

Seasonal behaviour of tidal damping and residual water level slope in the Yangtze River estuary: identifying the critical position and river discharge for maximum tidal damping

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Abstract. As a tide propagates into the estuary, river discharge affects tidal damping primarily through a friction term, attenuating tidal motion by increasing the quadratic velocity in the numerator, while reducing the effective friction by increasing the water depth in the denominator. For the first time, we also demonstrate a third effect of river discharge that may lead to the weakening of the channel convergence (i.e., landward reduction of channel width and/or depth). In this study, monthly averaged tidal water levels (2003-2014) at six gauging stations along the Yangtze River estuary were used to understand the seasonal behaviour of tidal damping and residual water level slope. Observations show that there is a critical value of river discharge, beyond which the tidal damping is reduced with increasing river discharge. This phenomenon is clearly observed in the upstream part of the Yangtze River estuary (between the Maanshan and Wuhu reach), which suggests an important cumulative effect of residual water level on tide-river dynamics. To understand the underlying mechanism, an analytical model has been used to quantify the seasonal behaviour of tide-river dynamics and the corresponding residual water level slope under various external forcing conditions. It was shown that a critical position along the estuary is where there is maximum tidal damping (approximately corresponding to a maximum residual water level slope), upstream of which tidal damping is reduced in the landward direction. Moreover, contrary to the common assumption that larger river discharge leads to heavier damping, we demonstrate that beyond a critical value tidal damping is slightly reduced with increasing river discharge, owing to the cumulative effect of resid-

ual water level on the effective friction and channel convergence. Our contribution describes the
20 seasonal patterns of tide-river dynamics in detail, which will, hopefully, enhance our understanding
of the nonlinear tide-river interplay and guide effective and sustainable water management in the
Yangtze River estuary and other estuaries with substantial freshwater discharge.

1 Introduction

Tide-river interactions and resulting residual water level profiles play a crucial role in large-scale
25 river deltas (e.g., the Mississippi River delta in the United States, the Rhine-Meuse delta in the
Netherlands, the Pearl River delta and the Yangtze River delta in China, the Ganges-Brahmaputra
delta in Bangladesh, etc.) because tide-river dynamics exert a tremendous impact on delta mor-
phodynamics, salt intrusion, and deltaic ecosystems (Hoitink and Jay, 2016; Hoitink et al., 2017;
Zhou et al., 2017). However, it is only in recent years that substantial effort has been devoted to
30 the nonlinear interaction between tidal waves and riverine flow in estuaries (e.g., Kukulka and Jay,
2003a; Buschman et al., 2009; Lamb et al., 2012; Sassi and Hoitink, 2013; Guo et al., 2014, 2015,
2016; Cai et al., 2014a,b, 2016, 2018; Leonardi et al., 2015; Zhou et al., 2018). Hence, many aspects
of tide-river interactions (e.g., seasonal behaviour of tidal damping and residual water level slope)
deserve further exploration.

35 The impact of river discharge on tidal wave propagation, especially on tidal damping, in estuaries
has long been the subject of intensive scientific interest (e.g., Dronkers, 1964; LeBlond, 1979; Godin,
1985, 1999; Jay, 1991; Horrevoets et al., 2004; Kukulka and Jay, 2003b; Cai et al., 2012b, 2014b,
2016; Guo et al., 2015; Leonardi et al., 2015; Alebregtse and de Swart, 2016; Zhang et al., 2018a).
It is worth noting that traditional methods for analysing tidal signals (e.g., harmonic and Fourier
40 analysis) are restricted due to the assumption of stationary signals. To correctly understand tidal
wave behaviour under the influence of river discharge, non-stationary tidal harmonic analysis has
been developed to better account for the nonlinear tide-river interactions (e.g., Jay and Flinchem,
1997, 1999; Kukulka and Jay, 2003a; Jay et al., 2011, 2015; Matte et al., 2013, 2014). Generally, it
was shown that river discharge tends to attenuate tidal energy and hence to enhance tidal damping
45 primarily through bottom friction (e.g., Godin, 1985, 1999; Guo et al., 2015). Recently, building on
a variety of previous studies on tidal damping (e.g., Horrevoets et al., 2004; Savenije et al., 2008;
Cai et al., 2012b,a; Savenije, 2012), Cai et al. (2014b, 2016) proposed an analytical hydrodynamic
model to investigate the underlying mechanism of tide-river interaction by means of an envelope
method, where an analytical expression for tidal damping can be obtained by subtracting high water
50 and low water envelopes. It is important to note that the river discharge impacts tidal damping
primarily via the friction term in the momentum equation: on the one hand, attenuating the tidal
motion via increasing the quadratic velocity in the numerator; and on the other hand, reducing the
effective friction by increasing the residual water level (hence water depth) in the denominator. This

effect is well illustrated in extreme cases where dredging along the upper estuary has significantly
55 increased the mean water depth resulting in strong tidal amplification for a given discharge (e.g., Jay
et al., 2011). However, little effort has been devoted to exploring the effect of river discharge on
channel convergence (represented by the gradient of cross-sectional area), which is the other control
factor for tide-river dynamics (e.g., Matte et al., 2018, 2019). In particular, the river discharge
affects the channel convergence primarily through residual water level and hence water depth and
60 cross-sectional area (Cai et al., 2014b, 2016).

Although the important role played by the residual water level on estuarine hydrodynamics was
recognized for some time (e.g., LeBlond, 1979; Godin and Martinez, 1994), only a few studies
explored the effects of a dynamic residual water level slope on tide-river dynamics (e.g., Buschman
et al., 2009; Sassi and Hoitink, 2013; Cai et al., 2014b, 2016). It is well-known that the steady
65 gradient of residual water level is mainly induced by a residual frictional effect (e.g., Cai et al.,
2014b, 2016), a density effect (e.g., Savenije, 2005, 2012) and nonlinear advective acceleration.
However, it should be noted that the effects of density and advective acceleration are generally
minor when compared with the frictional effect (this is detailed more in section 3.1). In addition,
the nonlinear tide-river interactions can be linearized by decomposing the friction term into different
70 components contributed by tidal forcing, river flow, and tide-river interaction alone (e.g., Buschman
et al., 2009; Sassi and Hoitink, 2013; Cai et al., 2016). This was made by using the Chebyshev
polynomials approach to approximate the quadratic velocity in the friction term (Dronkers, 1964;
Godin, 1991, 1999). In general, in the tide-dominated reach the residual water level is primarily
determined by tide–river interaction, whereas it is mainly controlled by the river flow alone in the
75 river-dominated reach (Cai et al., 2016).

The tide-river dynamics in the Yangtze River estuary, located on the east coast of China, have
received increasing attention in recent years owing to intensive climate change and human inter-
ventions (e.g., Three Gorges Dam construction, Deep Waterway Project) on both riverine and ma-
rine processes (e.g., Cai et al., 2014b,a, 2016; Guo et al., 2015; Zhang et al., 2015a,b; Alebregtse
80 and de Swart, 2016; Kuang et al., 2017; Shi et al., 2018; Zhang et al., 2018a). Traditionally, a
time-series analysis method (such as harmonic analysis in a non-stationary mode and continuous
wavelet transforms) was adopted to identify the non-stationary tide-river behaviour along the estu-
ary axis based on observed data or results from numerical models, such that the impacts of river
discharge on different tidal constituents can be quantified separately (e.g., Guo et al., 2015; Zhang
85 et al., 2015a,b; Shi et al., 2018; Zhang et al., 2018a). Although the tide-river dynamics in terms
of elevation and velocity fields can be accurately simulated using fully nonlinear numerical models
(e.g., Zhang et al., 2015a,b, 2018a), the cause–effect relations (e.g., the impact of river discharge on
tidal damping) cannot be explicitly identified by single realizations of numerical runs. To this aim,
analytical models are valuable instruments that can provide a straightforward insight. Additionally,
90 analytical models only need a minimum amount of data, and can explicitly provide estimates of

integral quantities (e.g. tidal amplitude, velocity amplitude, wave celerity and phase lag), while numerical models need to reconstruct them from temporal and spatial time series. Recently, idealized (or analytical) models with a strongly simplified geometry and flow characteristics were applied to the Yangtze River estuary in order to reproduce the first-order features of tide-river dynamics (e.g.,
95 Cai et al., 2014b,a, 2016; Alebregtse and de Swart, 2016). It is important to note that the idealized model proposed by Alebregtse and de Swart (2016) adopted a uniform depth for each channel, thus neglecting the residual water level caused by the strong tide-river interaction. As a result, their model is only applicable to the lower region of the Yangtze River estuary, where the tide dominates the river flow. In contrast, the analytical model proposed by Cai et al. (2014b, 2016) accounting for
100 the effects of residual water level can reasonably reproduce the first-order tide-river dynamics (only considering a predominant tidal constituent, e.g., M_2) in the Yangtze River estuary for a wide range of tide and river discharge conditions. Although many studies have been undertaken to understand the tide-river interactions in the Yangtze River estuary, previous studies mainly focused on the tidal properties near the estuary mouth (e.g., Lu et al., 2015; Alebregtse and de Swart, 2016; Zhang et al.,
105 2017) and investigations of tide-river dynamics are limited for the whole estuary, especially in the transitional zone with strongly nonlinear tide-river interactions. In this study, we adopt the analytical model proposed by Cai et al. (2014b, 2016) to quantify the impacts of river discharge on the seasonal behaviour of tide-river dynamics (e.g., tidal damping) and residual water level slope.

