





19 **Key Points:**

- 20       • Gap-filling of streamflow data performs well when the missing rate is less than 10%
- 21       • Small number of catchments showing large trend bias when the missing rate is up to
- 22       20%
- 23       • Poor gap-filling occurring in some wet catchments even with reasonable model
- 24       calibration

25

26

27 **Abstract.** Gap-filling streamflow data is a critical step for most hydrological studies, such

28 as streamflow trend, flood and drought analysis and hydrological response variable estimates

29 and predictions. However, there is lack of quantitative evaluation of the gap-filled data

30 accuracy in most hydrological studies. Here we show that when the missing rate is less than

31 10%, the gap-filled streamflow data obtained using calibrated hydrological models perform

32 almost as same as the benchmark data (less than 1% missing) for estimating annual trends for

33 217 unregulated catchments widely spread in Australia. Furthermore, the relative streamflow

34 trend bias caused by the gap-filling is not very large in very dry catchments where the

35 hydrological model calibration is normally poor. Our results clearly demonstrate that the gap-

36 filling using hydrological modelling has little impact on the estimation of annual streamflow

37 and its trends.

38 **Keywords:** streamflow, data, gap-filled, hydrological model, trend

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40



41 **1 Introduction**

42 Streamflow is channel runoff, i.e. the flow of water in streams and rivers and accumulated  
43 from surface runoff from land surface and groundwater recharge. It is one of the major water  
44 balance components in a catchment where precipitation is partially stored in surface water,  
45 soil and groundwater stores, and the rest is partitioned into two fluxes: evapotranspiration and  
46 streamflow. It is almost impossible to measure evapotranspiration dynamics at a catchment  
47 scale. In contrast, streamflow time series can be easily measured at a catchment outlet.  
48 Therefore, streamflow data becomes a fundamental dataset underpinning hydrological  
49 studies. Without such a dataset, it is hard to understand catchment hydrological processes  
50 under climate change and non-stationarity (Dai et al., 2009; Gedney et al., 2006a; Ukkola et  
51 al., 2015; Zhang et al., 2016b).

52 Unfortunately, streamflow data are not always continuously available and most gauges suffer  
53 from streamflow data missing issues (Dai et al., 2009). Often, the missing rate is important  
54 when selecting streamflow gauges, especially when the data is used for annual trend analysis.  
55 To choose qualified catchments, researchers often set up a threshold for the missing ratio, for  
56 instance 1% (Petroni et al., 2010), 5% (Ukkola et al., 2015), 10% (Déry et al., 2009), 15%  
57 (Liu and Zhang, 2017), and 20% (Lopes et al., 2016). Only those gauges with missing rate  
58 less than a particular threshold are selected, and the rest are excluded for further analysis  
59 because of high missing rates.

60 There are many methods used for gap-filling the missing data, including interpolation from  
61 nearby gauges (Lopes et al., 2016), statistical methods (Gedney et al., 2006b), and  
62 hydrological modelling (Dai et al., 2009). Among them, the hydrological modelling method  
63 is widely used since it fully considers the spatial heterogeneity and temporal variability of  
64 climate forcing data, and can achieve sufficient simulations when it is calibrated against a



65 small number of observations (Rojas-Serna et al., 2016; Seibert and Beven, 2009). This is  
66 particularly important in Australia where hydrological modelling is a major tool for  
67 simulating continuous streamflow at a catchment scale. More recently, the Australian Bureau  
68 of Meteorology used a hydrological model –GR4J– to infill missing daily streamflow data for  
69 222 Hydrologic Reference Stations (<http://www.bom.gov.au/water/hrs/about.shtml>). The gap-  
70 filled streamflow data are then used for trend analysis and providing hydrological information  
71 to all users.

