# Modelling of shallow water table dynamics using conceptual and physically based integrated surface water-groundwater hydrologic models

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**Abstract.** We present a new conceptual scheme of the interaction between unsaturated and saturated zones of the MOBIDIC (Modello Bilancio Idrologico DIstributo e Continuo) hydrological model which is applicable to shallow water table conditions. First, MODFLOW was coupled to MOBIDIC as the physically based alternative to the conceptual groundwater component of the MOBIDIC-MODFLOW. Then, assuming a hydrostatic equilibrium moisture profile in the unsaturated zone, a dynamic water table level dependent specific yield was added to MOBIDIC-MODFLOW and calculation of the groundwater recharge in MOBIDIC was revisited using a power type equation based on infiltration rate, soil moisture deficit, and a calibration parameter linked to the initial water table depth, soil type, and rainfall intensity. Using the Water Table Fluctuation (WTF) method for a homogeneous soil column, the parameter of the proposed groundwater recharge equation was determined for four soil types i.e., sand, loamy sand, sandy loam and loam under a pulse of rain with different intensities. The fidelity of the introduced modifications in MOBIDIC-MODFLOW was assessed by comparison of the simulated water tables against those of MIKE SHE, a physically based integrated hydrological modelling system simulating surface and groundwater flow, in two numerical experiments: a two-dimensional case of a hypothetical watershed in a vertical plane (constant slope) under a 1cm/day uniform rainfall rate, and a quasi-real three dimensional watershed under one month of measured daily rainfall hyetograph. The comparative analysis confirmed that the simplified approach can mimic simple and complex groundwater systems with an acceptable level of accuracy. In addition, the computational efficiency of the proposed approach (MIKE SHE took 180 times longer to solve the 3D case than the MOBIDIC-MODFLOW framework) demonstrates its applicability to real catchment case studies.

## 1 Introduction

Over the last decades, a number of integrated surface-subsurface hydrologic models have been developed. The main objective of such models is to conceptualize the hydrologic cycle in an integrated way, particularly by coupling the surface and subsurface (unsaturated and saturated zones) hydrological processes. Such integration is particularly important in humid regions where the water table is close to the surface and runoff generation is dominated by variable source area mechanisms (Dunne and Black, 1970; McDonnell and Taylor, 1987). In this runoff generation mechanism, infiltrated water enters the water

table, which rises until it reaches the surface, often in valley bottoms, creating areas where any additional precipitation results in saturation excess runoff (McDonnell and Taylor, 1987). Investigation of such runoff mechanism at the catchment scale can be addressed using physically based models in which the unsaturated zone (UZ) and the saturated zone (SZ) are either explicitly or implicitly coupled. In an explicit coupling approach, a 1D Richards' equation for the unsaturated zone is coupled to a three-

5     dimensional saturated flow. In this approach, it is assumed that flow in the unsaturated zone is only vertical and the groundwater recharge is computed using an iterative water table correction process. MIKE SHE (Refsgaard and Storm, 1995) is an example of such coupling approach. In the implicit coupling of the unsaturated-saturated zones, the whole subsurface flow process is described using a 3D variably saturated flow equation without an explicit distinction in the interaction between unsaturated and saturated zones (Camporese et al., 2010; Kollet and Maxwell, 2006). This approach more truly reflects the

10    physical processes governing flow but is computationally more expensive as compared to explicit approaches, which themselves require considerable computer resources to solve the unsaturated flow equation at the watershed scale. There is a third group of integrated surface-subsurface hydrologic models, namely externally coupled hydrologic models, where, already existing hydrologic and groundwater models are coupled, such as SWAT-MODFLOW (Chung et al., 2010); TOPNET-MODFLOW (Guzha and Hardy, 2010); and GSFLOW (Markstrom et al., 2008). MOBIDIC-MODFLOW, the integrated

15    surface-subsurface hydrologic model developed in this study, belong to that last category of models. Unlike in physically based integrated hydrologic models, the description of the flow in the unsaturated zone in externally coupled models is not based on the Richards equation and their simplified unsaturated-saturated coupling scheme can restrict their applicability in modelling of shallow water table fluctuations.

Seibert et al. (2003) distinguishes three types of interactions between unsaturated and saturated zones based on the water table

20    levels:

Type 1. The water table is relatively deep and there is only one-directional interaction between UZ and SZ. This means the soil moisture state in the unsaturated soil is independent of the groundwater level and the role of groundwater in runoff generation process is not considered.

Type 2. The water table is about at the root zone level. The unsaturated soil can get water from the capillary rise in groundwater

25    so the interaction becomes two-directional as groundwater recharge can be either positive or negative to create hydrostatic equilibrium with the water table. The unsaturated soil profile is assumed to have a constant vertical extension (unsaturated moisture capacity (the maximum amount of moisture the unsaturated layer can hold) is constant during the course of simulations). Such assumptions were made by different hydrological models such as TOPMODEL (Beven et al., 1995), SWAT (Neitsch et al., 2011) and MOBIDIC (Castillo et al., 2015).

30    Type 3. The water table is very close to the surface and unsaturated moisture capacity can no longer be assumed to be constant as the water table fluctuates. This is the case when water table rise results in a decrease in the unsaturated soil moisture capacity and a small amount of the infiltration causes a significant rise in groundwater level (due to the significantly small moisture deficit in unsaturated zone).

The main problems in modelling of type 3 shallow water tables using externally coupled integrated models lies in 1) the assumption of constant specific yield in the saturated flow module of the integrated model is incompatible with the nonlinear decrease in its value as water table rises up to the soil surface; and 2) the assumption of constant vertical extension for the unsaturated zone does not reflect the inverse relation between the unsaturated and saturated moisture storages discussed in (Duffy, 2013; Seibert et al., 2003).

With regard to these limitations, the objective of this study is to propose a series of modifications to the original conceptualization of the unsaturated and saturated flow process of MOBIDIC, in order to extend its applicability for modelling of shallow water table fluctuations while retaining its computational efficiency. To this aim, the conceptual saturated flow scheme of MOBIDIC was replaced with MODFLOW as a physically based three-dimensional groundwater model using the sequential coupling approach (Guzha and Hardy, 2010). Then, a novel methodology for revisiting the calculation of the groundwater recharge in MOBIDIC, the specific yield in MODFLOW, and the interaction between the unsaturated and saturated zones in MOBIDIC-MODFLOW was developed. The fully coupled surface-subsurface model MIKE SHE is used as a reference for comparison; hence the methodology is based on numerical benchmarking on hypothetical and realistic catchments. Using the Water Table Fluctuation (WTF) method (Healy and Cook, 2002) in MIKE SHE, the rises of a shallow water table were simulated under different sets of rainfall intensity, soil property and depth to water table. The simulated responses were then used to reformulate the groundwater recharge of MOBIDIC based on the assumption of a quasi-steady pressure profile in the unsaturated zone as water table fluctuates. The accuracy of the proposed modifications was first evaluated in a two-dimensional case (constant slope), where the simulated water table rises of the two models under a uniform rainfall rate were compared. In a second experiment, the approach was tested at the catchment scale and under unsteady rainfall conditions. Comparison of the simulated water table responses of the MOBIDIC-MODFLOW against those of MIKE SHE allowed us to evaluate how the unsaturated-saturated interaction scheme of the externally coupled models can be adapted for applications in shallow water table regions.

## 2 Water table fluctuation method

The Water Table Fluctuation (WTF) method is a simplified approach for the determination of groundwater recharge of an unconfined aquifer based on groundwater level fluctuations. This method is based on the assumption that the rise in groundwater levels is due to the groundwater recharge (Healy and Cook, 2002). Considering the groundwater budget for a representative element, (Fig. 1), any change in the water table level (groundwater storage) would be due to a combination of recharge to groundwater ($R$), inflow from upstream cell ($Q_u$), outflow to the downstream cell ($Q_d$) and evapotranspiration from groundwater ($ET_{GW}$) as follows:

$$\Delta S_{GW} = R + Q_u - Q_d - ET_{GW} \tag{1}$$

Where $\Delta S_{GW}[LT^{-1}]$ is the change in groundwater storage. Evapotranspiration from groundwater is taken as the direct root water uptake from the saturated zone. Unlike in deep water table conditions, groundwater evapotranspiration in shallow water table regions can be much greater than evapotranspiration from the unsaturated zone (Shah et al., 2007).

Assuming that water table rise is solely due to the recharge of groundwater requires the sum of other fluxes in Eq.1 to be zero. This means that the determination of the groundwater recharge using WTF is best applicable over short periods (hours to days) after onset of rainfall (before any significant redistribution of groundwater recharge to the other fluxes) (Healy and Cook, 2002). Therefore:

$$R = S_y \frac{\Delta h}{\Delta t} \tag{2}$$

Where $S_y[-]$ is the specific yield and $\frac{\Delta h}{\Delta t}$ is the change in water table over $\Delta t$. Application of the WTF method requires an estimation of the specific yield which is defined as the volume of drained water per unit drop in water table and aquifer area (Nachabe, 2002):

$$S_y = \frac{V_w}{A.\Delta h} \tag{3}$$

Where $V_w[L^3]$ is the volume of drained water, $A[L^2]$ is the area of the aquifer and $\Delta h[L]$ is the change in water table level. The specific yield is also defined as the difference between water contents at saturation $\theta_{sat}$ and at field capacity $\theta_{fld}$ (the moisture level below which water cannot be drained by gravity (Nachabe, 2002)). Such constant value for specific yield, however, holds only for deep water tables where changes of the soil moisture profile in the unsaturated zone due to water table drop are relatively small and the volume of drained water can be approximated as $(\theta_{sat} - \theta_{fld}) \times \Delta h$ (Fig. 2a). In shallow water tables however, the specific yield is small (in Fig. 2b, shaded area is smaller than $(\theta_{sat} - \theta_{fld}) \times \Delta h$) and approaches zero when the capillary fringe zone extends up to the soil surface (Nachabe, 2002).

## 3 Models description

### 3.1 MIKE SHE

MIKE SHE is one of the widely used physically based integrated surface-subsurface hydrological model for a wide range of spatiotemporal applications ranging from detailed theoretical (single soil column) to operational watershed scale studies (Graham and Butts, 2005). It has a modular structure for computation of the hydrological processes with different levels of complexity, which is advantageous particularly in large-scale watershed studies (Kollet et al., 2017). A detailed description of the computation of the hydrological processes in MIKE SHE can be found in Storm (1991) and DHI (2014). We present only the computation of flow in the unsaturated and saturated zones and their coupling approach.