The remainder of this paper is constructed as follows. An overview of the study area and datasets
110 used to study the seasonal behaviour of tidal damping and residual water level slope are described in section 2. Section 3 introduces the analytical hydrodynamic model for reproducing tide-river dynamics in estuaries. The main results illustrating the seasonal behaviour of tidal damping and residual water level slope are presented in section 4, after which a discussion is presented in section 5. Finally, some conclusions are drawn in section 6.

115 **2 Overview of the Yangtze River estuary**

2.1 Description of the study site

The Yangtze River estuary, located on the east coast of China, extends ~ 630 km from the Datong hydrological station (where the tidal limit is) to its mouth near the seaward end of the South Branch (Figure 1). Both tidal waves and river flow are the major sources of energy for the hydrodynamics
120 along the Yangtze River estuary. Specifically, the estuary is a meso-tidal type with a maximum and mean tidal range of 4.62 and 2.67 m near the estuary mouth, respectively. The tide has an irregular semidiurnal character with average flood and ebb duration of 5 and 7.5 hr, respectively (Zhang et al., 2012). According to the observed data in the Datong hydrological station (1950-2012), the annual mean river discharge is approximately $28,200 \text{ m}^3/\text{s}$ and the monthly average river
125 discharge reaches a maximum value of $49,500 \text{ m}^3/\text{s}$ in July and a minimum value of $11,300 \text{ m}^3/\text{s}$ in

January. Unlike previous studies focusing on the tidal hydrodynamics near the estuary mouth, here we mainly concentrate on the tide-river dynamics in the mainstream of the Yangtze River estuary, extending from Tianshenggang gauging station to the Datong hydrological station.

2.2 Datasets

130 Monthly averaged hydrological data (including tidal range and water level) from 6 tidal gauging stations (Tianshenggang: TSG; Jiangyin: JY, located 46 km upstream of TSG; Zhenjiang: ZJ, located 155 km upstream of TSG; Nanjing: NJ, located 236 km upstream of TSG; Maanshan: MAS, located 284 km upstream of TSG; Wuhu: WH, located 330 km upstream of TSG) along the Yangtze River estuary were collected from the Yangtze Hydrology Bureau of the People's Republic of China for 135 the period of 2003-2014. The tidal amplitude is defined as a half of the tidal range either during the flood or the ebb period and we determined the mean value by averaging the tidal amplitudes during flood and ebb periods. To correctly calculate the residual water level slope, measured water levels from the gauging stations have been corrected to the Huanghai 1985 datum of local mean sea level. Figure 2 illustrates the temporal variation of the monthly averaged tidal range H and residual water 140 level \bar{Z} observed at the 6 gauging stations together with the monthly averaged river discharge observed at the Datong (DT) hydrological station. In Figure 2, we observe a strongly seasonal variation in tidal range H (except for TSG and JY) and residual water level \bar{Z} due to the strongly fluctuating river discharge. For the residual water level, we also note that the more upstream the location of the station, the more evident the seasonal change is.

145 3 Analytical model for tide-river dynamics

3.1 Reproducing the residual water level profile in estuaries

The dynamics of residual water level can be derived from the one-dimensional momentum equation (e.g., Savenije, 2005, 2012):

$$\frac{\partial U}{\partial t} + U \frac{\partial U}{\partial x} + g \frac{\partial Z}{\partial x} + \frac{gh}{2\rho} \frac{\partial \rho}{\partial x} + g \frac{U|U|}{K^2 h^{4/3}} = 0, \quad (1)$$

150 where U is the cross-sectional averaged velocity, Z is free surface elevation, h is water depth, g is the acceleration of gravity, t is time, ρ is water density, x is the longitudinal coordinate directed landward, and K is the Manning-Strickler friction coefficient. Assuming a periodic variation of flow velocity, the integration of Equation (1) over a tidal cycle leads to an expression for the residual water level slope (e.g., Vignoli et al., 2003; Cai et al., 2014b, 2016):

$$155 \frac{\partial \bar{Z}}{\partial x} = -\frac{1}{K^2} \overline{\left(\frac{U|U|}{h^{4/3}} \right)} - \frac{1}{2g} \frac{\partial \bar{U}^2}{\partial x} - \frac{1}{2\rho_0} h \frac{\partial \bar{\rho}}{\partial x}, \quad (2)$$

where the over bars and the subscript 0 indicate the tidal average and the value at the seaward boundary, respectively. As shown in Equation (2) the residual water level slope is caused by three contributions made by residual friction, advective acceleration and density effects that correspond to the three terms on the right-hand side of Equation (2). Note that the contribution from advective acceleration to the residual water level slope:

$$\frac{\partial \bar{Z}_{adv}}{\partial x} = -\frac{1}{2g} \frac{\partial \bar{U}^2}{\partial x}, \quad (3)$$

can be easily integrated to:

$$\bar{Z}_{adv} = -\frac{1}{2g} (\bar{U}^2 - \bar{U}_0^2) = -\frac{1}{2} Fr_0 \left(\frac{\bar{U}^2}{\bar{U}_0^2} - 1 \right) \bar{h}_0, \quad (4)$$

where we introduced the Froude number, $Fr^2 = \bar{U}^2 / (g\bar{h})$, computed with the averaged variables. In this case, the correction is local (not cumulative) and proportional to the flow depth through a coefficient that is negligible as long as the velocity does not change significantly, and Fr is small, as is common for most tidal flows. With regard to the contribution from the density effect, it was shown by Savenije (2005, 2012) that the induced value of residual water level only amounts to around 1.25% of the estuary depth over the salt intrusion length. Hence, in this study we neglect the impact of density on the dynamics of residual water level.

Assuming negligible advective acceleration influence and density effect, integration of Equation (2) leads to an expression for the residual water level:

$$\bar{Z}(x) = -\int_0^x \frac{\partial \bar{Z}}{\partial x} = -\int_0^x \frac{U|U|}{K^2 h^{4/3}}, \quad (5)$$

if we assume $\bar{Z} = 0$ at the estuary mouth (where $x=0$).

3.2 Analytical solution for tide-river dynamics

To correctly reproduce the residual water level profile in estuaries, an iterative procedure is required to properly calculate the friction term as presented in Equation (5) because the velocity amplitude and water depth are unknown a priori. This is made by using the analytical hydrodynamic model proposed by Cai et al. (2016). In the analytical model, the fundamental assumption made for the geometry of the estuary is that the tidally averaged cross-sectional area \bar{A} and width \bar{B} can be approximated by the exponential functions (e.g., Cai et al., 2016):

$$\bar{A} = \bar{A}_r + (\bar{A}_0 - \bar{A}_r) \exp(-x/a), \quad (6)$$

$$\bar{B} = \bar{B}_r + (\bar{B}_0 - \bar{B}_r) \exp(-x/b), \quad (7)$$

where \bar{A}_0 and \bar{B}_0 are the cross-sectional area and width at the estuary mouth, \bar{A}_r and \bar{B}_r represent the asymptotic riverine cross-sectional area and width, whereas a and b denote the convergence lengths of the cross-sectional area and width, respectively. The tidally averaged depth \bar{h} can be computed directly following the assumption of a mostly rectangular cross-section, i.e., $\bar{h} = \bar{A}/\bar{B}$. The possible impact of the lateral storage areas (e.g., tidal flats or salt marshes) can be described by the storage width ratio $r_S = B_S/\bar{B}$ defined as the ratio of the storage width B_S and the tidally averaged stream width \bar{B} .

