1 Determination of vadose and saturated-zone nitrate lag times using long-

² term groundwater monitoring data and statistical machine learning

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11 Abstract. In this study, we explored the use of statistical machine learning and long-term groundwater nitrate monitoring data to 12 estimate vadose-zone and saturated-zone lag times in an irrigated alluvial agricultural setting. Unlike most previous statistical machine learning studies that sought to predict groundwater nitrate concentrations within aquifers, the focus of this study was to 13 leverage available groundwater nitrate concentrations and other environmental variables to determine mean regional vertical 14 15 velocities (transport rates) of water and solutes in the vadose zone and saturated zone (3.50 m/year and 3.75 m/year, respectively). The statistical machine learning results are consistent with two primary recharge processes in this Western Nebraska aquifer: (1) 16 diffuse recharge from irrigation and precipitation across the landscape, and (2) focused recharge from leaking irrigation conveyance 17 18 canals. The vadose-zone mean velocity yielded a mean recharge rate (0.46 m/year) consistent with previous estimates from 19 groundwater age-dating in shallow wells (0.38 m/year). The saturated zone mean velocity yielded a recharge rate (1.31 m/year) 20 that was more consistent with focused recharge from leaky irrigation canals, as indicated by previous results of groundwater age-21 dating in intermediate-depth wells (1.22 m/year). Collectively, the statistical machine-learning model results are consistent with 22 previous observations of relatively high-water fluxes and short transit times for water and nitrate in the primarily oxic aquifer. 23 Partial dependence plots from the model indicate a sharp threshold where high groundwater nitrate concentrations are mostly 24 associated with total travel times of seven years or less, possibly reflecting some combination of recent management practices and 25 a tendency for nitrate concentrations to be higher in diffuse infiltration recharge than in canal leakage water. Limitations to the machine learning approach include non-uniqueness of different transport rate combinations when comparing model performance 26 27 and highlight the need to corroborate statistical model results with a robust conceptual model and complementary information such 28 as groundwater age.

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35 1 Introduction

36 Nitrate is a common contaminant of groundwater and surface water that can affect drinking water quality and ecosystem 37 health. Predicting responses of aquatic resources to changes in nitrate loading can be complicated by uncertainties related to rates 38 and pathways of nitrate transport from sources to receptors. Lag times for movement of non-point source nitrate contamination 39 through the subsurface are widely recognized (Böhlke, 2002; Meals et al., 2010; Puckett et al., 2011; Van Meter and Basu, 2017) 40 but difficult to measure. Vadose (unsaturated zone) and groundwater (saturated zone) lag times are of critical importance for 41 monitoring, regulating, and managing the transport of contaminants in groundwater. However, transport time-scales are often 42 generalized due to coarse spatial and temporal resolution in data available for groundwater systems impacted by agricultural activities (Gilmore et al., 2016; Green et al., 2018; Puckett et al., 2011), resulting in a simplified groundwater management 43 approach. Regulators and stakeholders in agricultural landscapes are increasingly in need of more precise and local lag time 44 45 information to better evaluate and apply regulations and best management practices for the reduction of groundwater nitrate 46 concentrations (e.g., Eberts et al., 2013).

47 Field-based studies of lag times (time to move through both vadose zone and aquifer) commonly use vadose-zone 48 sampling and/or expensive groundwater age-dating techniques to estimate nitrate transport rates moving into and through aquifers 49 (Böhlke et al., 2002, 2007; Böhlke and Denver, 1995; Browne and Guldan, 2005; Kennedy et al., 2009; McMahon et al., 2006; 50 Morgenstern et al., 2015; Turkeltaub et al., 2016; Wells et al., 2018). Detailed process-based modelling studies focused on lag 51 times require complex numerical models combined with spatially intensive and/or costly hydrogeological observations 52 (Ilampooranan et al., 2019; Rossman et al., 2014; Russoniello et al., 2016). Thus, efficient but locally-applicable modelling 53 approaches are needed (Green et al., 2018; Liao et al., 2012; Van Meter and Basu, 2015). In this study, an alternative data-driven 54 approach (Random Forest Regression) leverages existing long-term groundwater nitrate concentration (referred to as [NO₃⁻] 55 hereafter) data and easily accessible environmental data to estimate vadose and saturated-zone vertical velocities (transport rates) 56 for the determination of subsurface lag times.

57 Statistical machine learning methods, including Random Forest, have been used successfully for modelling [NO₃⁻] 58 distribution in aquifers (Anning et al., 2012; Juntakut et al., 2019; Knoll et al., 2020; Nolan et al., 2014; Ouedraogo et al., 2017; 59 Rodriguez-Galiano et al., 2014; Rahmati et al., 2019; Vanclooster et al., 2020; Wheeler et al., 2015), but there has not been robust 60 analysis of model capabilities for estimating vadose and/or saturated-zone lag times. Proxies for lag time, such as well screen 61 depth, have been used as predictors in Random Forest models (Nolan et al., 2014; Wheeler et al., 2015). Decadal lag times have been suggested from using time-averaged nitrogen inputs as predictors (e.g., 1978-1990 inputs vs 1992-2006 inputs) and by 62 63 comparing their relative importance in the model (Wheeler et al., 2015). Application of similar machine learning methods 64 suggested groundwater age could be used as a predictor to improve model performance (Ransom et al., 2017). Hybrid models, 65 using both mechanistic models and machine learning, have also sought to integrate vertical transport model parameters and outputs 66 to evaluate nitrate-related predictors, including vadose-zone travel times (Nolan et al., 2018).

The objective of this study is to test a data-driven approach for estimating vadose and saturated-zone transport rates and lag times for an intensively monitored alluvial aquifer in western Nebraska (Böhlke et al., 2007; Verstraeten et al., 2001a, 2001b; Wells et al., 2018). Results are compared to the hydrogeologic, mechanistic understanding from previous groundwater studies to determine strengths and weaknesses of the approach as (1) a stand-alone technique, or (2) as an exploratory analysis to guide or complement more complex physical-based models or intensive hydrogeologic field investigations.

72 2 Methods

73 2.1 Site Description

74 The Dutch Flats study area is in the western Nebraska counties of Scotts Bluff and Sioux (Fig. 1). The North Platte River 75 delivers large quantities of water for crop irrigation in this region and runs along the southern portion of this study area. Irrigation 76 water is diverted from the North Platte River into three major canals (Mitchell-Gering, Tri-State, and Interstate Canals) that feed a 77 network of minor canals. Several previous Dutch Flats area studies have investigated groundwater characteristics and provided 78 thorough site descriptions of the semi-arid region (Babcock et al., 1951; Böhlke et al., 2007; Verstraeten et al., 2001a, 2001b; 79 Wells et al., 2018). The Dutch Flats area overlies an alluvial aquifer characterized by unconsolidated deposits of predominantly 80 sand and gravel, with the aquifer base largely consisting of consolidated deposits of the Brule, Chadron, or Lance Formation 81 (Verstraeten et al., 1995) (Fig. 2). Irrigation water not derived from the North Platte River is typically pumped from the alluvial 82 aquifer, or water-bearing units of the Brule Formation.

The total area of the Dutch Flats study area is roughly 540 km², of which approximately 290 km² (53.5%) is agricultural land (cultivated crops and pasture). Most agricultural land is concentrated south of the Interstate Canal (Homer et al., 2015). Due to the combination of intense agriculture and low annual precipitation, producers in Dutch Flats rely on a network of irrigation canals to supply water to the region. From 1908 to 2016, mean precipitation of 390 mm was measured at the nearby Western Regional Airport in Scottsbluff, NE (NOAA, 2017).

