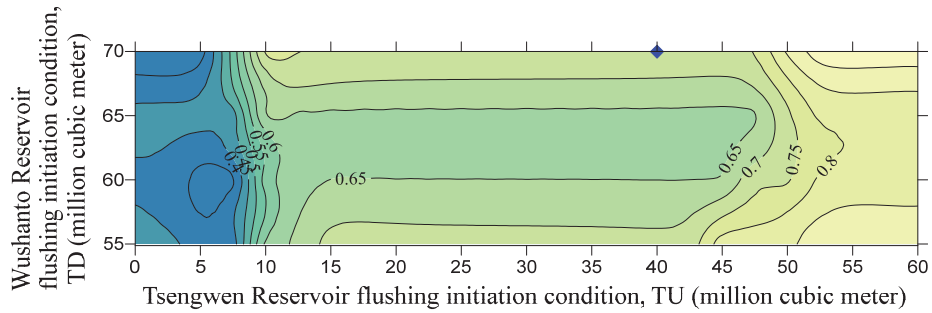
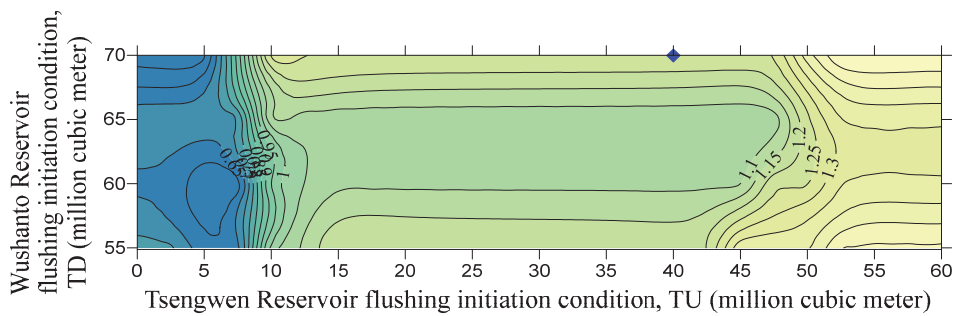
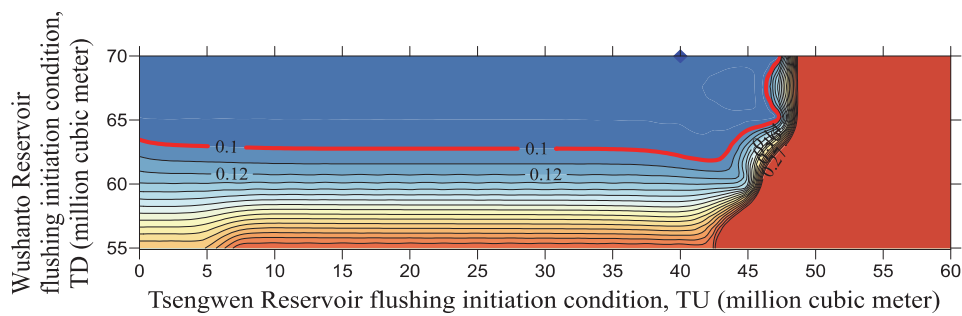



Fig. 14 Simulation results of the SRH-2D

Appendix 4 Sensitivity analysis of the flushing coefficient in the optimal scenario

The major uncertainty of the proposed method is the use of the empirical formula Eq. (1) to estimate the volume of flushed sediments. Due to the lack of field data, the flushing coefficient ψ is directly assigned as 60, a most common and conservative value found in

literatures (Atkinson, 1996). To investigate how this uncertainty affects the optimization procedure, sensitivity analysis is performed by applying another two values of ψ as 180 and 300, which are originated from IRTCES (1985). It turns out that the re-calibrated parameters by different values of ψ remain unchanged. To demonstrate this characteristic, sensitivity simulation trials are run by expanding the storage thresholds to activate flushing, T^U and T^D, of the 15th ten-day from the optimal solution, with a discrete interval of 1 million m^3. Fig. 15 depicts the contour maps of desilting volume and maximum monthly shortage ratio induced by empty flushing with axis as T^U and T^D for different values of ψ. It reveals that using a different ψ value only leads to a linearly-varied value of the objective function, while the optimal solution is dictated by the water shortage constraint and free of ψ. This validates the ability of the proposed approach to produce strategies which maximize the potential desilting performance under acceptable water shortage scenarios.

(a) Contour of the desilting volume for different T^U and T^D with $\psi = 60$

(b) Contour of the desilting volume for different T^U and T^D with $\psi = 180$

(c) Contour of the desilting volume for different T^U and T^D with $\psi = 300$

(d) Contour of the maximum monthly shortage ratio from June to July for different T^U and T^D with $\psi = 60$, 180

or 300

10 **Fig. 15 Results of sensitivity analysis of flushing coefficient and threshold storages for**

the 15th ten-day