Energy states of soil water – a thermodynamic perspective on soil water dynamics and storage controlled stream flow generation in different landscapes

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Abstract: The present study corroborates that a thermodynamic perspective on soil water is well suited to distinguish the typical interplay of gravity and capillarity controls on soil water dynamics in different landscapes. To this end, we express the driving matric and gravity potentials by their energetic counterparts and characterize soil water by its free energy state. The latter is the key to defining a new system characteristic determining the possible range of energy states of soil water, reflecting the joint influences of soil physical properties and height over nearest drainage (HAND) in a stratified manner. As this characteristic defines the possible range of energy states of soil water in the root zone, it also allows an instructive comparison of top soil water dynamics observed in two distinctly different landscapes. This is because the local thermodynamic equilibrium at a given HAND and the related equilibrium storage allow a subdivision of the possible free energy states into two different regimes. Wetting of the soil in local equilibrium implies that free energy of soil water gets positive, which in turn implies that the soil is in a state of a storage excess. While further drying of the soil leads to a negative free energy and a state of a storage deficit. We show that during one hydrological year the energy states of soil water visit distinctly different parts of their respective energy state spaces. Both study areas exhibit furthermore a threshold-like relation between the observed free energy of soil water in the riparian zone and observed streamflow, while the tipping points coincide with the local equilibrium state of zero free energy. We found that the emergence of a potential energy excess/storage excess in the riparian zone coincides with the onset of storage controlled direct streamflow generation. While such threshold behavior is not unusual, it is remarkable that the tipping is consistent with the underlying theoretical basis.

1 INTRODUCTION

1.1 Motivation

Only a minute amount of global water is stored in the root zone of the soil. Yet this tiny storage compartment crucially controls a variety of processes and ecosystem functions. The root soil water stock essentially supplies savannah vegetation (e.g. Tietjen et al., 2009; Tietjen et al. 2010) and more generally ecosystems during severe droughts (Gao et al., 2014). The soil water content controls infiltration, runoff formation and streamflow generation (Graeff et al., 2009; Zehe et al., 2010), it partly determines habitat quality of earthworms (e.g. Schneider et al.; 2018) and it is of key importance for soil respiration and emission of greenhouse gases in mountain rain forests (e.g. Koehler et al., 2012). Soil water dynamics is thereby controlled by the triple of infiltration, moisture retention and water release. These processes are driven by the intermittent rainfall and radiative forcing and controlled by multiple forces arising from capillarity, gravity, root water uptake and optionally osmosis. Steady state, hydraulic equilibrium conditions imply that the driving forces act in a balanced manner. In the simple case of absent vegetation and of a flat topography this force balance corresponds to the well-known hydraulic equilibrium, where the matric potential equals the negative of the gravity potential along the entire soil profile. The corresponding equilibrium soil water content profile, which is straightforward to calculate if depth to groundwater and the soil water retention curve are known, reflects thus a balance between the most the prominent influences: the local capillary control and the non-local gravitational control. Although these two controls are sensitive to distinctly different systems properties, these properties are not necessarily independent. The climatological and geological setting constraints the co-development or co-evolution of soils, geomorphology and vegetation (as suggested by e.g. Troch et al., 2015; Sivapalan and Bloschl, 2015; Saco and Moreno-de las Heras, 2013). One might hence wonder whether this constraint co-development created a distinctly typical interplay of capillary and gravitational controls on soil moisture. In the present study we show that this interplay manifests through a) distinct differences in soil water dynamics among different hydrological landscapes and b) a thermodynamic perspective on soil water dynamics to discriminate typical differences that cannot be inferred from the usual comparison of soil moisture observations.

1.2 Thermodynamic reasoning in hydrology and related earth sciences

Thermodynamic reasoning has a long tradition in earth science, ecology and hydrology and one of its key advantages is a joint treatment of mass fluxes and the related conversions of energy, including dissipation and entropy production. In geomorphology its dates back to the early work of Leopold and Langbein (1962) on the role of entropy in the evolution of landforms. Howard (1971, cited in Howard 1990) proposed that angles of river junctions are arranged in such way that they minimize stream power. Bolt and Frissel (1960) related soil water potentials to Gibbs free energy of soil water (referring to the early pioneers Edelfson and Anderson (1940)) and established a link between soil physics and thermodynamics. In ecology Lotka (1922a; 1992b) proposed that organisms that maximize their energy through put, have an advantage within the evolutionary selection process.

Thermodynamics gained substantial attention in catchment hydrology since the work of Reggiani et al. (1998a) and of Kleidon and Schymanski (2008). Reggiani et al. (1998a) employed thermodynamic reasoning and volume averaging to derive a model framework of intermediate complexity (Sivapalan, 2018). They introduced the idea of a representative elementary watershed REW, which can be seen as least spatial entity for building mesoscale hydrological models. This idea has been picked up and advanced by several follow-up studies dealing with the coding and successful application of REW-based hydrological models (Reggiani et al., 1998a; Reggiani et al., 1998b; Reggiani et al., 1999; Reggiani et al., 2000; Reggiani and Schellekens, 2003; Lee et al., 2005; Zhang et al., 2006; Tian et al., 2006; Lee et al., 2007) or the challenge to derive the necessary closure relations (Zehe et al., 2006; Beven, 2006).

Along a different avenue, Kleidon and Schymanski (2008) discussed the opportunity of using maximum entropy production (MEP, originally proposed by Paltridge, 1979) to predict steady state, close to equilibrium functioning of hydrological systems and to infer model parameters based on thermodynamic optimality. This idea has motivated several efforts to predict the catchment water balance using thermodynamic optimality. For instance, Porada et al. (2011) simulated the water balance of the 35 largest basins on Earth using the SIMBA model and inferred parameters controlling root water uptake by maximizing entropy production. They tested the plausibility of their assessment within the Budyko framework (Budyko 1958). Zehe et al. (2013) showed that a thermodynamic optimum density of macropores created by worm burrows which maximized dissipation of free energy during recharge events allowed an acceptable uncalibrated prediction of the rainfall runoff response of a lower mesoscale catchment with a physically based hydrological model. While this finding is at least an interesting incidence, the explanation why the worms should create their burrows in such a way is not straightforward. Hildebrandt et al. (2017) proposed that plants optimize their root water uptake by minimizing the necessary energetic investment through a spatially uniform water abstraction from uniform soils. Along similar lines of thought but at much larger scales Gao et al., (2014) proposed that ecosystems optmize their rooting depth. This is deemed to balance the advantage of vegetation to endure droughts of increasing return periods with the necessary energetic investment to expand their root system to enlarge the water holding capacity.

Kleidon et al. (2013) tested whether the topology of connected river networks can be explained through a maximization of kinetic energy transfer to sediment flows. They showed that the depletion of topographic gradients by sediment transport can be linked to a minimization in frictional dissipation in streamflow networks, which in turn implies a maximization of sediment flows against the topographic gradient and thus of power in the sediment flows. The idea that the topology of river networks reflects an energetic optimum - more precisely a minimum - is in fact much older and was already suggested by Howard (1990) and picked up by Rinaldo et al. (1996) as concept of minimum energy expenditure. Hergarten et al. (2014) transferred this idea to groundwater systems by analyzing preferential flow paths that minimize the total energy dissipation at a given recharge under the constraint of a given total porosity and by verifying those against data sets for spring discharge in the Austrian Alps.

Kleidon et al. (2014) and Renner et al. (2016) tested whether a two-layer energy balance model based on maximum power in combination with Carnot efficiency is suited to predict the partitioning of net short wave radiation into long wave outgoing radiation and turbulent fluxes of latent and sensible heat. During convective conditions their predictions were in good accordance with flux tower data at three sites with different land use.

While some of us might find the search for thermodynamic optimality exciting and promising, it is certainly not the Philosophers stone. Westhoff et al. (2013) found for instance that a conceptual model structure which was in accordance with MEP was not suited to predict timing of the water balance in the HJ Andrews experimental watershed. Thermodynamic optimality should thus be seen as a testable and sometimes helpful constraint, but it should not be mixed with a first principle such as the first and second law of thermodynamics (Westhoff et al. 2019). And thermodynamic optimality is restricted to explain system steady state, close to equilibrium functioning. The challenge is however to explain operation of hydrological systems under temporarily variable forcing (Westhoff et al. 2014) and far from equilibrium conditions.