88 While some groundwater is withdrawn for irrigation, and some irrigated acres in the study area are classified as 89 commingled (groundwater and surface water source), Scotts Bluff County irrigation is mostly from surface water sources. 90 Estimates determined every five years suggest surface water provided between 76.8% to 98.6% of the total water withdrawals from 91 1985 to 2015, or about 92% on average (Dieter et al., 2018). Canals transport water from the North Platte River to fields throughout 92 the study area, most of which are downgradient (south) of the Interstate Canal. Mitchell-Gering, Tri-State, and Interstate Canals 93 are the major canals in Dutch Flats, with the latter holding the largest water right of 44.5 m³/s (NEDNR, 2009). Leakage from 94 these canals provides a source of artificial groundwater recharge. Previous studies estimate the leakage potential of canals in the 95 region results in as much as 40% to 50% of canal water being lost during conveyance (Ball et al., 2006; Harvey and Sibray, 2001; 96 Hobza and Andersen, 2010; Luckey and Cannia, 2006). Leakage estimates from a downstream section of the Interstate Canal 97 (extending to the east of the study area; Hobza and Andersen (2010)) suggest fluxes ranging from 0.08 to 0.7 m day⁻¹ through the 98 canal bed. Assuming leakage of 0.39 m day⁻¹ over the Interstate Canal bed area (16.8 m width x 55.5 km length) within Dutch Flats yields 4.1 x 10⁵ m³ day⁻¹ of leakage. Applied over an on-average 151-day operation period (USBR, 2018), leakage from 99 Interstate Canal alone could approach 6.1 x 107 m³ annually, or about 29% of the annual volume of precipitation in the Dutch Flats 100 101 area.

102 A 1990s study investigated both spatial and temporal influences from canals in the Dutch Flats area (Verstraeten et al., 2001a, 2001b), with results later synthesized by Böhlke et al. (2007). Canals were found to dilute groundwater $[NO_3^-]$ locally with 103 104 low-[NO₃⁻] (e.g., [NO₃⁻] < 0.06 mg N L⁻¹ in 1997) surface water during irrigation season. $^{3}H/^{3}He$ age-dating was used to determine 105 apparent groundwater ages and recharge rates. It was noted that wells near canals displayed evidence of high recharge rates 106 influenced by local canal leakage. Data from wells far from the canals indicated that shallow groundwater was more likely 107 influenced by local irrigation practices (i.e., furrows in fields), while deeper groundwater was impacted by both localized irrigation 108 and canal leakage (Böhlke et al., 2007). Shallow groundwater in the Dutch Flats area has hydrogen and oxygen stable isotopic 109 compositions consistent with surface water sources (i.e., North Platte River and associated canals), indicating that most 110 groundwater intercepted by the monitoring well network has been affected by surface-water irrigation recharge (Böhlke et al., 111 2007; Cherry et al., 2020).

112 The Dutch Flats area is within the North Platte Natural Resources District (NPNRD), one of 23 groundwater management 113 districts in Nebraska tasked with, among other functions, improving water quality and quantity. The NPNRD has a large monitoring 114 well network consisting of 797 wells, 327 of which are nested. Nested well clusters are drilled and constructed such that screen 115 intervals represent (1) "shallow" groundwater intersecting the water table (length of screened interval = 6.1 m), (2) "intermediate" 116 groundwater from mid-aquifer depths (length of screened interval = 1.5 m), and "deep" groundwater near the base of the unconfined 117 aquifer (length of screened interval = 1.5 m). Depending on well location within the Dutch Flats area, depths of the water table and 118 base of aquifer are highly variable, such that shallow, intermediate, and deep wells can have overlapping ranges of depths below 119 land surface (Fig. 2).

120 Influenced by both regulatory and economic incentives, the Dutch Flats area has undergone a notable shift in irrigation 121 practices in the last two decades. From 1999 to 2017, center pivot irrigated area has increased by approximately 270%, from 122 roughly 3,830 hectares to 14,253 hectares, or from 13% to 49% of the total agricultural land area, respectively. Most of this shift 123 in technology has occurred on fields previously under furrow irrigation. Conventional furrow irrigation has an estimated potential 124 application efficiency ("measure of the fraction of the total volume of water delivered to the farm or field to that which is stored 125 in the root zone to meet the crop evapotranspiration needs," per Irmak et al. (2011)) of 45% to 65%, compared to center pivot 126 sprinklers at 75% to 85% (Irmak et al., 2011). Based on improved irrigation efficiency (between 10-40%), average precipitation 127 throughout growing season (29.5 cm for 15 April to 13 October (Yonts, 2002)), and average water requirements for corn (69.2 128 cm (Yonts, 2002)), converting furrow irrigated fields to center pivot over the aforementioned 14,253 hectares could represent a 129 difference of $1 \times 10^7 \text{ m}^3$ to $6 \times 10^7 \text{ m}^3$ in water applied. Those (roughly approximated) differences in water volumes are equivalent 130 to 6% to 28% of average annual precipitation applied over the Dutch Flats area, suggesting the change in irrigation practice does 131 have potential to alter the water balance in the area.

132 The hypothesis of lower recharge due to changes in irrigation technology was investigated by Wells et al. (2018) by 133 comparing samples collected in 1998 and 2016. Sample sites were selected based on a well's proximity to fields that observed a 134 conversion in irrigation practices (i.e., furrow irrigation to center pivot) between the two collection periods. While mean recharge 135 rate was not significantly different, a lower recharge rate was indicated by data from 88% of the wells. Long-term Dutch Flats 136 [NO₃] trends were also assessed in the study, suggesting decreasing trends (though statistically insignificant) from 1998 to 2016 throughout the Dutch Flats area, and nitrogen isotopes of nitrate indicated little change in biogeochemical processes. For additional 137 138 background, Wells et al., (2018) provides a more in-depth analysis of recent $[NO_3^-]$ trends in this region (see also, Fig. S1A in the 139 online Supplemental Material, which shows the nitrate data used in the present study).

140 As in other agricultural areas, nitrate in Dutch Flats groundwater is dependent on nitrogen loading at the land surface, rate 141 of leaching below crop root zones, rate of nitrate transport through the vadose and saturated zones, dilution from focused recharge 142 in the vicinity of canals, rate of discharge from the aquifer (whether from pumping or discharge to surface water bodies), and rates 143 of nitrate reduction (primarily denitrification) in the aquifer. Based on nitrogen and oxygen isotopes in nitrate and redox conditions 144 observed in previous studies, denitrification likely has a relatively minor or localized influence on groundwater nitrate in the Dutch 145 Flats area (Wells et al., 2018). Evidence of denitrification (from dissolved gases and isotopes (Böhlke et al., 2007, Wells et al. 146 2018)) was mostly limited to some of the deepest wells near the bottom of the aquifer. Leakage of low-nitrate water in the major 147 canals causes nitrate dilution in the groundwater (i.e., relatively little nitrate addition, at least from the upgradient canals). 148 Additional isotope data might be useful for documenting temporal shifts in recharge sources, or irrigation return flows to the river; 149 however, it is difficult to know exactly the location or size of the contributing area for each well, especially the deeper ones.

150 Other long-term changes to the landscape were evaluated by Wells et al. (2018) and included statistically significant 151 reductions in mean fertilizer application rates (1987–1999 vs. 2000–2012) and volume of water diverted into the Interstate Canal 152 (1983–1999 vs. 2000–2016), while a significant increase in area of planted corn occurred (1983–1999 vs. 2000–2016).

153 Precipitation was also evaluated, and though the mean has decreased over a similar time period, the trend was not statistically

154 significant.

