# Revision Notes (hess-2019-359)

## Responses to the comments of Editor:

**Recommendation:** The manuscript has been reviewed by two reviewers, and the authors have, in my view, responded adequately to the issues raised.

I have, however, two additional issues that were not raised by the reviewers, and which I like to share with the authors. I invite the authors to take my comments into account when submitting an improved version of the paper. I encourage the authors to submit a revised version of the paper, taking also the above details into account.

**Response:** We are appreciating to the editor for the useful comments and suggestions to the paper. Based on that, we have made corresponding changes to furtherly improve the quality of this paper. Below are the detailed responses to all comments. We cited first the comment, which is followed by our response and often by a section how the text will be revised in the manuscript. The text in blue are changes and additions in the original text. For clarity we do not show the removed text in the blue content.

**Comment1:** There are some references in the text that do not appear in the reference list; take for example the references cited in lines 55 to 62: of the 9 references, 5 do not appear in the reference list. Also check the reference in line 174.

**Response:** Thanks very much for this useful comment. We are sorry for not presenting the references in the reference list. Here we added corresponding references in L672-673, L694-696, L709-713, L742-744, L765-766 as following:

"Bouman, B. A. M., 2007. Water management in irrigated rice: coping with water scarcity. Int. Rice Res. Inst.."

"Jiang, Y., Xu, X., Huang, Q., Huo, Z., Huang, G., 2015. Assessment of irrigation performance and water productivity in irrigated areas of the middle Heihe River basin using a distributed agro-hydrological model. Agricultural water management, 147, pp.67-81."

"Men, B. H., 2000. Discussion on formula of channel flow loss and water utilization coefficient.

China Rural Water and Hydropower, 2, 33-34.

Morison, J.I.L., Baker, N.R., Mullineaux, P.M., Davies, W.J., 2008. Improving water use in crop production. Philosophical Transactions of the Royal Society B: Biological Sciences, 363(1491), pp.639-658."

"Surendran, U., Jayakumar, M., Marimuthu, S., 2016. Low cost drip irrigation: Impact on sugarcane yield, water and energy saving in semiarid tropical agro ecosystem in India. Science of the Total Environment, 573, pp.1430-1440."

"Williams, W.D., 1999. Salinisation: A major threat to water resources in the arid and semi-arid regions of the world. Lakes & Reservoirs: Research & Management, 4(3-4), pp.85-91."

**Comment2:** The manuscript is inconsistent with its units. All water fluxes should have a time dimension. So $W_{ls}$ (line 193-194) is the groundwater recharge per unit; and in your model you use a daily time step, so the correct unit is m/day. Same for $W_{as}$ (line 202-203), $I_n$ (line 203), $D_g$ (line 213), $W_{gr}$ (line 224), $P_{wg}$ (lines 251-252), $G_{wg}$ (lines 252-253). Check the correct unit of $K$ (permeability coefficient, lines 224-225), I think it should have a time dimension. Check eq.10 on consistency of the units/dimensions.

**Response:** Thanks very much for this useful comment. We are sorry for careless writing on the units of all water fluxes. Here we did a throughout check on all water fluxes' units and made corresponding corrections in L203-204, L212-214, L224, L227-228, L235-236, L255-258, L266-269 of revised manuscript as following:

"$W_{ls}$ is the daily groundwater recharge per unit area due to water conveyance loss in main and sub-main canals ($\mathrm{mday}^{-1}$)."

"where $W_{as}$ represents daily groundwater recharge per unit area due to water conveyance loss in lateral and field canals ($\mathrm{mday}^{-1}$), and $I_n$ is daily irrigation water depth applied per unit area ($\mathrm{mday}^{-1}$)."

"where $D_g$ is daily groundwater drainage per unit area ($\mathrm{mday}^{-1}$)."

"$h_g$ represents the daily groundwater table depth (mday$^{-1}$), and $h_{db}$ is the daily streambed depth of drainage ditch (mday$^{-1}$)."

"where $W_{gr}$ is the daily groundwater inflow of the current HRU from adjacent HRUs (mday$^{-1}$), and $K$ is the daily permeability coefficient of unconfined aquifers in the current HRU (mday$^{-1}$)."

"where $W_{grup}$, $W_{grdown}$, $W_{grleft}$ and $W_{grright}$ are the daily groundwater lateral runoff per unit area into the current groundwater unit from up and down or left and right adjacent groundwater unit, respectively (mday$^{-1}$). $SCa$ is the daily soluble salt content in the saturated zone below the transmission soil profile (mg m$^{-2}$day$^{-1}$)."

"$ext$ is the daily groundwater extraction per unit area (mday$^{-1}$). $P_{wg}$ is the daily percolation water depth to groundwater from the potential root zone (mday$^{-1}$), and $G_{wg}$ is the daily water depth supplied to the potential root zone from shallow groundwater due to the rising capillary action (mday$^{-1}$). $P_{sg}$ and $G_{sg}$ are the quantity of soluble salt in $P_{wg}$ and $G_{wg}$, respectively (mg m$^{-2}$day$^{-1}$)."

**Comment3:** The amount of irrigation water applied seems small (lines 320-323); I calculated an average gross irrigation application of 162 mm/year [(12x108)/(0.66*1.12*106*104)=0.162 m/year]. Kindly explain.

**Response:** Thanks very much for this useful comment and suggestion. We are sorry for the careless writing about the area of JFID, and the correct number should be 0.22 Mha. We made corresponding correction in L336 of revised manuscript as following:

"The JFID covers an area of 0.22 Mha…"

**Comment4:** Lines 388-391: What are thresholds for acceptable and good model performance for the 3 evaluation criteria used (NSE, R2 and RMSE)?

**Response:** Thanks for this useful comment. We made further explanation of the thresholds for acceptance and good model performance for these three evaluation indexes in L410-419 of revised manuscript as following:

"The *RMSE* indicates a perfect match between observation and simulation when it equals 0, and increasing *RMSE* values indicate an increasingly poor match. Singh et al. (2005) stated that *RMSE* values less than 50% of the standard deviation of the observed data could be considered low enough as an indicator of a good model prediction. Ranging between $-\infty$ and 1, the NSE indicates a perfect match between observed and predicted values when it equals to 1. Values between 0 and 1 are generally considered as acceptable levels of performance, whereas values less than 0.0 indicate that the simulation is worse than taking an average of observation, which indicates unacceptable performance. The $R^2$ ranging between 0 and 1 describes the proportion of the variance in the observed data, in which higher values indicating less error variance. Typically, $R^2 > 0.5$ is considered acceptable (Santhi et al., 2001)."

Additionally, we added two references in the reference list in L724-726 and L733-735 of revised manuscript as following:

"Santhi, C., Arnold, J.G., Williams, J.R., Dugas, W.A., Srinivasan, R., Hauck, L.M., 2001. Validation of the swat model on a large rwer basin with point and nonpoint sources 1. JAWRA Journal of the American Water Resources Association, 37(5), pp.1169-1188."

"Singh, J., Knapp, H.V., Arnold, J.G., Demissie, M., 2005. Hydrological modeling of the Iroquois river watershed using HSPF and SWAT 1. JAWRA Journal of the American Water Resources Association, 41(2), pp.343-360."

**Comment5:** Line 451: "readily available groundwater"; here I think you deal with the unsaturated zone, so do you rather mean: "readily available soil moisture"?

**Response:** Thanks very much for this comment and suggestion. We actually tried to express the parameter specific yield as the volume of water gained or lost under gravity or capillary action with a corresponding amount of water table rise or fall. Here we corrected the expression of sentence in L490-492 of revised manuscript as following:

"The specific yield indicated the readily available soil moisture released to crop root zone from shallow aquifer under capillary action for crop consumption."

**Comment6:** Figure 9: in an earlier iteration I asked the authors to improve the colour-scheme of this figure. You have done so, but in the process, you have, unfortunately, not standardized the scales (as you had done in the original version of this figure, and as you have also correctly done in your figure S3). For the reader it is therefore very difficult to compare the different years. So for each crop redraw the maps by keeping the colour scale fixed over the years.

**Response:** Thanks very much for this comment and suggestion. We redrew the IWP maps for three main crops in Fig.9 to make the scales standardized. After that, we believe that readers could compare the different years of IWP for three crops easily. Detailed changes see Fig.9 in the revised manuscript.

**Comment7:** Figure 9 once more: none of the maps contain blank pixels – this suggest that each pixel in all years have values for the productivity of all three crops. This I find highly surprising, and in fact unlikely, (but I admit that I do not know the irrigation district). Please explain.

**Response:** Thanks for this useful comment. Fig.9 represents the spatial distribution of IWP for three crops (wheat, maize and sunflower) at a given year at 1km*1km simulation unit scale. As you know, although main crops is wheat, maize and sunflower, spatial distribution of these crops is very complex and field plot is small.  we use remote sensing data to get cropping pattern map with resolution of 30m*30m, almost every HRU (1km*1km) have these crops. Thus, we can simulate IWP for each main crop in every HRU. Considering the heterogeneity of cropping pattern in the simulation unit, therefore, even if there is only one pixel of any crop planted in the 1km*1km simulation unit, the IWP of this crop should be reflected on the current simulation unit in the RIWP map in Fig.9. Fig. 9 only shows the IWP of crop located in related HRUs. Thus, we would like to keep our original Figure 9 in the revised manuscript expect for standardizing the scales. We have explained these in L526-529 of revised paper as following:

"As we mentioned before, the spatial distribution of these three crops is very complex in JFID and field plot is small, thus we use remote sensing data to obtain cropping pattern map with resolution of 30m*30m. Every HRU has these three crops, thus we can simulate IWP for each main crop in every HRU."

**Comment8:** Section 3.2.1 concludes about which crops have the highest productivity (lines 481-486). Here productivity in money value (expressed e.g. in US$/m3 or RMB/m3) would be the most convincing criterion. Do you have average farm gate prices of the three crops, so that you can convert the IWP (kg/m3) into RMB/m3? You suggest that sunflower has a much higher "benefit" (line 485) than wheat. Do you mean "price"?

**Response:** Thanks very much for these useful comments. Yes, "higher benefit" here indicated that sunflower has a much higher "price" per unit weight than the other two crops. We are currently working on another paper which is focused on addressing how productivity in money value varied under the effect of years of water saving agricultural development in JFID. Here, in this paper, we would like to focus on looking at the simulation result of our RIWP model, which is the IWP, crop yield per cubic meter of irrigation water applied.

**Comment9:** The manuscript still is weak in grammar, and reviewer #2 did a great job to highlight the major weaknesses. Please also check the following lines: 15, 72, 98, 146, 196, 206, 269, 293, 295, 296, 315, 364, 427.

**Response:** Thanks very much for this comment. We made further correction on writing to improve the quality of this paper. Below are detailed revised places:

L15-16 "Department of Land, Air and Water Resources & Department of Biological and Agricultural Engineering …"

L77: "However, remote sensing is looking at seeing…"

L106: "…productivity models in irrigated areas"

L157: "…first runs field IWP model"

L206-207: "Lateral and field canals are densely distributed in the irrigated area, and they are intermittently filled with low water flow."

L217: "In the drainage system module, only the groundwater draining into ditches is considered. …"

L285: "Finally, the weighted averages are used to update daily groundwater …"

L310-312: "Distribution of soil physical properties, moisture and salinity in unsaturated soil, groundwater table depth and salinity, need to be collected from many observation sites, which are uniformly or randomly spread over the study area."

L330-331: “…arid irrigated area with shallow groundwater, resulted from its arid-continental climate, over years of flood irrigation, and poor drainage systems”

L383-384: “…, which covers the growing seasons of all the three main crops.”

L459-460: “In the model, for each year, we adopt same drainage coefficient for all the ditches of the different orders, assuming a well operated condition.”

**__List of all relevant changes corresponding to the comments of Editor:__**

**Comment1:** L672-673 “Bouman, B. A. M., 2007. Water management in irrigated rice: coping with water scarcity. Int. Rice Res. Inst..”

L694-696 “Jiang, Y., Xu, X., Huang, Q., Huo, Z., Huang, G., 2015. Assessment of irrigation performance and water productivity in irrigated areas of the middle Heihe River basin using a distributed agro-hydrological model. Agricultural water management, 147, pp.67-81.”

L709-713 “Men, B. H., 2000. Discussion on formula of channel flow loss and water utilization coefficient. China Rural Water and Hydropower, 2, 33-34.

Morison, J.I.L., Baker, N.R., Mullineaux, P.M., Davies, W.J., 2008. Improving water use in crop production. Philosophical Transactions of the Royal Society B: Biological Sciences, 363(1491), pp.639-658.”

L742-744 “Surendran, U., Jayakumar, M., Marimuthu, S., 2016. Low cost drip irrigation: Impact on sugarcane yield, water and energy saving in semiarid tropical agro ecosystem in India. Science of the Total Environment, 573, pp.1430-1440.”

L765-766 “Williams, W.D., 1999. Salinisation: A major threat to water resources in the arid and semi-arid regions of the world. Lakes & Reservoirs: Research & Management, 4(3-4), pp.85-91.”

**Comment2:** L203-204 “$W_{ls}$ is the daily groundwater recharge per unit area due to water conveyance loss in main and sub-main canals (mday$^{-1}$).”

L212-214 "where $W_{as}$ represents daily groundwater recharge per unit area due to water conveyance loss in lateral and field canals ($\mathrm{mday}^{-1}$), and $I_n$ is daily irrigation water depth applied per unit area ($\mathrm{mday}^{-1}$)."

L224 "where $D_g$ is daily groundwater drainage per unit area ($\mathrm{mday}^{-1}$)."

L227-228 "$h_{\mathrm{g}}$ represents the daily groundwater table depth ($\mathrm{mday}^{-1}$), and $h_{db}$ is the daily streambed depth of drainage ditch ($\mathrm{mday}^{-1}$)."

L235-236 "where $W_{gr}$ is the daily groundwater inflow of the current HRU from adjacent HRUs ($\mathrm{mday}^{-1}$), and $K$ is the daily permeability coefficient of unconfined aquifers in the current HRU ($\mathrm{mday}^{-1}$)."

L255-258 "where $W_{grup}$, $W_{grdown}$, $W_{grleft}$ and $W_{grright}$ are the daily groundwater lateral runoff per unit area into the current groundwater unit from up and down or left and right adjacent groundwater unit, respectively ($\mathrm{mday}^{-1}$). $SCa$ is the daily soluble salt content in the saturated zone below the transmission soil profile ($\mathrm{mg\ m^{-2}day^{-1}}$)."

L266-269 "$ext$ is the daily groundwater extraction per unit area ($\mathrm{mday}^{-1}$). $P_{wg}$ is the daily percolation water depth to groundwater from the potential root zone ($\mathrm{mday}^{-1}$), and $G_{wg}$ is the daily water depth supplied to the potential root zone from shallow groundwater due to the rising capillary action ($\mathrm{mday}^{-1}$). $P_{sg}$ and $G_{sg}$ are the quantity of soluble salt in $P_{wg}$ and $G_{wg}$, respectively ($\mathrm{mg\ m^{-2}day^{-1}}$)."

**Comment3:** L336 "The JFID covers an area of 0.22 Mha…"

**Comment4:** L410-419 "The *RMSE* indicates a perfect match between observation and simulation when it equals 0, and increasing RMSE values indicate an increasingly poor match. Singh et al. (2005) stated that *RMSE* values less than 50% of the standard deviation of the observed data could be considered low enough as an indicator of a good model prediction. Ranging between $-\infty$ and 1, the NSE indicates a perfect match between observed and predicted values when it equals to 1. Values between 0 and 1 are generally considered as acceptable levels of performance, whereas values less than 0.0 indicate that the simulation is worse than taking an average of observation, which indicates unacceptable performance. The $R^2$ ranging between 0 and 1 describes the proportion of the variance in the observed data, in which higher values indicating less error variance. Typically, $R^2 > 0.5$ is considered acceptable (Santhi et al., 2001).”

L724-726 “Santhi, C., Arnold, J.G., Williams, J.R., Dugas, W.A., Srinivasan, R., Hauck, L.M., 2001. Validation of the swat model on a large rwer basin with point and nonpoint sources 1. JAWRA Journal of the American Water Resources Association, 37(5), pp.1169-1188.”

L733-735 “Singh, J., Knapp, H.V., Arnold, J.G., Demissie, M., 2005. Hydrological modeling of the Iroquois river watershed using HSPF and SWAT 1. JAWRA Journal of the American Water Resources Association, 41(2), pp.343-360.”

**Comment5:** L490-492 “The specific yield indicated the readily available soil moisture released to crop root zone from shallow aquifer under capillary action for crop consumption.”

**Comment6.** Figure 9 of revised manuscript

**Comment7:** L526-529 “As we mentioned before, the spatial distribution of these three crops is very complex in JFID and field plot is small, thus we use remote sensing data to obtain cropping pattern map with resolution of 30m*30m. Every HRU has these three crops, thus we can simulate IWP for each main crop in every HRU.”

**Comment8:** No change in context

**Comment9:** L15-16 “Department of Land, Air and Water Resources & Department of Biological and Agricultural Engineering …”

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L459-460 “In the model, for each year, we adopt same drainage coefficient for all the ditches of the different orders, assuming a well operated condition.”

**Responses to the comments of Reviewer #1:**

The study principally simulated soil hydrology and crop irrigation water productivity with recently developed regional temporal-spatial hydrological model in the arid district. These results attributes mainly to the dynamic-management of local agricultural water resources distribution and crop cropping system under changing climate environment, e.g. salinity, groundwater depth. The paper is well written and organized with novel idea and new findings. The model’s simulation results are reasonable. Suggest accept after addressing these comments:

**Response:** We are appreciating to the reviewer for the useful comments and suggestions to the paper. According to your comments, we have made further efforts to make the paper acceptable for publication. We make a large number of revisions based on the comments to make the paper easier to read. We believe that the quality of this paper has been fundamentally improved after that.

Below are the corresponding responses to the reviewer’s eight detailed comments. We cited first the comment, which is followed by our response and often by a section how the text will be revised in the manuscript. The text in blue are changes and additions in the original text. For clarity we do not show the removed text in the blue content.

**Comment1:** The title is too long and needs revision. Suggest: A novel regional irrigation water productivity model coupling soil hydrology and salinity dynamics in arid regions, China

**Response:** Thanks very much for this useful comment. We rewrote the title to "A novel regional irrigation water productivity model coupling irrigation-drainage driven soil hydrology and salinity dynamics, and shallow groundwater movement in arid regions, China".

**Comment2:** L39-40 in Abstract, how about the simulation agreement of validation and calibration plots?

**Response:** Thanks very much for this useful comment. We added the detailed model simulation performance in the L41-45 of revised manuscript as "The model reasonably well simulated soil moisture and salinity, as well as groundwater table depths and salinity. Overestimations of groundwater discharge were detected in calibration and validation due to the assumption of well-operated condition of drainage ditches, and regional evapotranspiration (ET) were reasonably estimated while ET in uncultivated area was slightly underestimated in RIWP model".

**Comment3:** Provide details on model's calibration procedure before L345 as subtitle 2.3.2.

**Response:** Thanks very much for this useful comment and suggestion. We added the detailed procedures of model's calibration and validation procedures in the revised manuscript as subtitle 2.3.3 as following:

### 2.3.3 Model calibration and validation

To comprehensively evaluate the accuracy and reliability of the model, the data in years 2010-2013 and in years 2006-2009 was respectively used as calibration and validation dataset. The daily measured soil moisture content of crop root zone (θ), electrical conductivity of soil water (EC), groundwater table depth ($h_g$) and groundwater salinity, were calibrated with measured data from the 22 soil water and salt observation sites and 55 groundwater observation sites (Fig. 5), which were mentioned in section 2.3.1. The RIWP simulated regional ET for each HRU was calibrated by the remote sensing based ET images obtained once per 8 days. The regional drainage processes was calibrated by the monthly groundwater drainage data from main ditches, in which the simulated drainage of each main ditch was the sum of drainage of its controlling HRUs.

We revised the name of subtitle 2.3.2 to “Parameterization of distributed RIWP model”.

**Comment4:** Crop growth is closely with ET? What are the model simulation performances of cash crops growth (biomass, LAI, phonology) and grain yield in the calibration and validation systems in the section of 3.1.

**Response:** Yes. The crop ET module embedded in the regional RIWP model is based on FAO Irrigation & Drainage 56 ($ET_m = K_c * ET_0; ET_0 = \frac{0.408\Delta(R_n-G)+900\gamma u_2\frac{(e_s-e_a)}{T+273}}{\Delta+\gamma(1+0.34u_2)}$ ) and the equation developed by Pereira et al. (2007) ($\frac{ET_{a\ ws}}{ET_m} = K_{sc} = K_{ss}K_{sw} = \left[1 - \frac{b}{100*k_y}(EC_e - EC_{et})\right]\frac{TAW_{salt}-D_r}{(1-p_{cor})TAW_{salt}}$) to estimate crop actual ET under water stress and/or saline condition. Actual ET is affected by the soil water and salt content in the crop current root zone, and due to the crop root growth during the growing season the crop root zone is changing with time. We applied an empirical equation to quantify the crop root depth change with time in our ET module. In one hand, ET is affected by the soil water and salt content in the root zone, on the other hand, ET will affect the soil water and salt content in the root zone due to its role of water balance component. Thus, crop growth is closely connected to ET in our study. We did not include the estimation of biomass such as LAI, crop height in the ET and yield estimation module in our study. Also, as crop yield is actually affected by the crop actual ET during the growing season, we used the model of Stewart et al. (1977) ($\frac{Y_a}{Y_m} = \prod_{j=1}^{n=4}\left(1 - k_y\left(\frac{ET_{aj}}{ET_{mj}}\right)\right)$) to calculate crop yield in our study, in which crop ET and yield has a positive correlation. However, due to the lack of yield data, we only calibrated regional ET and made validation, and the model simulation indicated a reasonable performance of regional ET.