72 One major concern for the hydrology community is to understand how reliable the gap-filled  
73 data is. Unfortunately there are no studies in the literature to comprehensively evaluate the  
74 reliability and accuracy of the gap-filled data that are influenced by different thresholds and  
75 by data missing patterns. Our study aims to provide a framework to evaluate the annual  
76 trends and annual variables obtained from gap-filled streamflow data using two hydrological  
77 models (GR4J and SIMHYD) together with a large streamflow dataset available across the  
78 Australian Continent (Zhang et al., 2013). This can guide researchers to more sensibly define  
79 a threshold for catchment selection and hydrological analysis.

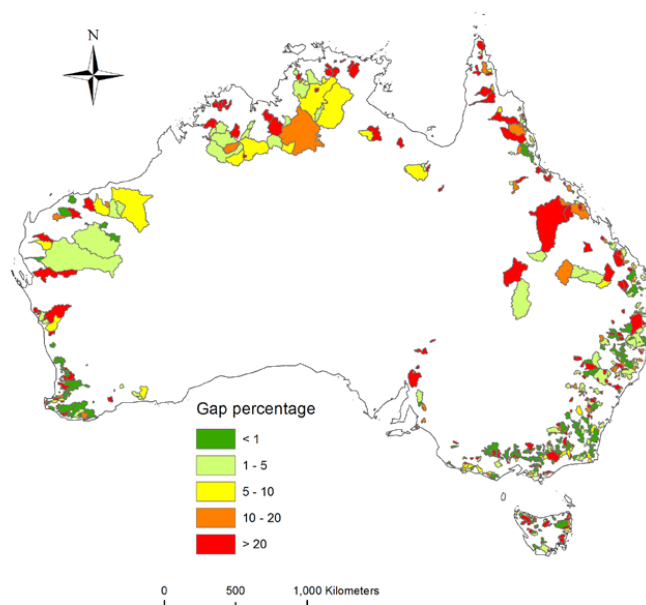
## 80 **2 Data and Methods**

### 81 **2.1 Data**

82 We obtained daily streamflow data set from 780 unregulated catchments widely spread across  
83 Australia (Zhang et al., 2013). The dataset has undergone strict quality assurance and quality  
84 control, including quality codes check and spike (i.e. outlier points) control, and covered the  
85 period from 1975 to 2012. This dataset has been used by modellers for various hydrological  
86 modelling and extreme-event studies (Li and Zhang, 2017; Liu and Zhang, 2017; Ukkola et  
87 al., 2016; Yang et al., 2017). The missing rate for the pre-1980 and post-2010 periods were  
88 high. To meet our study requirement, we selected 217 catchments with a data missing rate



89 less than 1% for the period 1981-2010 and the streamflow data for the 217 catchments are  
 90 regarded as ‘benchmark’ data (Figure 1). Out of the 780 catchments there are 146, 91, and 61  
 91 with the missing rate of 1-5%, 5-10%, and 10-20% during 1981-2010, respectively (Figure  
 92 1), and these catchments account for 38% of total available catchments. Table 1 summarises  
 93 major catchment attributes for the 217 selected catchments.



94

95 **Fig. 1.** The 780 unregulated catchments grouped by different streamflow data gaps for the  
 96 period of 1981-2010.

97

98 **Table 1.** Major catchment attributes for the 217 catchments

Attribute	Definition	Unit	Min	2.5 <sup>th</sup>	25 <sup>th</sup>	Median	75 <sup>th</sup>	97.5 <sup>th</sup>	Max
Area	Catchment area	km <sup>2</sup>	53	70	180	392	844	4562	72902
	Catchment		46	100	278	449	753	1194	1351
Elevation	average elevation above sea level	m							
Slope	Catchment mean slope	Degrees	0.3	0.6	2.0	3.9	7.7	12.0	13.6
P	Mean annual precipitation	mm/year	256	371	703	853	1107	1966	2473



ET <sub>p</sub>	Mean annual potential evapotranspiration	mm/year	906	968	1149	1235	1408	1791	1892
AI	Aridity index	-	0.38	0.55	1.11	1.44	1.89	4.75	6.47
Forest ratio	Ratio of forest to all land cover types	-	0.02	0.06	0.39	0.55	0.67	0.83	0.90

