



1 **Impact of skin effect on single-well push-pull tests with the presence of regional**  
2 **groundwater flow**

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18 **Abstract**

19 Single-well push-pull (SWPP) test is one of the most important ways to estimate aquifer  
20 transport parameters, e.g. porosity, dispersivity, rate of biogeochemical reaction, but its  
21 application for determining the regional groundwater velocity has rarely been discussed in  
22 previous studies. In this study, a new numerical model of SWPP test considering regional  
23 groundwater flow and skin effects was established using the finite-element COMSOL  
24 Multiphysics. The effects of regional groundwater flow velocity and skin properties on  
25 breakthrough curves (BTCs) were thoroughly analyzed. Several important results were  
26 obtained. Firstly, the regional groundwater velocity affects the types of BTCs through  
27 changing the pattern and location of the dividing streamline. Secondly, a positive (or  
28 negative) skin leads to a slower (or faster) tracer transport process. That is, a positive skin  
29 results in a higher concentration at early stage at a given time. Thirdly, a smaller hydraulic  
30 conductivity ratio  $\delta$  of the positive skin to the formation results in greater solute plume  
31 retardation in the skin zone. Besides, a larger thickness of the positive skin leads to a higher  
32 tracer concentration around the well. The opposite is true if the skin is negative. The general  
33 conclusion is that the skin effects on SWPP test are significant and should be considered.

34 **Keywords: push-pull test, regional groundwater velocity, solute transport, skin effect**



35 **1. Introduction**

36 The single-well push-pull (SWPP) tests have been commonly employed to estimate  
37 aquifer parameters, e.g. regional groundwater flow velocity, porosity, dispersivity,  
38 biogeochemical reaction rate (Gelhar and Collins, 1971; Hall et al., 1991; Schroth and Istok,  
39 2006). The process of this test can be summarized as follows: A tracer is injected into a target  
40 aquifer (push), then the mixed solution is pumped out from the same location (pull).  
41 Groundwater samples are taken at regular time intervals at the test well during the pumping  
42 process, and parameters can be obtained by fitting the observed breakthrough curves (BTCs)  
43 using a proper mathematical model. Generally, a complete SWPP test may consist of four  
44 phases: tracer injection, chasing, rest, and pumping. The chasing phase is to push the tracer  
45 away from the injection well (Istok et al., 1997), and the rest phase is for tracer to diffuse  
46 and/or react with the aquifer (if a reactive tracer is employed). Conservative or reactive  
47 tracers can be utilized, depending on the purpose of the test. In general, conservative tracers  
48 have been widely used to estimate regional groundwater flow velocity, porosity, and  
49 dispersivity, etc. (Leap and Kaplan, 1988; Haggerty et al., 2001; Hebig-Schubert, 2014).  
50 Similarly, one can obtain the information of sorption, cation exchange, microbial processes  
51 by applying reactive tracers (Trudell et al., 1986; Field et al., 2000; Tong et al., 2016). For  
52 instance, Tong et al. (2016) used SWPP tests to validate the abundant production of hydroxyl  
53 radicals due to the oxidization of subsurface sediments.

54 To interpret the SWPP test results, a proper mathematical model considering the  
55 fundamental physical and biogeochemical processes of the test is indispensable (Haggerty et  
56 al., 2001; Kleikemper et al., 2002; Schroth and Istok, 2006). From a transport perspective,



57 many existing models are governed by the conventional advection-dispersion equation  
58 (ADE), assuming the validity of Fick's law in the SWPP tests (Schroth et al., 2000; Huang et  
59 al., 2010). Subsequently, many analytical and numerical solutions of various single-well  
60 models have been developed. For instance, Huang et al. (2010) obtained an exact analytical  
61 solution of SWPP test by using Fick's law, considering a partially penetrating well in the  
62 aquifer. Besides ADE, a number of non-Fickian transport models of SWPP tests have also  
63 been developed in recent years to recognize the influence of media heterogeneity, especially  
64 in fractured aquifers (Chen et al., 2017). Such models include multi-rate mass transfer models  
65 (Haggerty et al., 2001), continuous time random walk (CTRW) (Le Borgne and Gouze,  
66 2008), and fractional advection-dispersion equation (FADE) models (Benson et al., 2004;  
67 Chen et al., 2017), to name a few. For instance, Chen et al. (2017) developed a fractional  
68 model of multistage SWPP test to simulate non-Fickian behavior for a fractured aquifer. In  
69 addition, Schroth et al. (2005) obtained an approximate analytical solution of SWPP test for  
70 spherical-flow conditions. Wang et al. (2017) investigated the impacts of transient flow and  
71 wellbore storage on SWPP test under transient Forchheimer flow using a finite-difference  
72 method.

73 As mentioned above, SWPP test is a powerful tool for aquifer characterization, including  
74 the determination of regional groundwater flow velocity. Traditionally, regional groundwater  
75 flow velocity can be obtained by three or more groundwater monitoring wells in the aquifer  
76 by conducting the natural gradient tracer tests rather than the SWPP tests (Pickens et al.,  
77 1981; Michie, 1996; Zimmermann and Huenges, 1999). However, the natural gradient tracer  
78 tests usually take much longer time to complete. This is particularly troublesome when the



79 medium is less permeable, and the regional groundwater flow velocity is relatively small  
80 (Schubert et al., 2011). The natural gradient tracer test method is also very costly to  
81 implement in deep aquifers as the installation of multiple wells in deep aquifers can be  
82 formidably expensive. In contrast, the SWPP test only needs a single well, thus can  
83 substantially reduce the cost of test, and becomes a nice alternative for the determination of  
84 regional groundwater flow velocity (Leap and Kaplan, 1988; Butler et al., 2009). To serve  
85 such a purpose, the SWPP tests usually consist of three phases: tracer injection, rest, and  
86 pumping. The rest phase allows the injected tracer to drift with regional groundwater  
87 velocity, thus it is a key phase to include. Leap and Kaplan (1988) obtained an equation for  
88 push-pull test to determine regional groundwater flow velocity in a confined aquifer, and a  
89 series of laboratory tests were conducted to verify the accuracy of the model, but the test  
90 results showed that if the solute transport drifted over the location of dividing streamline  
91 toward downstream, the calculated results of the regional flow velocity would produce a large  
92 error with the comparison to the actual value. After that, Hall et al. (1991) presented another  
93 type of SWPP test for determining regional groundwater velocity and effective porosity based  
94 on the method of Leap and Kaplan (1988), but Hall et al. (1991) required a directly  
95 downgradient monitoring well. It is notable that both approaches mentioned above have some  
96 limitations for determining regional groundwater velocity.

97 In addition, the impacts of skin near a pumping well are usually neglected for a SWPP  
98 test, which might bring about great errors for the estimation of aquifer parameters and  
99 regional groundwater flow velocity. During the process of well implementation, the intrusion  
100 of drilling mud into the aquifer in the vicinity of well is inevitable, which can result in the



101 change of the porosity and permeability surrounding the well screen (Hurst et al., 1969). This  
102 phenomenon can be regarded as the skin effect (Chen and Chang, 2002; Wang et al., 2012).  
103 The thickness of skin usually ranges from a few millimeters to several meters (Novakowski,  
104 1989). The skins can be classified into positive and negative types according to the hydraulic  
105 conductivity contrast between the skin and the formation zone. If the hydraulic conductivity  
106 of the skin is smaller than that of the formation zone, the skin is defined as a positive one.  
107 Otherwise, it is a negative skin (Park and Zhan, 2002; Yeh et al., 2003; Wen et al., 2011).  
108 Such a skin, regardless of positive or negative, will inevitably alter the flow field near the test  
109 well, thus its effect must be taken into consideration for interpreting the SWPP test. For  
110 instance, the streamlines of skin zone can converge toward the well in the case of a negative  
111 skin, but the opposite is true for a positive skin (Drost et al., 1968; Schubert et al., 2011).

112 In summary, the skin effect is a very important issue from the perspective of SWPP test  
113 interpretation. Through a careful check on the literature, we notice that the model of SWPP  
114 for estimating groundwater flow velocity needs further investigation, besides, the impacts of  
115 skin effects on SWPP tests for estimating groundwater flow velocity have rarely been  
116 studied, which will be the purpose of this study. To accomplish the objective, we will  
117 investigate a SWPP test containing three phases of injection, rest and pumping using a fully  
118 penetrating well. We will use the finite-element COMSOL Multiphysics to numerically  
119 simulate the steady-state, two-dimensional (2D) horizontal flow, with specific attention paid  
120 to the skin effect.