### 3.1.1 Unsatuarted flow

The unsaturated flow is described using the one dimensional Richards' equation as (Downer and Ogden, 2004):

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z}\left(k(\theta)\frac{\partial \psi}{\partial z}\right) + \frac{\partial k(\theta)}{\partial z} - S(z) \tag{4}$$

where $\theta[-]$ is the volumetric water content, $k(\theta)[LT^{-1}]$ is the unsaturated hydraulic conductivity, $\psi[L]$ is the pressure head in unsaturated soil, $z[L]$ is the elevation in vertical direction, and $S[T^{-1}]$ is a sink term (e.g. root extraction). The numerical solution of the Richards' equation is based on the implicit finite difference method in which the soil layer is discretized into the computational nodes and the discretized equation is solved with prescribed upper (rainfall rate or ponded water) and lower (water table level) boundary conditions (DHI, 2014). The main challenge with solving the Richards' equation is the computational burden, as it requires fine discretizations in terms of space and time (time steps of seconds to minute). This can be problematic particularly in long term watershed scale studies.

### 3.1.2 Saturated flow

Saturated flow in MIKE SHE is computed using the three-dimensional saturated flow equation as:

$$\frac{\partial}{\partial x}\left(K_x \frac{\partial h}{\partial x}\right) + \frac{\partial}{\partial y}\left(K_y \frac{\partial h}{\partial y}\right) + \frac{\partial}{\partial z}\left(K_z \frac{\partial h}{\partial z}\right) - Q = S\frac{\partial h}{\partial t} \tag{5}$$

Where $K_x, K_y, K_z\ [LT^{-1}]$ are the saturated hydraulic conductivity along the $x, y$ and $z$ axes, respectively, $h[L]$ is the groundwater head, $Q[T^{-1}]$ is the source/sink term and $S$ is the storativity coefficient$[-]$. The storativity coefficient is either the specific yield, $S_y$, for unconfined aquifers or the specific storage , $S_s$, for confined ones (DHI, 2014). Equation (5) is solved numerically over computational grid squares using the finite difference method with the Preconditioned- Conjugate Gradient (PCG) solver, which is also included in MODFLOW (DHI, 2014).

### 3.1.3 Unsaturated-Saturated zone coupling

The explicit coupling approach implemented in MIKE SHE has the advantage of employing different times steps for each zones (seconds to minutes for UZ and hours to day for SZ), which makes the system computationally less expensive compared to the implicit coupling approach (DHI, 2014). However, employing different time steps for the UZ and SZ may result in the generation of mass balance errors in calculating the water flux between the two zones due to 1) an incorrect value of $S_y$ (recommended value is $\theta_{sat} - \theta_{fld}$) in computing the saturated flow and 2) a fixed water table level while the UZ progresses to the next time step (Storm, 1991). The coupling between UZ and SZ follows an iterative process by which the water table is adjusted until the accumulated mass balance error for the entire soil layer (UZ+SZ) falls below a prescribed threshold. The process also calls for adjusting the soil moisture profile. The groundwater recharge is calculated once the iterative process has converged. It should be noted that $S_y$ is considered as constant in the computational process. The algorithm of iterative adjustments of the water table can be summarized as follows (Storm, 1991):

Step 1) at the beginning of the UZ time step, the accumulated mass balance error for the entire soil layer (UZ+SZ) of a soil column ($E_{cum}$) is calculated.

Step 2) if the accumulated error falls below the acceptable level, the water table does not require any adjustments and groundwater recharge is calculated as follows:

5 $$R = \frac{\partial}{\partial t} \int_{z_h}^{z_g} \theta(z)dz + \sum q_u \qquad (6)$$

Where $R$ is groundwater recharge, $\sum q_u$ is the net inflow to the unsaturated soil. The calculated recharge is applied as the upper boundary condition of the SZ module and simulation advances to the next time step.

Step3) if the calculated error is beyond the acceptable threshold, then the water table adjustment is required. Depending on the sign of $E_{cum}$ the water table will be either raised or lowered.

10    3-a) if $E_{cum} < 0$, it means less water is stored in the profile and therefore water table has to be raised. Using the updated moisture profile in UZ (only the last three nodes of the UZ profile (above water table) are updated), go to step 1 and repeat.

3-b) if $E_{cum} > 0$, it means more water is stored in the profile and therefore the water table is lowered. Using the updated moisture profile in UZ (same as described above only for the three lowest nodes of the UZ profile), go to

15    step 1 and repeat.

The iterative water table adjustment continues until the calculated $E_{cum}$ falls below the acceptable limit. Then the new groundwater recharge is calculated as:

$$R = -\frac{(h^* - h)S_y}{\Delta t} \qquad (7)$$

Where $h^*$ and $h$ are the water table after and prior the adjustments, respectively. The calculated groundwater recharge will

20    then be applied as the upper boundary condition of the SZ module and simulation advances to the next time step.

## 3.2 MOBIDIC

Modello Bilancio Idrologico DIstributo e Continuo (MOBIDIC) (Castelli et al.,2009) is a distributed continuous hydrologic model in which the components of the hydrologic system are conceptualized as a system of inter-connected reservoirs. Such a conceptual formulation of the model makes it computationally more efficient especially in large scale watershed modeling

25    (Castillo et al., 2015). The detailed description of the model is available in Castelli et al. (2009) and Castillo et al. (2015).

### 3.2.1 Unsaturated flow

In MOBIDIC, the unsaturated zone is described by two interconnected reservoirs i.e., the gravity and capillary reservoirs, to account for corresponding gravity and capillary forces in the unsaturated soil. The water content at field capacity ($\theta_{fld}$) is the threshold below which moisture is entirely held in the capillary reservoir. The gravity reservoir interacts with the saturated

30    zone via percolation to the groundwater and it may also redistribute the additional moisture to the downstream cells (lateral flow in the unsaturated zone) (Castillo et al., 2015). The capillary reservoir serves moisture to the plant roots (or evaporation

if there is no plant in the computational grid) and can also take moisture from lower groundwater via capillary rise (Castillo et al., 2015). The moisture capacities of the gravity reservoir and the capillary reservoir, $W_{g_{max}}$ [L] and $W_{c_{max}}$ [L], are defined as (Castillo et al., 2015):

$$W_{g_{max}} = d.(\theta_{sat} - \theta_{fld}) \tag{8}$$

5  $$W_{c_{max}} = d.(\theta_{fld} - \theta_{res}) \tag{9}$$

where $d[L]$ is the unsaturated soil thickness and $\theta_{sat}[-], \theta_{fld}[-], \theta_{res}[-]$ are the water content at saturation, field capacity and residual, respectively, which are determined based on soil texture classification (Rawls et al., 1982). At each time step, water available for infiltration (net precipitation plus the ponded water on the soil surface) is determined. The infiltration rate takes the minimum value among the saturated hydraulic conductivity, the allowable

10  moisture capacity in gravity reservoir and the available water. The infiltration rate, however, might be underestimated for low permeable soils in dry conditions when the capillary force at the soil surface is not negligible Castelli (1996). The gravity reservoir is replenished by the infiltrated water. Absorption flux (moisture that is extracted by from the gravity reservoir to the capillary reservoir) is calculated as (Castillo et al., 2015):

$$Q_{as} = \min\left\{W_g + I, \kappa\left(1 - \frac{W_c}{W_{c,max}}\right)\right\} \tag{10}$$

15  Where $\kappa[T^{-1}](0 \le \kappa \le 1)$ is a linear coefficient that controls the rate of the moisture transfer between the two reservoirs. Finer soils typically have higher $\kappa$ value because of low downward moisture gradient. The groundwater recharge ($Q_{per}$) is calculated as (Castillo et al., 2015) :

$$W_{g,u} = W_g + I - Q_{as} \tag{11}$$

$$Q_{per} = \begin{cases} \min\left\{\gamma\ W_{g,u}, \frac{\left[W_{g,u}+\left(\frac{z_w}{d}-1\right)W_{g,max}\right]}{dt}\right\} & if\ z_w \ge 0 \\ \min\left\{\frac{(W_{g,max}-z_w-W_{g,u})}{2dt}, (W_{g,max} - W_{g,u})/dt\right\} & if\ z_w < 0 \end{cases} \tag{12}$$

20  Where $z_w[L]$ is the depth to water table, $W_{g,u}[L]$ is updated moisture in gravity reservoir and $\gamma[T^{-1}](0 \le \gamma \le 1)$ is a coefficient that controls the rate of groundwater recharge. The available moisture storage in the gravity reservoir can also contribute to lateral flux to the adjacent cell and is calculated as (Castillo et al., 2015):

$$Q_{lat} = \beta(W_{g,u} - Q_{per}) \tag{13}$$

Where $\beta[T^{-1}](0 \le \beta \le 1)$ is a coefficient that determines the rate of lateral flow and $W_{g,u}$ is the updated moisture state in

25  gravity reservoir after reduction of groundwater recharge. It should be noted that, as the unsaturated flow is strictly vertical in MIKE SHE, we ignored the lateral redistribution of moisture in gravity reservoir ($\beta$=0) to make the structure of the two models consistent.

### 3.2.2 Saturated flow

Saturated flow in MOBIDIC is described either by a simplified linear reservoir (conceptual scheme) or the Dupuit assumption (Dupuit, 1848). In this study, MODFLOW (Harbaugh et al.,2000) was coupled to MOBIDIC as a physically based three-dimensional finite-difference based alternative groundwater flow model. MOBIDIC and MODFLOW were coupled using the sequential coupling approach in which the groundwater recharge and water table depth act as the boundary conditions of the coupled MOBIDIC-MODFLOW model (Guzha, 2008). At each daily time step, the water table level determined from the solution of MODFLOW in the previous time step is used in MOBIDIC for the calculation of groundwater recharge (equation 12). The calculated groundwater recharge is then applied as the upper boundary condition in MODFLOW and the water table level of the computation grid is updated. Note that, unlike in MIKE SHE, no fine spatiotemporal discretization of the system is required in MOBIDIC-MODFLOW, in which a daily time step has been used.

