# Process-Based Flood Frequency Analysis in an Agricultural Watershed Exhibiting Nonstationary Flood Seasonality

Guo Yu<sup>1</sup>, Daniel B. Wright<sup>1</sup>, Zhihua Zhu<sup>2</sup>, Cassia Smith<sup>3</sup>, Kathleen D. Holman<sup>4</sup>

<sup>1</sup>Department of Civil and Environmental Engineering, University of Wisconsin-Madison, Madison, 53706, USA

<sup>5</sup> <sup>2</sup>Department of Water Resources and Environment, Sun Yat-sen University, Guangzhou, 510275, China <sup>3</sup>Department of Civil and Environmental Engineering, Carnegie Mellon University, Pittsburgh, 15213, USA <sup>4</sup>US Department of the Interior, Bureau of Reclamation, Denver, 80225, USA

Correspondence to: Zhihua Zhu (zzhu264@wisc.edu)

Abstract. Floods are the product of complex interactions among processes including precipitation, soil moisture, and watershed morphology. Conventional flood frequency analysis (FFA) methods such as design storms and discharge-based statistical methods offer few insights into these process interactions and how they "shape" the probability distributions of floods. Understanding and projecting flood frequency in conditions of nonstationary hydroclimate and land use requires deeper understanding of these processes, some or all of which may be changing in ways that will be undersampled in observational records. This study presents an alternative "process-based" FFA approach that uses stochastic storm transposition to generate

- 15 large numbers of realistic rainstorm "scenarios" based on relatively short rainfall remote sensing records. Long-term continuous hydrologic model simulations are used to derive seasonally varying distributions of watershed antecedent conditions. We couple rainstorm scenarios with seasonally appropriate antecedent conditions to simulate flood frequency. The methodology is applied to the 4002 km<sup>2</sup> Turkey River watershed in the Midwestern United States, which is undergoing significant climatic and hydrologic change. We show that using only 15 years of rainfall records, our methodology can produce
- 20 accurate estimates of "present-day" flood frequency. We found that shifts in the seasonality of soil moisture, snow, and extreme rainfall in Turkey River exert important controls on flood frequency. We also demonstrate that process-based techniques may be prone to errors due to inadequate representation of specific seasonal processes within hydrologic models. If such mistakes are avoided, however, process-based approaches can provide a useful pathway toward understanding current and future flood frequency in nonstationary conditions and thus be valuable for supplementing existing FFA practices.

# 25 1 Introduction

Riverine floods, among the most common natural disasters worldwide, are the product of complex interactions between heavy rainfall, watershed and river channel morphology, and antecedent (i.e. initial) conditions including soil moisture and snowpack. Their impacts are projected to increase in the future due to hydrometeorological factors (e.g. Hyndman, 2014) and increased human development in flood prone areas (e.g. Ntelekos et al., 2010; Ceola et al., 2014; Prosdocimi et al., 2015). Estimating

30 the relationships between flood likelihood and severity is central to flood risk management and infrastructure design; these

relationships are typically represented by flood frequency distributions (or curves), while the broad family of procedures used to derive them is termed flood frequency analysis (FFA). Most existing FFA methods belong to one of three approaches: statistical analysis of streamflow observations, design storms, and continuous simulation or other so-called "derived" or "process-based" methods. Each has strengths and shortcomings, which are briefly summarized in Sect. 2 (see Wright et al.,

5 2014a for a distinct summary).

FFA is challenging even in stationary (i.e. unchanging) watershed and hydroclimatic conditions due to the scarcity of observations of large floods and the associated factors that generate them (Stedinger and Griffis, 2011). The role of soil moisture in flood frequency, for example, is very important (Berghuijs et al., 2016), but poorly understood due to a lack of long-term observations. Furthermore, the individual and joint flood causative factors will evolve as a watershed undergoes

10 changes in land use or hydroclimate (Machado et al., 2015). Leading causes of change (i.e. nonstationarity) include human intervention through land use change or reservoir construction (Konrad and Booth, 2002; Schilling and Libra, 2003; Villarini et al., 2009), natural climate variability (Enfield et al., 2001; Jain and Lall, 2000) and anthropogenic climate change driven by increasing greenhouse gas concentrations (Milly et al., 2008; Hirsch and Ryberg, 2012). Combinations of these will lead to nonstationary flood frequency, a challenge for which the bulk of existing FFA methods are ill-suited (El Adlouni et al., 2007;

15 Gilroy and McCuen, 2012).

In this study, we present an alternative FFA methodology that aims to "construct" the flood frequency curve through a combination of observations, stochastic methods, and hydrologic modeling that generates and combines the causative factors (i.e. processes) such as rainfall and soil moisture that produce floods. This concept is not new, and has traditionally be called "derived FFA" (e.g. Eagleson, 1972; Franchini et al., 2005; Haberlandt, 2008), though we prefer the more descriptive term

20 "process-based FFA" (after Sivapalan and Samuel, 2009; see Clark et al., 2015a, 2015b and Lamb et al., 2016; who discuss somewhat similar techniques). Sivapalan and Samuel (2009) argue in favor of process-based approaches in the face of nonstationary conditions, though they do not actually lay out a specific FFA procedure.
We present such a process-based procedure, and apply it to an agricultural watershed in the Midwestern United States that is

undergoing substantial seasonal hydroclimatic and hydrologic changes that have led to nonstationary flood frequency. We show that this procedure is useful for deciphering the underlying physical processes that drive flooding, as well as their changes in this watershed. Our methodology underscores the importance of seasonality in the joint contributions of rainfall,

- soil moisture, and snow to flood frequency. To our knowledge, this study is the first to explore the role that seasonal changes in hydroclimatic and hydrologic processes play in nonstationary flood frequency, though other studies have explored the importance of such processes in flood occurrence more generally (e.g. Berghuijs et al., 2016).
- 30 The structure of the paper is as follows: Section 2 briefly reviews the three aforementioned FFA approaches. Section 3 introduces the study region, watershed, and hydrometeorological data. Section 4 outlines the process-based FFA methodology used in this study, including the hydrologic model, the stochastic storm transposition (SST) procedure used to derive the synthetic rainfall scenarios, and elements of both continuous and event-based rainfall-runoff simulation. The nonstationary hydroclimate of the study watershed and trends in relevant hydrometeorological variables are analyzed in Sect. 5.1. Model

validation is presented in Sect. 5.1. Process-based FFA results are presented and compared with "conventional" statistical estimates in Sect. 5.3. Simulated flood seasonality is explored in Sect. 5.4. The relationships between rainfall and simulated peak discharge quantiles are examined in Sect. 5.5. Section 6 includes a summary and concluding remarks.

