1	Assessment of meteorological extremes using a synoptic weather generator and a downscaling
2	model based on analogues
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8	1. Abstract
9	Natural risk studies such as flood risk assessments require long series of weather variables. As an

10 alternative to observed series, which have a limited length, these data can be provided by weather 11 generators. Among the large variety of existing ones, resampling methods based on analogues have 12 the advantage of guaranteeing the physical consistency between local weather variables at each time 13 step. However, they cannot generate values of predictands exceeding the range of observed values. 14 Moreover, the length of the simulated series is typically limited to the length of the synoptic 15 meteorological records used to characterize the large-scale atmospheric configuration of the 16 generation day. To overcome these limitations, the stochastic weather generator proposed in this 17 study combines two sampling approaches based on atmospheric analogues: 1) a synoptic weather generator in a first step, which recombines days of the 20th century to generate a 1,000-year 18 19 sequence of new atmospheric trajectories and 2) a stochastic downscaling model in a second step, 20 applied to these atmospheric trajectories, in order to simulate long time series of daily regional 21 precipitation and temperature. The method is applied to daily time series of mean areal precipitation 22 and temperature in Switzerland. It is shown that the climatological characteristics of observed 23 precipitation and temperature are adequately reproduced. It also improves the reproduction of 24 extreme precipitation values, overcoming previous limitations of standard analogue-based weather 25 generators. 26

27 **2. Introduction**

28 Increasing the resilience of socio-economic systems to natural hazards and identifying the required 29 adaptations is one of today's challenges. To achieve such a goal, one must have an accurate 30 description of both past and current climate conditions. The climate system is a complex machine 31 which is known to fluctuate at very small time scales but also at large ones over multiple decades or 32 centuries (Beck et al. 2007). It is necessary to study meteorological series as long as possible in order 33 to catch all sources of variability and fully cover the large panel of possible meteorological situations. 34 Regarding weather extremes, the same need arises as estimating return levels associated to large 35 return periods cannot be successfully done without long climatic records (e.g. Moberg et al., 2006; 36 Van den Besserlaar et al., 2013). This comment also applies to all statistical analyses on any derived 37 variable, such as river discharge, for which multiple meteorological drivers come into play and for 38 which extreme events correspond to the combination of very specific and atypical hydro-39 meteorological conditions.

41 Using weather generators, long simulations of weather variables provide accurate descriptions of the 42 climate system and can be used for natural hazard assessments. Among the large panel of existing 43 weather generators, stochastic ones are used to construct, via a stochastic generation process, single 44 or multisite time series of predictands (e.g. precipitation, temperature) based on the distributional properties of observed data. These characteristics, and consequently the weather generator 45 46 parametrisation, are usually determined on a monthly or seasonal basis to take seasonality into 47 account. They can also be estimated for different families of atmospheric circulation, often referred 48 to as weather types. A state of the art of the most common methods which have been used for the 49 downscaling of precipitation (single or multi-site) is presented in Wilks (2012) or in Maraun et al., 50 (2010). More recent publications gather detailed reviews of some sub-categories of weather 51 generators (e.g. Ailliot et al., 2015 for hierarchical models). An increasing number of studies focuses 52 on the generation of multivariate and/or multi-site series of predictands (e.g. Steinschneider and 53 Brown, 2013; Srivastav and Simonovic, 2015; Evin et al. 2018a; Evin et al. 2018b). Stochastic weather 54 generators are able to produce large ensembles of weather time series presenting a wide diversity of 55 multiscale weather events. For all these reasons, they have been used for a long time to enlighten 56 the sensitivity and possible vulnerabilities of socio-eco-systems to the climate variability (Orlowsky et 57 al. 2010) and to weather extremes.