Concentrating on a predominantly tidal constituent (e.g., M_2) with frequency ω , it was shown by Cai et al. (2016) that tide-river dynamics are mainly determined by four externally defined, dimensionless parameters (see Table 1), i.e., the dimensionless tidal amplitude ζ defined as the ratio of the tidal amplitude to the depth, the estuary shape number γ (describing the cross-sectional area convergence), the friction number χ (representing the role of frictional dissipation), and the dimensionless river discharge φ (indicating the influence of freshwater discharge Q imposed at the upstream boundary), where η is the tidal amplitude, v is the velocity amplitude, $U_r = Q/\bar{A}$ is the river flow velocity and c_0 is the classical wave celerity in a prismatic frictionless channel, defined as $c_0 = \sqrt{g\bar{h}/r_S}$.

The analytical solutions for the main tide-river dynamics can be obtained by solving a set of four implicit equations:

the damping/amplification equation:

$$\delta = \frac{\mu^2(\gamma\theta - \chi\mu\lambda\Gamma)}{1 + \mu^2\beta}, \quad (8)$$

the phase lag equation:

$$\tan(\varepsilon) = \frac{\lambda}{\gamma - \delta}, \quad (9)$$

the scaling equation:

$$\mu = \frac{\sin(\varepsilon)}{\lambda} = \frac{\cos(\varepsilon)}{\gamma - \delta}, \quad (10)$$

the celerity equation:

$$\lambda = 1 - \delta(\gamma - \delta). \quad (11)$$

The main dependent dimensionless parameters in Equations (8)-(11) are presented in Table 1. They include the amplification/damping number δ , describing the rate of increase ($\delta > 0$), or decrease ($\delta < 0$) of the tidal wave amplitude along the channel axis, the velocity number μ indicating

the ratio of the actual velocity amplitude to the reference value in a prismatic frictionless channel, λ the celerity number denoting the ratio of the classical wave celerity c_0 to the actual wave celerity c , and ε the phase lag between high water (HW) and high water slack (HWS) or between low water (LW) and low water slack (LWS), where ϕ_Z and ϕ_U are the water level phase and velocity, respectively. The unknown parameters θ , β , and Γ in the damping/amplification equation account for the impact of river discharge, where θ and β are defined in Table 1, and Γ is given by:

$$\Gamma = \frac{1}{\pi} [p_1 - 2p_2\varphi + p_3\varphi^2 (3 + \mu^2\lambda^2/\varphi^2)] , \quad (12)$$

which is a friction factor derived by means of a Chebyshev polynomials approach (Cai et al., 2016). In Equation (12), p_i ($i=0, 1, 2, 3$) are the Chebyshev coefficients (see Dronkers, 1964, p.301), which are functions of the dimensionless river discharge φ through $\alpha = \arccos(-\varphi)$:

$$p_0 = -\frac{7}{120} \sin(2\alpha) + \frac{1}{24} \sin(6\alpha) - \frac{1}{60} \sin(8\alpha) , \quad (13)$$

$$p_1 = \frac{7}{6} \sin(\alpha) - \frac{7}{30} (3\alpha) - \frac{7}{30} \sin(5\alpha) + \frac{1}{10} \sin(7\alpha) , \quad (14)$$

$$p_2 = \pi - 2\alpha + \frac{1}{3} \sin(2\alpha) + \frac{19}{30} \sin(4\alpha) - \frac{1}{5} \sin(6\alpha) , \quad (15)$$

$$p_3 = \frac{4}{3} \sin(\alpha) - \frac{2}{3} \sin(3\alpha) + \frac{2}{15} \sin(5\alpha) . \quad (16)$$

The set of Equations (8)-(11) can be regarded as a consistent analytical framework for understanding tide-river dynamics in estuaries. For more details about the computation procedure, readers can refer to Cai et al. (2014a,b, 2016).

4 Results

4.1 Seasonal variation in tidal damping rate and residual water level slope

To understand the importance of seasonal changes in river discharge on tide-river dynamics, we first explore the seasonal variation of the tidal damping rate and the residual water level slope (Figure 3). Here, the tidal damping rate δ_H and the residual water level slope S can be estimated for a reach of length Δx :

$$\delta_H = \frac{1}{(\eta_1 + \eta_2)/2} \frac{\eta_2 - \eta_1}{\Delta x} , \quad (17)$$

$$S = \frac{\overline{Z_2} - \overline{Z_1}}{\Delta x}, \quad (18)$$

where η_1 and $\overline{Z_1}$ are the tidal amplitude and residual water level on the seaward side, respectively, whereas η_2 and $\overline{Z_2}$ are the corresponding values at a distance Δx upstream, respectively.

The study period covers tide-river dynamics under both low and high flow conditions, where the monthly average river discharge observed at the DT station ranges from approximately 9,174 to 61,400 m³/s so that the nonlinear interaction between tidal wave and river flow varies considerably. It has been previously shown that river discharge impacts the tidal damping rate and residual water level slope primarily through the friction term (Cai et al., 2014b, 2016). It can be clearly seen from Figure 3 that both the tidal damping rate and residual water level slope vary strongly with river discharge. Remarkably, it appears there is a threshold, corresponding to a critical value of river discharge, beyond which the relationship between the tidal damping rate and river discharge switches from negatively to positively correlated (Figure 3a). This is particularly the case in the upper reach between the MAS and WH stations when the river discharge threshold is approximately 35,000 m³/s. The underlying mechanism will be elaborated further in the discussion part (see Section 5.2). In Figure 3b, it appears that the residual water level slope is linearly correlated with river discharge.

4.2 Performance of the analytical model

The main geometric characteristics (including the tidally averaged cross-sectional area, width and depth) used in this paper were extracted from a digital elevation model (DEM) produced from Yangtze River estuary navigation charts surveyed in 2007. The elevations have been corrected to the local mean sea level of the Huanghai1985 datum. Figure 4 displays the longitudinal geometric quantities along the Yangtze River estuary axis, in combination with the best-fitting curves reproduced by functions (6) and (7). Table 2 shows the calibrated geometric characteristics, where we observe a relatively large value of cross-sectional area convergence length (151 km), with a relatively small value for width (44 km), suggesting a fast transition from a funnel shaped reach to a prismatic reach in terms of width.

The analytical model was calibrated and verified against the observed tidal amplitude and residual water level along the Yangtze River estuary on the basis of the monthly averaged hydrological data during 2003-2014. The adopted seaward tidal amplitude (at the TSG station) and upward river discharge (at the DT station) in the analytical model are displayed in Figure 2. Since the Yangtze River estuary features a typical semidiurnal character, for the sake of simplification, we used a typical M₂ tidal period (i.e., 12.42 hr). The only calibrated parameter in the analytical model is the Manning-Strickler friction coefficient K . The storage width ratio r_S was assumed as $r_S = 1$. The calibrated value of K is 80 m^{1/3}s⁻¹ in the seaward region ($x=0-32$ km), whereas a smaller value of $K=55$ m^{1/3}s⁻¹ is used in the river dominated region ($x=52-450$ km). Meanwhile, in order to avoid

270 discontinuous jump caused by the adoption of different friction coefficients, we adopted a friction
coefficient of $K=80-55 \text{ m}^{1/3}\text{s}^{-1}$ (indicating a linear reduction of the friction coefficient) over the
transitional reach ($x=32-52 \text{ km}$). Figure 5 shows a comparison between the observed and computed
tidal amplitude and residual water level at different gauging stations along the Yangtze River estuary
for a wide range of tide and river discharge conditions. We observe that the correspondence between
275 analytically computed results and observations is good with a high value for the coefficient of deter-
mination ($R^2 > 0.96$), suggesting a reasonable performance of the analytical model for reproducing
the first-order tide-river dynamics along the Yangtze River estuary. However, we note an overestima-
tion of the analytically computed residual water level at upstream stations (i.e., MAS and WH) for
values $>5 \text{ m}$, which is likely due to the oversimplification of the geometry and flow characteristics
280 (e.g., neglecting the M_4 and M_6 overtides) in the analytical model.

