



1 **A novel framework of deriving joint impoundment**  
2 **rules for large-scale reservoir system based on a**  
3 **classification-aggregation-decomposition approach**

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15  
16 **Abstract:** Joint and optimal impoundment operation of the large-scale reservoir system  
17 has become more crucial for modern water management. Since the existing techniques  
18 fail to optimize the large-scale multi-objective impoundment operation due to the  
19 complex inflow stochasticity and high dimensionality, we develop a novel combination  
20 of parameter simulation optimization and classification-aggregation-decomposition  
21 approach here to overcome these obstacles. There are four main steps involved in our  
22 proposed framework: (1) reservoirs classification based on geographical location and  
23 flood prevention targets; (2) assumption of a hypothetical single reservoir in the same  
24 pool; (3) the derivation of the initial impoundment policies by the non-dominated  
25 sorting genetic algorithm-II (NSGA-II); (4) further improvement of the impoundment  
26 policies via Parallel Progressive Optimization Algorithm (PPOA). The framework



27 potential is performed on China's mixed 30-reservoir system in the upper Yangtze River.  
28 Results indicate that our method can provide a series of schemes to refer to different  
29 flood event scenarios. The best scheme outperforms the conventional operating rule, as  
30 it increases impoundment efficiency from 89.50% to 94.16% and hydropower  
31 generation by 7.70 billion kWh (or increase 3.79%) while flood control risk is less than  
32 0.06.

33 **Keywords:** Large-scale reservoir system; Joint impoundment rules; Multi-objective  
34 operation; Classification-aggregation-decomposition; Yangtze River basin

## 35 **1 Introduction**

36 Rapid economic development and the growth of the human population are  
37 responsible for more serious and wider water-related challenges, which lead to greater  
38 stress on water resources management. One of the most effective measures to alleviate  
39 water issues is to regulate natural streamflow via reservoirs (Lauri et al., 2012;Ng et al.,  
40 2017). Cascade impoundment operation can properly achieve the goal since it stores  
41 excess water during the wet season and depletes reservoir storage during the dry season  
42 (Afshar et al., 2010;Labadie, 2004). In recent decades, impoundment operation has been  
43 one hot academic topic. Considerable research efforts (Liu et al., 2011;Paredes and  
44 Lund, 2006;Xu et al., 2017;Yeh, 1985) frequently point out that its key to the scientific  
45 operation is deriving effective operating policies. However, most of the literature  
46 merely focuses on the small-scale reservoir system, yet fails to address the complex  
47 inflow stochasticity and high dimensionality of the multi-objective trans-basin (Yan et  
48 al., 2012) and trans-province impoundment problems (Jurasz and Ciapala, 2017), even  
49 if the latter large-scale impoundment operation is more necessary and suitable for



50 modern water resources management (Wang et al., 2014;Zhou et al., 2018).

51 As a matter of fact, the inherent scientific characteristics of inflow stochasticity  
52 for large-scale impoundment operation has no difference with the small-scale one, there  
53 are three theoretical breakthroughs to cope with it: (1) implicit stochastic optimization  
54 (ISO) (Feng et al., 2017), (2) explicit stochastic optimization (ESO) (Goor et al., 2010),  
55 and (3) parameter simulation optimization (PSO) (Zhang et al., 2019). ISO requires  
56 ‘perfect inflow forecast’ and ESO behaves in a more complex way to explicitly  
57 incorporate all inflow probabilities. PSO is relatively preferred for large-scale operation  
58 (Celeste and Billib, 2009;Tan et al., 2017), which predefines a rule curve shape and then  
59 employs heuristic algorithms to identify the best parameter combination under all  
60 possible inflow scenarios. Regarding another well-known ‘high dimensionality’ in the  
61 PSO framework, the original simulation model is usually replaced by a surrogate model  
62 for simplification. The surrogate should preserve and describe the main features of the  
63 original model (Chu et al., 2015;Shaw et al., 2017;Zhang et al., 2017). The subtle  
64 combination of the PSO framework and a surrogate model has indeed made some  
65 achievements in addressing inflow stochasticity and dimensional curse of multi-  
66 reservoir hydropower (Glotic and Zamuda, 2015;Valdes et al., 1992) and flood control  
67 operations (Zhang et al., 2019), but is seldom utilized in large-scale impoundment  
68 operation.

69 The major challenge lies in the reliability of the surrogate model. On the one hand,  
70 it should highlight the reservoir storage state as the most vital indicator to track the  
71 original system status, since the highest priority of impoundment operation is to ensure



72 certain storage for flood prevention during the operating horizon and to raise enough  
73 end reservoir storage for water demand during the following dry period (Li et al.,  
74 2018;Xu et al., 2017); Additionally, it also should reduce the number of decision  
75 variables, making it possible to solve the curse of dimensionality. While it is noticed  
76 that reservoirs can be classified into different pools according to the tributaries and  
77 flood prevention targets (Zhang et al., 2014), a novel idea of ‘classification-  
78 aggregation-decomposition’ is naturally introduced to structure the proper surrogate  
79 model. The reservoirs in the same pool are firstly aggregated in water units to capture  
80 reservoir storage information, then a decomposition method is used to decentralize  
81 reservoir storage decisions into individual reservoirs in each pool. The salient feature  
82 of this approach is to simplify the large-scale system into several equivalent hypothetic  
83 reservoirs via aggregation, which caters to the replacement requirement of the  
84 impoundment model.

85       Nevertheless, the current decomposition methods still have some degree of  
86 drawbacks. Li et al. (2014a) and Zhang et al. (2019) allocated the virtual reservoir  
87 output to individual reservoirs by using the empirical equations. Both made a quick  
88 decision on decomposition forms but did not consider the maximum utilization of water  
89 resources. Tan et al. (2017) adopted an improved genetic algorithm to seek for the  
90 optimal decomposition scheme in the water-supply systems, but it is more time-  
91 consuming since the calculation of the evaluation function goes to an exponential  
92 increase with the number of involved reservoirs (Castelletti et al., 2012;Zhao et al.,  
93 2012). These common techniques cannot balance computing efficiency and optimal



94 operating rules well. This limits their further application in practice. Actually, the recent  
95 implementation of parallel computation has been proved able to reach a balance point  
96 (Li et al., 2014b;He et al., 2019), although the parallelization technique attracts little  
97 attention up to now. To this end, an emerging method-Parallel Progressive Optimization  
98 Algorithm (PPOA) (Feng et al., 2018b) is introduced to assist our decomposition  
99 strategy. It is a means of improving the quality of optimization while using a multi-core  
100 configuration to enhance execution efficiency (Cheng et al., 2014).

101 To verify the feasibility of the proposed framework, we select a typical mixed 30-  
102 reservoir system in China as the case study, where two objectives of reservoir  
103 impoundment efficiency (*IE*) and flood control risk (*FCR*) are simultaneously  
104 optimized, and then PPOA improves hydropower generation of individual reservoirs of  
105 each pool without *IE* and *FCR* distortion. The remainder of the paper is structured as  
106 follows: Section 2 addresses the 30-reservoir system and describes their conventional  
107 operating rules for impoundment operation; Section 3 introduces the framework in  
108 detail; Section 4 and Section 5 provide the experimental results and the application  
109 prospects of this method; Section 6 ends with the conclusions.

## 110 **2 Case study**

111 The Yangtze River (in Fig. 1a) basin possesses abundant water potential in China.  
112 It drains a catchment of 1.80 million km<sup>2</sup> with a total length of 6,300km. Its main  
113 tributaries include the Jinsha River, Yalong River, Min River, Jialing River, and Wu  
114 River. Owing to the subtropical monsoon climate, the Yangtze River basin often suffers  
115 from the uneven temporal and spatial distribution of flood hazards induced by heavy



116 rainfalls. A series of large reservoirs have been built along its mainstream and tributaries  
117 to allocate water resources in recent decades. Among them, a 30-reservoir system  
118 including the core Three Gorges Reservoir (TGR) (in Fig. 1b) is one of the most critical  
119 water conservancy projects in China. Most reservoirs in the system serve multi-  
120 purposes (e.g., flood control, energy generation, tourism), except for Ge-Zhou-Ba (GZB)  
121 which is a run-of-river hydropower station. Particularly, TGR serves as the largest water  
122 project around the world, which is not only equipped with 22.50 GW installed  
123 hydropower capacity, but also prevents downstream flood disaster. The 30-reservoir  
124 system usually implements an impoundment operation to develop water resources. The  
125 characteristic parameters of the 30 reservoirs are shown in Table 1.