**Comment5:** Each section of the three Results and Discussion is needed for greater improvement especially in global sensitivity analysis and irrigation water productivity. Provide more explanations regarding the cause of simulation results, except for comparison with similar previous study results.

**Response:** Thanks very much for this comment and suggestion. We have made further explanations of the cause of the simulation results in each section of the three Results and

Discussion. In section 3.1 Model performance, we added "Besides, the cumulative $ET_{RS}$ was taken by the 8 times of daily ET on satellite acquisition date, thus using the non-representative ETRS above the average daily value may also result in the underestimation of $ET_{IWP}$." and "In the uncultivated area (Fig.7a), simulated groundwater table level presented a slower and more flat decreasing trend than measured value. By assuming a completely non-vegetation coverage condition of uncultivated area while it is not actually the case, estimated groundwater evapotranspiration driven by capillarity will become smaller than its actual value, in which small vegetation will transpires amounts of water from soil and soil moisture is relatively low thus groundwater evapotranspiration is higher." in L471-473 and L479-484 of revised manuscript. In section 3.2 Global sensitivity analysis, we added "Due to the high sensitivity of IWP, groundwater table depth and salinity to the specific yield, it is highly recommended to use spatially variable values of specific yield rather than a constant one as a model input if it is available, which could greatly enhance the evaluation accuracy of the RIWP model. Also, it is indicated that the permeability coefficient of unconfined aquifers (K) did not significantly affect the IWP, groundwater table depth and salinity. Due to the lack of measurement data in our study, we adopted a unified K value for the whole study area, which also make the model simulations reasonable for their insensitive to this parameter." in L509-515 of the revised manuscript. In section 3.3 Regional irrigation water productivity, we added "Note that these IWP values were based on the simulated water balance and crop yields of individual HRU, which may deviate to a certain extent from the real values. It can still represent the utilization of water resources at the regional scale." and "As we can see in Fig. 9, the simulated IWP values for three crops were lower in the south, west, north and north-west of the JFID than in the other regions. The south of the JFID is the main canal for water diversion, which provide higher irrigation quota than other regions, in which results in a lower IWP. For the west of JFID, it is mainly uncultivated area, thus the IWP is lower than other regions. In the north-west of the JFID, main drainage ditch received the drainage water with high saline content from four sub-main ditches and drained all the way to the north of JFID. Ditch seepage water with high salinity resulted in the severe soil salinization in the north and north-west of JFID, which will restrict the crop growth and lower the IWP." in L521-524 and L547-551 of the revised manuscript.

**Comment 6:** L705, what are the measured values? Detail on figure title.

**Response:** Sorry about not describing the parameter value ranges in Table 3. These are the possible parameter value ranges of this study area, which referred to the local measurements, survey data and relevant research papers. We revised the Table title to "Table 3. The collected possible parameter variation ranges and calibrated values of the parameters describing soil hydraulic characteristics ($K_e$, $S_y$, $K$) and irrigation and drainage system ($\eta_{lc}$, $\eta_{fc}$, $\gamma_d$, $A$, $m$)." in L828-830 of revised manuscript. We added a note below the Table 3 to explain the source of the possible parameter value ranges in L831-835 of the revised manuscript as following:

"Note: The parameter value ranges were collected from local measurements, survey data and relevant research results. Soil texture of canal bed was silty sandy loam for 0-1 and 2-3 m depth below the ground, and sandy loam for 1-2 m. For silty sandy loam soil, the bulk density and saturated soil water conductivity are 502.3 mm d$^{-1}$ and 1.42gcm$^{-3}$, respectively. For sandy loam soil, the bulk density and saturated soil water conductivity are 1.49g cm$^{-3}$ and 592.6 mm d$^{-1}$, respectively. There were fine sand and sandy soil in the phreatic layer." And corresponding adjustment was made to the table title in L785-787 of the revised manuscript.

**Comment7:** Each section of L704 provide details on soil particle size, bulk density, saturated water conductivity in table 3.

**Response:** Sorry about the unclear expression of the soil texture and its hydraulic characteristics in Table 3. We have provided details about the soil particle size, bulk density and saturated water conductivity for canal bed and the phreatic layer in the note below Table 3 in L832-835 of the revised manuscript as "Soil texture of canal bed was silty sandy loam for 0-1 and 2-3 m depth below the ground, and sandy loam for 1-2 m. For silty sandy loam soil, the bulk density and saturated soil water conductivity are 502.3 mm d-1 and 1.42gcm$^{-3}$, respectively. For sandy loam soil, the bulk density and saturated soil water conductivity are 1.49g cm$^{-3}$ and 592.6 mm d$^{-1}$, respectively. There were mainly fine sand and sandy soil in the phreatic layer."

**Comment8:** Figure 10, there was no obvious difference in irrigation water productivity in groundwater 0-1 and 1-2 m? If not, provide the corresponding results between these groundwater levels

**Response:** Thanks very much for this comment. Yes, there was no obvious difference in irrigation water productivity between groundwater table depth in the range of 0-1 and 1-2m. When groundwater table level is shallower (0-1m), more groundwater evapotranspiration could contribute to crop water use, which will increase the irrigation water productivity. On the other hand, due to the high groundwater salinity bigger soluble salt content will go into the crop root zone, which enhance the salt stress on crop water use and thus decrease the irrigation water productivity. Similar, deeper groundwater table level will contribute less groundwater evapotranspiration but also less salt content to root zone for crop water use. In this way, the irrigation water productivity under the 0-1 m groundwater table depth was not obviously different from that under the 1-2 m groundwater table depth.

**List of all relevant changes corresponding to the comments of Editor:**

**Comment1:** L1-4 "A novel regional irrigation water productivity model coupling irrigation-drainage driven soil hydrology and salinity dynamics, and shallow groundwater movement in arid regions, China".

**Comment2:** L41-45 "The model reasonably well simulated soil moisture and salinity, as well as groundwater table depths and salinity. Overestimations of groundwater discharge were detected in calibration and validation due to the assumption of well-operated condition of drainage ditches, and regional evapotranspiration (ET) were reasonably estimated while ET in uncultivated area was slightly underestimated in RIWP model".

**Comment3: L387-396**

**"2.3.3 Model calibration and validation**

To comprehensively evaluate the accuracy and reliability of the model, the data in years 2010-2013 and in years 2006-2009 was respectively used as calibration and validation dataset. The daily measured soil moisture content of crop root zone (θ), electrical conductivity of soil water (EC), groundwater table depth ($h_g$) and groundwater salinity, were calibrated with measured data from the 22 soil water and salt observation sites and 55 groundwater observation sites (Fig. 5), which were mentioned in section 2.3.1. The RIWP simulated regional ET for each HRU was calibrated by the remote sensing based ET images obtained once per 8 days. The regional drainage processes was calibrated by the monthly groundwater drainage data from main ditches, in which the simulated drainage of each main ditch was the sum of drainage of its controlling HRUs. ”

**Comment4:** No change in context

**Comment5:** L471-473 “Besides, the cumulative $ET_{RS}$ was taken by the 8 times of daily ET on satellite acquisition date, thus using the non-representative ETRS above the average daily value may also result in the underestimation of $ET_{IWP}$.”

L479-484 “In the uncultivated area (Fig.7a), simulated groundwater table level presented a slower and more flat decreasing trend than measured value. By assuming a completely non-vegetation coverage condition of uncultivated area while it is not actually the case, estimated groundwater evapotranspiration driven by capillarity will become smaller than its actual value, in which small vegetation will transpires amounts of water from soil and soil moisture is relatively low thus groundwater evapotranspiration is higher.”

L509-515 “Due to the high sensitivity of IWP, groundwater table depth and salinity to the specific yield, it is highly recommended to use spatially variable values of specific yield rather than a constant one as a model input if it is available, which could greatly enhance the evaluation accuracy of the RIWP model. Also, it is indicated that the permeability coefficient of unconfined aquifers (K) did not significantly affect the IWP, groundwater table depth and salinity. Due to the lack of measurement data in our study, we adopted a unified K value for the whole study area, which also make the model simulations reasonable for their insensitive to this parameter.”

L521-524 “Note that these IWP values were based on the simulated water balance and crop yields of individual HRU, which may deviate to a certain extent from the real values. It can still represent the utilization of water resources at the regional scale.” L547-551 “As we can see in Fig. 9, the simulated IWP values for three crops were lower in the south, west, north and north-west of the JFID than in the other regions. The south of the JFID is the main canal for water diversion, which provide higher irrigation quota than other regions, in which results in a lower IWP. For the west of JFID, it is mainly uncultivated area, thus the IWP is lower than other regions. In the north-west of the JFID, main drainage ditch received the drainage water with high saline content from four sub-main ditches and drained all the way to the north of JFID. Ditch seepage water with high salinity resulted in the severe soil salinization in the north and north-west of JFID, which will restrict the crop growth and lower the IWP."

**Comment6:** L828-830 "Table 3. The collected possible parameter variation ranges and calibrated values of the parameters describing soil hydraulic characteristics ($K_e$, $S_y$, $K$) and irrigation and drainage system ($\eta_{lc}$, $\eta_{fc}$, $\gamma_d$, $A$, $m$)."

L831-835 "Note: The parameter value ranges were collected from local measurements, survey data and relevant research results. Soil texture of canal bed was silty sandy loam for 0-1 and 2-3 m depth below the ground, and sandy loam for 1-2 m. For silty sandy loam soil, the bulk density and saturated soil water conductivity are 502.3 mm d-1 and 1.42gcm-3, respectively. For sandy loam soil, the bulk density and saturated soil water conductivity are 1.49g $cm^{-3}$ and 592.6 mm $d^{-1}$, respectively. There were fine sand and sandy soil in the phreatic layer."

**Comment7:** L832-835 "Soil texture of canal bed was silty sandy loam for 0-1 and 2-3 m depth below the ground, and sandy loam for 1-2 m. For silty sandy loam soil, the bulk density and saturated soil water conductivity are 502.3 mm d-1 and 1.42gcm$^{-3}$, respectively. For sandy loam soil, the bulk density and saturated soil water conductivity are 1.49g $cm^{-3}$ and 592.6 mm $d^{-1}$, respectively. There were mainly fine sand and sandy soil in the phreatic layer."

**Comment8:** No change in context

## Responses to the comments of Reviewer #2:

**Recommendation:** I like this paper and believe it should be published with medium and minor edits. It is well-written and structured but will need some copy-editing as some of the English grammar and syntax can be improved. The main changes should relate to how the authors can make their model and its results more reader-friendly in that readers will want to know how this model helps users and managers better manage irrigation water. With the current version, it is not clear at the moment where these insights sit. In other words the author's own interpretation of their RIWP model needs to be more clearly written.

**Response:** We are appreciating to the reviewer for the useful comments and suggestions to the paper. We have made corresponding changes to improve the English grammar and syntax to improve the quality of this paper. In the sections of abstract and conclusion, we added the context about explaining how this model could be used by different stakeholders in irrigation water management, which makes this paper much more reader-friendly. Below are the detailed responses to all comments. We cited first the comment, which is followed by our response and often by a section how the text will be revised in the manuscript. The text in blue are changes and additions in the original text. For clarity we do not show the removed text in the blue content.

**Substantive comments:**

**Comment1:** The productivity model depends on four parameters; water supply from irrigation open canals, field crop water consumption, groundwater drainage into open ditches, and groundwater lateral flow. Can the authors explain why rainfall is not included in their model as a water supply to crop growth? How would the model work in an area with more rainfall than in their case study?

**Response:** Thanks very much for this useful comment. We are sorry for not explaining clearly in the original context. Contribution of rainfall is actually included in the field scale irrigation water productivity module, which is a developed field IWP model to simulate field water, salt, ET and crop yield under shallow groundwater condition. Rainfall is considered as an input of the vertical water balance equation contributing to crop growth. Detailed context and equation about considering rainfall in the water balance equation in field scale IWP model, referred to Xue et al., (2018), are as following:

Daily water and salt balances are required for the estimation of daily $ET_a$. Water balance in current root zone is as following:

$$WCr_i = WCr_{i-1} + R_{i-1} + I_{i-1} + RG_{i-1} + Gwr_{i-1} - ETa_{i-1} - Pwr_{i-1}$$

Thus, this model is reasonable and applicable for an area with more rainfall than in our case study.

**Comment2:** Can the authors explain why lateral movement between drainage 'bonds' the units together (line 160) but that lateral movement of irrigation water down channels does not? Surely irrigation water and drainage water are both moving laterally as well as vertically?

**Response:** Thanks very much for this useful comment. Irrigation water and drainage water are surely moving laterally and vertically. We are sorry about not explaining clearly in the original text. We are talking about the lateral exchange between adjacent groundwater units here, not the lateral water movement caused by drainage or irrigation conveyance. The study area is the arid region with shallow groundwater, which can be a very important water contribution source to crop growth. Due to the seepage loss from unsaturated soil profile to shallow groundwater and groundwater evapotranspiration going upward to unsaturated soil profile, the phreatic layer will be unstable and the groundwater table level will vary with it. Based on daily time step, we assumed that the groundwater level is unified in each HRU and the process of lateral water exchange of the phreatic layer between two adjacent HRUs were completed within one day. Additionally, it is indicated that the main irrigation canals and drainage ditches directly connect with groundwater and can be considered as the side boundaries in the model in lines 153-154 of original context.

**Comment3:** Seepage loss from channels is in the model, but I do not readily spot where seepage loss beneath the root zone from fields is accommodated?

**Response:** Thanks very much for this useful comment and suggestion. Sorry for not explaining clearly in the manuscript. Just like mentioned in comment1 that contribution of rainfall to crop growth is not readily spotted, the seepage loss beneath the root zone from fields is also included in the former developed field scale irrigation water productivity module. Seepage from crop root zone to deeper soil profile like potential root zone (Pwr), transmission zone and phreatic layer (Pwg) are considered as the components of water balance equation in the vertical soil profile. Detailed context and equation about considering field scale irrigation seepage in the water balance equation in field scale IWP model, referred to Xue et al., (2018), are as following:

Water balance in current root zone

$$WCr_i = WCr_{i-1} + R_{i-1} + I_{i-1} + RG_{i-1} + Gwr_{i-1} - ETa_{i-1} - Pwr_{i-1}$$

Water balance in potential root zone

$$WCg_i = WCg_{i-1} + Pwr_{i-1} - RG_{i-1} - Gwr_{i-1} - Pwg_{i-1} + Gwg_{i-1}$$

Groundwater balance

$$hg_i = hg_{i-1} - (1/S_y)(Pwg_{i-1} - Gwg_{i-1} - ext_{i-1})$$

**Comment4:** The authors write on page 17 a statement that the contribution of groundwater and proportion of non-beneficial soil evaporation are major influences on water productivity of their chosen crops. This seems to indicate that the productivity model is simply a biomass model related to the proportion of total water supply that ends up in transpiration? But there are other factors such as irrigation timing and scheduling that affect productivity. This makes this reviewer wonder what are the units of RIWP? And why are these units not utilised frequently throughout the paper? Thus in other words is this a production model not a productivity model?

**Response:** Thanks for this useful comments. We explained in the first paragraph of the Introduction in the original paper that IWP is defined as the crop yield per cubic meter of irrigation water supplied, and the unit of IWP is kg/m$^3$. The model is based on field ET of crop muti-growth stages and ET is computed with field daily hydrological model driven by irrigation scheduling, precipitation events, meteorology, and groundwater levels dynamics. As a result, irrigation scheduling has significant impact to field daily ET of different crop growth stages and final IWP. Furthermore, RIWP is the spatial distribution of IWP for an irrigated area, which is likely a map of IWP for different crops at the regional scale. Our RIWP model simulates yield response to water of different crops at the regional scale and is particularly suited to address conditions where water is a key limiting factor in crop production. It also provides an indicator which assesses the performance of the system, through the IWP or the yield that is produced per unit of irrigation water applied. Thus, we believe our model is more like a crop water productivity model.

**Comment5:** Also can the authors explain why, if nearly all the groundwater supplies and movements of water which are in the model come from irrigation both in the short and long-term, and not from rainfall or wider hydrogeological inflows, does the model ‘bother’ with groundwater as a factor determining IWP? Surely the main determinant of irrigation productivity in an entirely arid region is really only ‘irrigation supply’. This reviewer knows partly the answer but the authors must not assume the readers know this distinction.

**Response:** Thanks very much for this comment and suggestion. We are sorry for not considering the reader-friendly part for this paper. In arid region with shallow groundwater, irrigation caused seepage goes into groundwater and is stored in there temporarily. It looks like that the irrigation seepage is not consumed by crop and is counted in the non-beneficial irrigation water use. However, groundwater evapotranspiration will also go upward and contribute to crop water use, which makes the irrigation seepage water reusing by crop come true. This will increase the beneficial use of irrigation water and thus improve the IWP. Therefore, groundwater is also an important factor determining IWP in arid region with shallow groundwater. We have made further explanations of reason in L63-69 in the revised manuscript as following:

“Furthermore, by changing hydrological processes, irrigation and drainage affect water and salt dynamics in crop root zone, groundwater, and, eventually, crop production (Morison et al., 2008; Bouman et al., 2007). Specifically, in arid region, irrigation-caused deep seepage is the mainly recharge of groundwater. Shallow groundwater can in turn go upward and contribute to crop water use by capillary action, which means the irrigation seepage can be reused by the crop growth to improve IWP. Thus, RIWP analysis requires the quantification of the complex agro-hydrological processes, including soil water and salt dynamics, groundwater movement, crop water use and crop production.”

**Comment6:** Line 490 – can the authors explain why productivity declines when water supply from irrigation goes up? This may be consistent with other results, but it is counter to expectation? (Again the problem is that the units of IWP are not given in the main body of the paper).

**Response:** Sorry about not describing the definition and unit of IWP clearly in the main text of this paper. We make corresponding revision in L61-62 of revised manuscript as following:

“IWP is defined as the crop yield per cubic meter of irrigation water supplied, and the unit of IWP is kg/m$^3$ (Singh et al., 2004).”

Water productivity declines when water supply from irrigation goes up. This is because of the shallow groundwater condition of our case study. Irrigation water amount directly affects soil moisture of crop root zone and finally decides the crop yield. As is well-known, crop yield is directly linked to actual ET. Decreasing irrigation water depth results in a reduction of actual ET, while actual ET decreases slower than irrigation water depth does because of the contribution of groundwater evapotranspiration to crop water use (actual ET), which is directly linked to crop yield. Thus, as the ratio of crop yield and irrigation water amount, irrigation water productivity increases when irrigation water amount decrease.

**Comment7:** Can the authors be clear about what m3 of water on the denominator is about – is it total supply in cubic meters or is it total transpired cubic meters?

**Response:** Thanks for this useful comment. The $m^3$ of water on the denominator is the total supply in cubic meters. Also, as it is indicated in section 2.2 that the field irrigation water amount is the input of the field IWP module, which generates the IWP results for three crops in each HRU and map the spatial distribution of RIWP. We also revised the statement in L61-62 of revised manuscript as following:

"IWP is defined as the crop yield per cubic meter of irrigation water supplied, and the unit of IWP is $kg/m^3$ (Singh et al., 2004)."

**Comment8:** As a key comment, I think Section 3 needs to be re-written by starting or leading with key management results and insights that are readable by different stakeholders. At the moment this section is written with the model rather than the results in mind. The key management insights are buried deep within this section and are not easy to find. Here are some guide questions that show what I mean:

Which affects crop productivity more – irrigation dose/depth applied or the contribution from groundwater?

Which affects crop productivity more – lots of shallow irrigation applications or fewer deeper applications?

Which type of crop is most productive in coping with water supply coming from non-irrigation sources?

How is productivity negatively or positively affected by a combination of drainage and salts?

What explains the changing ‘red spots’ of high productivity in the maps in Figure 9 and whether and how this high level of productivity can be extended to the rest of the Jiefangzha Irrigation District so that everything becomes ‘red’.

I hope these examples show why the ‘results’ section currently does not clearly guide managers and planners.

**Response:** Thanks very much for these useful comments. As results of a new developed model, we firstly describe the performance of the model, followed by the parameters sensitivity analysis. At last, we try to get some insight of RIWP with the model. We revised the expression of model results to make them more reader-friendly to different stakeholders according to this reviewer’s suggestion. Finally, these parts are arranged in the revised manuscript with following sequence:

L442-445: Good agreements were obtained by RIWP model in simulating IWP and hydrological components during the calibration and validation periods. Table 2 tabulated the calibrated parameters describing crop growth and water usage, and Table 3 tabulated the possible variation ranges and calibrated values of the parameters describing soil hydraulic characteristics and irrigation and drainage system.

L495-501: We concluded that for shallow groundwater buried area like JFID, sometimes the effect of groundwater contribution on IWP would be greater than that of irrigation water depth applied. Applying lots of shallow irrigation to the crops may reduce the deep percolation and decrease the non-beneficial water use in evaporation. Applying fewer and deeper irrigation water applied will result in deeper percolation meanwhile greater groundwater contribution to beneficial crop water use. Thus, compared with lots of shallow irrigation applied, applying fewer deeper irrigation schedule may have greater effect on IWP in arid regions with shallow groundwater.

