

Response to Editor

Dear authors,

thank you very much for the revised version of your manuscript. Since all other reviewers suggested minor revisions, I only requested one of the reviewers (René Orth) to comment on the new version.

He appreciates the additional analyses performed, but still feels that some of the variables have not been validated, such as run-off. The reviewer suggests additional analyses, regarding (1) use updated version of the Jung et al. dataset (Jung et al., 2019) and (2) use the E-RUN dataset (Gudmundsson and Seneviratne, 2016) to validate the runoff.

I find that the manuscript has much improved and you have made good effort addressing the reviewers comments. I think the manuscript is almost ready for publication, given some amendments. In view of the fact that the Jung et al. (2019) paper was published only after the submission of the manuscript (although the data were available earlier), I will not insist on this additional analysis. However, please consider the Gudmundson and Seneviratne (2016) dataset. Please also attend to the detailed comments of the reviewer.

I am looking forward to your resubmitted manuscript,

Anke Hildebrandt.

Response: We thank the editor for the evaluation and comment on the revised manuscript. As suggested by the editor and reviewer, we have conducted additional analyses using the E-RUN database (Gudmundson and Seneviratne, 2016) and the FLUXCOM database (updated version of MPI database, Jung et al., 2019). We also revised the manuscript accordingly as well as conducted a point-by-point response to all the comments by the reviewer.

The main comment here is a further cross-validation of the CDR runoff based on the E-RUN database. The comparison results show that both the long-term mean (\bar{Q}) and standard deviation (σ_Q) of the monthly runoff in the E-RUN database are very similar with those in the CDR database. We further added the comparison results of runoff in the revised Supplementary Material, and also changed the text accordingly in the revised manuscript. Please also see R2C3 for a detailed response to this point.

Another comment is about using the FLUXCOM database instead of MPI in the validation of the CDR evapotranspiration E . As has been noted by the editor, the FLUXCOM database paper was published after the submission of this manuscript. In addition, the monthly FLUXCOM data is currently only available (open to public) for a much shorter period (2001-2010) compared with both the monthly CDR (1984-1010) and the original MPI (1982-1011) databases. As strongly suggested by R2, we conducted further comparison between the CDR and FLUXCOM databases, and the results are similar with those comparison between the CDR and MPI databases. Given the limited time period in the FLUXCOM database and the similarity of comparison results using the MPI and FLUXCOM databases, we choose to keep the results of the MPI database in the Supplementary Material. Please also see R2C2 for detailed response.

Again, we sincerely appreciate both the editor and reviewer for constructive suggestions and comments on the revised manuscript.

Response to Referee #2 (Dr René Orth)

R2C1: Second review of Yin and Roderick “Inter-annual variability of the global terrestrial cycle“

The paper has overall improved as the authors have addressed many of the concerns raised by me and the other reviewers. However, one important issue, and several minor points remain unresolved.

Response: We thank Dr René Orth for the evaluation and helpful comments on the revised manuscript. Please see detailed response to all the comments as follows.

R2C2: Main comment: As mentioned in my previous review, I think it is critical for this study to show that the discovered patterns are not just implemented in the model used to derive the CDR dataset. It has to be shown that similar patterns are present across independent datasets, as only this can indicate that nature is indeed operating this way. I appreciate efforts in this direction made by the authors, namely the consideration of the LandFlux-EVAL dataset, the Jung et al. dataset, and the ERA5 reanalysis. But I believe that these analyses need to be expanded before the paper can be published:

(1) I understand that the authors do not want to use GLEAM as a reference dataset as this was used in the derivation of the CDR reanalysis. But instead the Jung et al. dataset should be updated to the 2019 version (Jung et al. 2019). The authors stated in their response: 'We could replace the MPI we used with the updated database (Jung et al., 2019) but we do not see how that would alter the results.' This is not about altering the results, but about using state-of-the-art alternative datasets to illustrate the robustness of the CDR-based results. I do not see the point in using an almost 10-year old dataset while updated and much evolved datasets exist.

Response: As suggested by R2, we conducted further comparison between the CDR and FLUXCOM ($0.5^\circ \times 0.5^\circ$, monthly, 2001-2010) (updated version of MPI database, Jung et al., 2019) databases, and the results are shown in Fig. R1. The results are similar with the previous comparison between the CDR and MPI databases, showing underestimation of the monthly mean E and bias and scaling offset in the standard deviations of monthly E in the CDR database compared with the FLUXCOM database.

However, currently the monthly FLUXCOM database is only available (open to public) for the restricted period 2001-2010, which is much shorter than both the CDR (available during 1984-2010) and the MPI (available during 1982-2011) databases. Given the limited time period for the FLUXCOM database and the similar comparison results of the MPI and FLUXCOM to the CDR databases, we propose to keep the results based on the original MPI database in the Supplementary material.

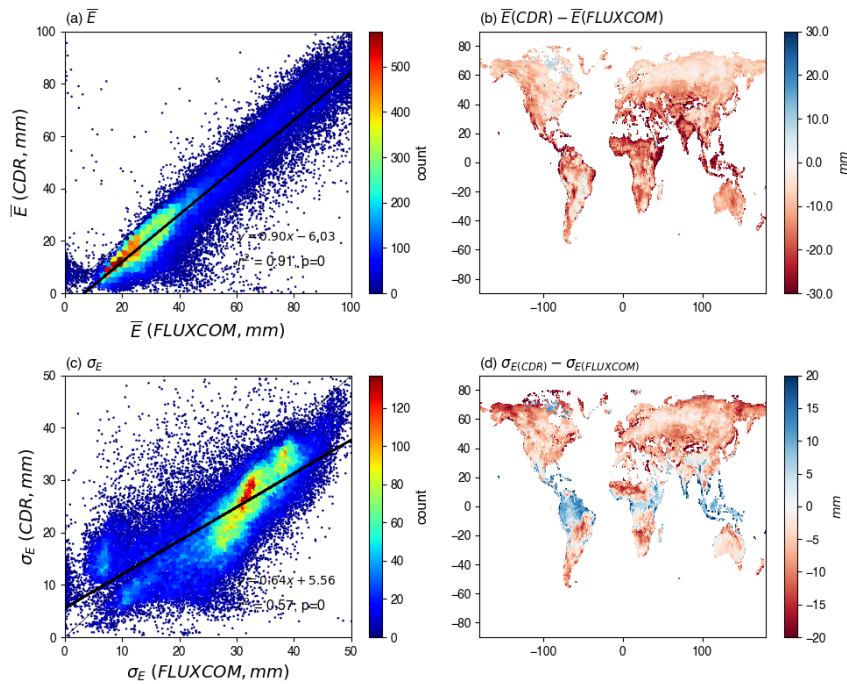


Figure R1. Comparison of monthly evapotranspiration E between FLUXCOM and Climate Data Record (CDR) databases. Top panels (a) (b) show comparison of the mean monthly (\bar{E}) while bottom panels (c) (d) show comparison of the standard deviation (σ_E) of monthly E .

R2C3: (2) I also appreciate the ERA5-based analyses which the authors have done in response to my previous comments. I share their conclusion that this dataset is not suitable to be used in the context of this study. However, this way the runoff results remain not confirmed with independent data. Therefore I suggest to use the E-RUN gridded runoff dataset (Gudmundsson and Seneviratne 2016) for this purpose.

I do not wish to remain anonymous - Rene Orth.

Response: As suggested, we conduct further comparison of the monthly runoff between the E-RUN ($0.5^\circ \times 0.5^\circ$, monthly, 1951-2015) (Gudmundsson and Seneviratne, 2016) and CDR databases. The comparison is conducted based on the overlap of time (1984-2010) and space (Europe) in both databases, and the results are shown in Figs. R2-R3. We can see that both the long-term mean (\bar{Q}) and standard deviation (σ_Q) of the monthly runoff show very similar spatial patterns in the E-RUN and CDR databases (Fig. R2). The grid-by-grid comparison also shows close agreement (Fig. R3). We have added these results to the revised Supplementary Material (Figs. S10-S11), and also added the text in the revised manuscript as follows (lines 165-169):

“The comparison of runoff Q between the E-RUN and CDR databases show that the two databases have very similar spatial patterns of both the long-term mean (\bar{Q}) and standard deviation (σ_Q) of the monthly Q (Fig. S10). The grid-by-grid comparison results are also encouraging, showing slight bias of both the long-term mean and standard deviation of monthly Q in the CDR database compared with the E-RUN database (Fig. S11).”

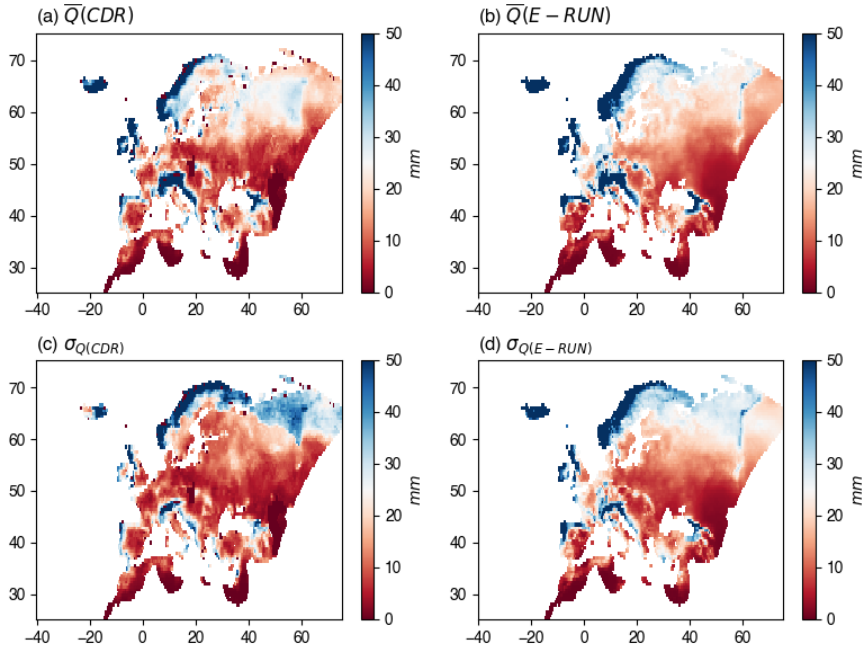


Figure R2. Mean (\bar{Q}) and standard deviation (σ_Q) of monthly runoff Q in the E-RUN and Climate Data Record (CDR) databases in the area of spatial overlap (Europe). Top panels (a) (b) show the mean monthly (\bar{Q}) while bottom panels (c) (d) show the standard deviation (σ_Q) of monthly Q .

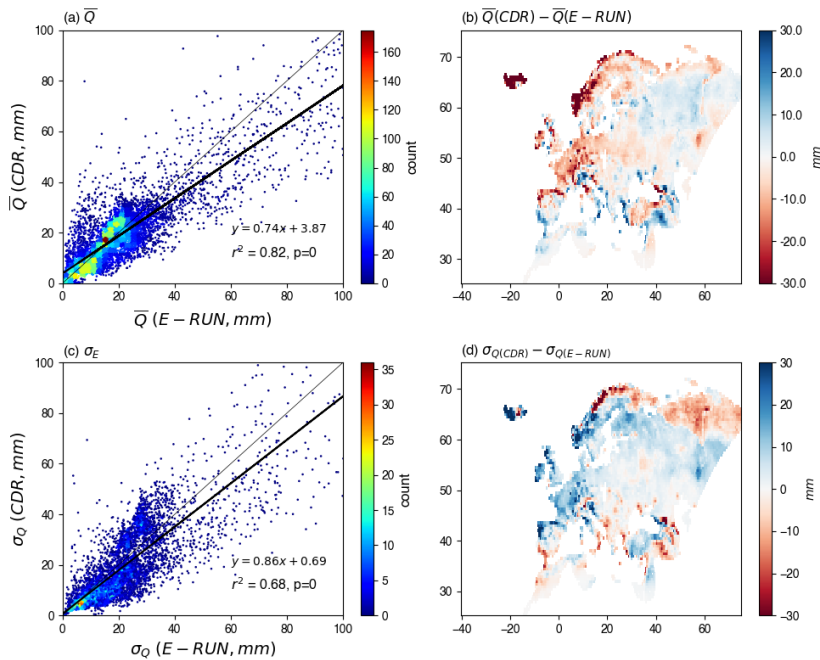


Figure R3. Comparison of monthly runoff Q between the E-RUN and Climate Data Record (CDR) databases in the area of spatial overlap (Europe). Top panels (a) (b) show comparison of the mean monthly (\bar{Q}) while bottom panels (c) (d) show comparison of the standard deviation (σ_Q) of monthly Q .

Specific comments:

R2C4: lines 53-55: This statement somewhat ignores the efforts leading to the ERA-Land (Balsamo et al. 2013) and MERRA-Land (Reichle et al. 2011) datasets.

Response: We have acknowledged the efforts in developing land-based products in the revised manuscript by modifying the sentence to (lines 53-57): “*Though efforts have been taken to develop land-based products from atmospheric reanalyses, e.g., ERA-Land (Balsamo et al. 2013) and MERRA-Land (Reichle et al. 2011) databases, however, the central aim of atmospheric re-analysis is to estimate atmospheric variables. That atmospheric-centric aim, understandably, ignores many of the nuances of soil water infiltration, vegetation water uptake, runoff generation and many other processes of central importance in hydrology.*”. The relevant reference has also been cited in the revised manuscript.

R2C5: line 75: 'the various ... databases' - after only reading the text up to this point it is not clear what is meant here

Response: It means the databases used in this study will be introduced and described in Section 2. To make this sentence more clear, we have modified it in the revised manuscript as follows (lines 77-79): “*We begin in Section 2 by describing the various climate and hydrologic databases used in this study, and also include a further assessment of the suitability of the CDR database for this initial variability study.*”.

R2C6: line 78: it should be 'these variabilities'

Response: Done. Thank you.

R2C7: lines 88/89: 'in time step t' - these are all fluxes which are accumulated during time steps t-1 and t; also, I would mention here that the time step considered in this study is 1 year

Response: We have added the annual time step in this sentence to make it more clear in the revised version (lines 90-91): “*with P the precipitation, E the evapotranspiration, Q the runoff and ΔS the total water storage change in time step t (annual in this study).*”. Thank you.

R2C8: lines 91/92: 'Eq (1) is the familiar...' - this sentence is an unnecessary repetition

Response: This sentence has been deleted in the revised manuscript. Thanks.