## 121 2. Mathematical model of the SWPP test



122 To illustrate the problem, we will use a conservative tracer. A confined aquifer is  
 123 assumed to be unbounded laterally with a uniform regional groundwater flow presented over  
 124 the entire duration of test. The aquifer is assumed to be homogeneous and horizontally  
 125 isotropic. A fully penetrating well is used so only the horizontal flow is of concern here. Flow  
 126 is assumed to be Darcian and transport is assumed to be Fickian. The test well radius is  
 127 assumed to be sufficiently small so that the wellbore effect is not a concern. The tracer is  
 128 injected with a constant rate and a constant concentration at the injection phase and is  
 129 pumped with a constant rate (which could be different from the injection rate) at the pumping  
 130 phase, after a certain period of rest phase to allow the injected tracer drifting with the regional  
 131 groundwater flow. The coordinate system is established as follows with the origin at the  
 132 center of the test well and the  $x$ -axis pointing to the direction of regional groundwater flow. A  
 133 2D schematic diagram investigated here is depicted in Fig.1.

### 134 **2.1 Mathematical model of groundwater flow**

135 Flow of the SWPP test is assumed to be steady-state, thus the groundwater flow velocity  
 136 can be expressed as the superposition of the flow component generated by the pumping well  
 137 and the regional flow:

$$138 \quad \vec{v} = \vec{v}_1 + \vec{v}_2 \quad (1)$$

$$139 \quad \vec{v}_1 = v_1 \vec{e}_r = Q / (2\pi\theta Br) \vec{e}_r \quad (2)$$

$$140 \quad \vec{v}_2 = v_2 \vec{e}_x = (-KJ / \theta) \vec{e}_x = (v_d / \theta) \vec{e}_x \quad (3)$$

$$141 \quad r = \sqrt{x^2 + y^2} \quad (4)$$

142 where the arrow over a symbol represents a vector hereinafter;  $\vec{v}_1$  is the average radial pore  
 143 velocity vector generated by the injection (or pumping well) with a magnitude of  $v_1$  [L/T] and



144  $\vec{e}_r$  is a unit vector along the radial direction;  $\vec{v}_2$  is the regional groundwater pore flow  
 145 velocity vector with a magnitude of  $v_2$  [L/T] and  $v_d$  is the regional groundwater Darcy flow  
 146 velocity, and  $\vec{e}_x$  is a unit vector long the  $x$ -axis;  $\vec{v}$  is the lumped groundwater flow velocity  
 147 near the well [L/T];  $B$  is the aquifer thickness [L];  $r$  is the radial distance [L];  $Q$  is the  
 148 injection or pumping rate [L<sup>3</sup>/T], which is positive for the injection and negative for pumping,  
 149 and  $Q$  is 0 during the rest phase;  $K$  is aquifer hydraulic conductivity [L/T];  $J$  is the hydraulic  
 150 gradient of regional flow [L/L];  $\theta$  is the aquifer effective porosity [dimensionless], which is  
 151 assumed to be the same as the total porosity of the aquifer when all the pore spaces are well-  
 152 connected with negligible immobile porosity;  $r$  is the radial distance [L] from the well and  $x$   
 153 and  $y$  are two horizontal coordinates [L], parallel and perpendicular to the regional  
 154 groundwater flow direction, respectively.

155 According to Fig.1, the boundary conditions for the domain of concern can be expressed  
 156 as:

$$157 \quad H(x, y)|_{s_1} = H_1, \quad H(x, y)|_{s_2} = H_2 \quad (5)$$

$$158 \quad K \frac{\partial H}{\partial n}|_{s_3} = 0, \quad K \frac{\partial H}{\partial n}|_{s_4} = 0 \quad (6)$$

159 where  $s_1, s_2, s_3$  and  $s_4$  are the boundaries of the model;  $s_1$  and  $s_2$  are constant-head boundaries  
 160 with prescribed heads of  $H_1$  and  $H_2$ , respectively; both  $s_3$  and  $s_4$  are no-flux boundaries.

161 Therefore, a constant regional flow field can be generated and one can obtain different values  
 162 of  $v_2$  by changing the head differences of  $H_1$  and  $H_2$ .

## 163 2.2 Mathematical model of solute transport

164 The ADE of a conservative solute without source/sink can be written as:





$$165 \quad \frac{\partial C}{\partial t} = \nabla \cdot (D \nabla C) - \nabla \cdot (\vec{v} C) \quad (7)$$

166 where  $C$  is the solute concentration [ $M/L^3$ ];  $t$  is the transport time [T];  $D$  is the hydrodynamic

167 dispersion [ $L^2/T$ ];  $\nabla \cdot$  and  $\nabla$  are the divergence operator and the gradient operator

168 respectively; the hydrodynamic dispersion is a velocity-dependent tensor depicted as:

$$169 \quad D_{xx} = \frac{\alpha_L v_x^2}{|\vec{v}|} + \frac{\alpha_T v_y^2}{|\vec{v}|} + D_{diff} \quad (8)$$

$$170 \quad D_{yy} = \frac{\alpha_L v_y^2}{|\vec{v}|} + \frac{\alpha_T v_x^2}{|\vec{v}|} + D_{diff} \quad (9)$$

$$171 \quad D_{xy} = D_{yx} = (\alpha_L - \alpha_T) \frac{v_x v_y}{|\vec{v}|} \quad (10)$$

$$172 \quad v = \sqrt{v_x^2 + v_y^2} \quad (11)$$

173 where  $D_{xx}$ ,  $D_{xy}$ , and  $D_{yy}$  are components of the hydrodynamic dispersion coefficient tensor

174 [ $L^2/T$ ];  $D_{diff}$  is the molecular diffusion coefficient [ $L^2/T$ ];  $\alpha_L$  is the longitudinal dispersivity

175 [L];  $\alpha_T$  is the transverse dispersivity [L]; the transverse dispersion effect is much smaller, thus

176 one usually assumes  $\alpha_L = 10\alpha_T$  (Guvanasen and Guvanasen, 1987; Chen et al., 1999; Chen et

177 al., 2006);  $v_x$  is pore velocity in the  $x$  direction;  $v_y$  is pore velocity in the  $y$  direction.

178 The initial condition is:

$$179 \quad C(r, 0) = 0, \quad (12)$$

180 During the injection phase, the inner boundary condition inside the well can be

181 described as:

$$182 \quad C(r, t) = C_0, \quad r = r_w, 0 < t < t_{inj} \quad (13)$$

183 where  $C_0$  represents the concentration of the injection phase [ $M/L^3$ ];  $r_w$  is the well radius [L];

184  $t_{inj}$  is the duration of the injection phase [T]. The third-type boundary condition may also be



185 used to replace the first-type boundary condition of Eq. (13). However, our numerical  
186 exercises indicate that both conditions yield nearly the same results except for a very short  
187 period of time since the start of injection. Therefore, without loss of generality, we use the  
188 first-type boundary condition here as an example to illustrate the methodology.

189 During the rest phase, the solute flux from the borehole into the aquifer is zero, but the  
190 solute concentration around the borehole is nonzero, therefore, rather than a constant  
191 concentration boundary, a constant-flux (or the third-type) boundary is more reasonable and  
192 can be described as:

$$193 \quad v_1 C - D \frac{\partial C}{\partial r} \Big|_{r \rightarrow r_w^-} = 0, \quad t_{inj} < t < t_{res} \quad (14)$$

194 where  $t_{res}$  is the duration of the rest phase [T]. Eq. (14) represents a zero-flux boundary.

195 During the rest phase,  $Q$  is 0.

196 During the pumping phase, the time-dependent concentration is measured in the  
197 borehole. The main target of the test is to obtain several parameters by fitting the observed  
198 breakthrough curves (BTCs) with corresponding theoretical BTCs obtained from a proper  
199 analytical or numerical solution. When solute transport through well screen, the boundary  
200 condition at the well screen is (Wang et al., 2017):

$$201 \quad \frac{\partial C}{\partial r} \Big|_{r \rightarrow r_w^-} = 0 \quad (15)$$

202 Because the values of velocity and concentration are different around the perimeter of  
203 the borehole, it is necessary to integrate the concentration around the borehole with the  
204 velocity as the weight to obtain the accurate value of concentration at the well, thus, the flux-  
205 averaged concentrations can be expressed as:



$$206 \quad \bar{C} = \frac{\oint_{l_w} v_w C_w}{\oint_{l_w} v_w}, \quad r = r_w, t_{res} < t < t_{pump} \quad (16)$$

207 where  $v_w$  represents the superposition velocity around the borehole during the pumping [L/T];

208  $C_w$  represents the concentration around the well perimeter [M/L<sup>3</sup>];  $\bar{C}$  is the concentration

209 inside the well [M/L<sup>3</sup>];  $l_w$  is the perimeter of the wellbore [L].

### 210 3. Numerical solution of the SWPP test

211 In this study, a steady-state flow model of 2D horizontal plane was developed based on

212 COMSOL Multiphysics, as shown in Fig. 1. The model region was set to be 40 m × 40 m,

213 and the well has a radius of 0.1 m. In addition,  $B=10$  m,  $K=8.0$  m/d,  $\theta=0.3$ . In this model,

214 constant-head boundaries were prescribed, and the value of  $H_2$  was set as constant 15 m,

215 according to Eq. (3), one can obtain different values of  $v_2$  by changing the value of  $H_1$ . In the

216 model, a continuous mass flux of injection or pumping rate was assigned at  $r=r_w$ , which can

217 be expressed as:

$$218 \quad N_0 = \frac{Q\rho}{2\pi r_w B} \quad (17)$$

219 where,  $N_0$  is the mass flux per unit thickness [M/L<sup>2</sup>/T];  $\rho$  is the density of groundwater

220 [M/L<sup>3</sup>]. The SWPP test was divided into three phases, the simulation results at the end of

221 each phase, including the hydraulic head and the solute concentration, were set as the initial

222 values for the simulation in the next phase.