L524-532: We could see there are “red HRUs” in Figure 9 changing with time and space due to different irrigation water depth applied under different groundwater conditions. Even different crop species can result in big difference in IWP…. This was because that the irrigation quota was reduced over this period, and the contribution of groundwater compensated the crop yield losses. With less irrigation water applied, the number of “red HRUs” will increase along with it.

L541-557: Particularly, when the farmlands had limited supply of irrigation water, the groundwater table depth and salinity played an important role on IWP. Through the drainage ditches, groundwater could drain both water and salt out of the field, thus the groundwater table level declines and the soluble salt content going upward along with groundwater evapotranspiration to crop root zone decreases. Despite the negative effect of draining water on IWP, the positive effect of draining salt out of the field will positively affect IWP….. Thus, properly groundwater drainage management and dealing with salt accumulation at the end of main drainage ditches in an irrigated area is also a pressing and unsolved problem for increasing the “red HRUs”, which needs to be figured out by irrigation managers.

L558-561: As the major food-producing region of China, improving water productivity means producing greater amounts of food crops with less amount of water, based on local or regional potential. With declining access to water resources, farmers will need to grow different crops to maintain or increase crop production profitability in the future.

L566-568: Thus, planting sunflowers should be promoted in the JFID when available irrigation water resources is declining in the future, and this practice will definitely increase the “red HRUs”.

**Comment9:** Can the authors also introduce some ‘future or methodological critical thinking’? In other words, how does such an approach really guide current managers in improving irrigation management? What future improvements to the method and model might allow this to happen? How does the author’s model differ from other regional irrigation productivity studies, eg. conducted by the Water for Food Institute, Nebraska.

**Response:** Thanks very much for this comment. Other regional irrigation productivity models, such as Aqua crop, consider the crop yield response to water and temperature stress. It also simulates soil evaporation and crop transpiration explicitly as individual processes. Aqua crop simulates the growth, biomass production, and harvestable yield. It did not take fully consideration of groundwater on crop water use and production. Differently, our RIWP consider the regional hydrological processes including water and salt stress on crop yield and IWP, and soil evaporation and crop transpiration processes are simulated together as evapotranspiration in this model. Because that IWP is the final and most important simulation index in RIWP model, only crop yield is simulated in our model while the crop biomass part are not included. The groundwater module in RIWP model can also capture the effect of shallow buried groundwater level and salinity on crop water use, which is very common in arid region with shallow groundwater. We added some future thinking and suggestions to irrigation managers in improving irrigation management based on our developed model in results and conclusion section of revised manuscript:

L558-561: As the major food-producing region of China, improving water productivity in JFID means producing greater amounts of food crops with less amount of water, based on local or regional potential. With declining access to water resources, farmers will need to grow different crops to maintain or increase crop production profitability in the future...........Thus, planting sunflowers should be promoted in the JFID when available irrigation water resources is declining in the future.

L591-598: Thus, keeping the groundwater table depth in the optimal range and sustainable is of great importance to reach higher crop IWP at the regional scale, irrigation managers may need to reasonably determine the irrigation quota and constantly maintain the drainage system. Groundwater sustainability includes spacing withdrawals to avoid excessive depletion and taking measures to safeguard or improve groundwater quality. To achieve this, regional irrigation managers may need to take monitoring efforts to establish historic and current conditions, research to model groundwater systems, forecast future variation, and policy to manage activities influencing groundwater table and quality.

L616-627: Programmed in Matlab (Mathworks Inc., 2015), RIWP model can be run on different operating systems. Furthermore, the model includes capability for parallelization of simulations to reduce batch run times when conducting simulations over large areas, conditions, and/or time periods. In the nearly future, enabling the code to be linked quickly with other disciplinary models to support integrated water resource management could be a great improvement of RIWP model. Also, we are going to develop a website used for long-term distribution of the RIWP model and associated documentation. Finally, RIWP model could improve knowledge of best practices to enhance water productivity for key irrigation decision-makers. The simplicity of RIWP model in its required minimum input data, which are readily available or can easily be collected, makes it user-friendly. It is also a very useful model for scenario simulations and for planning purposes, which can be used by economists, water administrators and managers working in the arid irrigated area with shallow groundwater.

**Minor comments:**

**Comment1:** Be consistent "water productivity model" in title, but "water productivity estimation" in key words.

**Response:** Sorry for not being consistent through the context. We revised the "water productivity estimation" to "water productivity model" in key words of revised manuscript.

**Comment2:** Is there a substantive difference between "irrigation water productivity (IWP)" and "regional irrigation water productivity (RIWP)"

**Response:** Thanks very much for this comment. Yes, irrigation water productivity is a definition, which is the crop yield per cubic meter of irrigation water amount. Regional irrigation water productivity represents the spatial distribution of irrigation water productivity, which is much more like a map of irrigation water productivity at the regional scale.

**Comment3:** Line 36. Are uncultivated lands bare lands, or natural vegetation?

**Response:** Thanks very much for this comment. The uncultivated lands, merely bare soil, accounted for about 34% of our study area. We explained this in line 435-436 of original manuscript as: The uncultivated area, merely bare soil, accounted for about 34% of the JFID, and the $ET_{IWP}$ of uncultivated area was merely soil evaporation. To avoid misleading readers in the former context, we corrected the expression of the sentence in L35-36 of revised manuscript as following: In each HRU, we considered four land-use types: sunflower fields, wheat fields, maize fields and uncultivated lands (merely bare soil).

**Comment4:** Line 45. I would use the words ‘depth applied’ or ‘delta and deltas’ when discussing water applied via irrigation (and not ‘depth’ alone). Otherwise this use is confusing “when groundwater table depth is in the range of 2 m to 4 m, regardless of irrigation water depths”

**Response:** Thanks very much for this comment. We made corresponding revisions in the context. All the “irrigation water depth” in the manuscript were rewritten to “irrigation water depth applied”.

**Comment5:** Line 54. I would not use a single figure of 90% here “where irrigated agriculture accounts for about 90% of the total”. I would use a range e.g. 70 to 90%

**Response:** Thanks very much for this comment. We revised the number to 70 to 90% and added the reference in the L56-58 of revised manuscript as following:

Especially, in arid and semi-arid regions of the world, where irrigated agriculture accounts for about 70 to 90% of the total water use (Jiang et al., 2015; Gao et al., 2017, Dubois, 2011)…

**Comment6:** Line 69 Field experiments may be costly but they do allow for calibration and an understanding of the relevant parameters and processes “but field experiments are expensive and time consuming, making it unsuitable for regional evaluation of IWP.” So field experiments still help with a regional evaluation?

**Response:** Thanks very much for this comment. Just like the reviewer said that field experiments may be costly but then do allow for calibration and understanding of the relevant parameters and processes. We are able to adopt the field experiment to accurately evaluate the IWP at the field scale. For a larger scale such as a watershed or an irrigated area, using field experiment to evaluate the IWP of multiple spots within the area of interest may not be a good way to reproduce the spatial distribution of IWP for its time-money consuming and lack of basic regional hydrological processes. However, after we obtain the evaluation results for regional hydrological processes and IWP, field experiments can still be helpful with the calibration part.

**Comment7:** Line 84, can an example of simplified distributed models be given? “There are two types of distributed hydrologic models that are used to integrate with crop models: numerical distributed models, such as SWAT and MODFLOW, and simplified distributed models based on water balance equations."

**Response:** Thanks very much for this comment. We are sorry about not explaining it clearly. We gave two example of simplified distributed models called FARME and HEC-HMS in L87-97 of the revised context as following:

"There are two types of distributed hydrologic models that are used to monitor complex regional hydrological processes: numerical distributed models, such as SWAT and MODFLOW, and simplified distributed models, such as FARME (Kumar and Singh, 2003) and HEC-HMS (USACE, 1999) based on water balance equations. Numerical, process-based models consider the entire complexity and heterogeneity of regional hydrological systems. MODFLOW is commonly used for groundwater dynamics simulation (Kim et al., 2008). But it is limited in well-monitored large irrigation areas, due to the large number of parameters and input data required. SWAT is used to simulate land surface hydrologic and crop growth processes. It relies on the digital elevation model (DEM) to delineate surface water flow pathways. However, many irrigation areas are quite flat, and surface water flow pathways are controlled by irrigation and drainage systems, instead of terrain elevation differences. Furthermore, SWAT alone does not describe the complex interactions between groundwater and soil water, which are fundamental in arid and semi-arid areas with shallow groundwater."

**Comment8:** Line 94 – suggest small change "However, the large spatial grids can hardly reflect the regional complex cropping pattern heterogeneity, and the large temporal steps cannot capture daily soil water" to this "However, the large spatial grids poorly reflect the regional complex cropping pattern heterogeneity, and the large temporal steps cannot capture daily soil water" SWAT alone does not describe the complex interactions between groundwater and soil water, which are fundamental in arid and semi-arid areas with shallow groundwater".

**Response:** Thanks very much for this comment. We have revised the original sentence to the recommended one in L100-104 of revised manuscript as following:

"However, the large spatial grids poorly reflect the regional complex cropping pattern heterogeneity, and the large temporal steps cannot capture daily soil water and salt dynamics which is essential for crop growth simulation. SWAT alone does not describe the complex interactions between groundwater and soil water, which are fundamental in arid and semi-arid areas with shallow groundwater."

**Comment9:** Line 139 The authors could do better in explaining what an HRU is? Is it an abstract artefact, or a real command unit within an irrigated landscape? Do irrigation managers use HRUs?

**Response:** Sorry for not explaining HRU more specifically. The hydrologic response unit (HRU) is an abstract artefact created by model developer, which provides an efficient way to discretize large watersheds where simulation at the field scale may not be computationally feasible. For a regional area, the smallest spatial unit of its hydrological processes is not generally defined by physically meaningful boundaries. The HRU is like the smallest spatial unit of the model, and the standard HRU definition approach lumps all similar land uses, soils, and slopes within a sub-basin based upon user-defined thresholds. HRU is more widely used by regional hydrological model developers and users, which may include some of the irrigation managers or researchers. Following are the revised context in L151-155 of the revised paper:

"The HRU is an abstract artefact created by hydrological developer and is like the smallest spatial unit of the model, which provides an efficient way to discretize large watersheds where simulation at the field scale may not be computationally feasible. In each HRU, soil texture and groundwater conditions are assumed to be homogeneous, but different cropping patterns can exist."

**Comment10:** Line 230 can this sentence about boundaries be explained? "There are three types of groundwater boundaries: river boundaries, drainage ditch boundaries and no flux boundaries"

**Response:** Thanks very much for this comment. Sorry for not explaining the boundary types specifically in the original paper. We revised the context in L241-246 of revised manuscript as following:

"There are three types of groundwater boundary conditions: river head (when the boundary HRU including irrigation canal and the daily river flux equals to the daily canal flux), river flux (when the boundary HRU including drainage ditches and the water heads in ditches are assumed constant and equal to the river head) and constant flux (when the boundary HRU is mainly barren area and no irrigation is applied, thus in our study 0 flux is assumed)."

**Comment11:** Line 258 spelling/grammar? "Cropping patterns are complex for each HRU and sometimes HRU include uncultivated land, forest". This should be "Cropping patterns are complex for each HRU and sometimes HRUs include uncultivated land, forest"

**Response:** Thanks very much for this comment. We revised the sentence to "Cropping patterns are complex for each HRU and sometimes HRUs include uncultivated land, forest" in L274-275 of the revised manuscript.

**Comment12:** Line 293 – correct this sentence to "Considering the high spatial heterogeneity, meteorological data need to be collected from all the weather stations within or close to the study area."

**Response:** Thanks very much for this comment. We made corresponding revision in L309-310 of the revised paper as following:

"Considering the high spatial heterogeneity, meteorological data need to be collected from all the weather stations within or close to the study area."

**Comment13:** Line 427 check grammar to this "the ditches of the same order share the same the drainage coefficient, assuming well-operated conditions. However,"

**Response:** Thanks very much for this comment. We are sorry for not express it clearly and made corresponding correction in L459-460 of the revised context as following:

"In the model, for each year, we adopt same drainage coefficient for all the ditches of the different orders, assuming a well operated condition."

**Comment14:** Line 502 – difficult to follow the argument with the current English. Should this not read "indicates that when irrigation applied decreased from 300<IWD<400mm to 200<IWD<300mm it lead to decreases in IWP caused by a reduction of ET." (But this seems to contradict statements made elsewhere in the paper?

**Response:** Thanks very much for this comment. Sorry for not expressing the result clearly. We made corresponding correction in L584-586 of the revised paper as following:

"…and it indicates that when irrigation applied decreased from 300<IWD<400mm to 200<IWD<300mm it leads to decreases in IWP, which is caused by faster reduction of ET than irrigation applied."

For the potential reason of this result, we made further explanation in the following sentences in the original paper. Due to the shallow buried groundwater table condition, groundwater contribution will make up for ET reduction when we applied smaller irrigation water amount. As most of the IWP variation rules under sallow groundwater condition in this paper, when the speed of reduction of irrigation water applied is higher than the reduction of ET, IWP increases. However, when irrigation water applied decreases from 300<IWD<400mm to 200<IWD<300mm at this time, IWP decreases, which means that there exists another reason accelerate the reduction of ET. Thus, we deduced that in this situation less irrigation water will weaken the role of irrigation on salt leaching and result in more severe salinization in crop root zone. The negative effect of salt stress on crop water use is greater than the positive effect of shallow groundwater contribution on crop water use at this situation.

**Comment15:** Line 505 onwards – very difficult to understand this text! "ET, which is less irrigation water will weaken the role of irrigation on salt leaching and result in more severe salinization in crop root zone. Thus, reasonably determining the irrigation quota and constantly maintaining the drainage system to keep the groundwater table depth in the optimal range is of great importance to reach higher crop IWP at the regional scale."

**Response:** Sorry for not clearly expressing the result and reason of it. We made corresponding correction in L586-594 of revised manuscript to make it easier to read as following:

"Shallow buried groundwater contribution will make up for ET reduction when smaller irrigation water applied, thus there exists another reason accelerate the reduction of ET. We deduced that less irrigation water would weaken the role of irrigation on salt leaching and result in more severe salinization in crop root zone. The negative effect of salt stress on crop water use is greater than the positive effect of shallow groundwater contribution on crop water use at this situation. Thus, keeping the groundwater table depth in the optimal range is of great importance to reach higher crop IWP at the regional scale, irrigation managers may need to reasonably determine the irrigation quota and constantly maintain the drainage system."

**Comment16:** Line 511. Does not make sense "In view of the particularity of irrigated areas, taking fully consideration of the supply," Perhaps this? "In view of the heterogeneous conditions of irrigated areas, taking fully consideration of the supply,"

**Response:** Thanks very much for this comment. We revised the original sentence following your recommendation in L600 of revised manuscript as:

"In view of the heterogeneous conditions of irrigated areas, taking fully consideration of the supply…"

**List of all relevant changes corresponding to the comments of Editor:**

**Substantive Comment1:** No change in context

**Comment2:** No change in context

**Comment3:** No change in context

**Comment4:** L119 "irrigation water depth applied"

L213 "irrigation water depth applied"

L525 "irrigation water depth applied"

L569 "irrigation water depth applied"

**Comment5:** L63-69 "Furthermore, by changing hydrological processes, irrigation and drainage affect water and salt dynamics in crop root zone, groundwater, and, eventually, crop production (Morison et al., 2008; Bouman et al., 2007). Specifically, in arid region, irrigation-caused deep seepage is the mainly recharge of groundwater. Shallow groundwater can in turn go upward and contribute to crop water use by capillary action, which means the irrigation seepage can be reused by the crop growth to improve IWP. Thus, RIWP analysis requires the quantification of the complex agro-hydrological processes, including soil water and salt dynamics, groundwater movement, crop water use and crop production."

**Comment6:** L61-62 "IWP is defined as the crop yield per cubic meter of irrigation water supplied, and the unit of IWP is kg/m$^3$ (Singh et al., 2004)."

**Comment7:** L61-62 "IWP is defined as the crop yield per cubic meter of irrigation water supplied, and the unit of IWP is kg/m$^{3"}$ (Singh et al., 2004). "

**Comment8:** L442-445 "Good agreements were obtained by RIWP model in simulating IWP and hydrological components during the calibration and validation periods. Table 2 tabulated the calibrated parameters describing crop growth and water usage, and Table 3 tabulated the possible variation ranges and calibrated values of the parameters describing soil hydraulic characteristics and irrigation and drainage system."

L495-501 "We concluded that for shallow groundwater buried area like JFID, sometimes the effect of groundwater contribution on IWP would be greater than that of irrigation water depth applied. Applying lots of shallow irrigation to the crops may reduce the deep percolation and decrease the non-beneficial water use in evaporation. Applying fewer and deeper irrigation water applied will result in deeper percolation meanwhile greater groundwater contribution to beneficial crop water use. Thus, compared with lots of shallow irrigation applied, applying fewer deeper irrigation schedule may have greater effect on IWP in arid regions with shallow groundwater."

L524-532 "We could see there are "red HRUs" in Figure 9 changing with time and space due to different irrigation water depth applied under different groundwater conditions. Even different crop species can result in big difference in IWP…. This was because that the irrigation quota was reduced over this period, and the contribution of groundwater compensated the crop yield losses. With less irrigation water applied, the number of "red HRUs" will increase along with it."

L541-557 "Particularly, when the farmlands had limited supply of irrigation water, the groundwater table depth and salinity played an important role on IWP. Through the drainage ditches, groundwater could drain both water and salt out of the field, thus the groundwater table level declines and the soluble salt content going upward along with groundwater evapotranspiration to crop root zone decreases. Despite the negative effect of draining water on IWP, the positive effect of draining salt out of the field will positively affect IWP….. Thus, properly groundwater drainage management and dealing with salt accumulation at the end of main drainage ditches in an irrigated area is also a pressing and unsolved problem for increasing the "red HRUs", which needs to be figured out by irrigation managers."

L558-561 "As the major food-producing region of China, improving water productivity means producing greater amounts of food crops with less amount of water, based on local or regional potential. With declining access to water resources, farmers will need to grow different crops to maintain or increase crop production profitability in the future."

L566-568 "Thus, planting sunflowers should be promoted in the JFID when available irrigation water resources is declining in the future, and this practice will definitely increase the "red HRUs"."

**Comment9:** L558-561 "As the major food-producing region of China, improving water productivity in JFID means producing greater amounts of food crops with less amount of water, based on local or regional potential. With declining access to water resources, farmers will need to grow different crops to maintain or increase crop production profitability in the future...........Thus, planting sunflowers should be promoted in the JFID when available irrigation water resources is declining in the future."

L591-598 "Thus, keeping the groundwater table depth in the optimal range and sustainable is of great importance to reach higher crop IWP at the regional scale, irrigation managers may need to reasonably determine the irrigation quota and constantly maintain the drainage system. Groundwater sustainability includes spacing withdrawals to avoid excessive depletion and taking measures to safeguard or improve groundwater quality. To achieve this, regional irrigation managers may need to take monitoring efforts to establish historic and current conditions, research to model groundwater systems, forecast future variation, and policy to manage activities influencing groundwater table and quality."

L616-627 "Programmed in Matlab (Mathworks Inc., 2015), RIWP model can be run on different operating systems. Furthermore, the model includes capability for parallelization of simulations to reduce batch run times when conducting simulations over large areas, conditions, and/or time periods. In the nearly future, enabling the code to be linked quickly with other disciplinary models to support integrated water resource management could be a great improvement of RIWP model. Also, we are going to develop a website used for long-term distribution of the RIWP model and associated documentation. Finally, RIWP model could improve knowledge of best practices to enhance water productivity for key irrigation decision-makers. The simplicity of RIWP model in its required minimum input data, which are readily available or can easily be collected, makes it user-friendly. It is also a very useful model for scenario simulations and for planning purposes, which can be used by economists, water administrators and managers working in the arid irrigated area with shallow groundwater."

**Minor comments:**

**Comment1:** L52 "water productivity model"

**Comment2:** No change in context

**Comment3:** L35-36 "In each HRU, we considered four land-use types: sunflower fields, wheat fields, maize fields and uncultivated lands (merely bare soil)."

**Comment4:** No change in context

**Comment5:** L63-69 "Furthermore, by changing hydrological processes, irrigation and drainage affect water and salt dynamics in crop root zone, groundwater, and, eventually, crop production (Morison et al., 2008; Bouman et al., 2007). Specifically, in arid region, irrigation-caused deep seepage is the mainly recharge of groundwater. Shallow groundwater can in turn go upward and contribute to crop water use by capillary action, which means the irrigation seepage can be reused by the crop growth to improve IWP. Thus, RIWP analysis requires the quantification of the complex agro-hydrological processes, including soil water and salt dynamics, groundwater movement, crop water use and crop production."

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L538-554 "Particularly, when the farmlands had limited supply of irrigation water, the groundwater table depth and salinity played an important role on IWP. Through the drainage ditches, groundwater could drain both water and salt out of the field, thus the groundwater table level declines and the soluble salt content going upward along with groundwater evapotranspiration to crop root zone decreases. Despite the negative effect of draining water on IWP, the positive effect of draining salt out of the field will positively affect IWP….. Thus, properly groundwater drainage management and dealing with salt accumulation at the end of main drainage ditches in an irrigated area is also a pressing and unsolved problem for increasing the "red HRUs", which needs to be figured out by irrigation managers."

L555-558 "As the major food-producing region of China, improving water productivity means producing greater amounts of food crops with less amount of water, based on local or regional potential. With declining access to water resources, farmers will need to grow different crops to maintain or increase crop production profitability in the future.”

L563-565 “Thus, planting sunflowers should be promoted in the JFID when available irrigation water resources is declining in the future, and this practice will definitely increase the “red HRUs”.”

