# Dear Prof. Erwin Zehe:

Many thanks for your work. I have revised the manuscript again as you and the reviewer suggested. I accepted almost all of the reviewer's suggestions. Major revisions include: 1) I have removed almost all of the second part of the results sections as the reviewer suggested; 2) Table 4 was displaced into the supplement. I think the revisions can better streamline the paper. In addition, I added the R codes in the supplement.

Best regards

Mingguo Zheng 2020-3-29

# **Response to Reviewer**

Many thanks for your comments. I accepted almost all of your suggestions this time. My responses are given as follows.

The new title "A mathematically precise method to partition climate and catchment effects on runoff" is less specific then the old one which I prefer. I have revised the title as suggested.

The second part of the results sections is concerned with the sensitivities, which I think is not so strongly related to the main message of this paper. For the sake of brevity, I suggest to remove it. This would focus the paper, allow to reduce the number of figures and avoid possible distraction of the reader.

As suggested, I have removed all of the second part and only remained Fig. 8.

In my first review I suggested to remove or adapt the results of catchments 10,11 since these only have 3 years for their base period, while the evaluation period is > 10 yrs. This short period is probably insufficient to allow stationary conditions, which are essential for such a method. The argument of the author to keep these catchments only because they have been published by another paper does not help here.

As suggested, I have removed the catchments from the analyses and made revisions in all related tables, figures and texts.

## Minor comments:

Figures 1-3 show different axes although I thought that they intend to show the same relationships. I suggest to make this more consistent.

I think the comments over, but I am sorry that the figures cannot have the same axes.

Figure 2: the annotation in the figure seems to be switched; also What represents the continuous lines?

Many thanks for your careful examination. The annotation was indeed switched. I have made revisions.

L653 "In this case, the integral path of the LI method can be considered as the broken line AB+BC in Fig. 3" There is no broken line in Fig.3 I have revised it as "path ABC".

1 2 3 4	A <u>line integral-based</u> mathematically precise method to partition climate and catchment effects on runoff Mingguo Zheng <sup>1, 2*</sup>
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#### 20 Abstract

It is a common task to partition the synergistic impacts of drivers in the environmental sciences. 21 22 However, there is no mathematically precise solution to this partition processtask. Here I presented a 23 line integral-based method, which addresses the sensitivity to the drivers throughout the drivers' ir evolutionary paths so as to ensure a precise partition. The method reveals that the partition depends on 24 25 both the change magnitude and pathway (timing of the change), but not on the magnitude alone unless used for a linear system. To illustrate this method, I used-applied the Budyko framework to partition the 26 27 effects of climatic and catchment conditions on the temporal change in the runoff for 21 catchments19 28 catchments from Australia and China. The proposed method reduces to the decomposition method when assuming a path in which climate change occurs first, followed by an abrupt change in catchment 29 properties. The proposed method re-defines the widely-used sensitivity at a point as the path-averaged 30 sensitivity. The total differential and the complementary methods simply concern the sensitivity at the 31 initial or/and the terminal state, so they cannot give precise results. Although the path-averaged 32 sensitivities varied greatly among the catchments, they can be readily predicted within the Budyko 33 framework. The path averaged sensitivity of water yield to climate conditions was found to be stable 34 over time. Space wise, moreover, the sensitivity can be readily predicted even in the absence of 35 streamflow observations, which facilitates the evaluation of future climate effects on streamflow. As a 36 mathematically accurate solution, the proposed method provides a generic tool to conduct quantitative 37 38 attribution analyses. 39

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40 **Keywords:** Runoff; Climate change; Human activities; Attribution analysis; Budyko

#### 42 1 Introduction

43 The impacts of certain drivers on observed changes of interest often require quantification in environmental sciences. In the hydrology community, both climate and human activities have posed 44 global-scale impact on hydrologic cycle and water resources (Barnett et al., 2008; Xu et al., 2014; 45 Wang and Hejazi, 2001). Diagnosing their relative contributions to runoff is of considerable relevance 46 to the researchers and managers. Unfortunately, performing a quantitative attribution analysis of runoff 47 changes remains a challenge (Wang and Hejazi, 2001; Berghuijs and Woods, 2016; Zhang et al., 2016); 48 this is to a considerable degree due to a lack of a mathematically precise method to decouple synergistic 49 50 and often confounding impacts of climate change and human activities.

Numerous studies have detected the long-term variability in runoff and attempted to partition the 51 effects of climate change and human activities through various methods (Dey and Mishra, 2017); these 52 include the paired-catchments method and the hydrological modeling method. The paired-catchment 53 method can filter the effect of climatic variability and thus isolate the runoff change induced by 54 vegetation changes (Brown et al., 2005). However, this method is capital intensive; moreover, it 55 generally involves small catchments and experiences difficulties when extrapolating to large catchments 56 (Zhang et al., 2011). The physical-based hydrological models often have limitations such as a high data 57 requirement, labor-intensive calibration and validation processes, and inherent uncertainty and 58 59 interdependence in parameter estimations (Binley et al., 1991; Wang et al., 2013; Liang et al., 2015). Conceptual models such as Budyko-type equations (see Section 2.1) have consequently gained interest 60 in recent years (see Section 2.1). 61

Within the Budyko framework, studies (Roderick and Farquhar, 2011; Zhang et al., 2016) have 62 used the total differential of runoff as a proxy for the runoff change and the partial derivatives as the 63 sensitivities (hereafter called the total differential method). The total differential, however, is simply a 64 first-order approximation of the observed change (Fig. 1(a)). This approximation has caused an error in 65 the calculation of climate impact on runoff, with the deviation ranging from 0 to 20 10<sup>-3</sup>m (or -118 to 66 174%) in China (Yang et al., 2014). The elasticity method proposed by Schaake (1990) is also based on 67 the total differential expression (Sankarasubramanian et al., 2001; Zheng et al., 2009). The method uses 68 the "elasticity" concept to assess the climate sensitivity of runoff. The elasticity coefficients, however, 69 have been estimated in an empirical way and are not physically sound (Roderick and Farquhar, 2011; 70 Liang et al., 2015). 71

The so-called decomposition method developed by Wang and Hejazi (2011) has also been widely used. The method assumes that climate changes cause a shift along a Budyko curve and then human interferences cause a vertical shift from one Budyko curve to another (Fig. 2). Under this assumption, the method extrapolates the Budyko models that are calibrated using observations of the reference period, in which human impacts remain minimal, to determine the human-induced runoff changes that occur during the evaluation period.

Recently, Zhou *et al.* (2016) established a Budyko complementary relationship for runoff and further applied it to partitioning the climate and catchment effects. Superior to the total differential method, the complementary method culminates by yielding a no-residual partition. Nevertheless, this method depends on a given weighted factor that is determined in an empirical but not a precise way. Furthermore, Zhou *et al.* (2016) argued that the partition is not unique in the Budyko framework because the path of the climate and catchment changes cannot be uniquely identified.

Obtaining a precise partition remains difficult, even when usinggiving a precise mathematical 84 model. This difficulty can be illustrated by using a precise hydrology model R = f(x, y), where R 85 represents runoff, and x and y represent the climate factors and catchment characteristics, respectively. 86 87 We assumed that R changes by  $\Delta R$  when x changed by  $\Delta x$  and y changes by  $\Delta y$ , *i.e.*,  $\Delta R = f(x + \Delta x, y + \Delta y) - f(x, y)$ . To determine the effect of x on  $\Delta R$ , *i.e.*  $\Delta R_x$ , a common practice is to 88 assume that y remains constant when x changes by  $\Delta x$ . We thus obtain:  $\Delta R_x = f(x + \Delta x, y) - f(x, y)$ . 89 Similarly, we can obtain:  $\Delta R_y = f(x, y + \Delta y) - f(x, y)$ . Although this derivation seems quite reasonable, it 90 91 is problematic as  $\Delta R_x + \Delta R_y \neq \Delta R$ . A further examination shows that a variable's effect on R seems to differ depending on the changing path (timing of the change). For example,  $\Delta R_x = f(x + \Delta x, y) - f(x, y)$ 92 and  $\Delta R_y = f(x + \Delta x, y + \Delta y) - f(x + \Delta x, y)$  if x changes first and y subsequently changes (Note that the 93 partition is precise with  $\Delta R_x + \Delta R_y = \Delta R$  at this moment). If v changes first and x subsequently changes, 94 the partition then becomes:  $\Delta R_x = f(x + \Delta x, y + \Delta y) - f(x, y + \Delta y)$  and  $\Delta R_y = f(x, y + \Delta y) - f(x, y)$ . In the 95 case of x and y changing simultaneously, unfortunately, current literature seems not to provide a 96 mathematically precise solution. 97

The aim of this study is to propose a mathematically precise method to conduct a quantitative 98 attribution to drivers. The method is based on the line integer (called the LI method hereafter) and takes 99 100 account of the sensitivity throughout the evolutionary path of the drivers rather than at a point as the total differential method does. In this way, the proposed method revises the widely used concept of 101 sensitivity at a point as the path-averaged sensitivity. To present and evaluate the proposed method, I 102 103 decomposed the relative influences of climate and catchment conditions on runoff within the Budyko 104 framework using data from <del>21 catchments</del>19 catchments from Australia and China. <del>I also examined the</del> spatio temporal variability of the path averaged sensitivities and assessed their spatio temporal 105 predictability. 106