### 3.2.3 Coupling Unsaturated and Saturated zones

Unlike MIKE SHE, coupling UZ-SZ in MOBIDIC-MODFLOW is not based on an iterative water table correction procedure. Based on the calculated water table level in the previous time step, the recharge to groundwater can be positive (recharge to groundwater) or negative (extraction from groundwater) Castillo (2014). The latter occurs when the saturated storage is bigger than moisture storage in the gravity reservoir ($W_g$). Therefore, the water table in the subsequent time step falls to establish a hydrostatic equilibrium with moisture level in gravity reservoir Castillo (2014). However in the former, groundwater is recharged by a higher moisture level in the gravity reservoir. This results in a rise in water table in the subsequent time step Castillo (2014). During the dry periods, the capillary reservoir may also receive water from the capillary rise from water table which is calculated as (Castillo et al., 2015):

$$Q_{cap} = \frac{\left[\left(\frac{d_w}{\psi_1}\right)^{-n} - \left(\frac{\psi}{\psi_1}\right)^{-n}\right] K_s}{1 + \left(\frac{\psi}{\psi_1}\right)^{-n} + (n-1)\left(\frac{d_w}{\psi_1}\right)^{-n}} \qquad (14)$$

where $d_w [L]$ is the mean distance of the unsaturated layer to water table, $\psi_1 [L]$ is the bubbling pressure, $n [-]$ is the product of pore size distribution index (Rawls et al., 1982) and pore size disconnected index (Brooks and Corey, 1964). The unsaturated soil water pressure ($\psi$) is a function of saturation state of the layer and pore size distribution index ($m$) and is calculated as (Castillo et al., 2015):

$$\psi = \psi_1 S^{-1/m} \qquad (15)$$

$$S = \frac{W_c + W_g}{W_{g_{max}} + W_{c_{max}}} \qquad (16)$$

It should be noted that the capillary rise is computed where the water table is within the soil profile ($z_w \leq d$), otherwise the capillary rise flux will be zero.

In Table 1, the differences between MIKE SHE and MOBIDIC-MODFLOW with regards to the conceptualization of the unsaturated flow, saturated flow, UZ-SZ coupling process, and limitations associated with the application in very shallow

water tables are summarized. Unlike their disparity in describing the unsaturated zone, the two models share similar formulation and numerical solution technique for the saturated flow module. The iterative water table adjustments approach in MIKE SHE, takes into account the variations of specific yield as water table rises/falls. In MOBIDIC-MODFLOW, the specific yield is instead defined as a soil hydraulic parameter and remains unchanged during the course of simulation. This, however, leads to an underestimation of the water table rise as a result of a very small value of specific yield as the water table approaches the ground surface (Abdul and Gillham, 1989).

## 4 Water Table Fluctuation method for a soil column using MIKE SHE

We use the WTF method for a soil column to understand how the rise in groundwater is affected by rainfall intensity, soil type and depth to water table and how much of the infiltrated rain will percolate to the groundwater. The step-by-step procedure is shown in Fig.4. Using a soil column with closed boundaries on the sides and bottom, the rise in groundwater level will be only due to the groundwater recharge (see eqs. 1 and 2). In shallow water table regions, as the water table rises, the specific yield nonlinearly decreases and, therefore, the actual rise in water table might be greater than what would be expected by assuming $S_y = \theta_{sat} - \theta_{fld}$. This is defined as ''reference water table rise'' (see Fig. 3) and is calculated as:

$$\Delta h = \frac{I}{(\theta_s - \theta_{fld})} \tag{17}$$

where $I[L/T]$ is the infiltrated water and $\Delta h[L]$ is the reference water table rise which is the expected rise in water table if the specific yield remains at its ultimate value ($\theta_{sat} - \theta_{fld}$) and the infiltrated water completely reaches to the water table. However, depending on the initial water table level and rainfall intensity, it is possible for the water table rise to be smaller than $\Delta h$ (e.g. for relatively deeper water table and/or low rainfall rate) or that the groundwater recharge takes a value greater than the infiltration rate. The actual water table rise was determined through the coupled unsaturated-saturated flow simulation in MIKE SHE and knowledge of ultimate specific yield allowed the calculation of groundwater recharge using equation 17. Therefore, by defining ($\frac{Re}{I}$) we can evaluate how the rise of the water table is related to the precipitation rate (assuming no infiltration excess runoff), soil hydraulic property, and depth to the water table. $\frac{Re}{I}>1, =, < 1$ means that the actual rise of the water table is larger, equal, or smaller than the reference rise, respectively. Once again, in MIKE SHE, $S_y$ is a constant input of the saturated flow module and changes regarding its value (decrease in its value when depth to water table decreases) is captured by the iterative unsaturated-saturated coupling procedure explained in section 3.1.3. The procedure was repeated for four soil types (see Table 2 for the hydraulic properties) and different rainfall intensities (up to the minimum of saturated hydraulic conductivity of the four soils to prevent infiltration excess runoff generation on the soil surface) to further investigate the significance of the rise in the water table of soil types with different characteristics in response to a given pulse of rain. In shallow water tables, loamy soils with larger capillary fringe range have substantially smaller specific yield values which result in a higher rise of water table compared to the sandy soils Gillham (1984). Therefore, its actual rise in the water table is expected to be larger than the reference rise. However, as loamy soils have smaller hydraulic conductivities compared to sand,

their water table response will be delayed especially for deep water tables. To avoid this delayed response, we focused our analysis to cases where the initial depths to the water table are at a maximum of 1.5m. Computational time steps were one second and one minute for UZ and SZ, respectively to avoid numerical instabilities in the simulated water tables by MIKE SHE.

5 **4.1 Simulation results**

Simulation results of the water table rises are shown in Fig. 5. Each dotted curve in the plots is associated with a specific initial depth to water table (ranging from 0.3 m to 1.5 m) and rainfall rate. The plots in Fig.5 are divided into two zones i.e., $\frac{Re}{I}>1$ (water table rise exceeds the reference rise, red dots) and $\frac{Re}{I}<1$ (water table rise is less than the reference rise, blue dots). Whereas the lower bound of the chosen initial depth to water table in Fig. 5 is 1.5m, the upper bound changes from 0.3 m for

10 sand to 0.9 m for loamy soil. This is due to the differences in water retention characteristics of the soils and initial moisture deficit in unsaturated zone. For example, in sandy soil with 30 cm initial depth to water table (capillary fringe is 15.98 cm), the moisture deficit is 14.98 mm. So, for the infiltration rate bigger than this value, the unsaturated soil becomes completely saturated and water table rises up to the soil surface as it can be seen in Fig. 5 (the upper curve ends at a rainfall rate of about 15 mm/day). The same argument applies to the other soil types. For loamy soil with capillary fringe value of 40.12 cm, the

15 initial depth to water table of 90cm corresponds to the moisture deficit of 23.97 mm in unsaturated zone. Therefore, the upper curve for loamy soil ends at this depth to water table and rainfall intensity.

For a given initial water table level, moving from low to high rainfall intensities results in increasing the ratio of recharge to infiltration, shifting from a situation where $\frac{Re}{I}<1$ (blue dots) to $\frac{Re}{I}>1$ (red dots). Also, while the case where $\frac{Re}{I}<1$ is more common in sandy soils, the opposite is found as soil texture becomes finer (e.g. loamy soil). This means that the actual water

20 table rise in fine textured soils (loamy sand to loam) is almost always larger than would be expected based on using a constant value for specific yield = $(\theta_{sat} - \theta_{fld})$.

Note that for all soil types analyzed, the $\frac{Re}{I} > 1$ values show small sensitivity to increases in rainfall intensity as the depth to water table gets larger, e.g. in sandy soils and loamy soils when the water table is deeper than 50cm and 1 m, respectively. This can be attributed to the existence of significant initial soil moisture deficits found at larger initial water table depths. On

25 the other hand, as the water table gets closer to the soil surface, an increase in the rainfall rate generates a significant water table rise, yielding to a substantial increase in $\frac{Re}{I}$. This demonstrates the importance of the soil moisture deficit (and its ratio to the precipitated rainfall) in significance of water table rise.

## 5 Changes in conceptualization of the UZ-SZ interactions in MOBIDIC-MODFLOW

As discussed in section 3, MOBIDIC's unsaturated soil depth ($d$ in Eqs.(7) and (8)) remains constant during the course of a simulation (both in rainy and subsequent draining periods). This is due to its conceptualization of UZ and SZ as their interaction is not aimed to address the reverse relationship between them in very shallow water table cases. The proposed changes in this paper aim to make the model applicable for such cases. The changes are as follows:

1-It is assumed that the unsaturated soil layer thickness, $d$, is no longer a constant input of the model and changes with water table fluctuations. Hence, the total moisture capacity of the reservoirs ($W_{g_{max}}$ and $W_{c_{max}}$) are determined similarly as in Eqs. (7) and (8), but with replacing $d$ by the depth to water table ($z_w$). Therefore, water table rise/fall results in a decrease/increase in moisture capacities of the reservoirs. Such assumption is valid when groundwater level is treated as a moving boundary and there is a continuous transfer of moisture between the unsaturated and saturated zones.

2-The specific yield in calculation of groundwater head by MODFLOW, is determined based on a soil water retention model (e.g. Brooks and Corey, 1964) and hydrostatic equilibrium assumption in unsaturated zone (suction profile in unsaturated zone changes from steady state to another over the changes in water table) (Hilberts et al., 2005) Duke (1972):

$$S_y = (\theta_{sat} - \theta_{res})\left\{1 - \left(\frac{\psi_1}{z_w}\right)^m\right\} \qquad z_w > \psi_1 \tag{18}$$

Where $z_w$ is depth to water table and other variables are as defined above. Validity of hydrostatic equilibrium assumption is justified in shallow water table regions where redistribution of the infiltrated water is rapid Bierkens (1998). Therefore, with any changes in water table level, specific yield is adjusted for the calculation of groundwater dynamics in the next time step. This is especially important in shallow water table cases as specific yield decreases significantly as water table rises up to the soil surface.

3- The groundwater recharge $R[LT^{-1}]$ is a function of available moisture in the gravity reservoir, unsaturated soil moisture deficit and infiltration rate and is calculated as:

$$R = I\left(\frac{W_g}{1+(Deficit)}\right)^{-\omega} \tag{19}$$

$$Deficit = \left(W_{g_{max}} + W_{c_{max}}\right) - (W_g + W_c) \tag{20}$$

Where $I[LT^{-1}]$ is the infiltration rate, and $\omega[-]$ is a function of soil type, infiltration rate and water table level, which determines how much water will be transferred to the saturated zone. It should be noted that, similar to the original conceptualization of the unsaturated flow in MOBIDIC, only gravity reservoir contributes to the groundwater recharge. The proposed conceptualization of the interaction between UZ and SZ are shown in Fig. 6. Starting with a hydrostatic equilibrium moisture profile in the UZ, the available moisture in the reservoirs, $W_g$ and $W_c$ as well as the moisture deficit of in the unsaturated profile are determined. The rise in water table results in a reduction of the moisture capacities of the reservoirs

$W_{g_{max}}$ and $W_{c_{max}}$, as well as $W_g$ and $W_c$ and the moisture deficit in unsaturated profile. When water table falls, however, there is an increase in these quantities.