4.3 Seasonal behaviour of tide-river dynamics

The calibrated analytical model is subsequently used to explore the response of the main tide-river
dynamics (represented by the damping/amplification number δ , the velocity number μ , the celerity
number λ and the phase lag ε) to the seasonal variation of river discharge (Figure 6 and Figures
285 S1-S3). Figure 6a shows the spatial-temporal patterns of the damping number δ for the studied
period (2003-2014), together with its minimum value δ_{min} indicating the maximum tidal damping.
The most noticeable feature of the spatial-temporal pattern of tidal damping is the seasonal variation
with river discharge, which is clearly illustrated by the temporal variation of the tidal damping critical
value δ_{min} (see red line in Figure 6a, varying between 233 and 500 km in the Yangtze estuary). To be
290 more specific, in Figure 6b, it can be observed that the critical value of tidal damping and its position
along the estuary are negatively correlated with the corresponding river discharge. Generally, the
critical value of tidal damping δ_{min} reaches its minimum in December or January when the monthly
average river discharge is minimum, and reaches its maximum in July with maximum river discharge
throughout the year. Similarly, we observe that the position along the estuary with the critical δ_{min}
295 reaches its maximum value for minimum river discharge, and minimum value for maximum river
discharge. Similar seasonal behaviour of velocity amplitude (denoted by the velocity number μ),
wave celerity (denoted by the celerity number λ) and phase lag (denoted by ε) can also be reproduced
using the calibrated analytical model (see Figures S1-S3 in the Supplemental Material). In general,
we observe a negatively correlated relation between μ , ε and Q , and a positively correlated relation
300 between λ and Q .

4.4 Seasonal behaviour of the residual water level slope

For a typical tidal river, it is usually observed that the tidal range is reduced when the residual water
level rises in the landward direction owing to the residual water level slope, which is mainly balanced
by the residual frictional effect (Cai et al., 2014b, 2016). To understand the underlying mechanism of

305 tidal wave propagation under the influence of river discharge, we adopted a decomposition method that can be used to quantify the contributions of tide, river and tide-river interaction to the residual water level slope S (see detailed derivation in Cai et al., 2016), computed as:

$$S = -\frac{1}{K^2 \bar{h}^{4/3} \pi} (p_0 v^2 + p_1 v U + p_2 U^2 + p_3 U^3 / v), \quad (19)$$

Equation (19) can be decomposed into three components contributing to the increase of residual
310 water level:

a tidal component:

$$S_t = \frac{1}{K^2 \bar{h}^{4/3} \pi} \left(\frac{1}{2} p_2 + p_0 \right) v^2, \quad (20)$$

a riverine component:

$$S_r = \frac{1}{K^2 \bar{h}^{4/3} \pi} (p_2 - p_3 \varphi) U_r^2, \quad (21)$$

315 and tide-river interaction component:

$$S_{tr} = \frac{1}{K^2 \bar{h}^{4/3} \pi} \left(-p_1 - \frac{3}{2} p_3 \right) v U_r. \quad (22)$$

Figure 7 shows the seasonal variation of the residual water level slope S , exhibiting a positively correlated relationship with the river discharge. It can be seen from Figure 7a that the temporal variation of critical value S_{max} (maximum value) is quite similar to the tidal damping (see Figure
320 6a), which suggests that the development of tide-river dynamics (e.g., tidal damping) is closely related to the residual water level slope. This indicates that both the maximum value of residual water slope S_{max} (Figure 7b) and its position along the estuary (Figure 7a) are positively correlated with river discharge. To further understand the relative importance of tidal forcing alone, river flow alone and tide-river interactions, Equations (20)-(22) were used to quantify the contributions made
325 by both tidal and riverine forcing. The results of these separate components are presented in Figure S4 (see the Supplemental Material), where we observe that the main contribution lies in the riverine component S_r . In addition, we note that the position of the maximum riverine component S_r is landward of the corresponding maximum values of the other two contributions (S_t and S_{tr}), which is mainly due to the relatively larger residual frictional effect introduced by the riverine forcing.

330 5 Discussion

5.1 Critical position of maximum tidal damping (corresponding to the minimum value of damping number δ)

To understand the main processes that control the development of a maximum tidal damping, we used the average values of the observed tidal amplitude at the TSG station and the river discharge at the DT station as model inputs and reproduced the main tide-river dynamics along the Yangtze estuary. Figure 8 shows the longitudinal variation of the main tidal dynamics (δ , λ , μ , and ε) and the contributions made by both tidal and riverine forcing to the residual water level slope together with the water depth for both the wet (Figures 8a, c, e) and dry seasons (Figures 8b, d, f). The discontinuous jump occurring at $x=42$ km depends on the adoption of different friction coefficients in the analytical model. Apparently, the critical position of maximum tidal damping is closer to the sea side during wet season (around $x=305$ km) than the dry season (around $x=410$ km) owing to the river discharge flush. In addition, the position of maximum tidal damping (corresponding to the minimum value of damping number δ , indicated by the dashed black line) is almost coincident with the maximum value of the celerity number λ and the minimum value of the velocity number μ . The slightly lagged responses of λ and μ to δ are due to nonlinear interaction between these main tide-river dynamics parameters, as described by the set of nonlinear Equations (8)-(11). This also indicates the significantly nonlinear effect caused by estuary shape, bottom friction and river discharge as the tidal wave propagating upriver. The change in phase lag ε directly follows from the phase lag equation $\tan(\varepsilon) = \lambda/(\gamma - \delta)$ (see Equation 9). As can be seen from Figures 8a-d, in general the phase lag ε is positively correlated with the damping number δ and the velocity number μ , while it is negatively correlated with the celerity number λ . Unlike tide-dominated estuaries with negligible residual water level, the key parameter that determines the nonlinear relationship between the phase lag ε and the other variables (δ , μ , λ) in tidal rivers lies in the water depth, which is controlled by the dynamics of residual water level. The underlying mechanism generating the maximum tidal damping can be clearly shown in Figures 8e, and f, where we observe that the residual water level slope S and its dominant river component S_r increase to a maximum value near the critical position of maximum tidal damping, beyond which it is reduced. This means that the main tide-river dynamics are driven by the residual water level slope and that the critical position of maximum tidal damping is primarily controlled by the riverine forcing component. Furthermore, we also note that the maximum value of S corresponds to the local minimum \bar{h} , which suggests a dominant impact of residual water level (hence water depth) on tide-river dynamics in the Yangtze River estuary.

It is also worth examining the longitudinal and seasonal variations of the two controlling parameters represented by the estuary shape number γ and the friction number χ (see Figure 9), which are closely related to the strength of tidal damping δ . Remarkably, it is important to note that the effect

of channel convergence (represented by γ) is stronger during the dry season (larger value of γ) than wet season. This indicates that river discharge also tends to reduce the channel convergence through generation of the residual water level slope. In addition, we observe a switch of γ from positive to negative at $x=290$ km and $x=394$ km for the wet and dry seasons, respectively (Figure 9a). The cause of the negative value for γ is that the cross-sectional area increases in the landward direction (hence $d\bar{A}/dx > 0$) owing to the increasing residual water level and depth. In Figure 9b, we observe a larger value for the friction number χ during the dry season than wet season, which is mainly due to the relatively larger tidal amplitude during the dry season and the residual water level (hence the water depth) increasing with river discharge (see the definition of χ in Table 1). Furthermore, it is also noted that χ asymptotically approaches 0 with distance. This means that in the upstream part of the estuary tide-river dynamics are primarily determined by the geometric effect (i.e., the divergence of the cross-sectional area) and the residual frictional effect caused by riverine forcing S_r (see Equation 21).

5.2 Critical river discharge for maximum tidal damping

Based on the analytical results, in Figure 10 we display how the tidal damping δ , the residual water level slope S and the residual water level \bar{Z} develop as a function of river discharge Q for different positions in the upstream river-dominated region, where the maximum tidal damping occurs. Figure 10a shows the tidal damping at different positions with different river discharges. It also displays the critical value of river discharge corresponding to maximum tidal damping. As expected, more river discharge is required to change tidal damping from a negative gradient (indicating a strengthening damping with respect to river discharge Q) to a positive gradient (indicating a weakening damping with respect to river discharge Q) for the seaward positions where tide exerts more influence. The critical river discharge is approximately $34,000 \text{ m}^3\text{s}^{-1}$ at $x=470$ km, and it gradually increases to $55,000 \text{ m}^3\text{s}^{-1}$ at $x=350$ km. In Figure 10a, we also note that beyond the critical value of maximum damping the δ appears to slightly increase until an asymptotic value is approached. Figures 10b and 10c show the relation between S , \bar{Z} and Q . It is noticeable that the curves for residual water level \bar{Z} appear as straight lines, corresponding to a consistent increase of residual water level slope S with river discharge Q . Unlike the longitudinal variation of the maximum S value (see Figures 8e, f), both S and \bar{Z} monotonously increase with Q . In addition, it can be seen from Figure 10a that there exists a threshold of approximate $15000 \text{ m}^3/\text{s}$ for the tidal damping with respect to the position along the estuary. At lower river discharges ($Q < 15000 \text{ m}^3/\text{s}$), the damping number δ tends to decrease (indicating a strengthening damping) in the landward direction, whereas it is the opposite at higher river discharges ($Q > 15000 \text{ m}^3/\text{s}$).