99

100 Out of the 217 catchments, about half of the catchments showed a significant decreasing

101 trend, 37% showing non-significant decreasing trend, and 13% showing non-significant

102 increasing trend (Figure 2), detected using Mann-Kendall trend analysis (see 2.3). This is

103 because Australia experienced the Millennium drought over the period 2001-2009, which

104 caused a dramatic streamflow reduction in this period (van Dijk et al., 2013). Trend analysis

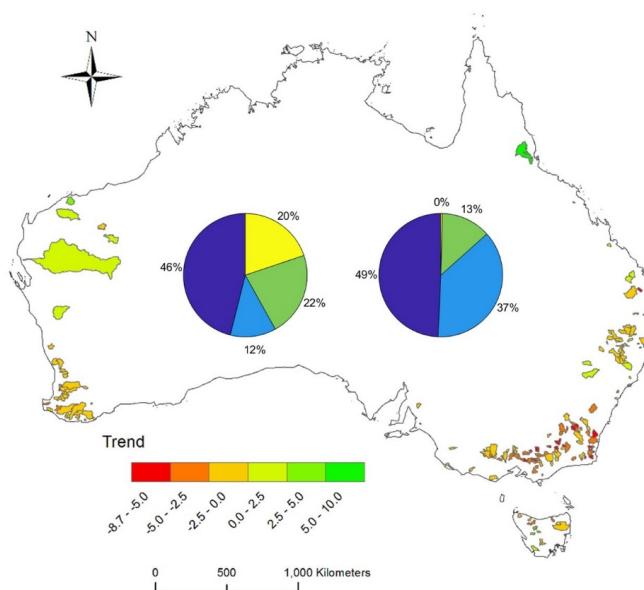
105 for the 217 catchments is explained in Section 2.3 and trend results are summarised in

106 Section 3.

107 Out of the 217 catchments, about 46% of catchments have no missing data in 1981-2010,

108 12% with the missing rate &lt;0.1%, 22% with the missing rate 0.1-0.5% and 20% with the

109 missing rate of 0.5-1% (Figure 2).



110

111 **Fig. 2.** Trends and streamflow data summary for the 217 catchments used in this study. Trend  
112 in annual streamflow is with a unit of mm/year/year. Left pie indicates the catchment  
113 percentage with different missing rates (dark blue with missing rate of 0%, navy blue with  
114 missing rate of 0-0.1%, green with missing rate of 0.1-0.5%, yellow with missing rate of 0.5-  
115 1.0%); right pie indicates the catchment percentage with different trends (dark blue with  
116 significant ( $p \leq 0.05$ ) decreasing trend, navy blue with non-significant ( $p > 0.05$ ) decreasing  
117 trend, green with non-significant ( $p > 0.05$ ) increasing trend, and yellow with significant ( $p \leq$   
118 0.05) increasing trend).

119 To drive the two hydrological models, we obtained daily meteorological time series  
120 (including minimum temperature, maximum temperature, incoming solar radiation, actual  
121 vapour pressure and precipitation) from 1975 to 2012 at  $0.05^\circ$  (~5 km) grid resolution from  
122 the SILO Data Drill of the Queensland Department of Natural Resources and Water  
123 ([www.nrw.gov.au/silo](http://www.nrw.gov.au/silo)). The data quality is reasonably good, indicated by the mean absolute



124 error for maximum daily air temperature, minimum daily air temperature, vapour pressure,  
125 and precipitation at 1.0°C, 1.4°C, 0.15 kPa and 0.40 mm/day (Jeffrey et al., 2001).