107

# 108 2 Methodology

109 2.1 Budyko Framework and the MCY equation

110 Budyko (1974) argued that the mean annual evapotranspiration (E) is largely determined by the water and energy balance of a catchment. Using precipitation (P) and potential evapotranspiration ( $E_0$ ) 111 proxies for water and energy availabilities respectively, the Budyko framework 112 as relates evapotranspiration losses to the aridity index defined as the ratio of  $E_0$  over P. The Budyko 113 114 framework has gained wide acceptance in the hydrology community (Berghuijs and Woods, 2016; Sposito, 2017). In recent decades, several equations have been developed to describe the Budyko 115 framework. Among them, the Mezentsev-Choudhury-Yang's equation (Mezentsev, 1955; Choudhury, 116 1999; Yang et al., 2008) (Called the MCY equation hereafter) has been widely accepted and was used 117 in this study: 118

119 
$$\frac{E}{P} = \frac{E_0/P}{\left(1 + (E_0/P)^n\right)^{1/n}}$$
(1)

120 where  $n \in (0,\infty)$  is an integration constant that is dimensionless, and represents catchment properties. Eq. 121 (3) requires a relatively long time scale whereby the water storage of a catchment is negligible and the water balance equation reduces to be R = P - E. Here I adopted a "tuned" *n* value that can obtain an 122 123 exact accordance between the calculated E by Eq. (1) and that actually encountered (= P - R).

The partial differentials of R with respect to P,  $E_0$ , and n are given as: 124

125 
$$\frac{\partial R}{\partial P} = R_P(P, E_0, n) = 1 - \frac{E_0}{(P^n + E_0^n)^{1/n}}$$
(2a)  
$$\frac{\partial R}{\partial P} = \frac{P^{n+1}}{(P^n + E_0^n)^{1/n}}$$

126 
$$\frac{\partial R}{\partial E_0} = R_{E_0}(P, E_0, n) = -\frac{P^{n+1}}{(P^n + E_0^n)^{1/n}}$$
(2b)  
127 
$$\frac{\partial R}{\partial E_0} = R_n(P, E_0, n) = \frac{-E_0 P n^{-1}}{(P^n + E_0^n)^{1/n}} \left[ \frac{\ln(P^n + E_0^n)}{(P^n + E_0^n)^{1/n}} - \frac{P^n \ln P + E_0^n \ln E_0}{(P^n + E_0^n)^{1/n}} \right]$$
(2c)

27 
$$\frac{\partial R}{\partial n} = R_n(P, E_0, n) = \frac{-E_0 P n^{-1}}{(P^n + E_0^n)^{1/n}} \left[ \frac{\ln(P^n + E_0^n)}{n} - \frac{P^n \ln P + E_0^n \ln E_0}{P^n + E_0^n} \right]$$
(2c)

#### 2.2 Theory of the line integral-based method 128

129 We start by considering an example of a two-variable function z = f(x, y) and assumed that x and y are independent. The function has continuous partial derivatives  $\partial z / \partial x = f_x(x, y)$  and  $\partial z / \partial y = f_y(x, y)$ . 130 131 Suppose that x and y vary along a smooth curve L (e.g. AC in Fig. 3) from the initial state  $(x_0, y_0)$  to the 132 terminal state (x<sub>N</sub>, y<sub>N</sub>), and z co-varies from z<sub>0</sub> to z<sub>N</sub>. Let  $\Delta z = z_N - z_0$ ,  $\Delta x = x_N - x_0$ , and  $\Delta y = y_N - y_0$ . Our goal is to determine a mathematical solution that quantifies the effects of  $\Delta x$  and  $\Delta y$  on  $\Delta z$ , *i.e.* 133 134  $\Delta z_x$  and  $\Delta z_y$ .  $\Delta z_x$  and  $\Delta z_y$  should be subject to the constraint  $\Delta z_x + \Delta z_y = \Delta z$ .

135 As shown in Fig. 3, points  $M_1(x_1, y_1), \dots, M_{N-1}(x_{N-1}, y_{N-1})$  partition L into N distinct segments. Let  $\Delta x_i = x_{i+1} - x_i$ ,  $\Delta y_i = y_{i+1} - y_i$ , and  $\Delta z_i = z_{i+1} - z_i$ . For each segment,  $\Delta z_i$  can be approximated as  $dz_i$ . 136

137 
$$\Delta z_i \approx dz_i = f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + \sum_{i=1}^N f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_x(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_y(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_y(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta y_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_y(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta x_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_y(x_i, y_i) \Delta x_i + f_y(x_i, y_i) \Delta x_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_y(x_i, y_i) \Delta x_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta z_i \approx \sum_{i=1}^N f_y(x_i, y_i) \Delta x_i \text{ . We then have: } \Delta z = \sum_{i=1}^N \Delta x_i \text{ . We then have: } \Delta x_i = \sum_{i=1}^N \Delta x_i \text{ . We then have: } \Delta x_i = \sum_{i=1}^N \Delta x_i = \sum_{i=1$$

thus obtain the following respective approximation of  $\Delta z_x$  and  $\Delta z_y$ :  $\Delta z_x \approx \sum_{i=1}^{N} f_x(x_i, y_i) \Delta x_i$  and 138

 $\Delta z_y \approx \sum_{i=1}^{N} f_y(x_i, y_i) \Delta y_i$ . Next, define  $\tau$  as the maximum length among of the N segments. The smaller the 139

value of  $\tau$ , the closer to  $\Delta z_i$  the value of  $dz_i$ , and then the more accurate the approximations are. The 140 approximations become exact in the limit  $\tau \rightarrow 0$ . Taking the limit  $\tau \rightarrow 0$  then converts the sum into 141 142 integrals and gives a precise expression (this is an informal derivation and please see Appendix A for a one):  $\Delta z = \lim_{\tau \to 0} \sum_{i=1}^{N} f_x(x_i, y_i) \Delta x_i + \lim_{\tau \to 0} \sum_{i=1}^{N} f_y(x_i, y_i) \Delta y_i = \int_L f_x(x, y) dx + \int_L f_y(x, y) dy$ 143 formal where ,

144 
$$\int_{L} f_{x}(x, y) dx = \lim_{\tau \to 0} \sum_{i=1}^{N} f_{x}(x_{i}, y_{i}) \Delta x_{i} \text{ and } \int_{L} f_{y}(x, y) dy = \lim_{\tau \to 0} \sum_{i=1}^{N} f_{y}(x_{i}, y_{i}) \Delta y_{i} \text{ denote the line integral of } f_{x} \text{ and } f_{y}$$

along *L* (termed integral path) with respect to *x* and *y*, respectively.  $\int_{L} f_x(x, y) dx$  and  $\int_{L} f_y(x, y) dy$  exist provided that  $f_x$  and  $f_y$  are continuous along *L*. We thus obtain a precise evaluation of  $\Delta z_x$  and  $\Delta z_y$ :

147 
$$\Delta z_x = \int_L f_x(x, y) dx \qquad (3a)$$
  
148 
$$\Delta z_y = \int_L f_y(x, y) dy . \qquad (3b)$$

149 Unlike the total differential method, the sum of  $\Delta z_x$  and  $\Delta z_y$  persistently equals  $\Delta z$  (Appendix B). 150 If f(x, y) is linear, then  $f_x$  and  $f_y$  are constant. Defining  $f_x(x, y)$  and  $f_y(x, y)$  remain constant at  $C_x$  and  $C_y$ 151 respectively, then  $\Delta z_x = C_x \Delta x$  and  $\Delta z_y = C_y \Delta y$ .  $\Delta z_x$  and  $\Delta z_y$  are thus independent of *L*. If f(x, y) is non-linear, 152 however, both  $\Delta z_x$  and  $\Delta z_y$  vary with *L*, as is exemplified in Appendix C. Hence, the initial and the 153 terminal states, together with the path connecting them, determine the resultant partition unless f(x, y) is 154 linear.

The mathematical derivation above applies to a three-variable function as well. By doing the line integrals for the MCY equation, we obtain the desired results:

157 
$$\Delta R_{P} = \int_{L} \frac{\partial R}{\partial P} dP \qquad (4a)$$
158 
$$\Delta R_{E_{0}} = \int_{L} \frac{\partial R}{\partial E_{0}} dE_{0} \qquad (4b)$$

159  $\Delta R_n = \int_L \frac{\partial R}{\partial n} dn \qquad (4c)$ 

where  $\Delta R_P$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$  denote the effects on runoff change of P,  $E_0$ , and n, respectively. The sum of  $\Delta R_P$  and  $\Delta R_{E_0}$  represents the effect of climate change, and  $\Delta R_n$  is often related to human activities although it probably includes the effects of other factors, such as climate seasonality (Roderick and Farquhar, 2011; Berghuijs and Woods, 2016). L denotes a three-dimensional curve along which climate and catchment changes have occurred. I approximated L by a series of line segments.  $\Delta R_P$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$ were finally determined by summing up the integrals along each of the line segments (see Section 2.3).