58 59 Other models used for the generation of weather sequences are based on the analogue method. 60 Since the description of the concept of analogy by Lorenz (1969), the analogue method has gained 61 popularity over time for climate or weather downscaling. This analogue model strategy has been 62 applied in many studies (Boe et al., 2007; Abatzoglou and Brown, 2012; Steinschneider and Brown 63 2013) and has been used to address a wide range of questions from past hydroclimatic variability 64 (e.g. Kuentz et al, 2015; Caillouet et al., 2016) to future hydrometeorological scenarios (e.g. Lafaysse 65 et al., 2014; Dayon et al., 2015). The standard analogue approach hypothesises that local weather 66 parameters are steered by synoptic meteorology. A set of relevant large scale atmospheric predictors 67 is used to describe synoptic weather conditions. From the atmospheric state vector, characterizing 68 the synoptic weather of the target simulation day, atmospheric analogues of the current simulation 69 day are identified in the available climate archive. Then, the analogue method makes the assumption 70 that similar large scale atmospheric conditions have the same effects on local weather. The local or 71 regional weather configuration of one of the analogue days is then used as a weather scenario for 72 the current simulation day. The key element of the analogue method is that it does not require any 73 assumption on the probability distributions of predictands. This is a noteworthy advantage for 74 predictands, such as precipitation, which have a non-normal distribution with a mass in zero. Most of 75 the studies using analogues focused on precipitation and temperature either for meteorological 76 analysis (Chardon, 2014; Daoud, 2016), or as inputs for hydrological simulations (Marty, 2012; 77 Surmaini et al., 2015). Nevertheless, analogues are increasingly used for other local variables such as 78 wind, humidity (Casanueva et al., 2014) or even more complex indices (e.g. for wild fire, Abatzoglou 79 and Brown, 2012). When multiple variables are to be downscaled simultaneously, another major 80 advantage of the analogue method is that the different predictands scenarios are physically 81 consistent and the simulated weather variables are bound to reproduce the correlations between 82 the variables (e.g. Raynaud et al., 2017) and sites (Chardon et al., 2014). Indeed, when analogue 83 models use the same set of predictors (atmospheric variables and analogy domains) for all 84 predictands, all surface weather variables and sites are sampled simultaneously from the historical 85 records, thus preserving inter-site and inter-variable dependency.

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The two simulation approaches (stochastic weather generators and analogue methods) described above present some important advantages for the generation of long weather series but also some sizeable drawbacks. Indeed, stochastic weather generators rely on strong assumptions about the statistical distributions of predictands. Identifying the relevant mathematical representations of the

91 processes and achieving a robust estimation of their parameters can be difficult, especially if the 92 length of the meteorological records is short. Modelling the spatial-temporal dependency between 93 variables/sites is often another challenge. Conversely, for the analogue-based approaches, the 94 identification of relevant atmospheric variables providing good prediction skills is not straightforward. The limited length of local weather records is also a critical issue since resampling 95 96 past observations restricts the range of predicted values. In particular, the simulation of unobserved 97 values of predictands is not possible. This can be problematic if one is interested in estimating 98 possible extreme values of the considered variable. Furthermore, the information on synoptic 99 atmospheric conditions required by analogue methods are generally coming from atmospheric 100 reanalyses, which also have a limited temporal coverage (e.g. from the beginning of the 20th century for ERA20C, Poli et al., 2013) and from the mid-19th century for 20cr (Compo et al. 2011). The length 101 102 of the generated time series is thus typically bounded by the length of the reanalyses.

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104 In this study we propose a weather generator (hereafter SCAMP+) building upon the SCAMP 105 approach presented by Chardon et al. (2018) and making use of reshuffled atmospheric trajectories, 106 following some of the developments by Buishand and Brandsma (2001) and Yiou et al. (2014). The 107 weather scenarios generated by SCAMP being limited by the coverage of the climate reanalyses, the 108 SCAMP+ model extends the pool of possible atmospheric trajectories. Using random transitions 109 between past atmospheric sequences, SCAMP+ generates unobserved atmospheric trajectories, on 110 which the 2-stage SCAMP approach can be applied. By exploring a wide variety of atmospheric 111 trajectories, SCAMP+ introduces some additional large-scale variability which improves the 112 exploration of possible weather sequences. In addition, as done in SCAMP (Chardon et al., 2018), the 113 SCAMP+ approach includes a simple stochastic weather generator which is estimated, for each generation day, from the nearest atmospheric analogues of this day. These two steps (random 114 115 atmospheric trajectories and random daily precipitation/temperature values) improve the 116 reproduction of extreme values, overcoming previous limitations of analogue-based weather 117 generators, usually known to underestimate observed precipitation extremes.

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119 These developments are carried out for the exploration of hydrological extremes (extreme floods) of 120 the Aare River basin in Switzerland (Andres et al. 2019a,b). Meteorological forcings, i.e. temperature 121 and precipitation, are thus simulated to be used as inputs of a hydrological model, for different sub-122 basins of the Aare river basin. Meteorological simulations from SCAMP+ have been used in the Swiss 123 EXAR project¹ and have proven its ability to estimate the discharge values associated to very large 124 return periods on the Aare River. In section 2, we describe in details the test region, the data and 125 three simulation approaches (a classical analogue method, referred to as ANALOGUE, SCAMP and 126 SCAMP+). Section 3 presents the main results on both climatological characteristics and extreme 127 values. Section 4 sums up the main outputs of this study and proposes some further developments 128 and analysis.