## 2 Review of FFA Approaches

## 5 2.1 Discharge-based Statistical Approaches

Statistical FFA approaches involve fitting a statistical distribution to extreme discharge observations and extrapolating this distribution to estimate quantiles such as the 100-year or 500-year discharge. While these approaches utilize direct observations of flooding (e.g. peak discharge or volume), long streamflow records at or near the given river cross section are needed for reliable quantile estimates. Such records are lacking in many locations, even in developed countries. Statistical approaches are

- 10 limited by the available observations; thus, the estimation distribution may not represent the "true" (unknown) distribution of possible outcomes (Linsley, 1986; Klemeš, 1986, 2000a, 2000b). In principle, regionalized FFA methods are able to improve quantile estimates both at gaged and ungauged locations (Dawdy et al., 2012); they make assumptions, however, regarding the transferability of regional information to specific locations and in doing so may neglect key geophysical processes that dominate the spatiotemporal variability of floods (Ayalew and Krajewski, 2017).
- 15 Though streamflow observations are the result of a range of complex factors including rainfall, soil moisture, and channel routing, without concurrent observations of these "upstream" variables, neither streamflow observations nor distributions fitted to them provide much insight into flood causes. Long-term records of such variables, particularly soil moisture, are virtually nonexistent. There have been numerous examples within the FFA literature pointing to situations in which discharge-based analyses can be inferior to those based on hydrologic modeling, including cases of basin storage "discontinuities" (Rogger et 20)
- 20 al., 2012), reservoirs (Ayalew et al., 2013), and land use change (Cunha et al., 2011). Finally, most statistical FFA methods assume that the magnitude of extreme flood events and quantiles are stationary. This assumption conflicts with numerous examples in which hydrological records exhibit various types of nonstationarity (e.g. Potter, 1976; Villarini et al., 2009; Douglas et al., 2000; Franks and Kuczera, 2002). Though nonstationary statistical FFA techniques do exist (e.g. Cheng et al., 2014; Gilleland and Katz, 2016; Serago and Vogel, 2018), they face severe limitations
- extrapolating to future conditions (Luke et al., 2017; Sivapalan and Samuel, 2009; Stedinger and Griffis, 2011) since they rarely consider the fundamental physical causes of change.

### 2.2 Design Storm Approaches

Design storm (DS) approaches use idealized rainfall scenarios of a given return period as inputs to a hydrologic model to simulate flood peaks. DS is widely used in practice due to its simplicity (Cudworth, 1989; Kjeldsen, 2007; Ball et al., 2016).

30 To some extent, the flood-producing physical processes are captured via the hydrologic model, which also provides a complete simulated flood hydrograph, as opposed to only the peak discharge or volume provided by statistical approaches. However,

DS approaches rely on at least three major assumptions: (1) point-based rainfall intensity-duration-frequency (IDF) estimates (which are subject to some of the same aforementioned statistical and data availability issues as flood discharges) can be converted into hyetographs using dimensionless temporal rainfall distributions and into basin-averaged estimates using area reduction factors (e.g. Svensson and Jones, 2010); (2) IDF estimates, based on annual rainfall maxima, produce flood peaks

- 5 which are quantiles of the distributions of flood annual maxima; and (3) there is a 1:1 equivalence between rainfall and simulated discharge quantiles (i.e. return periods or recurrence intervals), for example, a 100-year idealized rainfall event will produce a reasonable estimate of the 100-year peak discharge. The last of these assumptions discounts the possibility that watershed initial conditions such as soil moisture and snowpack can modulate the transformation of rainfall quantiles into discharge quantiles.
- 10 These assumptions are not without their shortcomings. Wright et al. (2014b), for example, showed significant disparities between observed point and basin-averaged rainfall extremes that cannot be captured using conventional ARF concepts. Using design storm in conjunction with a derived distribution approach, Viglione and Blöschl (2009) and Vigligone et al. (2009) demonstrated that the ratio of rainfall return period to flood peak return period is controlled by storm duration, a runoff coefficient (which is related to antecedent conditions), and a runoff threshold effect. Antecedent conditions can vary
- 15 substantially by season, meaning that high soil moisture may only infrequently coincide with extreme rainfall. Wright et al. (2014a) discusses additional design storm shortcomings in greater detail, including time of concentration concepts, while also pointing out that design storm approaches (like other hydrologic model-based FFA) can incorporate future projections in land use and rainfall more explicitly than can statistical discharge-based methods.

## 2.3 Continuous Simulation and Process-Based FFA Approaches

- 20 Continuous simulation (CS) and process-based approaches to FFA leverage the potential benefits of hydrologic models while minimizing the simplifying assumptions of DS methods. CS approaches typically use long series of historical or stochastically generated rainfall, temperature, and occasionally other meteorological variables as model inputs, to simulate long discharge time series. Peak flows can be extracted from these series and the flood frequency distribution can be obtained. Thus, event rainfall return period and duration and antecedent conditions do not need to be specified and the equality between rainfall and
- 25 discharge return period is not assumed (Calver et al., 1999, 2009). In addition, projections of future flood frequency can be developed by incorporating general circulation model (GCM) rainfall and temperature projections into the input meteorological series (Gilroy and McCuen, 2012; Rashid et al., 2017). On the other hand, CS approaches are limited by the general lack of reliable long-term time series of extreme rainfall and other meteorological data (Blazkova and Beven, 1997, 2002, 2009) and, in the case of sophisticated distributed approaches, by potentially high computational demands (Li et al., 2014; Peleg et al.,
- 30 2017). Stochastic rainfall generation techniques typically struggle to produce the extremes that are critical for flooding (e.g. Cameron et al., 2000; Furrer and Katz, 2008), and training such models for locations with rainfall nonstationarities and strong seasonal variations is nontrivial. Camici et al., (2011) and Li et al. (2014) present process-based FFA approaches that couple long CS simulation results with event-based simulations.

One argument in favor of CS and process-based approaches is that the complex joint relationships between flood drivers such as rainfall and soil moisture are resolved within the modeling framework and thus do not rely on users' assumptions. We demonstrate that caution is needed in the representation of seasonality; to briefly summarize, it is critical that both seasonality in input variables as well as seasonally varying processes within the model be "correct." Without verifying this, process-based

5 approaches may produce seemingly correct results as a result of incorrect methods.