- 166 2.3 Using the LI method to determine  $\Delta R_p$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$  within the Budyko Framework
- 167 1) Determining  $\Delta R_p$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$  assuming a linear integral path

168 <u>A curve can be approximated as a series of line segments.</u> A curve can always be approximated **\*** 169 as a series of line segments. Hence, we can first handle the case of a linear integral path. Given two

consecutive periods and assuming that the catchment state has evolved from  $(P_1, E_{01}, n_1)$  to  $(P_2, E_{02}, n_2)$ 

171 along a straight line L, let  $\Delta P = P_2 - P_1$ ,  $\Delta E_0 = E_{02} - E_{01}$ , and  $\Delta n = n_2 - n_1$ ; then the line L is given by

172 parametric equations:  $P = \Delta Pt + P_1$ ,  $E_0 = \Delta E_0t + E_{01}$ ,  $n = \Delta nt + n_1$ ,  $t \in [0,1]$ . Given these equations, Eq. (2)

173 becomes a univariate function of t, i.e.,  $\partial R / \partial P = R_P(t)$ ,  $\partial R / \partial E_0 = R_{E_0}(t)$ , and  $\partial R / \partial n = R_n(t)$ . Then,  $\Delta R_P$ ,

174  $\Delta R_{E_0}$ , and  $\Delta R_n$  can be evaluated as:

175 
$$\Delta R_P = \int_L \frac{\partial R}{\partial P} dP = \int_0^1 R_P(t) d(\Delta P t + P_1) = \Delta P \int_0^1 R_P(t) dt$$
(5a)

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176 
$$\Delta R_{E_0} = \int_L \frac{\partial R}{\partial E_0} dE_0 = \int_0^1 R_{E_0}(t) d(\Delta E_0 t + E_{01}) = \Delta E_0 \int_0^1 R_{E_0}(t) dt \qquad (5b)$$

177 
$$\Delta R_n = \int_L \frac{\partial R}{\partial n} dn = \int_0^1 R_n(t) d(\Delta nt + nt) = \Delta n \int_0^1 R_n(t) dt$$
(5c)

Unfortunately, I could not determine the antiderivatives of  $R_P(t)dt$ ,  $R_{E_0}(t)dt$  and  $R_n(t)dt$  and had 178 to make approximate calculations. As the discrete equivalent of integration is a summation, we can 179 approximate the integration as a summation. I divided the  $t \in [0,1]$  interval into 1000 subintervals of the 180 same width, *i.e.*, setting dt identically equal to 0.001, and then calculated  $R_P(t)dt$ ,  $R_{E_0}(t)dt$  and  $R_n(t)dt$  for 181 each subinterval. Let  $t_i = 0.001i - i \in [0,999]$  and is integer-valued  $\Delta R_p$ ,  $\Delta R_p$ ,  $\Delta R_n$ , and  $\Delta R_n$  are approximated 182 183 as:

184 
$$\Delta R_P \approx 0.001 \Delta P \sum_{i=0}^{999} R_P(t_i)$$
 (6a)

$$185 \qquad \Delta R_{E_0} \approx 0.001 \Delta E_0 \sum_{i=0}^{377} R_{E_0}(t_i)$$
(6b)  
$$186 \qquad \Delta R_n \approx 0.001 \Delta n \sum_{i=0}^{999} R_n(t_i)$$
(6c)

2) Dividing the evaluation period into a number of subperiods 187

I first determined a change point and divided the whole observation period into the reference and 188 evaluation periods. To determine the integral path, the evaluation period was further divided into a 189 number of subperiods. The Budyko framework assumes a steady state condition of a catchment and 190 191 therefore requires no change in soil water storage. Over a time period of 5-10 years, it is reasonable to assume that changes in soil water storage will be sufficiently small (Zhang et al., 2001). Here, I divided 192 193 the evaluation period into a number of 7-year subperiods with the exception for the final subperiod, 194 which varied from 7 to 13 years in length depending on the length of the evaluation period.

195 Determining  $\Delta R_p$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$  by approximating the integral path as a series of line-3) 3) 196 segments

197 A curve can be approximated as a series of line segments. For a short period, the integral path L198 can be considered as linear, which implies a temporally invariant change rate. For a long period in which the change rate  $\frac{may}{varyies}$  over time, L can be fitted using a number of line segments. Given a 199 200 reference period and an evaluation period comprising N subperiods, *Lassumed that* the catchment state 201 was assumed to evolved from  $(P_0, E_{00}, n_0), \dots, (P_i, E_{0i}, n_i), \dots$  to  $(P_N, E_{0N}, n_N)$ , where the subscript "0" 202 denotes the reference period, and "i" and "N" denote the ith and the final subperiods of the evaluation period, respectively. I used a series of line segments  $L_1, L_2, \ldots, L_N$  to approximate the integral path L, 203 where  $L_i$  connects points  $(P_{i-1}, E_{0,i-1}, n_{i-1})$  with  $(P_i, E_{0i}, n_i)$ . Then  $\Delta R_p$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$  were evaluated as the 204 sum of the integrals along each of the line segments, which were calculated using Eq. (6). 205

#### 206 2.4 Total-differential, decomposition and complementary methods

207 To evaluate the LI method, I compared it with the existing methods, including the 208 decomposition method, the total differential method, and the complementary method. The total differential method approximated  $\Delta R$  as dR: 209

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210 
$$\Delta R \approx dR = \frac{\partial R}{\partial P} \Delta P + \frac{\partial R}{\partial E_0} \Delta E_0 + \frac{\partial R}{\partial n} \Delta n = \lambda_P \Delta P + \lambda_{E_0} \Delta E_0 + \lambda_n \Delta n \tag{7}$$

where  $\lambda_P = \partial R/\partial P$ ,  $\lambda_{E_0} = \partial R/\partial E_0$ , and  $\lambda_n = \partial R/\partial n$ , representing the sensitivity coefficient of R with respect to P,  $E_0$ , and n, respectively. Within the total differential method,  $\Delta R_P = \lambda_P \Delta P$ ,  $\Delta R_{E_0} = \lambda_{E_0} \Delta E_0$ , and  $\Delta R_n = \lambda_n \Delta n$ . I used the forward approximation, *i.e.*, substituting the observed mean annual values of the reference period into Eq. (2), to estimate  $\lambda_P$ ,  $\lambda_{E_0}$ , and  $\lambda_n$ , as is standard in most studies (Roderick and Farquhar, 2011; Yang and Yang, 2011; Sun *et al.*, 2014).

The decomposition method (Wang and Hejazi, 2011) calculated  $\Delta R_n$  as follows:

$$\Delta R_n = R_2 - R'_2 = (P_2 - E_2) - (P_2 - E'_2) = E'_2 - E_2$$
(8)

where  $R_2$ ,  $P_2$ , and  $E_2$  represents the mean annual runoff, precipitation and evapotranspiration of the evaluation period, respectively;  $R'_2$  and  $E'_2$  represent the mean annual runoff and evapotranspiration, respectively, given the climate conditions of the evaluation period and the catchment conditions of the reference period (Fig. 2). Both  $E_2$  and  $E'_2$  were calculated by Eq. (1), but using *n* values of the evaluation period and the reference period respectively.

223 The complementary method (Zhou *et al.*, 2016) uses a linear combination of the complementary 224 relationship for runoff to determine  $\Delta R_P$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$ :

$$\Delta R = a \left[ \left( \frac{\partial R}{\partial P} \right)_1 \Delta P + \left( \frac{\partial R}{\partial E_0} \right)_1 \Delta E_0 + P_2 \Delta \left( \frac{\partial R}{\partial P} \right) + E_{0,2} \Delta \left( \frac{\partial R}{\partial E_0} \right) \right] + (1-a) \left[ \left( \frac{\partial R}{\partial P} \right)_2 \Delta P + \left( \frac{\partial R}{\partial E_0} \right)_2 \Delta E_0 + P_1 \Delta \left( \frac{\partial R}{\partial P} \right) + E_{0,1} \Delta \left( \frac{\partial R}{\partial E_0} \right) \right]$$
(9)

where the subscript 1 and 2 denotes the reference and the evaluation periods, respectively. *a* is a weighting factor and varies from 0 to 1. As suggested by Zhou *et al.* (2016), I set a = 0.5. Equation (9) thus gave an estimation of  $\Delta R_{P}$ ,  $\Delta R_{E_{P}}$ , and  $\Delta R_{n}$  as follows:

(10b)

229 
$$\Delta R_P = 0.5 \Delta P \left[ \left( \frac{\partial R}{\partial P} \right)_1 + \left( \frac{\partial R}{\partial P} \right)_2 \right]$$
(10a)

230 
$$\Delta R_{E_0} = 0.5\Delta E_0 \left[ \left( \frac{\partial R}{\partial E_0} \right)_1 + \left( \frac{\partial R}{\partial E_0} \right)_2 \right]$$
231 
$$\Delta R_0 = 0.5\Delta \left( \frac{\partial R}{\partial E_0} \right) (P_1, P_2) + 0.5\Delta \left( \frac{\partial R}{\partial E_0} \right) (F_0, F_0, F_0)$$

231 
$$\Delta R_n = 0.5\Delta \left(\frac{\partial R}{\partial P}\right) (P_{1+}, P_2) + 0.5\Delta \left(\frac{\partial R}{\partial E_0}\right) (E_{0,1+}, E_{0,2})$$
(10c)

#### 2.5 Data

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233 I collected runoff and climate data from 21-19 selected catchments evaluated in previous studies 234 (Table 1). The change-point years given in these studies were directly used to determine the reference 235 and evaluation periods for the LI method. As mentioned above, the LI method further divides the evaluation period into a number of subperiods. For the sake of comparison, the final subperiod of the 236 237 evaluation period was used as the evaluation period for the decomposition, the total differential and the 238 complementary methods (It can be equally considered that all of the four methods used the final 239 subperiod as the evaluation period, but the LI method cares about the intermediate period between the 240 reference and the evaluation periods and the other methods do not). NineEight of the 21 catchments19 241 <u>catchments</u> had a reference period comprising only one subperiod (Table 1), and the others had two to 242 seven subperiods.