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3. Data and Method

132 3.1 Studied region

This study is carried out on the Aare River basin which covers almost half of Switzerland (17,700 km²). The topography varies greatly within the basin with, on one hand, high mountains on its southern part (maximum altitude of 4270 m, Finsteraarhorn) and on the other hand, plains on the

¹ https://www.wsl.ch/en/projects/exar.html

northern part (minimum altitude of 310 m). These different characteristics coupled with the basin
being located at the crossroads of several climatic European influences give a wide diversity of
possible weather situations across the year.

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140 3.2 Atmospheric reanalysis and local weather data

141 The application of the analogue method requires a long archive providing an accurate description of 142 both past synoptic weather patterns and local atmospheric conditions. Indeed, a wide panel of 143 meteorological situations available for resampling is necessary in order to identify the best analogues 144 for the simulation (e.g. Van Den Dool et al., 1994; Horton et al., 2017). In most studies, synoptic 145 situations are provided by atmospheric reanalyses. Here, we use the ERA-20C atmospheric reanalysis 146 (Poli et al., 2013) which provide information on large scale atmospheric patterns on a 6 h basis from 147 1900 to 2010. Data are available at a 1.25° spatial resolution. More specifically, the set of predictors 148 used for the identification of atmospheric analogues is made of the geopotential height at 500 and 149 1000 hPa, the vertical velocities at 600 hPa, large scale precipitation and temperature. The 150 justification of these choices will be given in section 3.3.1.

151 The local and surface weather parameters of interest are retrieved from 105 weather stations for 152 precipitation and 26 weather stations for temperature, which are spread out homogeneously over 153 our target region, as presented on Figure 1. These data are available at a daily time step from 1930 to 154 2014. They have been spatially aggregated in order to obtain daily time series of mean areal 155 precipitation (MAP) and temperature (MAT) for the Aare region. The three weather generators 156 considered in this study aims at producing scenarios of daily time series of MAP and MAT. In this 157 study, a scenario is defined as a possible realization of the climate system under current climate 158 conditions (i.e. the climate observed for the past few decades). It can be noticed that many 159 applications of analogue-based approaches produce simulations at specific weather stations. 160 However, as shown by Chardon et al. (2016) for France, the prediction skill is significantly improved 161 when the prediction is produced for areal averages, which motivates the generation of MAP and 162 MAT values in this study.



Fig.1: The Aare River basin (red) and locations of the different precipitation (dots) and temperature(triangles) stations.

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168 3.3 Description of the three models

- 169 This section presents the three different models considered and evaluated in this study.
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171 3.3.1 ANALOGUE: Classical analogue model

172 The most basic model evaluated in this study, hereafter referred to as ANALOGUE, relies on a 173 standard 2-level analogue method. For each day of the simulation period (1900 – 2010), analogue 174 days are identified from candidate days. The candidate days, extracted from the archive period, i.e. 175 the period on which both predictors and local observations are available (1930 – 2010), are all days 176 of the archive located within a 61-day calendar window centred on the target day. This calendar filter 177 is expected to account for the possible seasonality of the large scale / small scale downscaling relationship. For instance, candidate days for May 15th 2000 are selected within the pool of days 178 ranging from April 15th to June 14th of each year of the archive. 179

The predictors used for the analogues selection been chosen based on Raynaud et al. (2017). They have been shown to guarantee both inter-variable physical consistency and good predictive skills according to the Continuous Ranked Probability Skill Score (CRPSS), for 4 predictands (precipitation, temperature, solar radiation and wind). In the present work, the predictors considered for each level for the two-level analogy are as follows:

The first level of analogy is based on daily geopotential heights at 1000 hPa and 500 hPa (HGT1000,
 HGT500) as proposed by Horton et al. (2012) and Raynaud et al. (2017). The analogy criterion used
 here is the Teweles–Wobus score (TWS) proposed by Teweles and Wobus (1954). This score has
 been found to lead to higher performances than a more classical Euclidian or Malahanobis distance

189 (Kendall et al. 1983; Guilbault et Obled, 1998; Wetterhall et al., 2005). It quantifies the similarity 190 between two geopotential fields by comparing their spatial gradients. It allows selecting dates that 191 have the most similar spatial patterns in terms of atmospheric circulation. From September to May, 192 the analogy is based on the geopotential fields on both the current day D and its following day D+1 at 193 12UTC. Thereby, the motions of low-pressure systems and fronts are better described and the 194 prediction skill of the method for precipitation is improved (e.g. Obled et al. 2002; Horton and 195 Brönnimann, 2019). In summer, only the geopotential fields on the current day are used as no similar 196 improvement could be found with a two-day analogy. During this first analogy level, 100 analogues 197 are selected for each day of the target period.