## 5.1 Interpretation of the new groundwater recharge equation in MOBIDIC-MODFLOW

To interpret the proposed groundwater recharge equation (Eqs. (19) and (20)), let us first analyze its limit values.

5   As $\frac{W_g}{1+(Deficit)} < 1$, a decrease in $\omega$ results in a decrease in $R$ (and vice versa). The coefficient $\omega$ can be either positive or negative. When positive, recharge to the groundwater reservoir is larger than the infiltration rate and when negative, groundwater recharge is a portion of the infiltration. The specific case for which $\omega = 0$ occurs when R = I. Such flexibility in value range of $\omega$ is important as it makes the model applicable for cases where adding small rainfall amount can cause a significant water table rise, which may occur in humid regions. However, its precise determination can be problematic as it is

10   a complex function of water table level, soil type, and rainfall (infiltration) intensity. In general, for a known water table level, an increase in rainfall rate will require a larger $\omega$ values to match the water table rise of the MIKE SHE and the MOBIDIC-MODFLOW. Equation 19 was calibrated for $\omega$ by using simulated water table rises of MIKE SHE. This allowed investigating how combinations of soil types, rainfall intensities and water table depths influence the behavior of groundwater recharge and how this can be captured using the conceptual UZ-SZ formulation as in MOBIDIC-MODFLOW.

15   **5.2 Simulation results**

Figure 7 displays the values of parameter $\omega$ in Eq. (19) obtained by fitting the water table rises of the MOBIDIC-MODFLOW model to the water table rises simulated by MIKE SHE for the cases presented in Fig. 5. The negative and positive values of $\omega$ are shown in red and blue dots, respectively. It can be seen that for a specified water table level, increasing the rainfall rate requires higher values of $\omega$ to fit the water table rise of MOBIDIC-MODFLOW to that of MIKE SHE. Furthermore, the

20   relationship is nonlinear. This further shows the complexity of the interactions between the UZ and SZ under shallow water table conditions. Note that in sandy soils, most of the $\omega$ values are negative, while the opposite is found for loamy soil. This is because the water table rise for loamy soils are larger than for sandy soils (smaller specific yield and available moisture deficit in unsaturated profile). Comparing the scatterplots in Fig. 7, reveals that that unlike loamy soils, in sandy soils with relatively deeper initial water tables, the changes in $\omega$ (with changes in rainfall rate) is quite small. This is related to the initial

25   moisture deficit in unsaturated profile as discussed in section 4.1.

These $\omega$ values are arranged in a look-up table that can be used to simulate the UZ-SZ interactions in MOBIDIC-MODFLOW in the following way: at each time step, based on the specified water table depth, soil type and rainfall rate, a value of $\omega$ is obtained by interpolation from the look-up tables. The determined $\omega$ are then used for calculation of the groundwater recharge using Eq. (19). The groundwater recharge is then applied as the upper boundary condition to the saturated computation layer.

30   Using the specific yield calculated with Eq. (18), MODFLOW updates the groundwater head and water table level values. The updated levels are then transferred to MOBIDIC-MODFLOW for the determination of moisture storages in the capillary and

gravity reservoirs ($W_g$ and $W_c$). This procedure is repeated for the entire simulation period. The next section compares the performance of the MOBIDIC-MODFLOW model against MIKE SHE in two cases, a hypothetical vertical 2-D slope model and a small a pseudo-hypothetical watershed.

## 6 Application of the modified unsaturated-saturated scheme of MOBIDIC-MODFLOW in two test cases

5 The appropriateness of the proposed changes in the conceptualization of UZ-SZ interactions of MOBIDIC-MODFLOW was tested by comparing its simulated water table results against those of MIKE SHE in two test cases. The description of the test cases follows.

### 6.1 Two-dimensional case

So far, our analysis focused on a single soil column in which the coefficient of the proposed groundwater recharge, $\omega$ (Fig. 7),
10 were determined based on the simulated water table rise by MIKE SHE (Fig. 5). In order to analyze the performance of the proposed approach in cases where there is lateral interaction between saturated computational grids, simulations of the water table rise were performed for a small soil box measuring 14m long, 1.5m high and 1m wide filled by sandy soil identical to the one used in the soil column analysis. The soil box has closed boundary conditions on $x = 0$, $x = 14$m and bottom side and it is assumed that initial water table is $h(x, 0) = 0.2$m. Since the rainfall is continuous during the entire simulation period,
15 configuration of the such boundary conditions results in higher water table rise in the toe of the slope (shallower water table) and generation of saturation excess runoff starting from downhill moving to the uphill. The hillslope is discretized into 28 columns ($\Delta x = 0.5$m) and the vertical discretization of the unsaturated layer in MIKE SHE is $\Delta z = 1$cm. A 10 mm/day constant rainfall is applied for 20 days and the simulated water table rises of the two models are compared.

### 6.1.1 Simulation results

20 The simulated water tables of the two models are shown in Fig. 8. It can be seen that the predicted water tables of the two models are very close. The slight mismatch between the predicted water table heads of the two models can be attributed to the fact that in MOBIDIC-MODFLOW, the response of groundwater to the precipitated water is immediate, that is, within the same time step (one day). This is not the case in MIKE SHE where the simulation time step is much shorter at one second. The saturated length (the length where water table at the soil surface) predicted by the two models are closely matched which
25 shows that the simplifications in UZ-SZ interaction of MOBIDIC-MODFLOW can mimic the complex dynamical interaction between the two zones. Note that the generated saturation excess runoff by two models were removed from the soil surface as the flow routing module was not included in the simulations.

## 6.2 Catchment scale

### 6.2.1 Borden catchment

In order to further evaluate the suitability of the proposed conceptualization of UZ-SZ in MOBIDIC-MODFLOW, the water table fluctuations of the two models at the Borden catchment for the month of May 2015 were compared. The Borden catchment is located approximately 70 km of Northwest of Toronto, Ontario (Jones et al., 2006). The site is about 20m wide and 80m long and it was subjected to several experimental (Abdul and Gillham, 1989) and numerical rainfall-runoff studies (Jones et al., 2006; Kollet et al., 2017; VanderKwaak and Loague, 2001). It is assumed that the catchment consists of a single homogeneous sandy soil identical as the one used in the previous simulations (see Table 2 for hydraulic properties) without any vegetation cover. The motivation for simplifying the watershed physiographic characteristics here was to evaluate the MOBIDIC-MODFLOW in a 'real' watershed, while emphasizing on differences in UZ-SZ dynamics simulated by the conceptual approach as compared to a physically based numerical model.

The digital elevation model (DEM) of the Borden catchment has a spatial resolution of 0.5m and is available at www.hpsc-terrsys.de and is shown in Fig. 9a. The initial water table level was assumed to be at 1m below the catchment's outlet (at elevation 1.98m). The site has closed boundaries on the sides and it has a horizontal bedrock at elevation 0 m. The measured rainfall at the Borden site for May 2015 used in the numerical experiment (data available at Environment Canada, 2015). The rainfall hyetograph (Fig. 11) consists of 10 events with total amount of 77.2 mm and maximum of 24.8 mm at day 25 where a significant rise in water table is expected. The catchment was subdivided into two zones based on the initial depth to water table as shown in Fig. 9b. Zone 1 represents the initial depth to water table less than 1.5m (red zone in Fig. 9b) and cells in zone 2 have the initial depth to water table larger than 1.5m (blue zone in Fig. 9b). The calculation of groundwater recharge and interaction between UZ-SZ followed the modifications presented in section 5 (the $\omega$ parameter in Eq. (19) was made variable for water table levels less than 1.5m) and changes in groundwater head in zone 2 was simulated using the original conceptualization of MOBIDIC explained in section 3.2. Therefore, these two structures together cover the dynamics of the water table for the whole catchment. Note that, for water table depths greater than 1.5m, the moisture capacities of the reservoirs ($W_{g_{max}}, W_{c_{max}}$) remains constant with a rise or fall of the water table (section 3.2). Such distinction based on depth to the water table was made to limit the extrapolation errors associated with the determination of $\omega$ for water table depths larger than 1.5m. Besides, for these zones the assumption of an inverse relationship between the unsaturated and saturated moisture storages is questionable as discussed in the introduction.

### 6.2.2 Simulation results

The difference in simulated water table level of the two models is shown in Fig. 10 for the selected simulation days after the rainy events. The predicted groundwater head of the models at the outlet of the catchment are also compared in Fig. 11. It can be seen that the two models generally compare well.

However MOBIDIC-MODFLOW is slightly predicting a higher water table rise as compared to MIKE SHE following rainfall events (e.g. events on days 11, 18 and 25). This is attributed to the interaction of saturated flow between the two zones (the saturated flow moves from grids in zone 2 to zone 1). The magnitude of the overestimation decreases over the course of simulations (for example the differences in water table levels are smaller at day 23 than day 6). This further shows that how the interaction between the zones with different characteristic of the interaction between the UZ and SZ (zone 1 with inverse relation between the unsaturated and saturated storage and zone 2 with direct relationship between them as classified in the introduction) can affect the overall behavior of the water table fluctuations at catchment scale. Therefore, that the rise in water table in a computational grid is also the result of the net incoming of saturated flow from surrounding grids for both models. That is why the predicted water able in MOBIDIC-MODFLOW is still slightly rising between two rainy days (from day 12 to day 17 and day 19 to day 24) as shown in Fig. 11. Consequently, the simulated water tables of the two models gradually converge in the days following a rainfall event (for example between the days 14 to 17 and 19 to 24) as the transient behavior simulated by MIKE SHE dissipates following a long redistribution period.

# 7 Discussion

The quick rise of the shallow water table in response to the precipitation was also observed in the experimental work of (Abdul and Gillham 1984). In their study, the water table response of a sandy soil packed in a $160 \times 120 \times 8$ cm box with a $12°$ surface slope with different initial water table levels under a uniform rainfall rate was investigated. The objective of the experiment was to evaluate the effect of the capillary fringe on the rise in water table and on streamflow generation. The results revealed that when the water table is very shallow, that is for the downhill regions of the slope where the capillary fringe extended to the soil surface, the water table rise was much greater than expected by the constant specific yield. The uphill regions, with a deeper water table depth, however, showed a delayed response due to the presence of the moisture deficit in the unsaturated zone. The simulated responses using MIKE SHE and MOBIDIC-MODFLOW (Figure 8) are consistent with the findings of (Abdul and Gillham 1984) attesting their capability in capturing the effect of the capillary fringe on the water table rise. Note that the coefficient $\omega$ in MOBIDIC-MODFLOW (Equation 19) changes as the water table level rises/falls and therefore, each computation grid in Figure 8 has a different value for $\omega$ at each time step.