223 A uniform skin near the well was considered in a confined aquifer, and the thickness of

224 the well skin was assumed to be constant and equal to  $r_s$  along the well screen in this model.

225 The skin hydraulic conductivity and effective porosity were set as  $K_s$  and  $\theta_s$  respectively. The

226 default values of the parameters were shown in Table 1.



227 The model domain was discretized into 21688 elements, and the mesh size was  
228 progressively refined near the well. When the number of element is doubled, the peak solute  
229 concentration for the pumping phase varied about 0.17%. Therefore the selected mesh is  
230 regarded as sufficiently fine for the problem investigated here. To check the accuracy of the  
231 numerical model further, the numerical solution for a special case (without skin) was used to  
232 compare with the analytical solution of Huang et al. (2010), who investigated a steady-state  
233 flow SWPP model with injection and extraction phases, without the regional groundwater  
234 flow, as shown in Fig.2. The simulated time span of tracer injection and pumping were 0.5  
235 and 1 day, respectively. The other parameters were given as:  $Q_{inj}= 50 \text{ m}^3/\text{d}$ ,  $Q_{pump}=-50 \text{ m}^3/\text{d}$ ,  
236  $B=10 \text{ m}$ ,  $\alpha_L=0.1 \text{ m}$ , 0.5 m, 1 m, and  $\theta=0.3$ .  $C_0$  at  $r=r_w$  was set as  $1.0 \text{ mol}/\text{m}^3$ . The results  
237 showed that our numerical solution agreed perfectly with the analytical solution. For the  
238 following analysis, the default values of the parameters are listed in Table 1.

#### 239 4. Results and discussions

##### 240 4.1. Effects of regional groundwater velocity on BTCs in the SWPP test

241 Fig. 3 shows the BTCs for the pumping phase with different regional groundwater  
242 velocities, like  $5 \times 10^{-7} \text{ m/s}$ ,  $1 \times 10^{-6} \text{ m/s}$ ,  $1.5 \times 10^{-6} \text{ m/s}$ ,  $2 \times 10^{-6} \text{ m/s}$ ,  $2.5 \times 10^{-6}$  and  $3 \times 10^{-6}$   
243 m/s. Besides,  $\alpha_L=0.1 \text{ m}$ ,  $Q_{inj}= 30 \text{ m}^3/\text{d}$ ,  $Q_{pump}=-15 \text{ m}^3/\text{d}$ , and the other parameters are the  
244 same as those used in Table 1. It is found that different regional groundwater velocities have  
245 great impacts on BTCs, and such impacts depend on the value of the regional groundwater  
246 velocities. It is found that the tracer concentration is smaller at early stage with a greater  
247 regional groundwater velocity. Additionally, it is notable that a larger regional groundwater  
248 velocity will result in a longer tailing.



249 Fig. 4 shows the superposition of flow components generated by the pumping well and  
250 the regional flow. For the pumping phase, one can see that there is a stagnation point (Sp)  
251 located at the dividing streamline (Ds) as shown in Fig.4. For a single tracer particle, whether  
252 it can be extracted out from the aquifer depends on the pattern and location of the dividing  
253 line, which acts like a fishing net to collect all the products together. Therefore, different  
254 convergence situations of tracer due to variable dividing streamlines result in a series of BTC  
255 types. In order to interpret this behavior explicitly, the concentration distributions in a 2D  
256 horizontal plane at  $t_{pump}=0$  hr with different regional groundwater velocities are shown in Fig.  
257 5. One can see that a certain amount of tracer mass may be retained near the symmetry axis  
258 ( $x$ -axis) and around the well when the regional groundwater velocity is relatively low, such as  
259  $v_d=1 \times 10^{-6}$  m/s and  $1.5 \times 10^{-6}$  m/s, as shown in Figs.5a-5b, resulting in relatively high  
260 concentrations in the wellbore at early stage. On the contrary, a larger regional groundwater  
261 velocity leads to a faster tracer transport process, causing the tracer mass drifting away from  
262 the well, as shown in Figs.5c-5d. Besides, one can also see that a larger regional groundwater  
263 velocity leads to a smaller distance from Sp to well, resulting in a smaller portion of tracer  
264 mass that can be extracted during the pumping phase. The opposite is true for the case of a  
265 smaller regional groundwater velocity. For instance, as for the tracer mass on the left side of  
266 the dividing streamline, they can be extracted by smaller velocities such as  $v_d=5 \times 10^{-7}$  m/s  
267 and  $1 \times 10^{-6}$  m/s, as shown in Figs.5a-5b, but very limited tracer can be captured with larger  
268 velocities like  $v_d=3 \times 10^{-6}$  m/s. And this further confirms the reasonability of the BTC types in  
269 Fig. 3.

#### 270 4.2 The effects of $t_{res}$ on BTCs in the SWPP test



271 Fig. 6 shows BTCs for the pumping phase with different  $t_{res}$ , like 6, 12, 24, and 36 hr.  
272 Besides,  $\alpha_L=0.1$  m,  $v_d=3 \times 10^{-6}$  m/s,  $Q_{inj}=30$  m<sup>3</sup>/d,  $Q_{pump}=-15$  m<sup>3</sup>/d and the other parameters  
273 are the same as those used in Table 1. It is found that the tracer concentration is smaller as  $t_{res}$   
274 increases in Fig. 6. This is because a longer time of rest phase means a farther distance of  
275 tracer drifting, leading to a smaller portion of tracer mass that can be extracted during the  
276 pumping phase. In order to interpret this behavior explicitly, the concentration distributions in  
277 a 2D horizontal plane at  $t_{pump}=0$  hr with different  $t_{res}$  are shown in Fig. 7. One can see that a  
278 longer  $t_{res}$  means that more tracer mass drifting over the location of Sp toward downstream,  
279 resulting in lower concentrations in the wellbore during the pumping phase in Fig. 7.  
280 According to the analysis above, there is a strong interaction between regional groundwater  
281 flow and well flow, thus proper choices of the duration of each phase, and the injection and  
282 pumping rates are vital for the success of a SWPP test. For instance, for the case of a  
283 relatively large regional groundwater velocity, one can decrease  $t_{res}$  or increase the magnitude  
284 of  $Q_{pump}$  to recollect the tracer as much as possible, thus avoiding the over- or under-  
285 estimation of hydraulic parameters from the SWPP test.

#### 286 4.3. The effects of porosity on BTCs in the SWPP test

287 Fig. 8 shows the effects of porosity  $\theta$  on BTCs during the pumping phase. The  
288 parameters are given as:  $\theta=0.1, 0.2, 0.3, 0.4$  and  $0.5$  respectively,  $v_d=3 \times 10^{-6}$  m/s,  $\alpha_L=0.1$  m,  
289  $Q_{inj}=30$  m<sup>3</sup>/d, and  $Q_{pump}=-30$  m<sup>3</sup>/d. It can be found that the concentration is smaller at early  
290 stage with a smaller porosity. It is also obvious that a smaller  $\theta$  will result in a longer tailing  
291 at late stage. The explanation is similar to that for Fig. 3, i.e., a smaller  $\theta$  means a faster pore  
292 velocity, resulting in faster solute transport according to Eq. (3).



#### 293 4.4. The effects of dispersivity on BTCs in the SWPP test

294 Fig. 9 shows the effect of  $\alpha_L$  on BTCs for the pumping phase. The values of  $\alpha_L$  are set as:

295  $\alpha_L = 0.01$  m, 0.05 m, 0.1 m, 0.5 m and the other parameters are given as:  $v_d = 2 \times 10^{-6}$  m/s,

296  $Q_{inj} = 30$  m<sup>3</sup>/d, and  $Q_{pump} = -30$  m<sup>3</sup>/d. As shown in Fig. 9, one can see that  $\alpha_L$  has a significant

297 impact on BTCs. At early stage of pumping, the concentration shows a decreasing trend with

298 increase of  $\alpha_L$ , This is because a larger dispersivity means a faster tracer transport, given the

299 same regional groundwater velocity, which causes much broader solute plume after the

300 injection and rest phases. A smaller dispersivity means a narrower solute plume. Therefore,

301 different dispersivities can change the characteristics of BTCs under the influence of regional

302 groundwater velocity.