## 126 2.2 Gap-filling experiments

127 For thoroughly investigating the potential impacts of infilled streamflow data on annual trend  
128 accuracy, we conducted three groups of experiments to test how the missing rates at 5%, 10%  
129 and 20% impact on streamflow trends. We followed three steps for each missing rate of  
130 experiments:

131 *1. Missing patterns were obtained using actual streamflow data.* We selected consecutive  
132 missing day pattern from actual data from the 780 catchments. For 5% group of missing rate  
133 experiments, we selected 44 catchments with missing rates in 4-6%; for 10% group of  
134 missing rate experiments, we selected 39 catchment with missing rate in 8-12%; for 20%  
135 group of missing rate experiments, we selected 22 catchments with missing rate in 18-22%.  
136 Figure 3 shows the probability distribution of consecutive missing days from each group of  
137 catchments, which is skewed toward the low end. We therefore used the two-parameter  
138 Gamma distribution to simulate probability distribution of consecutive missing days (Figure  
139 3). The Gamma distribution is expressed as

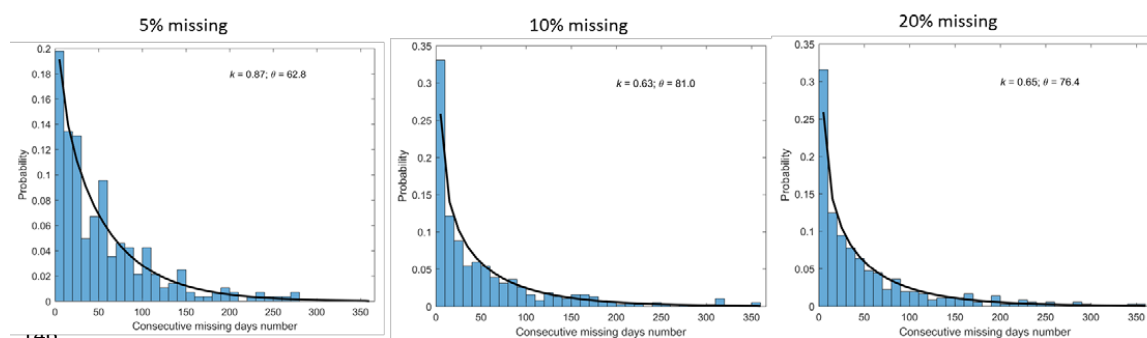
$$140 \quad X : \Gamma(k, \theta) = \text{Gamma}(k, \theta), \quad (1)$$

141 where  $X$  is the consecutive missing days number,  $k$  is shape parameter, and  $\theta$  is scale  
142 parameter. The corresponding probability density function in the shape-scale  
143 parameterization is

$$144 \quad f(x; k, \theta) = \frac{1}{\Gamma(k)\theta^k} x^{k-1} e^{-\frac{x}{\theta}}, \quad (2)$$

145 where  $\Gamma(k)$  is the gamma function.





147 **Fig. 3.** Missing patterns for three groups of catchments with missing rates 4-6%, 8-12%, 18-  
148 22% that represent 5%, 10% and 20% missing rates, respectively.

149 As seen from Figure 3, the two parameters are stable under the three groups of catchments.  
150 The  $k$  parameter varies from 0.63 to 0.87 and the  $\theta$  parameter changes from 62 to 81. It is  
151 noted that we removed all times when the number of consecutive missing days was  $> 365$ .  
152 We did that for a number of reasons. Firstly, gap-filling an entire year of missing data would  
153 likely impact annual trends. Secondly, the focus of this paper is on gap-filling short periods  
154 of missing data to be able to include more catchments in streamflow analyses. Thirdly,  
155 removing all periods of greater than 365 days allowed us to better fit a gamma distribution to  
156 the number of missing days.

157 *2. Generating random consecutive missing day numbers using random number generator*  
158 *(sampling without replacement) based on the Gamma distribution.* The random number  
159 generator was repeated 100 times to ensure the selected samples cover a wide range of  
160 streamflow time series.

161 *3. Gap-filling streamflow data.* The selected days were treated as ‘missing’ data and the  
162 unselected data were used for hydrological model calibration. The ‘missing’ data were then  
163 gap-filled using the simulated streamflow from the calibrated GR4J and SIMHYD models,  
164 respectively.