Comparing the simulated water table levels of the two models at Borden catchment (Fig. 10 and 11) attests for the soundness of the proposed UZ-SZ interaction scheme of MOBIDIC-MODFLOW at the catchment scale. The Mean Absolute Error of the predicted water table by MOBIDIC-MODFLOW compared to MIKE SHE for the outlet grid cell is 0.013 m. As the water table rises, the water table could be much shallower than expected by the ultimate value for specific yield ($\theta_{sat} - \theta_{fld}$). Therefore, the inclusion of a water table dependent expression for the specific yield in MOBIDIC-MODFLOW with the proposed groundwater recharge (Eq. (19)) allowed for modelling of such significant water table rise. Note that the modified MOBIDIC-MODFLOW does not have any additional calibration parameters, thereby the parameter uncertainties of the model remain unchanged. Comparison of the original and the modified equations of groundwater recharge in MOBIDIC (Equations

12 and 19, respectively) shows that both equations have only one calibration parameter ($\gamma$ in Equation 12 and $\omega$ in Equation 19). The proposed modifications, however, has the advantage of eliminating specific yield from the calibration parameters of MODFLOW using the water table dependent expression given in Equation 18. The required soil hydraulic parameters for application of Equation 18 is derived based on (Rawls and Brakensiek, 1989) soil texture database. Therefore, the modified MOBIDIC-MODFLOW has one less calibration parameter (specific yield) compared to the original structure of the MOBIDIC-MODFLOW.

In addition, the proposed modifications in the conceptualization of the unsaturated-saturated flow interaction of the groundwater are such that MOBIDIC-MODFLOW has the capability to take into account the inverse relation between the unsaturated and saturated moisture storage using a conceptual and computationally efficient framework. Modelling of such cases have been mostly addressed using physically based numerical models in which the subsurface flow is described either using a three-dimensional variably saturated flow or a one dimensional Richards' equation in the unsaturated zone coupled to a three-dimensional saturated flow equation. However the application of these complex models at the catchment scale can be cumbersome due to the required data and computational burden to run such models. On the other hand, the conceptual shallow water table unsaturated-saturated interaction schemes in the literature e.g., (Seibert et al., 2003) do not allow for capturing of the different water table responses of different soil types to the fallen pulses of precipitation shown in Figure 5. The coefficients of such conceptual models are often determined through the calibration process against few water table observations which does not represent the disparity in water table response of different soil types of the catchment. However, using responses of the physically based model MIKE SHE for the calibration of the new groundwater recharge, it has been possible to model, with a good computational efficiency, the difference in water table response of different soil types of the catchment. Note that, although the coefficient of $\omega$ in Equation 19 in MOBIDIC-MODFLOW was calibrated against the simulated water table responses of MIKE SHE, the model works independently. In this study, the purpose of comparing water table responses of the two models in test cases was to verify whether MOBIDIC-MODFLOW can reproduce the catchment scale simulated water table responses of MIKE SHE as the expected response of the catchment in absence of water table measurements.

An important advantage of the coupled MOBIDIC-MODFLOW presented in this paper lies in its capability to investigate phenomena such as saturation excess runoff without expensive computational burden. The physically based models such as MIKE SHE require very fine discretization of the unsaturated soil domain and require short time steps to avoid numerical instabilities. However, the proposed approach in MOBIDIC-MODFLOW works with identical time steps in both unsaturated and saturated zones, without discretization of the soil layer, which greatly improves the computational process. For example, the execution time for the Borden case took 10 minutes using a PC Core i7 with 8GB of RAM for MOBIDIC-MODFLOW, while taking 30 hours with MIKE SHE. This clearly indicates why such alternative modelling approaches are attractive for watersheds scale modelling purposes

It should be noted that, while coefficient $\omega$ in Eq.(19) was determined for sand, loamy sand, sandy loam and loam, the model was tested for sandy soils where the moisture retention in unsaturated zone is small and the assumption of quasi steady equilibrium moisture profile in unsaturated zone is legitimate, as discussed by (Bierkens, 1998). For finer textured soils,

however, such assumption may be questionable and, therefore, the approach presented in this study must be fully tested over a variety of soil textures to further evaluate its exactitude to broader watershed conditions. In addition to testing the proposed approach over a variety of soil textures, a next step will consist in extending the applicability of the approach against observations in real catchments where other hydrological processes, such as summer-fall evapotranspiration and spring snowmelt, affect groundwater recharge in shallow aquifers.

**8 Conclusion**

In this paper, we have presented a series of modifications to the conceptualization of the unsaturated and saturated flows of MOBIDIC a conceptual hydrologic model to extend its applications to shallow water tables where an inverse relationship between the unsaturated and saturated moisture storages exist. The modifications were: 1) replacement of the model's conceptual saturated flow scheme with MODFLOW; 2) revisiting the conceptualization of the interaction between the unsaturated and saturated zones and calculation of groundwater recharge; and 3) inclusion of a dynamic specific yield based on quasi-steady state pressure profile in the unsaturated zone. The key variables in modelling of shallow water table regions are 1) groundwater recharge and 2) specific yield. Groundwater recharge is usually considered as a function of unsaturated moisture state and is a fraction of infiltrated moisture into the unsaturated soil layer. However in shallow water table cases, its value can be larger than infiltration due to the capillary fringe above the water table, which causes a quick and significant water table rise (Jayatilaka and Gillham,1996). Specific yield in the shallow water table regions is no longer a constant soil property and significantly decreases as water table reaches to the soil surface. Investigation of such cases are mostly addressed using physical based models (e.g. Cloke et al., 2006) or using fully conceptual approaches (e.g. Seibert et al., 2003). Through the coupling of MODFLOW to MOBIDIC, we have modified the unsaturated-saturated flow interaction of the model based on the assumption of quasi-steady pressure profile in the unsaturated zone as water table changes. In turn, the static specific yield in MODFLOW could be replaced with the water table dependent dynamic specific yield such as derived by Duke (1972). Such modifications allowed the rapid and dynamic water table responses of shallow water table regions to be adequately captured. Also, the groundwater recharge in the model was defined with a power type equation whose parameter ($\omega$) was determined using the WTF method along with the physically-based MIKE SHE model for a homogeneous soil column with different initial water table levels under different rainfall intensities. The appropriateness of the proposed changes were evaluated by comparing the simulated water table responses of the model against those of MIKE SHE in a two-dimensional (single slope) case under continuous uniform rainfall rate and in a three-dimensional quasi-real catchment case (simplified Borden catchment) over a month of measured daily rainfall hyetograph. In the light of simulation results, the following conclusions can be derived:

1- Inclusion of a dynamic specific yield in investigation of shallow water table responses is essential. Indeed, when the water table is close to the soil surface, the significance of rise is much greater than would be expected based on the ultimate value of specific yield e.g., $\theta_{sat} - \theta_{fld}$, as investigated by Jayatilaka and Gillham (1996). While in MIKE

SHE, this is accounted for by using the iterative water table correction method, in MOBIDIC-MODFLOW this is addressed by assuming a hydrostatic equilibrium state between UZ-SZ. To the authors' knowledge, this has not been taken into account in simplified coupling of a hydrologic and a groundwater model.

2- The presented analysis showed a complex relation between the water table rise and rainfall rate, soil type, and depth to water tables. The simulation over different rainfall rates and water table levels showed that fine textured soils with large capillary fringe (consequently small unsaturated soil moisture deficit) could have water table at soil surface even with a low rainfall intensity. This is important for the investigation of saturation excess runoff in lowland near river zones of the catchments. Therefore, it is important for the model to distinguish such differences in the expected water table responses of different soil types for its suitability at the catchment scale.

3- The comparison of the simulated water tables of the two models at Borden case (Mean Absolute Error equals 1.3 cm) along with their execution times (30 hours with MIKE SHE against 10 minutes with MOBIDIC-MODFLOW) clearly demonstrates the applicability of simplified approach implemented in MOBIDIC-MODFLOW in investigation of the groundwater-surface water interaction. Further improvements of the approach with inclusion of other hydrological processes such as the effect of evapotranspiration on parameterization of the ($\omega$) in future work will enable its applicability in real, practical applications.

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# References

Abdul, A. S., and Gillham, R. W.: Laboratory Studies of the Effects of the Capillary Fringe on Streamflow Generation. Water Resources Research, 20(6), 691–698. https://doi.org/10.1029/WR020i006p00691, 1984.

Abdul, A. S., and Gillham, R. W.: Field studies of the effects of the capillary fringe on streamflow generation. Journal of Hydrology, 112(1), 1–18. https://doi.org/10.1016/0022-1694(89)90177-7, 1989.

Beven, K. J., Lamb, R., Quinn, P., and Freer, R.: TOPMODEL, in: *Computer Models of Watershed Hydrology* (pp. 627–668), edited by: Singh, Vijay.P, USA: Water Resources Publication, 1995.

Bierkens, M. F. P.: Modeling water table fluctuations by means of a stochastic differential equation. Water Resources Research, 34(10), 2485–2499. https://doi.org/10.1029/98WR02298, 1998.

Brooks, R. H., and Corey, A. T.: Hydraulic Properties of Porous Media. Colorado State University, 1964.

Camporese, M., Paniconi, C., Putti, M., and Orlandini, S.: Surface-subsurface flow modeling with path-based runoff routing, boundary condition-based coupling, and assimilation of multisource observation data. Water Resources Research, 46(2), W02512. https://doi.org/10.1029/2008WR007536, 2010.

Castelli, F., Menduni, G., and Mazzanti, B.: A distributed package for sustainable water management: a case study in the Arno Basin, in: Proceeding of The role of Hydrology in Water Resources Management, Capri, Italy, October 2008, IAHS (Vol. 327, PP. 52-61), 2009.

Castelli, F.: A simplified stochastic model for infiltration into a heterogeneous soil forced by random precipitation. Advances in Water Resources, 19(3), 133–144. https://doi.org/10.1016/0309-1708(95)00041-0,1996.

Castillo, A., Castelli, F., and Entekhabi, D.: Gravitational and capillary soil moisture dynamics for distributed hydrologic models. Hydrol. Earth Syst. Sci., 19(4), 1857–1869. https://doi.org/10.5194/hess-19-1857-2015, 2015.

Castillo, A. E.: Spatiotemporal variability of hydrologic response : an entropy-based approach using a distributed hydrologic model, Ph.D. thesis, Massachusetts Institute of Technology, USA, 189 pp., 2014.

Chenjerayi Guzha, A., and Hardy, T. B.: Simulating streamflow and water table depth with a coupled hydrological model. Water Science and Engineering, 3(3), 241–256. https://doi.org/10.3882/j.issn.1674-2370.2010.03.001, 2010.