In summary we think that there are four general arguments why a thermodynamic perspective on soil water dynamics and hydrology in general has much to offer. Firstly, surface runoff and particularly soil water fluxes dissipate a very large amount of their driving energy differences. As the dissipation and related entropy production rates depend on the soil material and on the spatial organization of the material as well (Zehe et al., 2010), one may quantify feedbacks between morphological/structural changes and hydrological processes within the same current. Secondly, energy is an extensive quantity, as such it is additive when different systems are merged, it grows with increasing system size and changes can be described through a balance. One may hence apply volumetric averaging and upscaling to energy for instance to derive macroscale effective constitutive relations and macroscale equations as shown by de Rooij (2009, 2011). In contrary the related gravity and matric potentials are intensive state variables and as such neither additive in the above specified sense, nor can their changes be balanced. Thirdly, it can be used to define and explain hydrological similarity based on a thermodynamically meaningful combination of catchment characteristics (Zehe et al., 2014; Seibert et al., 2017; Loritz et al., 2018). Last but not least, one may test whether thermodynamic optimality provides, despite of the fact that it is controversial, a means to test the recent proposition of Savenije and Hrachowitz (2017), stating that: 'Ecosystems control the hydrological functioning of the root zone in a way that it *continuously* optimizes the functions of infiltration, moisture retention and drainage of catchments. '

1.3 Objectives

In the following, we show that the free energy state of soil water is well suited for characterizing distinct differences in soil water dynamics among different landscapes. Based on the free energy state we define a system characteristic, which jointly accounts for the capillary and gravitational control of soil water dynamics, using height over the nearest drainage (HAND, Renno et al., 2008; Nobre et al., 2011) as a proxy for the gravity potential. These energy state functions are strongly sensitive to differences in topography and soil water characteristics of our two study areas and allow an instructive visualization of soil water dynamics in energetic terms. This reveals that the soil water stock in both landscapes operates distinctly differently with respect to the local thermodynamic equilibrium state of minimum free energy. More specifically we provide evidence that the local thermodynamic equilibrium state separates two regimes of a storage deficit and storage excess. During a one year period the observed energy states of the soil water in the study areas operated distinctly differently with respect to these regimes and visited distinctly different ranges of their corresponding energetic state space. Last but not least we provide evidence that the state of zero free energy does not only separate regimes of a storage deficit and a storage excess, it is furthermore also a theoretically motivated threshold, explaining the onset of storage controlled direct runoff production in our study areas.

2 THEORETICAL BACKGROUND

In the following we express the matric and gravity potentials by their energetic counterparts, following largely the work of Bolt and Frissel (1960) and de Rooij (2009), to characterize soil water storage by its free energy state and derive the energy state function.

2.1 Free energy of the soil water

Following the micro approach of Bolt and Frissel (1960) we start our derivation with the Gibbs free energy G (J) of a small soil volume V that contains a test body of water with mass M (kg). Assuming isotherm conditions, while neglecting osmotic forces and the energy of water adsorption leads to:

$$dG_{free} = VdP_e + V_w dp + Mgdz \qquad \text{Eq. (1)}$$

Where g (ms^{-2}) is gravitational acceleration, dz (m) denotes a change in position in the gravity field, P_e (Nm^{-2}) is the external pressure, p (Nm^{-2}) is the capillary pressure, dp the local pressure increment, which relates to the capillary pressure difference between water and air, V_w is the volume of the test water body. Please note that Eq. 1 is not total differential, this is why classical text books of thermodynamics use the symbol δ instead of the d, and speak of a variation in pressure or elevation.

In the next step, we express Eq. 1 as a change in volumetric energy density. When recalling a) that V_w equals the product of V and the soil water content θ (m^3m^{-3}) and b) that the water mass M equals the product of its density ρ (kgm^{-3}), V and θ, we obtain:

$$dg_{free} = \overbrace{dP_e}^{\text{Work}} + \overbrace{\theta dp}^{\text{capillaryenergy}} + \overbrace{\rho g \theta dz}^{\text{potentialenergy}} \quad \text{Eq. (2)}$$

The first term on the right-hand side is mechanical work per volume due to external pressure changes (for instance compression), the second term relates to changes in Gibbs free energy density related to capillary pressure changes, while the last term related to changes in potential energy of the gravity field. In the following the work term is neglected, as we are interested in those changes in Gibbs free which relate to dynamic changes in the stored water amount. As capillary pressure is equal to the product of matric potential ψ (m) times the unit weight of water Eq. (2) can be reformulated as follows:

$$dg_{free} = \rho g \theta d\psi + \rho g \theta dz \quad \text{Eq. (3)}$$

While we acknowledge that the first term on the right hand side is often referred to as matric potential energy (see e.g. Hillel, 2001), we think that the adjective potential is misleading due the correct meaning of potential energy and shortly explain why we deviate from established terminology here. Potential energy refers to the position of a test body of mass M in the gravity field and remains invariant when the inner state of the test (soil) body changes, for instance through compression, when exchanging the fluid mass in the pore space by the same mass of a different fluid. The Young-Laplace equation tells us that both operations change the matric potential in soil, either through a compaction of the soil pores and a reduced pore radius r (m) or through the change in surface tension σ (N/m):

$$\psi = -\frac{2\sigma \cos\phi}{\rho g}\left(\frac{1}{r_{max}} - \frac{1}{r_{min}}\right) \quad \text{Eq. (4)}$$

Where ϕ is the wetting angle. As this form of energy depends on the inner structure of the soil and on the chemical properties of the fluid, does partly determine the inner energy of the soil body in a thermodynamic sense, more precisely it relates to surface energy. We thus refer to term 1 in Eq. 3 as ‘capillary binding energy’, consistently with Zehe et al. (2013).

When deriving Eq. (3) with respect to time (and neglecting changes in z) we find that a change in soil water content implies a change in its free energy state:

$$\frac{\partial g_{free}}{\partial t} = \frac{\partial\left(e_{pot} + e_{cap}\right)}{\partial t} = \rho g\left[(\psi + \theta\frac{d\psi}{d\theta})\frac{\partial\theta}{\partial t} + z\frac{\partial\theta}{\partial t}\right] \text{ Eq. (5).}$$

Note that the potential energy density of soil water (the second term on the right hand side) grows linearly with increasing soil water content. On the contrary capillary binding energy shrinks with growing soil water content, as the absolute value of the matric potential declines non-linearly with increasing soil water content. The change in capillary energy density with a given change in soil water content is determined by the product of the actual soil water and the slope of the water retention curve. We thus state that the product of the well-known soil hydraulic potential, $\psi + z$, and the soil water content corresponds to the volumetric density of free energy of soil water per unit weight. The free energy of soil water for a larger volume is the volume integral of the total hydraulic potential times the soil water content over the volume of interest (de Rooij, 2009; Zehe et al., 2013):

$$E_{free} = E_{cap} + E_{pot} = \int \rho g\left(\psi(\theta) + z\right)\theta dV \text{ Eq. (6)}$$

The latter reflects both the binding state and the amount of water that is stored in a control volume at a given elevation above groundwater and thus reflects the local retention properties and the topographic setting as well. Not the change in potential energy of soil water at a given elevation scales linearly with the soil water content. One might thus wonder whether the dominance of the one or the other energy form may at least partly influence whether a system behaves in a linear or non-linear fashion.

2.2 Hydraulic equilibrium, thermodynamic equilibrium and related soil water content

The state of minimum Gibbs free energy corresponds to a state of maximum entropy and thus to thermodynamic equilibrium. With respect to Eq. (3) this is the case when gravity and matric potential are equal in absolute terms in the entire profile of the unsaturated zone:

$$\begin{gathered} d\psi = -dz \Leftrightarrow \\ \psi = -z + c \end{gathered} \text{ (Eq. 7).}$$

The integration constant c in Eq. (7) is, as it is well known, equal to zero as the matric potential is zero at the groundwater surface, for z=0. In hydraulic equilibrium the absolute value of Gibbs free energy of soil water is thus equal to zero. And the related soil water content, which balances capillary and gravitational influences, is straightforwardly calculated by substituting the matric potential in the soil water retention curve with the depth above groundwater, when the latter is known.

$$S_{eq} \equiv \frac{\theta}{\theta_s} \Big|(\psi = -z) \quad \text{Eq. (7)}$$

Where θ_s (m^3m^{-3}) is the saturated soil water content and S (-) is the relative saturation. This is illustrated in figure 1 for the retention curves of three distinctly different soils.

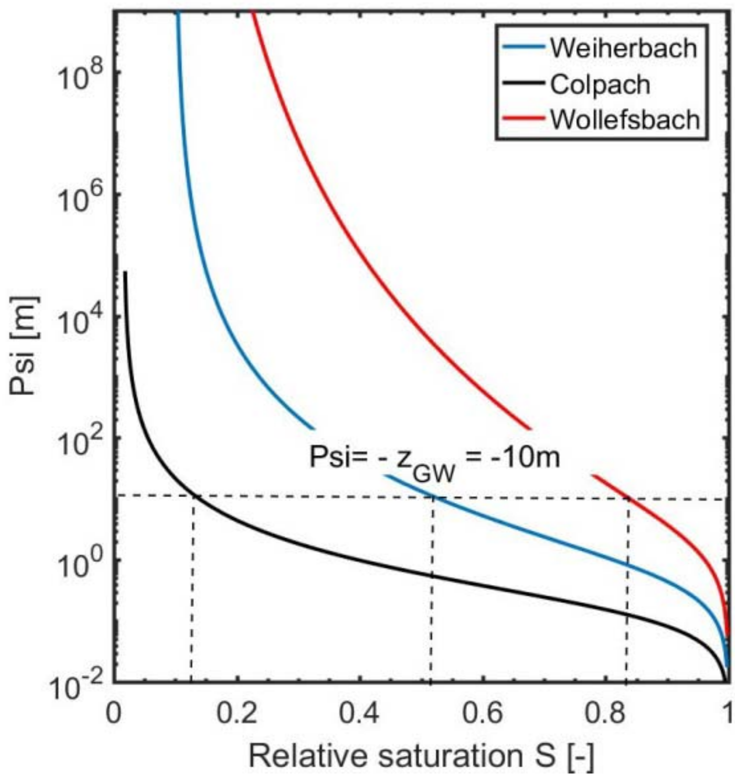

Figure 1: Soil water retention curves as function of relative saturation determined as explained in section 3.1. The dashed black lines mark the relative saturation at hydraulic equilibrium, assuming arbitrarily a depth to groundwater of z_{GW} = 10 m. The Wollefsbach and the Colpach are further characterised in section 3.