155 2.2 Statistical Machine Learning Modelling Framework

Statistical machine learning uses algorithms to assess and identify complex relationships between variables. Learned relations can be used to uncover nonlinear trends in data that might otherwise be overshadowed when using simple regression techniques (Hastie et al., 2009). In this study we used Random Forest Regression to evaluate site-specific explanatory variables (e.g., precipitation, vadose-zone thickness, depth to bottom of screen, etc.) that may impact the response variable, groundwater [NO₃⁻]. Additionally, as described in detail in Section 2.4, we estimated a range of total travel times (from land surface to the point of sampling) at each of the wells by varying vadose and saturated-zone transport rates. The relative importance of total travel time as a predictor variable was ultimately used to identify an optimal travel time and model.

163 2.3 Variables and Project Setup

Data from 15 predictors were collected and analysed (Table 1). Spatial variables were manipulated using ArcGIS 10.4. 164 165 The $[NO_3]$ dataset for the entire NPNRD had 10,676 observations from 1979 to 2014, and was downloaded from the Quality-166 Assessed Agrichemical Contaminant Database for Nebraska Groundwater (University of Nebraska-Lincoln, 2016). We used data 167 encompassed by the Dutch Flats model area $(2,829 [NO_3])$ observations from 214 wells). In order to have an accurate vadose-zone 168 thickness, only wells with a corresponding depth to groundwater record, of which the most recent record was used, were selected (2,651 observations from 172 wells). Over this period, several wells were sampled much more frequently than others (e.g., monthly 169 170 sampling, over a short period of record), especially during a U.S. Geological Survey (USGS) National Water-Quality Assessment (NAWOA) study from 1995 to 1999. To prevent those wells from dominating the training and testing of the model, annual median 171 172 $[NO_3^-]$ was calculated for each well and used in the dataset. The dataset was further manipulated such that each median $[NO_3^-]$ 173 observation had 15 complementary predictors (Table 1). The selected predictor variables capture drivers of long-term $[NO_3]$ and 174 [NO₃⁻] lags. After incorporating all data, including limited records of dissolved oxygen (DO), the final dataset included 1,049 175 [NO₃⁻] observations from 162 wells sampled between 1993 and 2013 (Figure S1A). Additional details of the data selection, sources, and manipulations may be found in the Supplemental Material. 176

Predictors were divided into two categories: static and dynamic (Table 1). Static predictors are those that either do not change over the period of record, or annual records were limited. DO, for example, could potentially experience slight annual variations, but data were not available to assign each nitrate sample a unique DO value. Instead, observations for each well were assigned the average DO value observed from the well. This approximation was considered reasonable because nitrate isotopic composition and DO data collected in the 1990s and by Wells et al. (2018) did not indicate any major changes to biogeochemical processes over nearly two decades. Total travel time (from ground surface to the point of sampling) was strictly considered a static predictor in this study and was used to link the nitrate-sampling year to a dynamic predictor value.

Dynamic predictors were defined in this study as data that changed temporally over the study period. Therefore, each annual median [NO₃⁻] was assigned a lagged dynamic value to represent the difference between the time of a particular surface activity (e.g., timing of a particular irrigation practice) and when groundwater sampling occurred. Dynamic predictors were available from 1946 to 2013 and included annual precipitation, Interstate Canal discharge, area under center pivot sprinklers, and area of planted corn (Fig. 3). Dynamic predictors were included to assess their ability to optimize Random Forest groundwater modelling and determine an appropriate lag time. Lag times were based on the vertical travel distance through both the vadose and 190 saturated zones (see Section 2.4). Area of planted corn was included as a proxy for fertilizer data, which were unavailable prior to 191 1987. However, analysis suggests there has been a 17% reduction (comparing the means of 1987-1999 to 2000-2012) in fertilizer 192 application rates per planted hectare, while area of planted corn has increased 16% (comparing the means of 1983-1999 to 2000-193 2016) in recent decades (Wells et al., 2018). This trend may be attributed to improved fertilizer management by agricultural producers. There was a likely trade-off in using this proxy; we were able to extend the period of record back to 1946, allowing for 194 195 analysis of a wider range of lag times in the model, but might have sacrificed some accuracy in recent decades when nitrogen 196 management may have improved. Lastly, vadose and saturated-zone transport rates were assumed to be constant over time (Wells 197 et al., 2018).

198 2.4 Vadose and Saturated-zone Transport Rate Analysis

199Ranges of vertical velocities (transport rates) through the Dutch Flats vadose zone and saturated zone were estimated200from ${}^{3}H/{}^{3}He$ age-dating derived recharge rates. The vertical velocities were determined from results published for samples collected201in 1998 (Böhlke et al., 2007, Verstraeten et al., 2001a) and 2016 (Wells et al., 2018) as

$$202 \quad V = \frac{R}{\theta},\tag{1}$$

203 where R is the upper and lower bound of recharge rates (m/yr), and θ is the mobile water content in the vadose zone or porosity in 204 the saturated zone. The ${}^{3}H/{}^{3}He$ data were used in this study solely for constraining the range of potential transport rates to evaluate 205 in the vadose and saturated zones, and as a base comparison to model results. The age-data, however, were not used by the model 206 itself when seeking to identify an optimum transport rate combination. Throughout the text, unsaturated (vadose)-zone vertical 207 transport rates will be abbreviated as V_u , while saturated-zone vertical transport rates will be V_s . In the vadose zone, θ was assigned 208 a constant value of 0.13, which was calibrated previously using a vertical transport model for the Dutch Flats area (Liao et al., 209 2012). In the saturated zone, θ was assigned a constant value of 0.35, equal to the value assumed previously for recharge 210 calculations (Böhlke et al., 2007). Vadose and saturated-zone travel times (τ) then were calculated using Equation 2:

211 $\tau = \frac{z}{v}$,

212 where τ is either vadose zone (τ_u) or saturated zone (τ_s) travel time in years, and z is the vadose-zone thickness (z_u) or distance 213 from the water table to well mid-screen (z_s) in meters.

(2)

214 Though Equations 1 and 2 do not explicitly consider horizontal groundwater flow, they are approximately consistent with 215 the distribution of groundwater ages (travel times from recharge), which increase with depth below the water table. Whereas 216 groundwater ages commonly increase exponentially with depth in idealized surficial aquifers with relatively uniform thickness and 217 distributed recharge (Cook and Böhlke, 2000), our linear approximation is based on several local observations, including (1) the 218 linear approximation is similar to the exponential approximation in the upper parts of idealized aquifers, (2) linear age gradients 219 may be appropriate in idealized wedge-shaped flow systems, as in some segments of the aquifer section (Figure 2), (3) focused 220 recharge under irrigation canals and distribution channels can cause distortion of vertical groundwater age gradients in 221 downgradient parts of the flow system, and (4) roughly linear age gradients were obtained from groundwater dating in the region, 222 though with substantial local variability (Böhlke et al., 2007). Discrete transport rates and travel times calculated from Equations 223 1 and 2 should be considered "apparent" rates and travel times, similar to apparent groundwater ages, which are based on imperfect 224 tracers and may be affected by dispersion and mixing. Nonetheless, the saturated open intervals of the monitoring wells used for 225 this study (< 6.1 m for shallow wells; 1.5 m for intermediate and deep wells) generally were short compared with the aquifer 226 thickness, such that age distributions within individual samples were relatively restricted in comparison to those of the whole 227 aquifer or of wells with long screened intervals. In addition, it is emphasized that the assumed mobile water content of 0.13 is a