165 For consistent interpretation thereafter, the benchmark streamflow data is regarded as  
166 ‘observed’ and the experiment ones as ‘filled’ ones. For each of the three experiments, there  
167 are 100 x 217 (21,700) ‘missing’ time series, with 100 representing sample times using the  
168 random number generator and 217 representing the number of catchments.

### 169 **2.3 Trend analysis**

170 We used the Mann–Kendall Tau-b non-parametric test including Sen’s slope method (Burn  
171 and Elnur, 2002) for annual streamflow trend analysis and significance testing for all the  
172 three groups of experiments and benchmark data.

173 We used the following equation to quantify the trend bias:

$$174 \quad B_t = T_{filled} - T_{obs}, \quad (3)$$

175 where  $B_t$  is the bias in annual streamflow trend (mm/year/year),  $T_{filled}$  is annual trend for gap-  
176 filled streamflow (mm/year/year),  $T_{obs}$  is annual trend in observed streamflow  
177 (mm/year/year). It measures the trend error between the infilled and observed runoff trends  
178 with  $B_t \approx 0$ , which indicates that the trend in observed annual runoff is almost the same as  
179 that in the infilled annual runoff.

180 We also defined relative trend bias ( $P_{Bt}$ ) as

$$181 \quad P_{B_t} = \frac{T_{filled} - T_{obs}}{T_{obs}} \times 100, \quad (4)$$

182

### 183 **2.4 Hydrological models**

184 Two widely used hydrological models SIMHYD and GR4J (Chiew et al., 2002; Chiew et al.,  
185 2010; Li et al., 2014; Oudin et al., 2008; Perrin et al., 2003; Zhang and Chiew, 2009; Zhang  
186 et al., 2016a) were used to infill daily ‘missing’ streamflow. Both models require daily



187 precipitation and daily potential evaporation (Priestley and Taylor, 1972) as model inputs,  
188 and model outputs are daily streamflow at each gauge. The daily inputs of the maximum and  
189 minimum temperatures, incoming solar radiation, and vapour pressure data were used to  
190 calculate the Priestley–Taylor daily potential evaporation.

191 The two models were calibrated using a global optimiser: genetic algorithm (The  
192 MathWorks, 2006) at each catchment, with the first six years (i.e., 1975–1980) for spin up  
193 and remainder (1981 to 2010) for modelling experiments. Since this study mainly evaluates  
194 the trends obtained using the gap-filled streamflow from hydrological modelling, it is crucial  
195 to predict high flow and mean flow as accurate as possible. To this end, the model calibration  
196 was to minimize the following objective function ( $F$ ) (Viney et al., 2009; Zhang et al.,  
197 2016b):

$$198 \quad F = (1 - NSE) + 5 \left| \ln(1 + B) \right|^{2.5}, \quad (5)$$

$$199 \quad B = \frac{\sum_{i=1}^N Q_{sim,i} - \sum_{i=1}^N Q_{obs,i}}{\sum_{i=1}^N Q_{obs,i}}, \quad (6)$$

200  
201 where  $NSE$  is the Nash-Sutcliffe-Efficiency of daily streamflow,  $B$  is the model bias,  $Q_{sim}$  and  
202  $Q_{obs}$  are the simulated and observed daily runoff,  $i$  is the  $i$ th day,  $N$  is the total number of days  
203 sampled. The  $NSE$  gives higher streamflow more weight, and varies between  $-\infty$  to 1 with  
204  $NSE > 0.6$  indicating a good agreement (Zhang and Chiew, 2009). The  $B$  measures water  
205 balance error between the observed and modelled daily streamflow, with  $B = 0$  indicating that  
206 the average of modelled daily streamflow is the same as the average of observed daily  
207 streamflow.