Chung, I., Kim, N.-W., Lee, J., and Sophocleous, M.: Assessing distributed groundwater recharge rate using integrated surface water-groundwater modelling: application to Mihocheon watershed, South Korea. Hydrogeology Journal, 18(5), 1253–1264. https://doi.org/10.1007/s10040-010-0593-1, 2010.

Cloke, H. L., Anderson, M. G., McDonnell, J. J., and Renaud, J.-P.: Using numerical modelling to evaluate the capillary fringe groundwater ridging hypothesis of streamflow generation. *Journal of Hydrology*, *316*(1), 141–162. https://doi.org/10.1016/j.jhydrol.2005.04.017, 2006.

DHI: MIKE SHE User Manual, Volume 2: Reference Guide, Danish Hydraulic Institute, 372 pp., 2014.

Downer, C. W., and Ogden, F. L.: Appropriate vertical discretization of Richards' equation for two-dimensional watershed-scale modelling. Hydrological Processes, 18(1), 1–22. https://doi.org/10.1002/hyp.1306, 2004.

Duffy, C. J.: Semi-Discrete Dynamical Model for Mountain-Front Recharge and Water Balance Estimation, Rio Grande of Southern Colorado and New Mexico, in: Groundwater Recharge in a Desert Environment: The Southwestern United States, edited by: Hogan, James F., Philips, Fred M., and Scanlon, Bridget R., American Geophysical Union (AGU), 255–271, https://doi.org/10.1029/009WSA14, 2013.

Duke, H. R.: Capillary properties of soils--influence upon specific yield. Amer Soc Agr Eng Trans ASAE. Retrieved from http://agris.fao.org/agris-search/search.do?recordID=US201302335007, 1972.

Dupuit, J.: Etudes théoriques et pratiques sur le mouvement des eaux courantes suivies de considérations relatives au régime des grandes eaux, au débouché à leur donner, et a la marche des alluvions dans les rivières à fond mobile Carilian-Goeury et Dalmont, France, 1848.

Graham, D., and Butts, M. B.: Flexible Integrated Watershed Modeling with MIKE SHE, in: Watershed models, edited by: Frevert, D., and Singh, V., (pp.). CRC Press, 245–271, 2005.

Guzha, A.: Integrating Surface and Sub Surface Flow Models of Different Spatial and Temporal Scales Using Potential Coupling Interfaces, Ph.D. thesis, Utah State University, USA, 243 pp., 2008.

Harbaugh, A. W., Banta, E. R., Hill, M. C., and McDonald, M. G.: MODFLOW-2000, The U.S. Geological Survey Modular Ground-Water Model - User Guide to Modularization Concepts and the Ground-Water Flow Process, Open File Rep.00–92, 127 pp., 2000.

Healy, R. W., and Cook, P. G.: Using groundwater levels to estimate recharge. Hydrogeology Journal, 10(1), 91–109. https://doi.org/10.1007/s10040-001-0178-0, 2002.

Hilberts, A. G. J., Troch, P. A., and Paniconi, C.: Storage-dependent drainable porosity for complex hillslopes. Water Resources Research, 41(6), W06001. https://doi.org/10.1029/2004WR003725, 2005.

5    Jayatilaka, C. J., and Gillham, R. W.: A deterministic-empirical model of the effect of the capillary fringe on near-stream area runoff 1. Description of the model. Journal of Hydrology, 184(3), 299–315. https://doi.org/10.1016/0022-1694 (95)02985-0, 1996.

Jones, J. P., Sudicky, E. A., Brookfield, A. E., and Park, Y.-J.: An assessment of the tracer-based approach to quantifying groundwater contributions to streamflow. Water Resources Research, 42(2), W02407.

10    https://doi.org/10.1029/2005WR004130, 2006.

Kollet, S.J., and Maxwell, R.: Integrated surface–groundwater flow modeling: A free-surface overland flow boundary condition in a parallel groundwater flow model. Advances in Water Resources, 29(7), 945–958. https://doi.org/10.1016/j.advwatres.2005.08.006, 2006.

Kollet, S., Sulis, M., Maxwell, R. M., Paniconi, C., Putti, M., Bertoldi, G., …, Sudicky, E., : The integrated hydrologic model

15    intercomparison project, IH-MIP2: A second set of benchmark results to diagnose integrated hydrology and feedbacks. Water Resources Research, 53(1), 867–890. https://doi.org/10.1002/2016WR019191, 2017.

Markstrom, S., Niswonger, R., Regan, R., Prudic, D., and Barlow, P.: GSFLOW - Coupled Ground-Water and Surface-Water Flow Model Based on the Integration of the Precipitation-Runoff Modeling System (PRMS) and the Modular Ground-Water Flow Model (MODFLOW-2005), Open File Rep. 6-D1, pp. 254, 2008.

20    McDonnell, J. J., and Taylor, C. H.: Surface and subsurface water contributions during snowmelt in a small Precambrian Shield watershed, Muskoka, Ontario. Atmosphere-Ocean, 25(3), 251–266. https://doi.org/10.1080/07055900.1987.9649274, 1987.

Nachabe, M. H.: Analytical expressions for transient specific yield and shallow water table drainage. Water Resources Research, 38(10), 1193. https://doi.org/10.1029/2001WR001071, 2002.

Neitsch, S. L., Arnold, J. G., Kiniry, J. R., and Williams, J. R.: Soil and Water Assessment Tool, Theoritical Documentation Version 2009 , Technical Report No. 406, Texas Water Resources Institute, pp., 647, 2011.

Rawls, W. J., Brakensiek, D. L., and Saxtonn, K. E.: Estimation of soil water properties. Transactions of the ASAE, 25(5), 1316–1320, 1982.

5  Refsgaard, C. J., and Storm, B.: MIKESHE, in: Computer models of catchment hydrology, edited by: Singh. V.P., Water resources publications, 809-846, 1995.

Seibert, J., Rodhe, A., and Bishop, K.: Simulating interactions between saturated and unsaturated storage in a conceptual runoff model. Hydrological Processes, 17(2), 379–390. https://doi.org/10.1002/hyp.1130, 2003.

Shah, N., Nachabe, M., and Ross, M.: Extinction Depth and Evapotranspiration from Ground Water under Selected Land

10     Covers. Ground Water, 45(3), 329–338. https://doi.org/10.1111/j.1745-6584.2007.00302, 2007.

Storm, B.: Modeling of Saturated Flow and the Coupling of Surface and Subsurface Flow, in: Recent advances in the modelling of hydrologic systems, edited by: D. S. Bowles & P. E. O'Connell, pp. 185–203, Springer Netherlands. https://doi.org/10.1007/978-94-011-3480-4_10, 1991.

VanderKwaak, J., and Loague, K.: Hydrologic-Response simulations for the R-5 catchment with a comprehensive physics-

15     based model. Water Resources Research, 37(4), 999–1013. https://doi.org/10.1029/2000WR900272, 2001.

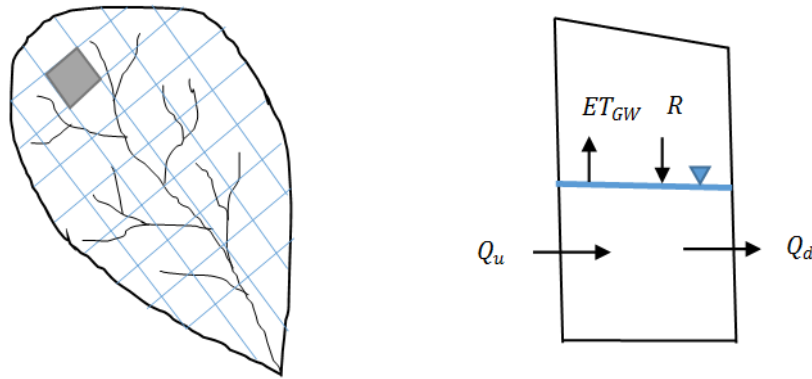
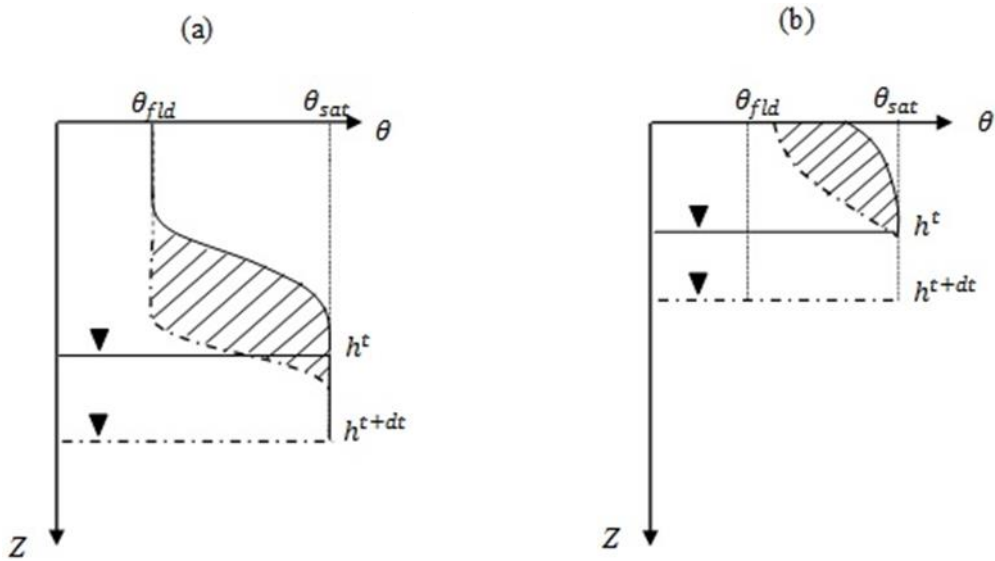



**Figure 1. Schematic view of computational grids in a catchment and corresponding input and output fluxes over the saturated zone.**

10      **Figure 2. Hypothetical soil moisture profile for (a) deep and (b) shallow water tables. The solid and dashed lines are the corresponding profiles before and after water table drops, respectively. The shaded area is the drained water due to a drop in the water table. Modified after Healy and Cook (2002).**