126 <Please insert Fig. 1 here>

127 <Please insert Table 1 here>

128 For the impoundment operation of these reservoirs, Conventional Operating Rules  
129 (CORs) are often individually predefined at the planning stage of reservoir  
130 construction to provide guidelines. As Fig. 2 shows, COR suggests that the reservoir  
131 water level should rise linearly throughout the whole impoundment horizon until it is  
132 up to the top of the conservation pool. However, overlapping the impoundment time  
133 of cascade reservoirs makes them compete with each other. It results in reduced water  
134 supplies to face the following non-flood season. In fact, two preset strategies of (1)  
135 advancing initial impoundment operation timing, but not earlier than Aug 1st; (2)  
136 raising the reservoir water levels, can be activated to excavate the potential benefits of  
137 joint impoundment operation on China's reservoir communities in the upper Yangtze



138 River basin (He et al., 2019). The aim of the joint impoundment operation of the 30-  
139 reservoir system is to make efficient water resources utilization, on the condition that  
140 it reserves enough storage capacity for flood control. The restored inflow series from  
141 Aug 1st to Dec 31st spanning over 57 years (i.e. 1956-2012) are collected from the  
142 Yangtze River (Changjiang) Water Resources Commission. The time step used is ten  
143 (or eleven) days, a traditional Chinese measure of time, and therefore there are 15  
144 operating periods for the five months per year.

145 <Please insert Fig. 2 here>

### 146 **3 Methodology**

147 Fig. 3 shows our research framework to derive the optimal impoundment rules for  
148 the 30-reservoir system. The methodological modules are summarized below:

149 (1) All reservoirs are classified into different pools (in Table 1) according to their  
150 geographic locations and flood prevention targets etc.;

151 (2) Reservoirs in the same pool are aggregated in water units to be a virtual  
152 reservoir and the virtual reservoir storage is treated as the state variable during the  
153 optimization process;

154 (3) PSO is employed to derive initial impoundment rules by considering the trade-  
155 offs between *IE* and *FCR*;

156 (4) PPOA helps formulate the final impoundment rules by boosting hydropower  
157 generation without *IE* and *FCR* distortion.

158 <Please insert Fig. 3 here>

#### 159 **3.1 Reservoirs classification**



160 During an impoundment optimization process, the dimensionality of decision  
161 variables increases linearly with the number of reservoirs; meanwhile, the  
162 computational burden of the objective function trends an exponential increase (Galelli  
163 and Castelletti, 2013). The vast reservoir community results in ‘dimensionality disaster’,  
164 which makes it tricky to derive effective joint rules. An attractive alternative to solve  
165 dimensionality restrictions is to classify these reservoirs and reduce their decision  
166 variables. The basic idea is to divide the 30-reservoir system into different pools  
167 according to their geographic distributions in the same tributary and flood prevention  
168 targets etc. (Heever and Grossmann, 2000; Saad et al., 1994).

### 169 3.2 Aggregation and decomposition schemes

170 Conceptually, these reservoirs in the same pool can be assembled into a virtual one.  
171 The hypothetical reservoir should retain the main characteristics yet ignore its hydraulic  
172 connection (Duran et al., 1985). As shown below, the reservoirs are aggregated in water  
173 units to simplify guidance on impoundment optimization (Tan et al., 2017):

$$174 \quad V_i^*(t) = \sum_{n=1}^{M_i} V_{i,n}(t) \quad (1)$$

$$175 \quad I_i^*(t) = \sum_{n=1}^{M_i} I_{i,n}(t) - Eva_i(t) \quad (2)$$

176 where  $V_i^*(t)$  and  $I_i^*(t)$  are hypothetical reservoir storage and inflow of the  $i$ th pool at  
177 time  $t$ , respectively;  $V_{i,n}(t)$  and  $I_{i,n}(t)$  are the storage and inflow from external sources  
178 of the  $n$ th reservoir of the  $i$ th pool at time  $t$ , respectively;  $Eva_i(t)$  is the sum loss of the  
179  $i$ th pool at time  $t$  (e.g., evaporation, seepage);  $M_i$  is the total number of reservoirs in the  
180  $i$ th pool.





181 As reservoir storage is often treated as the state variable for reservoir operation  
182 (Feng et al., 2018a; Chang and Chang, 2006), the virtual storage  $V_i^*(t)$  is chosen here  
183 as the state variable for the optimization process. It can be easily formulated by Eq. (1)  
184 in any case of reservoir topology (shown in Fig. 4). Fig. 4(a) and Fig. 4(b) are  
185 considered in our case study.

186 <Please insert Fig. 4 here>

187 The state variable  $V_i^*(t)$  of each pool at all periods could be determined by the  
188 aggregated impoundment rules. Another issue is how to allocate  $V_i^*(t)$  to individual  
189 reservoirs in the same pool. Some traditional decomposition strategies (e.g., fixed  
190 proportions) have been experimented well (Turgeon, 1980; Zhang et al., 2019). In our  
191 study, a similar decomposition way of the percentage of the allowable reservoir storage  
192 is initially taken:

193 
$$V_{i,n}(t) = SL_{i,n}(t) + (V_i^*(t) - \sum_{m=1}^{M_i} SL_{i,m}(t)) \times \frac{SS_{i,n}(t) - SL_{i,n}(t)}{\sum_{m=1}^{M_i} (SS_{i,m}(t) - SL_{i,m}(t))} \quad (3)$$

194 where  $SL_{i,n}(t)$  is the lower boundary of the  $n$ th reservoir storage of the  $i$ th pool at time  
195  $t$ ;  $SS_{i,n}(t)$  is the  $n$ th reservoir storage of the  $i$ th pool at time  $t$ , which is relative to its  
196 seasonal top of buffer pool.

### 197 3.3 Parameter simulation optimization (PSO)

198 The decomposition structure is embedded into the aggregation module, where the  
199 latter combines with the multi-objective impoundment model to explore trade-offs  
200 between the  $IE$  maximization and the  $FCR$  minimization (Liu et al., 2011; Zhou et al.,  
201 2015). We established the PSO framework (Giuliani et al., 2016; Celeste and Billib,  
202 2009) here to identify the initial impoundment strategies. As there are seven pools for



203 the 30-reservoir system and 15 decision variables for each virtual reservoir (one  
 204 decision variable corresponds to one operating period), there are a total of 105 (=7\*15)  
 205 decision variables for these seven virtual reservoirs rather than 450 (=30\*15) decision  
 206 variables in real.

### 207 3.3.1 Objective functions and constraints

208  $IE$  is a critical indicator for impoundment operation to assess water resources  
 209 potential in the case of controllable  $FCR$  (Zhou et al., 2018):

210 (1)  $IE$  represents future water resources utilization for the following non-flood  
 211 period, it can be defined as follows:

$$212 \max IE = \frac{1}{Y} \sum_{y=1}^Y \frac{\sum_{i=1}^I \sum_{n=1}^{M_i} (VE_{i,n}(y) - SD_{i,n})}{\sum_{i=1}^I \sum_{n=1}^{M_i} (SU_{i,n} - SD_{i,n})} \quad (4a)$$

$$213 IE_{i,n} = \frac{1}{Y} \sum_{y=1}^Y \frac{VE_{i,n}(y) - SD_{i,n}}{SU_{i,n} - SD_{i,n}} \quad (4b)$$

214 where  $IE_{i,n}$  is the annual impoundment efficiency of the  $n$ th reservoir of the  $i$ th pool;  
 215  $VE_{i,n}(y)$  is the end storage of the  $n$ th reservoir of the  $i$ th pool in the  $y$ th year;  $SU_{i,n}$ , and  
 216  $SD_{i,n}$  is the  $n$ th reservoir storages of the  $i$ th pool, which corresponds to their top of  
 217 conservation pool and inactive pool, respectively.  $I$  and  $Y$  are the number of all pools  
 218 and years, respectively.  $I$  is 7 in our case.

219 (2)  $FCR$ , another critical objective to control the impoundment process, can be  
 220 evaluated as follows:

$$221 \min FCR = \min \{ \max \{ FCR(t) \} \}, \quad (0 < t \leq T \cdot Y) \quad (5a)$$



$$222 \quad FCR(t) = \max\left\{\frac{\sum_{i=1}^I \sum_{n=1}^{M_i} (V_{i,n}(t) - SS_{i,n}(t))}{\sum_{i=1}^I \sum_{n=1}^{M_i} (SU_{i,n} - SS_{i,n}(t))}, 0\right\} \quad (5b)$$

$$223 \quad FCR_{i,n}(t) = \max\left\{\frac{V_{i,n}(t) - SS_{i,n}(t)}{\sum_{i=1}^I \sum_{n=1}^{M_i} (SU_{i,n} - SS_{i,n}(t))}, 0\right\} \quad (5c)$$

224 where  $FCR_{i,n}(t)$  is the  $FCR$  of the  $n$ th reservoir of the  $i$ th pool at time  $t$ ;  $T$  is the number  
 225 of operating periods in one year.