#### **3 Study Region and Data**

The study watershed of Turkey River is situated in northeastern Iowa (Fig. 1a, 1b). The portion upstream of the US Geological Survey (USGS) stream gage at Garber (gage number 05412500) has a drainage area of 4002 km<sup>2</sup>, with elevations ranging from approximately 426 m above sea level (masl) in the west to 197 masl at the stream gage (Fig. 1c). Streams in the upper

- 10 part of the catchment have relatively mild slopes, while the channels and hillslopes in the lower part are steeper. Soils are mainly loams and silts (IFC, 2014). According to USGS 2012 National Land Cover Dataset (NLCD), the Turkey River watershed is predominantly agricultural, with less than 2% urban land cover (Fig. 1d). Comparisons of NLCD from 1992, 2001, 2006, and 2012 indicate that land uses have not evolved significantly over time (results not shown), though the hydrologic impacts of subsurface tile drainage, which has become ubiquitous throughout the region, are poorly understood
- 15 and could exert meaningful influence on flooding (see, e.g. Schilling et al., 2014).



**Figure 1.** Study region. (a) Conterminous United States with the state of Iowa highlighted in grey. (b) Zoomed-in map showing Iowa (black outline) and the Turkey River watershed (red) and the extent of the stochastic storm transposition region (blue dash line). (c, d) Turkey River watershed showing land surface elevation (based on the USGS National Elevation Dataset) and land use (based on the USGS 2012 NLCD), respectively.

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We use daily discharge observations for 84 years (1933-2016) from the USGS streamgage at Garber to understand the hydroclimatology of flooding and to validate our FFA results. Daily discharge observations for 69 years (1948-2016), in conjunction with Global Historical Climate Network (GHCN) daily temperature and snow data are used to configure, calibrate, and validate the hydrologic model, as described in Sect. 4.1. CPC US Unified (CPC-Unified; Chen et al., 2008) and Stage IV

10 (Lin and Mitchell, 2005) precipitation data, available through the National Oceanic and Atmospheric Administration, are used for rainfall analyses. CPC-Unified provides daily, 0.25° rainfall estimates interpolated from rain gage observations, while Stage IV provides hourly, approximately 4 km estimates by merging data from rain gages and the National Weather Service Next-Generation Radar network (NEXRAD; Crum and Alberty, 1993). Analyses based on Stage IV use data from 2002-2016, while long-term analyses based on CPC-Unified use data from 1948-2016.

## 4 Methodology

The FFA approach presented in this study combines continuous simulation (CS), stochastic storm transposition (SST) using the RainyDay software, and event-based simulation. CS provides large samples of seasonally varying antecedent conditions, namely soil moisture and snowpack. SST produces large numbers of synthetic rainfall scenarios. Together, these drive event-

5 based simulations to generate the synthetic flood peaks that are used to derive flood frequency distributions. The approach is illustrated schematically in Fig. 2 and summarized in the following subsections.



Figure 2. Flow chart showing the process-based FFA approach. Dotted outlines delineate components associated with subsections 4.1, 4.2 and 4.3.

## 4.1 Hydrologic Model, Calibration, and Continuous Simulation

We used the lumped Hydrologiska Byråns Vattenavdelning (HBV) model (Bergström, 1992, 1995; Lindström et al., 1997).

- 5 HBV has been widely used to study hydrologic response in United States (Vis et al., 2015; Niemeyer et al., 2017) and other regions of the world (Harlin and Kung, 1992; Osuch et al., 2015; Seibert, 2003; Chen et al., 2012). The "HBV-Light" version (henceforth referred to as HBV; Seibert and Vis, 2012) used in this study consists of four main routines: snowpack, soil moisture, catchment response, and runoff routine. HBV simulates daily discharges based on time series of precipitation and air temperature, as well as estimates of long-term daily potential evapotranspiration. A list of model parameters is shown in
- 10 Table 1.

The process-based FFA methodology employed in this study could be coupled with other hydrologic models. A distributed model would allow for more realistic representation of important characteristics like changing land use, rainfall spatiotemporal structure, and flood wave attenuation in river channels, and could operate at higher (i.e. subdaily) temporal resolution. We selected HBV at the daily time step due to its simplicity, computational speed, and its ability to represent multiple watershed

15 hydrological processes.

We calibrated separate HBV models using both CPC and Stage IV rainfall. Most parameter values were the same for CPCand Stage IV-based models except for three snow routine parameters (TT, CFMAX, SFCF) and three recession coefficients (K0, K1, K2), allowing for the variability of model parameters for different climate conditions. For each model setup, we first calibrated the model with snowpack routine "turned off" (by setting TT parameter to a very low value) to obtain parameters

20 that can simulate summer floods adequately. Then, keeping these optimized non-snow routine parameters unchanged, we calibrated the snow routine parameters.

To determine the optimized model parameter sets in each procedures, we followed the Genetic Algorithm and Powell (GAP) optimization method as presented by Seibert (2000), which is briefly summarized here. First, 5000 parameter sets are randomly generated from a uniform distribution of the values of each parameter (Table 1), which were then applied to the HBV model

25 in order to maximize Kling Gupta Efficiency (Gupta et al., 2009) of simulated daily discharge. After the GAP has finished, the optimized parameter set were fine-tuned using Powell's quadratic convergent method (Press, 1996) with 1000 additional runs. Lastly, the optimized parameter set was manually adjusted to improve the fits between observed and simulated annual peak flow (see Lamb, 1999). More elaborate calibration and uncertainty estimation procedures such as Generalized Likelihood Uncertainty Estimation (GLUE; Beven and Binley, 1992; Beven, 1993; Beven and Binley, 2014) could be used, but are outside

30 the scope of our study.

The two different HBV models were then used to perform CS with historical CPC and Stage IV rainfall and temperature data to derive long-term simulated soil moisture and snowpack values, which are usually difficult to obtain via measurement. We

"pair" samples of these initial conditions with synthetic rainfall events to simulate hypothetical floods, as described in Sect. 4.2 and Sect. 4.3.