#### 303 4.5. The effects of skin hydraulic conductivity on BTCs in the SWPP test

304 As mentioned above, the well skin includes two general types, i.e., a positive skin or a

305 negative skin. Denoting the hydraulic conductivities of skin and aquifer (or formation zone)

306 respectively as  $K_s$  and  $K$ , one can use a new parameter  $\delta = K_s/K$  to reflect the skin impact,

307 where  $\delta$  is a parameter reflecting the type of the skin and called the “skin index” hereinafter.

308 Specifically,  $\delta < 1$  represents a positive skin, while  $\delta > 1$  represents a negative skin. Note that

309 the case of  $\delta = 1$  represents the case without a skin. In this section, we will provide a detailed

310 analysis on the impact of the skin hydraulic conductivity on SWPP test.

##### 311 4.5.1 Positive skin

312 Fig. 10 shows the effect of different skin indexes on BTCs for a positive skin case

313 during the pumping phase. The parameters are given as:  $v_d = 3 \times 10^{-6}$  m/s,  $Q_{inj} = 30$  m<sup>3</sup>/d,

314  $Q_{pump} = -30$  m<sup>3</sup>/d,  $\alpha_L = 0.1$  m,  $r_s = 0.6$  m,  $\delta = 1, 0.5, 0.25$  and 0.125, respectively. The results



315 indicate that the concentration gets higher at early stage of pumping when the skin index is  
316 lower, as shown in Fig. 10. This may be explained as follows. A skin with a lower  $\delta$  value (or  
317 a lower permeability value in respect to that of the formation) essentially serves as a  
318 somewhat “shield” around the test well that can make the spreading of the tracer mass out of  
319 the test well more difficult during the injection phase. Consequently, more tracer mass will be  
320 retained near the test well either in the skin or near the skin in the formation zone. Therefore,  
321 during the pumping phase of the test, more tracer mass can be extracted during the early stage  
322 of the pumping phase, leading to higher concentration during that stage. To further explicitly  
323 interpret this behavior, the concentration distributions in a 2D horizontal plane at  $t_{pump}=0$  hr  
324 with different  $\delta$  values are shown in Fig. 11. As can be seen in Fig.11, a lower skin hydraulic  
325 conductivity leads to more tracer accumulation in the skin zone after the rest phase. For  
326 instance, one can see that the solute plumes with high concentrations are clearly visible in  
327 skin zones for the cases of  $\delta=0.25$  and  $0.125$ .

#### 328 4.5.2 Negative skin

329 Fig. 12 shows the effect of different skin indexes on the BTCs for a negative skin case.  
330 The parameters are given as:  $v_d=3 \times 10^{-6}$  m/s,  $Q_{inj}= 30$  m<sup>3</sup>/d,  $Q_{ext}=-30$  m<sup>3</sup>/d,  $\alpha_L=0.1$  m,  $r_s=0.6$   
331 m, and  $\delta=1, 1.5, 2$  and  $3$ . In contract to what has been observed in Fig. 10 for a positive skin,  
332 the results indicate that the concentration gets lower at early stage of pumping when the skin  
333 index ( $\delta$ ) increases. This is because a negative skin is somewhat like a “high conductance  
334 zone” rather than a “shield”, and can facilitate the spreading of tracer mass away from the test  
335 well during the injection phase. Therefore, less tracer mass will be retained near the test well  
336 for a higher skin index, thus less concentration will be seen during the early stage of pumping





337 in the wellbore. Similar to what has been done for a positive skin in Fig. 11, the concentration  
338 distributions in a 2D horizontal plane at  $t_{pump}=0$  hr with different skin indexes are shown in  
339 Fig. 13. It is quite obvious to see that a larger skin hydraulic conductivity leads to a less tracer  
340 concentration in the skin zone at the early stage of the pumping phase. For instance, one can  
341 see that tracer accumulation in the skin zone for the cases of  $\delta=2$  and 3 are clearly less than  
342 the cases of  $\delta=1$  and 1.5.

#### 343 4.6. Effects of skin thickness on BTCs in the SWPP test

344 In this section, we will analyze the impacts of the skin thickness on BTCs.

##### 345 4.6.1 Positive skin

346 Firstly, we will analyze the impacts of the skin thickness on BTCs for a positive skin  
347 case. The parameters are given as:  $v_d=3 \times 10^{-6}$  m/s,  $Q_{inj}=30$  m<sup>3</sup>/d,  $Q_{ext}=-30$  m<sup>3</sup>/d,  $\delta=0.5$   
348 (positive skin),  $\alpha_L=0.1$  m, and  $r_s=0, 0.2, 0.4$  and  $0.6$  m, respectively. Fig. 14 shows the  
349 effects of the skin thickness (positive skin) on BTCs during the pumping phase. One can see  
350 that the concentration gets higher at early stage with the increase of  $r_s$ . The explanation is  
351 similar to that for Fig. 10, as a thicker positive skin means a thicker “shield” surrounding the  
352 test well, preventing the injected tracer mass from spreading further away from the test well,  
353 thus leading to higher concentrations during the early stage of the extraction phase. The  
354 concentration distributions in a 2D horizontal plane at  $t_{pump}=0$  hr with different positive skin  
355 thickness are shown in Fig. 15. It is evident that the tracer mass still accumulates in the skin  
356 zone 24 hr after the cease of the injection phase (rest phase), and the concentration is higher  
357 in the skin zone than that in the formation zone (see the case of  $r_s=0.6$  m). Besides, more



358 tracer can be found in the skin region with the increase of  $r_s$ , resulting in different shapes of  
359 BTCs in Fig.14.

#### 360 4.6.2 Negative skin

361 Similarly, we have also analyzed the impacts of the skin thickness on BTCs for a  
362 negative skin case. The parameters are given as:  $v_2=3 \times 10^{-6}$  m/s,  $Q_{inj}=30$  m<sup>3</sup>/d,  $Q_{ext}=-30$   
363 m<sup>3</sup>/d,  $\delta=2$  (negative skin),  $\alpha_L=0.1$  m,  $r_s=0, 0.2, 0.4$  and  $0.6$ m. Fig. 16 shows the effect of the  
364 skin thickness (negative skin) on BTCs during the pumping phase. At early stage, it can be  
365 found that the concentration shows a decreasing trend with the increase of  $r_s$ , and the peak  
366 values of BTCs also decrease with the increase of  $r_s$ . The explanation is similar to that for  
367 Fig. 12 as a thicker negative skin means a thicker high conductance zone surrounding the test  
368 well, which will facilitate the spreading of injected tracer mass further away from the test  
369 well. This is further supported by the concentration distributions in a 2D horizontal plane 24  
370 hr after the cease of injection (rest phase) with different negative skin thickness, as shown in  
371 Fig.17. It is evident from Fig. 17 that a greater portion of tracer mass migrates away from the  
372 test well after the cease of injection with a greater  $r_s$ . For instance, at early stage of extraction,  
373 one can see that the BTC values in the case of  $r_s=0.6$  m are lower than those in the case of  
374  $r_s=0.2$  m in Fig.16, and the tracer is transported further away from the test well in the case of  
375  $r_s=0.6$  m than that in the case of  $r_s=0.2$  m in Fig.17.

#### 376 5. Conclusions

377 In this study, a numerical model for a SWPP test with the presence of a regional  
378 groundwater flow field, considering both the positive and negative skin effects was  
379 investigated. There is a strong interaction between regional groundwater flow and well flow,



380 thus proper choices of the duration of each phase, and the injection and pumping rates should  
381 be done in advance before the SWPP test to recollect the tracer as much as possible. Besides,  
382 the numerical model of SWPP test can be used to obtain unknown parameters: i.e., regional  
383 groundwater velocity, effective porosity, dispersivity, and biogeochemical reaction rates, by  
384 fitting to the observed BTCs. The effects of both the hydraulic conductivities and thickness of  
385 the skin zone on BTCs had also been considered. The following conclusions can be drawn:

- 386 1. Regional groundwater velocity has a significant effect on the shape of BTCs, a lower  
387 regional groundwater velocity means that more tracer can be accumulated near the  
388 symmetry plane around the well. The opposite is true for a case of a larger regional flow  
389 velocity, resulting in a longer tailing of BTCs obtained during the extraction phase. In  
390 addition, the pattern and location of the dividing streamline determine the quantity of tracer  
391 mass extracted during the pumping phase.
- 392 2. We have proposed a skin index which is essentially the skin/formation hydraulic  
393 conductivity ratio to quantify the skin impact. A larger skin index results in a lower  
394 concentration for BTCs at early stage of pumping. On the contrary, a smaller skin index  
395 means a higher concentration for BTCs at early stage of pumping. In addition, a smaller  
396 skin index means that solute plume can accumulate more in the skin zone, otherwise, a  
397 larger skin index results in a solute plume drifting further away from the skin zone after the  
398 cease of the injection phase.
- 399 3. The impact of skin effect near a pumping well should not be neglected for SWPP test,  
400 particularly when the regional groundwater flow is presented. The positive (or negative)  
401 skin results in a faster (or lower) tracer transport process. A larger thickness of the positive



402 skin leads to a larger concentration of tracer near the symmetry plane around the well, but

403 the opposite is true for the case with a negative skin.