- calibrated parameter derived previously through inverse modelling and, as suggested by Liao et al. (2012), may have large uncertainties due to the varying site-specific characteristics known to exist from one well to the next.
- 230 Because of the influence of canal leakage on both intermediate and deep wells (Böhlke et al., 2007), only recharge rates 231 from shallow wells were used to estimate initial values and permissible ranges of vadose-zone travel times. The mean ($\bar{x} = 0.38$ 232 m/yr) and standard deviation ($\sigma = \pm 0.23$ m/yr) of all the 1998 (n = 7) and 2016 (n = 2) shallow recharge rates were calculated. 233 Using $\bar{x} \pm 1\sigma$, a range of recharge rates from 0.15 to 0.61 m/yr (i.e., rates that varied by a factor of four) were converted to transport 234 rates (V_u) using Equation 1. Calculated transport rates resulted in 1.15 to 4.69 m/yr as the range of vadose-zone transport rates. 235 Expanding the upper and lower bounds, a minimum vadose-zone transport rate of 1.0 m/yr and maximum of 4.75 m/yr was applied. 236 Vertical transport rates in the vadose zone were increased by increments of 0.25 m/yr from 1.0 to 4.75 m/yr, resulting in 16 possible 237 vadose-zone transport rates to evaluate in the Random Forest model.
- 238 Mean ($\bar{x} = 0.84$ m/yr) and standard deviation ($\sigma = \pm 0.73$ m/yr) of all shallow, intermediate, and deep well recharge rates 239 were included in identifying a range of saturated-zone recharge rates from 0.10 to 1.57 m/yr. A total of 35 and 8 recharge rates 240 were used from the Böhlke et al. (2007) and Wells et al. (2018) studies, respectively. Equation 1 was used to calculate saturated-241 zone transport rates (V_s) of 0.28 and 4.49 m/yr. Saturated-zone transport rates were increased by increments of 0.25 m/yr, from 242 0.25 to 4.5 m/yr, resulting in 18 unique saturated-zone transport rates to evaluate in the Random Forest model. The range of 243 transport rates suggested by groundwater age-dating was large (more than an order of magnitude) and are considered to include 244 rates likely to be expected in a variety of field settings. Presumably, similar model constraints and results could have been obtained 245 without the prior age data and with some relatively conservative estimates.
- Travel times τ_u and τ_s were calculated for each well based on z_u and z_s , respectively. For every possible combination of vadose and saturated-zone transport rates, a unique total travel time, τ_t , was calculated for each well based on the vadose and saturated-zone dimensions of that particular well.

249 $\tau_t = \tau_u + \tau_s,$

(3)

- The total travel times from Equation 3 were used to lag dynamic predictors relative to each nitrate sample date. For instance, a nitrate sample collected in 2010 at a well with a 20-year total travel time (e.g., $\tau_u = 10$ yrs and $\tau_s = 10$ yrs) would be assigned the 1990 values for precipitation (450 mm), Interstate Canal discharge (0.4 km³/yr), center pivot irrigated area (2484 hectares), and area of planted corn (8905 hectares).
- A total of 288 unique transport rate combinations (corresponding to different combinations of the 16 vadose and 18 saturated-zone transport rates) were evaluated. Each transport rate combination incorporated up to 1,049 groundwater $[NO_3^-]$ values in the Random Forest model.

257 2.5 Random Forest Application

258 Random Forests are created by combining hundreds of unskilled regression trees into one model ensemble, or "forest", 259 which collectively produce skilled and robust predictions (Breiman, 2001). Models of groundwater $[NO_3^-]$ were developed using 260 five-fold cross validation (Hastie et al., 2009), where each fold was used to build the model (training data) four times, and held out 261 once (testing data). The maximum and minimum of the groundwater $[NO_3^-]$ and each predictor were determined and placed into 262 each fold for training models to eliminate the potential for extrapolation during validation. The four folds designated to build the 263 model also underwent a nested five-fold cross validation, as specified in the *trainControl* function within the *caret* (Classification 264 and Regression Training) R package (Kuhn, 2008; R Core Team, 2017). Functions in caret were used to train the Random Forest 265 models. We repeated the five-fold cross validation process five times to create a total of 25 models, similar to the approach used by Nelson et al. (2018), in order to assess sensitivity of model performance to the data assigned to the training and testing folds. 266

267 Permutation importance, partial dependence and Nash-Sutcliffe Efficiency (NSE)) were quantified to evaluate model 268 performance and to interpret results. NSE (Nash and Sutcliffe, 1970) was calculated as

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$$NSE = 1 - \left[\frac{\sum_{l=1}^{n} (Y_{l}^{obs} - Y_{l}^{pred})^{2}}{\sum_{l=1}^{n} (Y_{l}^{obs} - Y^{mean})^{2}} \right],$$
 (4)

where *n* is the number of observations, Y_i^{obs} is the ith observation of the response variable ([NO₃⁻]), Y_i^{pred} is the ith prediction from the Random Forest model, and Y^{mean} is the mean of observations *i* through *n*. Values from negative infinity to 0 suggest the mean of the observed [NO₃⁻] would serve as a better predictor than the model. When NSE = 0, model predictions are as accurate as that of a model with only the mean observed [NO₃⁻] as a predictor. From 0, larger NSE values indicate a model's predictive ability improves, until NSE = 1, where observations and predictions are equal. NSE was calculated for both the training and testing data. For each tree, a random bootstrapped sample (i.e., data randomly pulled from the dataset, sampled with replacement) is

extracted from the dataset (Efron, 1979), as well as a random subset of predictors to consider fitting at each split. Thus, each tree
is grown from a bootstrap sample and random subset of predictors, making trees random and grown independent of the others.
Observations not used as bootstrap samples are termed out-of-bag (OOB) data.

279 When building a tree, all [NO₃] from the bootstrap sample are categorized into terminal nodes, such that each node is 280 averaged and yields a predicted [NO₃⁻]. The performance and mean squared error (MSE) of a Random Forest model is evaluated 281 by comparing the observed $[NO_3^-]$ of the OOB data to the average predicted $[NO_3^-]$ from the forest. OOB data from the training dataset may be used to evaluate both permutation importance, referred to in the rest of this text as variable importance, and partial 282 283 dependence. Variable importance uses percent increase in mean squared error (% incMSE) to describe predictive power of each 284 predictor in the model (Jones and Linder, 2015). During this process, a single predictor is permuted, or shuffled, in the dataset. 285 Therefore, each observed [NO₃⁻] has the same relationship between itself and all predictors, except one permuted variable. The 286 % incMSE of a variable is determined by comparing the permuted OOB MSE to unpermuted OOB MSE. Important predictors will result in a large % incMSE, while a variable of minor importance does little to impact a model's performance, as suggested by a low 287 288 %incMSE value.

Partial dependence curves serve as a graphical representation of the relationship between $[NO_3^-]$ and predictors in the Random Forest model ensemble (Hastie et al., 2009). In these models, the y-axis of a partial dependence plot represents the average of the OOB predicted $[NO_3^-]$ at a specific x-value of each predictor.

292 3 Results and Discussion

This study addressed a relatively unexplored use of Random Forest, which was to identify optimal lag times based on testing a range of transport rate combinations through the vadose and saturated zones, historical $[NO_3^-]$, and the use of easily accessible environmental datasets.

296 **3.1. Relative Importance of Transport Time and Dynamic Variables**

In our initial modelling (using both static and dynamic predictors), we anticipated that we could use the Random Forest model with the highest NSE to identify the optimal pair of vadose and saturated-zone transport rates. However, no clear pattern emerged among the different models (Fig. 4). Given the small differences and lack of defined pattern in testing NSE values, we selected ten transport rate combinations (the five top performing models, plus four transport rate combinations of high and low transport rates, and one intermediate transport rate combination) for further evaluation of variable importance and sensitivity to a range of transport rate combinations (Table 2). Median total travel time ranked third in variable importance, while the four dynamic variables consistently had the four lowest rankings (Fig. 5). Total travel time also had the greatest variability in importance among
the fifteen variables, with a range of 18.4% between the upper and lower values, suggesting some model sensitivity to lag times.
Excluding total travel time, the remaining variables had an average variable importance range of 6%.