Parameter	Description	Units	Min value	Max value	
Snow Routine					
TT	Threshold temperature for liquid and solid precipitation	°C	-3	3	
CFMAX	Degree-day factor	mm $d^{-1}$ °C <sup>-1</sup>	0.5	4	
SFCF	Snowfall correction factor	-	0.5	1.2	
CFR	Refreezing coefficient	-	0.01	0.1	
CWH	Water holding capacity of the snow storage	-	0.1	0.3	
Soil Moisture Routine					
FC	Maximum soil moisture storage (field capacity)	mm	100	550	
LP	Relative soil water storage below which AET is reduced linearly	-	0.3	1	
BETA	Exponential factor for runoff generation	-	1	5	
Response Routine					
PERC	Maximum percolation from upper to lower groundwater box	$mm d^{-1}$	0	10	
UZL	Threshold of upper groundwater box	mm	0	50	
<b>K</b> 0	Recession coefficient 0	$d^{-1}$	0.5	0.9	
K1	Recession coefficient 1	$d^{-1}$	0.15	0.5	
K2	Recession coefficient 2	d <sup>-1</sup>	0.01	0.15	
Routing Routine	2				
MAXBAS	Length of triangular weighting function	d	1	2.5	

Table 1. Overview of HBV model parameters and upper and lower parameter limits used for calibration.

## 4.2 Stochastic Storm Transposition

- 5 Stochastic storm transposition (SST) is a bootstrap method to generate realistic probabilistic rainfall scenarios through temporal resampling and spatial transposing of observed storms from the surrounding region. SST effectively "lengthens" the rainfall record via "space-for-time substitution." Unlike rainfall IDF curves, SST can preserve observed rainfall space-time structure, and, unlike design storm methods, obviates the need to equate rainfall duration to catchment response time (Wright et al., 2013, 2014a, 2014b). Alexander (1963), Foufoula-Georgiou (1989), and Fontaine and Potter (1989) provide general
- 10 descriptions of SST. Wilson and Foufoula-Georgiou (1990) apply the method for regional rainfall frequency analysis while Gupta (1972), Franchini et al. (1996), England et al. (2014) and Nathan et al. (2016) use it for FFA. Wright et al. (2013) used SST with a 10-year high-resolution radar rainfall dataset to estimate spatial IDF relationships. Wright et al. (2014a) used this approach with a physics-based distributed hydrologic model for FFA in a heavily urbanized watershed, demonstrating its usefulness in evaluating multi-scale flood response.

RainyDay is an open-source, Python-based SST software that couples SST methods with rainfall remote sensing data. A more detailed description can be found in Wright et al. (2017); not all of its features are used in this study. The following steps describe how RainyDay is used here:

- 1. We define a 6-degree (longitude) by 4-degree (latitude) geographic transposition domain ( $40^{\circ}$  to  $44^{\circ}$  N,  $90^{\circ}$  to  $96^{\circ}$  W;
- 5 blue dash line of Fig. 1 inset) which encompasses the Turkey River watershed. This same domain was used in Wright et al (2017) and, importantly for the SST approach, extreme rainfall properties are roughly homogeneous within it.
  - 2. The RainyDay software creates a "storm catalog" from 15 years of Stage IV (69 years of CPC) precipitation data that consists of the 450 (2070) most intense precipitation event within the transposition domain. These intense storms are in terms of 96-hour rainfall accumulation and have the same size, shape, and orientation of the Turkey River watershed,
- 10 which is oriented roughly northwest-southeast and with an area of 4002 km<sup>2</sup>. In order to avoid overlapping storms, these selected events must be separated by at least 24 hours. Storms that exhibit "radar artifacts" such as major bright band contamination or beam blockage are excluded from subsequent steps.

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- 3. The RainyDay software generates a Poisson-distributed integer *k* that represents a "number of storms per year." The rate parameter  $\lambda$  of this Poisson distribution is calculated by dividing the total number of rainfall events in the storm catalog by the number of years in the historical rainfall record (*e. g.*  $\lambda = 450/15 = 30.0$  storms per year).
- 4. RainyDay randomly selects k storms from the storm catalog and transposes the associated rainfall fields within the transposition domain by an east-west distance  $\Delta x$  and a north-south distance  $\Delta y$ , where  $\Delta x$  and  $\Delta y$  are drawn from a twodimensional Gaussian kernel density estimate based on the locations of the original storms in the storm catalog. For each of the k transposed storms, the time series of rainfall over the Turkey River watershed is computed. It must be noted that some of the k transposed storms may not "hit" Turkey River watershed, and thus their calculated watershed rainfall are zero. Steps 3 and 4 can be understood as temporal resampling of observed rainfall events to "synthesize" a hypothetical year of rainfall events over the transposition domain and, by extension, over the watershed. Although the rainfall events for the "synthetic" year do not form a continuous series, the dates associated with each observed storm event are recorded, thus facilitating seasonally-consistent flood simulations.
- 25 5. All k events within a synthetic year are assigned a new, randomly selected year from 1948-2016 (2002-2016) for CPC (Stage IV) rainfall data which used to select antecedent conditions. This ensures that the k rainfall events are all "embedded" within a single realistic annual representation of watershed conditions. This ensures that "wet" and "dry" years in terms of snowpack and soil moisture can potentially produce wet or dry years of flood response. Antecedent conditions are randomly selected from within seven days of the updated storm date to ensure realistic seasonality of storms
- 30 and watershed conditions. A storm that occurred on 15 July, 2016, for example, could be paired with initial conditions selected from a date ranging between 8-22 July from a randomly selected year, while the remaining k-1 events would be paired with seasonally appropriate initial conditions from the same selected year.
  - RainyDay repeats Steps 3-5 500 times to create one realization of 500 synthetic years of rainfall events for Turkey River. Twenty such realizations of 500 synthetic years each are generated. Unlike in the existing version of RainyDay, all rainfall

events within a synthetic year are retained for subsequent event-based flood simulations, since the modulating effects of antecedent conditions mean that the largest rainfall event in a given year does not necessarily produce that year's largest flood peak (this is explored in Sect. 5.4).

## 4.3 Event-Based Flood Simulation

- 5 Using the seasonally-consistent "paired" watershed initial conditions derived from CS (Sect. 4.1) and SST-based rainfall events (Sect. 4.2), HBV simulates the "event peak" (the maxima daily discharge). The largest peak among the *k* events that comprise a synthetic year represents the simulated annual maximum daily streamflow. This process is repeated for all 500 synthetic years within each realization, resulting in 500 annual maximum streamflow values, which are then ranked in descending magnitude. The annual exceedance probability  $p_e$  (i.e. the probability in a given year that an event of equal or greater
- 10 magnitude will occur) of each maximum streamflow are calculated by dividing its rank by 500 (the total number of simulated annual maximum daily streamflow). The twenty realizations provide estimates of variability for each flood quantile.