R2C9: line 96: known here?

Response: To make the meaning of this sentence more clear, we have removed the word 'known' and modified it in the revised manuscript as follows (lines 98-99): “*We use the Climate Data Record (CDR) database (Zhang et al., 2018) which is a recently released global land hydrologic re-analysis.*”.

R2C10: line 103: The SRB dataset only extends until 2007 (if I am not mistaken) while the analyses in this study consider a time period until 2010. How can you still use the SRB data then?

Response: The aim of this study is to investigate the inter-annual variability of global water cycle based on the CDR database, which extends from 1984 to 2010. During the construction process, the CDR database made some assumptions considering the 27-year period (1984-2010) as an integrity, e.g., the long-term (27-year) storage change to be zero. To better investigate the inter-annual variability by using the CDR database in this study, we choose to stick to the CDR period, i.e., 1984-2010.

While the SRB database is only available from 1984 to 2007 (not to 2010), we only use it to calculate the long-term E_o ($\overline{E_o}$) and further estimate the aridity index ($\overline{E_o}/\overline{P}$). We believe the three-year period difference would not have a material impact on the aridity index estimation or change the general conclusions in this study. Thanks.

R2C11: lines 105/106: Sentence is hard to understand, please rephrase.

Response: We have rephrased this sentence in the revised manuscript as follows (lines 107-108): “*In general, we anticipate two important factors, i.e., the water storage capacity and the presence of ice/snow at the surface, which are most likely to have influence on the partitioning of hydrologic variability.*”. Thanks.

R2C12: line 160: Please comment on the offset.

Response: We have added more details for the offset and modified the sentence in the revised manuscript as follows: “*In terms of variability, the standard deviations of monthly E from the CDR are in very close agreement with the LandFluxEVAL database (Fig. S7c), but there is a bias and scaling offset for the comparison with the MPI database particularly for the grid-cells with low standard deviation of E (Fig. S8c).*”.

R2C13: line 177: I would replace 'trend' with 'pattern'

Response: Done. Thank you.

R2C14: line 180: not clear what is meant here with 'physics of runoff generation'

Response: Yes, we agree that the ‘physics of runoff generation’ is not clear and we have replaced it with more specific term in the revised manuscript as follows (lines 187-189): “*However, there is substantial scatter due to, for example, regional variations related to seasonality, water storage change and the landscape characteristics*”.

R2C15: lines 178-181: Padron et al. 2017 is relevant in this context, and could be cited.

Response: The reference has now been cited in the revised manuscript. Thank you.

R2C16: lines 188, 203, 223: 'very different' is not obvious to me from the comparison of Figs 1 and 3. Please clarify.

Response: Here we mean it is very different between the partitioning of \bar{P} and σ_P^2 . In brief, the \bar{P} is mostly partitioned into \bar{E} or \bar{Q} . However, for the partitioning of σ_P^2 , σ_E^2 is generally very small with σ_P^2 mostly partitioned into σ_Q^2 , $\sigma_{\Delta S}^2$ and even the covariance components. Please see the more comprehensive and detailed analyses in the revised manuscript (lines 199-209).

R2C17: lines 225-226: This is an important finding which should be highlighted in the abstract and/or conclusions.

Response: Yes, the finding here has been added in the abstract (lines 11-12): “*Instead we find that σ_P^2 is mostly partitioned between σ_Q^2 , $\sigma_{\Delta S}^2$ and the associated covariances with limited partitioning to σ_E^2 .*”.

R2C18: lines 294-303: If the main conclusion is that things are complex, and there is no particular lesson learned here, then I would suggest to remove this section. It confuses readers and distracts from the relevant main messages of the study.

Response: While the results here are complex and not easy to understand, we still could have some implications obtained here, for example, the difference between partitioning of σ_P^2 at high and low temperature. That difference does show the important role of temperature in the partitioning of σ_P^2 , which might be helpful for the future studies. Therefore, we would like to keep this section in the revised manuscript.

R2C19: lines 307-328: It feels inconsistent that in addition to the wet and hot grid cell no wet and cold grid cell has been selected as a case study (as was done in the case of high and low water storage capacity).

Response: The reason we did not pick any case study site here is because there is substantial scatter in wet and cold conditions ($\bar{E}_o/\bar{P} \leq 0.5$ in first column of Fig. 8). The partitioning of σ_P^2 in wet and cold conditions is so complex that no grid-cell could be chosen as a representative case study site. Instead of a case study site, we further illustrate the importance of snow/ice presence in variance partitioning (lines 425-426) and expect more emphasis on this in the future studies that our manuscript will inspire.

R2C20: - While this study is performed at annual time scales, the authors could add some outlook/clarification that the revealed variability propagation across the water cycle might behave differently at shorter time scales

Response: Yes, we agree that the variability partitioning might be different at various time scales. In response, we have added an expectation for future work at various time scales in the revised manuscript (lines 408-410): “*These general principles of variance partitioning in the water cycle above may vary at different time scales (e.g., monthly, daily), and we expect more details of the variability partitioning across various temporal scales to be investigated in future studies.*”.

R2C21: - Figures 2,5, and others display physically implausible values - please comment on this

Response: Yes, there are some grid-cells showing physically implausible values in Figs. 2 and 5. In this study, we have tried to exclude the grid-cells with high uncertainty (please see Section 2.3 and Fig. S2), therefore, it is unlikely that those implausible values are caused by data uncertainty/error. While checking the location of those grid-cells, we found that they almost appear in/close to the Greenland. Therefore, we guess those physically implausible values are caused by the permanent ice/glacier. As also noted in this study, with the presence of snow/ice, it is very complex in the variance partitioning. In this study, we highlighted regions with snow/ice coverage. We expect future studies to further uncover the role of snow/ice in the variance partitioning and show details of these physically implausible values.

R2C22: - It is not intuitive that non-consistent (logarithmic/non-lagarithmic) axes are used for E_0/P across different figures.

Response: Yes, the axes for the aridity index (E_0/P) are linear in Figs. 2, 5 and 6 and logarithmic in Figs. 7 and 8. The underlying reason for that is because there are different purposes in presenting the results in these figures. In Figs. 2, 5 and 6, we show the relation of long-term mean and variance to E_0/P . It is better to use the regular non-logarithmic axes to compare with results in previous studies (e.g., Budyko-curve and Koster and Suarez analyses) that also use linear axes. While in Figs. 7 and 8, we highlight the role of storage capacity and physical phase (solid/liquid) in variance partitioning in both extremely dry and wet environments. We found the logarithmic axes to better show the necessary details in Figs. 7 and 8.

R2C23: References:

Balsamo, G., C. Albergel, A. Beljaars, S. Boussetta, E. Brun, H. Cloke, D. Dee, E. Dutra, J. Muñoz-Sabater, F. Pappengerger, P. de Rosnay, T. Stockdale, and F. Vitart, 2013: ERA Interim Land: a global land water resources dataset. *Hydrol. Earth Syst. Sci.*, 19, 389–407.

Gudmundsson, L., and S.I. Seneviratne, 2016: Observation-based gridded runoff estimates for Europe (E-RUN version 1.1). *Earth Syst. Sci. Data*, 8 (2), 279–295.

Jung, M., S. Koirala, U. Weber, K. Ichii, F. Gans, G. Camps-Valls, D. Papale, C. Schwalm, G. Tramontana, and M. Reichstein, 2019: The FLUXCOM ensemble of global land-atmosphere energy fluxes. *Scientific Data*, 6 (74).

Padron, R.S., L. Gudmundsson, P. Greve, and S.I. Seneviratne, 2017: Large- Scale Controls of the Surface Water Balance Over Land: Insights From a Systematic Review and Meta-Analysis. *Water Res. Resour.*, 53 (11), 9659-9678.

Reichle, R.H., R.D. Koster, G.J.M.D. Lannoy, B.A. Forman, Q. Liu, S.P.P. Mahanama, and A. Toure, 2011: Assessment and enhancement of MERRA land surface hydrology estimates. *J. Clim.*, 24, 6322–6338,

Response: We thank Dr René Orth for listing all the reference in the comments, and we have read and cite these reference accordingly in the revised manuscript.

Inter-annual variability of the global terrestrial water cycle

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Abstract:

1 Variability of the terrestrial water cycle, i.e., precipitation (P), evapotranspiration (E), runoff (Q) and water
2 storage change (ΔS) is the key to understanding hydro-climate extremes. However, a comprehensive global
3 assessment for the partitioning of variability in P between E , Q and ΔS is still not available. In this study, we use
4 the recently released global monthly hydrologic reanalysis product known as the Climate Data Record (CDR) to
5 conduct an initial investigation of the inter-annual variability of the global terrestrial water cycle. We first
6 examine global patterns in partitioning the long-term mean \bar{P} between the various sinks \bar{E} , \bar{Q} and $\bar{\Delta S}$ and
7 confirm the well-known patterns with \bar{P} partitioned between \bar{E} and \bar{Q} according to the aridity index. In a new
8 analysis based on the concept of variability source and sinks we then examine how variability in the
9 precipitation σ_P^2 (the source) is partitioned between the three variability sinks σ_E^2 , σ_Q^2 and $\sigma_{\Delta S}^2$ along with the
10 three relevant covariance terms, and how that partitioning varies with the aridity index. We find that the
11 partitioning of inter-annual variability does not simply follow the mean state partitioning. Instead we find that
12 σ_P^2 is mostly partitioned between σ_Q^2 , $\sigma_{\Delta S}^2$ and the associated covariances with limited partitioning to σ_E^2 . We also
13 find that the magnitude of the covariance components can be large and often negative, indicating that variability
14 in the sinks (e.g., σ_Q^2 , $\sigma_{\Delta S}^2$) can, and regularly does, exceed variability in the source (σ_P^2). Further investigations
15 under extreme conditions revealed that in extremely dry environments the variance partitioning is closely related
16 to the water storage capacity. With limited storage capacity the partitioning of σ_P^2 is mostly to σ_E^2 , but as the
17 storage capacity increases the partitioning of σ_P^2 is increasingly shared between σ_E^2 , $\sigma_{\Delta S}^2$ and the covariance
18 between those variables. In other environments (i.e., extremely wet and semi-arid/semi-humid) the variance
19 partitioning proved to be extremely complex and a synthesis has not been developed. We anticipate that a major
20 scientific effort will be needed to develop a synthesis of hydrologic variability.

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22 **1. Introduction**

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24 In describing the terrestrial branch of the water cycle, the precipitation (P) is partitioned into evapotranspiration
25 (E), runoff (Q) and change in water storage (ΔS). With averages taken over many years, $\overline{\Delta S}$ is usually assumed to
26 be zero and it has long been recognized that the partitioning of the long-term mean annual precipitation (\overline{P})
27 between \overline{E} and \overline{Q} was jointly determined by the availability of both water (\overline{P}) and energy (represented by the net
28 radiation expressed as an equivalent depth of water and denoted \overline{E}_o). Using data from a large number of
29 watersheds, Budyko (1974) developed an empirical relation relating the evapotranspiration ratio ($\overline{E}/\overline{P}$) to the
30 aridity index ($\overline{E}_o/\overline{P}$). The resultant empirical relation and other Budyko-type forms (e.g., Fu, 1981; Choudhury,
31 1999; Yang et al., 2008, Roderick and Farquhar, 2011; Sposito, 2017) that partition P between E and Q have
32 proven to be extremely useful in both understanding and characterising the long-term mean annual hydrological
33 conditions in a given region.

34

35 However, the long-term mean annual hydrologic fluxes rarely occur in any given year. Instead, society must
36 (routinely) deal with variability around the long-term mean. The classic hydro-climate extremes are droughts and
37 floods but the key point here is that hydrologic variability is expressed on a full spectrum of time and space scales.
38 To accommodate that perspective, we need to extend our thinking beyond the long-term mean to ask how the
39 variability of P is partitioned into the variability of E , Q and ΔS (e.g., Orth and Destouni, 2018).

40

41 Early research on hydrologic variability focussed on extending the Budyko curve. In particular, Koster and Suarez
42 (1999) used the Budyko curve to investigate inter-annual variability in the water cycle. In their framework, the
43 evapotranspiration standard deviation ratio (defined as the ratio of standard deviation for E to P , σ_E/σ_P) was (also)
44 estimated using the aridity index ($\overline{E}_o/\overline{P}$). The classic Koster and Suarez framework has been widely applied and
45 extended in subsequent investigations of the variability in both E and Q , using catchment observations, reanalysis
46 data and model outputs (e.g., McMahon et al., 2011; Wang and Alimohammadi 2012; Sankarasubramanian and
47 Vogel, 2002; Zeng and Cai, 2015). However, typical applications of the Koster and Suarez framework have
48 previously been at regional scales and there is still no comprehensive global assessment for partitioning the
49 variability of P into the variability of E , Q and ΔS . One reason for the lack of a global comprehensive assessment
50 is the absence of gridded global hydrologic data. Interestingly, the atmospheric science community have long

51 used a combination of observations and model outputs to construct gridded global-scale atmospheric re-analyses
52 and such products have become central to atmospheric research. Those atmospheric products also contain
53 estimates of some of the key water cycle variables (e.g., P , E), such as in the widely used interim ECMWF Re-
54 Analysis (ERA-Interim; Dee et al. 2011). Though efforts have been taken to develop land-based products from
55 atmospheric reanalyses, e.g., ERA-Land (Balsamo et al., 2013) and MERRA-Land (Reichle et al., 2011) databases,
56 however, the central aim of atmospheric re-analysis is to estimate atmospheric variables. That atmospheric-centric
57 aim, understandably, ignores many of the nuances of soil water infiltration, vegetation water uptake, runoff
58 generation and many other processes of central importance in hydrology.