Assuming arbitrarily a depth to groundwater of z_{GW} = 10 m in Eq. (7), leads to very different equilibrium saturation values. The equilibrium saturation of the clay rich soil in the Marl geological setting of the Wollefsbach catchment is with S_{eq}= 0.82 rather large, while the young silty soil located in the Colpach has a rather small saturation at equilibrium of S_{eq}=0.13. The loess soil from the Weiherbach is with S_{eq}= 0.53 in between these extremes. Note that two of those soils are located in our respective study areas Colpach and Wollefsbach located in Luxembourg (compare section 3). We added the in Germany located Weiherbach soil to complete the spectrum of possible endmembers. Although these values are very different in magnitude, they represent the respective equilibrium states, which these systems at this elevation will naturally approach when relaxing from external disturbances.

2.3 Free energy state as function of relative saturation

The equilibrium storages shown in figure 1 separate furthermore ranges of relative saturation were the corresponding free energy of the soil water is either negative or positive. This becomes obvious when plotting the specific free energy per unit volume e_{free} (m) of the soil water content at the same elevation above groundwater as function of the relative saturation for these soils (Fig. 2).

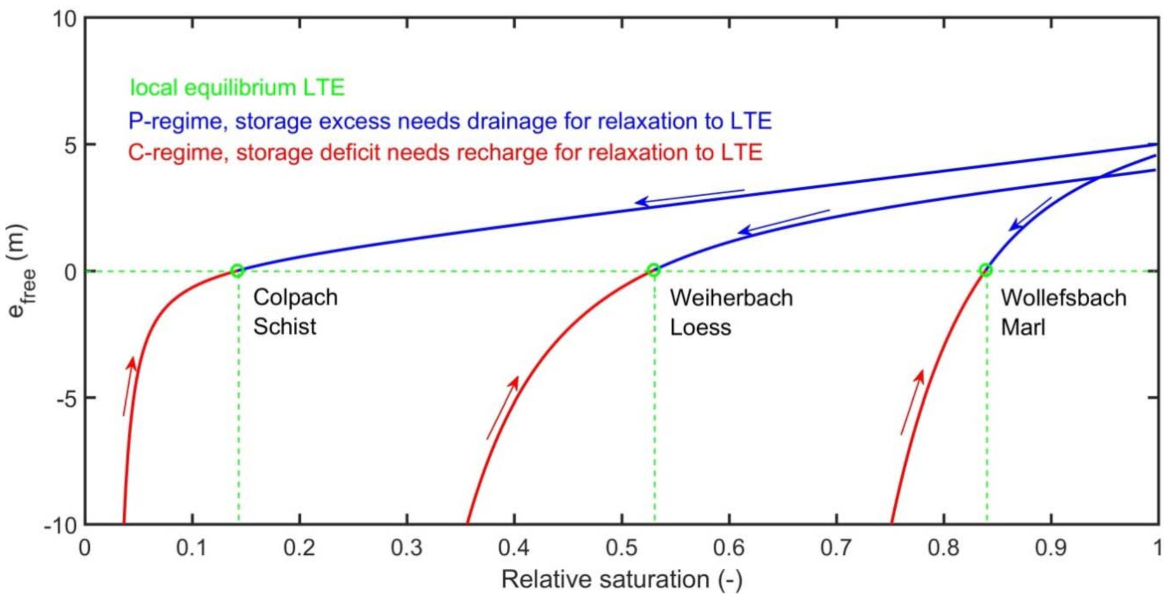

Figure 2: Weight specific free energy state of the soil water stock, as defined in Eq. (8), plotted against the relative saturation of the three different soils, assuming a depth to groundwater of 10m. The green lines mark the local equilibrium state where the absolute value of the specific free energy is zero and the corresponding equilibrium saturations. Free energy in the P-regime and C-regimes are plotted in solid blue and red respectively, the arrows indicate the way back to equilibrium.

$$e_{free} \equiv \frac{g_{free}}{\rho g} \equiv \left(\psi(\theta) + z\right) \cdot \theta = f\left(S \,\middle|\, z = \text{const}\right) \quad \text{Eq. (8)}$$

Note e_{free} is, as being defined as specific free energy per unit volume, equal to the product of total hydraulic potential and the soil water content. Note that we assume the soil to be in capillary contact with groundwater (see section 5.2 for further discussion). The horizontal green line in figure 2 marks the local equilibrium where the absolute value of the specific free energy at this particular elevation is zero. The vertical lines indicate the corresponding equilibrium saturations at the x-axis (corresponding to those in figure 1). These equilibrium storages separate the ranges of soil saturation where the corresponding free energy is positive (in blue). This is the case as the potential energy is larger than the capillary binding energy; we call this range the P-regime. In this regime dynamic in soil water content are dominantly driven by differences in potential energy and gravity dominates. Relaxation back to equilibrium requires the release of water to deplete the excess in potential energy, and the necessary amount is determined by the overshoot of free energy above zero.

Relative saturations smaller than S_{eq} are associated with negative free energy, as the absolute value of the capillary binding energy exceeds potential energy. We call this range the C-regime (in red) because differences in capillary binding energy and thus capillarity act as dominant driver for soil water dynamics. The system needs to recharge water to deplete the “energy deficit” below zero, and the necessary amount depends on the distance to equilibrium. Be aware that particularly small changes in soil water content may, depending on the size of $\theta d\psi/d\theta$.

Figure 2 depicts that the three different soils, when being arranged at the same geopotential level, are characterized by distinctly different energy state curves as function of relative saturation. The P-regime is very prominent for the Colpach soil – potential energy dominates over a wide range of saturation its e_{free} grows linearly with S for values larger than 0.2. The clay rich soil of the Wollefsbach has a diametrical pattern, capillarity dominates the energy state for 82% of the possible saturations and the absolute value of e_{free} grows in a strongly nonlinear way with declining saturation. The energy state function of the loess soil is in-between the other two extremes with an equilibrium at a saturation of 0.53%.

Due equation Eq. (8) the energy state functions shown in figure 2 depend on the soil water retention curve and the depth above groundwater. While depth to groundwater is usually not exactly known, height over the next drainage (HAND, Renno et al., 2008; Nobre et al., 2011) provides an easy to measure surrogate when taking the water level of the closest stream as reference. While depth to groundwater grows obviously proportionally to HAND, the related proportionality factor c is not straightforward to calculate. For draining rivers, c is less or equal to one, the minimum is expected to be in the order of 0.8, and c may increase with increasing distance to the river, reflecting the topography of the groundwater surface. In addition, the proportionality changes dynamically in response to the spatio-temporal pattern of groundwater recharge, the hydraulic properties of the aquifer, topography of an aquitard, and the water level in the stream. Yet we may in characterize the upper limit of free energy states of root zone soil water storages in a stratified manner by a 'family' of energy state curves, if we know: a) the retention functions of the soils, and b) the frequency distribution of HAND $h(z_{HAND})$ in the system of interest.

This family of curves characterizes how HAND and soil physical characteristics jointly control the free energy state of soil water as function of the relative saturation. The presentation of the energy state functions for our study areas in the following section 3 will reveal that all points in the root zone with the same soil water retention curve and which fall into the same bin of HAND are represented by the same energy state curve.

3 APPLICATION

The derived energy state function introduced in the last section defines the possible energy states of the soil water stock, a thermodynamic state space of the root zone so to say. Due to the intermittent rainfall and radiative forcing, their respective annual cycles, the free energy state of soil water will be pushed and pulled through this state space. It appears thus straightforward to visualize these storage dynamics, either observed or modeled, as pseudo oscillations of the corresponding free energy state in the respective energy state functions. This will teach us a) which part of the state space is actually visited by the system, and b) whether the system predominantly operates in one of these regimes or within both them. In the following, we briefly characterize the study areas and the dataset we use for this purpose.