198 - The second analogy level makes a sub-selection of 30 analogues within the 100 analogues identified 199 in the first analogy level. The analogy score used for the selection is the Root Mean Square Error 200 (RMSE). From September to May, the predictors are the vertical velocities at 600 hPa and the large 201 scale temperature at 2 meters. In summer, the vertical velocities but also other predictors such as 202 the Convective Available Potential Energy (CAPE) led to a rather poor prediction of precipitation due 203 to the coarse resolution of the atmospheric reanalysis, which prevent it from providing an accurate 204 simulation of convective processes. Consequently, large scale precipitation from the reanalysis has 205 been used as a predictor instead, resulting in predictive skills similar to the ones obtained for the rest 206 of the year. The different predictor sets retained for summer and the rest of the year illustrate the 207 differences typically observed between seasons for the main meteorological conditions and 208 processes.

The dimensions and position of the different analogy windows used to compute the analogy measures are presented on Figure 2. They follow the recommendations for the analogy windows optimisation presented in Raynaud et al. (2017) for all predictors.

212 With this 2-step analogy, 30 scenarios of daily MAP and daily MAT are obtained for each day of the

simulation period (1900-2010). Combined with the Schaake Shuffle method described in section
 3.3.4, the application of the ANALOGUE model leads to 30 scenarios of 110-year time series of daily

215 MAP and MAT.



Fig.2: Positions and dimensions of the analogy windows in the analogue model at both analogy levels. Z500,
 geopotential at 500 hPa ; Z1000, geopotential at 1000 hPa ; VV600, vertical velocities at 600 hPa ; P,
 precipitation ; T, temperature.

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221 3.3.2 SCAMP: Combined analog / generation of MAP and MAT values

The SCAMP model enhances the previous ANALOGUE approach which is not able to generate daily values exceeding the range of observed precipitation and temperature. SCAMP combines the analogue method with a day-to-day adaptive and tailored downscaling method using daily distributions adjustment (Chardon et al. 2018).

For each prediction day, the following discrete-continuous probability distribution proposed by Stern and Coe (1984) is fitted to the 30 MAP values obtained from the atmospheric analogues of this day:

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$$F_Y(y) = (1 - \pi) + \pi \cdot F_{GA}(y|y > 0, \alpha, \beta), \qquad (1)$$

where π is the precipitation occurrence probability, F_{GA} is the gamma distribution parameterized with a shape parameter $\alpha > 0$ and a rate parameter $\beta > 0$. The π parameter is directly estimated by the proportion of dry days, and the parameters α , β of the gamma distribution are estimated by applying the maximum likelihood method to the positive precipitation intensities among the 30 MAP values. 30 MAP values are then sampled from the distribution model (1) in order to obtain unobserved values of precipitation, possibly beyond past observations. When there are less than 5 positive MAP intensities in the analogues, we simply retrieve the MAP analog values. This distribution model corresponds to a simplified version of the combined analogue/regression model described inChardon et al. 2018 and we refer the reader to this paper for further information.

Similarly, for each prediction day, a Gaussian distribution $F_N(\mu, \sigma)$ is fitted to the 30 MAT values obtained from the analogues. A sample of 30 new MAT values is then generated from this fitted Gaussian distribution.

As for the ANALOGUE approach, the Schaake Shuffle reordering method is applied to the daily scenarios obtained from SCAMP. 30 scenarios of 110-year time series of daily MAP and MAT are produced.

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245 3.3.3 SCAMP+

As mentioned previously, the first limitation of the analogue method is related to the length of the synoptic weather information that is used to generate local predictands time series. In the present case, the length of time series that can be produced with the models ANALOGUE and SCAMP is limited to 110-year long weather scenarios.

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251 In SCAMP+, we extend the archive of synoptic weather information by rearranging the synoptic weather sequences, thus creating new atmospheric trajectories, used in turn as inputs to SCAMP. 252 253 This generation of new trajectories makes use of atmospheric analogues, following those of the 254 principles proposed in the weather generators described by Buishand and Brandsma (2001) and Yiou 255 et al. (2014). For any given day, the atmospheric synoptic weather is considered to have the 256 possibility to change its trajectory. The main hypothesis of this generation module is that if two days 257 J and K are close atmospheric analogues with atmospheric patterns heading in the same direction, 258 then their "future" are exchangeable and one could jump from one atmospheric trajectory to the 259 other. In other words, day J+1 is a possible future of day K and conversely day K+1 is a possible future 260 of day J. The probability p to jump from one trajectory to any other is considered as a parameter to 261 estimate.