### 226 3.3.2 Constraints

227 A reservoir operation model generally contains the following constraints:

228 (1) Mass balance equation:

$$229 \quad V_{i,n}(t+1) = V_{i,n}(t) + (I_{i,n}(t) + \sum_{j \in \Phi_{j,i,n}} R_j(t) - R_{i,n}(t)) \cdot \Delta t \quad (6)$$

230 (2) Reservoir storage limits

$$231 \quad SL_{i,n}(t) \leq V_{i,n}(t) \leq SS_{i,n}(t) \quad (7)$$

232 (3) Water discharge limits

$$233 \quad RL_{i,n}(t) \leq R_{i,n}(t) \leq RU_{i,n}(t), \quad R_{i,n}(t) = Q_{i,n}(t) + QS_{i,n}(t) \quad (8)$$

234 (4) Hydropower generation limits

$$235 \quad PL_{i,n}(t) \leq N_{i,n}(t) \leq PU_{i,n}(t) \quad (9)$$

236 (5) Boundary conditions

$$237 \quad Z_{i,n}(t) = \begin{cases} Z_{i,n,begin}, & t = 1, T+1, \dots, (Y-1)T+1 \\ Z_{i,n,end}, & t = T, 2T, \dots, YT \end{cases} \quad (10)$$

238 where

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$V_{i,n}(t), V_{i,n}(t+1)$	the $n$ th reservoir storage of the $i$ th pool at the beginning and end time $t$
$\Phi_{j,i,n}$	the upstream reservoir set which has a physical connection with the $n$ th reservoir of the $i$ th pool
$I_{i,n}(t)$	the $n$ th reservoir inflow of the $i$ th pool from external sources at time $t$

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$R_{i,n}(t)$	the $n$ th reservoir release of the $i$ th pool at time $t$
$\Delta t$	the time interval, day
$SL_{i,n}(t), SS_{i,n}(t)$	the lower and upper storage boundaries of the $n$ th reservoir of the $i$ th pool at time $t$
$RL_{i,n}(t), RU_{i,n}(t)$	the lower and upper water release boundaries of the $n$ th reservoir of the $i$ th pool at time $t$
$Q_{i,n}(t)$	the generation discharge of the $n$ th reservoir of the $i$ th pool at time $t$
$QS_{i,n}(t)$	the spillway water of the $n$ th reservoir of the $i$ th pool at time $t$
$PL_{i,n}(t), PU_{i,n}(t)$	the lower and upper hydropower output boundaries of the $n$ th reservoir of the $i$ th pool at time $t$
$Z_{i,n}(t)$	the water level of the $n$ th reservoir of the $i$ th pool at time $t$
$Z_{i,n,begin}, Z_{i,n,end}$	the annual top of buffer pool and top of conservation pool of the $n$ th reservoir of the $i$ th pool

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239 **3.3.3 Optimization algorithm**

240 The NSGA-II algorithm (Deb et al., 2002) has made some successful  
 241 achievements in the PSO work of the reservoir field (Lei et al., 2018; Lotfan et al., 2016).  
 242 It realizes a fast convergence in Pareto frontiers with the crowding distance and the non-  
 243 dominated sorting rank (Deb et al., 2002). NSGA-II is implemented in this paper, even  
 244 if some other heuristic algorithms may also be able to handle it. The experimental  
 245 parameter is set as: the population size = 64, generation = 100, cross-over probability =  
 246 0.9 and mutation rate = 0.1.

247 **3.4 Coordination model**

248 The above procedures could realize a quick impoundment policy but fail to make  
 249 further water resource utilization. Finally, yet importantly, the problem is how to  
 250 excavate water potential.

251 **3.4.1 Objective function and constraints**



252 For large-scale impoundment operations in China, reservoir release usually  
 253 generates hydropower and then is transmitted to water consumers. As  $IE$  and  $FCR$   
 254 occupy the highest priority, hydropower has to comply with the impoundment rules. A  
 255 good impoundment rule is to ensure that the impoundment quality of the reservoir is  
 256 achieved besides maximizing hydropower generation.

257 To this end, the corresponding coordination model is introduced below, which  
 258 maximizes the annual hydropower generation of the  $i$ th pool ( $E_i$ ):

$$259 \quad \max E_i = \frac{1}{Y} \sum_{n=1}^{M_i} \sum_{t=1}^{T \cdot Y} N_{i,n}(t) \cdot \Delta t, \quad N_{i,n}(t) = A_{i,n} Q_{i,n}(t) H_{i,n}(t) \quad (11)$$

260 where  $A_{i,n}$  is the power coefficient of the  $n$ th reservoir of the  $i$ th pool;  $H_{i,n}(t)$  is the  
 261 powerhead of the  $n$ th reservoir of the  $i$ th pool at time  $t$ ; other symbols refer to Section  
 262 3.3.2.

263 Except for the constraints described in Section 3.3.2, the additional constraints in  
 264 Eq. 12 and Eq. 13(a-b) for each pool must be met during the whole period.

$$265 \quad IE_i = \frac{1}{Y} \sum_{y=1}^Y \frac{\sum_{n=1}^{M_i} (VE_{i,n}(y) - SD_{i,n})}{\sum_{n=1}^{M_i} (SU_{i,n} - SD_{i,n})} \geq IE_i^* \quad (12)$$

$$266 \quad FCR_i \leq FCR_i^* \quad (13a)$$

$$267 \quad FCR_i = \max \left\{ \frac{\sum_{n=1}^{M_i} (V_{i,n}(t) - SS_{i,n}(t))}{\sum_{n=1}^{M_i} (SU_{i,n} - SS_{i,n}(t))}, 0 \right\}, \quad (0 < t \leq T \cdot Y) \quad (13b)$$

268 where initial  $IE_i^*$  and  $FCR_i^*$  of the  $i$ th pool are determined by Pareto Frontier in the  
 269 PSO framework.

### 270 3.4.2 Parallel progressive optimization algorithm (PPOA)

271 Recently, PPOA (Feng et al., 2018b) has emerged as a means of improving initial



272 solution quality. It can use abundant multi-core configuration to improve execution  
273 efficiency while keeping the performance of the standard progressive optimization  
274 algorithm (POA). The details of PPOA can be further referred to in other literature  
275 (Feng et al., 2018b; Xie et al., 2015). Here is illustrated as an example of PPOA with 3-  
276 reservoir and 3 levels per reservoir (in Fig. 5). Fig.5 shows that all the calculations of  
277 the 27 ( $=3^3$ ) state combinations are completely independent of each other for a single  
278 sub-problem. In other words, the fitness value of any one state combination has no  
279 influence on other state combinations, which reveals the good parallelism features.  
280 PPOA adopts a successive approximation strategy to gradually improve solution quality,  
281 which will make more sense with the dimensional expansion.

282 <Please insert Fig. 5 here>

## 283 **4 Results**

### 284 **4.1 Pareto Frontiers of NSGA-II between *IE* and *FCR***

285 With the help of the NSGA-II algorithm, a wide array of Pareto Frontier is  
286 explored within allowable impoundment storage capacity (in Table 2) and subsequently,  
287 *COR* serves as the benchmark. The initial *IE* and *FCR* values of the extensively  
288 distributed Pareto Frontier and the *COR* result for the whole research basin are  
289 visualized in Fig. 6.

290 <Please insert Table 2 here>

291 <Please insert Fig. 6 here>

292 Fig. 6 shows that the improvement of one objective is bound to be followed by the  
293 sacrifice of another objective. But these Pareto Frontiers still are able to adjustably  
294 counterbalance *IE* and *FCR* simultaneously. More specifically, the optimal initial *FCR*



295 solution (Solution ① in Fig. 6) can be considered while a wet inflow scenario during  
296 the impoundment horizon is predicted in advance; on the contrary, the optimal initial  
297 *IE* solution (Solution ③ in Fig. 6) could be more appropriate in a dry impoundment  
298 scenario; at the end, the compromised initial solutions can be competent for different  
299 impoundment scenarios with medium-scale inflow hydrograph.

300 We use the universal projection pursuit method (PP) (Friedman, 1987; He et al.,  
301 2020) to evaluate the quality of all the Pareto Frontiers. PP can transform the 2-  
302 dimensional values (*IE* and *FCR* values) to one-dimensional data with the help of the  
303 projection vector and rank all solutions according to the one-dimensional value.  
304 Because the possibility of large-scale flood events decreases over impoundment time,  
305 these Pareto solutions with latter *FCR* appearance time are more preferred by decision-  
306 makers. Finally, the Pareto Frontier (whose *IE* and *FCR* values are 94.16% and 0.06,  
307 respectively) is selected as the initial optimal solution (Solution ② in Fig. 6). Solution  
308 ① and ③ are also included in the next sections, as Solution ① always produces  
309 much higher *IE* than *COR* when there is no flood control risk ( $FCR = 0$ ); Solution ③  
310 makes a better deal with joint impoundment operation in dry scenarios when the  
311 influence of flood control can be ignored.