243 The 21-19 selected catchments have diverse climates and landscapes with 14-12 from Australia 244 and seven from China (Table 1). The catchments span from tropical to subtropical and temperate areas 245 and from humid to semi-humid and semiarid regions, with the mean annual rainfall varying from 506 to  $1014 \ 10^{-3}$ m and potential evaporation from 768 to  $1169 \ 10^{-3}$ m. The dryness index ranges between 0.86 246 and 1.91. The catchment areas vary by five orders of magnitude from 1.95 to 121,972 with a median 247 248  $606 \ 10^6 \text{m}^2$ . The key data includes annual runoff, precipitation, and potential evaporation. The record 249 length varied between  $\frac{15}{19}$  and  $\frac{75}{76}$  with a median of  $\frac{35}{39}$  years. All the catchments experienced 250 changes in climate and catchment properties over the observation periods. Among the 21 catchments, 251 fThe precipitation changes from the reference to the evaluation period ranged between -153271 and 79 252  $10^{-3}$ m yr<sup>-1</sup> for precipitation, and between -35 and 41  $10^{-3}$ m yr<sup>-1</sup> for potential evaporation (Table 2). The 253 coeval change in the parameter n of the MCY equation ranged between -0.2 to  $\frac{2.531.4}{2.531.4}$ . 254 eatchments experienced changes in climate and catchment properties over the observation periods. The 255 mean annual streamflow reduced for all catchments, ranging from 0.43 to  $\frac{229}{169}$  with a median 38 10 256  $^{3}$ m yr<sup>-1</sup>. For all catchments, tThe change in catchment properties mainly refer to the vegetation cover or land use change. More details of data and the catchments can be found in Zhang et al. (2011), Sun et al. 257 258 (2014), Zhang et al. (2010), Zheng et al. (2009), Jiang et al. (2015), and Gao et al. (2016).

#### 260 3 Results

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261

#### 3.1 Comparisons with existing methods

Table 3 lists the resultant values of  $\Delta R_p$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$  from the LI method and the three other methods. Please see the supplemental information section for detailed calculation steps.

264 Fig. 4(a) compares the resultant  $\Delta R_n$  of the LI method and the decomposition method. Although 265 they are quite similar, the discrepancies between these values can be up to  $>20 \ 10^{-3}$  m yr<sup>-1</sup>. The decomposition method assumes that climate change occurs first and then human interferences cause a 266 267 sudden change in catchment properties (Fig. 2). Such a fictitious path is identical to the path broken line 268 of AB+BC in Fig. 3, provided that x represents climate factors and y catchment properties. When 269 adopting ABC as the integral path, the LI method yielded the same results as the decomposition method 270 did (Fig. 4(b)). HenceAs a result, the decomposition method can be considered as a special case of the 271 LI method that uses a special integral path.

272 when adopting the AB+BC broken line in Fig. 3 as the integral path, as was demonstrated 273 elearly in Fig. 4(b).

The total differentiae method is predicated on an approximate equation, *i.e.* Eq. (7). The LI method reveals that the precise form of the equation is  $\Delta R = \overline{\lambda_P} \Delta P + \overline{\lambda_{E_0}} \Delta E_0 + \overline{\lambda_n} \Delta n$  (Appendix D), where  $\overline{\lambda_P}$ ,  $\overline{\lambda_{E_0}}$  and  $\overline{\lambda_n}$  (Table 4) denote the path-averaged sensitivity of R to P,  $E_0$ , and n, respectively. All points along the path have the same weight in determining  $\overline{\lambda_P}$ ,  $\overline{\lambda_{E_0}}$  and  $\overline{\lambda_n}$ . To determine them, the total differential and the complementary methods utilize only the initial or/and the terminal states. Neglecting **设置了格式:** 字体: (默认) Times New Roman, (中文)

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**设置了格式:**字体:(默认) Times New Roman, (中文) 宋体, 字体颜色:黑色 **设置了格式:**字体:(中文)宋体,字体颜色:黑色 the intermediate states would results in an imprecise partition, as was illustrated in Fig. 1 using a univariate function, and even a reverse trend estimation (see  $\Delta R_{E_0}$  for Catchment NO. 1 in Table 3).

281 Superior to the total differential method, the sum of  $\Delta R_{P}$ ,  $\Delta R_{\pi}$ , and  $\Delta R_{\pi}$  always equaled to  $\Delta R_{-}$  for 282 the LI method. Examination of the subperiods revealed that  $\partial R/\partial n$  was more temporally variable than 283  $\partial R/\partial P_{-}$ and  $\partial R/\partial E_{0}$  (discussed below). For this reason,  $\Delta R_{\pi}$  showed considerable discrepancies between 284 the two methods, but  $\Delta R_{T}$  as well as  $\Delta R_{\pi}$  matched closely between the two methods (Fig. 5).

-As with the LI method, the complementary method produced  $\Delta R_P$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$  that exactly summed up to  $\Delta R$ . Although its resultant  $\Delta R_P$ ,  $\Delta R_{E_0}$ , and  $\Delta R_n$  values were all in accordance with the LI method (Fig. 6), the LI method often yielded values beyond the bounds given by the complementary method (Fig. 7); this is because the maximum or minimum sensitivities do not necessarily occur at the initial or terminal states.

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#### 3.2 Spatio temporal variability of the path averaged sensitivities

 $-\overline{\lambda_P}$ ,  $\overline{\lambda_{E_0}}$  and  $\overline{\lambda_n}$  imply the average runoff change induced by a unit change in P,  $E_0$  and n, 291 respectively (Appendix D). Their spatio temporal variability is relevant to the prediction of the runoff 292 change. To evaluate their temporal variabilities, I calculated  $\overline{\lambda_{P}}$ ,  $\overline{\lambda_{E_{0}}}$  and  $\overline{\lambda_{n}}$  for each subperiod of the 293 294 evaluation period and assessed their deviation from those for the whole evaluation period. As shown in Fig. 8, the deviation was rather limited for  $\overline{\lambda_{P}}$  (averaged 8.6%) and  $\overline{\lambda_{E_{0}}}$  (averaged 13%), but was 295 considerable for  $\frac{1}{\hbar}$  (averaged 41%). Hence, it seems quite safe to predict the future climate effects on 296 runoff using the earlier  $\overline{\lambda_{P}}$  and  $\overline{\lambda_{E_{0}}}$  values, but care must be taken when using earlier  $\overline{\lambda_{n}}$  to predict future 297 298 catchment effect.

Different from the temporal variability,  $\overline{\lambda_P}$ ,  $\overline{\lambda_{E_0}}$  and  $\overline{\lambda_n}$  all varied by up to several times or even ten folds between the studied catchments (Table-Table S44). Strong correlations were observed between  $\overline{\lambda_P}$  and P, between  $\overline{\lambda_{E_0}}$  and P, and between  $\overline{\lambda_n}$  and n (Fig. 9). Fig. 10-8 shows that Eq. (2) reproduced  $\overline{\lambda_P}$ ,  $\overline{\lambda_{E_0}}$  and  $\overline{\lambda_n}$  very well taking the long-term means of P,  $E_0$ , and n as inputs, a fact that the dependent variable approached its average if the independent variables were set to be their averages. This finding is of relevance to the spatial prediction of  $\overline{\lambda_P}$ ,  $\overline{\lambda_{E_0}}$  and  $\overline{\lambda_n}$ .

Runoff data and, in turn, the parameter n in the MCY equation are often unavailable. It is thus 305 desirable to make predictions of  $\lambda_P$ .  $\overline{\lambda_{F_0}}$  and  $\overline{\lambda_n}$  in the absence of the parameter n. I developed three 306 strategies as follows: 1) using Eq. (2) and assuming n = 2 as n is typically in a small range from 1.5 to 307 308 2.6 (Roderick and Farquhar, 2011); 2) using P and  $E_0$  to establish regression models; 3) using the aridity index to establish regressions as the index appeared to be more strongly correlated with both  $\overline{\lambda_{F}}$  and  $\overline{\lambda_{E0}}$ 309 than P and  $E_0$  (Fig. 9). As shown in Fig. 11, the three strategies show similar performance although the 310 311 second one seems to perform better. All the strategies gave acceptable predictions of  $\lambda r$  and  $\lambda r_{0}$  but poor results for  $\overline{\lambda_n}$ , as it was primarily controlled by *n* (Fig. 9). Thus, more sophisticated approaches are 312 313 needed to predict the future catchment effect on runoff in the absence of runoff observations.