306 Dynamic variables had little influence on the model, despite common potential linkages to groundwater $[NO_3^-]$ (Böhlke 307 et al., 2007; Exner et al., 2010; Spalding et al., 2001). A pattern emerged among dynamic variables where the stronger the historical 308 trend of the predictor, the greater the importance of the predictor (Fig. 3; Fig. 5). For instance, center pivot irrigated area (highest 309 ranking dynamic variable) had the least noise and the most pronounced trend, while annual precipitation (lowest ranking variable) 310 was highly variable and lacked any trend over time (Fig. 3), and also may not be a substantial source of recharge (Böhlke et al., 311 2007). Further exploration could be done to test more refined and/or spatially varying predictors – for instance, annual median rainfall intensity for the growing season might have a more direct connection to nitrate leaching than total annual precipitation. 312 313 However, rainfall intensity data are not readily available. Likewise, availability of a long-term, detailed fertilizer loading dataset 314 would be advantageous in providing a more substantiated conclusion regarding the viability of applying dynamic variables to 315 determine vadose and saturated-zone lag. Dynamic variables could be of more use in other study areas that undergo relatively rapid 316 and pronounced changes (e.g., land use). In future work, the model sensitivity to dynamic variables could be tested through formal 317 sensitivity analysis and/or automated variable selection algorithms (Eibe et al., 2016).

Ultimately, results from initial analyses suggest that (1) the dynamic data did little to improve model performance, and (2) Random Forest was not able to relate the four considered dynamic predictors to $[NO_3^-]$ in a meaningful way that could be used to estimate lag time It is likely the influence of these dynamic predictors is dampened as nitrate is transported from the surface to wells such that data-driven approaches are unable to sort through noise to identify relationships.

322 **3.2** Use of Random Forest to determine transport rates

323 Due to their low relative importance as predictors, all four dynamic predictors were removed in the subsequent analysis. As discussed above, a notable variation in total travel time % incMSE was observed in Fig. 5, suggesting model sensitivity to this 324 325 variable. Additionally, a relationship between travel time and $[NO_3]$ has been suggested in the Dutch Flats area through previous 326 studies (Böhlke et al., 2007; Wells et al., 2018). Therefore, a second analysis of just the 11 static predictors was performed over 327 the full range of vadose and saturated transport rates (i.e., 288 combinations). However, in the second analysis, model sensitivity 328 to total travel time – evaluated with respect to the transport rate combination corresponding to the largest % incMSE of total travel 329 time – was used to determine a distinguished transport rate combination. In other words, models were re-trained and tested for all 330 transport rate combinations, each of which produced a unique set of values for the total travel time variable. As described in Section 331 2.5, the %_{inc}MSE value for total travel time was then based on the error induced in the model by permuting the calculated total 332 travel times across all the nitrate observations (i.e., randomly shuffling the total travel time variable, and thus disturbing the 333 structure of the dataset).

334 The Random Forest models were useful in identifying the relative magnitudes of V_u and V_s that led to high $\%_{inc}MSE$. 335 Based on the heat map of %incMSE, a band of transport rate combinations with consistently high %incMSE was visually apparent 336 (Fig. 6). The upper and lower bounds of the band translate to transport rate ratios (V_s/V_u) ranging from 0.9 to 1.5, and are values 337 that could be useful in constraining recharge and/or transport rate estimates in more complex mechanistic models of the Dutch 338 Flats area, as part of a hybrid modelling approach. This is especially important because recharge is one of the most sensitive parameters in a groundwater model (Mittelstet et al., 2011), yet one with high uncertainty. Whereas a saturated-zone velocity that 339 340 is greater than a vadose-zone velocity would be unexpected in many unconsolidated surficial aquifers receiving distributed 341 recharge, the statistical machine learning results are consistent with two contrasting primary recharge processes in the Dutch Flats

342 area: (1) diffuse recharge from irrigation and precipitation across the landscape, and (2) focused recharge from leaking irrigation 343 conveyance canals.

344 The %_{inc}MSE of total travel time in the second analysis (using only static variables) ranged from 20.6 to 31.5%, with the 345 largest %_{inc}MSE associated with vadose and saturated-zone transport rates of 3.50 m/yr and 3.75 m/yr, respectively (Fig. 6), and 346 the top four predictors for this transport rate combination were total travel time, vadose-zone thickness, dissolved oxygen, and 347 saturated thickness (Fig. 7). Converting those vadose and saturated-zone transport rates to recharge rates yielded values of 0.46 348 m/yr and 1.31 m/yr, respectively. Such a large difference between the two recharge values is consistent with the hydrologic 349 conceptual model of the Dutch Flats area. In fact, both model recharge rates compare favourably with recharge rates calculated 350 from the previous Dutch Flats studies using ${}^{3}H/{}^{3}He$ age-dating (Böhlke et al., 2007; Wells et al., 2018). For instance, the recharge 351 rate determined from the vadose-zone transport rate in this study (0.46 m/yr) was comparable to the mean recharge rate of 0.38 352 m/yr (n = 9) from groundwater age-dating at shallow wells, which are most representative of diffuse recharge below crop fields 353 that are present across most of the study area (e.g., Figure S2). Additionally, the recharge rate (1.31 m/yr) determined from the 354 saturated-zone transport rate was consistent with the mean recharge value derived from groundwater ages in intermediate wells 355 (1.22 m/yr, n = 13; Böhlke et al., 2007; Wells et al., 2018). Intermediate wells are variably impacted by focused recharge from 356 canals in upgradient areas. Given the similarity in diffuse recharge and focused recharge estimates from both Random Forest and 357 groundwater age-dating, the transport rate ratios (1.2 and 1.1, respectively) were consistent. That is, the Random Forest modelling 358 framework produced transport rates consistent with the major hydrological processes in Dutch Flats both in direct (i.e., transport 359 rate estimates) and relative (i.e., transport rate ratio) terms.

360 Assuming the Random Forest approach has accurately captured the two major recharge processes (diffuse recharge over 361 crop fields and focused recharge from canals), a comparison of recharge rates from all sampled groundwater wells representative 362 of recharge to the groundwater system as a whole (0.84 m/yr, n = 43) to the recharge rates from Random Forest modelling (0.46 m/yr, n = 43)363 and 1.31 m/yr) would provide an estimate of the relative importance of diffuse versus focused recharge on overall recharge in 364 Dutch Flats. Under these assumptions, diffuse recharge would account for approximately 55%, while focused recharge would 365 account for about 45% of total recharge in the Dutch Flats area. Similarly, Böhlke et al. (2007) concluded that these two recharge 366 sources contributed roughly equally to the aquifer on the basis of groundwater age profiles, as well as from dissolved atmospheric 367 gas data indicating mean recharge temperatures between those expected of diffuse infiltration and focused canal leakage.

368 Partial dependence plots, which illustrate the impact a single predictor has on $[NO_3]$ in the model with respect to other predictors (Fig. 8), largely reflect the conceptual understanding of the system from previous studies including Böhlke et al. (2007) 369 370 and Wells et al. (2018). Key features that strengthen confidence in the Random Forest modelling include (1) depth to bottom screen, where groundwater $[NO_3]$ is lower at greater depths, (2) the effects of minor and major canals, where groundwater $[NO_3]$ 371 372 in the vicinity of canals is diluted by canal leakage, and the influence of major canals extends a longer distance when compared to 373 that of minor canals, (3) land surface elevation, where elevations indicating proximity to major canals are associated with relatively 374 lower groundwater $[NO_3^-]$, and (4) DO concentration, where higher DO concentration is linked to higher groundwater $[NO_3^-]$. We 375 note that decreasing DO and $[NO_3^-]$ with groundwater age can be explained by DO reduction and historical changes in $[NO_3^-]$ 376 recharge, whereas groundwater chemistry and nitrate isotopic data recorded in both this study and previous Dutch Flats studies 377 suggest denitrification was not a major factor in this alluvial aquifer.

