

1 **“The Probability Distribution of Daily Precipitation at the Point and**
2 **Catchment Scales in the United States” by Lei Ye et al.**

3 **Response to Simon M. Papalexiou (Referee #1)**
4

5 We greatly appreciate you for your constructive comments and suggestions. Our
6 responses to the comments are listed below.
7

8 **Comment 1: It only makes sense to advance a single continuous pdf for the wet**
9 **day case, regardless of where the data arises from, if one adds zeros, the**
10 **Lmoments will always land exactly on the Pearson Type III curve**

11 Response:

12 Thank you for pointing this out. In the revised manuscript, we will eliminate all the
13 results relating to the ‘all day’ or $X \geq 0$ conditions, focusing only on the probability
14 distribution of wet-day precipitation.
15

16 **Comment 2: Lines 363-365: “demonstrating that the parameter Gamma**
17 **distribution cannot describe the tail behavior of full-record series of**
18 **precipitation as has often been assumed in the past.” These lines are just the**
19 **opportunity for commenting on tail issues. Summary shape statistics are of**
20 **course affected by the tail behaviour but they are not sufficient to reveal in a**
21 **robust way the behaviour of the tail if the whole sample is used (I mean all**
22 **nonzero values) and not values that belong to the tail. For example in the**
23 **paper the authors cite (Papalexiou and Koutsoyiannis, 2016) after the fitting**
24 **using L-moments various measures were proposed in order to compare the**
25 **fitting in the most extreme value, the largest extremes the whole sample etc.**
26 **The author can see that the performance of distributions changed, still the**
27 **GG performed better but the BrXII increased its performance too. I just want**
28 **to say that indeed this approach can favour specific distributions and exclude**
29 **others like the G2 the authors mention, yet this is based judging the whole**

30 **distributional shape properties and it is not really robust to judge on the tail**
31 **when using the whole nonzero sample. Also other global studies indicated the**
32 **sub exponential nature of tails focusing on using only “tail” data (Papalexiou**
33 **et al., 2013; Serinaldi and Kilsby, 2014); the latter was also applied in a**
34 **seasonal basis, which by the way might be also a nice idea, i.e., the authors to**
35 **explore seasonal variation.**

36 *Response:*

37 Thank you for the comments. The sentence will be removed in the revised manuscript
38 since our analysis of the full-record series of precipitation will be eliminated. The
39 reviewer has suggested a good idea to explore the seasonal variation of the distribution
40 of daily rainfall, which will be a portion of our future work. We will consider ideas
41 introduced by Papalexiou and Koutsoyiannis (2016) and others concerning the impact
42 of seasons on rainfall distributions. We are aware that the choice of a suitable
43 distribution for modeling rainfall would be quite different if we were to focus our
44 attention on the extreme tail behavior, as is the case for example, when one fits a
45 distribution to the series of annual maxima or peaks above some threshold. However
46 given our interest in all wet-day daily precipitation, most situations of practical
47 relevance and concern are not with extreme rainfall, thus our attention will focus on the
48 complete series of wet-day amounts, without special attention given to the largest
49 values.

50
51 **Comment 3: The P3 distribution is just the two-parameter Gamma distribution**
52 **(G2) with an additional location parameter which does not affect the shape**
53 **characteristics and thus $\tau\tau_3$ and $\tau\tau_4$. So the curve of P3 shown in $\tau_4-\tau\tau_3$ ratio**
54 **plots is the same as the G2. And obviously they have the same tail. The same**
55 **holds for GPA and GP2 and for any other distribution that has one shape**
56 **parameter and additional location parameters are added. Maybe to ease the**
57 **reader, as different formulations can be found in the literature, it would be no**
58 **harm to add a table of the distributions functions used.**

59 Response:

60 Thank you. We will add a table to show the distribution functions. We appreciate the
61 comments of the reviewer reminding us of the fact that addition of a location parameter
62 does not impact the shape of the distribution.

63

64 **Comment 4: The Weibull distribution could also be added in the analysis as a
65 representative of distributions with stretched exponential tails.**

66 Response:

67 Thanks. We will add the analysis of Weibull distribution in the revision. Again, we
68 emphasize that our interest is in the entire distribution, without focusing attention on
69 the extreme tail behavior. We leave it to others to evaluate the distribution of annual
70 maximum precipitation to focus attention on extreme tail behavior of daily rainfall
71 amounts.

72

73 **Comment 5: When we use distributions with a location parameter to describe a
74 positive variable like the nonzero precipitation this parameter might end far
75 from zero or even negative indicating a lower bound. So, this distribution
76 cannot be used in stochastic modelling of precipitation as it will result in
77 inconsistent values. It would be interesting the authors to actually show some
78 box plots of the estimated parameters.**

79 Response:

80 We indeed found that some parameters are far from zero too. Box plots will be added
81 to illustrate the behavior of the distribution parameters of interest.

82

83 **Comment 6: The principle of parsimony should always be applied. If the authors,
84 generate samples from a 4-parameter distribution like the kappa and try to
85 estimate a posteriori the parameters, even for the sample sizes used here, they
86 will find a huge variability that makes, in my opinion, the operational use of
87 4-parameter distributions quite risky. Of course a 4-parameter distribution
88 like the kappa has a great flexibility, yet this does imply that a better fitting**

89 **to an observed sample is a better choice to extrapolate values for large return**
90 **periods.**

91 Response:

92 We fully agree that in most applications in hydrology, the principle of parsimony is
93 absolutely paramount, due to the short samples available for fitting distributions.
94 However, in this application, with samples sizes in the tens of thousands, concerns over
95 parsimony are not nearly as critical, even when estimating the Kappa distribution. This
96 fact has been shown nicely in the recent paper by Blum et al (2017) where they
97 demonstrated, for similarly length samples of daily streamflow the sampling properties
98 of estimated Lmoments from synthetic samples in their Figure 2.

99

100 **Comment 7: The authors, since this is the first large scale study on catchment**
101 **precipitation, could provide some analysis on the relation of catchment size**
102 **and distributional shape. As the spatial averaging process will tend to make**
103 **the distributions more bell-shaped and with thinner tails. This is the**
104 **explanation of the performance decrease of the heavy-tailed distribution**
105 **shown in Fig. 7 compared to Fig. 6 (commenting on the Wet-day; full-day**
106 **results should be modified).**

107 Response:

108 Thank you for your suggestion. In the revised manuscript, we will explore the relation
109 of catchment size and distribution shape. Of interest is the impact of catchment size on
110 both the LSkewness and LKurtosis of the fitted distributions of wet-day precipitation
111 amounts.

112

113 **Comment 8: Some regions of the USA, mainly in Midwest, show quite intense**
114 **changes (or maybe natural variability) on extremes. The authors could also**
115 **comment on that or do a quick extra analysis on the daily precipitation.**

116 Response:

117 Thank you. We will explore/comment on the changes of extremes in Midwest if
118 possible, but again, we remind the reviewer, that our attention is not on the behavior of

119 extreme precipitation, but rather, is on the distribution of the complete series of wet day
120 daily amounts under all conditions, not just extreme conditions.

121

122 **Comment 9: I believe the literature should be updated with many other works, e.g.,**
123 **there are several papers that are using other distributions for daily**
124 **precipitation, e.g., one that came to mind is the by Wilson and Toumi (2005).**

125 *Response:*

126 Thank you. We will update the literature review with a focus on the distribution of wet-
127 day precipitation amounts.