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60 Hydrologists have only recently accepted the challenge of developing their own re-analysis type products with
61 perhaps the first serious hydrologic re-analysis being published as recently as a few years ago (Rodell et al., 2015).
62 More recently, the Princeton University group has extended this early work by making available a gridded global
63 terrestrial hydrologic re-analysis product known as the Climate Data Record (CDR) (Zhang et al., 2018). Briefly,
64 the CDR was constructed by synthesizing multiple in-situ observations, satellite remote sensing products, and
65 land surface model outputs to provide *gridded* estimates of global land precipitation P , evapotranspiration E ,
66 runoff Q and total water storage change ΔS ($0.5^\circ \times 0.5^\circ$, monthly, 1984-2010). In developing the CDR, the authors
67 adopted local water budget closure as the fundamental hydrologic principle. That approach presented one
68 important difficulty. Global observations of ΔS start with the GRACE satellite mission from 2002. Hence before
69 2002 there is no direct observational constraint on ΔS and the authors made the further assumption that the mean
70 annual ΔS over the full 1984-2010 period was zero at every grid-box. That is incorrect in some regions (e.g.
71 Scanlon et al., 2018) and represents an observational problem that cannot be overcome. However, our interest is
72 in the year-to-year variability and for that application, the assumption of no change in the mean annual ΔS over
73 the full 1984-2010 period is unlikely to lead to major problems since we are not looking for subtle changes over
74 time. With that caveat in mind, the aim of this study is to use this new 27-year gridded hydrologic re-analysis
75 product to conduct an initial investigation of the inter-annual variability of the terrestrial branch of the global
76 water cycle.

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78 The paper is structured as follows. We begin in Section 2 by describing the various climate and hydrologic
79 databases used in this study, and also include, a further assessment of the suitability of the CDR database for this

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84 initial variability study. In Section 3, we examine relationships between the mean and variability in the four water
85 cycle variables (P , E , Q and ΔS). In Section 4, we first relate the ~~variabilities~~ to the classical aridity index and
86 then use those results to evaluate the theory of Koster and Suarez (1999). Subsequently we examine how the
87 variance of P is partitioned into the variances (and relevant covariances) of E , Q and ΔS and undertake an initial
88 survey that investigates some of the factors controlling the variance partitioning. We conclude the paper with a
89 discussion summarising what we have learnt about water cycle variability over land by using the CDR database.

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91 2. Methods and Data

92 2.1 Methods

93 The water balance is defined by,

$$94 P(t) = E(t) + Q(t) + \Delta S(t) \quad (1)$$

95 with P the precipitation, E the evapotranspiration, Q the runoff and ΔS the total water storage change in time

96 step t (annual in this study). By the usual variance law, we have,

$$97 \sigma_P^2 = \sigma_E^2 + \sigma_Q^2 + \sigma_{\Delta S}^2 + 2cov(E, Q) + 2cov(E, \Delta S) + 2cov(Q, \Delta S) \quad (2)$$

98 that includes all relevant variances (denoted σ^2) and covariances (denoted cov). Eq. (2) can be thought of as the
99 hydrologic variance balance equation.

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101 2.2 Hydrologic and Climatic Data

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103 We use the ~~Climate Data Record (CDR) database (Zhang et al., 2018) which is a~~ recently released global land
104 hydrologic re-analysis. This product includes global precipitation P , evapotranspiration E , runoff Q and water
105 storage change ΔS ($0.5^\circ \times 0.5^\circ$, monthly, 1984-2010). In this study we focus on the inter-annual variability and
106 the monthly water cycle variables (P , E , Q and ΔS) are aggregated to annual totals. The CDR does not report
107 additional radiation variables and we use the NASA/GEWEX Surface Radiation Budget (SRB) Release-3.0
108 (monthly, 1984-2007, $1^\circ \times 1^\circ$) database (Stackhouse et al., 2011) to calculate E_o (defined as the net radiation
109 expressed as an equivalent depth of liquid water, Budyko, 1974). We then calculate the aridity index (\bar{E}_o/\bar{P}) using
110 P from the CDR and E_o from the SRB databases (see Fig. S1a in the Supplementary Material).

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117 ~~In general, we anticipate two important factors, i.e., the water storage capacity and the presence of ice/snow at the~~
118 ~~surface, which are most likely to have influence on the partitioning of hydrologic variability. For the storage, the~~
119 active range of the monthly water storage variation was used to approximate the water storage capacity (S_{max}). In
120 more detail, the water storage $S(t)$ at each time step t (monthly here) was first calculated from the accumulation
121 of $\Delta S(t)$, i.e., $S(t) = S(t-1) + \Delta S(t)$ where we assumed zero storage at the beginning of the study period (i.e., $S(0)$
122 = 0). With the resulting time series available, S_{max} was estimated as the difference between the maximum and
123 minimum $S(t)$ during the study period at each grid-box (see Fig. S1b in the Supplementary Material). The
124 estimated S_{max} shows a large range from 0 to 1000 mm with the majority of values from 50 to 600 mm (Fig. S1b),
125 which generally agrees with global rooting depth estimates assuming that water occupies from 10 to 30% of the
126 soil volume at field capacity (Jackson et al., 1996; Wang-Erlandsson et al., 2016; Yang et al., 2016). To
127 characterise snow/ice cover, and to distinguish extremely hot and cold regions, we also make use of a gridded
128 global land air temperature dataset from the Climatic Research Unit (CRU TS4.01 database, monthly, 1901-2016,
129 $0.5^\circ \times 0.5^\circ$) (Harris et al., 2014). (see Fig. S1c in the Supplementary Material).

130

131 2.3 Spatial Mask to Define Study Extent

132

133 The CDR database provides an estimate of the uncertainty ($\pm 1\sigma$) for each of the hydrologic variables (P , E , Q ,
134 ΔS) in each month. We use those uncertainty estimates to identify and remove regions with high relative
135 uncertainty in the CDR data. The relative uncertainty is calculated as the ratio of root mean square of the
136 uncertainty ($\pm 1\sigma$) to the mean annual P , E and Q at each grid-box following the procedure used by Milly and
137 Dunne (2002a). Note that the long term mean ΔS is zero by construction in the CDR database, and for that reason
138 we did not use ΔS to calculate the relative uncertainty. Grid-boxes with a relative uncertainty (in P , E and Q) of
139 more than 10% are deemed to have high relative uncertainty (Milly and Dunne, 2002a) and were excluded from
140 the study extent. The excluded grid-boxes were mostly in the Himalayan region, the Sahara Desert and in
141 Greenland. The final spatial mask is shown in Fig. S2 and this has been applied throughout this study.

142

143 2.4 Further Evaluation of CDR Data for Variability Analysis

144

145 In the original work, the CDR database was validated by comparison with independent observations including (i)
146 mean seasonal cycle of Q from 26 large basins (see Fig. 8 in Zhang et al., 2018), (ii) mean seasonal cycle of ΔS

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154 from 12 large basins (Fig. 10 in Zhang et al., 2018), (iii) monthly runoff from 165 medium size basins and a
155 further 862 small basins (Fig. 14 in Zhang et al., 2018), (iv) summer E from 47 flux towers (Fig. 16 in Zhang et
156 al., 2018). Those evaluations did not directly address variability in various water cycle elements. With our focus
157 on the variability we decided to conduct further validations of the CDR database beyond those described in the
158 original work. In particular, we focussed on further independent assessments of E and we use monthly (as opposed
159 to summer) observations of E from FLUXNET to evaluate the variability in E . We also compare the
160 evapotranspiration E in the CDR with two other gridded global E products that were not used to develop the CDR
161 including the LandFluxEval database ($1^\circ \times 1^\circ$, monthly, 1989-2005) (Mueller et al., 2013) and the Max Planck
162 Institute database (MPI, $0.5^\circ \times 0.5^\circ$, monthly, 1982-2011) (Jung et al., 2010). The runoff Q in the CDR is further
163 compared with the gridded European Q product E-RUN ($0.5^\circ \times 0.5^\circ$, monthly, 1951-2015) (Gudmundsson and
164 Seneviratne, 2016).

166 For the comparison to FLUXNET observations (Baldocchi et al., 2001; Agarwal et al., 2010) we identified 32
167 flux tower sites (site locations are shown in Fig. S3 and details are shown in Table S1) having at least three years
168 of continuous (monthly) measurements using the FluxnetLSM R package (v1.0) (Ukkola et al. 2017). The monthly
169 totals and annual climatology of P and E from CDR generally follow FLUXNET observations, with high
170 correlations and reasonable Root Mean Square Error (Figs. S4-S5, Table S1). Comparison of the point-based
171 FLUXNET (~ 100 m – 1 km scale) with the grid-based CDR (~ 50 km scale) is problematic since the CDR
172 represents an area that is at least 2500 times larger than the area represented by the individual FLUXNET towers
173 and we anticipate that the CDR record would be “smoothed” relative to the FLUXNET record. With that in mind,
174 we chose to compare the ratio of the standard deviation of E to P between the CDR and FLUXNET databases and
175 this normalised comparison of the hydrologic variability proved encouraging (Fig. S6).

177 The comparison of E between the CDR and the LandFluxEval and MPI databases also proved encouraging. We
178 found that the monthly mean E from the CDR database is slightly underestimated compared with LandFluxEval
179 database (Fig. S7a), but agrees closely with the MPI database (Fig. S8a). In terms of variability, the standard
180 deviations of monthly E from the CDR are in very close agreement with the LandFluxEval database (Fig. S7c),
181 but there ~~is~~ a bias and scaling offset for the comparison with the MPI database particularly for the grid-cells with
182 low standard deviation of E (Fig. S8c). The comparison of runoff Q between the E-RUN and CDR databases show
183 that the two databases have very similar spatial patterns of both the long-term mean (\bar{Q}) and standard deviation

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185 (σ_Q) of the monthly Q (Fig. S10). The grid-by-grid comparison results are also encouraging, showing slight bias
186 of both the long-term mean and standard deviation of monthly Q in the CDR database compared with the E-RUN
187 database (Fig. S11).

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189 We concluded that while the CDR database was unlikely to be perfect, it was nevertheless suitable for an initial
190 exploratory survey of inter-annual variability in the terrestrial branch of the global water cycle.

191

192 3. Mean and Variability of Water Cycle Components

193 3.1 Mean Annual P , E , Q and the Budyko Curve

194

195 The global pattern of mean annual P , E , Q using the CDR data (1984-2007) is shown in Fig. 1. The mean annual
196 P (\bar{P}) is prominent in tropical regions, southern China, eastern and western North America (Fig. 1a). The
197 magnitude of mean annual E (\bar{E}) more or less follows the pattern of \bar{P} in the tropics (Fig. 1b) while the mean
198 annual Q (\bar{Q}) is particularly prominent in the Amazon, South and Southeast Asia, tropical parts of west Africa
199 and in some other coastal regions at higher latitudes (Fig. 1c).

200

201 We relate the grid-box level ratio of \bar{E} to \bar{P} in the CDR database to the classical Budyko (1974) curve using the
202 aridity index (\bar{E}_o/\bar{P}) (Fig. 2a). As noted previously, in the CDR database, $\bar{\Delta S}$ is forced to be zero and this enforced
203 steady state (i.e., $\bar{P} = \bar{E} + \bar{Q}$) allowed us to also predict the ratio of \bar{Q} to \bar{P} using the same Budyko curve (Fig.

204 2b). The Budyko curves follow the overall pattern in the CDR data, which agrees with previous studies showing
205 that the aridity index can be used to predict water availability (e.g., Gudmundsson et al., 2016). However, there is
206 substantial scatter due to, for example, regional variations related to seasonality, water storage change and the
207 landscape characteristics (Milly, 1994a, b, Padrón et al., 2017). With that caveat in mind, the overall patterns are
208 as expected with \bar{E} following \bar{P} in dry environments ($\bar{E}_o/\bar{P} > 1.0$) while \bar{E} follows \bar{E}_o in wet environments
209 ($\bar{E}_o/\bar{P} \leq 1.0$) (Fig. 2).

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211 3.2 Inter-annual Variability in P , E , Q and ΔS

212

213 We use the variance balance equation (Eq. 2) to partition the inter-annual σ_P^2 into separate components due to σ_E^2 ,
214 σ_Q^2 , $\sigma_{\Delta S}^2$ along with the three covariance components ($2cov(E, Q)$, $2cov(E, \Delta S)$, $2cov(Q, \Delta S)$) (Fig. 3). The

217 spatial pattern of σ_P^2 (Fig. 3a) is very similar to that of \bar{P} (Fig. 1a), which implies that the σ_P^2 is positively
218 correlated with \bar{P} . In contrast the partitioning of σ_P^2 to the various components is very different from the
219 partitioning of \bar{P} (cf. Fig. 1 and 3). First we note that while the overall spatial pattern of σ_E^2 more or less follows
220 σ_P^2 , the overall magnitude of σ_E^2 is much smaller than σ_P^2 and σ_Q^2 in most regions, and in fact σ_E^2 is also generally
221 smaller than $\sigma_{\Delta S}^2$. The prominence of $\sigma_{\Delta S}^2$ (compared to σ_E^2) surprised us. The three covariance components
222 ($cov(E, Q)$, $cov(E, \Delta S)$, $cov(Q, \Delta S)$) are also important in some regions. In more detail, the $cov(E, Q)$ term is
223 prominent in regions where σ_Q^2 is large and is mostly negative in those regions (Fig. 3e), indicating that years with
224 lower E are associated with higher Q and vice-versa. There are also a few regions with prominent positive values
225 for $cov(E, Q)$ (e.g., the seasonal hydroclimates of northern Australia) indicating that in those regions, years with
226 a higher E are associated with higher Q . The $cov(E, \Delta S)$ term (Fig. 3f) has a similar spatial pattern to the
227 $cov(E, Q)$ term (Fig. 3e) but with a smaller overall magnitude. Finally, the $cov(Q, \Delta S)$ term shows a more
228 complex spatial pattern, with both prominent positive and negative values (Fig. 3g) in regions where σ_Q^2 (Fig. 3c)
229 and $\sigma_{\Delta S}^2$ (Fig. 3d) are both large.

230

231 These results show that the spatial patterns in variability are not simply a reflection of patterns in the long-term
232 mean state. On the contrary, we find that of the three primary variance terms, the overall magnitude of (inter-
233 annual) σ_E^2 is the smallest implying the least (inter-annual) variability in E . This is very different from the
234 conclusions based on spatial patterns in the mean P , E and Q (see section 3.1). Further, while σ_Q^2 more or less
235 follows σ_P^2 as expected, we were surprised by the magnitude of $\sigma_{\Delta S}^2$ which, in general, substantially exceeds the
236 magnitude of σ_E^2 . Further, the magnitude of the covariance terms can be important, especially in regions with high
237 σ_Q^2 . However, unlike the variances, the covariance can be both positive and negative and this introduces additional
238 complexity. For example, with a negative covariance it is possible for the variance in Q (σ_Q^2) to exceed the variance
239 in P (σ_P^2). To examine that in more detail we calculated the equivalent frequency distribution for each of the plots
240 in Fig. 3. The results (Fig. S9) further emphasise that in general, σ_E^2 is the smallest of the variances (Fig. S9b).
241 We also note that the frequency distributions for the covariances (Fig. S9efg) are not symmetrical. In summary,
242 it is clear that spatial patterns in the inter-annual variability of the water cycle (Fig. 3) do not simply follow the
243 spatial patterns for the inter-annual mean (Fig. 1).