The underlying mechanism for achieving a critical river discharge for maximum tidal damping can be primarily attributed to the cumulative effect of residual water level \bar{Z} altering the water depth and hence the channel convergence and effective friction, according to the definitions of estuary shape

number γ and friction number χ in Table 1. Figure 11 presents these two controlling parameters (γ and χ) as a function of river discharge Q . It can be clearly seen in Figure 11a that there exists an apparent switch of the estuary shape number γ from positive (indicating a reduction of cross-sectional area in the landward direction) to negative (indicating an increase of cross-sectional area in the landward direction). In addition, more river discharge is required to achieve a switch in estuary shape number γ for the seaward positions where tide exerts more influence. The main reason for such a switch is the consistent increase of residual water level and hence water depth and cross-sectional area with river discharge. On the other hand, the effective friction induced by tidal forcing (represented by χ) asymptotically approaches 0 with the river discharge (see Figure 11b), which suggests that the estuarine system is primarily controlled by the divergence of the cross-sectional area and the residual frictional effect caused by riverine forcing (represented by S_r in Equation 21) for high river discharge conditions. Additionally, we can conclude that the asymptotic behaviour of tidal damping δ with high river discharge (as shown in Figure 10a) is due to the corresponding asymptotic behaviour of estuary shape number γ and friction number χ (and hence the residual frictional effect indicated by S as presented in Figure 10b).

5.3 Model limitation and transferability

Although the current analytical model can well reproduce the first-order tide-river dynamics, it also has some limitations. The fundamental assumption is that the tidal wave can be described by a combination of a steady residual term (generated by the river discharge) and a time-dependent harmonic wave (introduced by the tidal flow). Thus, the proposed model can only capture the tidal asymmetry caused by tide-river interaction while it neglects the tidal asymmetry introduced by astronomical tides (e.g., nonlinear interactions among K_1 , O_1 and M_2), overtides (e.g., M_4) and compound tides (e.g., MSf). Consequently, the proposed analytical method is preferably applied to tidal rivers with a predominant tidal constituent (e.g., M_2 or K_1).

It is assumed that both the tidally averaged cross-sectional area and channel width can be approximated by exponential functions following Equations (6)-(7). However, this is not a restrictive assumption since the model in principle can be applied to an arbitrary estuarine shape (i.e., bed elevation and channel width), as long as the variation of the cross-section is gradual. The proposed model can also be used to quantify the spring-neap variability of the tide-river dynamics based on daily averaged tidal amplitude and river discharge conditions (see example in Cai et al., 2016). However, the model cannot be used to explore the tide-river dynamics within a tidal cycle since it is based on a tidally averaged scale. This means that it may not be applicable to the cases with rapidly varying river discharge.

435 **5.4 Implications for sustainable water management and sediment transport**

Knowledge of the development and evolution of tide-river dynamics that determine the behaviour of tidal damping and residual water level slope under external forcing (e.g., tidal and riverine flow) and geometry changes (e.g., deepening and land reclamation) are essential for improving the sustainable water management in estuaries. Adopting the method proposed in this study, one can evaluate the
440 influence of human interventions occurred in the estuarine system (such as large-scale sand excavation, dredging for navigational channel or freshwater withdrawal) on flood control structures (e.g. storm surge barriers, flood gates), and aquatic environment (e.g., such as salt intrusion and the related water quality). For instance, Cai et al. (2019) explored how the freshwater regulation of the Three Gorges Dam (the world's largest hydroelectric station in terms of installed power capacity) may af-
445 fect the alteration of tidal limit in the Yangtze estuary by means of the analytical model proposed in this paper. It was shown that the largest change of tidal limit by around 75 km occurred in October owing to the substantial increase in freshwater discharge. When combined with ecological or salt intrusion models, the analytical approach presented in this study is particularly useful for a quick computation of the longitudinal distribution of the salinity (e.g., Cai et al., 2015). Using salinity as a
450 general predictor, it is possible to assess the potential impacts of human interventions on the aquatic ecosystem health in general (e.g., water quality, water utilization and agricultural development in the estuarine area).

As tide propagates into an estuary, it is distorted and becomes asymmetric due to significant nonlinear interactions with geometry and river flow. Tidal asymmetry is regarded as one of the most
455 important mechanisms generating residual sediment transport (e.g., Friedrichs and Aubrey, 1988; Parker, 1991; Guo et al., 2014, 2015, 2016; Zhang et al., 2018b). Although the current analytical method can only deal with tide-river interaction for a single predominant tidal constituent (e.g., M_2), the model does capture the major tidal asymmetry induced by geometric effect and riverine flow (e.g., the tidal asymmetry caused by the residual river flow) and can well reproduce the seasonal
460 behaviour of tidal damping and residual water level slope. It was shown by Lamb et al. (2012) that the erosion and deposition patterns along an estuary are strongly related to the shape of the residual water level profile, which we have shown to be linked to the tide-river dynamics and the geometry of the estuary. The successful reproduction of the seasonal behaviour of tide-river dynamics and residual water level slope in the Yangtze estuary suggests that the proposed analytical approach can
465 be used as a tool for detecting the evolution of estuarine morphology under various external forcing conditions. However, further studies are required to quantify the relationship between the residual water level slope and the estuarine morphology.

6 Conclusions

Both observations and analytical model results show a critical value of river discharge that causes
470 maximum tidal damping in the upstream part of the tidal river, challenging the concept of how river
discharge dampens tidal waves. The residual water level slope, mainly balanced by the residual
frictional effect, plays a key role in determining the evolution of tide-river dynamics under a wide
range of tidal and riverine forcing conditions. A critical position along the estuary is where there is
maximum tidal damping, upstream of which the residual water level slope is reduced. The location
475 of this position moves seaward with the increase of river discharge. From that position landwards,
the effect of river discharge on tidal damping becomes weaker instead of stronger, indicating a
weakening of the backwater effect induced by the residual frictional effect. It is worth noting that the
underlying mechanism of generating critical position along the estuary is similar to that of generating
critical river discharge due to the fact that for a given (constant) river discharge, the more upstream in
480 a tidal river, the stronger effect caused by the river discharge, which is analogous to a river discharge
increase at a given (fixed) location.

Moreover, analytical model results show that more river discharge is required to change the maximum
tidal damping critical value from a negative to a positive gradient for the seaward positions
where the tide exerts stronger impact. The underlying mechanism has to do with the fact that river
485 discharge affects tidal damping, on the one hand, attenuating tidal motion by increasing the quadratic
velocity in the numerator, and on the other hand, reducing the effective friction by increasing the
water depth in the denominator. The occurrence of critical river discharge suggests the cumulative
effect of residual water level (increasing the water depth and the cross-sectional area) that exceeds
the threshold of tide-river dynamics, beyond which tidal damping weakens with river discharge.
490 To the best of our knowledge, this is one of the few studies that shows the gradient switch of the
cross-sectional area (i.e., $d\bar{A}/dx$) and tidal damping (i.e., $d\delta/dx$) with the river discharge, shedding
new light on the impact of river discharge on tidal damping in alluvial estuaries (see also Matte
et al., 2018, 2019). Moreover, the results obtained in this study will, hopefully, provide scientific
guidelines for water resources management (e.g., flood control and salt intrusion prevention) in the
495 Yangtze River estuary and other tidal rivers worldwide.