3.1 Study areas

The Colpach and the Wollefsbach catchments belong to the Attert experimental basin (Pfister et al., 2002; Pfister et al., 2017), and are distinctly different with respects to soils, topography, geology and landuse (Fig. 4). Both catchments have been extensively characterized in previous studies with respect to their physiographic characteristics, dominant runoff generation mechanisms and available data (Wrede et al., 2015; Martinez-Carreras et al., 2015;

Loritz et al., 2017; Angermann et al., 2017). Hence, we focus here exclusively on those system characteristics which determine their respective energy state functions. The Colpach has an elevation range from 265 to 512 m.

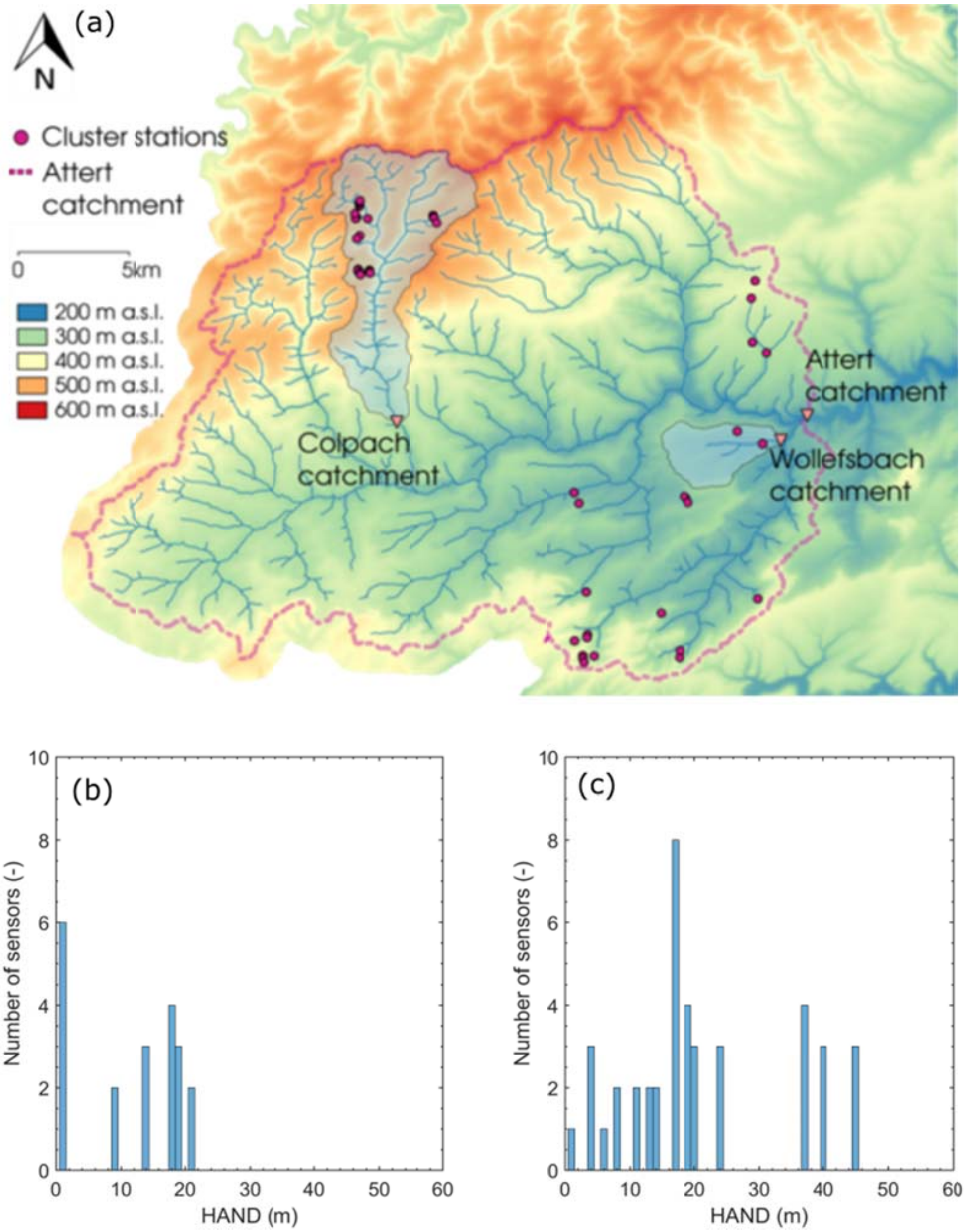

Figure 3: Map of the Attert basin with the Colpach and Wollefsbach catchments (Panel a, taken from Loritz et al. 2017). The red dots mark the cluster sites of the CAOS research unit, which collect besides the standard hydro-meteorological data, soil moisture and the soil water potential. Panels b and c show the distribution of the sensors along HAND for the Wollefsbach and Colpach, respectively.

Soils are young silty haplic Cambisols that formed on schistose periglacial deposits. Despite of their high silt content they are characterized by a high permeability and high porosity

(Jackisch et al., 2017), because the fine silt aggregates embed a fast draining network of coarse inter-aggregate pores. In contrary, the Wollefsbach has a much more gentle topography from 245 to 306 to m.a.s.l. Soils in this marl geological setting range from sandy loams to thick clay lenses.

3.2 Storage data, soil water characteristics and energy state functions

For this study, we use data from a distributed network of 45 sensor clusters spread across the entire Attert experimental basin (Fig. 3) collected within the hydrological year 2013/14. These clusters measure, among other variables, soil moisture and matric potentials within three replicated profiles in 0.1, 0.3 and 0.5 m depths using Decagon 5TE capacitive soil moisture sensors. In this application we focus on data collected in 0.1 m depth, the distributions of sensors along HAND in the Wollefsbach and the Colpach are shown in figure 3 b and c respectively. Note that we use HAND as an estimator for the depth to groundwater here. Soil water retention was in both catchments analyzed by Jackisch (2015) using a set of 62 undisturbed soil cores from the Colpach and 25 undisturbed soil cores from the Wollefsbach (Figure 4 a and b).

Here we do not use these point relations but representative, macroscale soil water retention functions to derive the energy state function of our study areas (Fig. 4 c and d). These were derived by Jackisch (2015) from the raw data of all experiments as follows. He pooled the matching pairs of soil water content and matric potential of all experiments in a landscape into a single sample (Fig. 5 c and d). When using the tension ($pF = \log_{10}(-\psi)$) as independent variable, we interpret the corresponding soil water contents of the 62 or 25 experiments as conditional random variable. The sample reflects the heterogeneity of the soil and needs to be characterized by a conditional frequency distribution $h(\theta \mid \psi)$. And the latter needs in turn to be characterized by its moments and percentiles. The averaged soil water content at each matric potential/tension-level $\overline{\theta}(\psi)$ is an estimator to the expectation value of the soil water content at this tension.

We define the representative retention curve as the one that relates the expected soil water storage to the matric potential $\overline{\theta}=f(\psi)$ and the latter may be obtained by fitting a suitable retention function to the data, we used the van Genuchten model here (Jackisch, 2015). Note that this relation cannot be observed at a single site. It is an effective macroscale retention function characterizing the relation between the expected soil water content in the landscape and the matric potential, reflecting random distribution $h(\theta \mid \psi)$.