208 For each catchment, GR4J and SIMHYD were calibrated using benchmark data and 100 time  
209 series of streamflow data with ‘missing’ data (see Section 2.2), respectively. For benchmark  
210 data without any missing data (46% catchments) there are no gap-filling required; for the



211 benchmark data with missing rate less than 1%, the calibrated continuous streamflow data  
212 were used to fill the gaps. For the ‘missing’ experiments, the calibrated continuous  
213 streamflow data for each ‘missing’ replicate were used to infill the artificially-made ‘missing’  
214 data. Table 2 summarises the model calibrations carried out for benchmark and each  
215 experiment. Finally, there were 1,302,434 model calibrations and 1,302,000 times of gap-  
216 filling carried out. Finally, the trends estimated from benchmark were used to evaluate those  
217 obtained from the ‘missing’ experiments.

218 **Table 2.** Summary of model calibration number carried out for benchmark and data ‘missing’  
219 experiments

Model	Benchmark	5% missing	10% missing	20% missing	Sum
GR4J	217	217,000	217,000	217,000	651,217
SIMHYD	217	217,000	217,000	217,000	651,217
Sum	434	434,000	434,000	434,000	1,302,434

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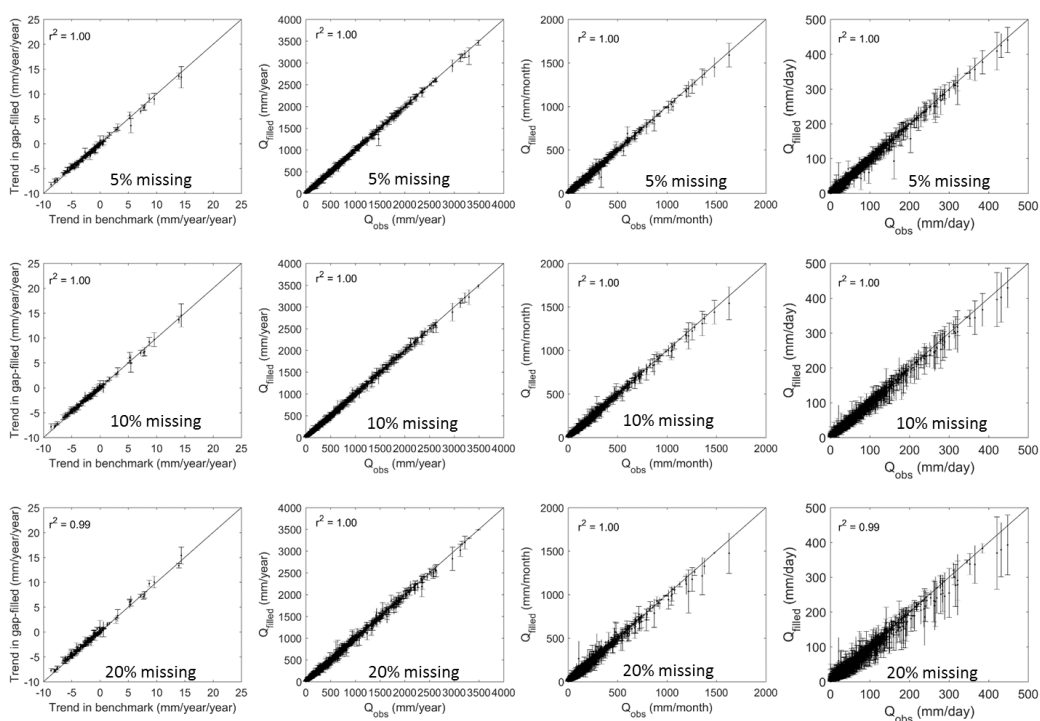
### 221 3 Results

222 The gap-filled data from the two hydrological models were evaluated against the benchmark  
223 data. Figures 4 and 5 summarise the performance of the gap-filled data for estimating annual  
224 trend, annual streamflow, monthly streamflow and daily streamflow, respectively. Overall,  
225 the two models perform similarly. The three missing rate experiments (5%, 10%, and 20%)  
226 perform almost the same as the benchmark (Figures 4 and 5). The coefficient of  
227 determination ( $r^2$ ) between the gap-filled trends and observed trends is more than 0.98 for the  
228 three experiments and two hydrological models.