**Comment8:** L100-104 “However, the large spatial grids poorly reflect the regional complex cropping pattern heterogeneity, and the large temporal steps cannot capture daily soil water and salt dynamics which is essential for crop growth simulation. SWAT alone does not describe the complex interactions between groundwater and soil water, which are fundamental in arid and semi-arid areas with shallow groundwater.”

**Comment9:** L151-155 “The HRU is an abstract artefact created by hydrological developer and is like the smallest spatial unit of the model, which provides an efficient way to discretize large watersheds where simulation at the field scale may not be computationally feasible. In each HRU, soil texture and groundwater conditions are assumed to be homogeneous, but different cropping patterns can exist.”

**Comment10:** L241-246 “There are three types of groundwater boundary conditions: river head (when the boundary HRU including irrigation canal and the daily river flux equals to the daily canal flux), river flux (when the boundary HRU including drainage ditches and the water heads in ditches are assumed constant and equal to the river head) and constant flux (when the boundary HRU is mainly barren area and no irrigation is applied, thus in our study 0 flux is assumed).”

**Comment11:** L274-275 “Cropping patterns are complex for each HRU and sometimes HRUs include uncultivated land, forest”

**Comment12:** L309-310 “Considering the high spatial heterogeneity, meteorological data need to be collected from all the weather stations within or close to the study area.”

**Comment13:** L459-460 “In the model, for each year, we adopt same drainage coefficient for all the ditches of the different orders, assuming a well operated condition.”

**Comment14:** L584-586 "…and it indicates that when irrigation applied decreased from 300<IWD<400mm to 200<IWD<300mm it leads to decreases in IWP, which is caused by faster reduction of ET than irrigation applied."

**Comment15:** L586-594 "Shallow buried groundwater contribution will make up for ET reduction when smaller irrigation water applied, thus there exists another reason accelerate the reduction of ET. We deduced that less irrigation water would weaken the role of irrigation on salt leaching and result in more severe salinization in crop root zone. The negative effect of salt stress on crop water use is greater than the positive effect of shallow groundwater contribution on crop water use at this situation. Thus, keeping the groundwater table depth in the optimal range is of great importance to reach higher crop IWP at the regional scale, irrigation managers may need to reasonably determine the irrigation quota and constantly maintain the drainage system."

**Comment16:** L600 "In view of the heterogeneous conditions of irrigated areas, taking fully consideration of the supply…"

# A novel regional irrigation water productivity model coupling irrigation-drainage driven soil hydrology and salinity dynamics, and shallow groundwater movement in arid regions, China

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# Abstract:

The temporal and spatial distribution of regional irrigation water productivity (RIWP) is crucial for making agricultural related decisions, especially in arid irrigated areas with complex cropping patterns. Thus, we developed a new RIWP model for an irrigated agricultural area with complex cropping patterns. The model couples the irrigation and drainage driven soil water and salinity dynamics and shallow groundwater movement, to quantify the temporal and spatial distributions of the target hydrological and biophysical variables. We divided the study area into 1 km×1km hydrological response units (HRUs). In each HRU, we considered four land-use types: sunflower fields, wheat fields, maize fields and uncultivated lands (merely bare soil). And we coupled the regional soil hydrological processes and groundwater flow by taking a weighted average of the water exchange between unsaturated soil and groundwater under different land-use types. The RIWP model was calibrated and validated using eight years of hydrological variables obtained from regional observation sites in a typical arid irrigation area of North China, Hetao Irrigation District. The model reasonably well simulated soil moisture and salinity, as well as groundwater table depths and salinity. Overestimations of groundwater discharge were detected in calibration and validation due to the assumption of well-operated condition of drainage ditches, and regional evapotranspiration (ET) were reasonably estimated while ET in uncultivated area was slightly underestimated in RIWP model. Sensitivity analysis indicates that soil evaporation coefficient and specific yield are the key parameters for RIWP simulation. The results showed that, from 2006 to 2013, RIWP decreased from maize to sunflower to wheat. It was found that the maximum RIWP can be reached when groundwater table depth is in the range of 2 m to 4 m, regardless of irrigation water depths applied. This implies the importance of groundwater table control on RIWP. Overall, our distributed RIWP model can effectively simulate the temporal and spatial distribution of RIWP and provide critical water allocation suggestions for decision makers.

**Keywords**: Arid irrigated area, regional water productivity model, shallow groundwater, irrigation process, drainage, cropping patterns

# 1. Introduction

Under the increasing food demand of growing populations worldwide, water resources is limiting food production in many areas (Kijne et al., 2003; Fraiture and Wichelns, 2010). Especially, in arid and semi-arid regions of the world, where irrigated agriculture accounts for about 70 to 90% of the total water use (Jiang et al., 2015; Gao et al., 2017, Dubois, 2011), water deficit and related land salinity are the two major limitations to agricultural production (Williams, 1999; Xue et al., 2018). To maximize agricultural production, the improvement of irrigation water productivity (IWP) is vital (Bessembinder et al., 2005; Surendran et al., 2016). IWP is defined as the crop yield per cubic meter of irrigation water supplied, and the unit of IWP is kg/m$^3$ (Singh et al., 2004). Furthermore, by changing hydrological processes, irrigation and drainage affect water and salt dynamics in crop root zone, groundwater, and, eventually, crop production (Morison et al., 2008; Bouman, 2007). Specifically, in arid region, irrigation-caused deep seepage is the mainly recharge of groundwater. Shallow groundwater can in turn go upward and contribute to crop water use by capillary action, which means the irrigation seepage can be reused by the crop growth to improve IWP. Thus, RIWP analysis requires the quantification of the complex agro-hydrological processes, including soil water and salt dynamics, groundwater movement, crop water use and crop production. Various methods have been used to evaluate IWP, such as field measurements (Talebnejad et al., 2015; Gowing et al., 2009), remote sensing (Zwart and Bastiaanssen, 2007), and distributed hydrological models (Singh, 2005; Jiang et al., 2015; Steduto et al., 2009). Field experiments have been widely used to evaluate the effect of water management on IWP (Talebnejad et al., 2015; Gowing et al., 2009), but field experiments are expensive and time consuming, making it unsuitable for regional evaluation of IWP. Conveniently revealing temporal and spatial distributions of ET and crop yields, remote sensing is commonly used to quantify regional IWP (Thenkabail and Prasad, 2008). However, remote sensing is looking at seeing the past IWP distribution, but cannot readily predict the impacts of water management practices on IWP.

Recently, distributed integrated crop and hydrologic models have been widely used to simulate the complex agro-hydrological processes coupled with salt dynamics and crop production (Aghdam et al., 2013; Noory et al., 2011; van Dam, 2008; Vanuytrecht et al., 2007). Taking advantages of geographic information systems (GIS), distributed integrated crop and hydrologic models provide precise simulations of regional hydrological processes and crop growth, by incorporating the heterogeneity of soil moisture, salinity and texture, groundwater table depth and salinity, and cropping patterns (Amor et al., 2002; Bastiaanssen et al., 2003a; Jiang et al., 2015; Nazarifar et al., 2012; Xue et al., 2017).

There are two types of distributed hydrologic models that are used to monitor complex regional hydrological processes: numerical distributed models, such as SWAT and MODFLOW, and simplified distributed models, such as FARME (Kumar and Singh, 2003) and HEC-HMS (USACE, 1999) based on water balance equations. Numerical, process-based models consider the entire complexity and heterogeneity of regional hydrological systems. MODFLOW is commonly used for groundwater dynamics simulation (Kim et al., 2008). But it is limited in well-monitored large irrigation areas, due to the large number of parameters and input data required. SWAT is used to simulate land surface hydrologic and crop growth processes. It relies on the digital elevation model (DEM) to delineate surface water flow pathways. However, many irrigation areas are quite flat, and surface water flow pathways are controlled by irrigation and drainage systems, instead of terrain elevation differences.

Simplified distributed models often employ mass balance equations to describe the soil water and salt dynamics (Sharma, 1999; Sivapalan et al., 1996), which means less input parameters, and larger spatial grids and temporal steps. However, the large spatial grids poorly reflect the regional complex cropping pattern heterogeneity, and the large temporal steps cannot capture daily soil water and salt dynamics which is essential for crop growth simulation. SWAT alone does not describe the complex interactions between groundwater and soil water, which are fundamental in arid and semi-arid areas with shallow groundwater.

After all, there are still two big challenges for developing a distributed integrated irrigation water productivity models in irrigated areas. First, the networks of irrigation canals and drainage ditches cause spatial heterogeneity in irrigation, drainage, deep percolation, canal seepage and groundwater table depth within the irrigation area. But previous studies have overlooked the important role of the networks of irrigation canals and drainage ditches in RIWP evaluations. Second, the multi-scale matching problem comes out when coupling unsaturated and saturated zone in irrigation areas with complex cropping patterns, as the spatial heterogeneity of cropping patterns is much stronger than that of groundwater table depth. However, most of the existing distributed hydrological models simulated the hydrological processes within the same hydrological response unit (HRU) between unsaturated and saturated zones independently, but overlooked the lateral exchange of groundwater between adjacent HRUs.

Therefore, the main objectives of our study are to (1) develop a RIWP model framework coupling the irrigation and drainage processes, soil water and salt dynamics, crop water and salt response processes, and lateral movement of groundwater and salt; and (2) analyze the distributed RIWP of the study area and find the effects of crop type, irrigation water depth applied and groundwater table depth on RIWP.

# 2. Methods

We will present a four-module integrated RIWP model, the coupling between the modules and one case study evaluating the model performance.

## 2.1 Regional irrigation water productivity model

General descriptions will be given for the four modules and their integration, as well as the division and connections of HRUs, and boundary conditions of the model. Then, detailed descriptions will be given for each of the four modules: irrigation system module, drainage system module, groundwater module, and field scale IWP module.

### 2.1.1 General descriptions

A four-module integrated RIWP model was developed, to simulate the complex system including water supply from irrigation open canals, field crop water consumption, groundwater drainage into open ditches, and groundwater lateral flow.

**(1) Four modules and their integration**

The developed RIWP model couples an irrigation system module, a drainage system module, a groundwater module and a field scale IWP evaluation module (Fig. 1). The irrigation system module simulates the water flow along canals and the canal seepage to groundwater (the recharge of the groundwater module), and it provides the amount of water available for field scale irrigation. The drainage system module simulates the drainage to main drainage ditches from groundwater, and this is the discharge of the groundwater module. The groundwater module is used to simulate the groundwater lateral movement, the groundwater boundary for field scale water-salt balance processes, and the groundwater level dynamics for the drainage module. In the field scale IWP module, vertical movement of water and salt in soil profile is simulated, to obtain the soil moisture and salinity of the crop root zone, and to calculate field scale irrigation water productivity. This module provides deep percolation to the groundwater module and obtains capillary rise to soil from the groundwater module. The above mentioned four modules will be described comprehensively in 2.1.2 to 2.1.5.

**(2) Hydrological response units**

The irrigation area is spatially heterogeneous in terms of soil, land use, meteorology and groundwater. To include the spatial heterogeneities in the simulation of regional water and salt dynamics and its impact on crop growth, the irrigation district was divided into hydrological response units (HRUs) (Kalcic et al., 2015). The HRU is an abstract artefact created by hydrological developer and is like the smallest spatial unit of the model, which provides an efficient way to discretize large watersheds where simulation at the field scale may not be computationally feasible. In each HRU, soil texture and groundwater conditions are assumed to be homogeneous, but different cropping patterns can exist. For example, sunflower fields, wheat fields, maize fields and uncultivated lands. As the irrigation quota is different for different cropping patterns, the model first runs field IWP model for each cropping pattern independently in each HRU, to obtain the soil water and salt dynamics, IWP, and groundwater recharge. Then, the groundwater levels and salinity of each HRU can be updated according to the area proportions of different cropping patterns in each HRU. The groundwater flow is determined by pressure head gradient between adjacent HRUs.

**(3) Boundary conditions**

The upper boundary of the model is the atmospheric boundary layer above the plant canopy, which determines reference ET, and precipitation. The main irrigation canals and drainage ditches directly connect with groundwater and can be considered as the side boundaries in the model. With the canal conveyance water loss deducted from the gross water supplied, the amount of water diverted into the field can be calculated as the actual amount of irrigation. The local irrigation schedules of different crops and the actual time of canal water supply are both considered to determine the actual irrigation time and irrigation amounts. The lower boundary is the confining bed at the bottom of phreatic layer. The phreatic layer is vitally important due to its vertical exchange with the unsaturated soil zone in each HRU and its lateral exchange with adjacent HRUs to bond the whole region together.

### 2.1.2 Irrigation system module

When irrigation water passes through canals, no matter lined or unlined, seepage loss occurs which recharges groundwater. In a large irrigation area, there are many main, sub-main, lateral, and field canals, which are categorized as the first-, second-, third-, and fourth-order canals, respectively. During the water allocation period, canal seepage loss from different levels of canals can be divided into two parts. One part is the seepage loss from the main and sub-main canals, which are permanently filled with water and recharge directly into groundwater along the route. The other part is the seepage loss from lateral and field canals, which are intermittently filled with water and only recharge the groundwater units within their control area. Each HRU has its corresponding groundwater unit, which is used when calculating lateral exchange of groundwater between adjacent HRUs.

We calculated the decreasing water flow along canal, and water losses in main and sub-main canals as follows (Men 2000):

$$\sigma = \frac{A}{100Q^m} \tag{1}$$

$$\sigma = \frac{dQ}{Qdl} \tag{2}$$

where $\sigma$ represents the water loss coefficient per unit length per unit flow in canal ($m^{-1}$). $A$ is the soil permeability coefficient of canal bed ($m^{3m-1}day^{-m}$), m is the soil permeability exponent of canal bed (-), and their values depend on the soil type of the canal bed (please refer to Guo (1997) for the values). $Q$ represents the daily net flow in canal ($m^3day^{-1}$), and $dQ$ represents the daily flow loss of the water conveyance within $dl$ distance in canal ($m^3day^{-1}$).

Thus, Eq. (1) is equal to Eq. (2), and they can be transformed into:

$$Q^{m-1}dQ = Adl \tag{3}$$

Integrations of both sides of Eq. (3) gives:

$$\int_{Q_L}^{Q_g} Q^{m-1}\, dQ = \int_0^L A\, dl \tag{4}$$

$$Q_L = ({Q_g}^m - ALm)^{1/m} \tag{5}$$

where $Q_g$ is the daily gross flow in the head of canal (m$^3$day$^{-1}$), and $Q_L$ is the daily net flow in canal at $L$ distance away from canal head (m$^3$day$^{-1}$). Thus, flow loss in water conveyance process can be calculated as follows:

$$Q_{Ls} = \frac{A}{100}({Q_g}^m - ALm)^{(1-m)/m} \tag{6}$$

$$W_{ls} = Q_{ls}/(n_1 \times A_{su}) \tag{7}$$

where $Q_{Ls}$ is the daily groundwater recharge due to water conveyance loss in main and sub-main canals (m$^3$day$^{-1}$), $W_{ls}$ is the daily groundwater recharge per unit area due to water conveyance loss in main and sub-main canals (mday$^{-1}$). $n$ represents the total number of HRUs along selected main and sub-main canals (-), and $A_{HRU}$ is the area of each HRU (m$^2$).

Lateral and field canals are densely distributed in the irrigated area, and they are intermittently filled with low water flow. Thus, it is assumed that seepage from these canals uniformly recharges groundwater units within their control area. The canal seepage is estimated by an empirical formula:

$$W_{as} = I_n * \eta_{mc} * (1 - \eta_{sbmc}) + I_n * \eta_{mc} * \eta_{sbmc} * (1 - \eta_{lc}) + I_n * \eta_{mc} * \eta_{sbmc} * \eta_{lc} * (1 - \eta_{fc}) \tag{8}$$

where $W_{as}$ represents daily groundwater recharge per unit area due to water conveyance loss in lateral and field canals (mday$^{-1}$), and $I_n$ is daily irrigation water depth applied per unit area (mday$^{-1}$). $\eta_{\mathrm{mc}}$, $\eta_{\mathrm{sbmc}}$, $\eta_{\mathrm{lc}}$ and $\eta_{\mathrm{fc}}$ are the utilization coefficient of main, sub-main, lateral and field canals, respectively (-).

### 2.1.3 Drainage system module

In the drainage system module, only the groundwater draining into ditches is considered. Because the precipitation directly on ditches is negligible in arid and semi-arid area. The drainage processes are simulated based on the spatial distributions of main, sub-main, and lateral ditches, which are grouped into the first-, second-, and third-order ditches, respectively. Drainage is estimated by comparing local groundwater levels and ditch bottom elevation. According to Tang et al. (2007), the groundwater drainage was calculated by:

$$D_g = \begin{cases} \gamma_d \times \left(h_{db} - h_g\right) & ; \; h_{db} > h_g \\ 0 & ; \; h_{db} < h_g \end{cases} \tag{9}$$

where $D_g$ is daily groundwater drainage per unit area ($\text{mday}^{-1}$). $\gamma_d$ is drainage coefficient (-), which describes the groundwater table decline caused by the elevation difference between groundwater table and the streambed of the drainage ditch. And it depends on the underlying soil conductivity and the average distance between the drainage ditches. $h_g$ represents the daily groundwater table depth ($\text{mday}^{-1}$), and $h_{db}$ is the daily streambed depth of drainage ditch ($\text{mday}^{-1}$).

### 2.1.4 Groundwater module

For a plain irrigation area, usually groundwater levels are relatively flat on a large scale. In our model, it is assumed that groundwater lateral flow exists between one HRU and its four adjacent HRUs (Fig. 2). Using water table gradient, groundwater flow between current HRU and its adjacent HRUs can be calculated by:

$$W_{gr} = (K \times h \times B \, \frac{L_{ga} - L_g}{D}) / \mathrm{B}^2 \tag{10}$$

where $W_{gr}$ is the daily groundwater inflow of the current HRU from adjacent HRUs ($\text{mday}^{-1}$), and $K$ is the daily permeability coefficient of unconfined aquifers in the current HRU ($\text{mday}^{-1}$). $h$ represents the thickness of unconfined aquifers, which is the difference between water table and upper confined bed and varies with water table changes (m). $B$ is the length of groundwater unit (m) and here the value is 1km. $L_{ga}$ and $L_g$ represents the water table level of adjacent HRUs and the current HRU, respectively (m). $D$ is the distance between the center of the current HRU and the centers of its adjacent HRUs (m). There are three types of groundwater boundary conditions: river head (when the boundary HRU including irrigation canal and the daily river flux equals to the daily canal flux), river flux (when the boundary HRU including drainage ditches and the water heads in ditches are assumed constant and equal to the river head) and constant flux (when the boundary HRU is mainly barren area and no irrigation is applied, thus in our study 0 flux is assumed).

Based on the field scale simulation, groundwater lateral exchange, canal seepage and groundwater drainage are added in the daily water and salt balance calculations of each groundwater unit at regional scale:

$$hg_i = hg_{i-1} - (1/S_y)(Pwg_{i-1} - Gwg_{i-1} - ext_{i-1} + W_{grupi-1} + W_{grdowni-1} + W_{grlefti-1} + W_{grrighti-1} + W_{lsi-1} + W_{asi-1} - D_{gi-1}) \qquad (11)$$

$$SCa_i = Za \times Sa_{i-1} + \mathrm{W}_{grupi-1} \times Sa_{upi-1} + \mathrm{W}_{grdowni-1} \times Sa_{downi-1} + \mathrm{W}_{grlefti-1} \times Sa_{lefti-1} + \mathrm{W}_{grrighti-1} \times Sa_{righti-1} + (\mathrm{W}_{lsi-1} + \mathrm{W}_{asi-1}) \times Is_{\mathrm{i}-1} - D_{gi-1} \times Sa_{\mathrm{i}-1} + Psg_{i-1} - Gsg_{i-1} \qquad (12)$$

where $W_{grup}$, $W_{grdown}$, $W_{grleft}$ and $W_{grright}$ are the daily groundwater lateral runoff per unit area into the current groundwater unit from up and down or left and right adjacent groundwater unit, respectively (mday$^{-1}$). $SCa$ is the daily soluble salt content in the saturated zone below the transmission soil profile (mg m$^{-2}$day$^{-1}$). $Z_a$ is the thickness of the saturated zone which is the difference between the groundwater table depth and the depth that groundwater table fluctuations largely cannot reach (m). $Z_a$ only affect the soluble salt concentration in the groundwater salt balance, while it has no effect on the water balance and groundwater fluctuation simulation. $Sa$, $Sa_{up}$, $Sa_{down}$, $Sa_{left}$ and $Sa_{right}$ is the salt concentration of the current groundwater unit and its up and down or left and right adjacent groundwater units, respectively (mg m$^{-3}$). $Is$ is the salt concentration of the irrigation water (mg m$^{-3}$). $S_y$ represents the specific yield (-), which is the ratio of the volume of water that can be drained by gravity to the total volume of the saturated soil/aquifer. $ext$ is the daily groundwater extraction per unit area (mday$^{-1}$). $P_{wg}$ is the daily percolation water depth to groundwater from the potential root zone (mday$^{-1}$), and $G_{wg}$ is the daily water depth supplied to the potential root zone from shallow groundwater due to the rising capillary action (mday$^{-1}$). $P_{sg}$ and $G_{sg}$ are the quantity of soluble salt in $P_{wg}$ and $G_{wg}$, respectively (mg m$^{-2}$day$^{-1}$). The detailed calculations of the water and salt exchange components between unsaturated soil and groundwater, such as $P_{wg}$ and $G_{wg}$, were described in our previously developed water productivity model at field scale (Xue et al., 2018).