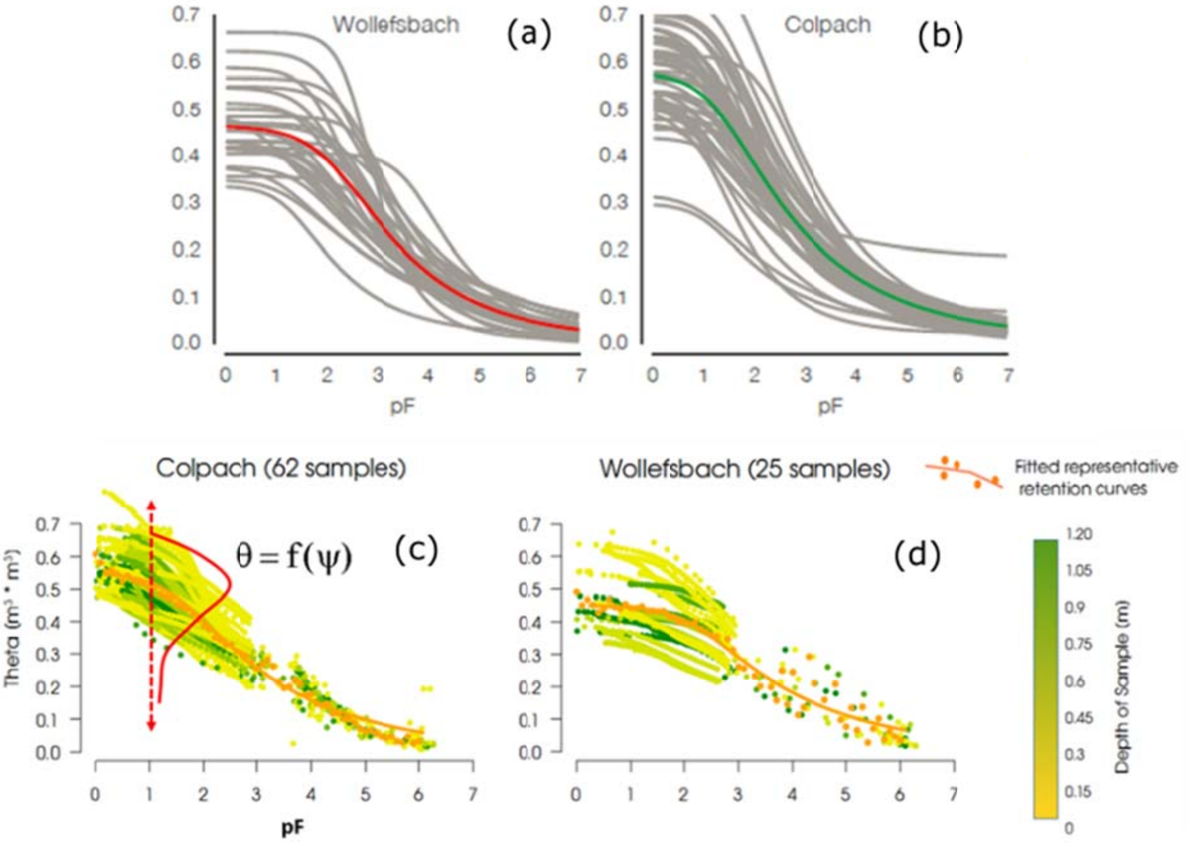

Figure 4: Panel a and b show the retention functions Jackisch (2015) derived from individual soil cores by means of multistep outflow experiments. Panels c and d illustrate the procedure of pooling the soil water contents observed at given tension (pF = $\log_{10}(\psi)$) of all experiments into conditional random samples. The orange points mark the averaged $\overline{\theta}$ values as function of the tension and the solid lines are the mark fitted van Genuchten functions. Note that these representative curves are shown in color in panel a and b as well. The color code of the individual data points in panel c and d relates to the depth of the sample below surface.

Loritz et al (2017, 2018) used these effective retention functions for setting up physically-based hydrological models for both catchments, which yielded simulations of stream flow and soil moisture dynamics in good accordance with observations. Test simulations with randomly selected retention functions of individual experiments (Fig. 4 b) and based on the averages of the van Genuchten parameters of 62 experiments performed clearly worse.

Based on these representative retention functions and the frequency distributions of HAND (Fig. 5 b and d) we compiled the energy state functions of both catchments (Fig. 5 a and c) according to Eq. 8, thereby using HAND as surrogate for the depth to groundwater. As stated in the previous section, the energy state function consists of a family of curves, which characterize the free energy state of the soil water as function of the relative saturation, stratified along the bin centroids of the corresponding frequency distributions of HAND.

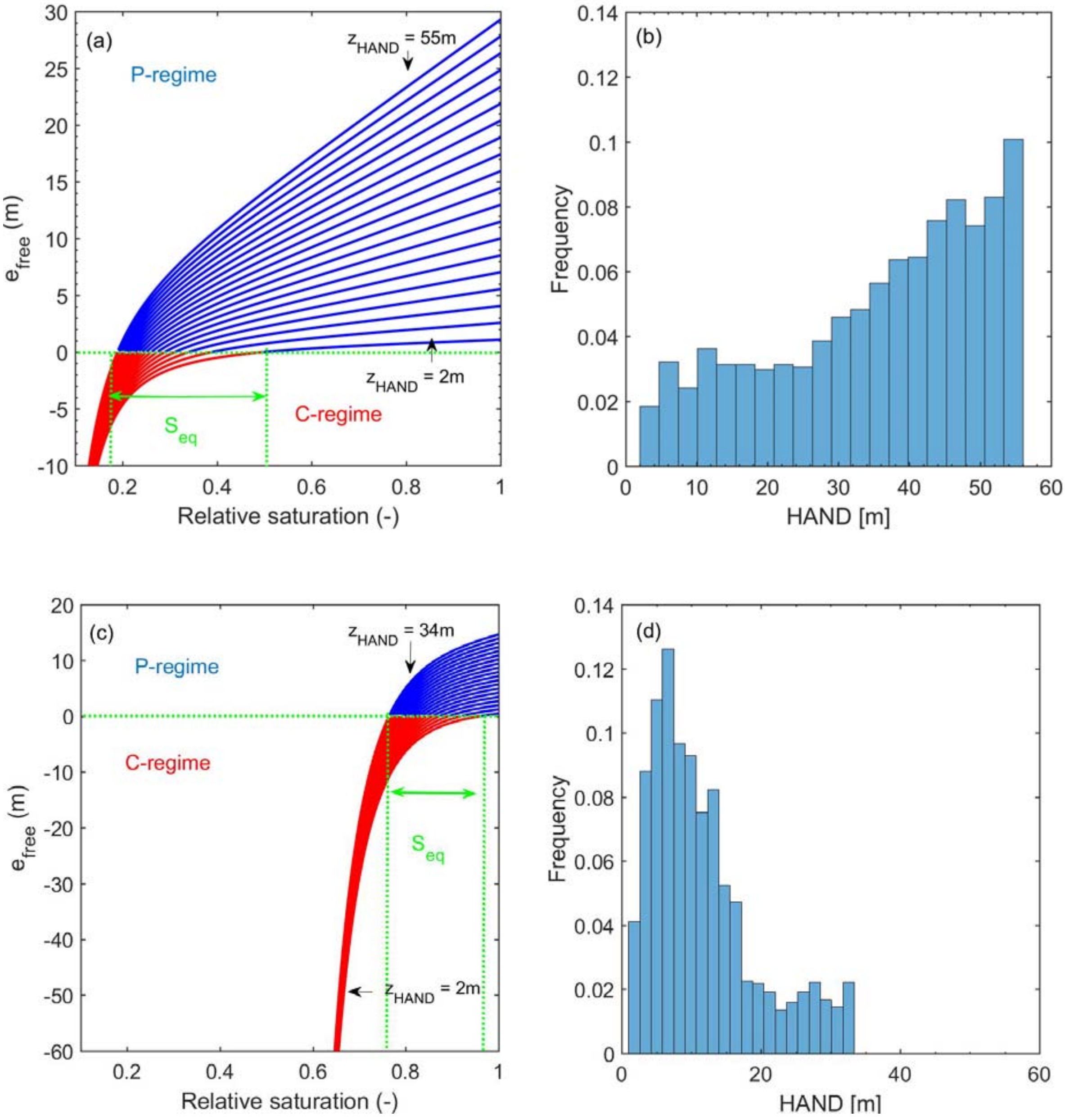

Figure 5: Energy state functions of the Colpach (a) and the Wollefsbach (c) derived from the corresponding frequency distributions range of HAND (panels b and c) and the representative retention functions (note the differences in scales). The horizontal green line mark the equilibrium of zero free energy, the vertical green lines mark the corresponding ranges of equilibrium saturations. Please note that e_{free} at a relative saturation of 1 equals the product of HAND and the soil water content at saturation.

Note that the wider HAND range in the Colpach causes a clear dominance of the P-Regime over a large saturation range. More importantly, figure 5a reveals that for relative saturations larger than ~0.4 free energy is a multilinear function of relative saturation. This means that the specific free energy density is at each HAND level a linear function of relative saturation, but the slope of the energy state curves does increase with increasing HAND. The corresponding range of equilibrium saturations is between 0.18 and 0.5. The absolute values of e_{free} are in the corresponding C-regime less than 20m. In the root zone of the Wollefsbach free energy is contrarily a strongly non-linear function of relative saturation (fig. 5c). The C-regime is very prominent and e_{free} drops below – 100 m for saturations smaller than 0.6. This mainly due to the high clay content in the soil and to a lesser degree it also reflects the smaller HAND in this landscape. Consistently, we find the ranges of equilibrium saturation between 0.78 and 0.98.

4 RESULTS

4.1 Soil moisture and its free energy state at two distinct cluster sites

In a first step we inter-compare the free energy states of the soil moisture stock (Fig. 6) which was observed at two arbitrarily selected sites in the respective study catchments. Both sites are located 20 m above their respective streams. The soil water content in the clay rich top soil of the Wollefsbach site is in the winter and fall period rather uniform and on average 0.15 m^3m^{-3} larger than in the Colpach (Fig. 6a). While the soil water content at the Colpach site appears much more variable in these periods. Both sites dry out considerably during the summer period and start to recharge with the beginning of the fall. Figure 6a depicts furthermore that the site in the Colpach operates clearly above the corresponding equilibrium soil water content, $\theta_{eq} = 0.139\ m^3m^{-3}$, while the site in the Wollefsbach drops below its equilibrium soil water content, $\theta_{eq} = 0.364\ m^3m^{-3}$, and operates in the C-regime for almost 3 months.