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#### 315 4 Discussion

The LI method highlights the role of the evolutionary path in determining the resultant partition. Yet, it seems that no studies have accounted for the path issue while evaluating the relative influences of drivers. The limit of the LI method is high data requirement for obtaining the evolutionary path. When the <u>path</u> data are unavailable, the complementary method can be considered as an alternative. The complementary method is free of residuals; moreover, it employs both data of the reference and the evaluation periods, thereby generally yielding sensitivities closer to the path-averaged results than the total differentiae method.

323 While using the Budyko models, a reasonable time scale is relevant to meet the assumption that changes in catchment water storage are small relative to the magnitude of fluxes of P, R and E 324 (Donohue et al., 2007; Roderick and Farquhar, 2011). A seven-year time scale was used in the present 325 326 study, as most studies have suggested that a time period of 5-10 years (Zhang et al., 2001; Zhang et al., 2016; Wu et al., 2017a; Wu et al., 2017b; Li et al., 2017) or even one year (Roderick and Farquhar, 327 2011; Sivapalan et al., 2011; Carmona et al., 2014; Ning et al., 2017) is reasonable. Nevertheless, some 328 studies argued that the time period should be longer than ten years (Li et al., 2016; Dey and Mishra, 329 2017). If this is the case, the high temporal variation of  $\overline{\lambda}$  shown in Fig. 8 might be caused by water 330 331 storage changes, rather than actual changes in the catchment properties. This uncertainty should be addressed. Using the Gravity Recovery and Climate Experiment (GRACE) satellite gravimetry, Zhao et 332 al. (2011) detected the water storage variations for three largest river basins of China, namely, the 333 Yellow, Yangtze, and Zhujiang. The Yellow River mostly drains an arid and semiarid region (P, 450 334  $10^{-3}$ m; R, 70  $10^{-3}$ m; E, 380  $10^{-3}$ m), and the Yangtze (P, 110  $10^{-3}$  m; R, 550  $10^{-3}$ m; E, 550  $10^{-3}$ m) and 335 the Zhujiang river basins (P, 1400  $10^{-3}$ m; R, 780  $10^{-3}$ m; E, 620  $10^{-3}$ m) are humid. The amplitude of the 336 water storage variations between years were 7, 37.2, and 65  $10^{-3}$ m for the three rivers respectively, at 337 338 one magnitude order smaller than the fluxes of P, R and E. Although the observations cannot be directly extrapolated to other regions, the possibility seems remote that the use of a 7-year aggregated time 339 strongly violates the assumption of the steady state condition. 340

The mutual independence between the drivers is crucial for a valid partition. In the present study, although annual P and  $E_0$  exhibited significant correlation for most catchments (p<0.05), the aggregated P,  $E_0$  and n over a 7-year period showed minimal correlation (mostly p>0.1). The interdependence between the drivers can considerably confound the resultant partitions of the LI method and other existing methods.

The LI method re-definevises the widely used concept of sensitivity at a point as the path-346 347 averaged sensitivity. Mathematically, the LI method is unrelated to a functional form and hence applies to communities other than just hydrology. For example, identifying the carbon emission budgets (an 348 allowable amount of anthropogenic  $CO_2$  emission consistent with a limiting warming target), is crucial 349 350 for global efforts to mitigate climate change. The LI method suggested that the emission budgets depends on both the emission magnitude and pathway (timing of emissions), which is in line with a 351 352 recent study by Gasser et al. (2018). Hence, aAn optimal pathway would facilitate an elevated carbon 353 budget unless the carbon-climate system behaves in a linear fashion.

This study presented the LI method using time-series data, but it applies equally to the case of spatial series of data. Given a model that relates fluvial or aeolian sediment load to the influencing 带格式的:段落间距段前:0磅

factors (e.g. rainfall and topography), for example, the LI method can be used to separate their contributions to the sediment-load change along a river or in the along-wind direction.

358

#### 359 5 Conclusions

Based on the line integral, I created a mathematically precise method to partition the synergistic 360 361 effects of several factors that cumulatively drive a system to change from a state to the other. The method is relevant for quantitative assessments of the relative roles of the factors on the change in the 362 system state. I applied the LI method to partition the effects of climatic and catchment conditions on 363 364 runoff within the Budyko framework. The method reveals that in addition to the change magnitude, the 365 change pathways of climatic and catchment conditions also play a role<del>control their impacts on runoff</del>. 366 Instead of using the runoff sensitivity at a point, the LI method uses the path-averaged sensitivity, thereby ensuring a mathematically precise partition. I further examined the spatio temporal variability 367 368 of the path averaged sensitivity. Time wise, the runoff sensitivity to climate is stable but that to 369 catchment properties is highly variable, suggesting that predicting future climate effects using earlier 370 observations is reliable but care must be taken when predicting future catchment effects. Space-wise 371 (between catchments) the runoff sensitivity both to climatic and catchment conditions was highly 372 variable, but it can be accurately depicted by long-term means of the climatic and catchment conditions. 373 As a mathematically accurate scheme, the LI method has the potential to be a generic attribution 374 approach in the environmental sciences.

#### 376 Data availability

The data used in this study are freely available by contacting the authors.

#### 378

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#### 379 Author contribution

380 MZ designed the study, analyzed the data and wrote the manuscript.

#### 382 Competing interests

383 The authors declare that they have no conflict of interest.

384

385 Appendix A: Mathematical proof of  $\Delta z = \int_{z} f_x(x, y) dx + \int_{z} f_y(x, y) dy$ 

We define that the curve *L* in Fig. 3 is given by a parametric equation: x = x(t), y = y(t),  $t \in [t_0, t_N]$ , then  $\Delta z = z_N - z_0 = f[x(t_N), y(t_N)] - f[x(t_0), y(t_0)]$ . Substituting the parametric equations, we obtain:

389 The right-hand side of the equation =  $\int_{y} f_x(x, y) dx + \int_{y} f_y(x, y) dy$ 

390 = 
$$\int_{t_0}^{t_N} f_x[x(t), y(t)] dx(t) + \int_{t_0}^{t_N} f_y[x(t), y(t)] dy(t)$$

 $= \int_{-\infty}^{t_N} \left\{ f_x[x(t), y(t)] x'(t) + f_y[x(t), y(t)] y'(t) \right\} dt$ (A1) 391 Let g(t) = f[x(t), y(t)], and after using the chain rule to differentiate g with respect to t, we obtain: 392  $a'(t) = \partial g \, dx + \partial g \, dy = f[r(t) v(t)]r'(t) + f[r(t) v(t)]v'(t)$ 202 (A2)

$$g(t) = \frac{\partial x}{\partial x} \frac{dt}{dt} + \frac{\partial y}{\partial y} \frac{dt}{dt} = f_{x[x(t), y(t)]x(t)} + f_{y[x(t), y(t)]y(t)}$$

Thus, g'(t) is just the integrand in Eq. (A1), and Eq. (A1) can then be rewritten as: 394

The right-hand side of the equation 
$$= \int_{t_0}^{t_N} g'(t) dt = [g(t)]_{t_0}^{t_N} = g(t_N) - g(t_0)$$
  
 $= f[x(t_N), y(t_N)] - f[x(t_0), y(t_0)] =$  The left-hand side of the equation

**Appendix B: The sum of**  $\int_{x} f_x(x, y) dx$  and  $\int_{y} f_y(x, y) dy$  is path-independent 397

**Theorem:** Given an open simply-connected region G (*i.e.*, no holes in G) and two functions P(x, y)398 and Q(x, y) that have continuous first-order derivatives, if and only if  $\partial P/\partial y = \partial Q/\partial x$  throughout G. 399 then  $\int_{V} P(x, y) dx + \int_{V} Q(x, y) dy$  is path independent, *i.e.*, it depends solely on the starting and ending 400 point of L. 401

We have  $\partial f_x/\partial y = \partial^2 z/\partial x \partial y$  and  $\partial f_y/\partial x = \partial^2 z/\partial y \partial x$ . As  $\partial^2 z/\partial x \partial y = \partial^2 z/\partial y \partial x$ , we can state that 402  $\partial f_x / \partial y = \partial f_y / \partial x$ , meeting the above condition and proving that  $\int_{x} f_x(x, y) dx + \int_{y} f_y(x, y) dy$  is path 403 independent. The statement was further exemplified using a fictitious example in Appendix C. 404