244

245 3.3 Relation Between Variability and the Mean State for P , E , Q

246

247 Differences in the spatial patterns of the mean (Fig. 1) and inter-annual variability (Fig. 3) in the global water
248 cycle led us to further investigate the relation between the mean and the variability for each separate component.

249 Here we relate the standard deviation (σ_P , σ_E , σ_Q) instead of the variance to the mean of each water balance flux
250 (Fig. 4) since the standard deviation has the same physical units as the mean making the results more comparable.

251 As inferred previously, we find σ_P to be positively correlated with \bar{P} but with substantial scatter (Fig. 4a). The
252 same result more or less holds for the relation between σ_Q and \bar{Q} (Fig. 4c). In contrast the relation between σ_E and

253 \bar{E} is very different (Fig. 4b). In particular, σ_E is a small fraction of \bar{E} and this complements the earlier finding (Fig.
254 4b) that the inter-annual variability for E is generally smaller than for the other physical variables (P , Q and ΔS).

255 (The same result was also found using both LandFluxEVAL and MPI databases, see Fig. S12 in the
256 Supplementary Material.) Importantly, unlike P and Q , E is constrained by both water and energy availability

257 (Budyko, 1974) and the limited inter-annual variability in E presumably reflects limited inter-annual variability
258 in the available (radiant) energy (E_o). This is something that could be investigated in a future study.

259

260 4. Relating the Variability of Water Cycle Components to Aridity

261 In the previous section, we investigated spatial patterns of the mean and the variability in the global water cycle.

262 In this section, we extend that by investigating the partitioning of σ_P^2 to the three primary physical terms (σ_E^2 , σ_Q^2 ,
263 $\sigma_{\Delta S}^2$) along with the three relevant covariances. For that, we begin by comparing the Koster and Suarez (1999)

264 theory against the CDR data and then investigate how the partitioning of the variance is related to the aridity index
265 \bar{E}_o/\bar{P} (see Fig. S1a in the Supplementary Material). Following that, we investigate variance partitioning in relation

266 to both our estimate of the storage capacity S_{\max} (see Fig. S1b in the Supplementary Material) as well as the mean
267 annual air temperature \bar{T}_a (see Fig. S1c in the Supplementary Material) that we use as a surrogate for snow/ice

268 cover. We finalise this section by examining the partitioning of variance at three selected study sites that represent
269 extremely dry/wet, high/low water storage capacity and the hot/cold spectrums.

270

271 4.1 Comparison with the Koster and Suarez (1999) Theory

272

273 We first evaluate the classical empirical curve of Koster and Suarez (1999) by relating ratios σ_E/σ_P and σ_E/σ_P to
274 the aridity index (Fig. 5). The ratio σ_E/σ_P in the CDR database is generally overestimated by the empirical Koster

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276 and Suarez curve, especially in dry environments (e.g., $\overline{E_o}/\overline{P} > 3$) (Fig. 5a). The inference here is that the Koster
277 and Suarez theory predicts σ_E/σ_P to approach unity in dry environments while the equivalent value in the CDR
278 data is occasionally unity but is generally smaller. With σ_E/σ_P generally overestimated by the Koster and Suarez
279 theory we expect, and find, that σ_Q/σ_P is generally underestimated by the same theory (Fig. 5b). The same
280 overestimation was found based on the other two independent databases for E (LandFluxEVAL and MPI) (Fig.
281 [S13](#)). This overestimation is discussed further in section 5.

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283 4.2 Relating Inter-annual Variability to Aridity

284

285 Here we examine how the fraction of the total variance in precipitation accounted for by the three primary variance
286 terms along with the three covariance terms varies with the aridity index ($\overline{E_o}/\overline{P}$) (Fig. 6). (Also see Fig. [S14](#) for
287 the spatial maps.) The ratio σ_E^2/σ_P^2 is close to zero in extremely wet regions and has an upper limit noted
288 previously (Fig. 5a) that approaches unity in extremely dry regions (Fig. 6a). The ratio σ_Q^2/σ_P^2 is close to zero in
289 extremely dry regions but approaches unity in extremely wet regions but with substantial scatter (Fig. 6b). The
290 ratio $\sigma_{\Delta S}^2/\sigma_P^2$ is close to zero in both extremely dry/wet regions (Fig. 6c) and shows the largest range at an
291 intermediate aridity index ($\overline{E_o}/\overline{P} \sim 1.0$).

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293 The covariance ratios are all small in extremely dry (e.g., $\overline{E_o}/\overline{P} \geq 6.0$) environments and generally show the largest
294 range in semi-arid and semi-humid environments. The peak magnitudes for the three covariance components
295 consistently occur when $\overline{E_o}/\overline{P}$ is close to 1.0 which is the threshold often used to separate wet and dry
296 environments.

297

298 4.3 Further Investigations on the Factors Controlling Partitioning of the Variance

299

300 Results in the previous section demonstrated that spatial variation in the partitioning of σ_P^2 into σ_E^2 , σ_Q^2 , $\sigma_{\Delta S}^2$ and
301 the three covariance components is complex (Fig. 6). To help further understand inter-annual variability of the
302 terrestrial water cycle, we conduct further investigations in this section using two factors likely to have a major
303 influence on the variance partitioning of σ_P^2 . The first is the storage capacity S_{\max} (see Fig. S1b in the
304 Supplementary Material). The second is the mean annual air temperature $\overline{T_a}$ (see Fig. S1c in the Supplementary
305 Material) which is used here as a surrogate for snow/ice presence.

308

309 4.3.1 Relating Inter-annual Variability to Storage Capacity

310

311 We first relate the partitioning of σ_p^2 to water storage capacity (S_{\max}) by repeating Fig. 6 but instead we use a
312 logarithmic scale for the x-axis and we distinguish S_{\max} via the background colour (Fig. 7). To eliminate the
313 possible overlap of grid-cells in the colouring process, all the grid-cells over land are further separated using
314 different latitude ranges (as shown in the four columns of Fig. 7), i.e., 90N-60N, 60N-30N, 30N-0 and 0-90S. We
315 find that S_{\max} is relatively high in wet environments ($\overline{E_o}/\overline{P} \leq 1.0$, Fig. 7a) but shows no obvious relation to the
316 partitioning of σ_p^2 . However, in dry environments ($\overline{E_o}/\overline{P} > 1.0$) the ratio σ_E^2/σ_p^2 apparently decreases with the
317 increase of S_{\max} (Fig. 7a-d). That relation is particularly obvious in extremely dry environments ($\overline{E_o}/\overline{P} \geq 6.0$) at
318 equatorial latitudes where there is an upper limit of σ_E^2/σ_p^2 close to 1.0 when S_{\max} is small (blue grid-cells in Fig.
319 7c). The interpretation for those extremely dry environments is that when S_{\max} is small, σ_p^2 is almost completely
320 partitioned into σ_E^2 (Fig. 7bc) with the other variance and covariance components close to zero. While for those
321 same extremely dry environments, as S_{\max} increases, the partitioning of σ_p^2 is shared between σ_E^2 and $\sigma_{\Delta S}^2$ and their
322 covariance (Fig. 7cks) while σ_Q^2 and its covariance components remain close to zero (Fig. 7gow). However, at
323 polar latitudes in the northern hemisphere (panels in the first and second columns of Fig. 7) there are variations
324 that could not be easily associated with variations in S_{\max} which led us to further investigate the role of snow/ice
325 on the variance partitioning in the following section.

326

327 4.3.2 Relating Inter-annual Variability to Mean Air Temperature

328

329 To understand the potential role of snow/ice in modifying the variance partitioning, we repeat the previous
330 analysis (Fig. 7) but here we use the mean annual air temperature ($\overline{T_a}$) to colour the grid-cells to (crudely) indicate
331 the presence of snow/ice (Fig. 8). The results are complex and not easy to simply understand. The most important
332 difference revealed by this analysis is in the hydrologic partitioning between cold (first column) and hot (third
333 column) conditions in wet environments ($\overline{E_o}/\overline{P} \leq 0.5$). In particular, when $\overline{T_a}$ is high, σ_p^2 is almost completely
334 partitioned into σ_Q^2 in wet environments (e.g., $\overline{E_o}/\overline{P} \leq 0.5$, Fig. 8g). In contrast, when $\overline{T_a}$ is low in a wet
335 environment ($\overline{E_o}/\overline{P} \leq 0.5$ in first column of Fig. 8), there are substantial variations in the hydrologic partitioning.
336 That result reinforces the complexity of variance partitioning in the presence of snow/ice.

337

339

340 The previous results (Section 4.3) have demonstrated that the partitioning of σ_P^2 is influenced by the water storage
 341 capacity (S_{\max}) in extremely dry environments ($\overline{E_o}/\overline{P} \geq 6.0$) and that the presence of snow/ice is important (as
 342 indicated by mean air temperature ($\overline{T_a}$)) in extremely wet environments ($\overline{E_o}/\overline{P} \leq 0.5$). In this section, we examine,
 343 in greater detail, several sites to gain deeper understanding of the partitioning of σ_P^2 . For that purpose, we selected
 344 three sites based on extreme values for the three explanatory parameters, i.e., $\overline{E_o}/\overline{P}$ (Fig. S1a), S_{\max} (Fig. S1b) and
 345 $\overline{T_a}$ (Fig. S1c). The criteria to select three climate sites are as follows, Site 1: dry ($\overline{E_o}/\overline{P} \geq 6.0$) and small S_{\max} (S_{\max}
 346 ≈ 0), Site 2: dry ($\overline{E_o}/\overline{P} \geq 6.0$) and relatively large S_{\max} ($S_{\max} \gg 0$) and Site 3: wet ($\overline{E_o}/\overline{P} \leq 0.5$) and hot ($\overline{T_a} > 25$
 347 $^{\circ}\text{C}$). For each of the three classes, we use a representative grid-cell (Fig. 9) to show the original time series (Fig.
 348 10) and the partitioning of the variability (Fig. 11).

349

350 We show the P , E , Q and ΔS time series along with the relevant variances and covariances in Fig. 10. Starting
 351 with the two dry sites, at the site with low storage capacity (Site 1), the time series shows that E closely follows
 352 P leaving annual Q and ΔS close to zero (Fig. 10a). The variance of P ($\sigma_P^2 = 206.9 \text{ mm}^2$) is small and almost
 353 completely partitioned into the variance of E ($\sigma_E^2 = 196.9 \text{ mm}^2$), leaving very limited variance for Q , ΔS and all
 354 three covariance components (Fig. 10b). At the dry site with larger storage capacity (Site 2), E , Q and ΔS do not
 355 simply follow P (Fig. 10c). As a consequence, the variance of P ($\sigma_P^2 = 2798.0 \text{ mm}^2$) is shared between E ($\sigma_E^2 =$
 356 1150.2 mm^2), ΔS ($\sigma_{\Delta S}^2 = 800.5 \text{ mm}^2$) and their covariance component ($2\text{cov}(E, \Delta S) = 538.4 \text{ mm}^2$, Fig. 10d).
 357 Switching now to the remaining wet and hot site (Site 3), we note that Q closely follows P , with ΔS close to zero
 358 and E showing little inter-annual variation (Fig. 10e). The variance of P ($\sigma_P^2 = 57374.4 \text{ mm}^2$) is relatively large
 359 and almost completely partitioned into the variance of Q ($\sigma_Q^2 = 57296.4 \text{ mm}^2$), leaving very limited variance for
 360 E and ΔS and the three covariance components (Fig. 10f). We also examined numerous other sites with similar
 361 extreme conditions as the three case study sites and found the same basic patterns as reported above.

362

363 To put the data from the three case study sites into a broader variability context we position the site data onto a
 364 backdrop of original Fig. 6. As noted previously, at Site 1, the ratio σ_E^2/σ_P^2 is very close to unity (Fig. 11a), and
 365 under this extreme condition, we have the following approximation,

$$366 \quad \sigma_P^2 \approx \sigma_E^2 \quad (\text{Site 1, dry and } S_{\max} \approx 0) \quad (3)$$

367 In contrast, for Site 2 with the same aridity index but higher S_{\max} , we have,

368
$$\sigma_P^2 \approx \sigma_E^2 + \sigma_{\Delta S}^2 + 2cov(E, \Delta S) \quad (\text{Site 2, dry and } S_{\max} \gg 0) \quad (4)$$

369 Finally, at Site 3, we have,

370
$$\sigma_P^2 \approx \sigma_Q^2 \quad (\text{Site 3, wet and hot}) \quad (5)$$

371

372 4.5 Synthesis

373

374 The above simple examples demonstrate that aridity $\overline{E_o}/\overline{P}$, storage capacity S_{\max} and to a lesser extent, air
 375 temperature $\overline{T_a}$, all play some role in the partitioning of σ_P^2 to the various components. Our synthesis of the results
 376 for the partitioning of σ_P^2 is summarised in Fig. 12. In dry environments with low storage capacity ($S_{\max} \approx 0$) we
 377 have minimal runoff and expect that σ_P^2 is more or less completely partitioned into σ_E^2 (Fig. 12a). In those
 378 environments, (inter-annual) variations in storage $\sigma_{\Delta S}^2$ play a limited role in setting the overall variability.
 379 However, in dry environments with larger storage capacity ($S_{\max} \gg 0$), σ_E^2 is only a small fraction of σ_P^2 (Fig. 12a)
 380 leaving most of the overall variance in σ_P^2 to be partitioned to $\sigma_{\Delta S}^2$ and the covariance between E and ΔS (Fig.
 381 12c and Fig. 12e). This emphasises the hydrological importance of water storage capacity in buffering variations
 382 of the water cycle under dry conditions.