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492 **Figure Captions:**

493 Fig.1 The schematic diagram of the flow system.

494 Fig.2 Comparison between the numerical solutions of this study and the analytical solutions  
495 of Huang et al. (2010).

496 Fig.3 BTCs for different values of  $v_d$  at the well during the pumping phase.

497 Fig.4 The schematic diagram of the flow system for the pumping phase.

498 Fig.5 Concentration distributions in a 2D horizontal plane at  $t_{pump}=0$  hr. a)  $v_d = 1 \times 10^{-6}$  m/s;  
499 b)  $v_d = 1.5 \times 10^{-6}$  m/s; c)  $v_d = 2 \times 10^{-6}$  m/s; d)  $v_d = 3 \times 10^{-6}$  m/s.

500 Fig.6 BTCs for different values of  $t_{res}$  at the well during the pumping phase.

501 Fig.7 Concentration distributions in a 2D horizontal plane at  $t_{pump}=0$  hr. a)  $t_{res} = 6$  hr; b)  $t_{res} =$   
502  $126$  hr; c)  $t_{res} = 24$  hr; d)  $t_{res} = 36$  hr.

503 Fig.8 BTCs at the well during the pumping phase with  $\theta=0.1, 0.2, 0.3, 0.4, 0.5$ .

504 Fig.9 BTCs at the well during the pumping phase with  $\alpha_L=0.01$  m, 0.05 m, 0.1 m, 0.5 m.

505 Fig.10 BTCs for the case of a positive skin at the well during the pumping with  $r_s=0.6$  m, and  
506  $\delta= 1, 0.5, 0.25$  and  $0.125$ .

507 Fig.11 2D horizontal plane distributions of concentration for a positive skin with  $r_s=0.6$  m at  
508  $t_{pump}=0$  hr. a)  $\delta= 1$ ; b)  $\delta= 0.5$ ; c)  $\delta= 0.25$ ; d)  $\delta= 0.125$ .

509 Fig.12 BTCs for the case of a negative skin at the well during the pumping with  $r_s=0.6$  m,  
510 and  $\delta= 1, 1.5, 2$  and  $3$ .

511 Fig.13 2D horizontal plane distributions of concentration for a negative skin with  $r_s=0.8$  m at  
512  $t_{pump}=0$  hr. a)  $\delta= 1$ ; b)  $\delta= 1.5$ ; c)  $\delta= 2$ ; d)  $\delta= 3$ .

513 Fig.14 BTCs for the case of a positive skin at the well during the pumping phase with  $r_s=0$  m,  
514  $0.2$  m,  $0.4$  m,  $0.6$  m.



515 Fig.15 Concentration distributions for a positive skin at 2D horizontal plane after 24 hr of

516 rest. a)  $r_s=0$  m; b)  $r_s=0.2$  m; c)  $r_s=0.4$  m; d)  $r_s=0.6$  m.

517 Fig.16 BTCs for the case of a negative skin at the well during the pumping with  $r_s=0$  m,

518 0.2m, 0.4 m and 0.6 m.

519 Fig.17 Concentration distributions for a negative skin at 2D horizontal plane after 18 hr of

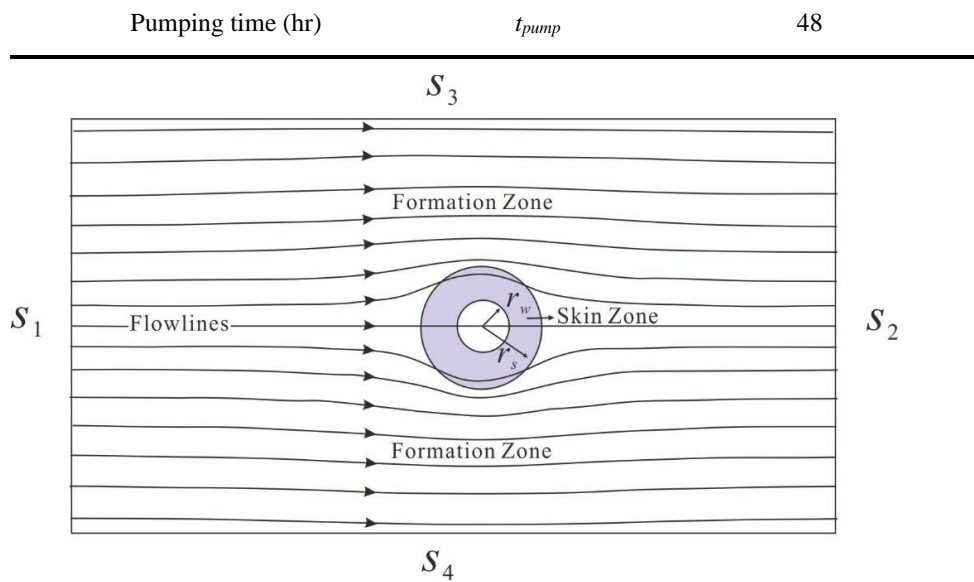
520 rest. a)  $r_s=0$  m; b)  $r_s=0.2$  m; c)  $r_s=0.4$  m; d)  $r_s=0.6$  m.

521



522 Table 1. The parameter values used in this study

Parameter name	Symbols	Values
Aquifer thickness (m)	$B$	10
Radius of well screen (m)	$r_w$	0.1
Density of groundwater(kg/m <sup>3</sup> )	$\rho$	1000
Effective porosity of aquifer	$\theta$	0.3
Hydraulic conductivity of aquifer (m/d)	$K$	8
Constant heads of $S_1$ (m)	$H_1$	15.22, 15.44, 15.69, 15.65, 15.87, 16.08, 16.30
Constant head of $S_2$ (m)	$H_2$	15.0
Regional groundwater Darcy velocities (m/s)	$v_d$	$5 \times 10^{-7}$ , $1 \times 10^{-6}$ , $1.5 \times 10^{-6}$ , $2 \times 10^{-6}$ , $2.5 \times 10^{-6}$ , $3 \times 10^{-6}$
Longitudinal dispersivities of aquifer (m)	$\alpha_L$	0.01, 0.05, 0.1, 0.5
Hydraulic conductivity of skin zone (m/d)	$K_s$	1, 2, 4, 12, 16, 24
Effective porosity of skin zone	$\theta_s$	0.21, 0.24, 0.27, 0.33, 0.36, 0.39
Injection or pumping rate (m <sup>3</sup> /d)	$Q$	15, 30
Mass flux per unit area (kg/(m <sup>2</sup> · s))	$N_0$	0.02765, 0.5529
Injection time (hr)	$t_{inj}$	6
Rest time (hr)	$t_{res}$	24



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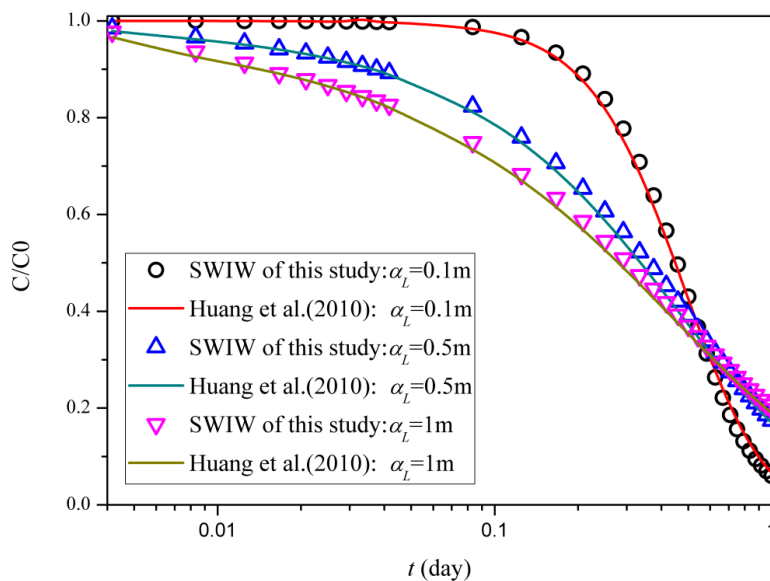
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528 **Fig.1**



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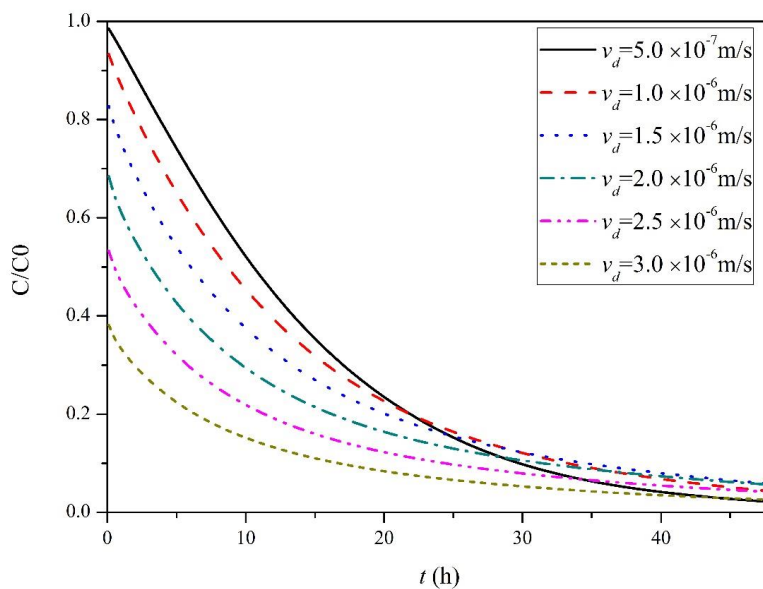
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534 **Fig.2**