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The principle of a random atmospheric trajectory generation is sketched on Figure 3. In the present 263 264 work, the only predictor involved to compare the synoptic atmospheric configuration between 2 265 different days is the geopotential height field at 1000 hPa, for both the present day and its followers. 266 The spatial analogy domain is the one used in Philipp et al. (2010) for the identification of Swiss weather types. The first line of Figure 3 presents an observed atmospheric trajectory in HGT1000 267 from February 8th to February 12th 1934. On the February 9th, we look for analogues of the current 268 day and its following day D+1. This is done to ensure that the two initial states are similar (high 269 pressure system located over France on February 9th 1934 and on its analogue, January 28th 1921) 270 and that the main features move in similar directions (high pressure system heading South-East on 271 both February 10th 1934 and January 29th 1921). 272

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Practically, the five best analogues of the current atmospheric 2-day sequence are identified and one of those sequences is then selected with a probability p to generate the new day of the new trajectory. The same method is repeated for this new day to find its future day (as illustrated in Figure 3 for the sequence January 30th 1921 - February 12th 1925) and extend the new trajectory with one additional day. This process is repeated as long as necessary. In the present work, it was used to generate a 1000-year trajectory of daily synoptic weather situations. Rather large differences between the synoptic weather situation can be obtained after some days between the observed atmospheric sequence (e.g. February 12th 1934) and the random atmospheric trajectory (February 12th 1925). As we will show later on, such a method leads to higher weather variability at multiple time scales.

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To insure that two consecutive days of the generated sequences belong to the appropriate season, the five 2-day analogue sequences are identified within a +/-15-day moving window centred on the

calendar day of the target simulation day (e.g. all June days if the target day is xxxx-06-15th).

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Fig.3: Construction of a new 5-day atmospheric trajectory from an observed synoptic weather sequence. Each sub-figure presents the geopotential at 1000hPa on the domain of interest. The black squares and arrows give the new atmospheric trajectory and the blue shading highlights the two-day analogue that helps "changing of atmospheric direction".

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295 The transition probability p from one observed trajectory to another indirectly determines the level 296 of persistency of synoptic configurations. In this study, it has been calibrated in order to guarantee a 297 good climatology of the large scale atmospheric sequences. To do so, we analysed the mean 298 frequency and duration of each of the 9 weather types proposed for Switzerland by Philipp et al. (2010) in the observed synoptic series and in different reconstructed ones for transition probability p 299 300 ranging from 1/10 (one transition every 10 days in average) to 1 (one transition per day in average). 301 The results presented on Figure 4 shows that a transition probability of 1/7 is necessary to generate 302 atmospheric trajectories that present a relevant persistency within each weather type.



Fig.4: Mean persistency of each of the 9 weather types (indicated by the different circles in each panel), as defined by Philipp et al. (2010), in the observed time series and in the simulated ones for transition probabilities ranging from 1 to 1/10 for the generation of atmospheric trajectories.

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The long time series of synoptic weather generated with the above approach is further used as inputs to the SCAMP generator described in the previous section. The SCAMP+ approach leads to 30 scenarios of daily MAP and MAT, each of these scenarios being based on the 1000-year random atmospheric trajectories sequence. The output of this approach, combined with the Schaake Shuffle method described in the next section, is thus composed of 30 scenarios of 1000-year time series of daily MAP and MAT.

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315 3.3.4 Temporal consistency: Application of the Schaake Shuffle

For each model (ANALOGUE, SCAMP and SCAMP+) and each day of the simulation period, 30 316 317 scenarios of daily MAP and MAT are produced. To improve the temporal/physical consistency between two consecutive days or between the temperature and precipitation scenarios (partially 318 319 induced by the synoptic weather series), we use the Schaake Shuffle method initially proposed by 320 Clark et al. (2004). This method makes use of both the inter-variable physical and the intra-variable 321 temporal consistency in observations to combine, at best, the outputs of any weather generator and 322 reconstruct consistent predictands time series. It is particularly useful if one is interested in 323 generating relevant precipitation accumulation scenarios over several days. A full description of the 324 Schaake Shuffle method can be found in Clark et al. (2004) and some applications can be found in 325 Bellier et al. (2017) or in Schefzik (2017). Here, the Schaake Shuffle consists in modifying the sequences of MAP and MAT values, preserving the association of the ranks of MAP and MAT and rearranging sequences between days D and D+1. Shuffled MAP and MAT sequences between consecutive days then have similar associations than what has been observed. In this study, we give priority to the temporal consistency of precipitation first. Temperature scenarios are recombined in a second step.