Figure 6 b and c provide the corresponding free energy states of both soil water time series as function of the soil saturation. Observations are shown as black circles and the related theoretical energy state curves, calculated after Eq. 8 are in blue. The first thing to note is that the observed free energy states for both sites scatter nicely around the theoretical curves. More interestingly one can see that the spreading of the free energy state of the soil water stock is at both sites distinctly different. The free energy state of soil water at the Colpach site is during the entire hydrological year in the P-regime and hence subject to an overshoot in potential energy (Fig. 6b). The site operates in the linear range of the energy state curve and fluctuates around an average weight specific energy density of 3.2 m, which corresponds to an energy density of $2.9*10^4$ Jm^{-3}. While the observations spread across a total range of 3 m (2.9 10^4 Jm^{-3}) their standard deviation is 0.44 m ($3.0*10^3$ Jm^{-3}). The coefficient of variation of the free energy state of the soil water content is hence with 0.14 rather small.

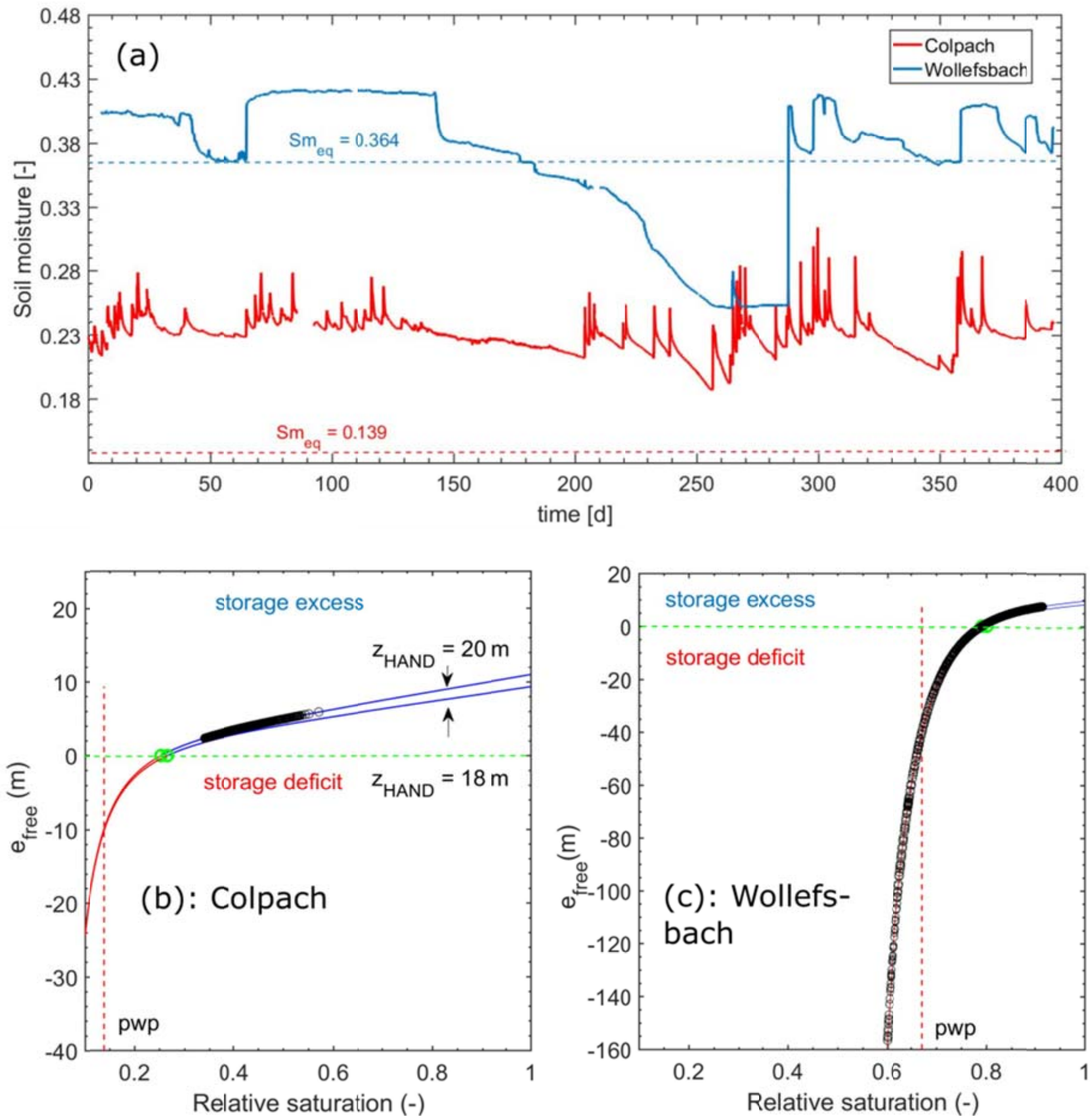

Figure 6: Top soil water content observed at cluster sites in the Colpach and the Wollefsbach catchment (panel a) and the corresponding free energy states in their respective energy state curves (panel b and c note the different scaling of the ordinates). The black circles mark the observations. The vertical dashed line marks the permanent wilting point, which is due to the definition of the total free energy in Eq. 8 not simply equal to a total hydraulic potential of -133 m. Panels b and c show additionally the energy state curve when contamination the real value with and error of 2 m (z_{HAND} = 18 m). This is to highlight that an error in the estimated depth to groundwater implies a substantial mismatch between observations and the theoretically predicted curve.

In the Wollefsbach the weight specific free energy density of soil water spreads across a much wider range of almost 180m, which corresponds to $1.79*10^6$ Jm^{-3} (Fig. 6c). The average specific free energy density is with - 44.3 m ($-4.41*10^5$ Jm^{-3}) strongly negative, the distribution is highly skewed towards the negative value and the coefficient of variation is with 2.8 much larger. Most importantly the system operates qualitatively differently as it switches to the C regime during the dry spell in the summer period and stays there for nearly three months. Please note that the free energy declines to the values which are clearly below the permanent wilting point pwp. (As specific free energy is the product of the total soil hydraulic potential and the soil water content, its value at the pwp does not simply correspond to – 133m). To understand this strong decline in soil water content it is important to recall that drying of the top 0.1 m of the soil, is strongly influenced by evaporation and that the water potential of unsaturated air is at a relative humidity of 90% clearly below the permanent wilting point (Porada et al., 2011).

We hence state that the free energy state of the soil water stock reveals a distinctly different dynamic behavior of both sites, which cannot be derived from the comparison of the corresponding soil water moisture time series. The Colpach site is characterized by permanent storage excess, though the corresponding soil water content is always smaller than in the Wollefsbach. Free energy of the soil water stock is in this range a linear function of relative saturation. This implies that the energy difference which dominantly drives soil water dynamics changes linearly with soil water content, or in other terms gravity potential dominates against matric potential. The retention function in Figure 1 shows that the matric potential in the Colpach is at the minimum observed saturation of S=0.3 (Figure 6b) equals -2 m. This implies according to Eq. 8 that $e_{free} = - 0.3* \theta s\ 2m + 0.3* \theta s\ 20\ m = 2.91$ m and that potential energy is 10 times larger than capillary binding energy. For larger saturations the first term remains rather constant while the second grows linearly with saturation. In contrary, the Wollefsbach shows a strongly non-linear behavior at this site and it switches to a storage deficit when the soil saturation drops below 0.79 (Fig. 6a). In a further step we contaminated the HAND values of both sites with an error of 2m and plotted the corresponding energy state curves (z_{HAND} = 18 m). This curve does considerably mismatch the observations (Figure 6b, c). This corroborates a) that HAND is a good estimator of depth to groundwater at this point and b) that an error in the estimated depth to groundwater leads to a mismatch between the theoretical energy state curve and the observed values. This implies that the observed energy states will also change with changing groundwater surface, as further detailed in the discussion.

4.2 Soil moisture and its free energy state within the entire observation domain

Figure 7 presents the free energy states of the soil moisture which was observed at all cluster sites in the Colpach (panel a, N = 41) and the Wollefsbach (panel b, N = 20). The respective heights above the channel range from 1 to 45 m in the Colpach and from 1 to 22m in the Wollefsbach (Fig. 3 b and c).