### 2.1.5 Field scale irrigation water productivity module

Cropping patterns are complex for each HRU and sometimes HRUs include uncultivated land, forest land and other non-agricultural land. In our model, with high resolution land use map, different cropping patterns can be separated to simulate soil water and salt processes, and the responses of ET and crop yields to water and salt content of root zone. Here, we employed our previously developed field IWP model to simulate field water, salt, ET and crop yield under shallow groundwater condition (Xue et al., 2018). The soil profile is vertically divided into four soil zones: the current root zone, the potential root zone, the transmission zone, and the saturated zone. In each HRU, the soil water and salt balance processes, and water productivity are independently simulated for each cropping pattern under its corresponding groundwater unit condition. For uncultivated lands, only water and salt balance are simulated, and its IWP is 0. Then, the water and salt exchange between unsaturated soil and groundwater of different cropping patterns are weighted averaged by area proportion. Finally, the weighted averages are used to update daily groundwater table and salinity (Fig. 3).

## 2.2 Modules coupling and calculating flowchart

The simulation was by daily temporal step and by HRU spatial step. The irrigation system module simulates the canal seepage to groundwater and the field irrigation water amount. And the canal seepage to groundwater is the recharge of the groundwater module, while the field irrigation water amount is the input of the field IWP module. The drainage system module simulates the groundwater drainage to drainage ditches, which is the discharge of the groundwater module. The groundwater module is used to simulate the groundwater table depth, which is the input of the field IWP module and also the input of the drainage module. In the field scale IWP module, the deep percolation to groundwater under different cropping patterns are simulated independently and their weighted average is the recharge of the groundwater module. The salt exchange is simulated together with water exchange. The groundwater module is used to simulate the groundwater lateral movement between the current HRU and its adjacent HRUs to update the groundwater level at next time step. By coupling the irrigation system module, drainage system module and groundwater module with the field IWP model, this RIWP model simulates the temporal and spatial distribution of IWP in the whole irrigation area from the beginning to the end of the growing season.

The model was implemented in a combination of ArcGIS, MATLAB, and Microsoft Excel (Fig. 4).

The HRUs was created in ArcGIS as fishnet, with each grid numbered. In MATLAB, the HRUs were represented by a matrix and the daily time step was represented by a vector. At each time step, all the HRUs were traversed by a nested loop. Then the updated information for the current time step was used to calculate the next time step. Microsoft Excel stored ArcGIS vector layer and its attribute data for MATLAB modeling, and also stored MATLAB output results for ArcGIS analysis and visualization.

Considering the high spatial heterogeneity, meteorological data need to be collected from all the weather stations within or close to the study area. Distribution of soil physical properties, moisture and salinity in unsaturated soil, groundwater table depth and salinity, need to be collected from many observation sites, which are uniformly or randomly spread over the study area. Then, each data set can be interpolated in ArcGIS by inverse distance weight to obtain a spatial distribution vector layer. For each layer, the average value in each HRU are calculated by ArcGIS using geometric division statistics. The vector layer of irrigation control zones and the vector layer of drainage control zones is respectively overlaid with the HRU division layer in ArcGIS, to obtain the HRU numbers controlled by each irrigation control zone and each drainage control zone. The HRU numbers controlled by the same zone are stored in the same matrix for batch simulation in MATLAB. In MATLAB, soil water and salt balances and field scale IWP for main crops are simulated simultaneously for each HRU; whereas, groundwater lateral exchange are simulated between adjacent HRUs. At the end of the model simulation, soil moisture and salinity, groundwater table depth and salinity, ET, crop yield and IWP for different land use types in each HRU can be obtained. Then, the area proportion weighted average in each HRU can be imported into ArcGIS to visualize the spatial distribution.

## 2.3 Model evaluation

We will provide a case study using the above developed new RIWP model, to test its applicability, and to provide sensitivity analysis of the parameters.

### 2.3.1 Description of study area and data

As a typical sub-district of the Hetao Irrigation District, the Jiefangzha Irrigation District (JFID) is a typical arid irrigated area with shallow groundwater, resulted from its arid-continental climate, over years of flood irrigation, and poor drainage systems (Fig. 5). Located in the Hetao Plain, the JFID is very flat with an average slope of 0.02% from southeast to northwest (Xu et al., 2011). The mean annual precipitation is only 155 mm, of which 70% occurs between July to September; while the mean annual potential evaporation is 1938 mm. The mean annual temperature is 7℃, with the lowest and highest monthly average being −10.1℃ and 23.8℃ in January and July, respectively. The JFID covers an area of 0.22 Mha, of which 66% is irrigated farmland area. Wheat, maize and sunflower as the main crops in this region, taking up more than 90% of the irrigated farmland area. The $12\times10^8$ $m^3$ annual irrigation water is diverted from the Yellow River. Due to the poor maintenance of drainage ditches, it is quite common in this area to have poor drainage situations. Therefore, the annual average groundwater table depth ranges from 1.5 to 3.0 m during the crop growing season. Soils in the JFID are spatially heterogeneous and primarily composed of silt loam in the northern region and sandy loam in the southern region. Shallow groundwater table and strong evaporation makes soil salinization a very serious problem in this area, which is becoming the main constraint of crop production.

An irrigation and drainage network include four main irrigation canals, sixteen sub-main irrigation canals, five main drainage ditches, and twelve sub-main drainage ditches are controlling the water movement in the JFID (Fig. 5). The streambed depths of the regional main, sub-main and lateral ditches were collected by a regional survey in 2016. Daily water flow data in the main and sub-main irrigation canals and monthly data of the five main drainage ditches were obtained from the local Irrigation Administration Bureau. A total of 55 groundwater observation wells are installed in the JFID (Fig. 5). Groundwater level was measured on the 1st, 6th, 11th, 16th, 21th and 26th of each month, and groundwater salinity was measured 3 times each month. Near the groundwater observation wells, soil moisture was measured four times, and soil electrical conductivity was measured once before wheat sowing and once before autumn irrigation. Due to the spatially homogeneous climate in JFID, daily meteorological data (air temperature, humidity, wind speed and precipitation) was obtained from Hangjinghouqi weather station for the calculation of regional reference ET.

HJ-1A, HJ-1B and Landsat NDVI images with 30 m resolution during the period of 2006-2013 were downloaded from the official website of China Centre for Resources Satellite Data and Application

(2013) and USGS (2013), to determine the annual cropping pattern distributions. Due to the lack of measured ET, the ET estimated by SEBAL model using MODIS images from NASA (2013) was used as a reference to compare with simulated ET values (Bastiaanssen et al., 2003b).

### 2.3.2 Parameterization of distributed RIWP model

The JFID was divided into 2485 1km×1km HRUs (Fig. S1a in the supplementary material). In terms of boundary conditions, the upper Quaternary 4 aquifer layer was regarded as the phreatic layer in the model. It was modeled as an aquitard with loamy soil. From north to south, the thickness of aquifer in JFID varies from 2 to 20m with an average of 7.4m (Bai et al., 2008). Thus, the initial value of the average thickness of unconfined aquifer is set as 7.4m. The water level contour maps of JFID during 1997-2002 by Bai (200) were used to determine the direction of water flow near the groundwater boundary. Based on the topography conditions, land-use types, locations of main canals and ditches, and directions of water flow, the regional phreatic layer was divided into 5 zones with river, drainage and impervious boundary conditions (Fig. S1b).

The JFID was divided into four irrigation control sections and five drainage control sections, each section was controlled by one main irrigation canal or one main drainage ditch. These sections were further divided into 48 irrigation control sub-areas and 17 drainage control sub-areas, each sub-area was controlled by one sub-main irrigation canal or one sub-main drainage ditch (Fig. S2). The sunflower fields, wheat fields, maize fields and uncultivated lands are the four cropping patterns, i.e., land-use types, in the RIWP model. In many other researches about distributed hydrological models, when considering the applied irrigation schedule the sowing and irrigations of a particular crop were just set as on the same day over the whole study area, which may be a simplification of actual conditions (Singh, 2005). In our study, the irrigation time and irrigation water amount of each HRU were co-determined by both the local irrigation schedule of the three main crops, and the actual water amount flowing into the fields.

The simulation period was from April 1st to September 20th, which covers the growing seasons of all the three main crops. The initial crop parameters were set as the default values suggested for sunflower, wheat, and maize by Allen et al. (1998). The empirical values of regional canal utilization and ditch drainage coefficient were obtained from Jiefangzha administration.

### 2.3.3 Model calibration and validation

To comprehensively evaluate the accuracy and reliability of the model, the data in years 2010-2013 and in years 2006-2009 was respectively used as calibration and validation dataset. The daily measured soil moisture content of crop root zone (θ), electrical conductivity of soil water (EC), groundwater table depth ($h_g$) and groundwater salinity, were calibrated with measured data from the 22 soil water and salt observation sites and 55 groundwater observation sites (Fig. 5), which were mentioned in section 2.3.1. The RIWP simulated regional ET for each HRU was calibrated by the remote sensing based ET images obtained once per 8 days. The regional drainage processes was calibrated by the monthly groundwater drainage data from main ditches, in which the simulated drainage of each main ditch was the sum of drainage of its controlling HRUs. Overall, the soil hydraulic parameters, the crop water productivity related coefficient, and the canal conveyance and ditch drainage parameters were all calibrated with observed data in years 2010-2013, and then validated with observed data in years 2006-2009.

To quantify the model performance, the root mean square error (RMSE), the Nash and Sutcliffe model efficiency (NSE) and the coefficient of determination ($R^2$) were used as the indicators. RMSE was used to measure the deviation of simulated values from the measured ones, NSE was commonly used to verify the credibility of the hydrological model, and $R^2$ represented the degree of linear correlation. The indicators were calculated as follows:

$$RMSE = \left[\frac{\sum_{i=1}^{n}(Output_s - Output_o)^2}{n}\right]^{0.5} \tag{13}$$

$$NSE = 1 - \frac{\sum_{i=1}^{n}(Output_s - Output_o)^2}{\sum_{i=1}^{n}(Output_o - Output_m)^2} \tag{14}$$

$$R^2 = 1 - \frac{\sum_{i=1}^{n}(Output_o - \overline{Output_o})(Output_s - \overline{Output_s})}{\sqrt{\sum_{i=1}^{n}(Output_o - \overline{Output_o})^2}\sqrt{\sum_{i=1}^{n}(Output_s - \overline{Output_s})^2}} \tag{15}$$

where *n* is the number of simulations; $Output_s$ and $Output_o$ are simulated and observed values of model outputs, respectively; $\overline{Output_s}$ and $\overline{Output_o}$ are the average values of simulated and observed model outputs, respectively. The *RMSE* indicates a perfect match between observation and simulation when it equals 0, and increasing *RMSE* values indicate an increasingly poor match. Singh et al. (2005) stated that *RMSE* values less than 50% of the standard deviation of the observed data could be considered low enough as an indicator of a good model prediction. Ranging between $-\infty$ and 1, the NSE indicates a perfect match between observed and predicted values when it equals to 1. Values between 0 and 1 are generally considered as acceptable levels of performance, whereas values less than 0.0 indicate that the simulation is worse than taking an average of observation, which indicates unacceptable performance. The $R^2$ ranging between 0 and 1 describes the proportion of the variance in the observed data, in which higher values indicating less error variance. Typically, $R^2 > 0.5$ is considered acceptable (Santhi et al., 2001).

### 2.3.4 Global sensitivity analysis

To find the key parameters significantly impacting the model output, a global sensitivity analysis was conducted. The analysis related the changes in three output variables—RIWP, groundwater table depth and groundwater salinity—to eight parameters in the RIWP model. The Latin Hypercube Sampling (LHS) (please see Mckay, 1979; Muleta et al., 2005; Wang et al., 2008 for detailed descriptions of the sampling method), a typical sampling method for sensitivity and uncertainty analysis, was used to sample the parameter space. According to Dai (2011), to ensure that the test points were evenly distributed in space and to guarantee the accuracy of the test, the test number was set as 20, more than double of the parameter number which was 8. For uniform distributions, the parameter range was subdivided into 20 equal intervals. Each interval was sampled only once to generate random values of the possible parameter sets. The possible parameter value ranges referred to the local measurements, survey data and relevant research papers. Additionally, considering the spatial heterogeneity of the three output variables, 22 evenly distributed groundwater observation sites in JFID were selected for the global sensitivity analysis. Based on the LHS method, 20 groups of parameter combinations were obtained and the simulation was run for 20 times. Finally, the sensitivity of the three output variables to the eight parameters were determined in SPSS Statistics. The absolute values of the obtained Standardized Regression Coefficients (SRCs) quantified the significance of each parameter to each output variable (Table 1) (Cheng et al., 2018; Cannavó, 2012). And the plus or minus sign of the SRCs indicated the positive or negative correlations between the corresponding parameter and output variable pairs.

# 3. Results and Discussion

## 3.1 Model performance

Good agreements were obtained by RIWP model in simulating IWP and hydrological components during the calibration and validation periods. Table 2 tabulated the calibrated parameters describing crop growth and water usage, and Table 3 tabulated the possible variation ranges and calibrated values of the parameters describing soil hydraulic characteristics and irrigation and drainage system. The agreement between the observed and simulated soil moisture content in crop root zone both in calibration (Fig. 6a, $RMSE$=2.867 cm$^3$ cm$^{-3}$, $NSE$=0.330, $R^2$=0.502) and validation (Fig. 6b, $RMSE$=2.989 cm$^3$ cm$^{-3}$, $NSE$=0.232, $R^2$=0.548) indicates the reasonable performance of the RIWP model. The good performance of the RIWP model was also indicated by the simulation of the soil salt content both in calibration (Fig. 6c, $RMSE$=1.108 dS m$^{-1}$, $NSE$=0.612, $R^2$=0.657) and validation (Fig. 6d, $RMSE$=1.205 dS m$^{-1}$, $NSE$=0.525, $R^2$=0.590). The simulated and observed groundwater table depth (Fig. 6e, $RMSE$=0.786m, $NSE$=0.424 and $R^2$=0.509 in calibration; Fig. 6f, $RMSE$=0.667m, $NSE$=0.637 and $R^2$=0.504 in validation) and groundwater salinity (Fig. 6g, $RMSE$<10%, $NSE$=0.813 and $R^2$=0.815 in calibration; Fig. 6h, $RMSE$<10%, $NSE$=0.604 and $R^2$=0.730 in validation) at 55 observation sites are in good agreement as well.

The model did not perform very well on simulating groundwater drainage. The overestimated drainage (Fig. 6i-j) was due to the different operating conditions of the drainage ditches of the different order. Remember that we classified the main, sub-main and lateral drainage ditches into the first-, second- and third-order ditches, respectively. In the model, for each year, we adopt same drainage coefficient for all the ditches of the different orders, assuming a well operated condition. However, the actual operating conditions of the ditches of the different orders cannot be the same, resulting in the simulation discrepancy.

The ET simulated by the RIWP model ($ET_{IWP}$) and the ET estimated by the SEBAL model using MODIS images ($ET_{RS}$) agrees well both in calibration (RMSE=1.918mm, $NSE$=0.274 and $R^2$ = 0.561) and in validation (RMSE=2.132mm, $NSE$ =0.189 and $R^2$ =0.498) (Fig. 6l). Furthermore, the comparison of the spatial distribution of cumulative $ET_{IWP}$ and $ET_{RS}$ during crop growth season showed that $ET_{IWP}$ was lower than $ET_{RS}$ in uncultivated area, while they agreed well in farmland (Fig. S3). The uncultivated area, merely bare soil, accounted for about 34% of the JFID, and the

$ET_{IWP}$ of uncultivated area was merely soil evaporation. This, resulted in the underestimation of actual ET in uncultivated area compared to the ET acquired by remote sensing images, which was consistent with previous studies (Singh, 2005; Tian et al., 2015). Besides, the cumulative $ET_{RS}$ was taken by the 8 times of daily ET on satellite acquisition date, thus using the non-representative $ET_{RS}$ above the average daily value may also result in the underestimation of $ET_{IWP}$.

To test the model performances under different cropping patterns, one representative site was selected for each cropping pattern to compare the observed and simulated time series of groundwater table depth (Fig.7). Results indicated that the model can adequately capture the groundwater dynamics at the four representative sites. Occasionally, the simulated groundwater table depth declines fast, while the observed value rises. This is most likely due to the fact that we ignored the time lag between groundwater recharge from soil and deep percolation. In the uncultivated area (Fig.7a), simulated groundwater table level presented a slower and more flat decreasing trend than measured value. By assuming a completely non-vegetation coverage condition of uncultivated area while it is not actually the case, estimated groundwater evapotranspiration driven by capillarity will become smaller than its actual value, in which small vegetation will transpires amounts of water from soil and soil moisture is relatively low thus groundwater evapotranspiration is higher.

### 3.2 Global sensitivity analysis

Recall that the global sensitivity analysis was to determine the sensitivity of the three output variables to eight parameters. The three output variables were RIWP, groundwater table depth, and groundwater salinity; while, the eight parameters were those parameters describing soil hydraulic characteristics and irrigation and drainage system, tabulated in Table 3. Specific yield ($S_y$), followed by soil evaporation coefficient ($K_e$), are the two key parameters influencing the RIWP (Fig. 8a). The specific yield indicated the readily available soil moisture released to crop root zone from shallow aquifer under capillary action for crop consumption. Thus, its significant positive influence on RIWP was explained. The soil evaporation coefficient indicated the proportion of water that transferred into the atmosphere but was not used by crops. Therefore, its significant negative impact on RIWP was expected. We concluded that for shallow groundwater buried area like JFID, sometimes the effect of groundwater contribution on IWP would be greater than that of irrigation water depth applied. Applying lots of shallow irrigation to the crops may reduce the deep percolation and decrease the non-beneficial water use in evaporation. Applying fewer and deeper irrigation water applied will result in deeper percolation meanwhile greater groundwater contribution to beneficial crop water use. Thus, compared with lots of shallow irrigation applied, applying fewer deeper irrigation schedule may have greater affect on IWP in arid regions with shallow groundwater. And for both groundwater table depth (Fig. 8b) and groundwater salinity (Fig. 8c), specific yield was the only key parameter. Canal seepage was expected to cause the variation of groundwater table depth around the canal at the local scale. However, the results indicated that the variation of groundwater table depth would be more susceptible to the local groundwater properties, i.e., specific yield, than to canal seepage at the regional scale. We speculate that the lateral groundwater movement might compensate the variation of groundwater table depth caused by the canal seepage. Salt moves with water. Thus, the variation of groundwater salinity was also dominated by the specific yield. Due to the high sensitivity of IWP, groundwater table depth and salinity to the specific yield, it is highly recommended to use spatially variable values of specific yield rather than a constant one as a model input if it is available, which could greatly enhance the evaluation accuracy of the RIWP model. Also, it is indicated that the permeability coefficient of unconfined aquifers ($K$) did not significantly affect the IWP, groundwater table depth and salinity. Due to the lack of measurement data in our study, we adopted a unified $K$ value for the whole study area, which also make the model simulations reasonable for their insensitive to this parameter.

## 3.3 Regional irrigation water productivity

### 3.3.1 Spatial distribution of irrigation water productivity

Validated by the measured soil moisture and salinity, groundwater table depth and salinity, drainage water depth and ET, especially, the year 2006-2013 time series of groundwater table depth under the four cropping patterns, the developed RIWP model can be used to estimate the spatial distribution of IWP for the three main crops over the period of 2006-2013 (Fig. 9). Note that these IWP values were based on the simulated water balance and crop yields of individual HRU, which may deviate to a certain extent from the real values. It can still represent the utilization of water resources at the regional scale. We could see there are “red HRUs” in Figure 9 changing with time and space due to different irrigation water depth applied under different groundwater conditions. Even different crop species can result in big difference in IWP. As we mentioned before, the spatial distribution of these three crops is very complex in JFID and field plot is small, thus we use remote sensing data to obtain cropping pattern map with resolution of 30m*30m. Every HRU has these three crops, thus we can simulate IWP for each main crop in every HRU. The RIWP of the three main crops showed a trend of decline during the period of 2006-2010 (Fig. 9a-e).This was mainly attributed to the increasing irrigation quota, as the excess water lowered the IWP. Whereas, during the period of 2011-2013 (Fig. 9f-h), the RIWP of the three main crops showed an increasing trend. This was because that the irrigation quota was reduced over this period, and the contribution of groundwater compensated the crop yield losses. With less irrigation water applied, the number of “red HRUs” will increase along with it.

Under a given irrigation water distribution, the spatial distribution of ET was the key factor controlling the RIWP distribution. And the spatial distribution of ET was fundamentally determined by the solar energy, and the water and salt dynamics of soil. Recall that the climate and, therefore, the solar energy, was homogeneous in JFID. Then, the spatial heterogeneity of RIWP must be attributed to the water and salt heterogeneity caused by the spatial heterogeneity of the cropping pattern, groundwater table depth, and irrigation and drainage networks. Particularly, when the farmlands had limited supply of irrigation water, the groundwater table depth and salinity played an important role on IWP. Through the drainage ditches, groundwater could drain both water and salt out of the field, thus the groundwater table level declines and the soluble salt content going upward along with groundwater evapotranspiration to crop root zone decreases. Despite the negative effect of draining water on IWP, the positive effect of draining salt out of the field will positively affect IWP. As we can see in Fig. 9, the simulated IWP values for three crops were lower in the south, west, north and north-west of the JFID than in the other regions. The south of the JFID is the main canal for water diversion, which provide higher irrigation quota than other regions, in which results in a lower IWP. For the west of JFID, it is mainly uncultivated area, thus the IWP is lower than other regions. In the north-west of the JFID, main drainage ditch received the drainage water with high saline content from four sub-main ditches and drained all the way to the north of JFID. Ditch seepage water with high salinity resulted in the severe soil salinization in the north and north-west of JFID, which will restrict the crop growth and lower the IWP. Thus, properly groundwater drainage management and dealing with salt accumulation at the end of main drainage ditches in an irrigated area is also a pressing and unsolved problem for increasing the "red HRUs", which needs to be figured out by irrigation managers.