#### 312 4.2 Optimal results of the final impoundment policies

313 We improved these three alternatives (i.e., Solution ①, ②, and ③) by the  
314 PPOA and obtained the final three representative impoundment policies (I, II and III)  
315 accordingly.

##### 316 4.2.1 Behavior performance between *IE* and *FCR*



317           The relationships between *IE* and *FCR* of the impoundment policies I, II, III as  
318 well as COR for each of the 30 reservoirs are shown in Fig.7. Fig. 7 can easily  
319 distinguish the numerical changes (i.e. the *IE* and *FCR* increment) of reservoirs. For  
320 example, Reservoir D4 occupies the maximum *IE* value of 99.78% and Reservoir G1  
321 occupies the maximum *FCR* value of 0.13. For Reservoir D4 with the maximum *IE*, it  
322 illustrates that there is enough inflow in pool D to contribute to its small impoundment  
323 storage, but upstream reservoirs with larger impoundment storage (Reservoirs D2 and  
324 D3) in the same pool are difficult to fill up, even if their *FCR* value slightly increase.  
325 Reservoir G1 has the maximum *FCR* value because Pool G fails to regulate massive  
326 water from the upstream tributaries and large interval catchment area. Reservoir G1  
327 also has an ideal *IE* result yet leaves inadequate storage to control flood risk, once it  
328 activates the pre-set principle of raising the reservoir water level. In addition, it is  
329 obvious that under the benchmark of COR, some of the other reservoirs can get better  
330 *IE* improvement with a little or no *FCR* increase. For example, when the optimal  
331 impoundment policy I is adopted, the *IE* increase of the four reservoirs in pool C varies  
332 from 1.41% to 11.84%, while flood control standard remains unchanged (*FCR* is still  
333 0). This means that: (1) these two pre-set strategies can have only positive effects on  
334 impoundment operation when they are reasonably regulated; (2) the larger the required  
335 impoundment storage of a reservoir, the better the potential impoundment prospect. The  
336 sharp *IE* improvement of Reservoir G1 with the largest impoundment storage further  
337 proves it. Reservoir G1 increases *IE* from 85.66% of COR to 94.64% of the  
338 impoundment policy I (i.e. 1.99 billion m<sup>3</sup> increment of impoundment storage). By





339 contrast, the *IE* increment of reservoirs in pool A (except for Reservoir A6) and pool B  
340 is relatively less, where these reservoirs with smaller impoundment storage are operated  
341 by just lifting water level but remaining the initial impoundment timing unchanged.

342 <Please insert Fig. 7 here>

343 Fig. 7 also contains other significant information. Pools A, B, and F are not  
344 sensitive to *FCR*. Their maximum *FCR* values are still 0 under our proposed  
345 impoundment policies. It implies that these pools have enough flood control storage to  
346 deal with relatively easier flood control tasks. With the implement of the impoundment  
347 policy III, the other four investigative pools (C, D, E, and G) suffers from different  
348 degrees of flood control risk, especially Reservoir G1 (*TGR*) in pool G. Aiming at *FCR*  
349 varieties of Reservoir D2, D3 and D4 (in the same tributary) which are equipped with  
350 synchronous impoundment operations (i.e. all the impoundment timings start at Sep.  
351 20th and end on Oct. 31st), it shows that the maximum *FCR* value decreases from  
352 upstream to downstream. The geographic elevations of these reservoirs have a  
353 substantial influence on their *FCR* distribution with the impact of spare reservoir  
354 storage. When runoff flows along cascade reservoirs, the upstream reservoir gives  
355 priority to storage volumes increment to lift water levels, which causes a decrease of  
356 downstream reservoir inflow. Consequently, the maximum *FCR* value of the  
357 downstream reservoir can be obviously reduced. Nevertheless, with the staggered  
358 impoundment time, these *FCR* values (e.g., Pool C) do not follow the principle of  
359 sequential decrease of Pool D. The *FCR* varieties of these reservoirs equipped with  
360 asynchronous impoundment operations in the same pool are more complicated to be



361 analyzed.

#### 362 **4.2.2 Impact of optimal impoundment policies on hydropower generation**

363 In this study, hydropower generation is the only indicator to assess water resource  
364 utilization of each pool. It is necessary to analyze the impact of the optimal  
365 impoundment policies on hydropower generation with comparison to COR. For the  
366 COR rule, the total simulated hydropower of the seven pools is 203.3 billion kWh. The  
367 top three are Pool C, G, and A, whose proportions are 43.04%, 20.78% and 14.18% (in  
368 Fig. 8), respectively. The sum of them is more than 75%. Hence, these three pools  
369 should be more focused when the PPOA algorithm coordinates individual reservoirs.

370 <Please insert Fig. 8 here>

371 We set the maximum number of iterations of the PPOA algorithm for Pool A, C,  
372 and G larger than other pools. Fig. 9 gives the hydropower generation results of seven  
373 pools with three different impoundment rules. It indicates that the optimal  
374 impoundment rules I, II and III can increase hydropower generation of the COR rule  
375 by 3.11%, 3.79%, and 3.89%, respectively. The top three growth rates are Pool G, C,  
376 and A. Especially, we can realize the huge potential hydropower of Pool G as its growth  
377 rate ranging from 5.26% to 7.41%. The reason owes to that Pool G possesses abundant  
378 water resources, where Reservoir G1 (TGR) is the largest hydropower plant in the world  
379 and Reservoir G2 (GZB) is one run-of-river hydropower plant. They can generate  
380 hydropower by converting kinetic energy into electricity more efficiently. Pool C can  
381 also increase hydropower by 3.27%~4.07%. It increases so much hydropower outputs  
382 because its four reservoirs located along the mainstream of the Yangtze River are



383 equipped with large installed hydropower capacity (47.81 GW in total, see Table 1),  
384 thereinto, Reservoir C2 (BHT) is the second-largest hydropower station in China.  
385 However, the growth rates of hydropower of the other five pools are not obvious, even  
386 if there are six reservoirs in Pool A and seven reservoirs in Pool G. They stay low  
387 efficiency from potential energy to electricity, since they store limited water resources  
388 for future use.

389 <Please insert Fig. 9 here>

390 Moreover, Fig. 10 visualizes the hydropower increment of each pool in different  
391 streamflow scenarios (assumed that one year represents one scenario). It shows more  
392 hydropower details. It can be inferred that the optimal impoundment policy II is more  
393 suitable for all scenarios in comparison with the impoundment I or III. Policy II and III  
394 tap more hydropower potential of Pool C, G than I, but the flood control risk of II is  
395 smaller than III. The hydropower increments of Pool A for policy II level off, which  
396 illustrates that its impoundment rule is suitable for all the (wet, normal and dry)  
397 scenarios. The hydropower increments of Pool B, D, E, and F incur a negative loss in  
398 several dry scenarios, despite their annual average output present an increase. The slight  
399 adverse changes in these dry years are due to when the upstream reservoirs in these  
400 pools need more water to fill up their impoundment storage, the negative effect of the  
401 reduced generation discharge overweight the positive effect of the raising water head  
402 in the same time.

403 In addition, the hydropower growths of Pool C and G vary greatly with scenarios.  
404 It further reveals that due to the complex hydraulic connections among the pools, the



405 single impoundment rule of Pool C and G cannot deal with all scenarios.

406 <Please insert Fig. 10 here>

#### 407 **4.3 Other evaluation indicators**

408 Advanced joint impoundment operation will not only enhance water supply and  
409 hydropower generation but also make other benefits including economy, CO<sub>2</sub> emission  
410 reduction and so on, since it involves many factors directly or indirectly related to  
411 impoundment efficiency (Zhou et al., 2018). Here we present the boxplot of the outflow  
412 of all the seven pools (A–G) during the impoundment horizon to reveal its positive  
413 influence on downstream.

414 Fig. 11 intuitively shows that the optimal impoundment policy II can improve  
415 downstream streamflow requirements by altering its outflow distribution. For example,  
416 it keeps the minimum downstream streamflow in Pool G no lower than 8000 m<sup>3</sup>/s in  
417 order to meet ecological needs, but the COR rule fails to satisfy this requirement in  
418 some dry scenarios. Moreover, it ensures downstream streamflow no higher than 39,900  
419 m<sup>3</sup>/s for downstream flood control in most years and 54,000 m<sup>3</sup>/s for its own flood  
420 control safety in a few wet scenarios. It still behaves well than the COR rule to alleviate  
421 pressure on downstream flood control, where its maximum downstream streamflow is  
422 lower than that of the COR rule.