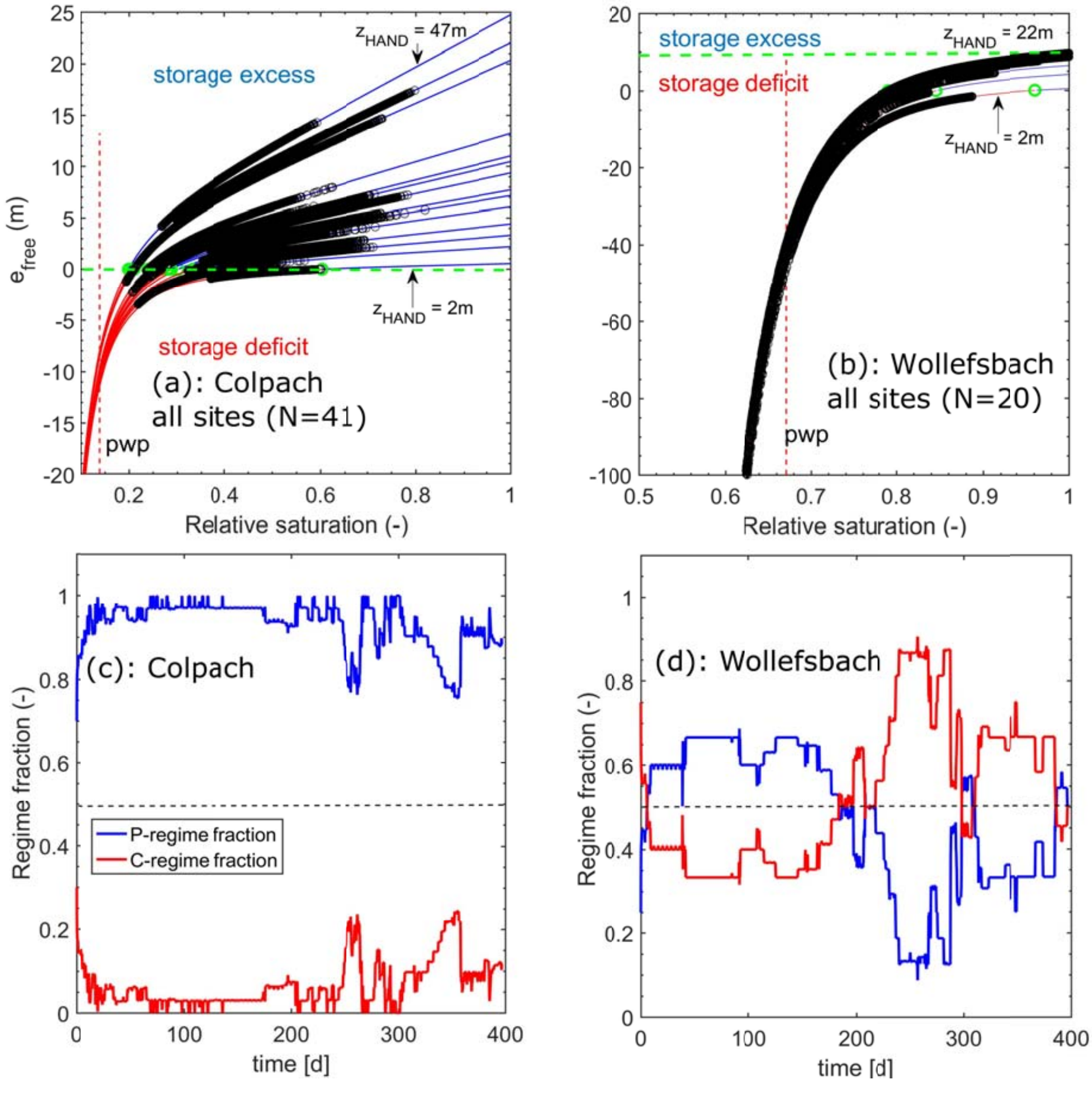

Figure 7: Free energy of all observations in the Colpach (a) and Wollefsbach (b) plotted in their corresponding energy state function (note the different scales). The black circles mark the observations. The horizontal green lines mark the equilibrium of zero free energy. Panel c and d show which fractions of the data set was in the P or in the C regime as function of time. Note that the corresponding distributions of HAND are shown in Figure 3 b and c.

Generally, the observed free energy states scatter again nicely around the energy state curves of the corresponding HAND. The Colpach operates except for a few sites most of the time in the linear range of the P-regime, indicating that soil moisture dynamics is dominated by potential energy differences. Observations in the Colpach generally spread across a wide range of relative saturations, and the corresponding "amplitudes" of the free energy deviations are clearly larger as at the single site shown in Figure 6 b. This is because sensor clusters with the same HAND were pooled into the same subsample regardless of their separating distance. For instance, at z_{HAND} = 1 m the subsample consisted of 1 cluster with three replicate soil moisture profiles, at z_{HAND} = 17 we had for instance 3 sensor clusters and thus in total 8 soil moisture profiles. The partly large spreading of the observations may hence be explained by a combination of local scale heterogeneity and large scale differences in the drivers of soil water dynamics such as rainfall or local characteristics of forest vegetation.

Despite of the large spreading, 80% of the Colpach sites operated permanently in the P-Regime (Fig. 7c). During the wet season it is more than 90 % of the sites, between day 250 and 400, quite a few profiles switch into the C-regime and thus to a storage deficit. These profiles are mostly located at the smallest heights over the next drainage, while only some of those are at a larger HAND of 37 m and 22 m.

In the Wollefsbach we find, consistently with figure 7b, a clear drop of free energy into the C-regime during the dry spell in the summer period. All sites drop clearly below the permanent wilting point, which corroborates the strong evaporative drying of the top soil in this landscape. In contrary to the Colpach, the fractions of profiles which operate in the different regimes are much more variable in time (Fig. 7d). During the observation period, on average 50% of the profiles operate in the C-regime and thus a storage deficit. The minimum is 30% and the C-regime fraction peaks at 90% at day 250. Note that more than 50% of the sites are continuously in the C-regime during the second half of the observation period. These differences are consistent with the strongly different runoff generation behavior of both systems, as further detailed in the next section.

4.3 Free energy state as control of stream flow generation

An interesting question is whether the free energy state of the soil water content and particularly the separation of the C- and the P-regimes is helpful to explain the onset of storage controlled stream flow generation in both landscapes. As storage controlled runoff response to rainfall is not generated everywhere in the catchment but mostly in the riparian zone, the energy state of soil water at large values HAND is pretty unimportant in this respect.

We thus plotted for the entire hydrological year the observed streamflow in both catchments against the energy state of soil water for sites at the smallest HAND values of 2m which are close to the riparian zone (Figure 8 a and b).

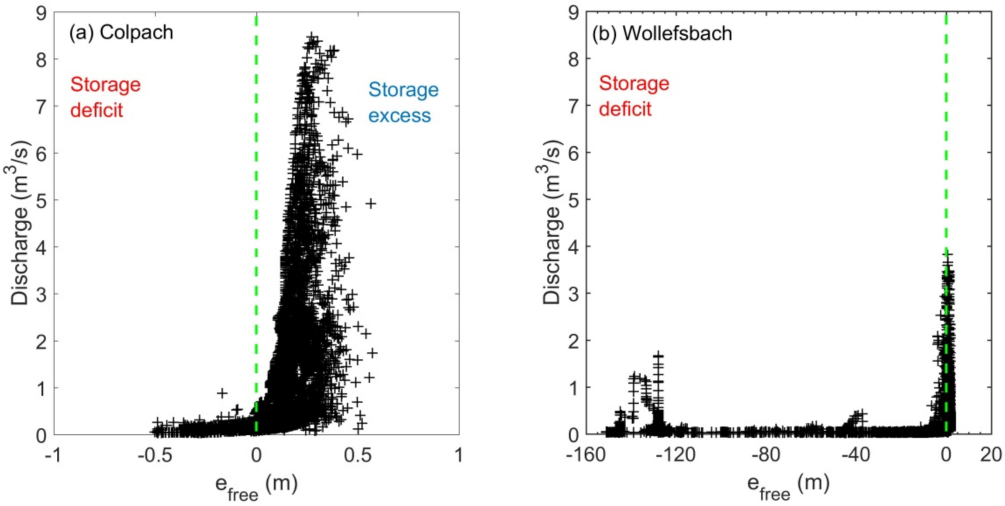

Figure 8: Observed stream flow in the Colpach (Panel a, drainage area is 19.2 km^2) and the Wollefsbach (Panel b, drainage area is 4.5 km^2) plotted against the free energy of sites in their corresponding riparian zones.

Both scatter plots reveal distinct threshold like dependence of streamflow on the free energy state of soil water and note that the threshold coincides with the state of zero free energy, which separates the C- from the P-Regime. Streamflow in the Colpach is rather uniform, if the riparian zone is with respect to the local equilibrium in a storage deficit (Fig. 8a), while streamflow shows a strong variability when the system switches to a storage excess in the P-regime. The transition to a state of storage excess, which implies that the system needs to release water to relax back to local equilibrium, coincides with the onset of storage controlled streamflow generation. The variability of streamflow in P-regime does of course also reflect the variability in the rainfall forcing. Streamflow in the C-Regime likely feeds exclusively from groundwater. This behavior is pretty much consistent with our theoretical expectation.

In the Wollefsbach we observe a slightly different pattern. On the one hand there is a similar sharp increase of streamflow when free energy of soil water in the riparian zone switches from the C- to the P-regime. On the other hand one may observe distinct values of stream flow for specific free energy densities of in the range between -1m and 10m, at -40 m and below -120 m. This reflects infiltration excess runoff generation, which is frequently observed in this Marl setting, as these states correspond to unsaturated hydraulic conductivities of either 5 10^{-7} m/s or 1 10^{-9} m/s or even smaller values. Although overland flow also occurs in the

Colpach, it only occurs on compacted forest roads, but not in the riparian zone or in upslope pristine areas.