## 5. Results

## 5.1 Hydroclimatology and Nonstationarity

Four distinct time periods (Fig. 3a) are considered for analyzing the changing hydroclimatology in Turkey River: the USGS
daily mean streamflow period of record (1933-2016), a more recent period of apparent elevated flood activity (1990-2016), the period of the Stage IV rainfall record (2002-2016), and the period of the CPC rainfall record (1948-2016). Results here and in subsequent subsections "align" with one or more of these time periods.

The hydroclimate of Turkey River is changing, as shown using the Mann-Kendall (MK) test for monotonic trends (Mann, 1945), a nonparametric method used to determine trend direction and significance (Table 2). Since 1948, annual precipitation and discharge show significant increases (*p*<0.05) and their variability has also increased, while annual maximum daily

discharge has decreased, though not significantly. It is important to note, however, that there are two counteracting seasonal trends (see also Fig. 3a): annual daily discharge maxima have decreased significantly in March-April, but have increased somewhat in May-September. Thus, the lack of statistically significant change in annual maximum daily discharge in Turkey River masks changes in the seasonality of flooding.

**Table 2.** Mann-Kendall trend test (two sided) for hydrological variables. *p*-values are given in parentheses; bolded values are significant at the 5% level. Analyses of trends in variances examine changes in the absolute values of residuals obtained from a linear regression using the Thiel-Sen estimator (Sen, 1968).

Data	Time Range	Trend
Annual Discharge	1933-2016	† ( <b>0.001</b> )
Annual Max. Daily Discharge	1933-2016	↓ (0.447)
Variance of Annual Max. Daily Discharge	1933-2016	↑ (0.056)
Annual Max. Daily Discharge in March-April	1933-2016	<b>↓</b> (0.002)
Annual Max. Daily Discharge in May-September	1933-2016	↑ (0.089)
Annual Precipitation	1948-2016	† ( <b>0.003</b> )
Annual Max. Daily Precipitation	1948-2016	↑ (0.362)
Annual Max. 4-day Precipitation	1948-2016	↑ (0.419)
Annual Mean Temperature	1948-2016	↓ (0.462)
March-May Mean Temperature	1948-2016	↑ (0.443)

We examine this flood seasonality, both in observations and in our continuous HBV simulations (Fig. 3b). The seasonal

- 5 distribution of flood occurrence for 1948-2016 shows a March-April maximum, with elevated flood activity continuing through May and June. This is distinct from, though overlaps somewhat with the seasonality of both the four-day annual maxima of rainfall, which occur most frequently in the June-September period, and simulated daily annual maxima soil moisture, which only tend to occur in March-April. These results highlight that flood activity is the product of seasonal variations in both soil moisture and rainfall. (Four-day rainfall shown in Fig. 3b since it is used in SST; seasonality in one-day rainfall is similar;
- 10 results not shown).

The March-April peak of flood occurrence corresponds with relatively high soil moisture associated with snowmelt, rain on or frozen soil, and frequent spring rains. The secondary peak of flood occurrence in May-June is associated with larger flood magnitudes (including the flood of record, in 2004) due to organized thunderstorm systems. Widespread flooding in Iowa in June 2008 showed that such thunderstorm systems make critical contributions to the upper tail of flood peak distributions in

15 the region (Smith et al., 2013). Although the frequent August-September heavy rainfall events evident in Fig. 3b have not triggered any recorded annual flood peaks in Turkey River, our process-based FFA demonstrates that they may still relevant to current and future flood frequency, as shown in Sect. 5.4.

The largest annual maxima (over 800 m<sup>3</sup> s<sup>-1</sup>) occur in May-July (Fig. 3c), consistent with the broader climatology of flooding in Iowa (Smith et al., 2013; Villarini et al., 2011). Furthermore, both the seasonality and magnitude of flood peaks have shifted

20 since approximately 1990 (Fig. 3a, 3c), with March-April (May-September) floods decreasing (increasing) in magnitude, leading to a shift in the seasonality of the overall distribution of annual maxima daily streamflow from a high in March prior to 1990 to a prolonged high from April to June post-1990. Although the small sample size of the annual maxima daily discharge during this elevated 1990-2016 late-spring and summertime flood period may affect the reliability of the derived distribution of flood occurrence, Park and Markus (2014) also reported a significant shift toward summertime flooding in the nearby

Pecatonica River. Statistically based FFA (including nonstationary methods) based on annual maxima discharges may fail to capture the impact of this shifting seasonality on flood frequency.



Figure 3. (a) Linear trends for two groups of annual maxima daily discharge: March-April floods (blue) and May-September floods (red) using the nonparametric Thiel-Sen estimator (Sen, 1968). The October-February maxima daily discharge are in black dots and its trend line is not calculated because only nine annual maxima occur during this period. The four critical time ranges are shown in black lines. (b) Occurrence densities of the date during the year for the observed annual daily maxima discharge, observed annual 4-day maxima precipitation, and simulated annual daily maxima soil moisture in Turkey River watershed from 1948 to 2016. (c) The magnitude and date during the year for annual flood peaks (black dots)and sample probability density functions (PDFs) for flood in different periods (1933-1989, 1990-2016). In this study, all probability densities for occurrence date are estimated using Gaussian kernel smoothing.

#### 5.2 Model Validation

We validated the performance of continuous HBV simulations with respect to flood seasonality, frequency of annual daily discharge maxima, and normalized peak flow (i.e. the simulated or observed daily discharge divided by the 2-year flood),

15 using both Stage IV and CPC as precipitation inputs (Fig. 4). We also validated two model structures: one with and the other

without the HBV snowpack module. The purpose for this latter validation effort is to highlight the importance of proper process representation (and subsequent validation) in process-based FFA.