As the major food-producing region of China, improving water productivity means producing greater amounts of food crops with less amount of water, based on local or regional potential. With declining access to water resources, farmers will need to grow different crops to maintain or increase crop production profitability in the future. The comparison between the RIWP of different crops (comparing the three columns in Fig. 9) showed that maize had the highest IWP, wheat had the lowest IWP, and the IWP of sunflower was in the middle. Therefore, modestly increasing the planting area of maize will improve the crop production per unit irrigation water amount. In addition, the RIWP of sunflower is a little higher than that of wheat, and the benefit and the salt tolerance of sunflower are both much higher than those of wheat. Thus, planting sunflowers should be promoted in the JFID when available irrigation water resources is declining in the future, and this practice will definitely increase the "red HRUs".

### 3.2.2 The impact of irrigation water depth applied and groundwater table depth on irrigation water productivity

In arid shallow groundwater area, irrigation water productivity (IWP) is affected by irrigation water depth (IWD) applied and groundwater table depth ($h_g$). In all the four simulated $h_g$ ranges, IWP decreased when IWD increased (Fig. 10a), which was consistent with Huang et al. (2005). Moreover, the magnitude of IWP decrease per unit increase of IWD was different under different $h_g$ ranges. The magnitude of IWP decrease under shallower $h_g$ was smaller than that under deeper $h_g$. This effect of increasing $h_g$ on the relationship between IWP and IWD was consistent with Gao et al. (2017). The above results indicate that when irrigation water is insufficient, groundwater can compensate the crop water demand. However, when irrigation water is excessive, a large proportion will eventually drain through the drainage ditches, and the IWP drops. Additionally, among the four $h_g$ ranges, the highest IWP was obtained in the range of 2-3m (Fig. 10b), which was consistent with Xue et al. (2018). This indicates that a $h_g$ deeper than that provides insufficient water for crop growth; whereas, a $h_g$ shallower than that will increase root zone soil salinity and salt stress of crops. The negative effect of shallow groundwater salinity can also be found in Fig. 10a when $h_g$ is less than 2m, and it indicates that when irrigation applied decreased from 300<IWD<400mm to 200<IWD<300mm it leads to decreases in IWP, which is caused by faster reduction of ET than irrigation applied. Shallow buried groundwater contribution will make up for ET reduction when smaller irrigation water applied, thus there exists another reason accelerate the reduction of ET. We deduced that less irrigation water will weaken the role of irrigation on salt leaching and result in more severe salinization in crop root zone. The negative effect of salt stress on crop water use is greater than the positive effect of shallow groundwater contribution on crop water use at this situation. Thus, keeping the groundwater table depth in the optimal range and sustainable is of great importance to reach higher crop IWP at the regional scale, irrigation managers may need to reasonably determine the irrigation quota and constantly maintain the drainage system. Groundwater sustainability includes spacing withdrawals to avoid excessive depletion and taking measures to safeguard or improve groundwater quality. To achieve this, regional irrigation managers may need to take monitoring efforts to establish historic and current conditions, research to model groundwater systems, forecast future variation, and policy to manage activities influencing groundwater table and quality.

# 4. Conclusions

In view of the heterogeneous conditions of irrigated areas, taking fully consideration of the supply, consumption and drainage processes of irrigation water and groundwater, a distributed RIWP model was developed to couple the irrigation water flow processes along main canals and drainage processes, water and salt transport processes in soil profile, groundwater water and salt lateral transport, and agricultural water productivity module. Especially, a new method was designed and incorporated to couple regional soil hydrology process and groundwater flow, with the spatial difference of cropping pattern. Taking advantages of remote sensing and GIS tools, the quantitative distributed RIWP model needs fewer soil and groundwater hydraulic parameters and crop growing parameters and only readily available data of several observation sites at the regional scale, and regional water and salt process can be simulated on a daily time step. Despite the simplifications involved, the proposed methods of irrigation canal and drainage ditches digitization and groundwater-runoff lateral exchange simulation between grids make the spatial IWP simulation in a real distributed way, instead of using a field scale model applied in a distributed mode to simulate all simulation units independently. The calibration and validation results indicates a good performance of RIWP model applied in this typic study area, and spatial distribution of IWP for different crops can be produced.

Programmed in Matlab (Mathworks Inc., 2015), RIWP model can be run on different operating systems. Furthermore, the model includes capability for parallelization of simulations to reduce batch run times when conducting simulations over large areas, conditions, and/or time periods. In the nearly future, enabling the code to be linked quickly with other disciplinary models to support integrated water resource management could be a great improvement of RIWP model. Also, we are going to develop a website used for long-term distribution of the RIWP model and associated documentation. Finally, RIWP model could improve knowledge of best practices to enhance water productivity for key irrigation decision-makers. The simplicity of RIWP model in its required minimum input data, which are readily available or can easily be collected, makes it user-friendly. It is also a very useful model for scenario simulations and for planning purposes, which can be used by economists, water administrators and managers working in the arid irrigated area with shallow groundwater.

## Data availability

The simulation results of the water budget during the simulation period of the JFID in this study are available from the authors upon request (jiyxue@ucdavis.edu).

## Author contributions

JYX and ZLH developed the idea to develop the conceptual RIWP model for irrigated area in arid region with shallow groundwater and complex cropping patterns. JYX wrote the programming code of the RIWP model in Matlab. JYX collected and processed the multiple datasets with the help of SW, GHH and XX and prepared the paper. The results were extensively commented on and discussed by ZLH, IW, IK, ZPS, and CZW.

# Competing interests

The authors declare that they have no conflict of interest.

# Acknowledgements

This study was supported by the National Key Research and Development Program of China (2017YFC0403301), the National Natural Science Foundation of China (51679236, 51639009) and the International Postdoctoral Exchange Fellowship Program from the Office of China Postdoctoral Council (20180044). Special thanks also go to the adminstration of Hetao Irrigation District and Shahaoqu experimental station for providing information and data.

# Reference

Aghdam, E. N., Babazadeh, H., Vazifedoust, M., Kaveh, F., 2013. Regional modeling of wheat yield production using the distributed agro-hydrological swap. Advances in Environmental Biology, 7(7).

Amor, V.M., Ashim, D.G., Rainer, L., 2002. Application of GIS and crop growth models in estimating water productivity. Agricultural Water Management, 54, 205–225.

Bai, Z. 2008. Numerical simulation and analysis of the groundwater and salt dynamics in Jiefangzha irrigation scheme of Hetao irrigation district. (Master Dissertation). China Agricultural University. (In Chinese)

Bai, Z., Xu, X., 2008. Numerical simulation of the groundwater and salt dynamics in Jiefangzha irrigation scheme of Hetao irrigation district. Water Saving Irrigation (2), 29-31. (In Chinese)

Bastiaanssen, W., Ahmad, M. D., Tahir, Z., Kijne, J. W., Barker, R., Molden, D., 2003a. Upscaling water productivity in irrigated agriculture using remote-sensing and gis technologies. Iwmi Books Reports, 289-300.

Bastiaanssen, W. G. M., Zwart, S. J., Pelgrum, H., Dam, J. C. V., 2003b. Remote sensing analysis.

In Dam, J.C. van, R.S. Malik (Eds.), 2003. Water productivity of irrigated crops in Sirsa district, India. Integration of remote sensing, crop and soil models and geographical information systems. WATPRO final report, including CD-ROM. ISBN 90-6464-864-6: 85-100.

Bessembinder, J. J. E., Leffelaar, P. A., Dhindwal, A. S., Ponsioen, T. C., 2005. Which crop and which drop, and the scope for improvement of water productivity. Agricultural Water Management, 73(2), 113-130.

Bouman, B. A. M., 2007. Water management in irrigated rice: coping with water scarcity. Int. Rice Res. Inst..

Cannavó, F., 2012. Sensitivity analysis for volcanic source modeling quality assessment and model selection. Computers and Geosciences, 44(13), 52-59.

CERSDA, 2013. http://www.cresda.com/EN/, last access: 15 November 2017.

Dai, Y. B., 2011. Uncertainty analysis of vehicle accident reconstruction results based on Latin Hypercube Sampling. (Doctoral dissertation), Changsha University of Science and Technology. (In Chinese)

Dubois, O., 2011. The state of the world's land and water resources for food and agriculture: managing systems at risk. Earthscan.

Fraiture, C. D., Wichelns, D., 2010. Satisfying future water demands for agriculture. Agricultural Water Management, 97(4), 0-511.

Gao, X., Huo, Z., Qu, Z., Xu, X., Huang, G., Steenhuis, T. S., 2017. Modeling contribution of shallow groundwater to evapotranspiration and yield of maize in an arid area. Scientific Reports, 7, 43122.

Gowing, J. W., Rose, D. A., Ghamarnia, H., 2009. The effect of salinity on water productivity of wheat under deficit irrigation above shallow groundwater. Agricultural Water Management, 96(3), 517-524.

Guo, Y., 1997. Irrigation and Drainage Engineering. China Water Power Press.

Huang, Y., Chen, L., Fu, B., Huang, Z., Gong, J., 2005. The wheat yields and water-use efficiency in the loess plateau: straw mulch and irrigation effects. Agricultural Water Management, 72(3), 209-222.

Jiang, Y., Xu, X., Huang, Q., Huo, Z., Huang, G., 2015. Assessment of irrigation performance and water productivity in irrigated areas of the middle Heihe River basin using a distributed agro-hydrological model. Agricultural water management, 147, pp.67-81.

Kalcic, M. M., Chaubey, I., Frankenberger, J., 2015. Defining soil and water assessment tool (SWAT) hydrologic response units (HRUs) by field boundaries. International Journal of Agricultural & Biological Engineering, 8(3), 69-80.

Kijne, J. W., Barker, R., Molden, D. J., 2003. Water productivity in agriculture: limits and opportunities for improvement. Wallingford, UK: CABI, IWMI.

Kim, N. W., Chung, I. M., Won, Y. S., Arnold and Jeffrey, G., 2008. Development and application of the integrated SWAT-MODFLOW model. Journal of Hydrology, 356(1-2), 1-16.

Kumar, R., Singh, J., 2003. Regional water management modeling for decision support in irrigated agriculture. Journal of irrigation and drainage engineering, 129(6), 432-439.

Mckay, M. D., Beckman, R. J., Conover, W. J., 1979. A comparison of three methods for selecting values of input variables in the analysis of output from a computer code in wsc '05: proceedings of the 37th conference on winter simulation. Technometrics, 21(2), 239-245.

Men, B. H., 2000. Discussion on formula of channel flow loss and water utilization coefficient. China Rural Water and Hydropower, 2, 33-34.

Morison, J.I.L., Baker, N.R., Mullineaux, P.M., Davies, W.J., 2008. Improving water use in crop production. Philosophical Transactions of the Royal Society B: Biological Sciences, 363(1491), pp.639-658.

Muleta, M. K., Nicklow, J. W., 2005. Sensitivity and uncertainty analysis coupled with automatic calibration for a distributed watershed model. Journal of Hydrology, 306(1), 127-145.

NASA, 2013. https://modis.gsfc.nasa.gov/, last access: 18 November 2017.

Nazarifar, M., Kanani, M., Momeni, R., 2012. Analysis of spatial and temporal variations in crop water productivity of the rainfed wheat for a regional scale analysis. Agriculture, 58(2), 65-73.

Noory, H., S.E.A.T.M. van der Zee, Liaghat, A. M., Parsinejad, M., Dam, J. C. V., 2011. Distributed agro-hydrological modeling with swap to improve water and salt management of the voshmgir irrigation and drainage network in northern iran. Agricultural Water Management, 98(6), 1062-1070.

Santhi, C., Arnold, J.G., Williams, J.R., Dugas, W.A., Srinivasan, R., Hauck, L.M., 2001. Validation of the swat model on a large rwer basin with point and nonpoint sources 1. JAWRA Journal of the American Water Resources Association, 37(5), pp.1169-1188.

Sharma, B. R., 1999. Regional salt- and water-balance modelling for sustainable irrigated agriculture. Agricultural Water Management, 40(1), 0-134.

Singh, O. P., Sharma, A., Singh, R., Shah, T., 2004. Virtual water trade in dairy economy irrigation water productivity in Gujarat. Economic and political weekly, 39(31), 3492-3497.

Singh, R., 2005. Water productivity analysis from field to regional scale. (Doctoral Dissertation). Wageningen University.

Singh, J., Knapp, H.V., Arnold, J.G., Demissie, M., 2005. Hydrological modeling of the Iroquois river watershed using HSPF and SWAT 1. JAWRA Journal of the American Water Resources Association, 41(2), pp.343-360.

Sivapalan, M., Viney, N. R., Jeevaraj, C. G., 1996. Water and salt balance modelling to predict the effects of land - use changes in forested catchments. 3. The large catchment model. Hydrological Processes, 10(3), 429-446.

Steduto, P., Hsiao, T. C., Raes, D., Fereres, E., 2009. Aquacrop--the FAO crop model to simulate yield response to water: i. concepts and underlying principles. Agronomy Journal, 101(3), 448-459.

Surendran, U., Jayakumar, M., Marimuthu, S., 2016. Low cost drip irrigation: Impact on sugarcane yield, water and energy saving in semiarid tropical agro ecosystem in India. Science of the Total Environment, 573, pp.1430-1440.

Talebnejad, R., Sepaskhah, A. R., 2015. Effect of deficit irrigation and different saline groundwater depths on yield and water productivity of quinoa. Agricultural Water Management, 159, 225-238.

Tang, Q., Hu, H., Oki, T., Tian, F., 2007. Water balance within intensively cultivated alluvial plain in an arid environment. Water Resources Management, 21(10), 1703-1715.

Thenkabail and Prasad, S., 2008. Water productivity mapping methods using remote sensing. Journal of Applied Remote Sensing, 2(1), 023544.

Tian, Y., Zheng, Y., Zheng, C., Xiao, H., Fan, W., Zou, S., et al., 2015. Exploring scale-dependent ecohydrological responses in a large endorheic river basin through integrated surface water-groundwater modeling. Water Resources Research, 51(6), 4065-4085.

USGS, 2013. *https://earthexplorer.usgs.gov/*, last access: 18 March 2018.

USACE. HEC-HMS Hydrologic Modeling System User's Manual, Version 2.0 - Draft. U.S. Army Corps of Engineers, Hydrologic Engineering Center, Davis, CA, 1999.

Vanuytrecht, E., Raes, D., Steduto, P., Hsiao, T. C., Fereres, E., Heng, L. K., 2014. Aquacrop: fao's crop water productivity and yield response model. Environmental Modelling & Software, 62, 351-360.

Van Dam, J. C., Groenendijk, P., Hendriks, R. F. A., Kroes, J. G., 2008. Advances of modeling water flow in variably saturated soils with SWAP. Vadose Zone J,7(2), 640-653.

Wang, H. C., Du, P. F., Zhao, D. Q., Wang, H. Z., Li, Z. Y., 2008. Global sensitivity analysis for urban rainfall-runoff model. China Environmental Science, 28(8), 725-729.

Williams, W.D., 1999. Salinisation: A major threat to water resources in the arid and semi-arid regions of the world. Lakes & Reservoirs: Research & Management, 4(3-4), pp.85-91.

Xu, X. 2011. Simulation of hydrological process and its responses to agricultural water-saving practices in Hetao irrigation districts (Doctoral Dissertation). China Agricultural University. (In Chinese)

Xue, J., Guan, H., Huo, Z., Wang, F., Huang, G., Boll, J., 2017. Water saving practices enhance regional efficiency of water consumption and water productivity in an arid agricultural area with shallow groundwater. Agricultural Water Management, 194, 78-89.

Xue, J., Huo, Z., Wang, F., Kang, S., Huang, G., 2018. Untangling the effects of shallow groundwater and deficit irrigation on irrigation water productivity in arid region: new conceptual model. Science of the Total Environment, 619-620, 1170-1182.

Zhao, C., Shen, B., Huang, L., Lei, Z., Hu, H.,Yang, S., 2009. A dissipative hydrological model for the hotan oasis (DHMHO). Water Resources Management, 23(6), 1183.

Zwart, S. J., Bastiaanssen, W. G. M., 2007. Sebal for detecting spatial variation of water productivity and scope for improvement in eight irrigated wheat systems. Agricultural Water Management, 89(3), 287-296.

## Table Captions

Table 1. The significance level of the input parameter to the model output variables

Table 2. Calibrated crop parameters of wheat, sunflower and maize for regional irrigation water productivity model

Table 3. The collected possible parameter variation ranges and calibrated values of the parameters describing soil hydraulic characteristics ($K_e$, $S_y$, $K$) and irrigation and drainage system ($\eta_{lc}$, $\eta_{fc}$, $\gamma_d$, $A$, $m$).

Table 1. The significance level of the input parameter to the model output variables

| *SRC* value | Significance level |
|---|---|
| $0.8\leq\lvert SRC\rvert\leq 1$ | Very important |
| $0.5\leqslant\lvert SRC\rvert\leqslant 0.8$ | Important |
| $0.3\leqslant\lvert SRC\rvert\leqslant 0.5$ | Unimportant |
| $0\leqslant\lvert SRC\rvert\leqslant 0.3$ | Irrelevant |

Table 2. Calibrated crop parameters of wheat, sunflower and maize for regional irrigation water productivity model

| Parameters | Calibrated value | | |
|---|---|---|---|
| | Wheat | Sunflower | Maize |
| Rate of yield decrease per unit of excess salts, *b* (%/(ds/m)) | 7.1 | 12 | 12 |
| Average fraction of TAW that can be depleted from the root zone before moisture stress, *p* (-) | 0.55 | 0.45 | 0.55 |
| Crop coefficient at crop initial stage, $k_{c1}$ (-) | 0.3 | 0.3 | 0.3 |
| Crop coefficient at crop development stage, $k_{c2}$ (-) | 0.73 | 0.8 | 0.75 |
| Crop coefficient at mid-season stage, $k_{c3}$ (-) | 1.15 | 1 | 1.2 |
| Crop coefficient at last season stage, $k_{c4}$ (-) | 0.4 | 0.7 | 0.6 |
| Yield response factor, $K_y$ (-) | 1.15 | 0.95 | 1.25 |
| Electrical conductivity of the saturation extract at the threshold of $EC_e$ when crop yield firstly reduces below $Y_m$ at last season stage, $EC_{et}$ (dS/m) | 5 | 1.7 | 2 |

Table 3. The collected possible parameter variation ranges and calibrated values of the parameters describing soil hydraulic characteristics ($K_e$, $S_y$, $K$) and irrigation and drainage system ($\eta_{lc}$, $\eta_{fc}$, $\gamma_d$, $A$, $m$).

| Parameters | Description | Value range | | Calibrated value |
|---|---|---|---|---|
| | | Min | Max | |
| $K_e$ | Soil evaporation coefficient, (-) | 0.1 | 0.35 | 0.25 |
| $\eta_{lc}$ | Water utilization coefficient of lateral canal, (-) | 0.81 | 0.91 | 0.88 |
| $\eta_{fc}$ | Water utilization coefficient of field canal, (-) | 0.81 | 0.86 | 0.89 |
| $S_y$ | Specific yield, (-) | 0.02 | 0.15 | 0.15 |
| $\gamma_d$ | Drainage coefficient, (-) | 0.02 | 0.06 | 0.03 |
| $K$ | Permeability coefficient of unconfined aquifers, (mm/day) | 731 | 12701 | 1150 |
| $A$ | Soil water permeability coefficient, (-) | 0.7 | 3.4 | 3.4 |
| $m$ | Soil water permeability exponent, (-) | 0.3 | 0.5 | 0.5 |

Note: The parameter value ranges were collected from local measurements, survey data and relevant research results. Soil texture of canal bed was silty sandy loam for 0-1 and 2-3 m depth below the ground, and sandy loam for 1-2 m. For silty sandy loam soil, the bulk density and saturated soil water conductivity are 502.3 mm d$^{-1}$ and 1.42gcm$^{-3}$, respectively. For sandy loam soil, the bulk density and saturated soil water conductivity are 1.49g cm$^{-3}$ and 592.6 mm d$^{-1}$, respectively. There were fine sand and sandy soil in the phreatic layer.

## Figure Captions

**Fig.1.** Schematic diagram of the conceptual RIWP model and the coupling between its sub-modules.

**Fig.2.** Schematic diagram of groundwater lateral runoff exchange between HRUs.

**Fig.3.** Schematic diagram of coupling soil water and salt dynamics, and groundwater level and salinity. And the IWP evaluation in each HRU.

**Fig.4.** Procedure chart of regional irrigation water productivity simulation.

**Fig.5.** Location of the Jiefangzha Irrigation District.

**Fig.6.** Relationship between the simulated and measured values during the crop growing season in calibration and validation period.

**Fig.7.** The comparison of the simulated and measured groundwater table depth for 4 typical sites during the crop growing season in the years of 2006-2013. (Note: a- uncultivated area during the years of 2006-2013; b- uncultivated area from 2006-2008, and sunflower field and maize field from 2009-2013; c, d- sunflower, wheat and maize field in the years of 2006-2013)

**Fig.8.** Parameter sensitivity analysis results of model for the three output variables: (a) irrigation water productivity, (b) groundwater table depth and (c) groundwater salinity.