423 <Please insert Fig. 11 here>

#### 424 **5 Discussion**

425 Due to the classification-aggregation-decomposition approach we put forward in  
426 this study, the novel framework of deriving joint impoundment rules can effectively



427 overcome the tricky ‘curse of dimensionality’. In order to explore the computational  
428 efficiency of this method, we work in a Matlab environment equipped with a Windows  
429 system (Intel<sup>R</sup> Core<sup>TM</sup> i5-4590 CPU @ 3.30 GHz and 8.00 GB of RAM) and list the  
430 results of calculation time for different numbers of pools (shown in Fig. 12). Fig. 12  
431 indicates that computational time increases with the number of pools, but does not  
432 increase exponentially with the number of reservoirs. It owes to the fact that in our  
433 method, the number of decision variables depends on the number of pools rather than  
434 the number of reservoirs. Its outstanding performance will become more prominent as  
435 the scale of the research reservoir is expanded. More specifically, time increases from  
436 499 seconds to 8448 seconds when the number of reservoirs is from 6 to 30, which  
437 provides new possibilities for optimizing the so vast reservoir community in 10-days  
438 timescale. But actually, our proposed method can also optimize the daily impoundment  
439 operation of the mixed 30-reservoir system by taking about 39700 seconds (almost 11  
440 hours), when we make several experiments assuming that daily runoff value of each  
441 reservoir can be discretized to be the same as its 10-day (11-day) runoff value.

442 <Please insert Fig. 12 here>

443 In addition, the novel method also inherits the inherent advantages of the multi-  
444 objective optimization algorithm (NSGA-II here). Aiming at multi-objective reservoir  
445 management, it not only produces the most optimal solutions as we referred to in  
446 Section 4 but also generates a series of optimal strategies that can compromise well on  
447 each objective. In our case, it gives rise to the operational alternatives available to  
448 decision-makers in terms of the *IE* results.



449 Last but not least, we have to emphasize the benefits due to the introduction of the  
450 PPOA mechanism. Compared to the final optimization results of traditional  
451 decomposition strategies (i.e. Eq. (3)) (Zhang et al., 2017;Zhang et al., 2019), this  
452 method can use PPOA to boost hydropower generation of the mixed 30-reservoir  
453 system without *IE* and *FCR* distortion. The results between impoundment policies (I, II  
454 and II) and the traditional optimal solutions (①, ②, and ③) are compared. The final  
455 optimal *IE* and *FCR* results of impoundment policy I, II, III are 93.47% and 0, 94.16%  
456 and 0.06, 94.22% and 0.14, respectively. It can be seen that the *FCR* value can further  
457 be reduced (e.g., *FCR* of III is 0.14, less than that of Solution ③, 0.18). However, all  
458 three policies increase hydropower generation to varying degrees: 209.65 billion of I vs  
459 206.34 billion of ①, 211.02 billion of II vs 208.77 billion of ②, and 211.22 billion of  
460 III vs 208.98 billion of ③. It also has a positive reference on future work of large-scale  
461 flood control and hydropower operations.

## 462 **6 Conclusions**

463 This study attempts to structure an adept framework of deriving joint  
464 impoundment rules, in which the classification-aggregation-decomposition and  
465 parameter-simulation-optimization approach are coupled to deal with the complex  
466 inflow stochasticity and high dimensionality in the large-scale cascade reservoirs, and  
467 then PPOA algorithm further improves the performance of operating rules. With a case  
468 study of the mixed 30-reservoir system in the upper Yangtze River, some vital  
469 conclusions are summarized below:

470 (1) A large number of reservoirs can be classified into several pools and the



471 reservoirs in the same pool can be assembled to be an equivalent hypothetical reservoir.  
472 It proves another feasible pathway to overcoming the classical dimensionality issue in  
473 such a giant impoundment system via reducing decision variables.

474 (2) The multi-objective evolutionary algorithm coupled with the classification-  
475 aggregation-decomposition approach has powerful capabilities for the complicated  
476 cascade impoundment operation. With the help of the NSGA-II algorithm, the widely  
477 distributed Pareto Frontiers enable water resources managers to favorably decide the  
478 appropriate initial operating policies for a perfect compromise among the conflicting  
479 objectives.

480 (3) The PPOA method can help further increase hydropower generation of each  
481 pool without *IE* and *FCR* distortion. In comparison to the COR rule, our selected  
482 optimal impoundment rule can increase reservoir impoundment efficiency from 89.50%  
483 to 94.16% and hydropower generation by 7.70 billion kWh (or increase 3.79%) while  
484 the flood control risk is less than 0.06.

485

#### 486 **Data availability**

487 The inflow data and reservoir characteristics parameters of the 30-reservoir system  
488 can be accessed by writing to the authors and filling a non-disclosure agreement under  
489 certain conditions.

490

#### 491 **Author contributions**

492 SLG and SKH conceived the original idea, and they designed the methodology.



493 SKH and KBC collected the data. SKH developed the model code and performed the  
494 simulations, with some contributions from ZL, LLD, and HHB. SKH wrote the paper,  
495 SLG, CYX, and DS revised the paper.

496

#### 497 **Competing interests**

498

499 The authors declare that they have no conflict of interest.

500

#### 501 **Acknowledgments**

502 We would like to thank the Yangtze River Commission for providing research data  
503 for the reservoir community.

504

#### 505 **Financial support**

506 Our sincere gratitude goes to the fundings from the National Key Research and  
507 Development Plan (NO. 2016YFC0402206) of China, the National Natural Science  
508 Foundation of China (NO. 51879192, NO. 51879194) and China Scholarship Council  
509 (CSC).





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653



654 **List of Table**

655

656 **Table 1** Impounding times and characteristic parameters of the 30-reservoir system in  
657 seven pools (A-G) in the upper Yangtze River

658 **Table 2** The sum storage capacity of  $SS_{i,n}(t)$  of all reservoirs in the same pool at different  
659 periods (billion  $m^3$ )

660





661 **Table 1**  
 662 Impounding times and characteristic parameters of the 30-reservoir system in seven pools (A-G) in the upper Yangtze River

Pool	Reservoir	Initial time of impoundment		End time of impoundment (COR, PSO)	Annual top of buffer pool (m)	Top of conservation pool (m)	Total storage capacity (billion m <sup>3</sup> )	Storage capacity for flood control (billion m <sup>3</sup> )	Installed hydropower capacity (GW)
		COR <sup>a</sup>	PSO <sup>b</sup>						
Pool A <sup>c</sup> (middle Jinsha River)	(A1) LY	Aug. 1 <sup>st</sup>	Aug. 1 <sup>st</sup>	Sep. 30 <sup>th</sup>	1605	1618	0.81	0.17	2.40
	(A2) AH	Aug. 1 <sup>st</sup>	Aug. 1 <sup>st</sup>	Sep. 30 <sup>th</sup>	1493.3	1504	0.89	0.22	2.00
	(A3) JAQ	Aug. 1 <sup>st</sup>	Aug. 1 <sup>st</sup>	Sep. 30 <sup>th</sup>	1410	1418	0.91	0.16	2.40
	(A4) LKK	Aug. 1 <sup>st</sup>	Aug. 1 <sup>st</sup>	Sep. 30 <sup>th</sup>	1289	1298	0.56	0.13	1.80
	(A5) LDL	Aug. 1 <sup>st</sup>	Aug. 1 <sup>st</sup>	Sep. 30 <sup>th</sup>	1212	1223	1.72	0.56	2.16
	(A6) GYY	Oct. 1 <sup>st</sup>	Sep. 20 <sup>th</sup>	Oct. 31 <sup>st</sup>	1128.8	1134	2.25	0.25	3.00
Pool B (Yalong River)	(B1) LHK	Aug. 1 <sup>st</sup>	Aug. 1 <sup>st</sup>	Sep. 30 <sup>th</sup>	2845	2865	10.15	2.00	3.00
	(B2) JP	Aug. 1 <sup>st</sup>	Aug. 1 <sup>st</sup>	Sep. 30 <sup>th</sup>	1859	1880	7.99	1.60	3.60
	(B3) ET	Aug. 1 <sup>st</sup>	Aug. 1 <sup>st</sup>	Sep. 30 <sup>th</sup>	1190	1200	5.80	0.90	3.30
Pool C (Downstream Jinsha River)	(C1) WDD	Aug. 10 <sup>th</sup>	Aug. 1 <sup>st</sup>	Sep. 10 <sup>th</sup>	952	975	3.94	2.44	10.20
	(C2) BHT	Aug. 10 <sup>th</sup>	Aug. 1 <sup>st</sup>	Sep. 30 <sup>th</sup>	785	825	20.60	7.50	16.00
	(C3) XLD	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	560	600	12.67	4.65	13.86
	(C4) XJB	Sep. 10 <sup>th</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	370	380	5.16	0.90	7.75
Pool D (Min River)	(D1) ZPP	Oct. 1 <sup>st</sup>	Sep. 20 <sup>th</sup>	Oct. 31 <sup>st</sup>	850	877	1.11	0.17	0.76
	(D2) XEX	Oct. 1 <sup>st</sup>	Sep. 20 <sup>th</sup>	Oct. 31 <sup>st</sup>	3105	3120	2.80	0.87	0.54
	(D3) SJK	Oct. 1 <sup>st</sup>	Sep. 20 <sup>th</sup>	Oct. 31 <sup>st</sup>	2480	2500	2.90	0.66	2.00
	(D4) PBG	Oct. 1 <sup>st</sup>	Sep. 20 <sup>th</sup>	Oct. 31 <sup>st</sup>	841	850	5.33	0.73	3.60