Simulated flood seasonality varies substantially during the CPC period of record (1948-2016) depending on the inclusion of the snowpack routine (Fig. 4a). Differences are less for the Stage IV period of record (2002-2016), due to the decreasing role

- 5 of snowpack in deriving the floods in recent years (Fig. 4b). In both cases, the seasonality of flooding simulated using HBV is improved with the inclusion of the snowpack module, with a higher (lower) frequency of springtime (summertime) floods which more closely resembles observations. Empirical (i.e. plotting position-based) distributions for the simulated annual daily discharge maxima are mostly within the 90% confidence interval (obtained by nonparametric bootstrap) of the observations (Fig. 4c, 4d). CPC-based simulation results differ considerably depending on the inclusion of the snowpack module for more
- 10 common events, but differences in simulated maxima vanish as flood magnitude increases (e.g. AEP<0.1). This is because the most extreme flood events occur later in the season and are thus independent of snowpack or snowmelt processes. Differences are generally negligible between Stage IV-based simulations with and without snowpack, since floods in this more recent period are generally driven by summertime thunderstorms. These findings are consistent with the general understanding of the regional seasonality of flooding in the region, as discussed in Sect. 5.1.</p>
- 15 We compared all simulated and observed flood peaks that can be associated with a USGS observed daily streamflow value that is at least three times the mean annual daily discharge (Fig. 4e, 4f). When associating simulated and observed flood peaks, we look within a 2-day window to allow for modest errors in simulated flood peak timing. All peaks in Figs. 4e and 4f are normalized by the median annual (i.e. 2-year) flood, which, as a rule of thumb, can be considered as the "within bank" threshold. Again, HBV with the snowpack routine outperforms the model without it, especially for the small to modest flood
- 20 events in CPC-based simulations. The model without snowpack underestimates small to modest flood events in two cases due to the neglect of potential snowmelt contributions. While modest scatter exists in the Stage IV-based simulated peaks, there is no obvious systematic bias with event magnitude when the snowmelt routine is included. The good performance of the Stage IV simulations suggests that, when focusing on the recent period of elevated flood activity, Stage IV may be a more suitable rainfall input than CPC-Unified. In addition, CPC rainfall is known to contain errors in the extreme tail, due to gage
- 25 "undercatch", insufficient gage density to properly sample convective rain cells, and spatial averaging of such cells over large areas, which effectively reduces peak rainfall depths.



**Figure 4.** HBV model validation for flood seasonality (**a**, **b**), frequency of annual max. daily discharge (**c**, **d**) and normalized peak flow (**e**, **f**) for CPC and Stage IV-based continuous simulations. Model validation is performed for HBV simulations with and without using CPC for 1948-2016 (**panels a, c, e**) and Stage IV for 2002-2016 (**panels, b, d, f**). The 90% confidence intervals for the empirical distributions of observed maximum daily discharges (**c, d**) are derived using nonparametric bootstrapping. Flood peak discharge in (**e**) and (**f**) is defined as a data point with USGS observed value that is at least three times the average observations. Peak discharges are normalized by the median of annual daily discharge maxima (i.e. the 2-year flood). Straight solid black lines indicate 1:1 correspondence, while dashed lines denote an envelope within which the modeled values are within 50% of observed.

We also validate HBV's snowpack routine using observed GHCN daily snow depth for two simulation periods (Fig. 5a, 5b) and using USGS daily streamflow observations for Stage IV-based period (Fig. 5c). Because of their differing spatial resolutions and physical representations, point-scale GHCN daily snow depths cannot be directly compared to the watershed-scale snow water equivalent simulated by HBV. Instead, we validate snowpack simulations in terms of the snowpack occurrence, defined as the number of nonzero snowpack on a particular date divided by the total number of years in the historical or simulated record. For example, there are 50 days in the GHCN observations when snowpack is present on January 1st in the 69-year period from 1948-2016, thus the occurrence rate is 0.72 (50 divided by 69). The HBV model with the



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**Figure 5.** Percentage of days with nonzero snowpack present in observations and simulations (**a**, **b**) and hydrograph validation for Stage IVbased simulation (**c**). For each day within a year, the percent with nonzero snowpack is calculated as the ratio of the number of years in which snowpack is present on that day to the total years (69 years for CPC and 15 years for Stage IV). Observed and simulated hydrographs are normalized by the median annual flood, which is indicated by the dashed blue line.

Model hydrograph validation is provided in Fig. 5c for the Stage IV period (2002-2016), when major flooding occurred throughout Iowa. Model performance shows no obvious evidence of systematic bias in the streamflow simulations (see also Fig. 4f). Although flood seasonality derived from Stage IV-based simulation differs slightly from observations (see also Fig. 4a), these mismatches are associated with flood events smaller than the median annual flood (blue dash line in Fig. 5c). Stage

IV-based simulations do not show bias flood magnitude in late summer. In other words, remaining biases in terms of flood seasonality generally correspond with frequent, small-magnitude events that are typically of less interest in FFA. We therefore conclude that the HBV model with snowpack is generally suitable for subsequent process-based FFA.

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#### 5.3 Flood Frequency Analyses

RainyDay-based flood frequency distributions for Turkey River at Garber using both Stage IV and CPC precipitation are compared with the distribution based on statistical analyses of discharge observations using 1933-2016 USGS annual maxima daily streamflows (Fig. 6). The latter is estimated using the HEC-SSP software (Bartles et al., 2016), which implements

- 10 methods from Bulletin 17B (Interagency Advisory Committee on Water Data, 1982) using "station skew" to fit the log-Pearson Type III distribution. Observed annual daily streamflow maxima from 1933 to 2016 are also shown, where plotting position  $(p_e)$  is estimated using the Cunnane plotting position (Cunnane, 1978). As mentioned above, different HBV parameters are used for the Stage IV and CPC-based simulations; this is necessary due to the differing time periods and error properties of these two precipitation datasets.
- 15 The Stage IV-based flood frequency curve agrees reasonably well with the Bulletin 17B results for  $p_e > 0.3$  (left panel of Fig. 6), but yields higher estimates for rarer events. The CPC-based curve, on the other hand, matches closely with Bulletin 17B. The Stage IV analyses use shorter but more recent (2002-2016) meteorological and hydrological records than the other frequency curves. When streamflow observations are divided into two groups (1933-1989 and 1990-2016), it becomes clear that the recent peak flood observations align well with the Stage IV-based SST results (right panel of Fig. 6). This, along with
- 20 the increasing trend of annual mean precipitation and discharge shown in the previous subsection, suggests that, despite the relatively short (15-year) rainfall record used, Stage IV- driven process-based FFA adequately reflects flood frequency in the wetter recent climate (a similar result is shown in Wright et al., 2017), while the CPC-based and Bulletin 17B methods, both based on much longer data records fail to do so.

The results shown in Fig. 6 suggest that the recent shift from spring to summer flood activity is accompanied by a substantial

- 25 shift in the flood frequency distribution. The close agreement between process-based results using CPC and the statisticallybased analysis using Bulletin 17B suggests that even in stationary situations with long records, statistical methods do not necessarily produce superior results to process-based approaches. Process-based FFA using CPC precipitation from 2002-2016 closely resembles the Stage IV-based FFA (results not shown), suggesting that rainfall process nonstationarity, rather than differences between different input datasets, are the primary drivers of the differences in the CPC-based and Stage IV-
- 30 based results in the left panel of Fig. 6.