#### 405 Appendix C: A fictitious example to show how the LI method works

Runoff (R, 10<sup>-3</sup>m yr<sup>-1</sup>) at a site is assumed to increase from 120 to 195 10<sup>-3</sup>m yr<sup>-1</sup> with  $\Delta R = 75 \ 10^{-3}$ 406 407  $^{3}$ m yr<sup>-1</sup>; meanwhile, precipitation (P, 10<sup>-3</sup> m yr<sup>-1</sup>) varies from 600 to 650 10<sup>-3</sup>m yr<sup>-1</sup> ( $\Delta P = 75 \ 10^{-3}$ m yr<sup>-1</sup>) and the runoff coefficient ( $C_R$ , dimensionless) varies from 0.2 to 0.3 ( $\Delta C_R = 0.1$ ). The goal is to partition 408 409  $\Delta R$  into the effects of the precipitation ( $\Delta R_P$ ) and runoff coefficient ( $\Delta R_{\alpha}$ ), provided that P and  $C_R$  are independent. We have a function  $R = PC_R$  and its partial derivatives  $\partial R / \partial P = C_R$  and  $\partial R / \partial C_R = P$ . Given a 410 path L along which P and  $C_R$  change and using Eq. (3), the LI method evaluates  $\Delta R_P$  and  $\Delta R_{\alpha}$  as: 411 412

$$\Delta R_{C_R} = \int_L \partial R / \partial C_R dC_R = \int_L P dC_R \text{ and } \Delta R_P = \int_L \partial R / \partial P dP = \int_L C_R dP \quad (C1)$$

The result differs depending on L but the sum of  $\Delta R_P$  and  $\Delta R_{C_s}$  uniformly equals  $\Delta R$ . This 413 414 dynamic is demonstrated using Fig. 3, in which we considered that the x-axis represents  $C_R$  and the yaxis P. Point A denotes the initial state ( $C_R = 0.2$ , P = 600) and point C the terminal state ( $C_R = 0.3$ , P =415 650). I calculated  $\Delta R_P$  and  $\Delta R_{C_R}$  along three fictitious paths as follows: 416

L=AC. Line segment AC has equation  $P = 500C_R + 500, 0.2 \le C_R \le 0.3$ . Let's take  $C_R$  as the 417 1) parameter and write the equation in the parametric form as  $P = 500C_R + 500$ ,  $C_R = C_R$ ,  $0.2 \le C_R \le 0.3$ . By 418 substituting the equation into Eq. (C1), we have: 419

420 
$$\Delta R_{CR} = \int_{AC} P dC_R = \int_{0.2}^{0.3} (500C_R + 500) dC_R = 62.5$$

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421 
$$\Delta R_P = \int_{AC} C_R dP = \int_{AC} C_R d(500C_R + 500) = 500 \int_{0.2}^{0.3} C_R dC_R = 12.5$$

422 2) 
$$L=AB+BC$$
. To evaluate on the broken line, we can evaluate separately on AB and BC and then sum  
423 them up. The equation for AB is  $P = 600, 0.2 \le C_R \le 0.3$ , while for BC is  $C_R = 0.3, 600 \le P \le 650$ . Notes

424 that a constant 
$$C_R$$
 or  $P$  implies that  $dC_R = 0$  or  $dP = 0$ . Eq. (C1) then becomes:

425 
$$\Delta R_{C_R} = \int_{AB+BC} P dC_R = \int_{AB} P dC_R + \int_{BC} P dC_R = \int_{0.2}^{0.3} 600 dC_R + 0 = 60$$

426 
$$\Delta R_P = \int_{AB+BC} C_R dP = \int_{AB} C_R dP + \int_{BC} C_R dP = 0 + \int_{600}^{650} 0.3 dP = 15$$

427 3) L=AD+DC. The equation for AD is  $C_R = 0.2$ ,  $600 \le P \le 650$  and is P = 650,  $0.2 \le C_R \le 0.3$  for DC. 428  $\Delta R_P$  and  $\Delta R_{CR}$  are evaluated as:

429 
$$\Delta R_{CR} = \int_{AD+DC} P dC_R = \int_{AD} P dC_R + \int_{DC} P dC_R = 0 + \int_{0.2}^{0.3} 650 dC_R = 65$$

430 
$$\Delta R_P = \int_{AD+DC} C_R dP = \int_{AD} C_R dP + \int_{DC} C_R dP = \int_{600}^{000} 0.2 dP + 0 = 10$$

431 As expected, the sum of  $\Delta R_P$  and  $\Delta R_{CR}$  persistently equals  $\Delta R$  although  $\Delta R_P$  and  $\Delta R_{CR}$  varies with *L*. 432

## 433 Appendix D: Mathematical proof of the path-averaged sensitivity

434 If the interval  $[x_0, x_N]$  in Fig. 3 is partitioned into N distinct bins of the same width  $\Delta x_i = \Delta x/N$ . Eq. 435 (3a) can then be rewritten as:

436 
$$\Delta Z_x = \int_L f_x(x, y) dx = \lim_{\tau \to 0} \sum_{i=0}^{N-1} f_x(x_i, y_i) \Delta x_i = \lim_{\tau \to 0} N \Delta x_i \frac{\sum_{i=0}^{N-1} f_x(x_i, y_i)}{N} = \Delta x \lim_{\tau \to 0} \frac{\sum_{i=0}^{N-1} f_x(x_i, y_i)}{N} = \overline{\lambda} x \Delta x$$

437 where  $\overline{\lambda_x} = \lim_{r \to 0} \frac{\sum_{i=1}^{N} f_x(x_i, y_i)}{N}$ , denoting the average of  $f_x(x, y)$  along the curve *L*. Likewise, we have

438  $\Delta Z_y = \overline{\lambda_y} \Delta y$ , where  $\overline{\lambda_y}$  denotes the average of  $f_y(x, y)$  along the curve *L*. As a result:

$$439 \qquad \Delta Z = \overline{\lambda_x} \Delta x + \overline{\lambda_y} \Delta y \tag{D1}$$

440 The result can readily be extended to a function of three variables. Applying the mathematic 441 derivation determined above to the MCY equation results in a precise form of Eq. (7):

442 
$$\Delta R = \Delta R_P + \Delta R_{e_0} + \Delta R_n = \lambda_P \Delta P + \lambda_{E_0} \Delta E_0 + \lambda_n \Delta n, \qquad (D2)$$

443 where  $\Delta R_P = \overline{\lambda_P \Delta P}$ ,  $\Delta R_{E_0} = \overline{\lambda_{E_0} \Delta E_0}$ ,  $\Delta R_n = \overline{\lambda_n \Delta n}$ , and  $\overline{\lambda_P}$ ,  $\overline{\lambda_{E_0}}$  and  $\overline{\lambda_n}$  denote the arithmetic mean of  $\partial R / \partial P$ ,

- 444  $\partial R/\partial E_0$ , and  $\partial R/\partial n$  along a path of climate and catchment changes, respectively. Because  $\overline{\lambda_P} = \Delta R_P / \Delta P$ ,
- 445  $\overline{\lambda_{E_0}} = \Delta R_{E_0} / \Delta E_0$ , and  $\overline{\lambda_n} = \Delta R_n / \Delta n$ ,  $\overline{\lambda_P}$ ,  $\overline{\lambda_{E_0}}$  and  $\overline{\lambda_n}$  also imply the runoff change due to a unit change in *P*, 446  $E_0$  and *n*, respectively.
- 447

#### 448 Appendix E: Path-averaged sensitivity in one-dimensional cases

Given a one-dimensional function z=f(x) and its derivative f'(x). We assumed that f'(x)averages  $\overline{\lambda}_x$  over the range  $(x, x + \Delta x)$ , *i.e.*  $\overline{\lambda}_x = \lim_{x \to 0} \frac{\sum_{i=1}^{N} f'(x_i)}{N}$ . According to the mean value theorem for integrals,  $\overline{\lambda}_x = \int_x^{x+\Delta x} f'(x) dx / \Delta x$ . In terms of the Newton-Leibniz formula,  $\int_x^{x+\Delta x} f'(x) dx = f(x + \Delta x) - f(x) = \Delta z$ . Thus, we obtain:  $\overline{\lambda}_x = \Delta z / \Delta x$ .

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580	Table 1. Summar	y of the long-term	hydrometeorological	characteristics of the	e selected catchments <sup>a</sup>

							0			
Catchment	Area	R	р	Fo	п	AI	Reference	Evaluation	The final	
No. <sup>b</sup>	$(10^{6}m^{2})$	Λ	1	<b>L</b> 0	n	л	Period	Period	Subperiod	
1	391	218	1014	935	3.5	0.92	1933-1955	1956-2008	1998-2008	
2	16.64	32.9	634	1087	3.16	1.71	1979-1984	1985-2008	1999-2008	
3	559	183	787	780	2.68	0.99	1960-1978	1979-2000	1993-2000	
4	606	73	729	998	3.07	1.37	1971-1995	1996-2009	2003-2009	
5	760	77.9	689	997	2.66	1.45	1970-1995	1996-2009	2003-2009	
6	502	57.2	730	988	3.59	1.35	1974-1995	1996-2008	1996-2008	
7	673	431	1013	953	1.34	0.94	1947-1955	1956-2008	1998-2008	
8	390	139	840	1021	2.61	1.22	1966-1980	1981-2005	1995-2005	
9	1130	20.7	633	1077	3.79	1.7	1972-1982	1983-2007	1997-2007	
<del>10</del>	3.2	37.5	<del>631</del>	<del>95</del> 4	<del>3.49</del>	1.51	<del>1989-1991</del>	<del>1992-2009</del>	<del>1999-2009</del>	
<del>,11</del>	<del>1.95</del>	111	<del>767</del>	<del>901</del>	<del>3.06</del>	<del>1.18</del>	<del>1990-1992</del>	<del>1993-2005</del>	<del>1993-2005</del>	
<u>1210</u>	89	272	963	826	2.82	0.86	1958-1965	1966-1999	1987-1999	
<u>+311</u>	243	38.5	735	1010	4.27	1.37	1989-1995	1996-2007	1996-2007	
1412	56.35	65.8	744	1007	3.35	1.35	1989-1995	1996-2008	1996-2008	
<u>+513</u>	14484	385	893	1022	1.11	1.14	1970-1989	1990-2000	1990-2000	
<u>1614</u>	38625	461	985	1087	1.03	1.1	1970-1989	1990-2000	1990-2000	
<u>1715</u>	59115	388	897	1161	1.02	1.29	1970-1989	1990-2000	1990-2000	
<u>1816</u>	95217	371	881	1169	1.03	1.33	1970-1989	1990-2000	1990-2000	
<u>1917</u>	121,972	171	507	768	1.17	1.52	1960-1990	1991-2000	1991-2000	
<u>2018</u>	106,500	60.5	535	905	2.25	1.69	1960-1970	1971-2009	1999-2009	
<del>21<u>19</u></del>	5891	34.4	506	964	2.54	1.91	1952-1996	1997-2011	2004-2011	