229 Since errors in gap-filled trends likely to be different and different time steps when daily  
230 infilled streamflow data is used, we further investigate how gap-filled errors are propagated  
231 from daily to monthly and to annual scales under the three gap-filling cases (5%, 10%, and

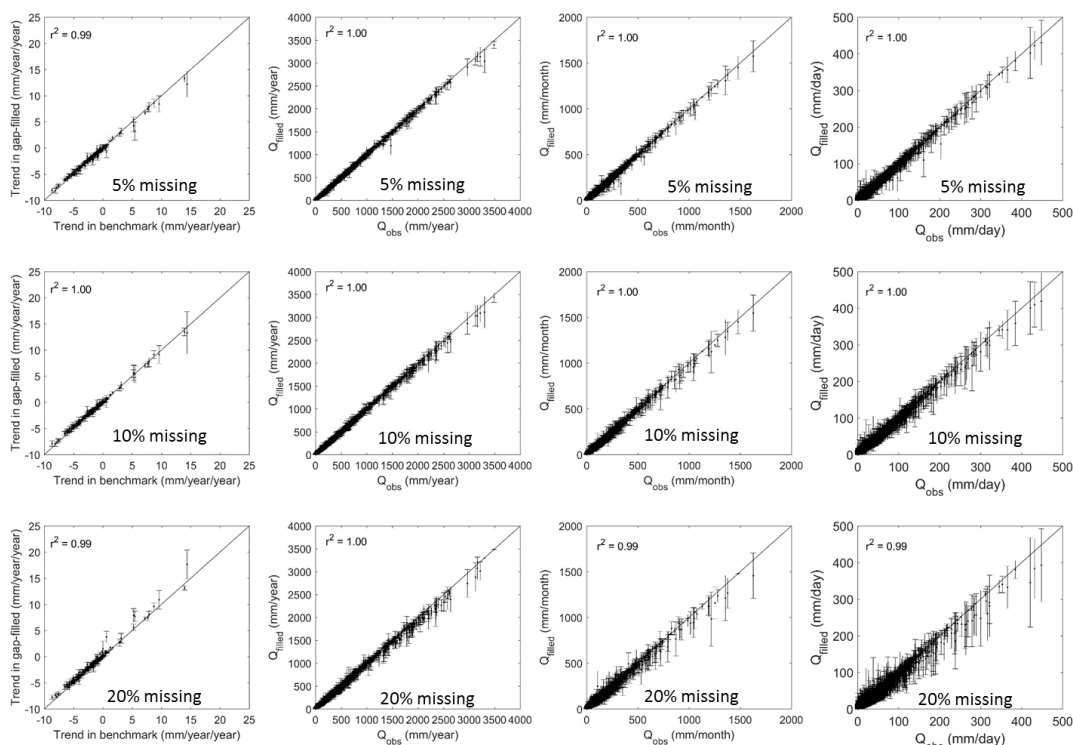


232 20%) (Figures 4 and 5). It is expected that daily gap-filled streamflow has a larger standard  
 233 deviation from the benchmark than monthly and annual streamflow since the streamflow was  
 234 gap-filled at daily scale. This indicates that the temporal aggregation smooths the gap-filled  
 235 error strongly, and it generates very reasonable monthly and annual streamflow estimates  
 236 with less standard deviation. It is interesting to note that both models tend to underestimate  
 237 very high flows though they are calibrated against the NSE of daily streamflow which puts a  
 238 larger weight on correctly representing higher flows.