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Table 1. Dimensionless parameters adopted in the analytical model for tide-river dynamics

Local variables	Dependent variables
Dimensionless tidal amplitude $\zeta = \eta/\bar{h}$	Amplification number $\delta = c_0 d \eta / (\eta \omega d x)$
Estuary shape number $\gamma = c_0 (\bar{A} - \bar{A}_r) / (\omega a \bar{A})$	Velocity number $\mu = v / (r_S \zeta c_0) = v \bar{h} / (r_S \eta c_0)$
Friction number $\chi = r_S g c_0 \zeta [1 - (4\zeta/3)^2]^{-1} / (\omega K^2 \bar{h})$	Celerity number $\lambda = c_0 / c$
Dimensionless River discharge $\varphi = U_r / v$	Phase lag $\varepsilon = \pi/2 - (\phi_Z - \phi_U)$
$\beta = \theta - r_S \zeta \varphi / (\mu \lambda), \quad \theta = 1 - (\sqrt{1 + \zeta} - 1) \varphi / (\mu \lambda)$	

Table 2. Characteristics of geometric parameters in the Yangtze River estuary

Characteristics	River	Mouth	Convergence length a or b (km)
Cross-sectional area \bar{A} (m ²)	12,135	51,776	151
Width \bar{B} (m)	2005	6735	44

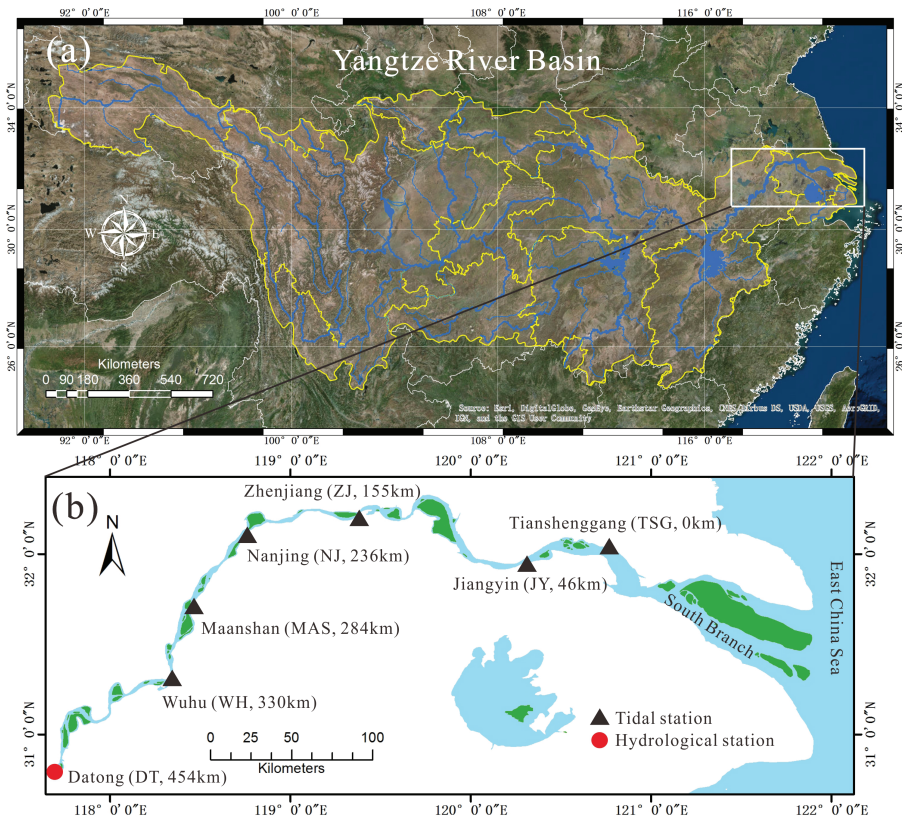


Fig. 1. Sketch map of the Yangtze River basin (a) and the Yangtze River estuary (b) displaying the location of gauging (triangle) and hydrological (circle) stations.

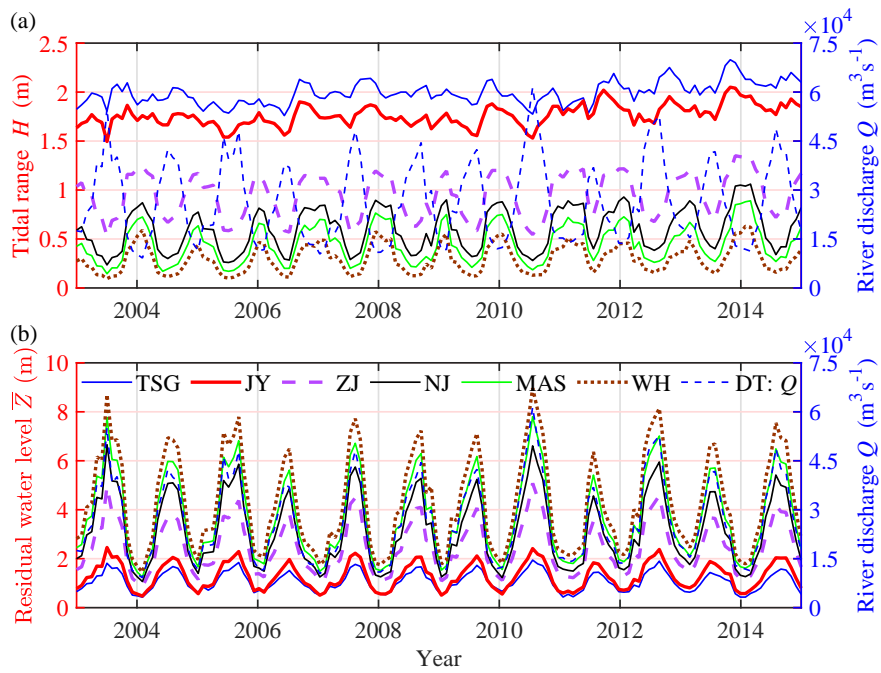


Fig. 2. Temporal (monthly averaged) variations of observed tidal range H (a) and residual water level \bar{Z} (b) at different gauging stations along the Yangtze River estuary together with the observed river discharge at Datong hydrological station.

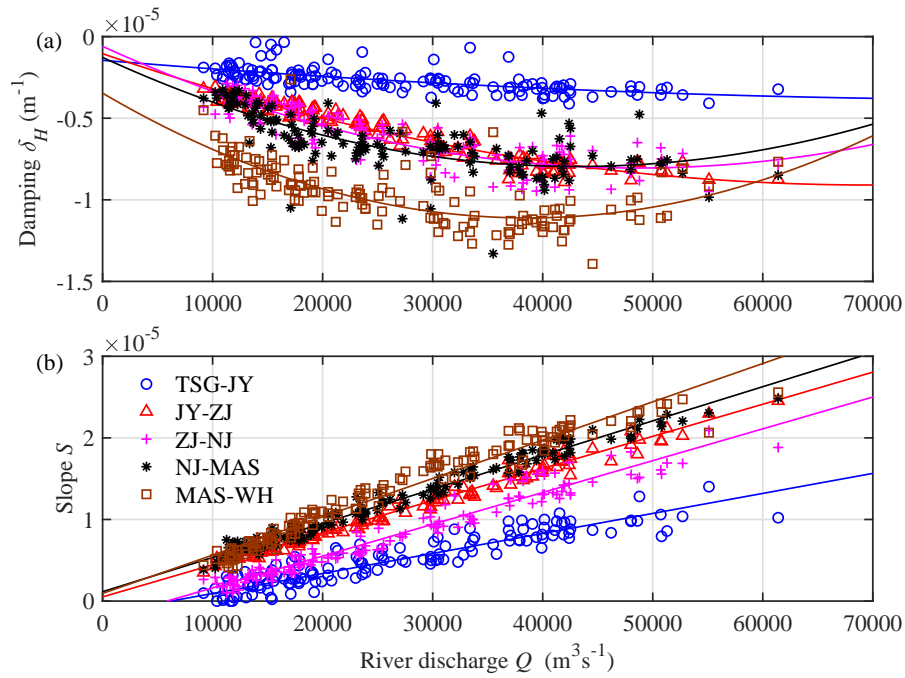


Fig. 3. Scatterplot and liner regression line of tidal damping rate δ_H (a) and residual water level slope S (b) for different reaches in the Yangtze River estuary as a function of river discharge observed at the DT hydrological station. Subplot (a) also presents the quadratic regression lines, while subplot (b) presents the linear regression lines.