Figure 6. Peak discharge analyses for Turkey River at Garber, IA. (a) RainyDay with Stage IV (2002-2016) and CPC-(1948-2016) rainfall and USGS frequency analyses using Bulletin 17B methods. All observed USGS annual maxima daily streamflow from 1933 to 2016 are also shown. Shaded areas denote the ensemble spread (RainyDay-based results) and the 90% confidence intervals (Bulletin 17B-based analysis), respectively. (b) Same as (a), but with the USGS observations divided into pre-1990 and post-1990 groups, and replotted to highlight recent changes in flood frequency.

#### **5.4 Simulated Flood Seasonality**

As shown in Sect. 5.1, the recent climatology of flooding in Turkey River watershed shows a peak in flood occurrence during March-April, with elevated activity (including high-magnitude events) continuing through July, reflective of the regional flood

- 10 "mixture distribution" (e.g. Smith et al., 2011). March-April flooding is associated with springtime rains, high soil moisture, and potentially snowmelt processes, while May-July flooding results from warm-season organized thunderstorm systems. It is important that any process-based FFA approach capture the influence of this mixture on the flood frequency curve. The seasonal distribution of simulated flood occurrence and magnitude using Stage IV- and CPC-based results show that most
  - simulated floods in our process-based approach occur between March and June (Fig. 7), in accordance with observed annual
- 15 maxima daily discharge (Fig. 3c). The peak of occurrence using Stage IV is shifted several weeks later than the CPC-based results, which agrees with the recent shift in seasonality of flood observations shown in the Fig. 3c. Although many simulated events still occur in April, our results show the largest peaks occur later, in May-September. This is consistent with Villarini et al. (2011), who showed that warm season organized convective systems are responsible for some of the largest peaks in Iowa.
- 20 Our process-based results show that August-September storms have the potential to cause severe flooding (Fig. 7), despite the lack of large floods during this time of year in the stream gage record. Stage IV- and CPC-based storm catalogs generated by RainyDay include major storms from the surrounding region, including several large late-summer events capable of producing

substantial flood response, and which indeed to induce large floods within our process-based analysis. This suggests that the general lack of major late-summer floods in the watershed's observational record may not be a feature of the "true" (unknown) distribution of flooding in the watershed, but rather due to limited size of the observational record. This result is supported by regional analysis of floods (Villarini et al. 2011) and points to the potential for SST to improve understanding of flood

5 frequency seasonality relative to discharge-based approaches alone.



Figure 7. Time of occurrence during the year for simulated peak discharge in Turkey River at Garber using (a) CPC and (b) Stage IV.

To demonstrate that the discrepancies between the process-based FFA results generated using CPC and using Stage IV- are driven by changes in physical processes, rather than by differences in model structure (i.e. parameter values), we compared

10 FFA results generated using CPC-based for 1948-2016 and 2002-2016, in terms of event rainfall, initial soil moisture, flood type and peak magnitude (Fig. 8). Compared with the 1948-2016 period (Figure. 8a), there are fewer flood events driven by snowmelt or rain-on-snow during 2002-2016 (Fig. 8b) but more driven by rainfall. This is particular true for flood events (larger than 1000 m<sup>3</sup> s<sup>-1</sup>). In addition, some of the rainfall-driven floods from 2002-2016 were caused by relatively low rainfall but high initial soil moisture, in accordance with the significant increasing trend of annual precipitation and discharge (Table 2).



**Figure 8.** The simulated flood magnitude using CPC rainfall during 1948-2016 (a) and 2002-2016 (b) periods, and corresponding antecedent conditions. The blue triangles denote the snow related flood events (e.g. snowmelt was nonzero in the simulation) and grey dots represent the non-snow related flood events (e.g. rainfall driven). The size of the triangles or dots indicate the antecedent soil moisture with higher value in larger shape. The black dash line indicates the 1000 m<sup>3</sup> s<sup>-1</sup> flood magnitudes.

### 5.5 Comparison of rainfall and peak discharge quantiles

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We examined the relationships between the return periods of 96-hour basin-averaged rainfall accumulations and simulated peak discharge for Turkey River at Garber using Stage IV-based results (Fig. 9; CPC-based results show similar patterns and thus are not shown here). Antecedent soil moisture for each simulated event is also shown. Similar to Wright et al. (2014a), Fig. 9 shows that simulated peak discharge quantiles can differ substantially from the rainfall quantiles of the rainfall that produce them. For instance, 500-year ( $p_e = 0.002$ ) rainfall events can cause simulated peak discharges ranging from 11-year ( $p_e = 0.091$ ) to 500-year ( $p_e = 0.002$ ), corresponding to a range in peak discharge of 1072 to 2743 m<sup>3</sup> s<sup>-1</sup>. Peak discharge quantiles are always larger (in terms of return period) than the quantiles of rainfall that produced them in wet antecedent soil moisture conditions, while the reverse is true in for dry conditions. These results also demonstrate that the DS assumption of

15 1:1 equivalency between rainfall and peak discharge quantiles does not hold in Turkey River. Rainfall spatial variability and drainage network structure, which are ignored in this study due to the lumped (i.e. non-distributed) nature of HBV, further complicate the relationship between rainfall and discharge quantiles.



**Figure 9.** Relationships between rainfall and simulated peak discharge return periods estimated via our process-based method using Stage IV rainfall data. Spearman rank correlation  $\rho_s$  is given. Color indicates the normalized modeled antecedent soil moisture value calculated as <u>soil moisture-min.soil moisture</u> \* 100%.

- 5 We further examine the relationship between annual rainfall and annual flood peak maxima. In Sect. 2.2, we pointed out that DS methods utilize IDF curves, which are usually estimated using annual maxima from rain gage records and which depict quantiles from the distribution of annual rainfall maxima. DS methods use quantiles from this distribution to generate flood estimates, implicitly assuming that annual rainfall maxima produce annual discharge maxima. In our process-based FFA approach, we do not assume that annual discharge maxima are the result of the largest rainfall event of the year. Rather, lower-
- 10 magnitude rainfall events, combined with high soil moisture, could produce the highest discharge. Table 3 shows the percentage of annual peak flow driven by annual maximum gains with increasing return period for both CPC-based and Stage IV-based results. For simulated peak flow with  $p_e > 0.01$ , a large portion of simulated annual peak flow is not caused by the annual maximum rainfall. For rarer peak flows ( $p_e \le 0.01$ ), over 90% of these flood events are driven by the annual maximum rainfall, pointing to the fact that the tail of flood peaks is driven by extreme rainfall, with antecedent conditions playing a
- 15 modulating role.