The partial dependence plot (Fig. 8) for total travel time exhibits a pronounced threshold, where $[NO_3^-]$ is markedly higher for groundwater with travel time less than seven years. It is possible this reflects long-term stratification of groundwater $[NO_3^-]$, stemming from the suggested patterns stated above as nitrate varies with aquifer depth due to the influences of diffuse and focused recharge in the region. This seven-year threshold is slightly lower than a previous estimate of mean groundwater age in the aquifer 382 (8.8 years; Böhlke et al., 2007; where groundwater age excludes vadose-zone travel time) and suggests that shallow groundwater

383 can respond relatively rapidly to changes in nitrogen management in the Dutch Flats area.

384 3.3 Opportunities and limitations of Random Forest approach in estimating lag times

385 Overall, results suggest that in a complex system such as Dutch Flats, Random Forest was able to identify reasonable 386 transport rates for both the vadose and saturated zones, and with additional validation, this method may offer an inexpensive (i.e., compared to groundwater age-dating across a large monitoring well network and/or complex modelling) and reasonable technique 387 388 for estimating lag time from historical monitoring data. Further, this approach allows for additional insight on groundwater 389 dynamics to be extracted from existing monitoring data. However, this study was conducted in the context of a larger project 390 (Wells et al., 2018) and built on prior research on groundwater flow and $[NO_3^-]$ in the study area (Böhlke et al., 2007). Therefore, 391 it is critical in future work to incorporate site-specific knowledge, process understanding, and approaches for increasing 392 interpretability of machine learning models (Lundberg et al., 2020, Saia et al., 2020), as highlighted in key considerations below.

- 393
- 394 Some key considerations for future application of this approach include:
- (1) The Random Forest approach might be useful for estimating future recharge and [NO₃⁻] using multiple potential management scenarios, as long as considered management scenarios fall within the range of historical observations used to train the model. This information could be used to inform policy makers of the impact that current and future management decisions will have on recharge and [NO₃⁻].
- (2) The Dutch Flats overlies a predominantly oxic aquifer, where nitrate transport is mostly conservative. In aquifers with heterogeneity in denitrification potential and/or distinct nitrate extinction depths (Liao et al., 2012; Welch et al., 2011), this approach may be biased toward oxic portions of the aquifer where the nitrate signal is preserved. Similarly, vertical profiles of [NO₃⁻] and isotopic composition in the vadose zone could provide valuable data to investigate (1) the amount of nitrate stored in the vadose zone, and (2) whether nitrate undergoes any biogeochemical changes while being transported through the vadose zone to the water table.
- 405 (3) While estimates of vadose and saturated-zone transport rates determined from % incMSE are consistent with previous 406 studies, the predictive performance of the selected model (based on NSE and visual inspection of predicted versus 407 observed nitrate plots) was not substantially different than other models tested. In other words, the "optimal model" was 408 only weakly preferred in terms of predicting [NO₃⁻]. Testing the approach of using %_{inc}MSE in other vadose and saturated 409 zones, with substantial comparison to previous transport rate estimates, is warranted. This would be especially valuable 410 in an area with a well-defined input function for nitrate that could be compared to a reconstructed input function from the 411 model. Further, in aquifer settings with relatively evenly distributed recharge, optimized travel times to wells could be used to estimate the infiltration date of samples, thus providing an optimized view of historical variation of [NO3-] entering 412 413 the subsurface, as illustrated in Figure S1B. In the Dutch Flats area, however, such an analysis is complicated by effects 414 of subsurface nitrate dilution by local recharge from canal leakage.
- (4) Despite potential non-uniqueness in prediction metrics, the heat map of %_{inc}MSE did reveal an orderly pattern suggesting
 consistent transport rate ratios. For modelling efforts where recharge rates are a key calibration parameter, identification
 of a range of reasonable recharge rates, and/or the ratio of recharge rates from diffuse and focused recharge sources for a
 complex system will reduce model uncertainty and improve results. This statistical machine learning approach, which
 essentially leverages nitrate as a tracer (albeit with an unknown input function in this case), may provide valuable insight

- 420 to complement relatively expensive groundwater age-dating or vadose-zone monitoring data, or perhaps as a standalone
- 421 approach for first-order approximations.
- 422 (5) The demonstrated statistical machine learning approach is apparently well-suited for drawing out transport rate
 423 information from a site with two distinct recharge sources (diffuse versus focused recharge sources) driving the
 424 groundwater nitrate dynamics. Further testing is needed at sites where recharge and nitrate dynamics are more subtle.

425 4 Conclusions

426 The Dutch Flats area exhibits large variations in [NO₃⁻] throughout a relatively small region in western Nebraska. Long-427 term groundwater [NO₃⁻] monitoring and previous groundwater age-dating studies in Dutch Flats provided an opportune setting to test a new application of statistical machine learning (Random Forest) for determining vadose and saturated-zone transport rates. 428 429 Overall results suggest Random Forest has the capability to both identify reasonable transport rates (and lag time) and key variables 430 influencing groundwater [NO₃⁻], albeit with potential for non-unique results. Limitations were also identified when using dynamic 431 predictors to model groundwater [NO₃⁻]. Utilizing only static predictors, and Random Forest's ability to evaluate variable 432 importance, vadose-zone and saturated-zone transport rates were selected based on model sensitivity to changing the total travel time predictor. In other words, total travel time variable importance was evaluated for 288 different transport rate combinations, 433 434 and the combination with a total travel time having the largest influence over the model's ability to predict $[NO_3]$ was selected for 435 additional examination. This analysis identified a vadose-zone and saturated-zone transport rate combination consistent with rates 436 previously estimated from ³H/³He age-dating in Böhlke et al. (2007) and Wells et al. (2018), indicating a combination of distributed 437 and focused sources of irrigation recharge to this aquifer

438 Future studies could include assessments of the proper conditions for application of dynamic predictors and include 439 comparisons of data-driven analyses with complementary datasets and/or modelling (e.g., field-based recharge rate estimates, 440 finite-difference flow model). Despite noted limitations, partial dependence plots and relative importance of predictors were largely 441 consistent with previous findings and mechanistic understanding of the study area, giving greater confidence in model outputs. 442 The influence of canal leakage on groundwater recharge rates and [NO₃⁻], for example, was consistent with previous Dutch Flats 443 studies. Partial dependence plots suggest a threshold of higher $[NO_3]$ for groundwater with total travel time (vadose and saturated-444 zone travel times, combined) of less than seven years, indicating the potential for relatively rapid groundwater [NO₃⁻] response to widespread implementation of best management practices. Additionally, research is needed to determine the minimum number of 445 446 observations needed to effectively apply the framework shown here.

447

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451

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464 Supplemental Material: An online file accompanying this article contains additional figures, tables, and details of methods used
 465 for the study.

466

467 **Code and Data Availability:** Code is available on request. Data used in the random forest model and described in the supplemental

468 material is available via the University of Nebraska – Lincoln Data Repository (<u>https://doi.org/10.32873/unl.dr.20200428</u>).