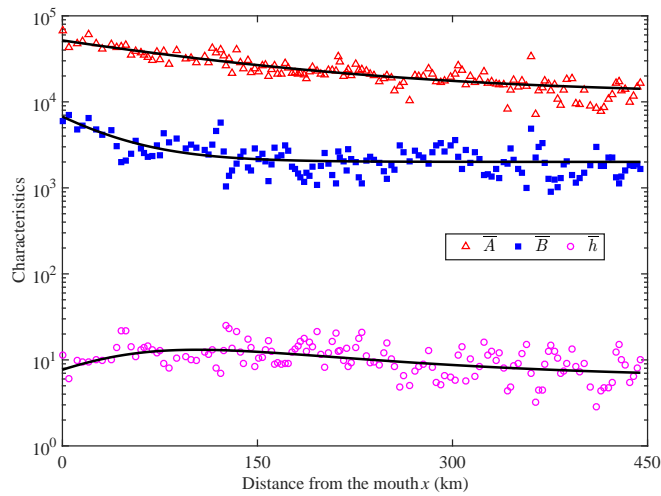


Fig. 4. Longitudinal variation of the main geometric characteristics (cross-sectional area, width and depth) along the Yangtze River estuary. The thick black lines represent the best fitting curves.

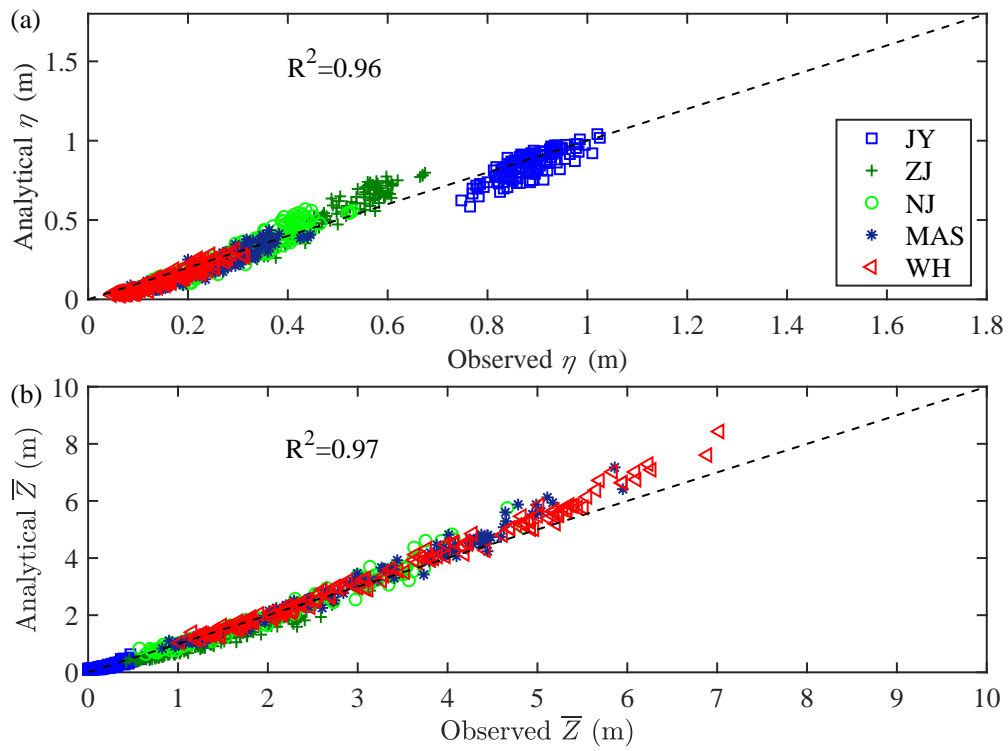


Fig. 5. Comparison of analytically computed tidal amplitude η (a) and residual water level \bar{Z} (b) against the observations in the Yangtze River estuary during the study period (2003-2014).

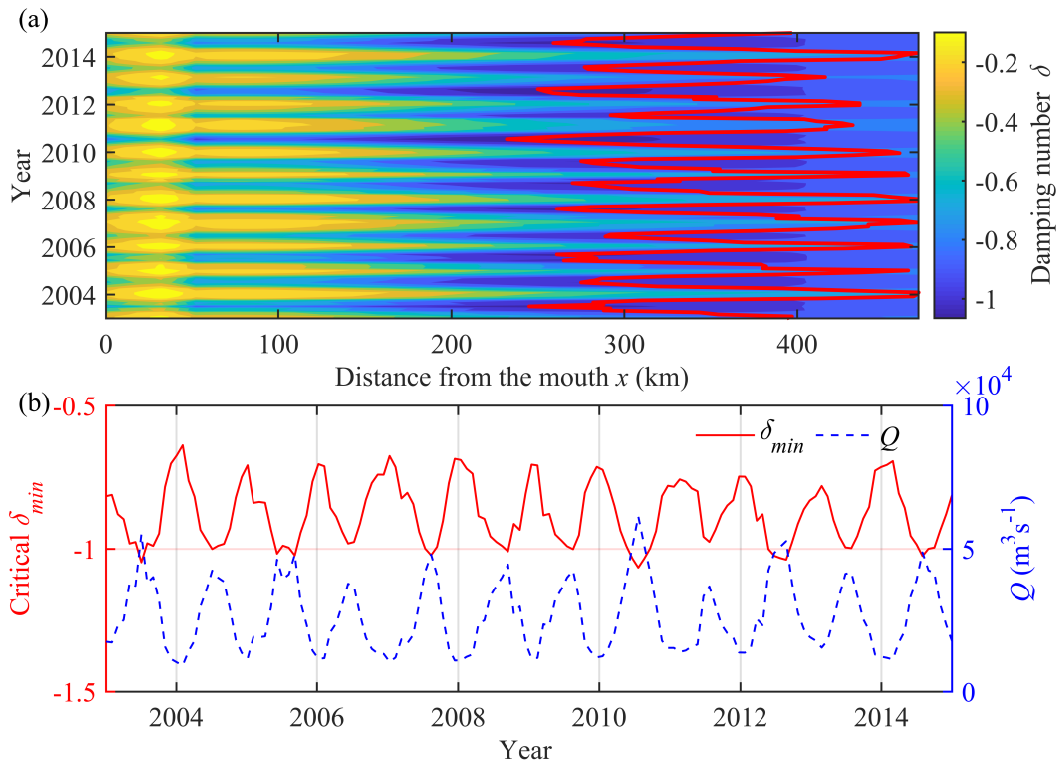


Fig. 6. Contour plot of the damping number δ together with its minimum value δ_{min} (indicated by the red line) for each month (a) and the relation between the critical value and river discharge Q (b).

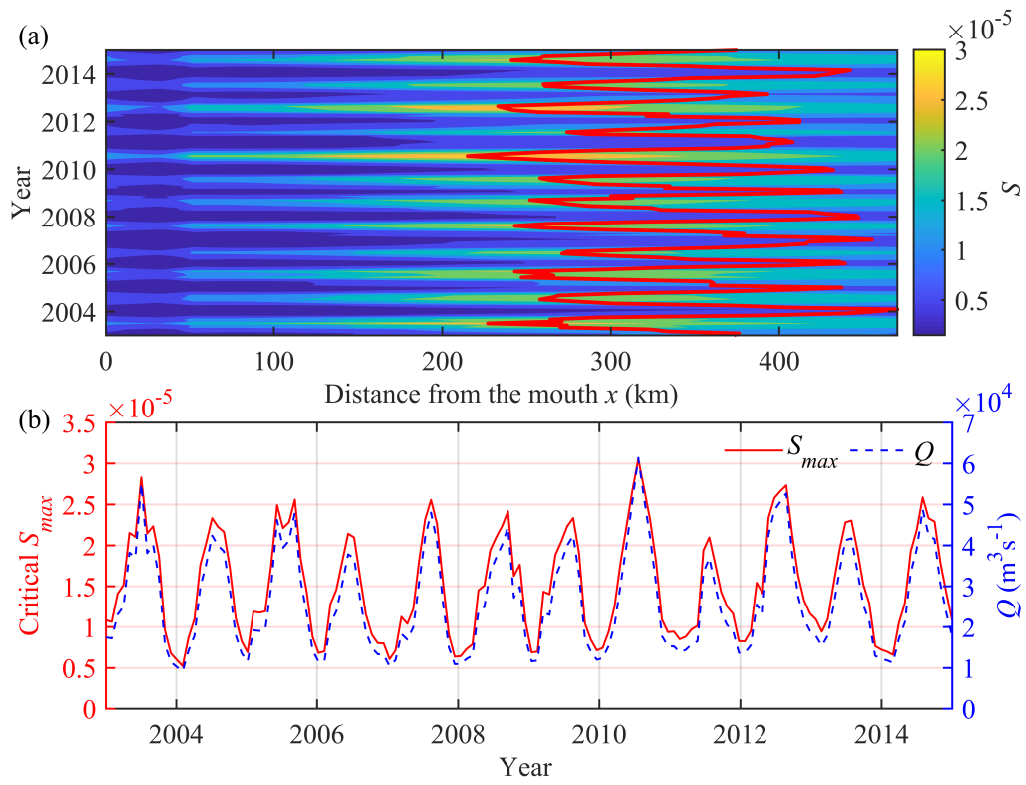


Fig. 7. Contour plot of the residual water level slope S together with its minimum value S_{max} (indicated by the red line) for each month (a) and the relation between the critical value and river discharge Q (b).