	(E1) BK	Oct. 1 <sup>st</sup>	Sep. 20 <sup>th</sup>	Oct. 31 <sup>st</sup>	695	704	0.22	0.10	0.30
Pool E (Jialing River)	(E2) BZS	Oct. 1 <sup>st</sup>	Sep. 20 <sup>th</sup>	Oct. 31 <sup>st</sup>	583	588	2.55	0.28	0.70
	(E3) TZK	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	447	458	4.07	1.44	1.10
	(E4) CJ	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	200	203	2.22	0.20	0.50
	(F1) HJD	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	1138	1140	4.95	0.15	0.60
Pool F (Wu River)	(F2) DF	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	968	970	1.02	0.04	0.57
	(F3) WJD	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	756	760	2.30	0.18	1.25
	(F4) GPT	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	628.1	630	6.45	0.20	3.00
	(F5) SL	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	435	440	1.59	0.18	1.05
	(F6) ST	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	357	365	0.92	0.21	1.12
	(F7) PS	Sep. 1 <sup>st</sup>	Aug. 20 <sup>th</sup>	Sep. 30 <sup>th</sup>	287	293	1.47	0.23	1.75
	Pool G (TGR-GZB)	(G1) TGR	Sep. 10 <sup>th</sup>	Aug. 20 <sup>th</sup>	Oct. 31 <sup>st</sup>	145	175	45.07	22.15
	(G2) GZB	-	-	-	-	66	1.58	-	2.72

663 **Note:**

664 (a) COR: Conventional Operating Rule; (b) PSO: Parameterization Simulation Optimization.



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666

667 **Table 2**

668 The sum storage capacity  $SS_{i,n}(t)$  of all reservoirs in the same pool at different periods  
669 (billion  $m^3$ )

Pool	Aug.10 <sup>th</sup>	Aug.20 <sup>th</sup>	Aug.31 <sup>st</sup>	Sep.10 <sup>th</sup>	Sep.20 <sup>th</sup>	Sep.30 <sup>th</sup>	Oct.10 <sup>th</sup>	Oct.20 <sup>th</sup>	Oct.31 <sup>st</sup>
A	5.40	5.73	6.16	6.29	6.41	6.51	6.51	6.51	6.51
B	20.05	21.74	22.65	23.68	23.68	23.68	23.68	23.68	23.68
C	29.21	33.50	35.95	38.85	41.13	41.40	41.40	41.40	41.40
D	9.29	9.29	9.61	9.94	10.38	11.16	11.44	11.66	11.66
E	4.82	4.97	5.52	6.34	6.40	6.42	6.53	6.56	6.56
F	15.37	15.71	16.04	16.26	16.26	16.26	16.26	16.26	16.26
G	18.12	19.75	21.51	24.76	30.04	32.60	39.31	39.31	39.31

670 **Note:** the meaning of  $SS_{i,n}(t)$  is referred in Eq. (3).



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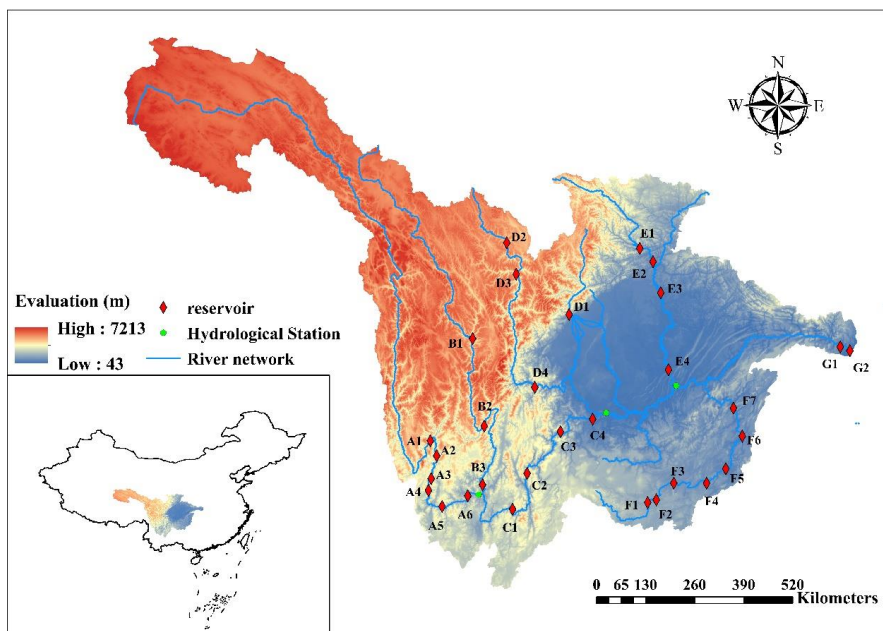
700 **Fig. 12** Computational efficiency for different numbers of pools

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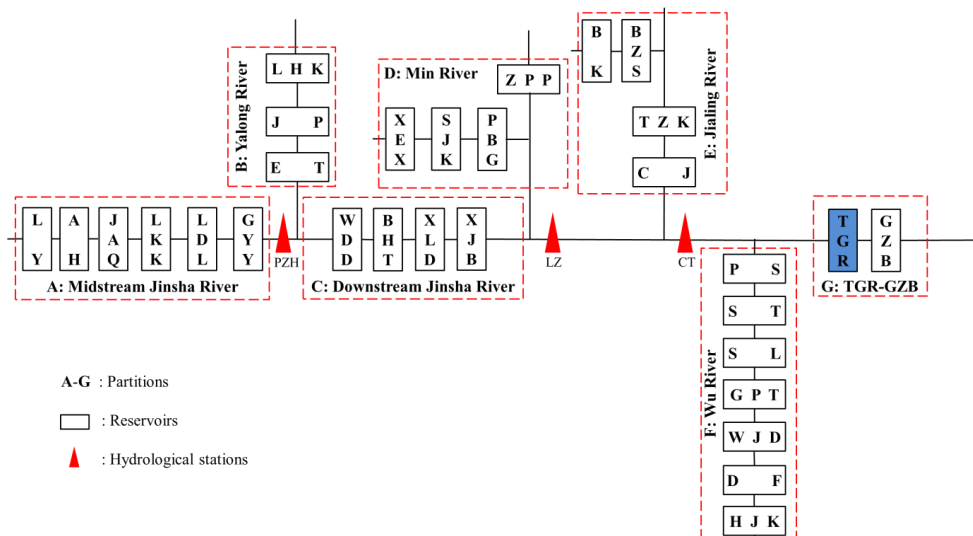


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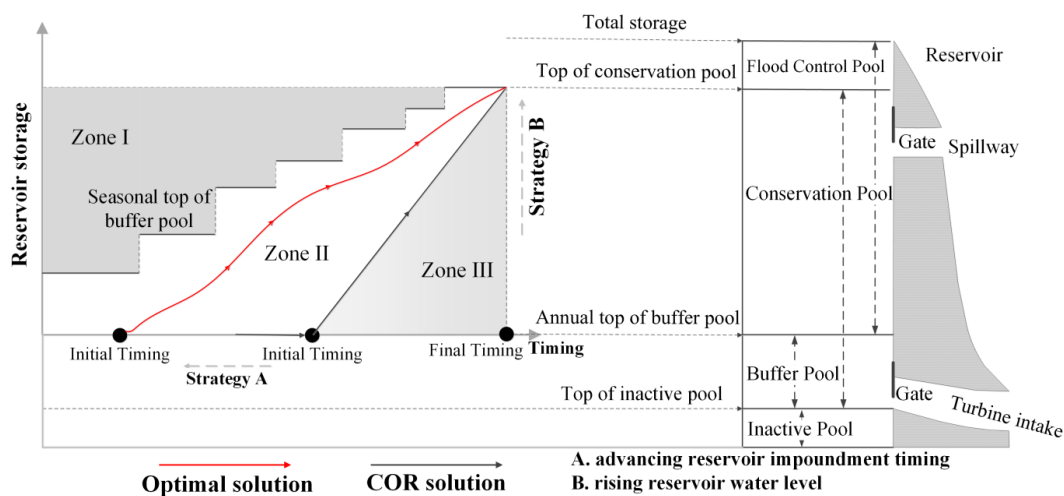
Fig. 1a Geographic distribution of the 30-reservoir system