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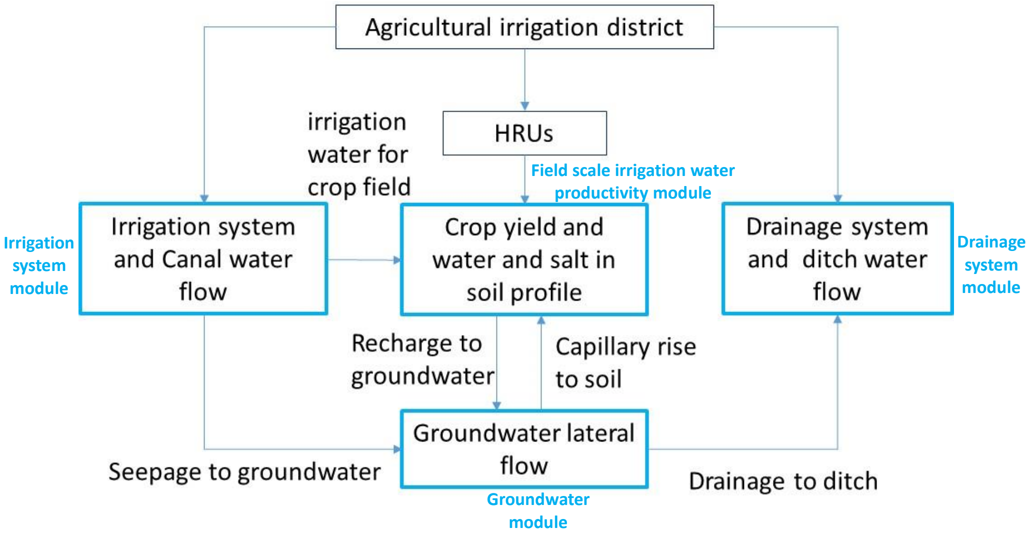
**Fig.10.** (a) Simulated regional irrigation water productivity under various groundwater table depth ($h_g$) conditions with different irrigation water amount ($I_n$) applied, and (b) its statistical analysis results. In Fig.10a, W, S and M represents wheat, sunflower and maize, respectively



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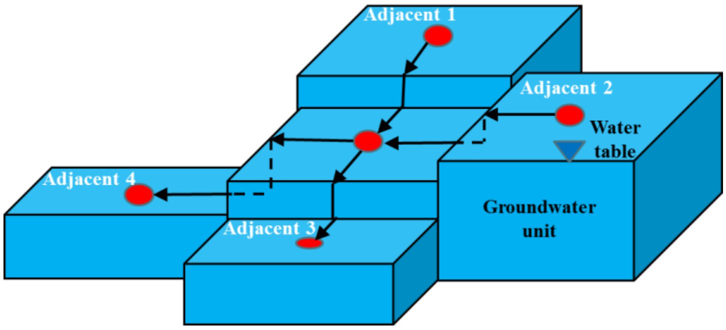
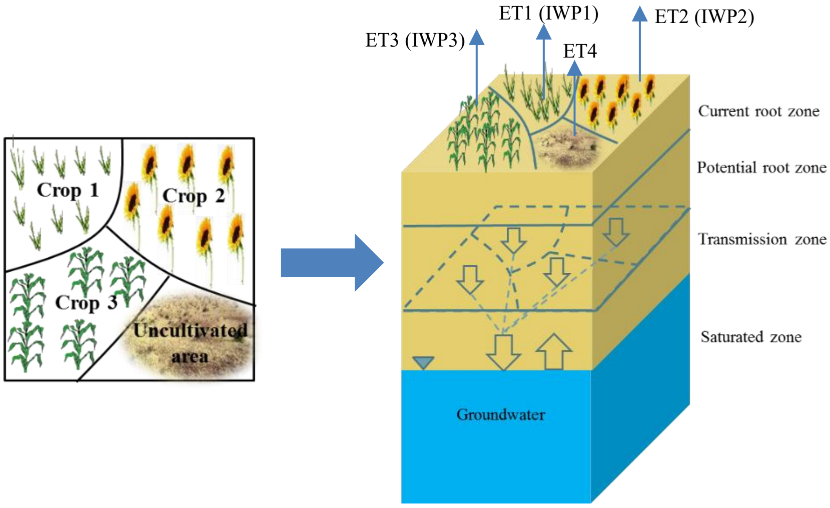


**Fig.2.** Schematic diagram of groundwater lateral exchange between adjacent HRUs.



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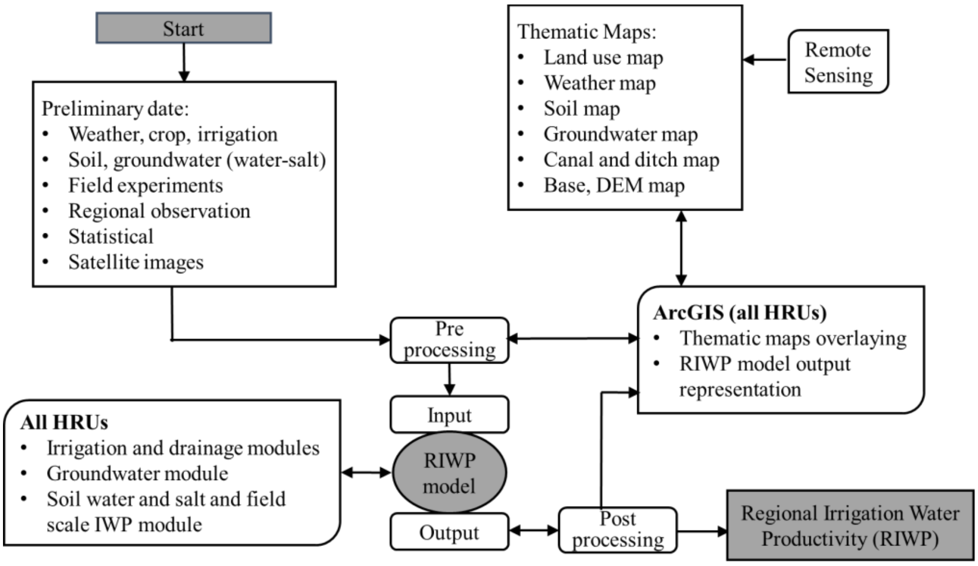


**Fig.4.** Procedure chart of regional irrigation water productivity simulation.

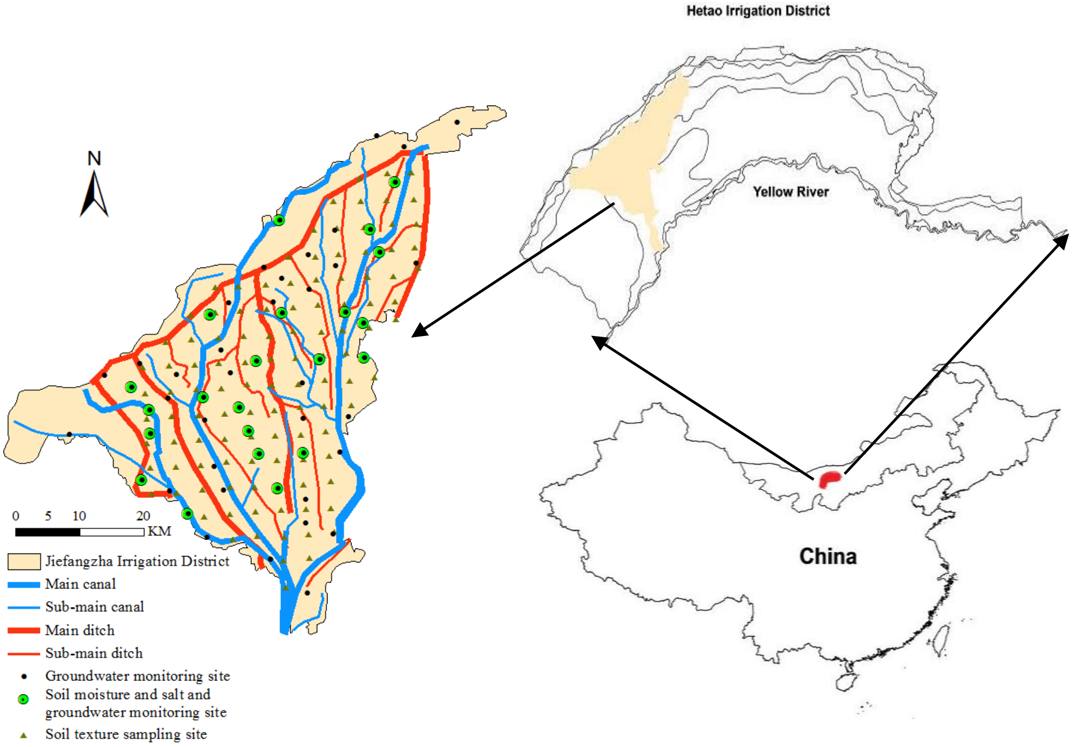
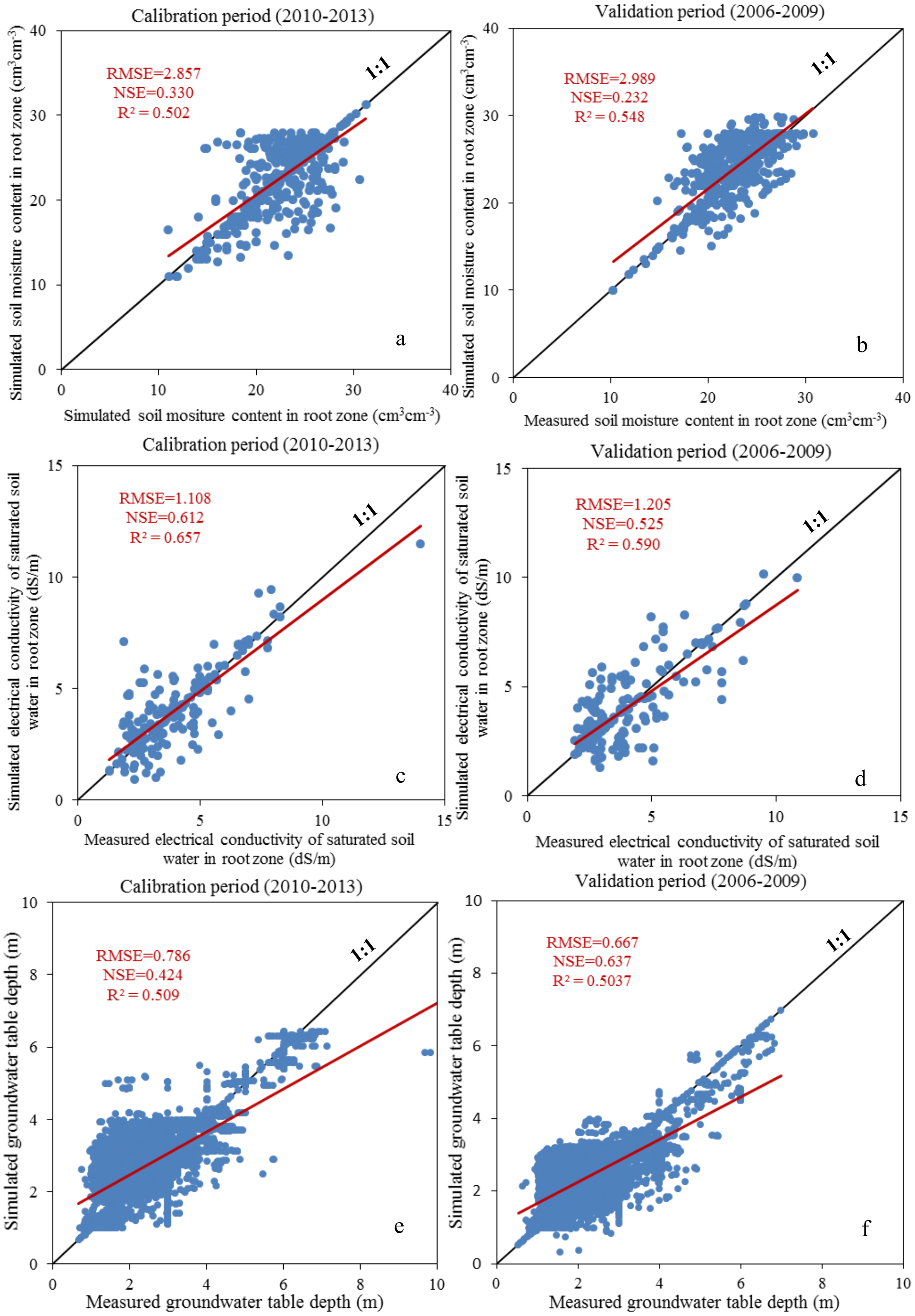


**Fig.5.** Location of the Jiefangzha Irrigation District.


Calibration period (2010-2013)
RMSE=2.857
NSE=0.330
R² = 0.502
1:1
a
Simulated soil moisture content in root zone (cm³cm⁻³)
Simulated soil mositure content in root zone (cm³cm⁻³)
0
10
20
30
40
Validation period (2006-2009)
RMSE=2.989
NSE=0.232
R² = 0.548
1:1
b
Simulated soil moisture content in root zone (cm³cm⁻³)
Measured soil moisture content in root zone (cm³cm⁻³)
Calibration period (2010-2013)
RMSE=1.108
NSE=0.612
R² = 0.657
1:1
c
Simulated electrical conductivity of saturated soil water in root zone (dS/m)
Measured electrical conductivity of saturated soil water in root zone (dS/m)
0
5
10
15
Validation period (2006-2009)
RMSE=1.205
NSE=0.525
R² = 0.590
1:1
d
Simulated electrical conductivity of saturated soil water in root zone (dS/m)
Measured electrical conductivity of saturated soil water in root zone (dS/m)
Calibration period (2010-2013)
RMSE=0.786
NSE=0.424
R² = 0.509
1:1
e
Simulated groundwater table depth (m)
Measured groundwater table depth (m)
0
2
4
6
8
10
Validation period (2006-2009)
RMSE=0.667
NSE=0.637
R² = 0.5037
1:1
f
Simulated groundwater table depth (m)
Measured groundwater table depth (m)

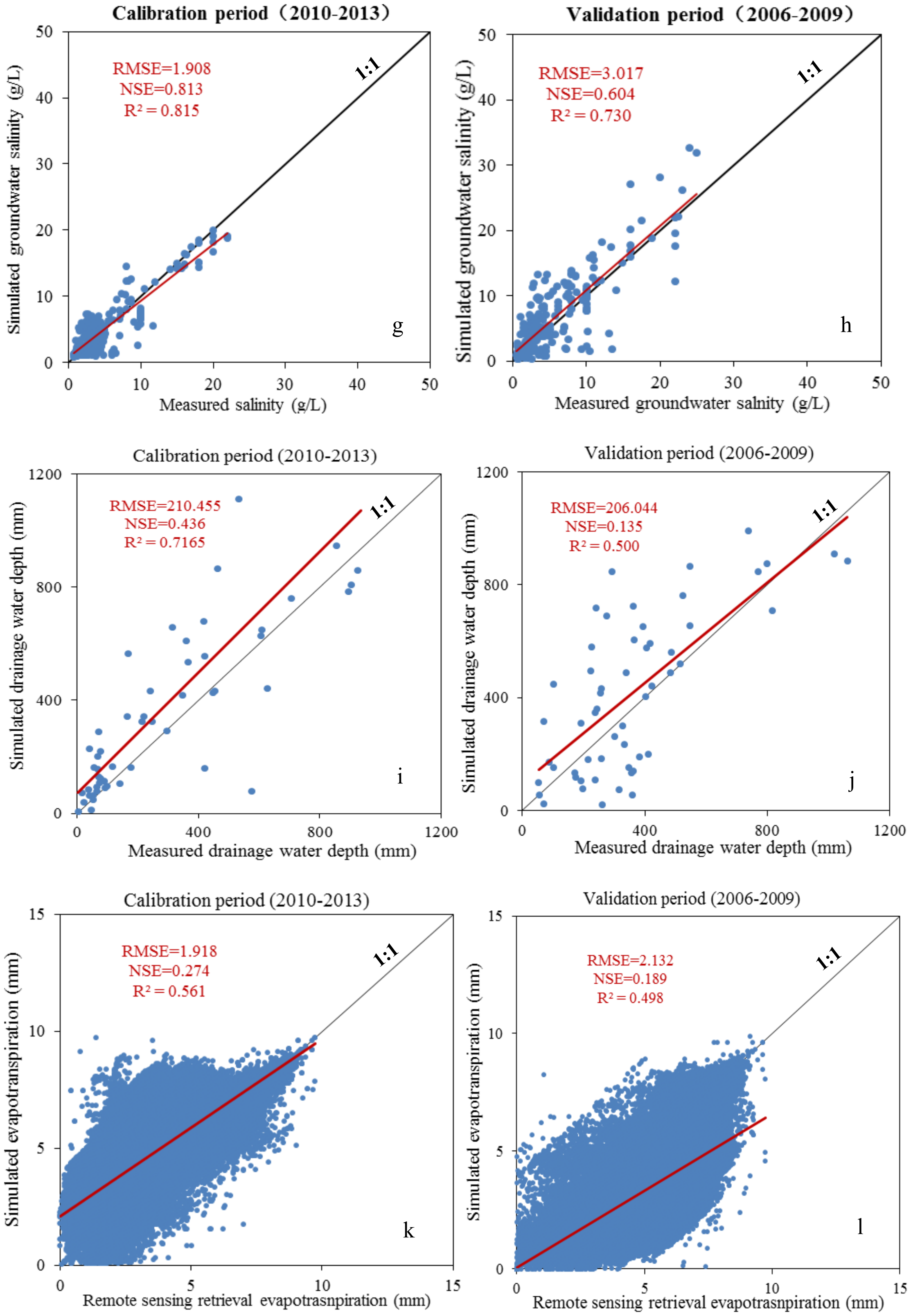
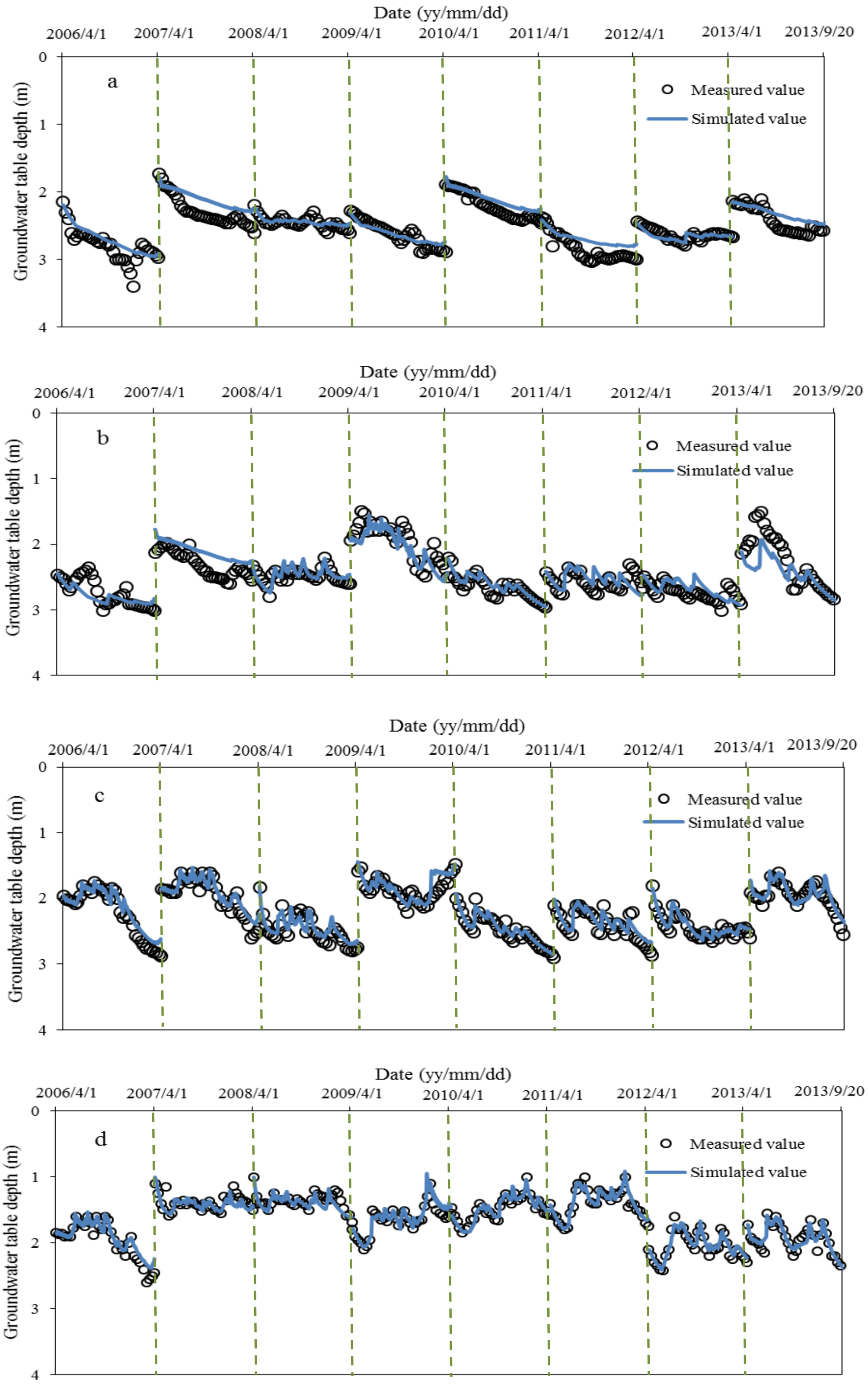


**Fig.6.** Relationship between the simulated and measured values during the crop growing season in calibration and validation period.