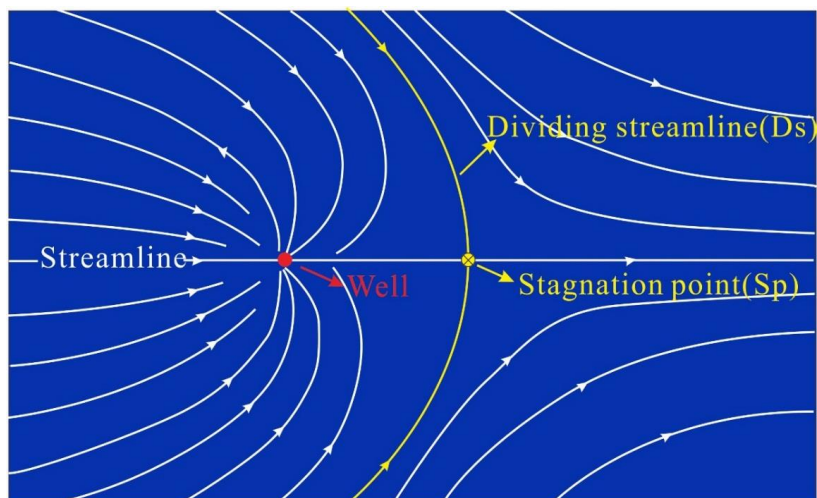
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539 **Fig.3**



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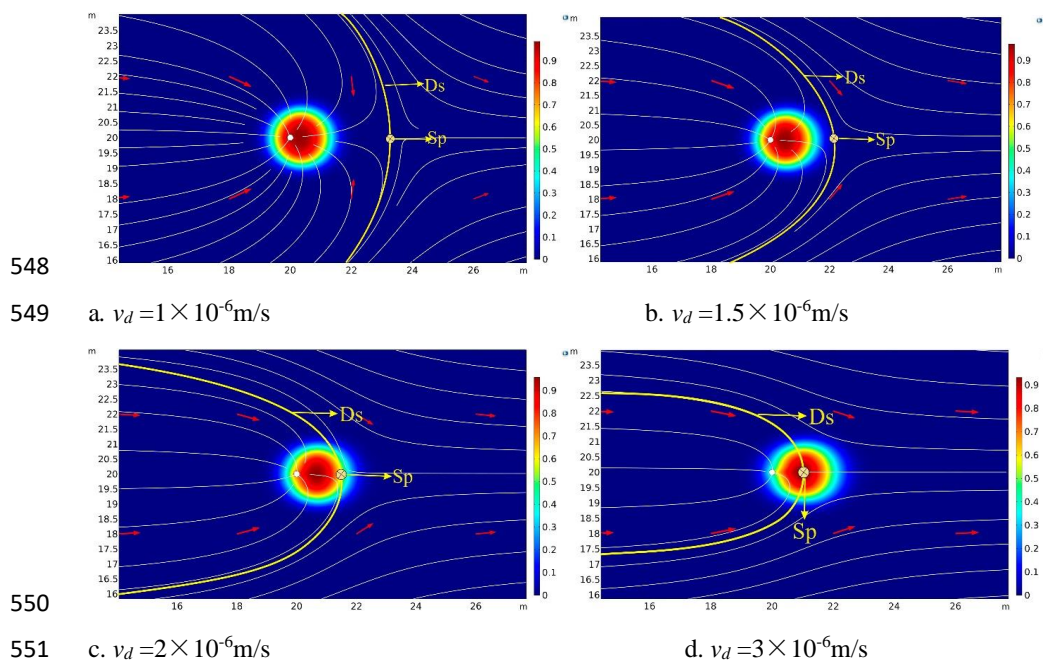
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546 Fig.4

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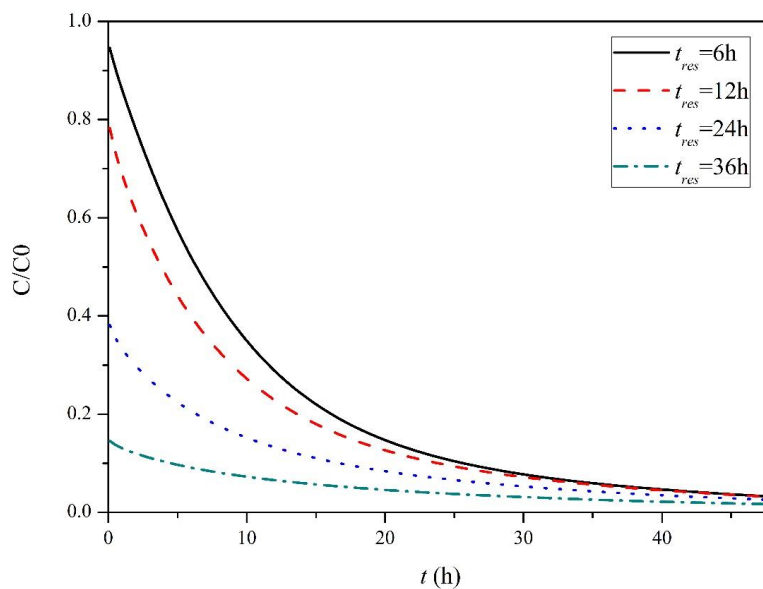
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555 **Fig.5**





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559 Fig.6

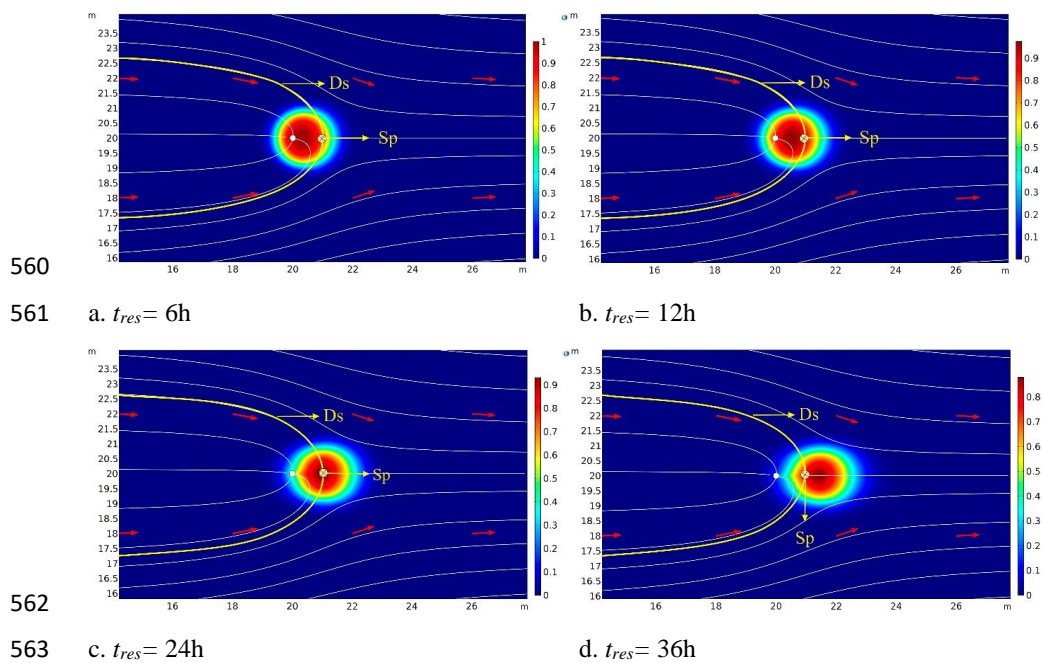
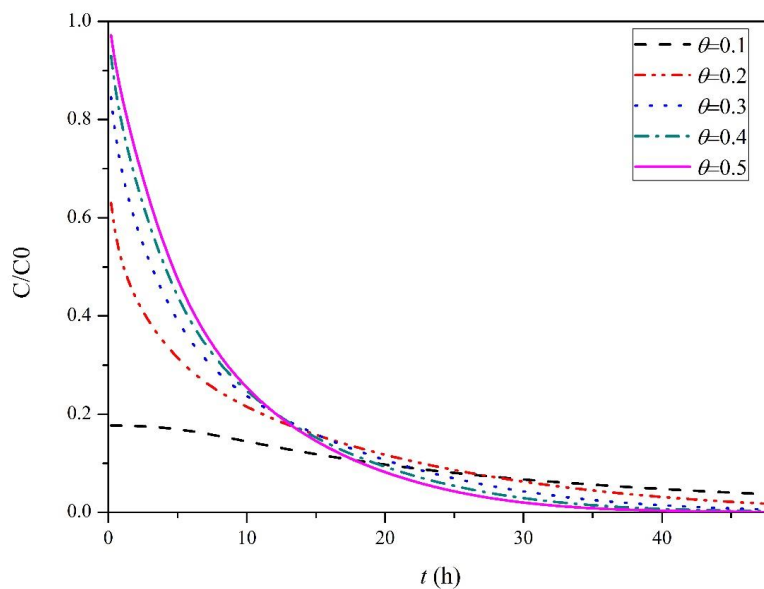