The different components of the models ANALOGUE, SCAMP and SCAMP+ are summarized in Figure5.

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335 Fig.5: Illustration of the different steps applied (grey boxes) with models ANALOGUE, SCAMP and SCAMP+.

- 336 Outputs obtained after each step are indicated in red.
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4. Results

This section presents different statistical properties of the scenarios obtained with the 3 models and discusses the performances of each model by comparison with observed statistical properties. For the sake of consistency between the outputs, we compare the 30 scenarios of 111 years obtained from ANALOGUE and SCAMP to 300 scenarios of 100 years from SCAMP+ (i.e. each scenario of 1,000 years is divided into 10 scenarios of 100 years).

344 4.1 Climatology

For both temperature and precipitation, the 3 models lead to an accurate simulation of their seasonal fluctuations (Figure 6). However, one can notice the slight overestimation of winter

temperature and an underestimation of July and August precipitation. SCAMP also tends to have asmaller inter-annual variability compared to ANALOGUE and SCAMP+.



Fig.6: Observed and simulated seasonal cycles of temperature and precipitation for ANALOGUE, SCAMP and SCAMP+. The grey shadings present the inter-quantiles intervals at 50%, 90% and 99% levels. Simulated seasonal cycles are obtained using 30 scenarios of 111 years from ANALOGUE and SCAMP and 300 scenarios of 100 years from SCAMP+.

354 The distributions of seasonal precipitation amounts and seasonal temperature averages are 355 presented in Figure 7. Whatever the season, the three models are able to generate drier and wetter 356 seasons than the observed ones (Figure 7a). The very similar results obtained for ANALOGUE and 357 SCAMP suggest that the daily distribution adjustments used in SCAMP do not introduce more 358 variability at the seasonal scale. SCAMP+ is able to generate seasonal values that significantly exceed 359 the maximum values simulated by ANALOGUE and SCAMP (by 100 mm to 200 mm). This strongly 360 suggests that a large part of the seasonal variability comes from the variability of the synoptic weather trajectories, the unobserved weather trajectories produced by SCAMP+ leading to a wider 361 362 exploration of extreme seasonal values.



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Fig.7a: Observed and simulated boxplots of seasonal precipitation amounts for ANALOGUE, SCAMP and
 SCAMP+ (Spring: March, April, May. Summer: June, July, August. Autumn: September, October, November.
 Winter: December, January, February).

The same comments can be made for spring and autumn temperatures (Figure 7b). For those variables however, SCAMP+ fails to simulate extremely hot summers or cold winters. This limitation will be further discussed in the next section with some additional analysis and opportunities for improvement.



372Fig.7b: Observed and simulated boxplots of mean seasonal temperature for models ANALOGUE, SCAMP and373SCAMP+ (Spring: March, April, May. Summer: June, July, August. Autumn: September, October, November.

374 Winter: December, January, February).

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4.2 Daily Precipitations Extremes

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As mentioned in section 1, simple analogue methods cannot simulate unobserved precipitation extremes at the temporal resolution of the simulation (here daily). Moreover, for higher aggregation durations, they also tend to underestimate observed precipitation extremes. Figure 8 presents the precipitation values obtained with the three models for different return periods (from 2 year to 200 years) and different aggregation durations (from 1 to 5 days).

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Considering 1-day extreme events, ANALOGUE is obviously not able to generate precipitation accumulations that exceed the maximum observed one. Combining the analogue method with daily distribution adjustments (SCAMP) overcomes this issue with maximum values reaching 115 mm. SCAMP+ leads to similar results.

389 The large underestimation of daily extremes obtained with ANALOGUE leads to an important 390 underestimation of 3-day and 5-day extremes. Despite a better simulation of daily values, SCAMP 391 does not improve significantly the reproduction of 3-day and 5-day extremes. SCAMP+ outperforms 392 both models for all durations, and generates precipitation extremes in agreement with observed 393 extremes. Whatever the return period, the variability between the different 100-year scenarios is 394 larger with SCAMP than with ANALOGUE and much larger with SCAMP+. This again suggests that 3 to 395 5-day extreme events can arise from atypical synoptic conditions, possibly not available in a 110-year 396 long weather archive. Thanks to the random atmospheric trajectories, SCAMP+ is able to generate 397 such conditions.





400 Fig.8: Return level analysis of extreme precipitation values associated to model ANALOGUE, SCAMP and 401 SCAMP+ for accumulation over 1, 3 and 5 days. The grey shadings present the inter-quantiles intervals at 402 50%, 90% and 99% levels (30 x 111-year scenarios for models ANALOGUE and SCAMP and 300 x 100-year 403 scenarios for SCAMP+).