383

384 Under extremely wet conditions, the largest difference in variance partitioning is not due to differences in storage
 385 capacity but is instead related to differences in mean air temperature. In wet and hot environments, we have
 386 maximum runoff and find that σ_P^2 is more or less completely partitioned into σ_Q^2 (Fig. 12b) while the partitioning
 387 to σ_E^2 and $\sigma_{\Delta S}^2$ is small. However, in wet and cold environments, the variance partitioning shows great complexity
 388 with σ_P^2 being partitioned into all possible components. We suggest that this emphasises the hydrological
 389 importance of thermal processes (melting/freezing) under extremely cold conditions.

390

391 However, the most complex patterns to interpret are those for semi-arid to semi-humid environments (i.e.,
 392 $\overline{E_o}/\overline{P} \sim 1.0$). Despite a multitude of attempts over an extended period we were unable to develop a simple useful
 393 synthesis to summarise the partitioning of variability in those environments. We found that the three covariance
 394 terms all play important roles and we also found that simple environmental gradients (e.g., dry/wet, high/low
 395 storage capacity, hot/cold) could not easily explain the observed patterns. We anticipate that vegetation related
 396 processes (e.g., phenology, rooting depth, gas exchange characteristics, disturbance, etc.) may prove to be
 397 important in explaining hydrologic variability in these biologically productive regions that support most of human

398 population. This result implies that a major scientific effort will be needed to develop a synthesis of the controlling
399 factors for variability of the water cycle in these environments.

400

401 5. Discussion and Conclusions

402

403 Importantly, hydrologists have long been interested in hydrologic variability, but without readily available
404 databases it has been difficult to quantify water cycle variability. For example, we are not aware of maps showing
405 global spatial patterns in variance for any terms of the water balance (except for P). In this study, we describe an
406 initial investigation of the inter-annual variability of the terrestrial branch in the global water cycle that uses the
407 recently released global monthly Climate Data Record (CDR) database for P , E , Q and ΔS . The CDR is one of
408 the first dedicated hydrologic reanalysis databases and includes data for a 27-year period. Accordingly, we could
409 only examine hydrologic variability over this relatively short period. Further, we expect future improvements and
410 modifications as the hydrologic community seeks to further develop and refine these new reanalysis databases.
411 With those caveats in mind, we started this analysis by first investigating the partitioning of P in the water cycle
412 in terms of long-term mean and then extended that to the inter-annual variability using a theoretical variance
413 balance equation (Eq. 2). Despite the initial nature of this investigation we have been able to establish some useful
414 general principles.

415

416 The mean annual P is mostly partitioned into mean annual E and Q , as is well known, and the results using the
417 CDR were generally consistent with the earlier Budyko framework (Fig. 2). Having established that, the first
418 general finding is that the spatial pattern in the partitioning of inter-annual variability in the water cycle is not
419 simply a reflection of the spatial pattern in the partitioning of the long-term mean. In particular, with the variance
420 calculations, the annual anomalies are squared and hence the storage anomalies do not cancel out like they do
421 when calculating the mean. With that in mind, we were surprised that the inter-annual variability of water storage
422 change ($\sigma_{\Delta S}^2$) is typically larger than the inter-annual variability of evapotranspiration (σ_E^2) (cf. Fig. 3b and 3d).
423 The consequence is that $\sigma_{\Delta S}^2$ is more important than σ_E^2 for understanding inter-annual variability of global water
424 cycle. A second important generalisation is that unlike the variance components which are all positive, the three
425 covariance components in the theory (Eq. 2) can be both positive and negative. We report results here showing
426 both large positive and negative values for the three covariance terms (Fig. 3efg). This was especially prevalent
427 in biologically productive regions ($0.5 < \overline{E_o}/\overline{P} < 1.5$, Fig. 3eg). When examining the mean state, we are accustomed

428 to think that P sets a limit to E , Q and ΔS , as per the mass balance (Eq. 1). But the same thinking does not extend
429 to the variance balance since the covariance terms on the right hand side of Eq. 2 can be both large and negative
430 leading to circumstances where the variability in the sinks (σ_E^2 , σ_Q^2 , $\sigma_{\Delta S}^2$) could actually exceed variability in the
431 source (σ_P^2). These general principles of variance partitioning in the water cycle above may vary at different time
432 scales (e.g., monthly, daily), and we expect more details of the variability partitioning across various temporal
433 scales to be investigated in future studies.

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434
435 Our initial attempt to develop deeper understanding of variance partitioning was based on a series of case studies
436 located in extreme environments (wet/dry vs hot/cold vs high/low water storage capacity). The results offered
437 some further insights about hydrologic variability. For example, under extremely dry (water-limited)
438 environments, with limited storage capacity (S_{\max}) we found that E follows P and σ_E^2 follows σ_P^2 , with σ_Q^2 and $\sigma_{\Delta S}^2$
439 both approaching zero. However, as S_{\max} increases, the partitioning of σ_P^2 progressively shifts to a balance between
440 σ_E^2 , $\sigma_{\Delta S}^2$ and $\text{cov}(E, \Delta S)$ (Figs. 10-12). This result explains the overestimation of σ_E/σ_P by the empirical theory of
441 Koster and Suarez (1999) which implicitly assumed no inter-annual change in storage. The Koster and Suarez
442 empirical theory is perhaps better described as an upper limit that is based on minimal storage capacity, and that
443 any increase in storage capacity would promote the partitioning of σ_P^2 to $\sigma_{\Delta S}^2$ particularly under dry conditions
444 (Figs. 10-12).

445
446 In extremely wet/hot environments (i.e., no snow/ice presence) we found σ_P^2 to be mostly partitioned to σ_Q^2 (with
447 both σ_E^2 and $\sigma_{\Delta S}^2$ approaching zero, Fig. 10). In contrast, in extremely wet/cold environments, the partitioning of
448 σ_P^2 was highly (spatially) variable presumably because of spatial variability in the all-important thermal processes
449 (freeze/melt).

450
451 The most complex results were found in mesic biologically productive environments ($0.5 < \overline{E_o}/\overline{P} < 1.5$), where all
452 three covariance terms (Eq. 2) were found to be relatively large and therefore they all played critical roles in the
453 overall partitioning of variability (Fig. 6). As noted above, in many of these regions, the (absolute) magnitudes of
454 the covariances were actually larger than the variances of the water balance components E , Q and ΔS (e.g., Fig.
455 3). That result demonstrates that deeper understanding of the process-level interactions that are embedded within

458 each of the three covariance terms (e.g., the role of seasonal vegetation variation) will be needed to develop
459 process-based understanding of variability in the water cycle in these biologically productive regions ($0.5 < \overline{E_o} / \overline{P}$
460 < 1.5).

461

462 The syntheses of the long-term mean water cycle originated in 1970s (Budyko, 1974), and it took several decades
463 for those general principles to become widely adopted in the hydrologic community. The hydrologic data needed
464 to understand hydrologic variability are only now becoming available. With those data we can begin to develop a
465 process-based understanding of hydrologic variability that can be used for a variety of purposes, e.g., deeper
466 understanding of hydro-climatic behaviour, hydrologic risk analysis, climate change assessments and hydrologic
467 sensitivity studies are just a few applications that spring to mind. The initial results presented here show that a
468 major intellectual effort will be needed to develop a general understanding of hydrologic variability.

469

470

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478

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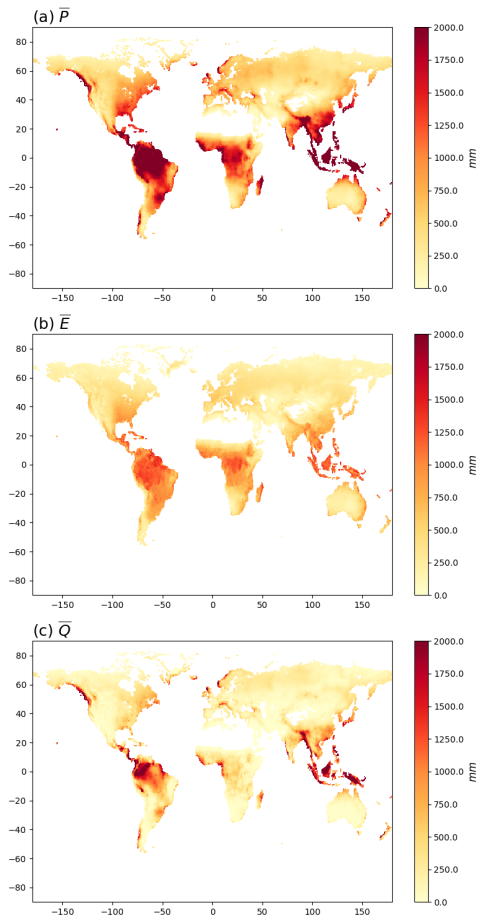
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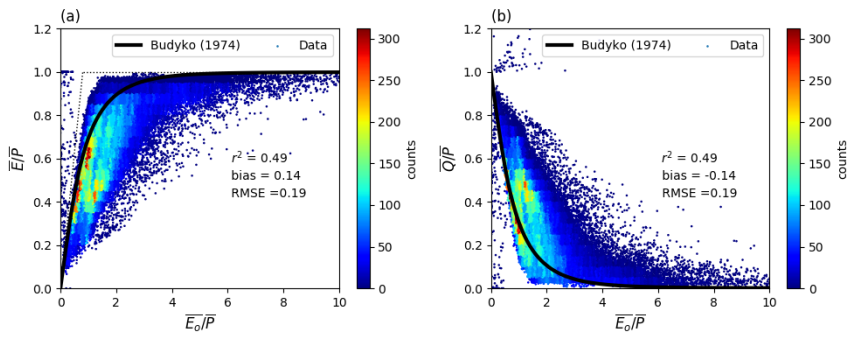
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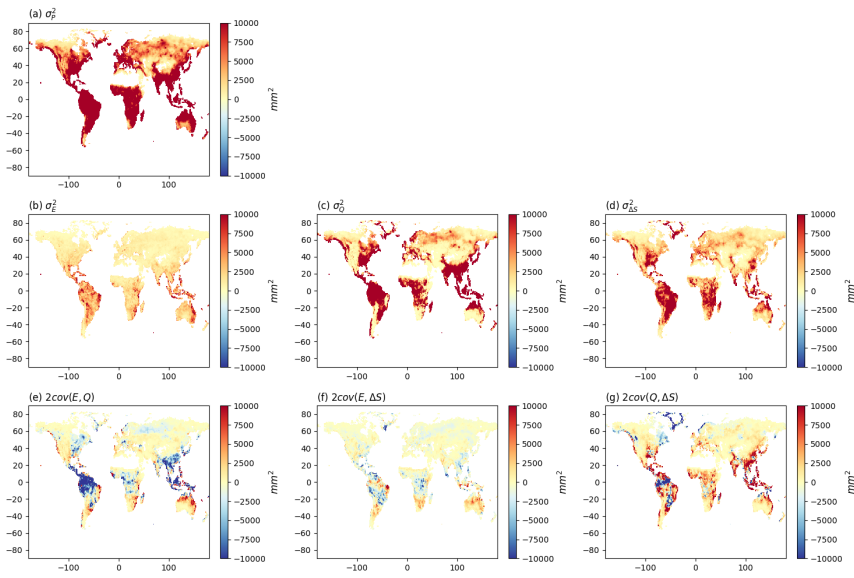
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622 2a). The curve on the right panel (Fig. 2b) is calculated assuming a steady state ($\overline{Q/P} = 1 - \overline{E/P}$).

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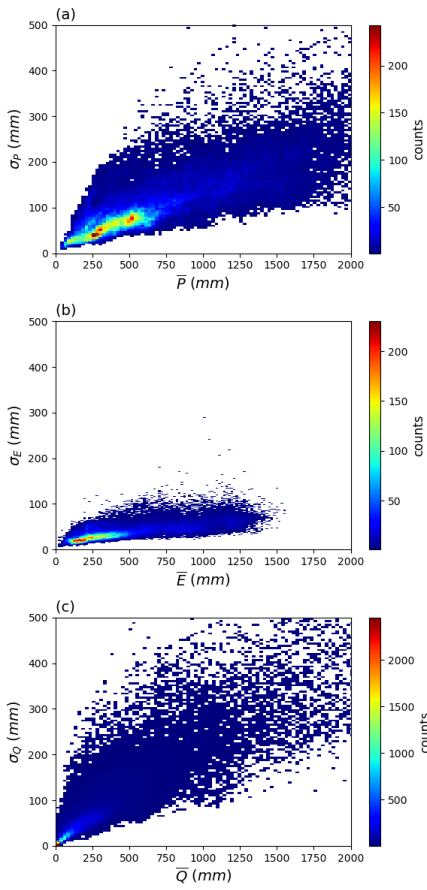


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627 have multiplied the covariances by two (see Eq. 2).