Fig.7



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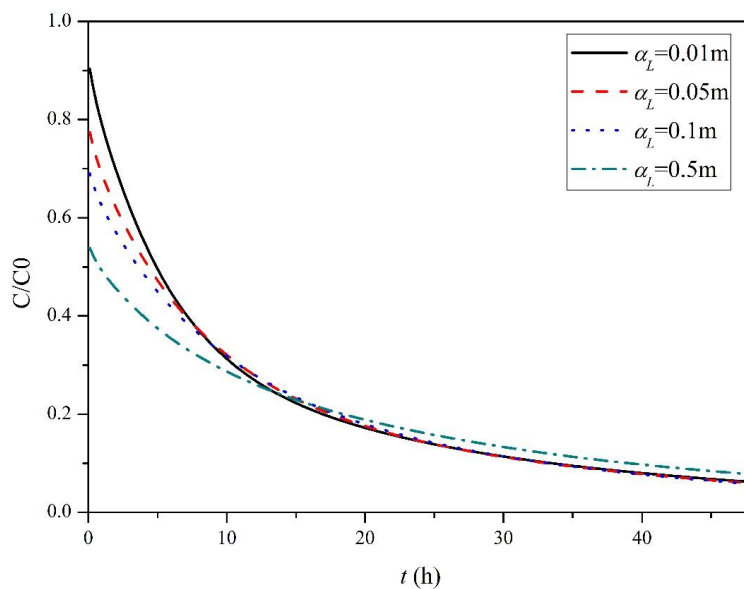
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572 Fig.8



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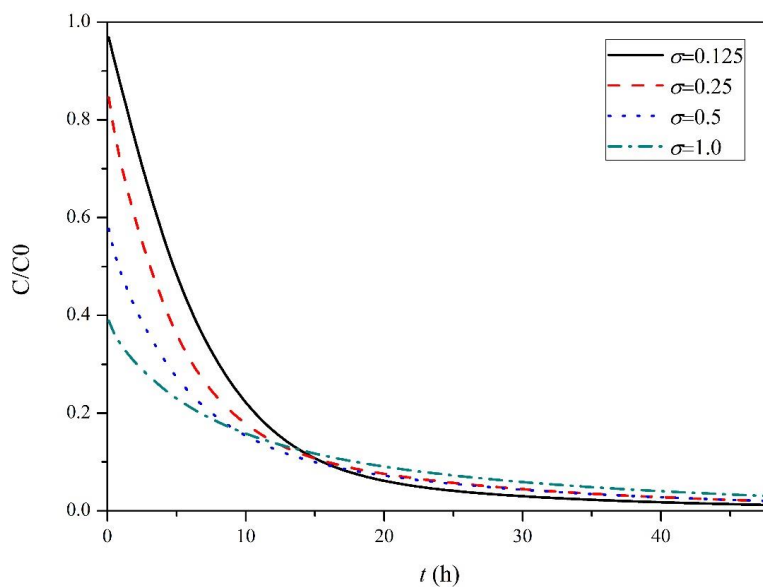


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577 **Fig. 9**



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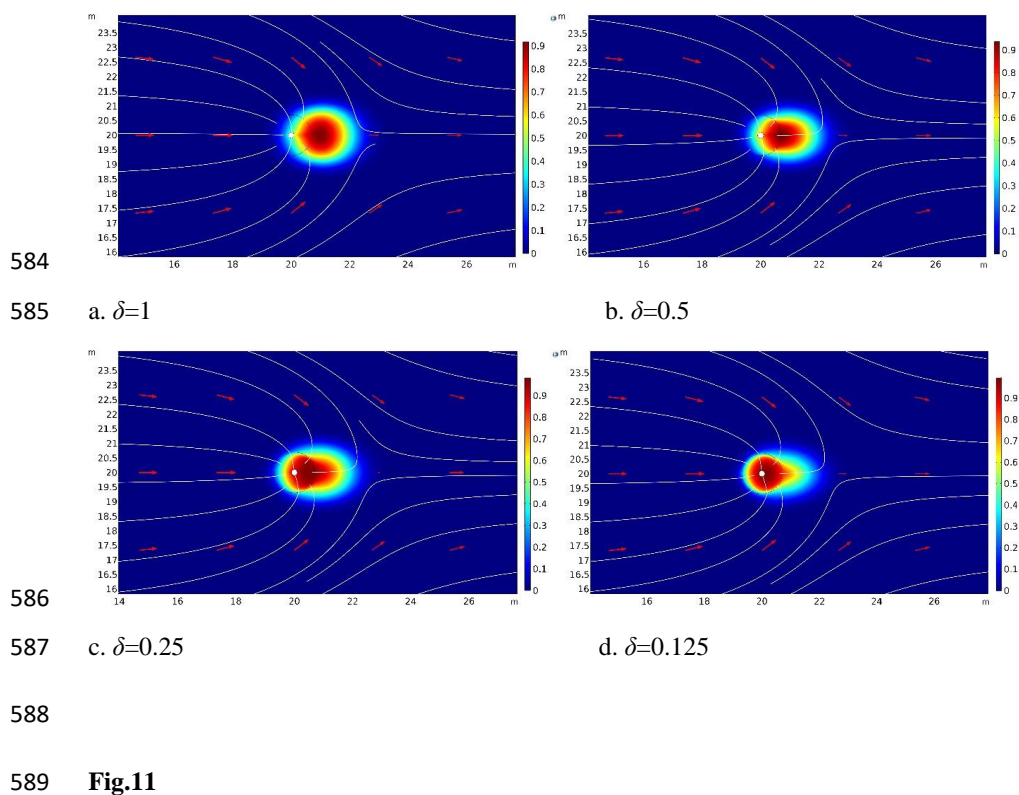
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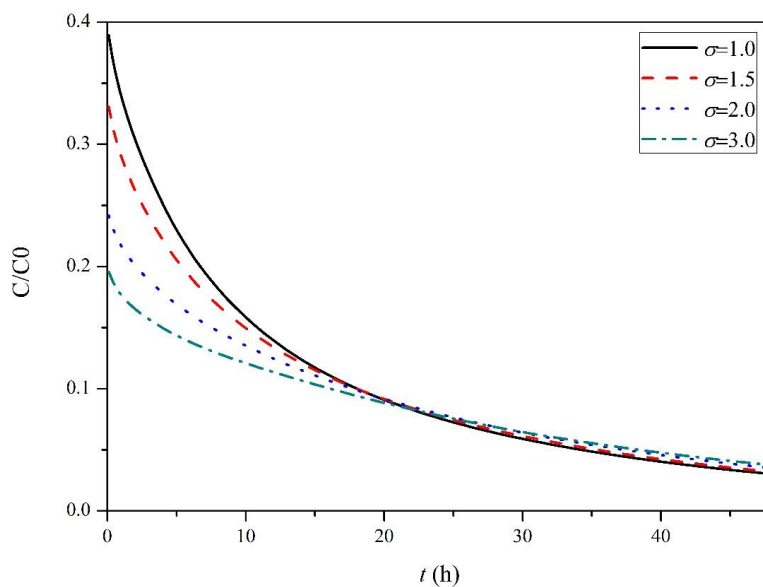
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583 **Fig.10**