<sup>a</sup>*R*, *P*, and  $E_0$  represent the mean annual runoff, precipitation and potential evaporation, all in 10<sup>-3</sup>m yr<sup>-1</sup>. *n* (dimensionless) is the parameter representing catchment properties in the MCY equation. *AI* is the dimensionless aridity index ( $AI = E_0/P$ ). Data of Catchments 1-<u>14-12</u> were derived from Zhang *et al.* (2010). Data of Catchments <u>1513-18-16</u> were from Sun *et al.* (2014). Data of Catchments <u>1917-21-19</u> were from Zheng *et al.* (2009), Jiang *et al.* (2015), and Gao *et al.* (2016), respectively. I used the change points given in the literatures to divide the observation period into the reference and elevation periods. The LI method further divides the evaluation period into a number of subperiods. The column "The 

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final Subperiod" denotes the final subperiod, which was used as the evaluation period for the total differential method, the decomposition method and the complementary method. The bold and italie rows denote that the column "Evaluation Period" is the same as the column "The final Subperiod".

<sup>b</sup>Catchments 1-14-12 are in Australia and the others are in China. 1: Adjungbilly CK; 2: Batalling Ck; 3: Bombala River; 4: Crawford River; 5: Darlot Ck; 6: Eumeralla River; 7: Goobarragandra CK; 8: Jingellic CK; 9: Mosquito CK; 10: Pine Ck; 11: Red Hill; 1210: Traralgon Ck; 1311: Upper Denmark 

River; 1412: Yate Flat Ck; 1513: Yangxian station, Hang River; 1614: Ankang station, Hang River; 1715: Baihe station, Hang River; 1816: Danjiangkou station, Hang River; 1917: Headwaters of the Yellow River Basin; 2018: Wei River; 2119: Yan River. 

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601	Table 2	Companiana	of	D

601	<b>Table 2.</b> Comparisons of R (mm yr <sup>-1</sup> ), P (mm yr <sup>-1</sup> ), $E_0$ (mm yr <sup>-1</sup> ), and n (dimensionless) between the
602	reference and the evaluation periods <sup>a</sup>

Catchment	n	n	D	n	F	F					AE	
No.	$K_1$	$\kappa_2$	$P_1$	$P_2$	$E_{01}$	$E_{02}$	$n_1$	$n_2$	$\Delta R$	$\Delta P$	$\Delta E_0$	$\Delta n$
1	223	216	959	1038	950	928	2.7	4.1	-7.2	79.2	-21	1.4
2	40.6	31	655	629	1087	1087	3	3.2	-9.7	-27	0	0.2
3	249	127	847	736	780	780	2.3	3.2	-122	-112	0.4	0.9
4	90.6	41.5	753	685	1002	989	2.9	3.7	-49	-67	-13	0.8
5	94.9	46.3	718	633	1000	992	2.5	3	-49	-85	-9	0.5
6	70.8	34.3	756	687	989	987	3.4	4.1	-36	-69	-2	0.6
7	575	406	1123	995	931	957	1.1	1.4	-169	-128	25	0.3
8	139	139	871	821	1043	1008	2.7	2.5	-0.4	-50	-35	<u>-0.2</u>
9	24.1	19.2	659	621	1100	1067	3.7	3.8	-4.9	-37	-33	0.1
<del>10</del>	<del>116</del>	24.3	<del>588</del>	<del>638</del>	<del>927</del>	<del>958</del>	1.7	4.2	- <del>92</del>	<del>50.4</del>	<del>31</del>	2.5
-11	<del>297</del>	<del>68</del>	<del>986</del>	716	<del>884</del>	<del>905</del>	2.3	<del>3.6</del>	-229	-271	22	1.3
<u>10<mark>12</mark></u>	301	265	992	956	820	828	2.7	2.8	-36	-36	7.4	0.1
<u>11<mark>13</mark></u>	48.5	32.6	752	725	991	1021	4.2	4.4	-16	-28	30	0.2
<u>12<mark>14</mark></u>	90.4	52.6	753	739	991	1015	2.9	3.7	-38	-14	24	0.8
<u>1345</u>	435	295	948	795	1008	1047	1.1	1.2	-139	-153	38	0.1
<u>14<del>16</del></u>	520	353	1035	894	1074	1109	1	1.2	-167	-141	35	0.2
<u>15</u> 17	441	291	939	820	1149	1182	1	1.2	-151	-119	33	0.2
<u>16</u> 18	412	296	913	821	1163	1179	1	1.1	-116	-92	15	0.2
<u>17</u> 19	180	144	512	491	774	751	1.1	1.3	-36	-21	-23	0.2
<u>18</u> 20	90.2	52.1	585	520	895	908	2.1	2.3	-38	-65	13	0.2
<u>19</u> 21	37.7	24.6	521	462	954	995	2.6	2.5	-13	-59	41	<u>0-0.1</u>

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603	<sup>a</sup> The subscript "1" denotes the reference period and "2" denotes the evaluation period. $\Delta X = X_2 - X_1$ (X as
604	a substitute for $R, P, E_0$ , and $n$ ).

622	<b>Table 3.</b> Effects of precipitation ( $\Delta R_P$ , 10 <sup>-3</sup> m yr <sup>-1</sup> ), potential evapotranspiration ( $\Delta R_{E_0}$ , 10 <sup>-3</sup> m yr <sup>-1</sup> ), and
623	catchment changes ( $\Delta R_n$ , 10 <sup>-3</sup> m yr <sup>-1</sup> ) on the mean annual runoff determined from the four evaluated
624	methods

Catchment	LI Method			Decomposition Method	Total	Differe Method	ential I	Con	nplemer Method	ntary	
NO."	$\Delta R_P$	$\Delta R_{E_0}$	$\Delta R_n$	$\Delta R_n$	$\Delta R_P$	$\Delta R_{E_0}$	$\Delta R_n$	$\Delta R_P$	$\Delta R_{E_0}$	$\Delta R_n$	
1	-70.9	-8.99	-24.3	-44.6	-67	4.82	-62	-60.7	4.34	-47.3	
2	-6.49	0.95	-9.74	-9.65	-7.2	1.3	-13	-6.23	1.13	-10.2	
3	-89	25.9	-140	-128	-104	26.6	-483	-88	25.7	-140	
4	-18.1	2.09	-35.4	-36.3	-18	2.37	-58	-14.8	1.99	-38.5	
5	-27.9	1.14	-21.3	-18.6	-34	1.18	-27	-28.1	0.97	-20.9	
6	-19.9	0.29	-16.7	-14.9	-24	0.36	-22	-19.9	0.29	-16.7	
7	-211	-7.19	-101	-90.9	-236	-6.9	-134	-211	-6.21	-102	
8	-32.2	12.3	-14.4	-12.6	-35	12.6	-15	-32.9	11.9	-13.3	
9	-11.8	3.02	-9.96	-8.45	-13	0.85	-20	-8.76	0.56	-10.5	
<del>10</del>	<del>19.47</del>	-5.61	-119	<del>-96.5</del>	<del>0.91</del>	-10	-291	0.56	-6.53	<del>-99.1</del>	
<u>_11</u>	<del>-150</del>	-7.46	-71.8	<del>-60.7</del>	<del>-188</del>	<del>-9.4</del>	-113	-144	-7.04	<del>-78.3</del>	
<u>10</u> 12	-9.88	-3.99	-79.2	-82	-11	-0.5	-154	-10.8	-0.57	-81.6	
11,13	-6.98	-4.36	-4.54	-4.21	-8	-5.1	-5.2	-7	-4.38	-4.51	
1214	-4.84	-4.42	-28.7	-27.9	-5.6	-5	-37	-4.85	-4.4	-28.6	
<u>13<del>15</del></u>	-104	-8.56	-24.8	-23	-110	-9.4	-27	-103	-8.52	-25.1	
1416	-99.3	-7.99	-58.8	-56	-105	-8.3	-68	-99	-7.92	-59.1	
15,17	-78.8	-6.26	-63.9	-61	-84	-6.5	-76	-78.6	-6.2	-64.2	
<u>16<del>18</del></u>	-60.1	-2.79	-53.5	-52	-64	-2.9	-62	-60	-2.77	-53.6	
<u>17<del>19</del></u>	-11.9	3.89	-27.6	-27	-12	3.81	-31	-11.9	3.85	-27.5	
<u>18</u> 20	-27.5	-2.46	-18.5	-17	-31	-4.4	-26	-25.5	-3.47	-19.5	
<u>19</u> 21	-10.4	-3.47	-2.11	-3.4	-9.9	-4.8	-4.8	-8.27	-3.86	-3.82	