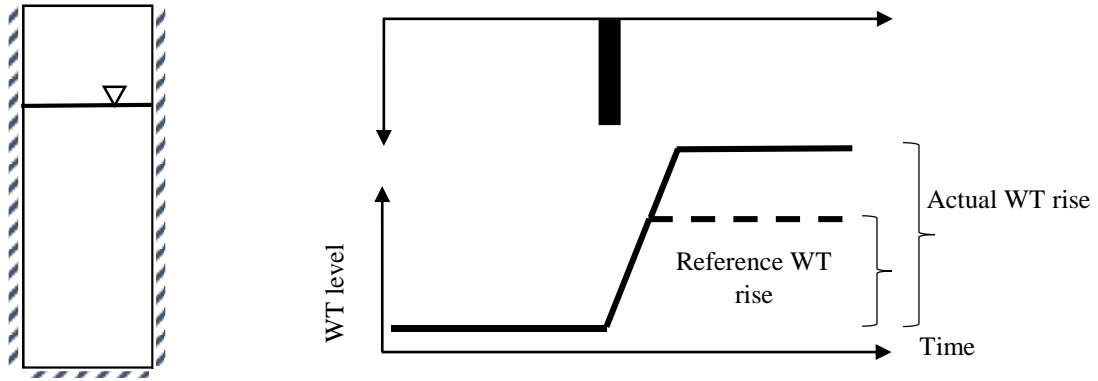



**Figure 3. Schematic representation of actual and reference water table rise using the WTF method for a soil column subjected to a single pulse of rainfall. In this case the actual water table rise is larger than the reference value, which occurs when the water table is very close to the soil surface.**

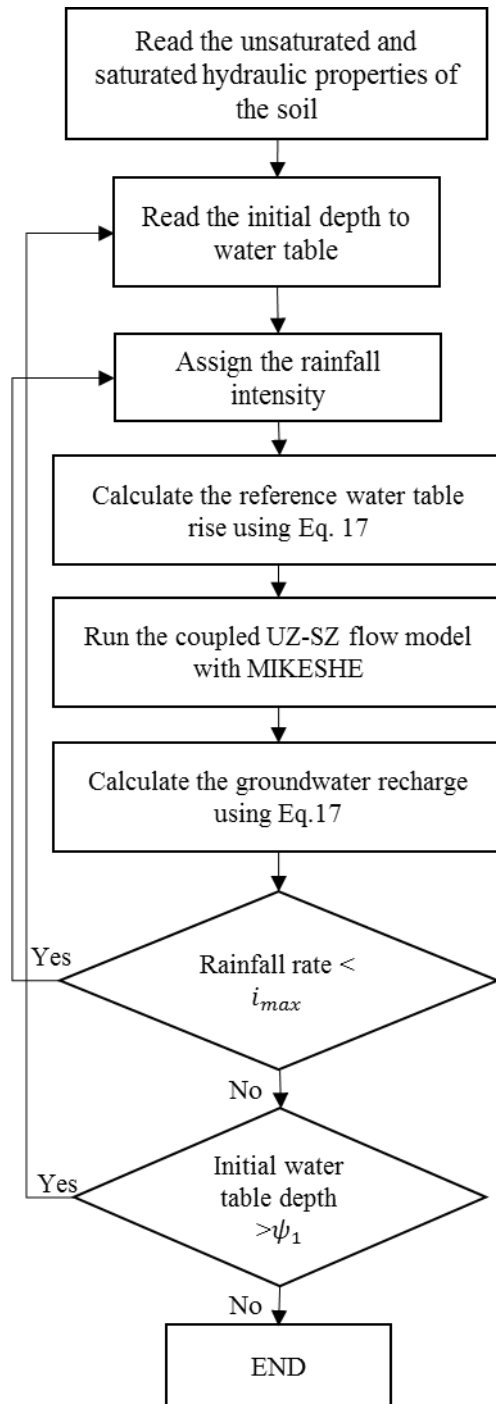



**Figure 4. Step-by-step procedure of the WTF method used in MIKE SHE. $i_{max}$ is the minimum of saturated hydraulic conductivity of the four soil types. $\psi_1$ is the soil bubbling pressure given in Table 2.**

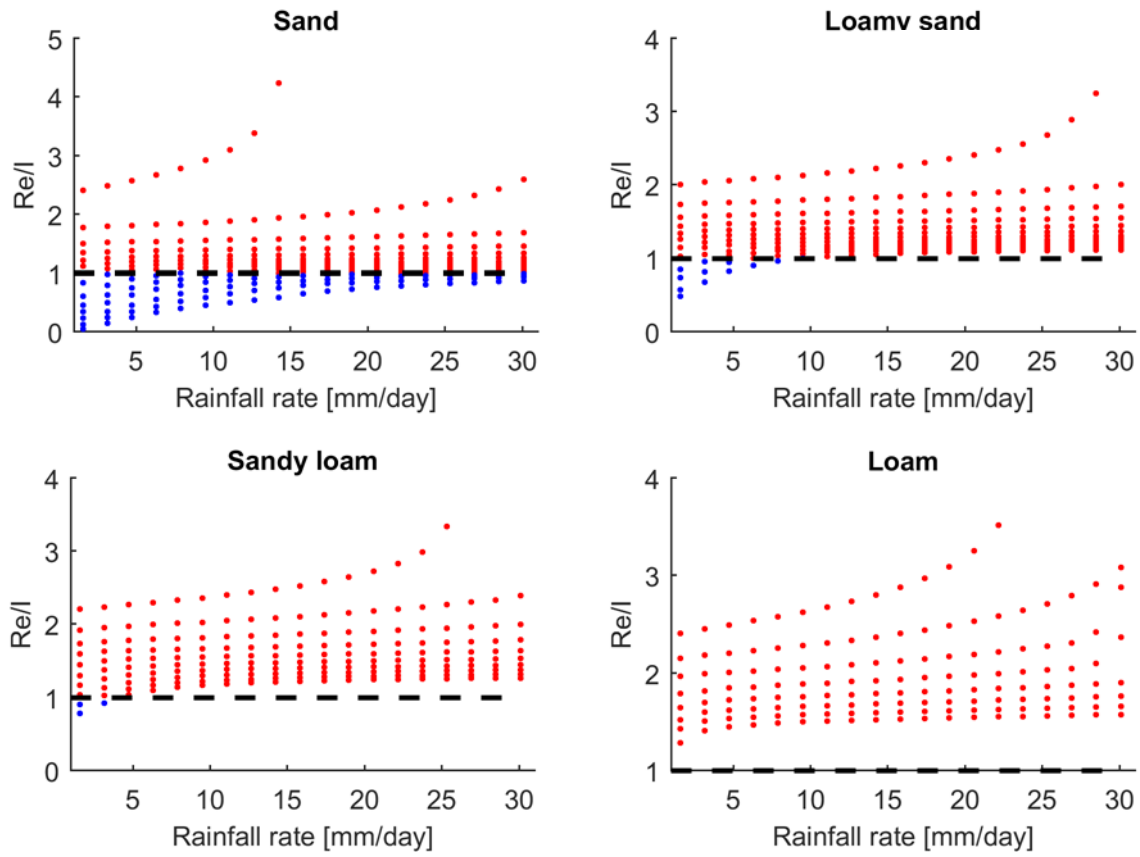



**Figure 5. Variations of the ratio of recharge/infiltration with rainfall and initial depth to water table in different soil types simulated by MIKE SHE. The red dots are $\frac{Re}{I} \geq 1$ and the blue dots are $\frac{Re}{I} < 1$.**

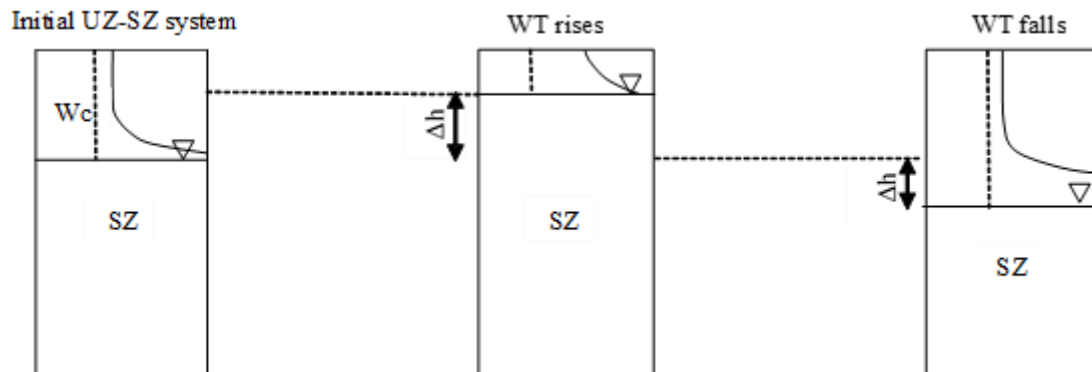



**Figure 6. Conceptualization of the interaction between UZ-SZ in MOBIDIC-MODFLOW in rising and falling water table conditions.**