404 4.3 Multi-annual variability

Figure 9.a and 9.b present examples of simulated time series of annual MAP and MAT obtained with ANALOGUE and SCAMP models. Concerning SCAMP+, four (among the 10 possible scenarios) illustrative time series associated to different 100-year atmospheric trajectories are shown. For all models, we present the dispersion between the 30 annual values obtained from the 30 time series associated to the different atmospheric trajectories. This dispersion is very small for temperature and rather large in comparison for precipitation, illustrating the important uncertainty in the Large-Scale to Small-Scale relationship for this variable in this region.

For ANALOGUE and SCAMP, the simulated year-to-year variations of annual precipitation and temperature are in agreement with the observed ones. The successions of dry/wet or cold/warm years are well simulated in both temporality and amplitude and the positive trend in temperature starting in 1980 is also adequately reproduced. Similar results are obtained for seasonal precipitation and temperature (not shown). These results illustrate the determinant influence of the large-scale conditions on local weather in this region and the relevance of a generation process based on atmospheric analogues.

419 In contrast, the chronological year-to-year variations produced by the different runs of SCAMP+ 420 present different features. The annual precipitation and temperature time series obtained from 421 different runs of SCAMP+ resulting from different large-scale atmospheric trajectories, they cannot 422 be directly compared to the observed time series. This highlights the ability and interest of SCAMP+ 423 to explore non-observed sequences of precipitation and temperature at annual and multi-annual 424 scales. Finally, it must be noticed that SCAMP+ simulations are not expected to reproduce the 425 warming observed after 1980. Indeed, the different runs presented in Figure 9b are associated to 426 different 100-year subsets of the 1000-year atmospheric trajectories simulation and do not include 427 any trend (see discussion in Section 5).



Fig.9a: Time series of annual MAP for the ANALOGUE model (1900-2010), SCAMP (1900-2010) and 4 different 100-year atmospheric trajectories of SCAMP+. The observed annual MAP (1930-2014) is presented with the black solid line in the plots associated to ANALOGUE and SCAMP models. The grey shadings present the inter-quantiles intervals at 50%, 90% and 99% levels (30 x 111-year scenarios for models ANALOGUE and SCAMP and 30 x 100-year scenarios for SCAMP+).



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Fig.9b: Time series of annual MAT for the ANALOGUE model (1900-2010), SCAMP (1900-2010) and 4 different 100-year atmospheric trajectories of SCAMP+. The observed annual MAT (1930-2014) is presented with the black solid line in the plots associated to ANALOGUE and SCAMP models. The grey shadings present the inter-quantiles intervals at 50%, 90% and 99% levels (30 x 111-year scenarios for models ANALOGUE and SCAMP and 30 x 100-year scenarios for SCAMP+).

440 **5. Discussion and conclusions**

441 The different extensions of the classical analogue method introduced in this study aim at generating 442 long regional weather time series without suffering from the main limitations of analogue models. 443 Indeed, due to the limited extent of the observed time series and the impossibility to simulate 444 unobserved daily scenarios, analogue models usually underestimate observed precipitation 445 extremes. These limitations are relaxed by SCAMP+, the weather generator proposed in this study. 446 SCAMP+ generates unobserved and plausible atmospheric trajectories, and, in addition, provides 447 unobserved samples of daily temperature and precipitation using distribution adjustments. Such a 448 generation process explores a larger weather variability at multiple time scales, which leads to a 449 better reproduction of precipitation extremes.

SCAMP+ is built upon a number of past studies carried out in the target region with Analogue-based downscaling approaches. Different sensitivity analyses could be performed in order to ass the impact of the different modelling choices, e.g. the set of predictors used for the analogues selection, the number of analogues selected for the different analogy levels or the parameters related to the generation of atmospheric trajectories (e.g. probability of transition between large scale trajectories).

456 SCAMP+ is obviously not free of limitations. A first issue is relative to the quality of observations used 457 in the model, especially at the synoptic scale. ERA20C reanalyses used here are produced using sea 458 level pressure and wind measurements only. This guarantees a certain quality of the geopotential at 459 1000 hPa. The quality of 500 hPa data and of the other predictors is conversely questionable (namely 460 large-scale temperature, precipitation and vertical velocities), as they do not beneficiate from the 461 assimilation of observed data. This may impact the quality of the downscaling method. For instance, 462 this could explain why the mean seasonal cycle of monthly precipitation is not well reproduced in our results (see for instance the underestimation of the mean precipitation in August). Using higher 463 464 quality data is expected to partly address such limitations. Indeed, using ERA-Interim reanalyses (Dee 465 et al, 2011) instead of ERA20C removes the biases and mis-reproductions mentioned above (not 466 shown), a much larger panel of weather observations being assimilated in ERA-Interim. However, 467 ERA-Interim covers a much smaller time period than ERA20C (roughly 50 years). Using ERA-Interim 468 for our simulations would make the panel of observed synoptic situations much less representative 469 of possible ones, and would impact the ability of our model to generate long-term climate variability.