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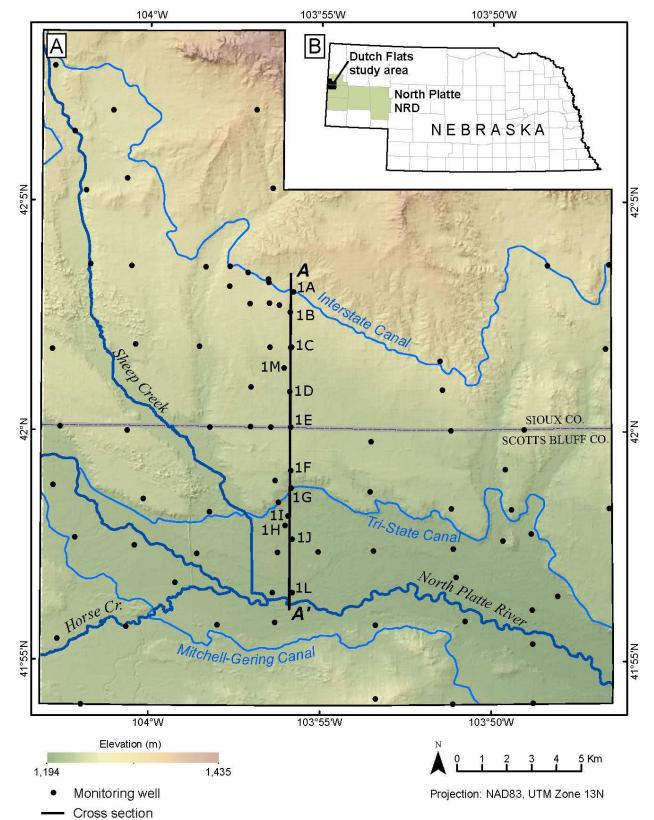
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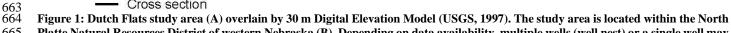
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- Platte Natural Resources District of western Nebraska (B). Depending on data availability, multiple wells (well nest) or a single well may
 be found at each monitoring well location. Transect A-A' represents the location and wells displayed in the Fig. 2 hydrogeologic cross section.

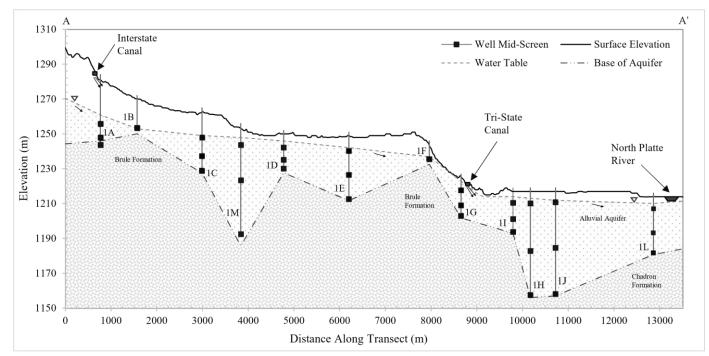
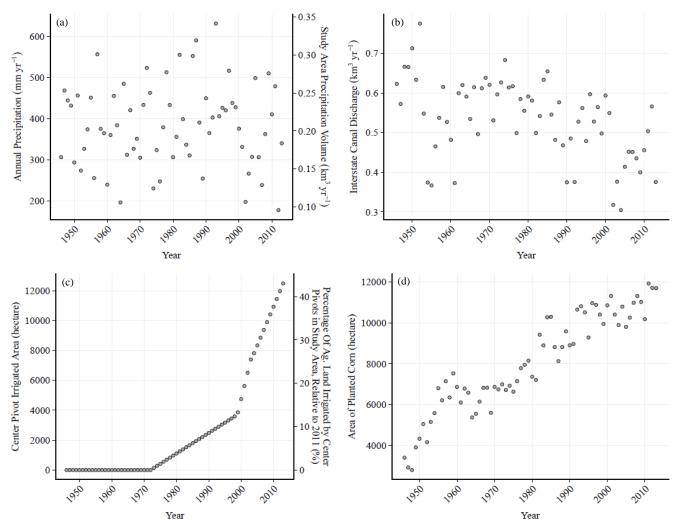
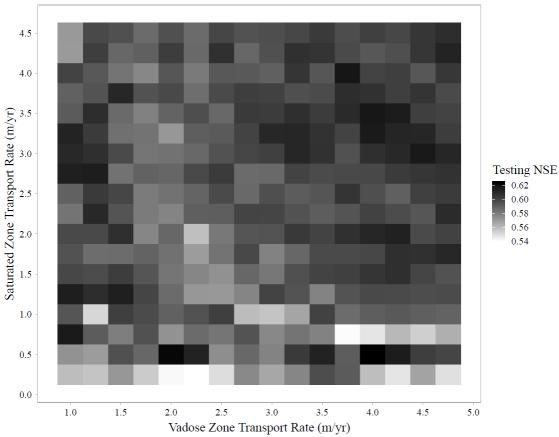


Figure 2: Cross-section along representative well transect (see Fig. 1) within the Dutch Flats area. Surface elevation data
were derived from a 30-meter Digital Elevation Model (USGS, 1997). Water surface and base of aquifer elevations were
sourced from a 1998 Dutch Flats study (Böhlke et al., 2007, Verstraeten et al., 2001a, 2001b). Small black arrows beneath
the surface indicate general groundwater flow direction.

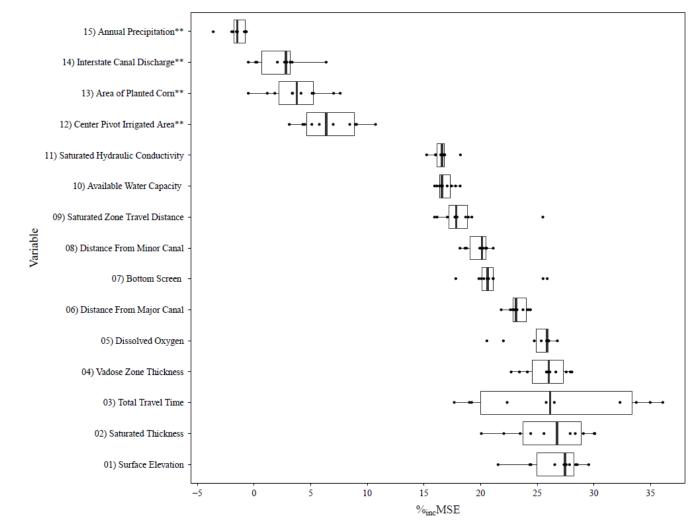


678 679 Figure 3: Time series plots of all four dynamic predictors. Figures represent (a) annual precipitation, (b) Interstate canal discharge, (c) center pivot irrigated area, and (d) area of planted corn from 1946 to 2013.

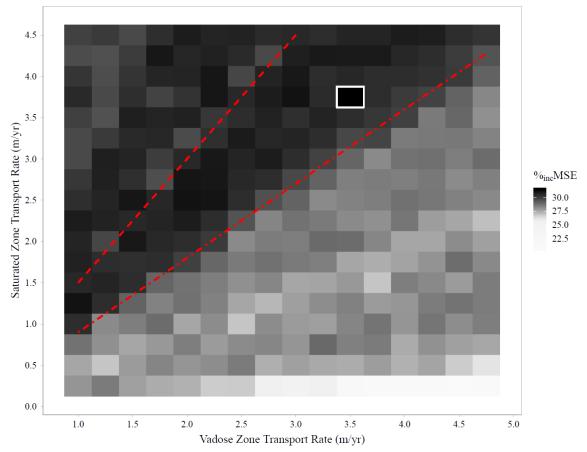


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Figure 4: Heat map of testing NSE results from 288 vadose and saturated-zone transport rate combinations. Testing NSE in this figure is the median of all 25 model outputs from each of the 288 transport rate combinations. No clear pattern of optimal vadose and saturatedzone transport rate combinations was observed.