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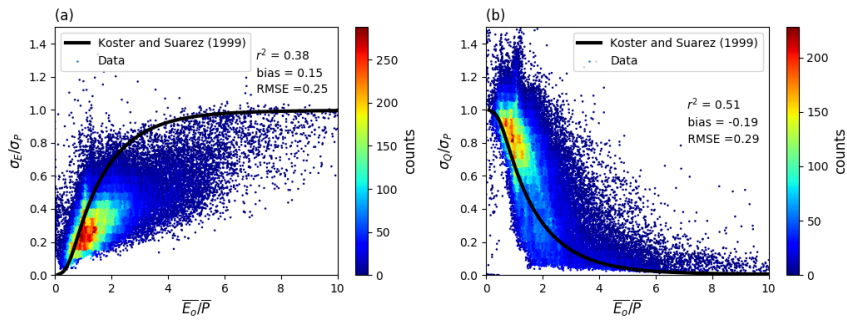
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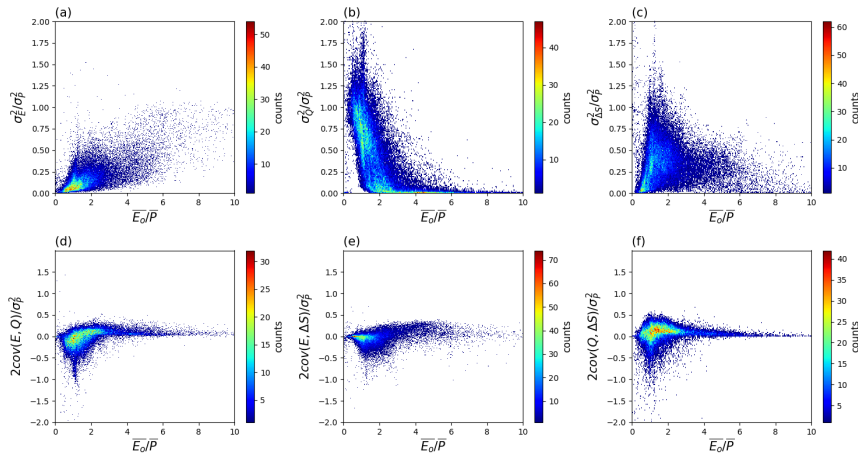
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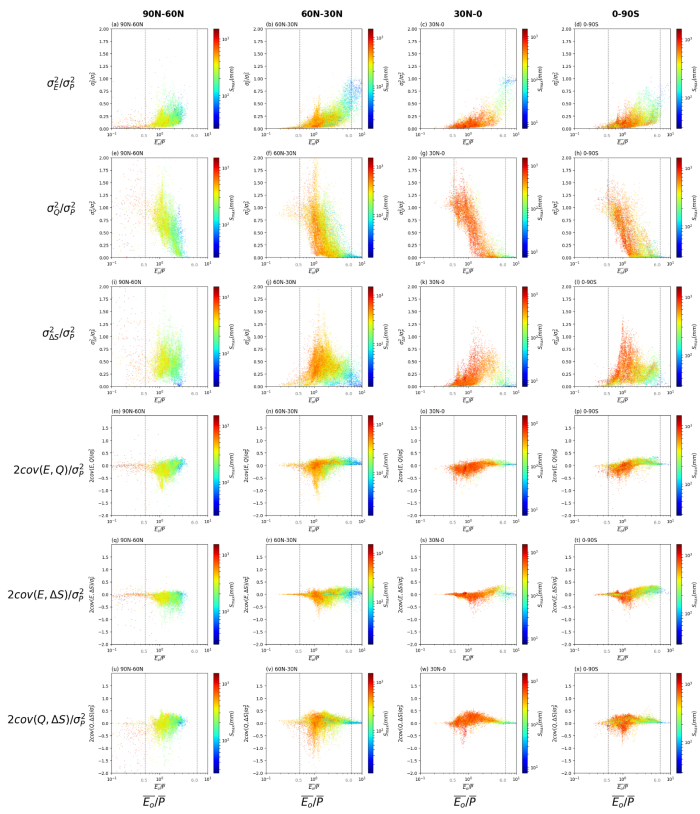
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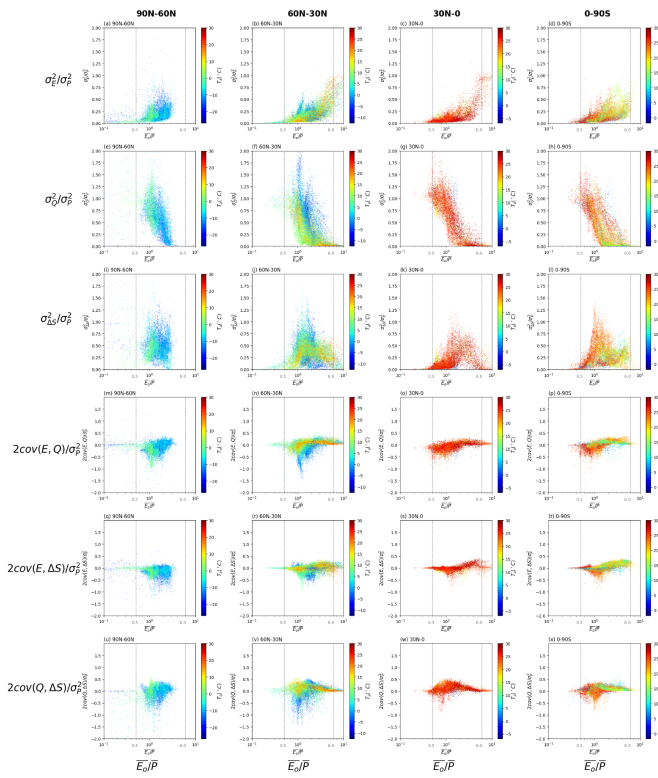
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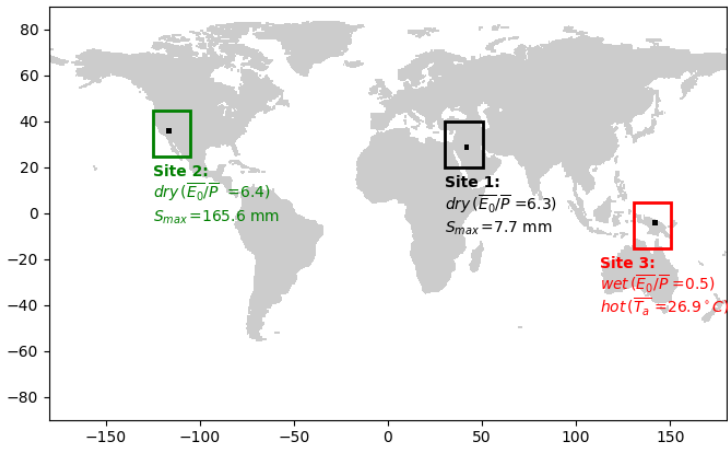
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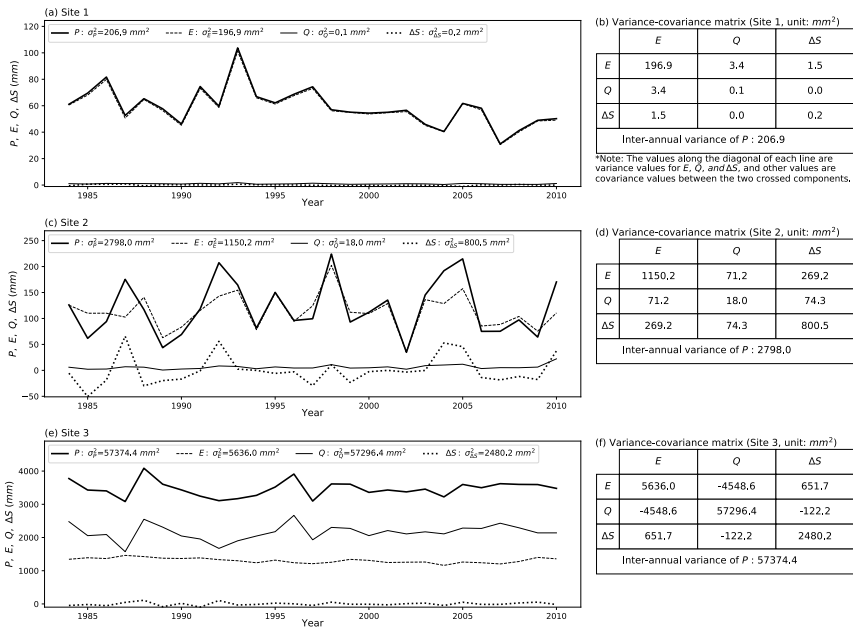
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664 Figure 9. Locations of three representative grid-cells used as case study sites.

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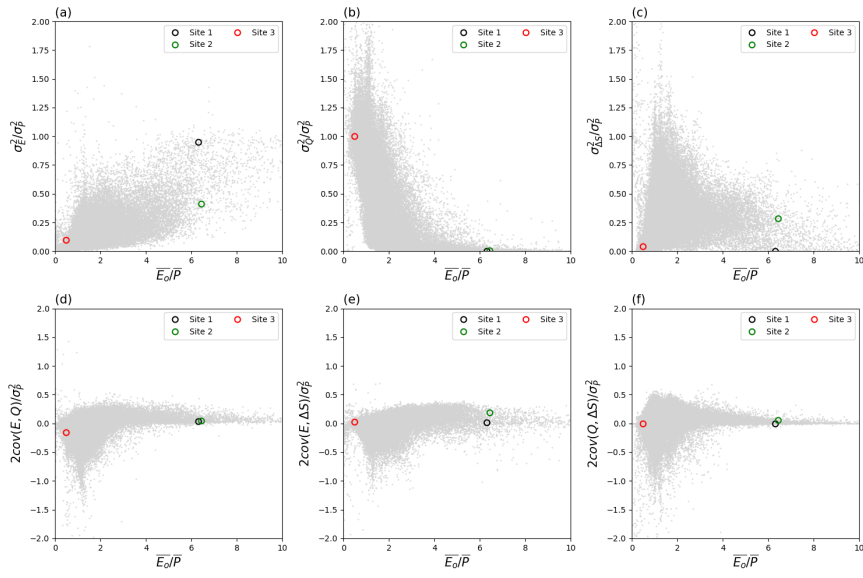


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668 **Figure 10. Inter-annual time series (P , E , Q and ΔS) and the associated variance-covariance matrix (E , Q and ΔS) for**
 669 **case study Sites 1-3. Left column shows time series for (a) Site 1, (c) Site 2 and (e) Site 3, with right column i.e., (b), (d)**
 670 **and (f), the associated variance-covariance matrix for three sites. Note that the covariance values in the tables should**
 671 **be multiplied by two to agree with the variance-covariance balance in Eq. (2).**

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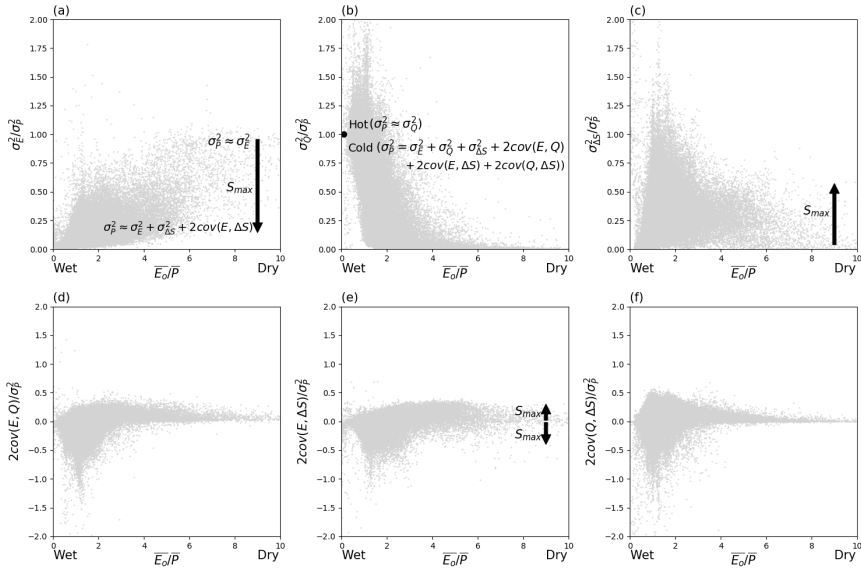
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675 **Figure 11. Location of three case study sites in the water cycle variability space. The grey background dots are from**

676 **Fig. 6.**

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680 **Figure 12. Synthesis of factors controlling variance partitioning. The arrows denote trends with increasing S_{max} . The**
 681 **grey background dots are from Fig. 6.**

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Inter-annual variability of the global terrestrial water cycle

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Supplementary Material

This Supplementary Material contains Figures S1-S14 and Table S1.

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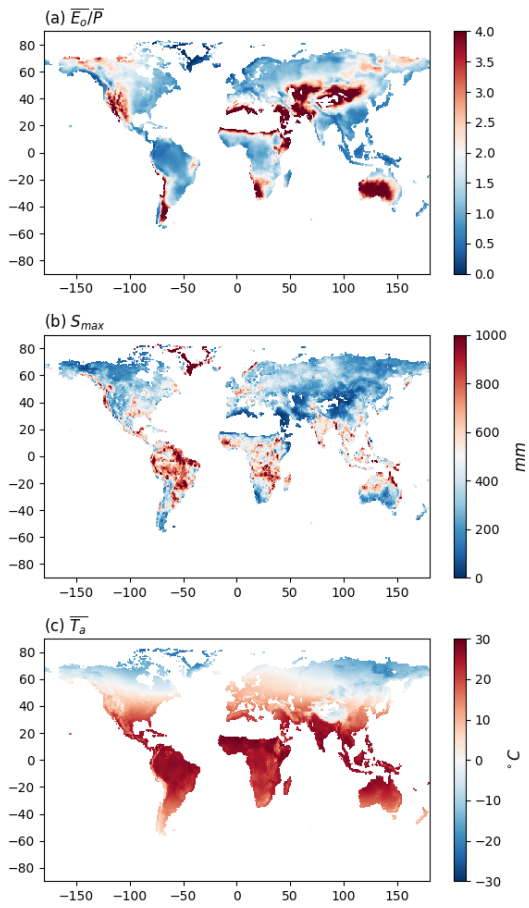


Figure S1. (a) Aridity index ($\overline{E_o/P}$), (b) water storage capacity (S_{max}) and (c) mean annual air temperature ($\overline{T_a}$) used in the analysis.

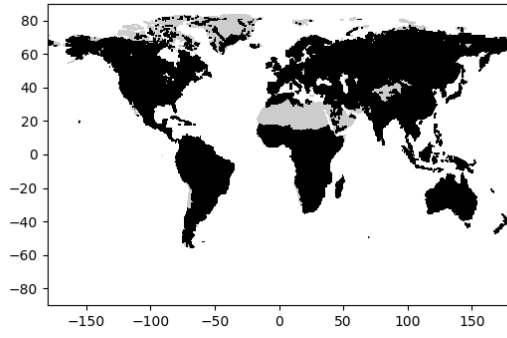


Figure S2. Spatial mask used in this study. Grey areas (e.g., Himalayan region, Sahara Desert, Greenland) have been masked out of the CDR database.

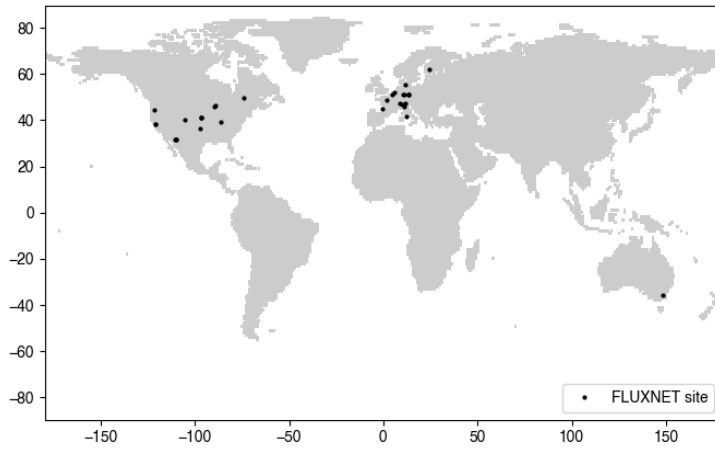


Figure S3. Location of the 32 FLUXNET sites used to evaluate the Climate Data Record (CDR).