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Fig. 1b Schematic diagram of the 30-reservoir system

**Fig. 1** Location information of the mixed 30 reservoirs in the upper Yangtze River



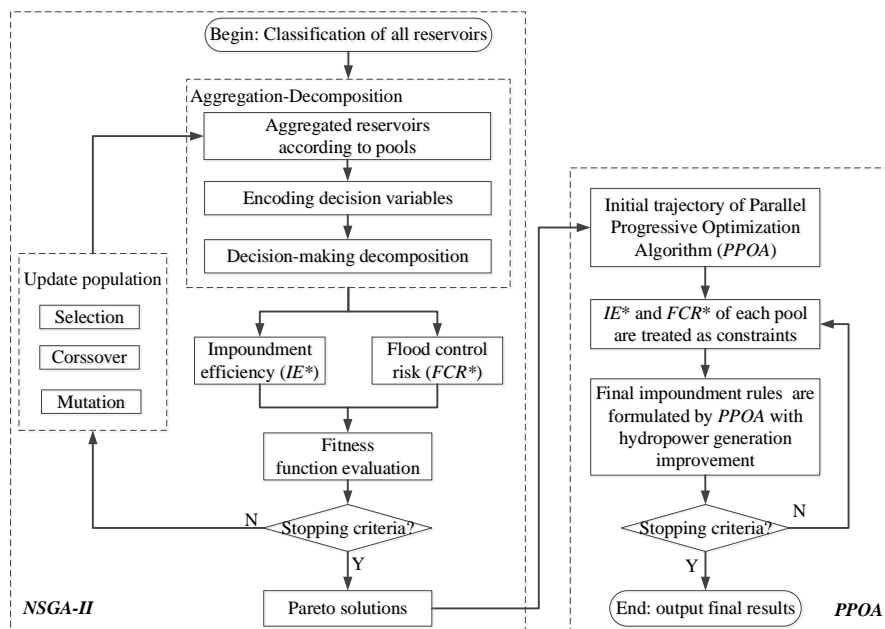
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**Fig. 2** The schematic diagram of two activate strategies for advanced impoundment



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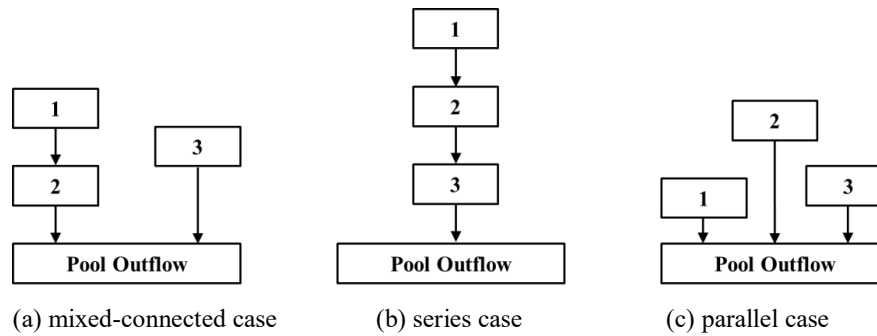
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**Fig. 3** Flowchart of deriving joint impoundment rules for the large-scale reservoir system



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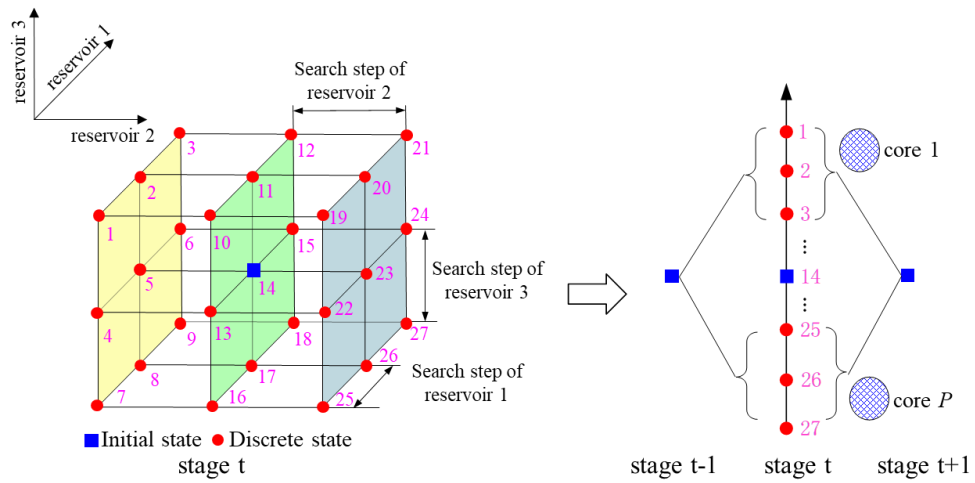
720 **Fig. 4** Three general topological cases of reservoir location  
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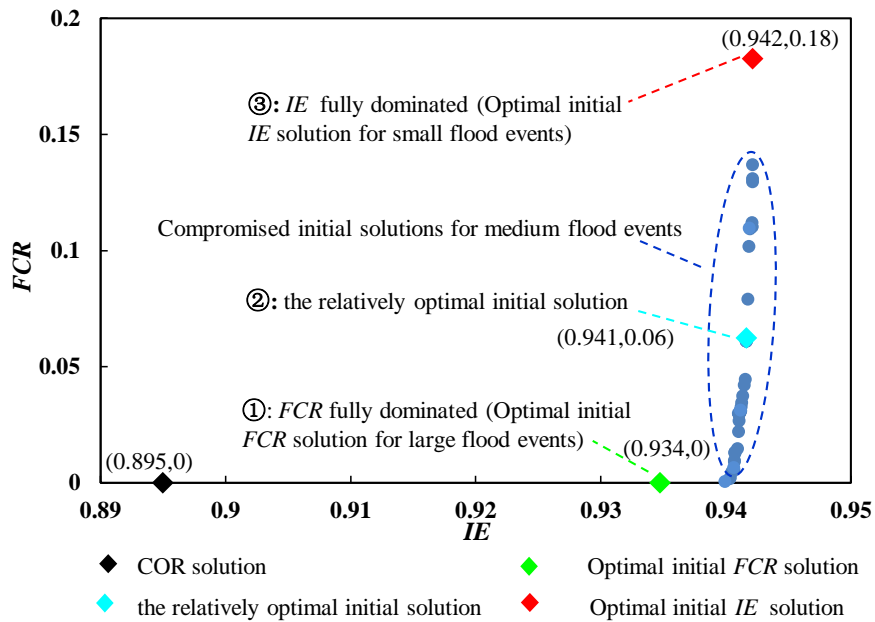
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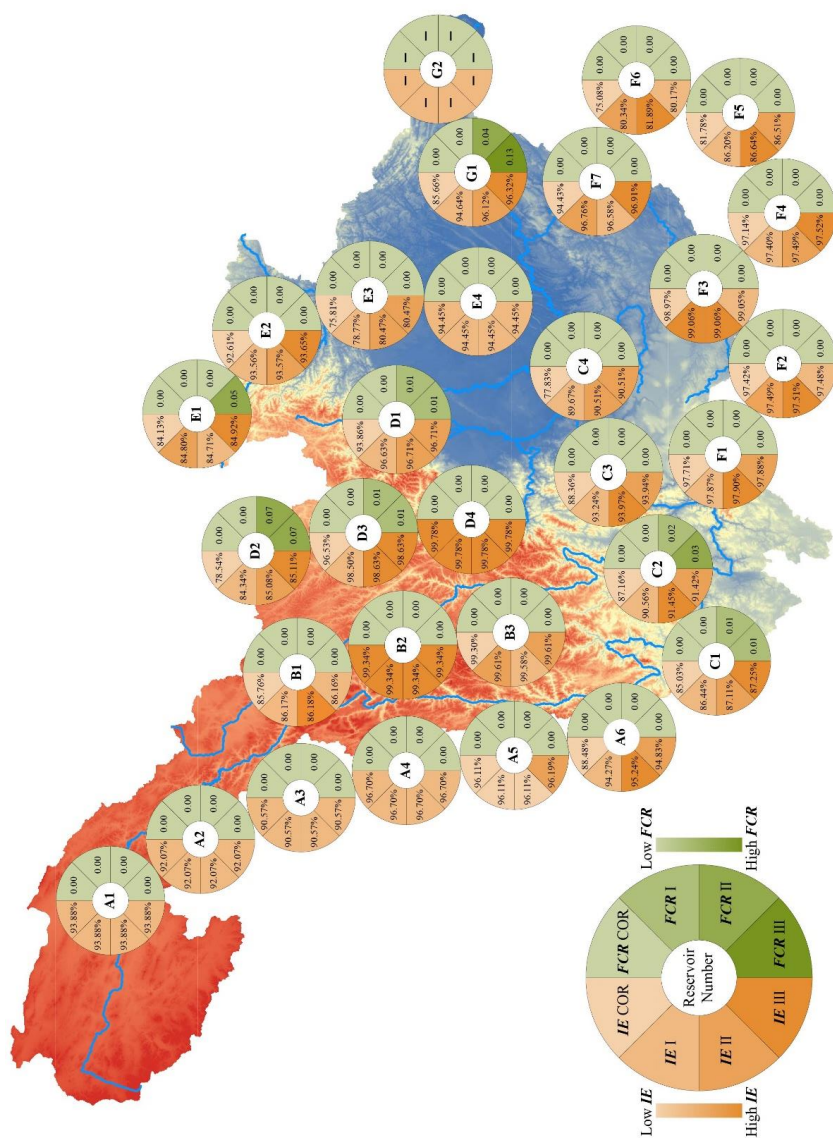
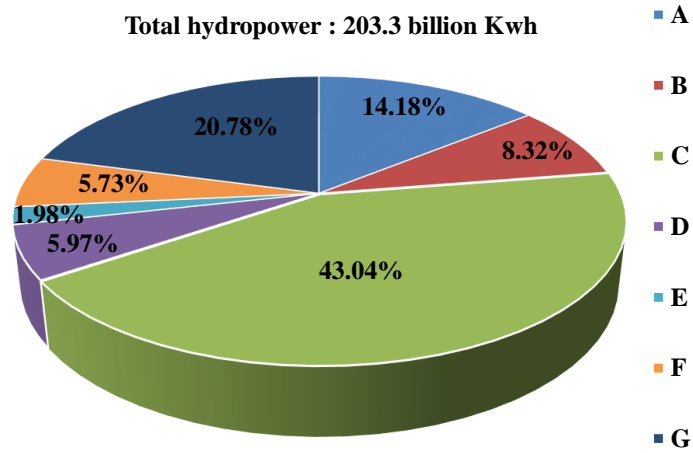