	Driven by Annual Maximum Rainfall			
Return Period	CPC-based results	Stage IV-based		
		results		
1-2	24%	37%		
2-5	32%	45%		
5-10	39%	67%		
10-20	48%	77%		
20-50	60%	80%		
50-100	72%	84%		
100-200	77%	85%		
200-500	93%	95%		

Table 3. Percentages of simulated annual maxima daily flows driven by 96-hour rainfall annual maximum.

#### **6** Summary and Conclusions

Interactions between rainfall, land cover, river channel morphology, and watershed antecedent conditions are important drivers of flood response. Standard approaches to estimate extreme flood quantiles (termed flood frequency analysis; FFA), however,

- 5 often take a superficial view of these interactions, as argued in Sect. 2. This study presents an alternative FFA framework that combines elements of observational analysis, stochastic rainfall generation, and continuous and event-scale hydrologic simulation. We apply the framework to Turkey River, an agricultural watershed in the Midwestern United States that is undergoing significant hydroclimatologic and hydrologic change which is increasing the magnitude of the largest flood events and shifting their occurrence from the spring to summer.
- 10 We use Stochastic Storm Transposition (SST) to create and resample from "storm catalogs" developed from both 15 years of high-resolution bias-corrected radar rainfall and from 69 years of gridded rain gage observations to produce large numbers of rainfall scenarios for Turkey River. These scenarios, when coupled with seasonally realistic watershed conditions, can help to reconstruct the seasonal and secular variations in meteorological and hydrological processes and their interactions, providing an alternative FFA approach which is well-suited to nonstationary environments (see also Sivapalan and Samuel, 2009). While
- 15 statistical approaches can in principle be applied to investigate the impacts of seasonality on FFA (e.g. Ouarda et al., 2006), such methods still do not directly provide process-level understanding of the factors that "shape" flood frequency. Unlike design storm approaches to FFA, the synthetic rainfall scenarios derived by the SST-based procedure do not require any assumptions regarding the spatial and temporal structure of rainfall, since they are driven by the structure and variability of historical observed storms.
- 20 Our analyses show that using the most recent 15 years of rainfall can produce realistic "present-day" flood quantile estimates that reflect the nonstationarities in rainfall and watershed conditions. The use of longer records, both within our procedure and conventional statistical FFA methods, leads to underestimates of current flood frequency due to their inability to represent recent shifts in flood activity in Turkey River. Our results challenge some common FFA assumptions, including the design

storm presumption that rainfall annual maxima produce discharge annual maxima and the assumption of 1:1 equivalence in rainfall and flood quantiles. We paint a more complex picture in Turkey River, in which the shifting seasonality in rainfall and watershed conditions combine to shape the flood frequency. Spatial variability in rainfall structure, soil moisture, land use and watershed morphology, which are ignored in this study due to the use of a lumped hydrologic model, add further complexity

- 5 to the flood-generating processes. The proposed framework can be employed with more sophisticated distributed hydrologic models, thus facilitating the examination of rainfall spatial variability and its interactions with other factors (e.g. heterogeneous watershed characteristics and river network processes; Zhu et al., 2018; Viglione et al., 2010b, 2010a). This coupling may prove particularly useful for FFA in large watersheds in which there is a practically infinite number of different combinations of such spatially and temporally varying processes that could produce floods—a population that is almost certain to be undersampled in stream gage records and poorly served by design storm assumptions.
- A number of issues remain that make broader usage of our process-based framework challenging. Perhaps the biggest limitation of process-based approaches is the necessity of discharge observations, which are central to both identifying hydrologic changes and to calibrate and validate the hydrologic model. Thus, usage of the approach in ungaged basins may not produce satisfactory results. This issue is fundamental to other FFA techniques as well. Statistically-based discharge
- 15 analyses, for example, similarly rely on streamflow observations, while design storm approaches also require hydrologic model calibration.

We also note that caution is needed when attempting to employ process-based FFA. We were able to produce very similar flood frequency distributions using our approach, regardless of whether or not the HBV hydrologic model's snowpack routine was "turned on" or off (results omitted for brevity), despite very different simulated seasonality of flooding. This highlights

- 20 that process-based frequency analyses can be influenced by poor model process representation that can lead to seemingly "correct" results for the wrong reasons. This implies that the modeler must have sufficient data and experience to recognize such issues. It also illustrates a key issue in FFA using both statistical approaches and process-based methods: flood quantiles, though the product of interactions between physical processes, reveal relatively little about those underlying processes that produce them. This is particularly problematic in changing hydroclimatic or watershed conditions, because nonstationary
- 25 behavior is likely the result of seasonal shifts in one or more processes that may affect flooding in ways that are not well-reflected in observational records. Our results showing that major floods could occur in Turkey River in the late summer under current hydroclimatic conditions, despite their absence in the instrumental record, is one example of this. Failure to recognize and model such shifts could lead to results for past or present flood conditions that appear to be correct, but that may lead to incorrect inferences about future conditions.
- 30 In summary, our framework and results highlight the opportunity and challenge with process-based FFA approaches; namely, that progress on understanding and estimating flood frequency and how it is evolving in an era of unprecedented changes in land use and climate requires better understanding of how the underlying physical processes, and the interactions between them, are changing. Poor model representation of key hydrological processes, however, can lead to incorrect conclusions about present or future flood frequency. Despite the challenge, we share the view of Sivapalan and Samuel (2009) that process-based

approaches hold great potential for advances in FFA research and practice, particularly in projecting future flood hazards in conjunction with data and modeling advances in the climate science community. We do not propose that process-based approaches should necessarily supplant more conventional discharge-based analyses, and acknowledge that discharge observations are essential in such studies. Rather, we anticipate a gradual "merging" of statistical and process-based stochastic

5 simulation techniques as well as of the associated observations and synthetic data.

#### Software and model code

The RainyDay software is available at Github (<u>https://github.com/danielbwright/RainyDay2</u>). A web-based version of RainyDay is available at D. Wright's research group website (<u>http://her.cee.wisc.edu/projects/rainyday</u>).

#### **Competing interests**

10 The authors declare that they have no conflict of interest.

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