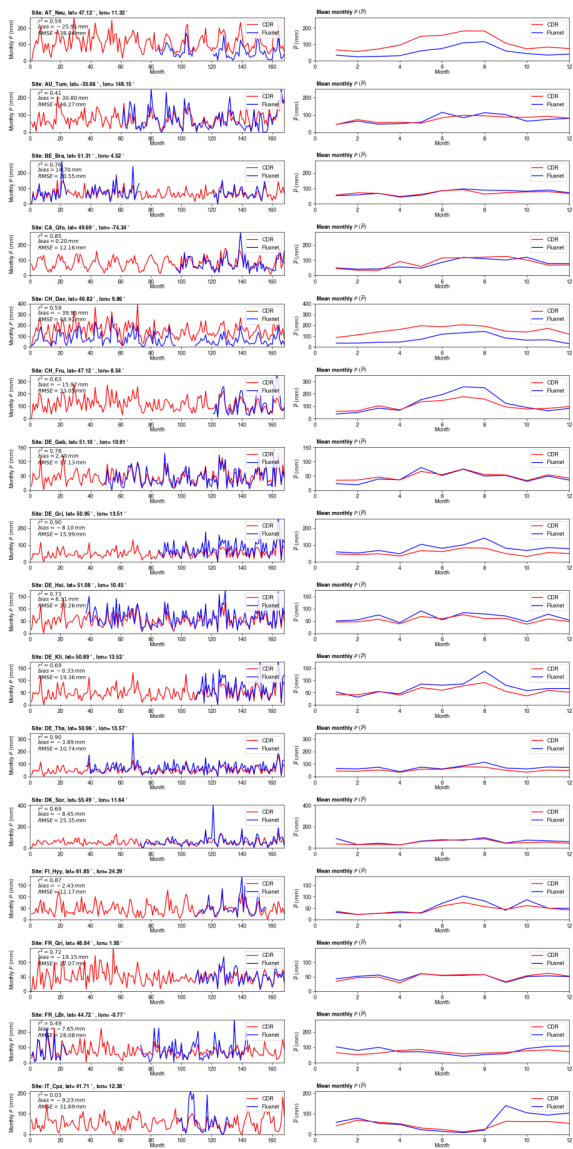


Figure S4. Comparison of monthly precipitation P time series (left panels) and mean monthly P (right panels) between FLUXNET observations at 32 sites (Table S1) and the Climate Data Record (CDR).

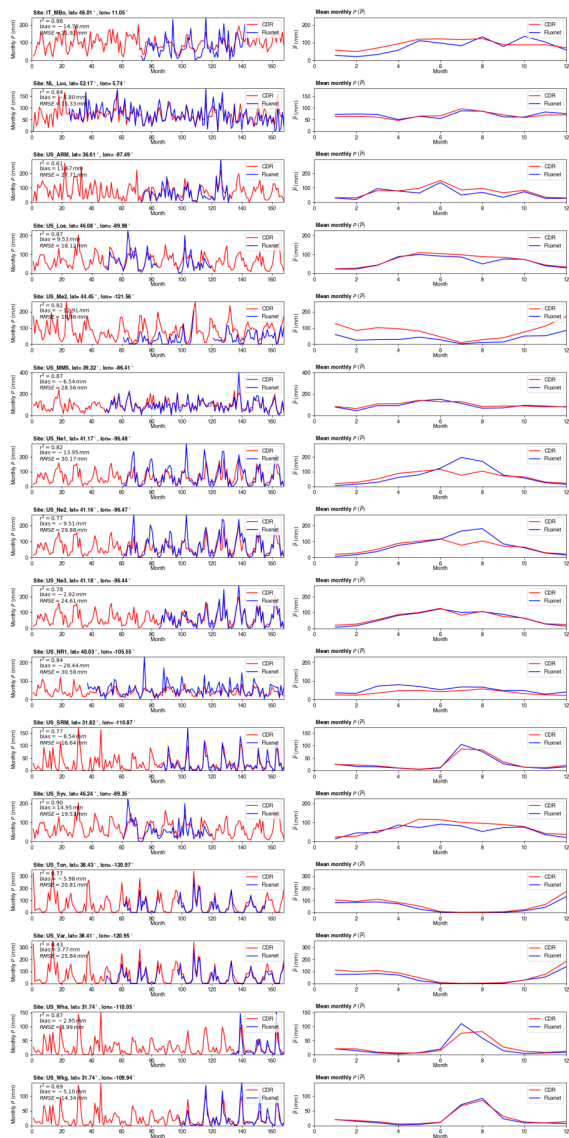


Figure S4 continued.

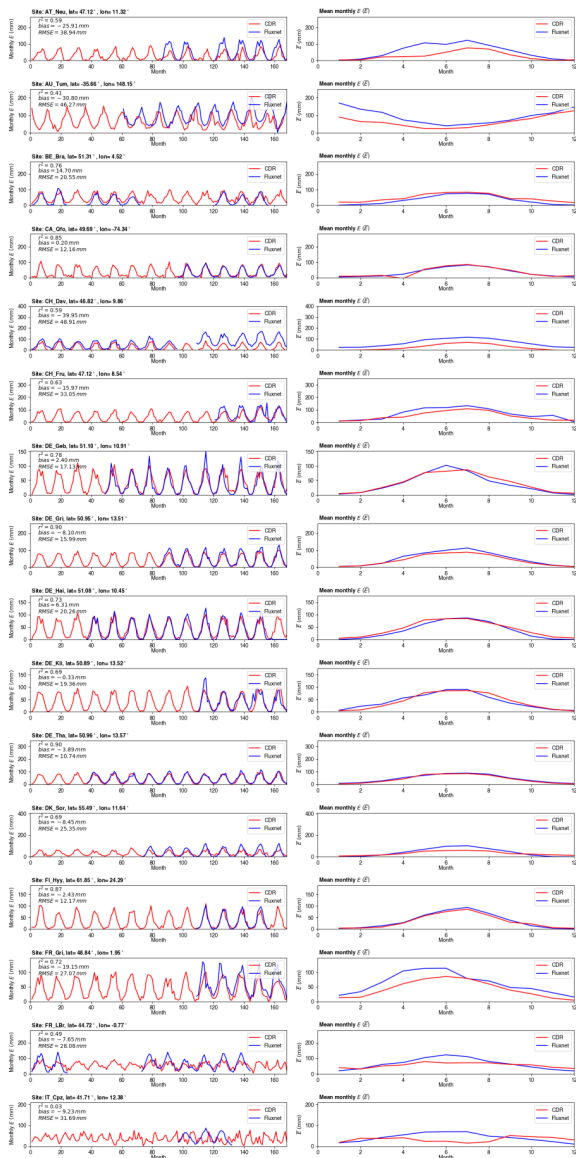


Figure S5. Comparison of monthly evapotranspiration E time series (left panels) and mean monthly E (right panels) between FLUXNET site observations and the Climate Data Record (CDR).

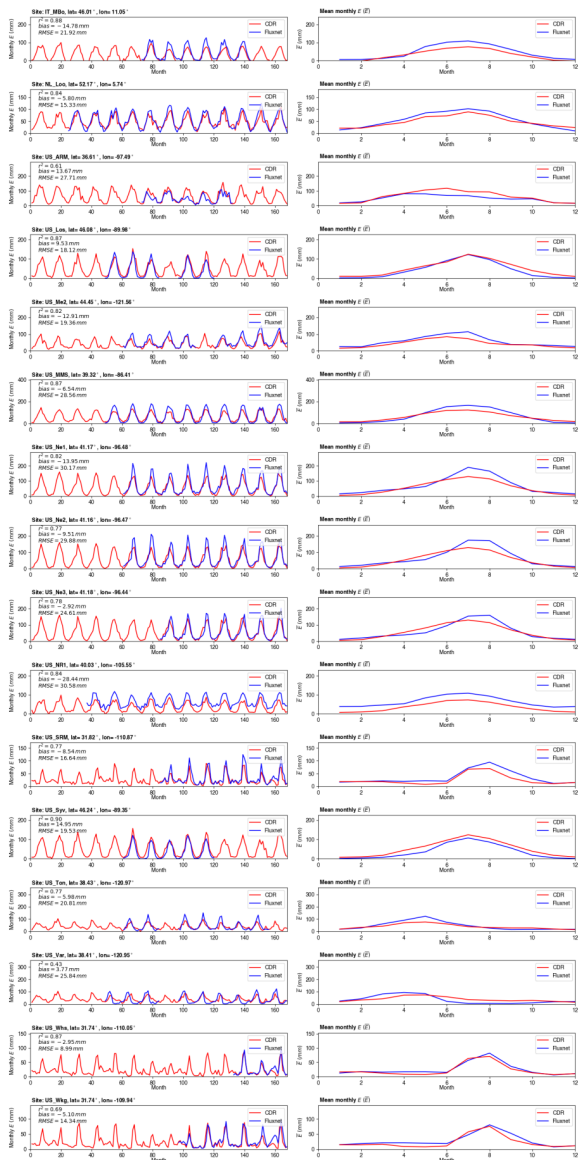


Figure S5 continued.

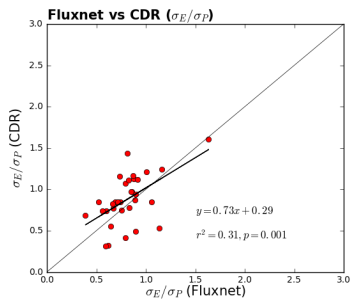


Figure S6. Comparison of ratio of standard deviation of monthly evapotranspiration E to precipitation P (σ_E/σ_P) between FLUXNET site observations and the Climate Data Record (CDR).

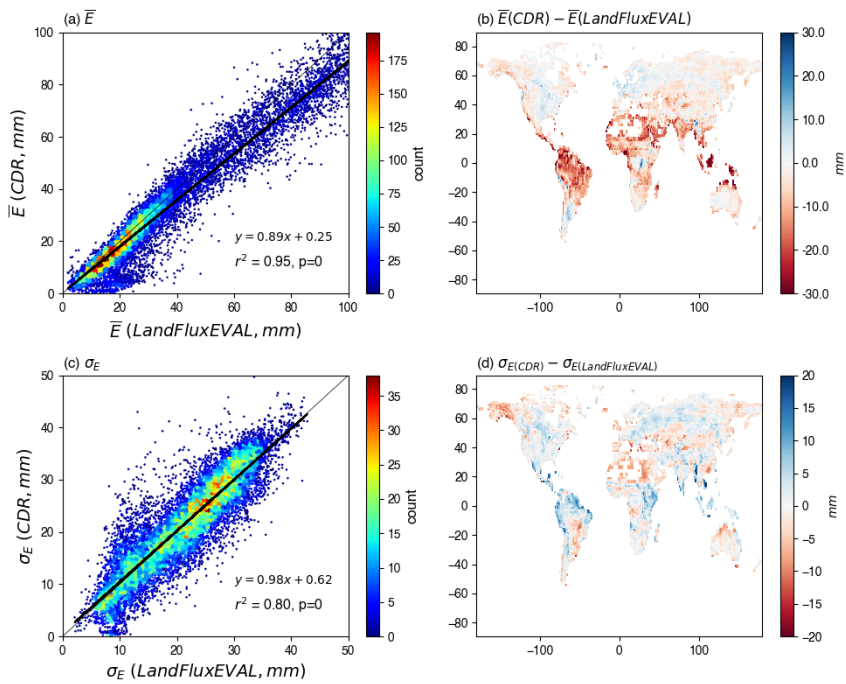


Figure S7. Comparison of monthly evapotranspiration E between LandFluxEVAL and Climate Data Record (CDR) databases. Top panels (a) (b) show comparison of the mean monthly (\bar{E}) while bottom panels (c) (d) show comparison of the standard deviation (σ_E) of monthly E .

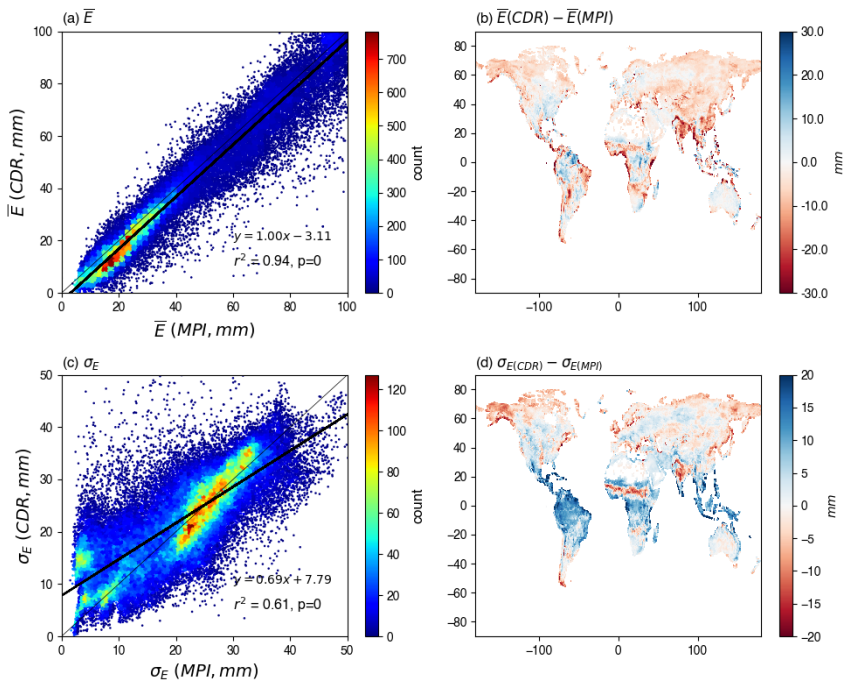


Figure S8. Comparison of monthly evapotranspiration E between Max Planck Institute (MPI) and Climate Data Record (CDR) databases. Top panels (a) (b) show comparison of the mean monthly (\bar{E}) while bottom panels (c) (d) show comparison of the standard deviation (σ_E) of monthly E .