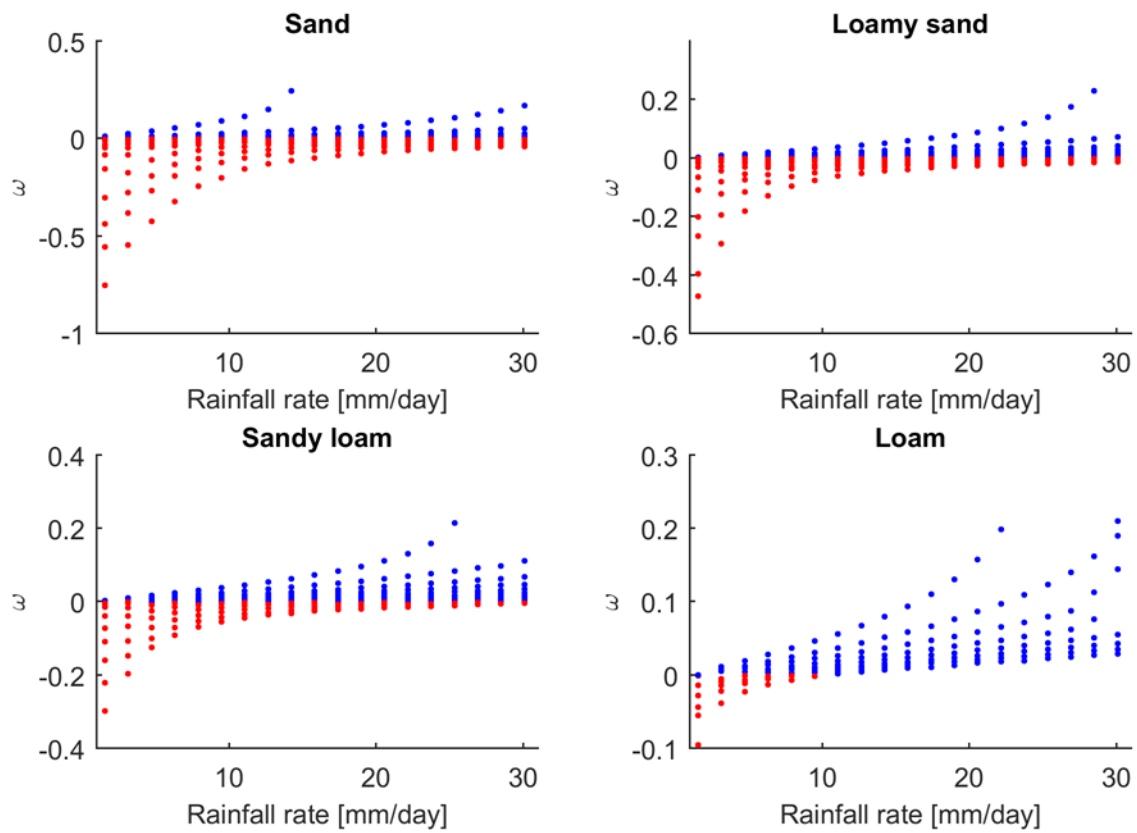



**Figure 7. Variations in $\omega$ against rainfall intensity for different initial water table level and soil types.**

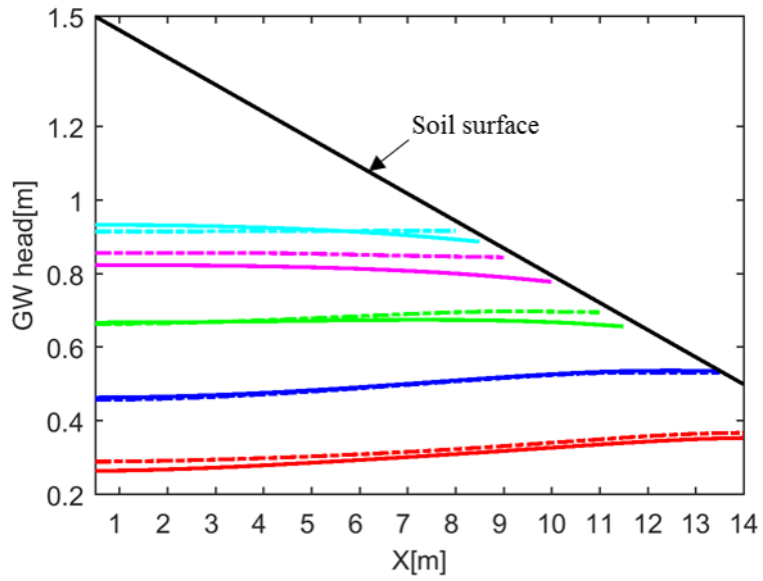
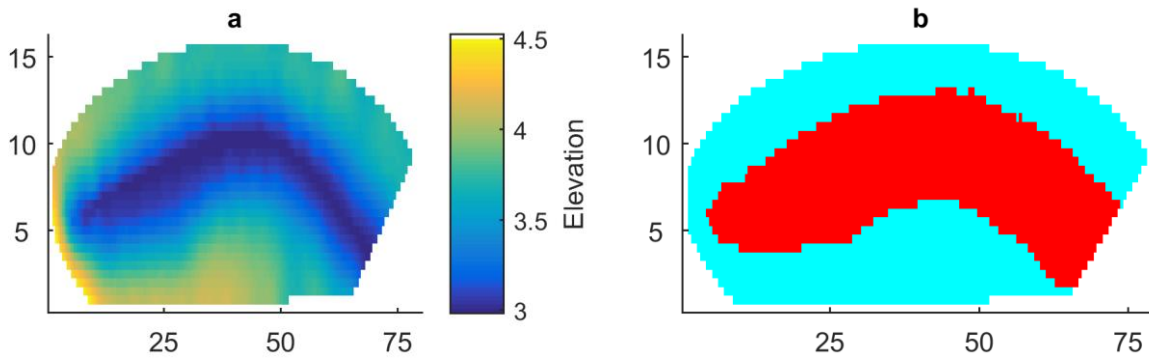



**Figure 8. Simulated water table level after 4 (red), 8 (blue), 12 (green), 16 (magenta) and 20 days (sky blue) with MIKE SHE (solid lines) and MOBIDIC-MODFLOW (dashed lines).**

5    **Figure 9.  a) The digital elevation model of Borden catchment and b) zoning map of the catchment based on depth to water table less than 1.5m (red) and greater than1.5m (blue).**

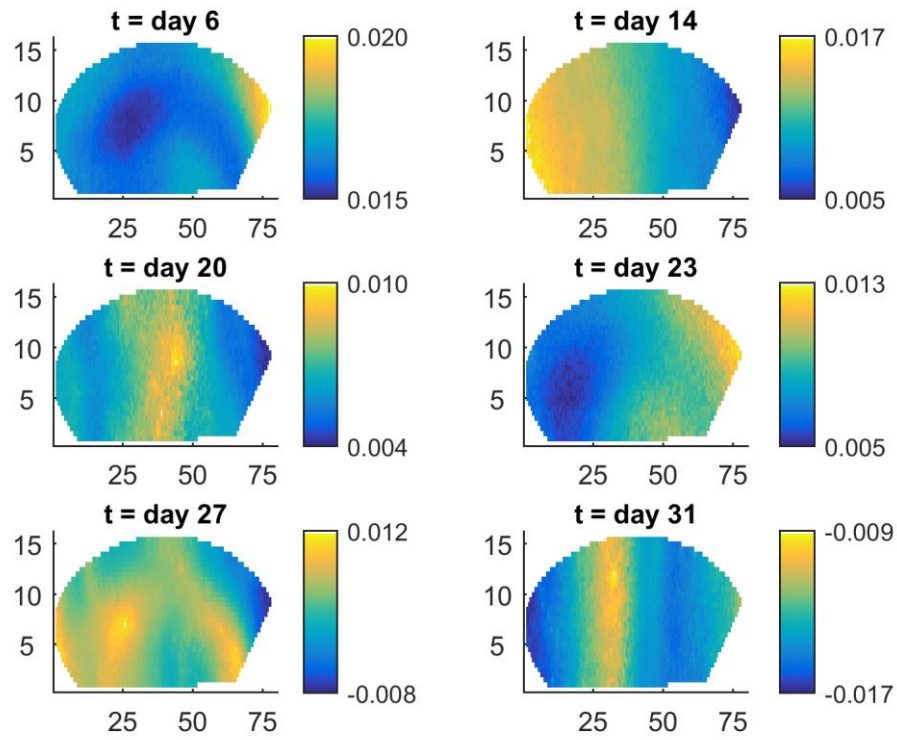



**Figure 10. The difference in simulated water tables by MIKE SHE and MOBIDIC-MODFLOW ($h_{MOBIDIC} - h_{MIKESHE}$) [m] at different time steps.**

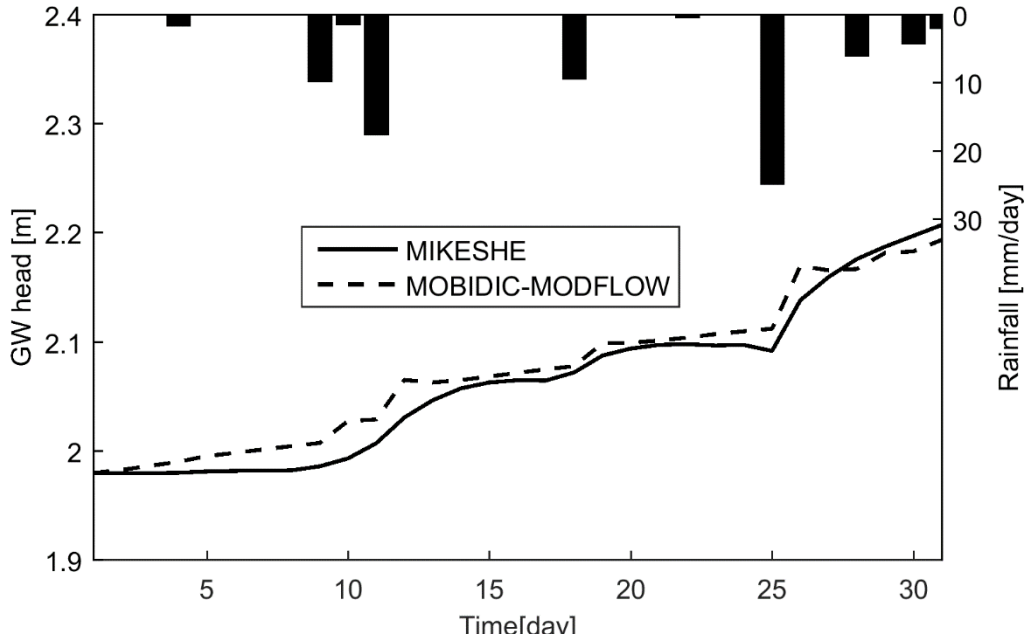



**Figure 11. Simulated water table depth by MIKE SHE (solid lines) and MOBIDIC-MODFLOW (dashed lines) at the outlet grid of Borden catchment.**

**Table 1. Comparison of the subsurface flow processes in MOBIDIC-MODFLOW and MIKE SHE.**

| Model/Process | Unsaturated zone | Saturated zone | UZ-SZ coupling | Applications in shallow water table regions |
|---|---|---|---|---|
| **MIKE SHE** | 1D Richards | 3D finite difference | Iterative water table correction in each UZ time steps | Applicable in both deep and shallow water table regions. The dynamic variations of the specific yield in shallow water table regions is handled using the UZ-SZ coupling approach. However, the iterative process increases the computational burden of the model. |
| **MOBIDIC-MODFLOW** | Dual reservoir | 3D finite difference | Sequential coupling | Since specific yield is assumed to be constant, it has limitations in modelling of the water table fluctuations of the humid regions. The simplified UZ-SZ coupling approach makes the model computationally efficient. |

**Table 2. Hydraulic properties of the soil types used in this study based on (Rawls et al., 1982) and simulated range of initial water table depths.**

| Parameter | Sand | Loamy sand | Sandy loam | Loam |
|---|---|---|---|---|
| $\theta_{sat}$ | 0.437 | 0.437 | 0.453 | 0.463 |
| $\theta_{fld}$ | 0.091 | 0.125 | 0.207 | 0.270 |
| $\theta_{res}$ | 0.02 | 0.035 | 0.041 | 0.027 |
| $K_s \left[ {cm}/{hr} \right]$ | 21 | 6.11 | 2.59 | 1.32 |
| $\psi_1 \, [cm]$ | 15.98 | 20.58 | 30.2 | 40.12 |
| $m$ | 0.694 | 0.553 | 0.378 | 0.252 |
| Initial depth to water table | 0.3m-1.5m | 0.5m-1.5m | 0.7m-1.5m | 0.9m-1.5 |