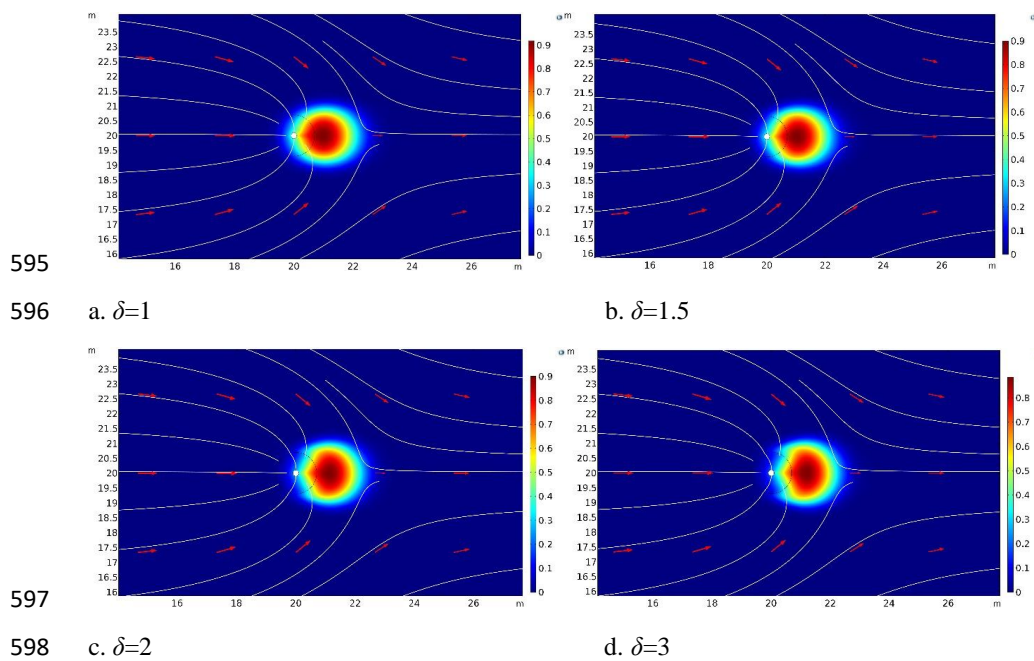
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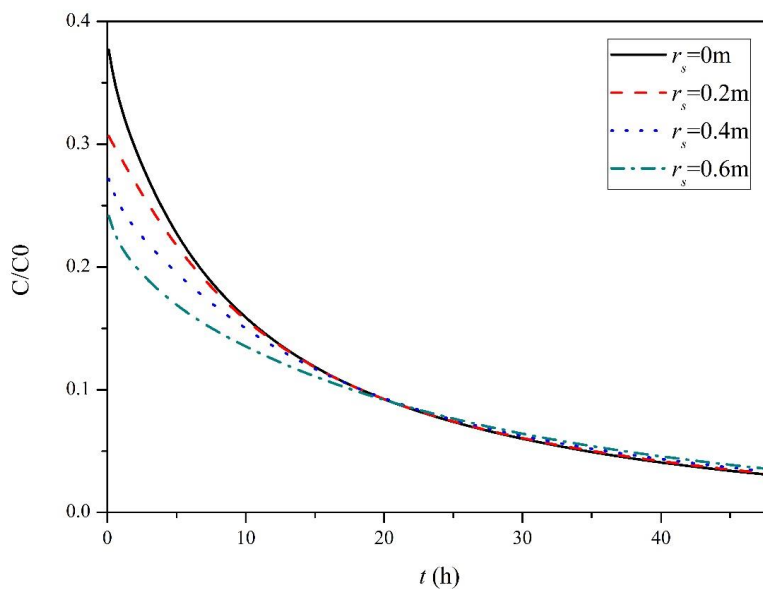
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594 **Fig.12**







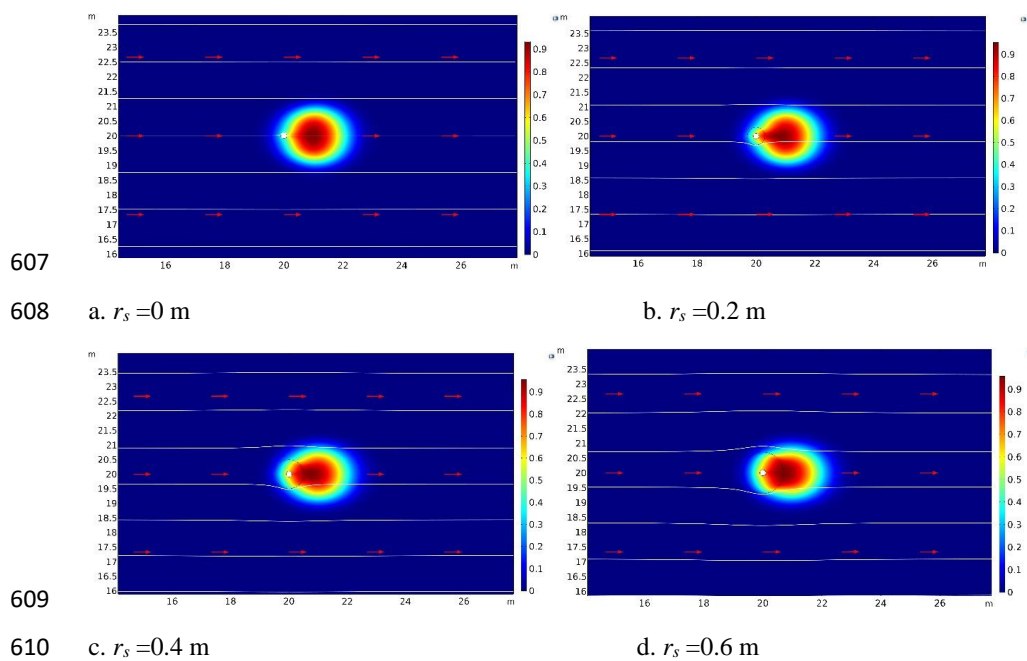
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606 **Fig.14**

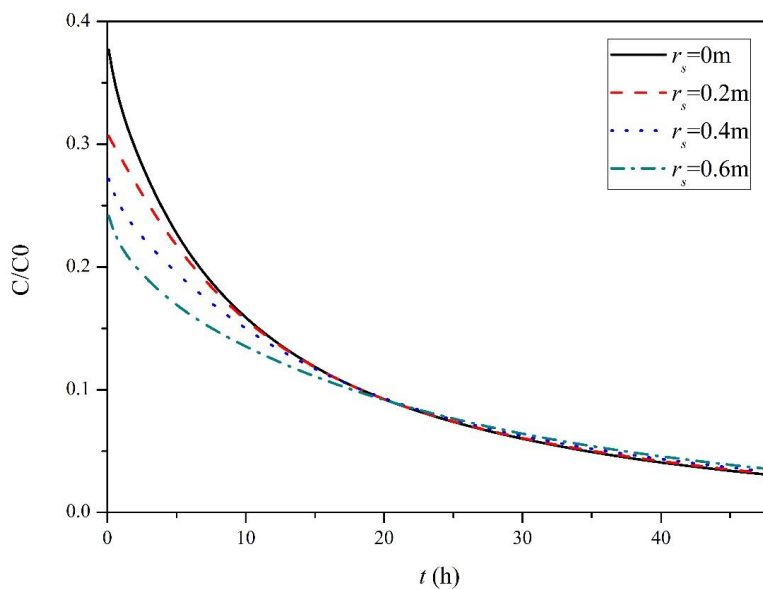


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614 **Fig.15**



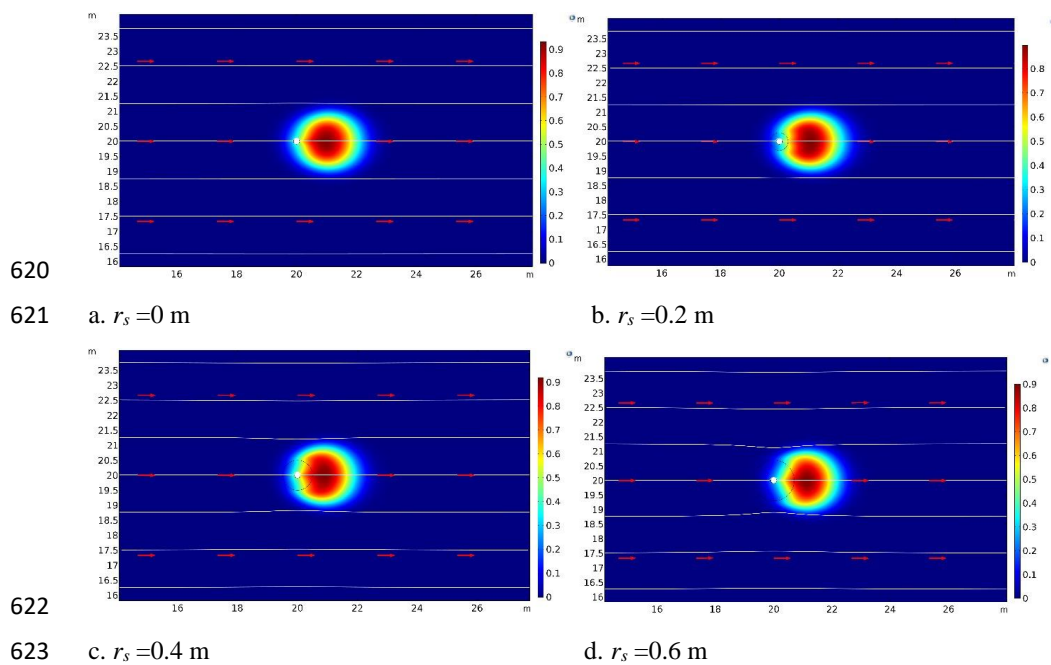
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619 **Fig. 16**



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626 **Fig. 17**

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