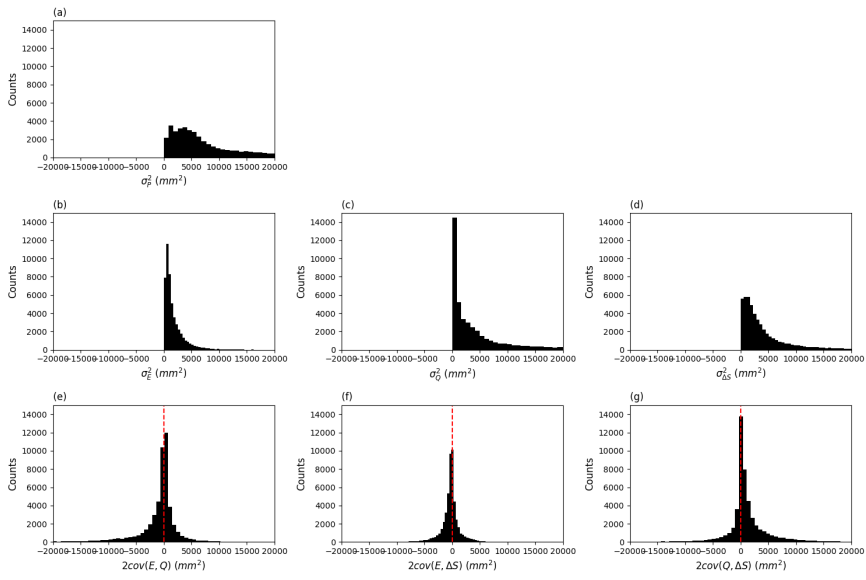
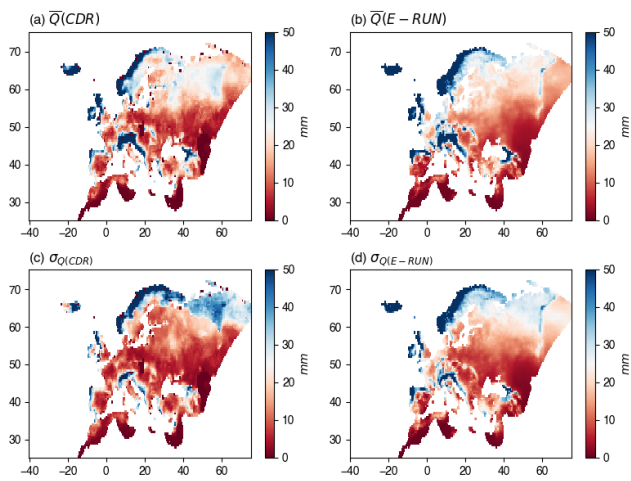
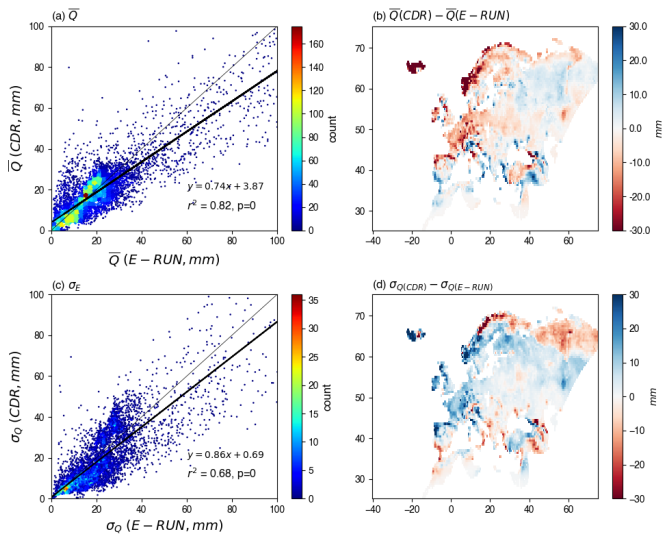


Figure S9. Distribution for each of the water cycle variances (σ_P^2 , σ_E^2 , σ_Q^2 , $\sigma_{\Delta S}^2$) and covariances ($cov(E, Q)$, $cov(E, \Delta S)$, $cov(Q, \Delta S)$) shown in Fig. 3. Note that we have multiplied the covariances by two (see Eq. 2).



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Figure S10. Mean (\bar{Q}) and standard deviation (σ_Q) of monthly runoff Q in the E-RUNOFF and Climate Data Record (CDR) databases in the area of spatial overlap (Europe). Top panels (a) (b) show the mean monthly (\bar{Q}) while bottom panels (c) (d) show the standard deviation (σ_Q) of monthly Q .



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Figure S11. Comparison of monthly runoff Q between the E-RUNOFF and Climate Data Record (CDR) databases in the area of spatial overlap (Europe). Top panels (a) (b) show comparison of the mean monthly (\bar{Q}) while bottom panels (c) (d) show comparison of the standard deviation (σ_Q) of monthly Q .

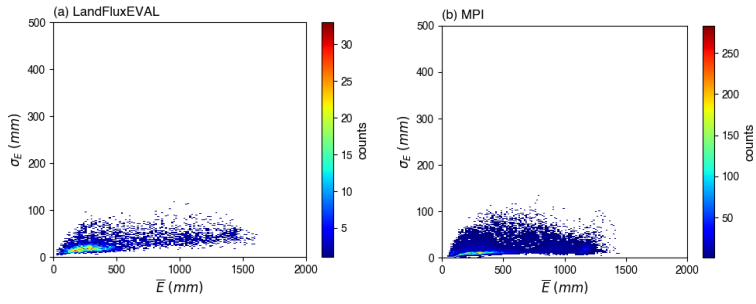


Figure S12. The same as Fig. 4b in main text but using evapotranspiration E data from the (a) LandFluxEVAL and (b) MPI databases.

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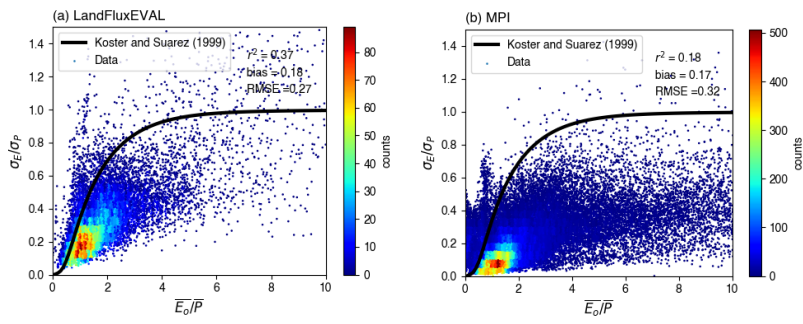


Figure S13. The same as Fig. 5a in main text but using evapotranspiration E data from the (a) LandFluxEVAL and (b) MPI databases.

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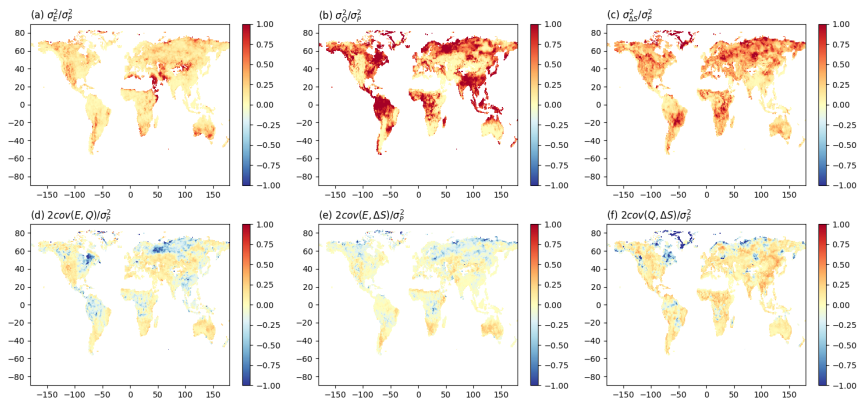


Figure S14. Inter-annual water cycle variances (σ_E^2 , σ_Q^2 , $\sigma_{\Delta S}^2$) and covariances ($cov(E, Q)$, $cov(E, \Delta S)$, $cov(Q, \Delta S)$) expressed as a fraction of the variance of P (σ_P^2). Note that we have multiplied the covariances by two (see Eq. 2).

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Table S1. Summary of comparisons of monthly precipitation P and evapotranspiration E between observations at 32 FLUXNET sites and the CDR database.

Site ID	Site Name	Lat	Lon	Ref	Data period	r^2 (P)	bias (P , mm)	RMSE (P , mm)	r^2 (E)	bias (E , mm)	RMSE (E , mm)
AT_Neu	Neustift	47.1167	11.3175	Wohlfahrt et al., 2008	2004 - 2005, 2007 - 2010	0.64	53.54	61.53	0.59	-25.91	38.94
AU_Tum	Tumbarumba	-35.6566	148.1517	Leuning et al., 2005	2002 - 2010	0.56	1.08	39.34	0.41	-30.80	46.27
BE_Bra	Brasschaat	51.3076	4.5198	Carrara et al., 2004	1997 - 1998, 2000 -2002, 2007 - 2009	0.64	-3.05	26.66	0.76	14.70	20.55
CA_Qfo	Quebec - Eastern Boreal, Mature Black Spruce	49.6925	-74.3421	Bergeron et al., 2006	2005 - 2010	0.57	4.43	31.77	0.85	0.20	12.16
CH_Dav	Davos	46.8153	9.8559	Zielis et al., 2014	1997 - 2004, 2006 - 2010	0.64	82.53	91.39	0.59	-39.95	48.91
CH_Fru	Früebüel	47.1158	8.5378	Imer et al., 2013	2007 - 2010	0.65	-15.42	55.86	0.63	-15.97	33.05
DE_Geb	Gebesee	51.1001	10.9143	Anthoni et al., 2004	2001 - 2010	0.69	3.78	17.69	0.78	2.40	17.13
DE_Gri	Grillenburg	50.9500	13.5126	Prescher et al., 2010	2004 - 2010	0.70	-26.32	37.67	0.90	-8.10	15.99
DE_Hai	Hainich	51.0792	10.4530	Knohl et al., 2003	2000 - 2012	0.70	-10.35	23.17	0.73	6.31	20.26
DE_Kli	Klingenberg	50.8931	13.5224	Prescher et al., 2010	2006 - 2010	0.68	-13.61	28.05	0.69	-0.33	19.36
DE_Tha	Tharandt	50.9624	13.5652	Grünwald and Bernhofer, 2007	2000 - 2010	0.66	-18.71	32.35	0.90	-3.89	10.74
DK_Sor	Soroe	55.4859	11.6446	Pilegaard et al., 2011	2003 - 2010	0.45	-11.07	39.31	0.69	-8.45	25.35
FI_Hyy	Hyytiala	61.8474	24.2948	Suni et al., 2003	2006 - 2009	0.78	-7.07	20.43	0.87	-2.43	12.17
FR_Gri	Grignon	48.8442	1.9519	Loubet et al., 2011	2006 - 2010	0.69	-0.81	12.35	0.72	-19.15	27.07
FR_LBr	Le Bray	44.7171	-0.7693	Berbigier et al., 2001	1997 -1998, 2003 - 2008	0.56	-9.19	39.93	0.49	-7.65	28.08
IT_Cpz	Castelporziano	41.7053	12.3761	Garbulsky et al., 2008	2005 - 2007	0.76	-15.90	40.42	0.03	-9.23	31.69

IT_MB0	Monte Bondone	46.0147	11.0458	Marcolla et al., 2011	2003 - 2008	0.36	12.43	48.14	0.88	-14.78	21.92
NL_Loo	Loobos	52.1666	5.7436	Moors 2012	1999 - 2010	0.56	-2.16	24.78	0.84	-5.80	15.33
US_ARM	ARM Southern Great Plains site-Lamont	36.6058	-97.4888	Baldocchi and Sturtevant 2015	2003 - 2007	0.71	13.53	31.78	0.61	13.67	27.71
US_Los	Lost Creek	46.0827	-89.9792	Baker et al., 2003	2001 - 2003, 2005 - 2006	0.52	7.76	32.82	0.87	9.53	18.12
US_Me2	Metolius mature ponderosa pine	44.4523	-121.5574	Law (2002-2014)	2002 - 2005, 2007 - 2010	0.54	45.31	56.84	0.82	-12.91	19.36
US_MMS	Morgan Monroe State Forest	39.3232	-86.4131	Novick and Phillips (1999-2014)	2001 - 2010	0.72	6.60	31.44	0.87	-6.54	28.56
US_Ne1	Mead - irrigated continuous maize site	41.1651	-96.4766	Suyker (2001-2013a)	2002 - 2010	0.45	-6.64	51.86	0.82	-13.95	30.17
US_Ne2	Mead - irrigated maize-soybean rotation site	41.1649	-96.4701	Suyker (2001-2013b)	2002 - 2010	0.56	-8.77	46.45	0.77	-9.51	29.88
US_Ne3	Mead - rainfed maize-soybean rotation site	41.1797	-96.4397	Suyker (2001-2013c)	2004 - 2010	0.88	2.28	21.43	0.78	-2.92	24.61
US_NR1	Niwot Ridge Forest (LTER NWT1)	40.0329	-105.5464	Blanken (1998-2014)	2000 - 2010	0.51	-16.06	29.57	0.84	-28.44	30.58
US_SRM	Santa Rita Mesquite	31.8214	-110.8661	Barron-Gafford et al., 2011	2004 - 2010	0.81	1.34	15.40	0.77	-8.54	16.64
US_Syv	Sylvania Wilderness Area	46.2420	-89.3477	Desai et al., 2008	2002 - 2006	0.33	13.17	40.68	0.90	14.95	19.53
US_Ton	Tonzi Ranch	38.4316	-120.9660	Baldocchi et al., 2010	2002 - 2003, 2005 - 2009	0.89	14.68	27.44	0.77	-5.98	20.81

US_Var	Vaira Ranch- Ione	38.4133	-120.9507	Baldocchi et al., 2004	2001 - 2003, 2005 - 2010	0.86	16.91	30.92	0.43	3.77	25.84
US_Whs	Walnut Gulch Lucky Hills Shrub	31.7438	-110.0522	Biederman et al., 2016	2008 - 2010	0.65	1.89	21.26	0.87	-2.95	8.99
US_Wkg	Walnut Gulch Kendall Grasslands	31.7365	-109.9419	Biederman et al., 2016	2005 - 2010	0.78	1.59	15.66	0.69	-5.10	14.34

* Significant r^2 values (linear regression $p < 0.05$) are shown in bold.

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