Fig. 7 Spatial varieties of IE and FCR of each reservoir relative to the different optimal impoundment rules



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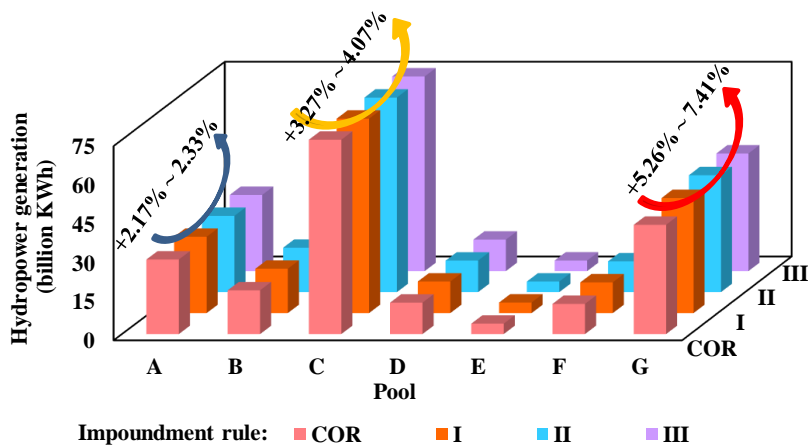


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734 **Fig. 8** Hydropower proportion of each pool based on the COR rule



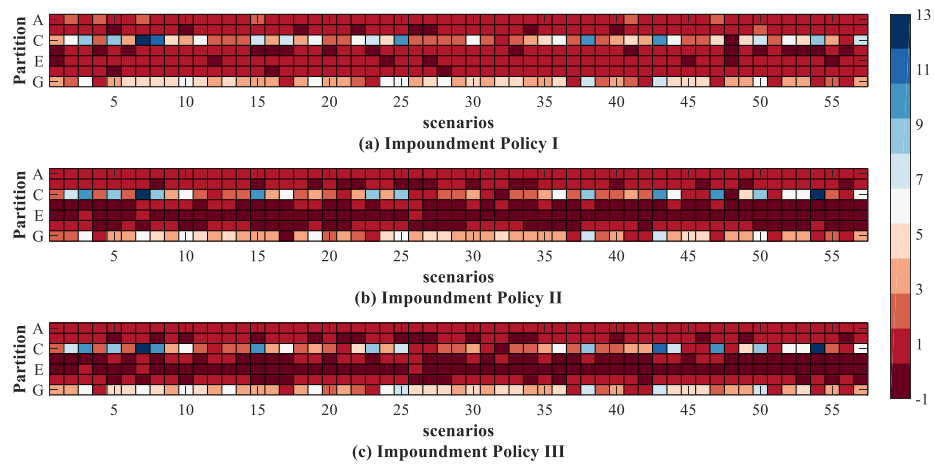
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 739 **Fig. 9** The hydropower results of the 30 reservoirs in seven pools for different  
 740 impoundment rules



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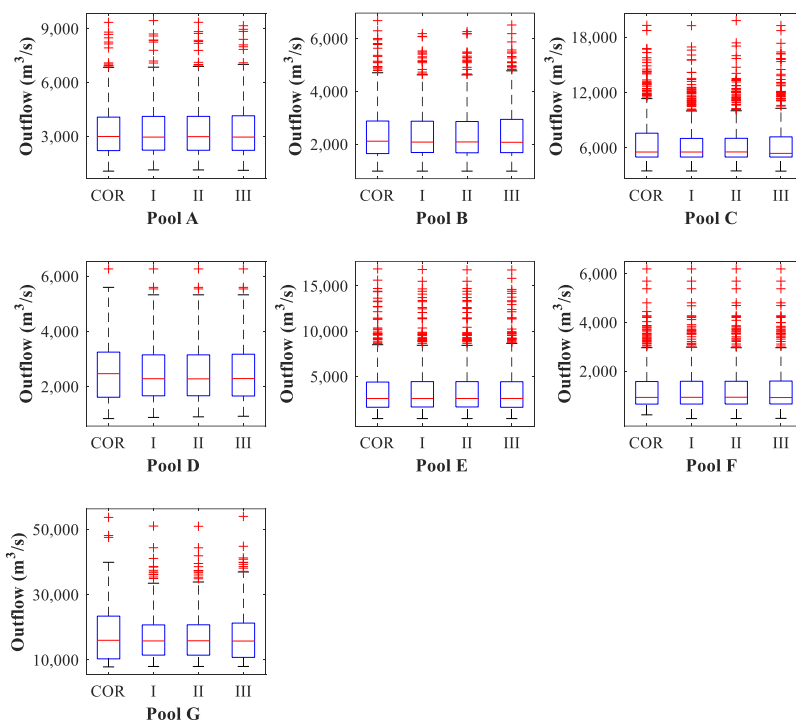


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743 **Fig. 10** Hydropower increment of seven pools (A-G) for three optimal impoundment  
744 policies compared to the COR rule in different streamflow scenarios (Unit: billion kWh)



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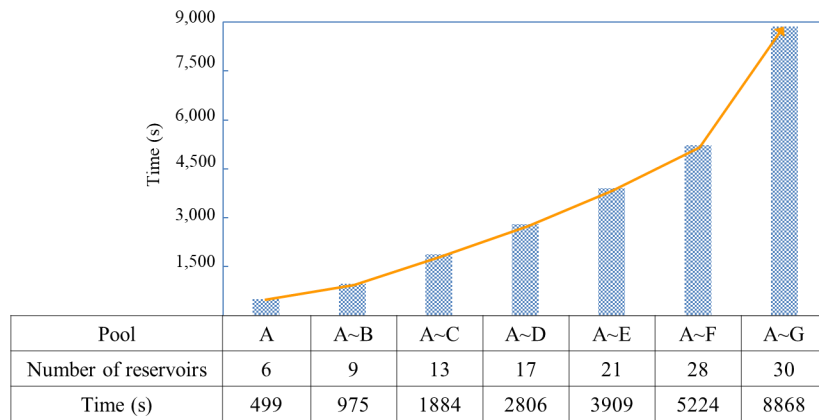
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750

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