5 DISCUSSION AND CONCLUSIONS

The presented results provide clear evidence that a thermodynamic perspective on soil water storage provides holistic information for judging and inter-comparing soil water dynamics, which cannot be inferred from soil moisture observations alone. In the following we reflect the general idea of using free energy as state measure, discuss its promises as well as its limiting assumptions. We then move on to the more specific differences in the storage dynamics in both studied catchments. And we close by reflecting on the seeming paradox between the known local non-linearity of soil physical characteristics and the frequent argumentation that hydrological systems often behave much more linearly.

5.1 Free energy and the energy state function – options and limitations

Our results clearly show that free energy as function of relative soil saturation holds the key to define a meaningful state space of the root zone of a hydrological landscape. This space of possible energy states consists of a family of energy state curves, where each of those characterizes how free energy density evolves at a height above the next drainage, depending on the triad of the matric potential, HAND (i.e. as a surrogate for the unknown gravity potential) and soil water content. The free energy state of soil water reflects in fact the balance between its capillary binding energy and geo-potential energy densities and we showed that this balance determines:

- Whether a system is at given elevation above groundwater locally in its equilibrium storage state (e_{free} ==0), in a state of a storage deficit (e_{free} <0) or in state of a storage excess (e_{free} >0);
- The regime of storage dynamics. Soil water dynamics in the C-regime (e_{free} <0) are dominated by capillarity i.e. differences in local matric potentials act as dominant driver. The soil needs to recharge to relax to its local equilibrium. Or it is in the P-regime (e_{free} >0) dominated by potential energy, i.e. the non-local linear gravitational control dominate soil water dynamics, the system needs to release water to relax to local equilibrium.

The energy level function turned out to be useful for inter-comparing distributed soil moisture observations among different hydrological landscapes, as it shows the trajectory of single sites or of the complete set of observations in its energy state space. This teaches us which part of the state space is actually ‘visited’ by the system during the course of the year, whether the system operates predominantly in a single regime, whether it switches between both regimes during dry spells and how much water needs to be released or recharged locally for relaxing back to local equilibrium and how often it actually reaches its equilibrium.

Note that the usual comparison of soil water contents alone did not yield this information. On the contrary from this we would conclude that the site in the Wollefsbach is, due to the higher soil water content, always ‘wetter’ than the corresponding site in the Colpach. The free energy state reveals, however, the exact opposite, we have a storage excess at Colpach site for the entire year while the Wollefsbach site is in summer in a storage deficit. We thus propose that the term wet and dry should only be used with respect to the equilibrium storage as meaningful reference point.

The free energy state of soil water in the riparian zone of both study catchments has furthermore been proven to be rather helpful to explain the onset of streamflow generation. We found a distinct threshold behavior for storage controlled runoff production in both catchments, and clear hints at overland flow contributions in the Wollefsbach. While we admit that a threshold like dependence of the onset of runoff is frequently reported (Ragan, 1968, Gillham, 1984, McDonnell, 1990, Bishop, 1991, Tromp-van Meerveld et al. 2006) we like to stress that the tipping point we found here has a theoretical basis. In both areas it coincides with local equilibrium state of zero free energy – the onset of a potential energy excess of soil water in the riparian zone coincides with the onset of storage controlled streamflow generation.

The apparent strong sensitivity of the free energy state of soil water to the estimated depth to groundwater, offers on new opportunities for data based learning and an improved design of measurement campaigns, but it also determines the limits of the proposed approach. With respect to the first aspect, we could show that an error of 2 m in the assumed depth to groundwater lead to a clear deviation of the observed free energy states from the theoretical energy level curve. This offers either the opportunity to estimate depth to groundwater from joint observations of soil moisture and matric potential, in case the local retention function is known. This can, for instance, be done by minimizing the residuals between the observation and the theoretical curve as function of depth to groundwater. Or it allows for the derivation of a retention function based on the joint observations of soil moisture, matric potential and depth to groundwater. Here, we need again to minimize the residuals between the observation and the theoretical curve but this time as function of the parameters of the soil water retention curve. Due to this strong sensitivity it is furthermore important to stratify soil moisture observations both according to the installed depth of the probe and according to the elevation of the site above groundwater, or the height over the next stream. The latter is important because depth to groundwater determines the equilibrium storage the site will approach when relaxing from external forcing.

Despite of all these opportunities for learning, the sensitivity of free energy to the estimated depth to groundwater implies that the site of the system is still in hydraulic contact with the aquifer. This key assumption is certainly violated if the soil gets so dry that the water phase becomes immobile while the air phase becomes the mobile phase. And it might get violated if depth to groundwater becomes too large. Last but not least the groundwater surface may change either seasonally, or in some systems more rapidly, and this might imply step changes in the energy state function and the storage equilibrium.

We nevertheless conclude that it is worth to collect joint data sets either of the triple of soil moisture, matric potential and the retention function at distributed locations (as we did in the CAOS research unit as explained in (Zehe et al. 2014)) or even preferable on the quadruple of soil moisture, matric potential, retention function and depth to groundwater. Soil moisture observations alone appear not very informative about the system state. This is because they do neither tell anything about the binding state of water, nor about how the system deviates from its equilibrium and which process is “needed” to relax.

5.2 Storage dynamics in different landscapes – local versus non local controls

In line with our proposition we found indeed a distinctly typical interplay between capillary and gravitational controls on soil water in our study areas, and those were in the Colpach substantial different compared to the Wollefsbach. The observations clearly revealed that the top soil in the Colpach operates the entire hydrological year largely in a state of storage excess due to an overshoot in potential energy. Soil water dynamics is mainly driven by differences in potential energy, which means that the linear and non-local gravitational control dominates. Most interestingly we found that the free energy state of the soil operated for a considerable time of the year in the linear range of the P-regime, which implies that the storage dynamics is (multi) linear. This means that the specific free energy density is at each HAND level a linear function of relative saturation, but the slope of the energy state curves does increase with increasing geopotential. We found furthermore that the annual variation of the averaged free energy of the soil water stock was rather small. Zehe et al. (2013) found a similar, almost steady state behavior, for the averaged free energy of the soil water stock in the Mallalcahuello catchment in Chile, which also operated in the P-regime the entire year. Note that both landscapes are characterized by a pronounced topography, by well drained highly porous soils (Blume et al., 2008a; Blume et al., 2008b; Blume et al., 2009) and that both are predominantly forested. In both landscape subsurface storm flow and thus storage controlled runoff generation is the dominant mechanism of streamflow generation. This is consistent with our finding that gravity is the dominant control of soil water dynamics.

On the contrary the Wollefsbach was characterized by a seasonal change between both regimes: operation in the P-regime during the wet season and a drop to a C-Regime and a storage deficit during the dry summer period. Free energy was at all sites on average negative, and a non-linear function of the relative saturation. Interestingly we found the same seasonality for the Weiherbach catchment in Germany, a dominance of potential energy during the wet season and a strong dominance of capillary surface energy in summer (Zehe et al 2013). Note that both landscapes are characterized by cohesive soils, more silty in the Weiherbach and more clay rich in the Wollefsbach, and a gentle topography. And both are used for agriculture. In both areas Hortonian overland flow would play the dominant role, but this process is actually strongly reduced due to a large amount of worm burrows acting as macropores (Zehe and Blöschl; 2004; Schneider et al., 2018) . Both landscapes are also controlled by tile drains. In both areas the soil water dynamics is dominated by capillarity during the summer period, which means that the local soil physical control dominates root zone soil moisture dynamics.

5.3 Concluding remarks

Overall we conclude that a thermodynamic perspective on hydrological systems provides valuable insights helping us to better understand and characterize different landscapes. Given the strong relation between a potential energy excess of soil water in the riparian zone and the onset of storage controlled streamflow production we found in our study areas it seems promising to further explore the value of free energy for hydrological predictions. We also conclude that it makes sense to use the terms wet and dry only with respect to the equilibrium storage as meaningful reference point, because the latter determines whether the soil is with respect to the free energy state in a state of storage excess or a storage deficit. Another key finding is that the energy level function, which can be seen as a straightforward generalization of the soil retention function, accounts jointly for capillary and gravitational control on soil moisture dynamics. With this we link the non-linear soil physical control and the topographical control on storage dynamics in a stratified manner and use HAND as a surrogate for the gravitational potential. A nice co-lateral finding is that a linear dependence of free energy on soil saturation does not compromise the non-linearity of soil water characteristics. In contrary it may be explained by the dominance of potential energy for catchments with pronounced topography and during not too dry conditions, and this implies that at least the energy difference driving soil water dynamics is a linear function of the stored water amount. The latter is the basis of the linear reservoir, which is frequently used in conceptual modelling. The option for linear behavior of the subsurface is hence not only inherent to Darcy's law of the saturated zone, as has been shown by de Rooij (2013) by deriving aquifer scale flow equations for strip aquifers. Even in the top of the unsaturated zone a linear relation between storage and driving potential energy differences might emerge. This inherent option for linear behavior is likely the reason why conceptual models, which usually do not account for soil physical characteristics, work in some catchments very well and in others they don’t. Based on the presented findings one could speculate that conceptual models work well in system which are dominated by potential energy.

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