625	#The hold an	d italic number	denote that the	evaluation period	comprises (	s single sub	pariod
	The bold an	a nune nunioen	denote that the	evaluation period	r comprises c	i single subj	Jerroa

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**Table 4.** Comparisons of the path averaged sensitivities with the point sensitivities of runoff<sup>a, b</sup>

)	Table 4.	Com	<del>barison</del>	<del>s of the</del>	<del>) path a</del>	verageo	l sensit	<del>ivitie</del>
	Catchm- ent NO.	$\frac{1}{\lambda_P}$	$\overline{\lambda_{E_0}}$	$\frac{1}{\lambda_n}$	2 Pf	<del>LEOF</del>	Anj	
	+	<del>0.68</del>	<del>-0.55</del>	-17	<del>0.621</del>	<del>-0.39</del>	<del>-71.8</del>	
	2	<del>0.2</del>	-0.08	-27.3	<del>0.227</del>	<del>-0.1</del>	<del>-30.9</del>	
	3	<del>0.58</del>	-0.36	-26.7	0.68	-0.42	<del>-79</del>	
	4	0.3	-0.16	-30.5	0.39	-0.2	-50.1	
	5	<del>0.33</del>	<del>-0.14</del>	<del>-43.1</del>	<del>0.394</del>	<del>-0.19</del>	<del>-59.4</del>	
	6	<del>0.29</del>	-0.16	-26.5	0.352	-0.2	<del>-34.9</del>	
	7	0.71	-0.32	-223	<del>0.781</del>	<del>-0.33</del>	<del>-299</del>	
	8	<del>0.49</del>	-0.26	<del>-77.9</del>	<del>0.478</del>	-0.27	<del>-64.9</del>	
	9	<del>0.16</del>	-0.07	<del>-11.8</del>	<del>0.161</del>	<del>-0.07</del>	<del>-17.6</del>	
	<del>10</del>	0.27	-0.12	-40.9	<del>0.45</del>	<del>-0.16</del>	<del>-99.9</del>	
		<del>0.55</del>	<del>-0.35</del>	<del>-56.1</del>	<del>0.695</del>	<del>-0.44</del>	<del>-88.2</del>	
	<mark>12</mark>	0.72	- <del>0.45</del>	<u>-57.3</u>	0.74	- <del>0.53</del>	<del>-61.1</del>	
	<mark>,13</mark>	0.25	<del>-0.15</del>	<del>-19.8</del>	<del>0.29</del>	<del>-0.17</del>	<u>-22.5</u>	
	<mark>.14</mark>	<del>0.34</del>	<del>-0.18</del>	-37.2	<del>0.393</del>	-0.21	<del>-48.6</del>	
	<mark>15</mark>	<del>0.68</del>	-0.22	<del>-275</del>	<del>0.719</del>	<del>-0.25</del>	<del>-303</del>	
	<mark>,16</mark>	0.7	-0.23	-326	<del>0.745</del>	<del>-0.2</del> 4	<del>-378</del>	
	<mark>,17</mark>	<del>0.66</del>	<del>-0.19</del>	-320	<del>0.708</del>	-0.2	<del>-378</del>	
	<mark>,18</mark>	<del>0.65</del>	<del>-0.19</del>	-315	0.692	<del>-0.19</del>	<del>-363</del>	
	<mark>,19</mark>	<del>0.58</del>	<del>-0.17</del>	<del>-153</del>	0.602	<del>-0.17</del>	<del>-175</del>	
	<mark>,20</mark>	<del>0.32</del>	-0.12	<del>-50.1</del>	0.402	<del>-0.16</del>	<del>-69.6</del>	
	<mark>21</mark>	0.2	-0.06	-29.2	<del>0.23</del> 4	<del>-0.09</del>	-34	

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 $\overline{\lambda_P}$  (10<sup>-3</sup>m10<sup>-3</sup>m<sup>-1</sup>),  $\overline{\lambda_{E_0}}$  (10<sup>-3</sup>m - 10<sup>-3</sup>m<sup>-1</sup>), and  $\overline{\lambda_n}$  (dimensionless) represent the path averaged

642 sensitivities of runoff to precipitation, potential evaporation, and catchment properties (see Appendix D).

643 If the evaluation period comprised only one subperiod,  $\overline{\lambda_P}$ ,  $\overline{\lambda_{E_0}}$  and  $\overline{\lambda_n}$  was calculated as:  $\overline{\lambda_P} = \Delta R_P / \Delta P$ ;

- 644  $\overline{\lambda_{E_0}} = \Delta R_{E_0} / \Delta E_{\overline{v}}, \text{and} \overline{\lambda_n} = \Delta R_n / \Delta \overline{n}$ . If the evaluation period comprised N>1 subperiods, the equations became: 645  $\overline{\lambda_r} = \sum_{i=1}^{N} |\Delta R_n| / \sum_{i=1}^{N} |\Delta P_i|, \overline{\lambda_{E_0}} = -\sum_{i=1}^{N} |\Delta R_{E_0}| / \sum_{i=1}^{N} |\Delta E_0|, \overline{\lambda_n} = -\sum_{i=1}^{N} |\Delta R_n| / \sum_{i=1}^{N} |\Delta R_n|, where the subscript$ *i*denotes the*i*th
- 646 <del>subperiod.</del>
- <sup>b</sup> $\mathcal{P}_{\mathcal{P}}$ ;  $\mathcal{A}_{\mathcal{P}}$ ;  $\mathcal{A}_{\mathcal{D}^{\circ}}$ ;  $\mathcal{A}_{\mathcal{D}}$  represent the point sensitivities of runoff of the total differential method, which was calculated by substituting the observed mean annual values of the reference period into Eq. (2).
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- 651



**Fig. 1.** For a non-linear function z = f(x), the total differential method (a) and the complementary method (b) fails to accurately estimate the effect  $(\Delta z_x)$  of x on z when x changes by  $\Delta x$ , but the LI method (c) does. For a univariate function, the z change is exclusively driven by x, so that  $\Delta z_x$  should be equal to  $\Delta z$ .  $\Delta z_x = \Delta z$  in (c) but not in (a) and (b).  $\overline{\lambda_x}$  in (c) represents the average sensitivity along the curve AC and  $\overline{\lambda_x} = \Delta z/\Delta x$ , see Appendix E for details.



Fig. 2. A schematic plot to illustrate the decomposition method. Pont A denotes the initial state (the reference period) and Point C denotes the terminal state (the evaluation period).  $R_2$  represents the mean annual runoff of the evaluation period, and  $R_2$  the mean annual runoff given the climate conditions of the evaluation period and the catchment conditions of the reference period. See Section 2.4 for details. 





Fig. 4. Comparisons between the LI method and the decomposition method. (a) Comparison of the estimated contributions to the runoff changes from the catchment changes ( $\Delta R_n$ ); (b) the decomposition method is equivalent to the LI method that assumes a sudden change in catchment properties following climate change. In this case, the integral path of the LI method can be considered as the broken linepath ABC AB+BC in Fig. 3 (x represents climate factors and y catchment properties, i.e. n) and  $\Delta R_n = \int_{AB+BC} \frac{\partial R}{\partial n} dn = \int_{AB} \frac{\partial R}{\partial n} dn + \int_{BC} \frac{\partial R}{\partial n} dn = 0 + \int_{BC} \frac{\partial R}{\partial n} dn = \int_{n_1}^{n_2} f_n(P_2, E_{02}, n) dn , \text{ where the subscript "1"}$ denotes the reference period and "2" denotes the final subperiod of the evaluation period. 







**Fig. 6.** Comparisons of (a)  $\Delta R_P$ , (b)  $\Delta R_{E_0}$ , and (c)  $\Delta R_\pi$  between the LI method and the complementary method (a = 0.5).











705 706 Fig. 8. Boxplots showing the temporal variability of the path averaged sensitivities of water yield to precipitation  $(\overline{\lambda_{P}})$ , potential evapotranspiration  $(\overline{\lambda_{E_0}})$ , and catchment properties  $(\overline{\lambda_{n}})$ . D (%) was 707 calculated as the relative difference between the sensitivity of the whole evaluation period and that of a 708 subperiod. In the calculations, I excluded the catchments that had an evaluation period comprising only 710 one subperiod. The boxes span the inter quartile range (IQR) and the solid lines are medians. The 711 whiskers represent the data range, excluding statistical outliers, which extend more than 1.5IQR from the box ends.



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