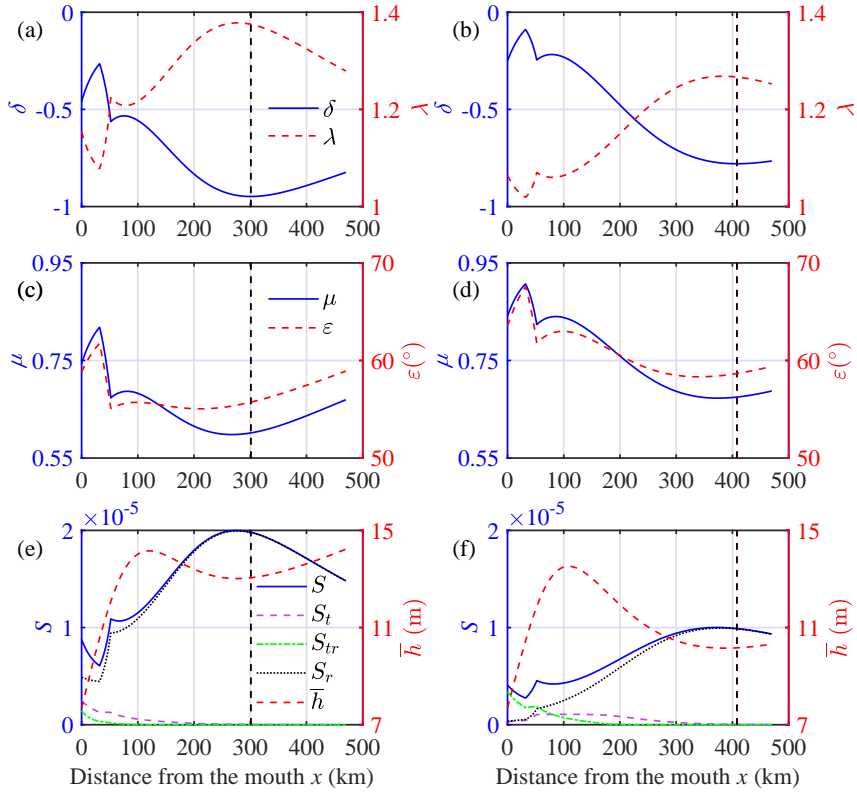


Fig. 8. Longitudinal variation of the main tide-river dynamics (a, b, c, d) and contributions of tidal and riverine forcing to the residual water level slope together with the water depth (e, f) for the wet (a, c, e) and dry seasons (b, d, f) in the Yangtze estuary. The dashed lines in each subplot represent the critical position for maximum tidal damping (corresponding to the minimum value of damping number δ).

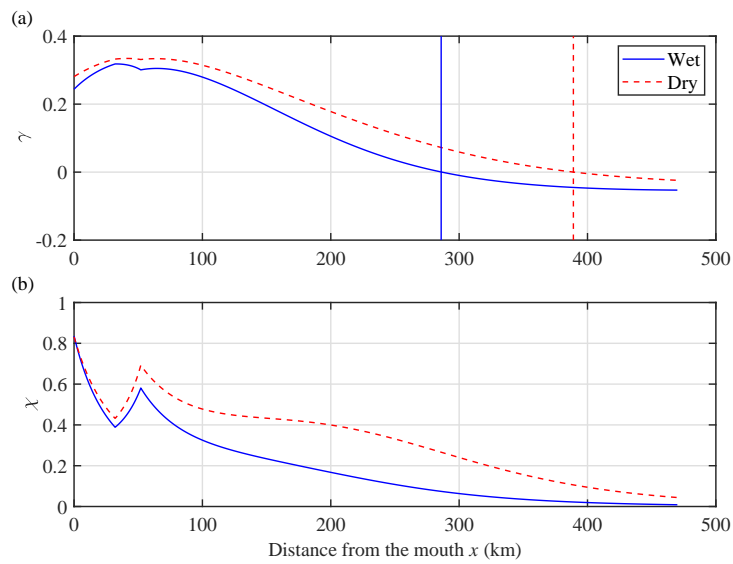


Fig. 9. Longitudinal variation of the estuary shape number γ (a) and the friction number χ (b) for the wet and dry seasons in the Yangtze estuary. Subplot (a) also indicates the position of the critical value of channel convergence (i.e., $\gamma=0$) using the corresponding lines for the wet and dry seasons.

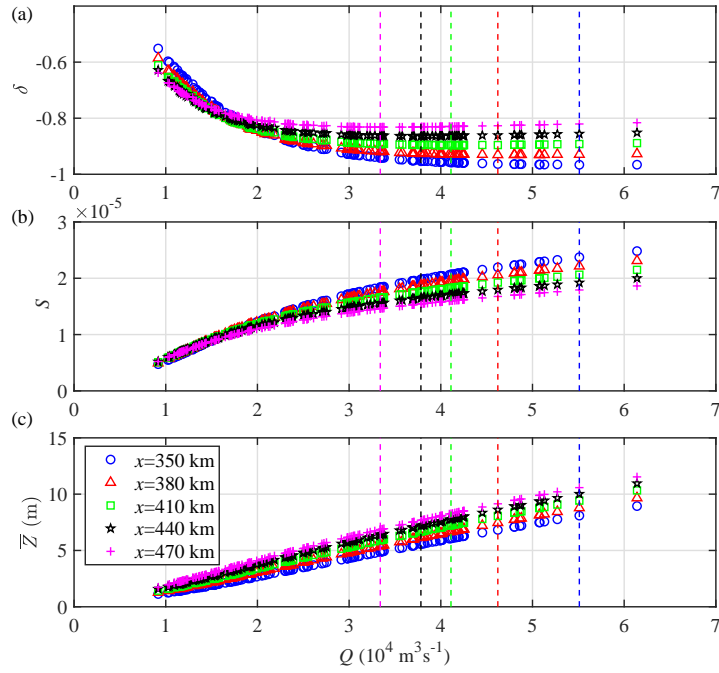


Fig. 10. Relationship between the tidal damping number δ (a), the residual water level slope S (b), the residual water level \bar{Z} (c) and the corresponding river discharge Q imposed at the DT hydrological station for different positions, indicated by different symbols. The dashed lines with the same colour as the symbols were used to identify the critical river discharge for the maximum tidal damping (corresponding to the minimum value of δ in subplot a).

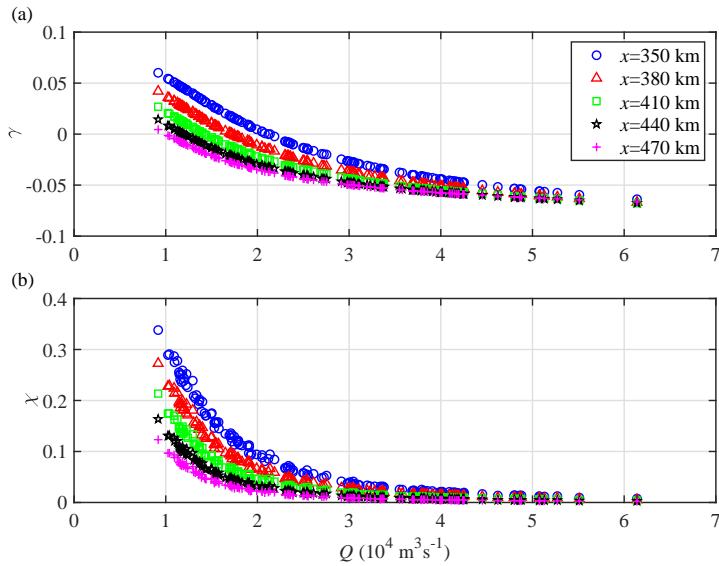


Fig. 11. Relationship between the estuary shape number γ (a), the friction number χ (b) and the river discharge Q .