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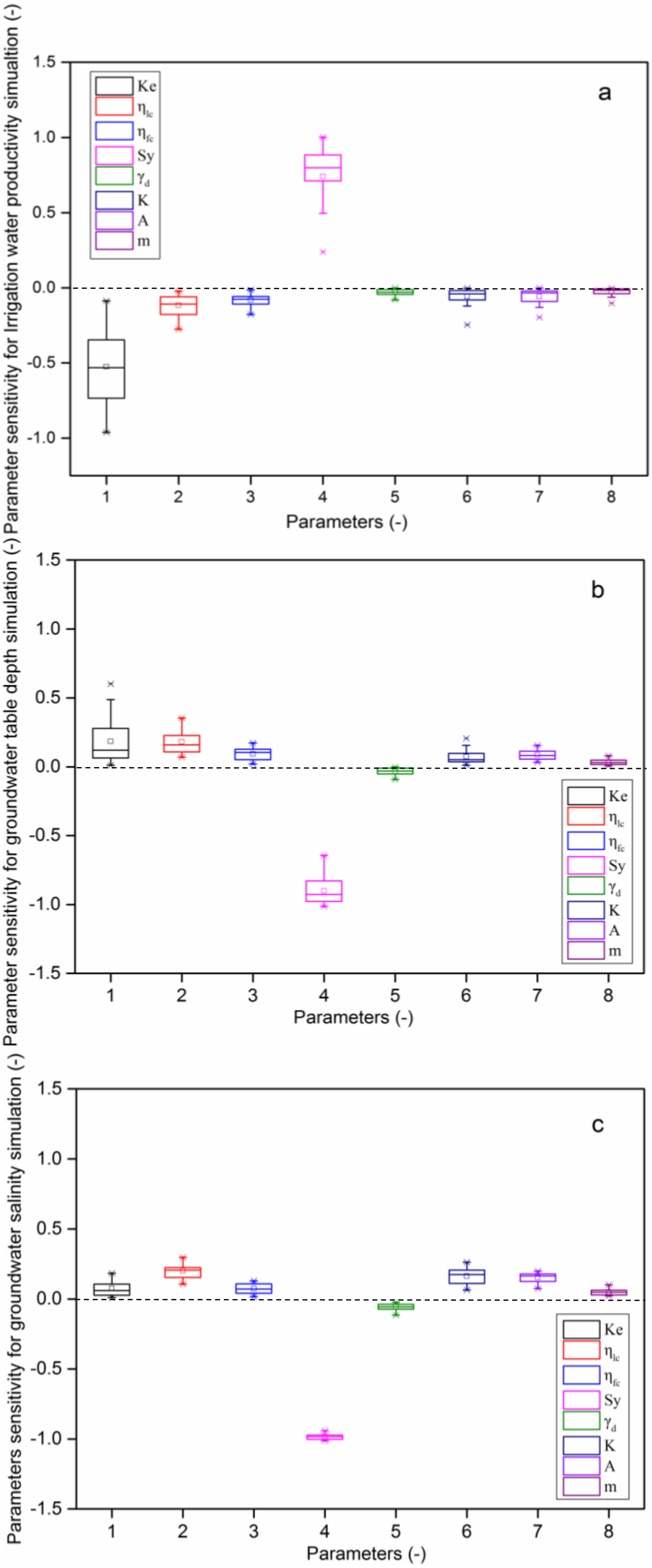

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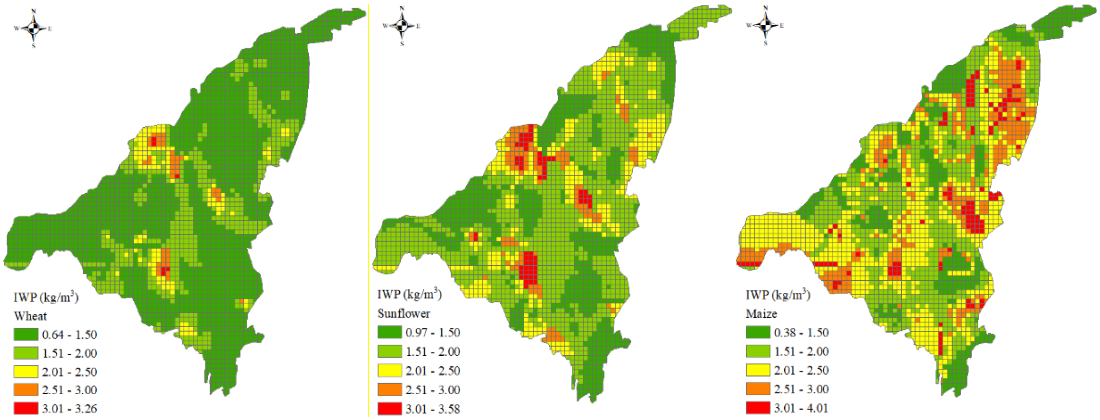
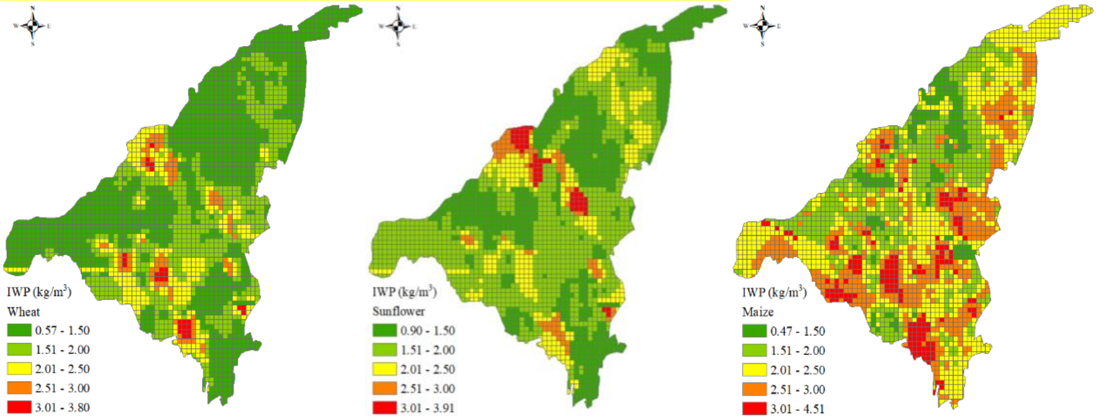
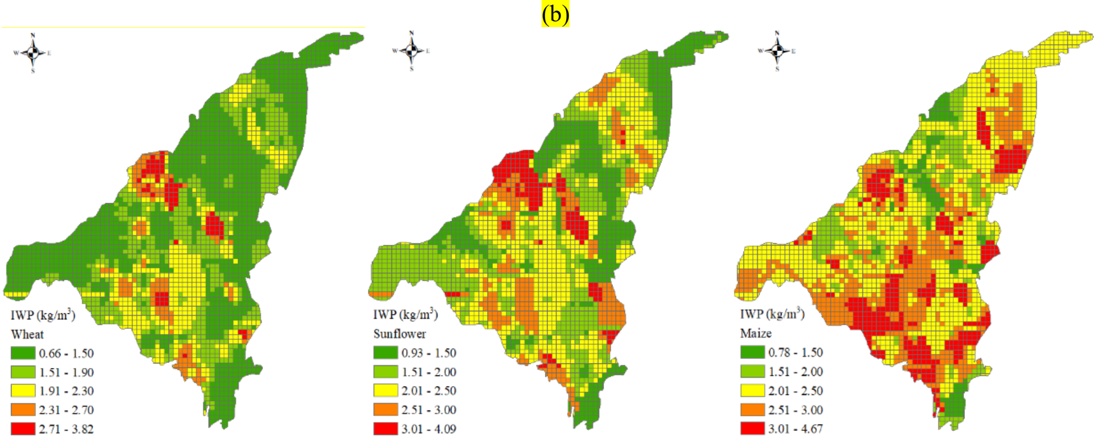

IWP (kg/m³)
Wheat
🟩 0.64 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.26
IWP (kg/m³)
Sunflower
🟩 0.97 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.58
IWP (kg/m³)
Maize
🟩 0.38 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.01

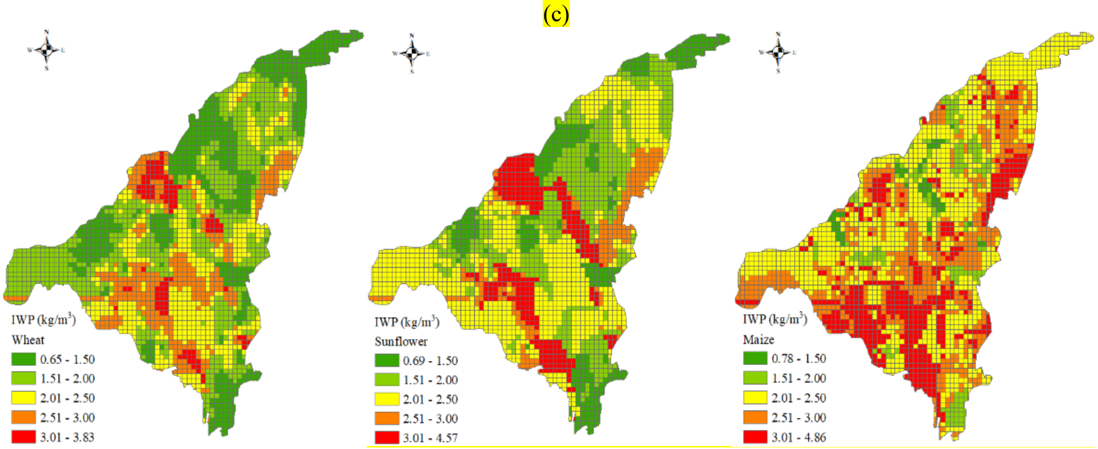
(a)


IWP (kg/m³)
Wheat
🟩 0.57 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.80
IWP (kg/m³)
Sunflower
🟩 0.90 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.91
IWP (kg/m³)
Maize
🟩 0.47 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.51

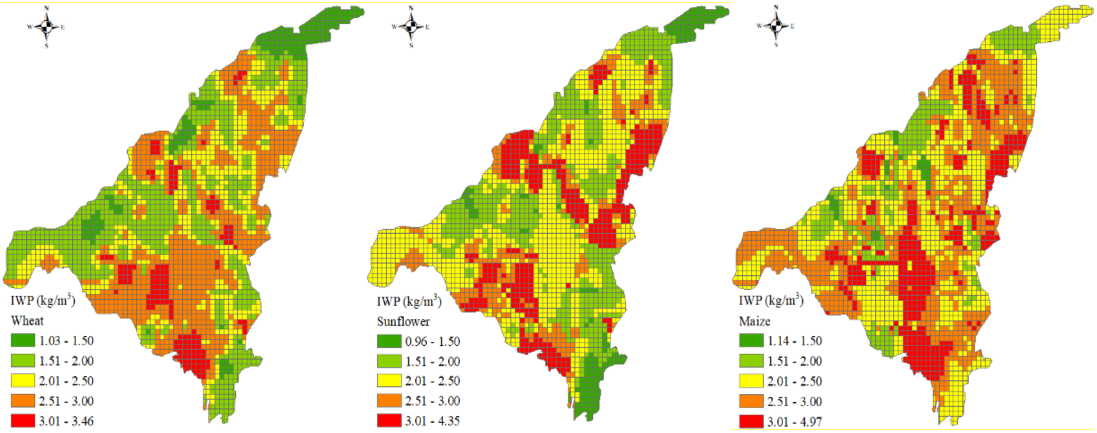
(b)


IWP (kg/m³)
Wheat
🟩 0.66 - 1.50
🟩 1.51 - 1.90
🟨 1.91 - 2.30
🟧 2.31 - 2.70
🟥 2.71 - 3.82
IWP (kg/m³)
Sunflower
🟩 0.93 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.09
IWP (kg/m³)
Maize
🟩 0.78 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.67

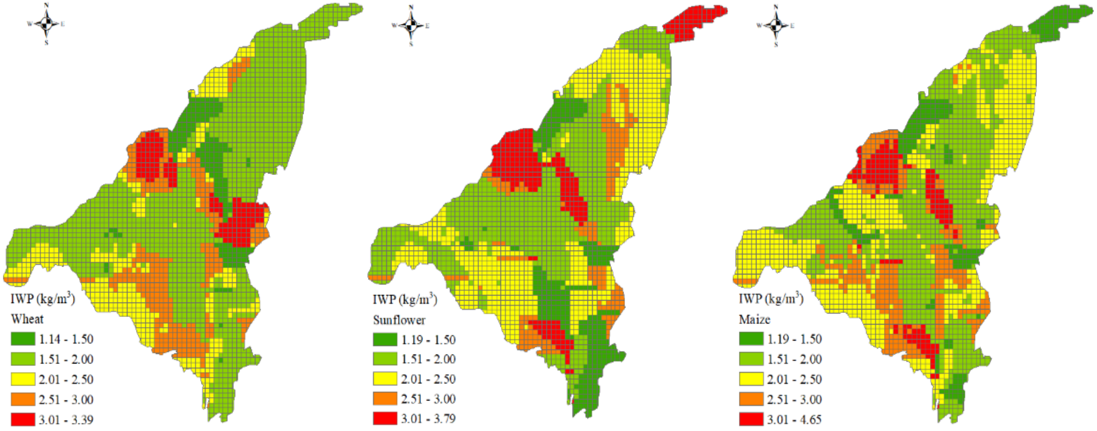
(c)


IWP (kg/m³)
Wheat
🟩 0.65 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.83
IWP (kg/m³)
Sunflower
🟩 0.69 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.57
IWP (kg/m³)
Maize
🟩 0.78 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.86

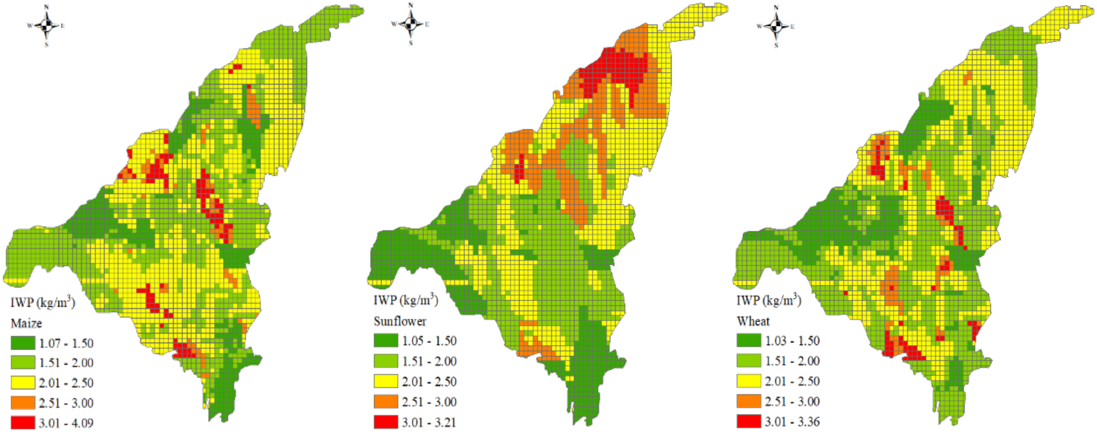
(d)


IWP (kg/m$^3$)
Wheat
🟩 1.03 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.46
IWP (kg/m$^3$)
Sunflower
🟩 0.96 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.35
IWP (kg/m$^3$)
Maize
🟩 1.14 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.97

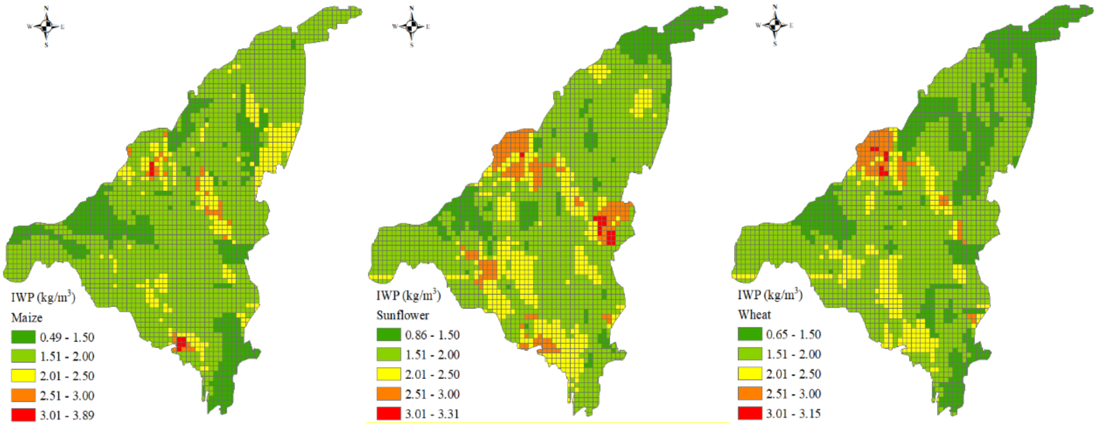
(e)


IWP (kg/m$^3$)
Wheat
🟩 1.14 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.39
IWP (kg/m$^3$)
Sunflower
🟩 1.19 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.79
IWP (kg/m$^3$)
Maize
🟩 1.19 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.65

(f)


IWP (kg/m$^3$)
Maize
🟩 1.07 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 4.09
IWP (kg/m$^3$)
Sunflower
🟩 1.05 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.21
IWP (kg/m$^3$)
Wheat
🟩 1.03 - 1.50
🟩 1.51 - 2.00
🟨 2.01 - 2.50
🟧 2.51 - 3.00
🟥 3.01 - 3.36

(g)



(h)

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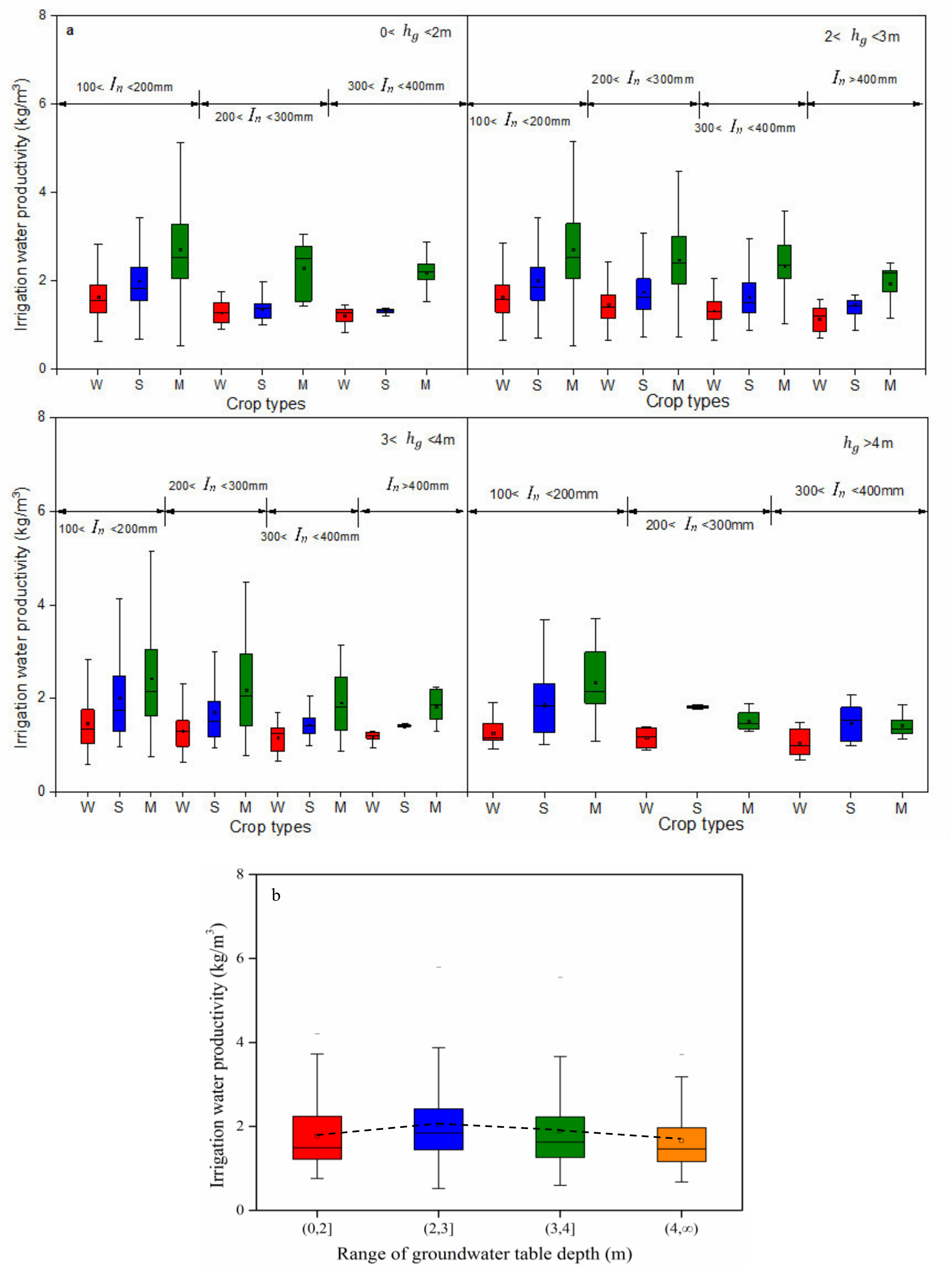

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