470 As highlighted previously, a noticeable limitation of SCAMP+ is its difficulty to generate very hot 471 summers or cold winters. The predictors used for the selection of the analogues may actually prevent 472 the simulation of very cold/hot seasons. Choosing the geopotential height at 1000hPa on two consecutive days guarantees similar positions of high/low pressure systems and comparable 473 474 movements of these features for the target day and its analogues. This guarantees that the transition 475 from one atmospheric trajectory to another is correct in terms of anticyclonic or unsettled weather 476 but this cannot guarantee that the transition is correct in terms of air masses temperatures. This 477 might prevent the generation of long hot/cold sequences. A possible improvement of the method 478 would be to include some temperature predictor in the selection of analogue days. Similarly, 479 SCAMP+ is able to generate relevant inter-annual fluctuations of unobserved climate time series. 480 However, long-term fluctuations do not seem to be efficiently generated (at least for temperature). 481 These types of variations are actually driven by very large scale or global phenomena such as the Atlantic Multi-decadal-Oscillation (AMO – Hurrell and al., 1997; Trigo et al., 2002 and Roger et al.,
1997). In SCAMP+, we do not account for such driving phenomena. Introducing additional drivers
such as the AMO index in the generation of atmospheric trajectories could improve the results in this
respect.

486 Trends in observed predictors and predictands, as a result of global warming, could be an additional 487 issue. For instance, the mean elevation of geopotential fields is often expected to increase with mean 488 temperature. Such trends may be detrimental for the simulations, because the analogues 489 identification process would be carried out in a non-homogenous data-set. In the present work for 490 instance, trends in the second analogy level predictors (VV600, P and T) might result, to some extent, 491 in selecting analogues preferentially within the same decade rather than distant ones. This could 492 then reduce the reshuffling potential of the method. This issue is likely to be less critical for the first 493 analogy level of SCAMP and for the generation of atmospheric trajectories in SCAMP+. In this case, 494 analogues are selected according to the Teweles-Wobus score which compares the shapes of 495 geopotential fields and not their absolute values. Quantifying the similarity between these 496 geopotential fields, instead of differences in magnitude, removes the influence of a potential long 497 term trend in this predictor.

498 All in all, SCAMP+ weather generator paves the way for more developments and applications. As part 499 of the EXAR project (see acknowledgments), the model was coupled with a spatial and temporal 500 disaggregation model and fed a distributed hydrological model in order to generate long series of 501 discharge data (Andres et al., 2019a,b). Additional evaluations on the inter-variable co-variability 502 showed that the physical consistency between temperature and precipitation is well reproduced in 503 our simulations and that the model thus efficiently simulates the precipitation phase and the 504 statistical characteristics of liquid/solid precipitation. SCAMP+ has a low computational cost and is 505 able to generate multiple weather sequences which are consistent with possible trajectories of large-506 scale atmospheric conditions, which motivates future applications to other regions and other local 507 weather variables.

- 508
- 509 Data availability.

510 Precipitation and temperature data have been downloaded from Idaweb 511 (https://gate.meteoswiss.ch/idaweb/), a data portal which provides users in the field of teaching and 512 research with direct access to archive data of MeteoSwiss ground-level monitoring networks. 513 However, the acquired data may not be used for commercial purposes (e.g., by passing on the data 514 to third parties, by publishing them on the internet). As a consequence, we cannot offer direct access 515 to the data used in this study. Atmospheric predictors are taken from the European Centre for 516 Medium-Range Weather Forecasts (ECMWF) ERA20C atmospheric reanalysis (Poli et al., 2013), 517 available at the following address: https://www.ecmwf.int/en/forecasts/datasets/reanalysis-518 datasets/era-20c.

519

520 *Author contributions.*

521 J. Chardon and D. Raynaud developed the different models considered here. D. Raynaud carried out 522 the simulations, produced the analyses and the figures presented in this study. All authors 523 contributed to the analysis framework and to the redaction.

- 524
- 525 *Competing interests.*

- 526 The authors declare that they have no conflict of interest.
- 527

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