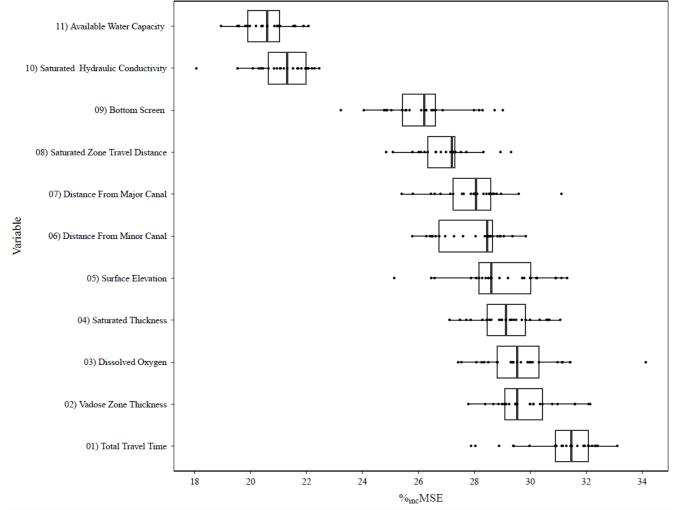


686 687 Figure 5: Boxplot of the %incMSE from the ten transport rate combinations shown in Table 2. Each boxplot has ten points for each 688 transport rate combination, representing the median % incMSE from the 25 models (five-fold cross validation, repeated 5 times). A larger 689 % incMSE suggests the variable had a greater influence on a model's ability to predict [NOs⁻]. **Denotes dynamic predictors.

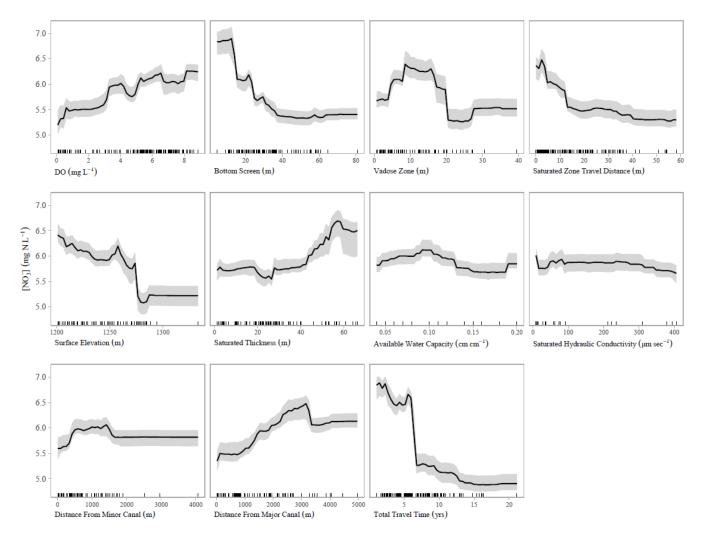


690 691 Figure 6: Heat map of %incMSE (median from 25 models) from variable importance of total travel time for each of the 288 transport 692 rate combinations evaluated. Red dashed lines indicate upper ($V_s / V_u = 1.5$, long dashes) and lower (0.9, short dashes) bounds of the 693 band of transport rate combinations with consistently higher %incMSE. The white square highlights the single transport rate

694 combination with the highest %incMSE.



697 Figure 7: Plot from secondary analysis exploring variable importance of the transport rate combination with the largest median % incMSE in total travel time (Vu = 3.5 m/yr; Vs = 3.75 m/yr). Each point is from one of 25 Random Forest models run for this evaluation. A larger %incMSE suggests the variable had a greater influence on a model's ability to predict [NOs⁻].



702Figure 8: Partial dependence plot for model evaluating transport rate combination of $V_u = 3.5$ m/yr and $V_s = 3.75$ m/yr. Tick marks on704each plot represent predictor observations used to train models.

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715 Table 1. List of the 15 predictors used for Random Forest evaluation. Average (avg.) and median (med.) values are shown.

Predictor		Predictor Type	Source	
Center Pivot Irrigated Area (avg. = 2618; med. = 1037) ^a	hectare	Dynamic	NAIP; NAPP; Landsat-1,5, 7, 8 ^b	
Interstate Canal Discharge (avg. = 0.53 ; med. = 0.55) ^a	km ³ yr ⁻¹	Dynamic	USBR (2018)	
Area of Planted Corn (avg. = 8065 ; med. = 7869) ^a	hectare	Dynamic	NASS (2018)	
Precipitation (avg. = 384 ; med. = 377) ^a	mm yr ⁻¹	Dynamic	NOAA (2017)	
Available Water Capacity (avg. $= 0.1$; med. $= 0.1$)	cm cm ⁻¹	Static	NRCS (2018)	
Dissolved Oxygen (avg. = 4.6 ; med. = 5.4)	mg L ⁻¹	Static	C. Hudson, Personal Communication (2018)	
Distance from a Major Canal (avg. = 1462.2; med. = 1161.4)	m	Static	USGS (2012) ^b	
Distance from a Minor Canal (avg. = 633.2; med. = 397.6)	m	Static	USGS (2012) ^b	
Bottom Screen (avg. $= 26.9$; med. $= 24.4$)	m	Static	UNL (2016) ^b	
Saturated Hydraulic Conductivity (avg. = 68; med. = 28)	µm sec⁻¹	Static	NRCS (2018)	
Saturated Thickness (avg. = 30.2; med. = 27.6)	m	Static	T. Preston, Personal Communication (2017) ^b	
Saturated-Zone Travel Distance (avg. = 13.3; med. = 7)	m	Static	UNL (2016) ^b	
Surface Elevation (DEM) (avg. = 1244; med. = 1248)	m	Static	USGS (1997)	
Total Travel Time (avg. = 6.4 ; med. = 5.7) ^c	years	Static	UNL (2016) ^b	
Vadose-Zone Thickness (avg. = 9.9; med. = 7.3)	m	Static	T. Preston, Personal Communication (2017); A. Young, Personal Communication (2016)	

^a Average and median span from 1946 to 2013

^b Data required further analysis to yield calculated values; data sources are USDA (2017) and USGS (2017)

 $^{\rm c}Average$ and Median reflects transport rates of $V_u{=}\ 3.5\ m/yr$ and $V_u{=}\ 3.75\ m/yr$

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717 Table 2. Summary of ten vadose and saturated-zone transport rate combinations selected from 288 unique potential combinations from 718 the analysis including dynamic variables.

-	Vadose-zone Transport Rate (m/yr)	Sat. Zone Transport Rate (m/yr)	Test NSE	[NO3 ⁻] - Observations ^a	Total Travel Time (yrs)	
					Mean (±1σ)	Median
Five Top- Performing Transport Rates	4.00	0.50	0.623	878	19.9 (± 15.8)	11.3
	2.00	0.50	0.622	861	21.6 (± 15.0)	16.5
	3.75	4.00	0.617	1049	6 (± 3.7)	5.4
	4.00	3.50	0.617	1049	6.3 (±4.1)	5.7
	4.50	3.00	0.616	1049	6.7 (± 4.7)	5.7
Extreme and Midrange Transport Combinations	4.75	4.50	0.608	1049	5.1 (± 3.2)	4.6
	2.75	2.25	0.599	1049	9.6 (± 6.3)	8.5
	1.00	4.50	0.570	1049	12.6 (± 7.7)	10.8
	1.00	0.25	0.559	607	26.7 (± 13.3)	20.6
	4.75	0.25	0.548	664	21.3 (± 15.0)	14.9

⁷¹⁹ ^aIn cases with slow transport rates, lag times were relatively long and not all [NO₃⁻] data could be used in the model. For example, a slow transport rate combination

720 resulting in a lag time with the infiltration year prior to 1946 could not be included. Thus, some models were ultimately based on <1,049 observations.