2

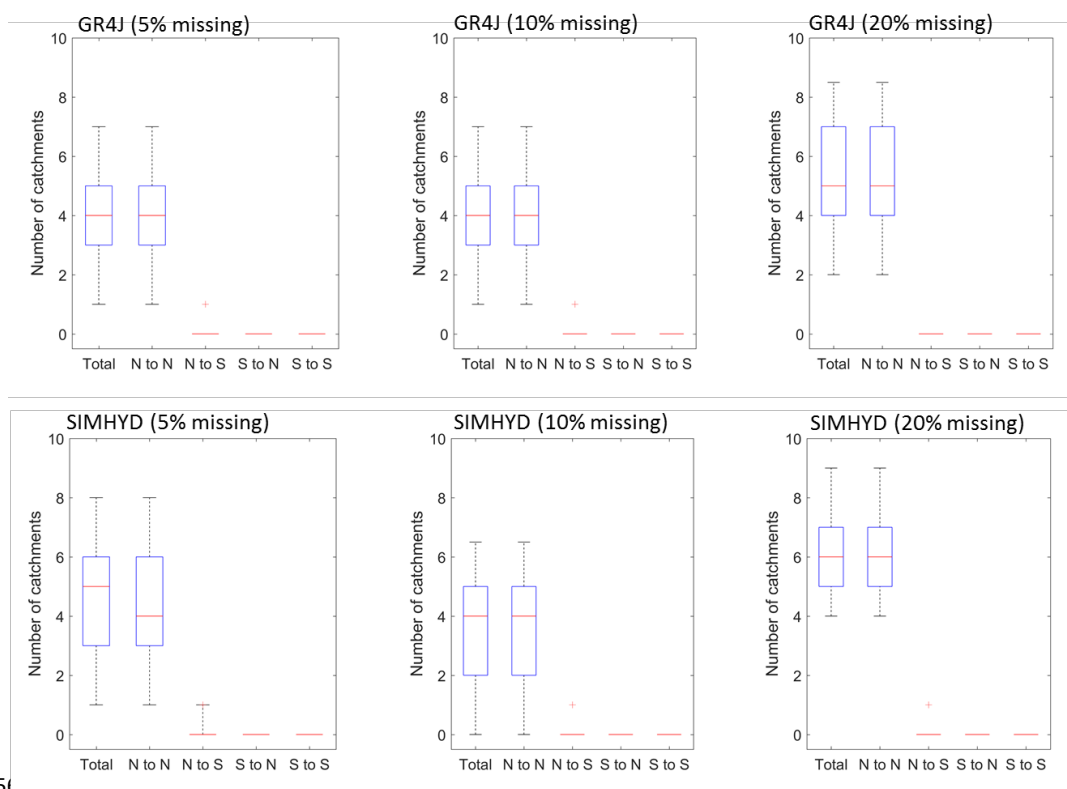
240 **Fig. 4.** Comparisons between the observed streamflow (x-axis) and gap-filled ones (y-axis) for  
 241 streamflow trend (mm/year/year, left panels), annual streamflow (mm/year, second left panels),  
 242 monthly streamflow (mm/month, second right panels) and daily streamflow (mm/day, right  
 243 panels). The gaps were filled using GR4J. Error bar represents standard deviation of the 100  
 244 replicates for each group of 'missing' experiments.



2

246 **Fig. 5.** Same as Fig. 4 but using SIMHYD.

247 Figure 6 further summarises the catchments with trend direction mismatch between the  
248 benchmark and gap-filled data (i.e. change from negative to positive or change from positive  
249 to negative). For the experiments with 5% and 10% missing rates and for GR4J, there are less  
250 than 8 out of the 217 catchments showing a trend mismatch and almost all of them show non-  
251 significant trends ( $p > 0.05$ ). For the experiments with a 20% missing rate for GR4J, there are  
252 less than 10 out of the 217 catchments showing trend mismatch and all of them show non-  
253 significant trends. SIMHYD results are almost the same as GR4J results. All these indicate that  
254 there is very marginal influence on annual streamflow trend directions when the missing rate  
255 is less than 20%.



250

257 **Fig. 6.** Trend mismatch analysis between the gap-filled and benchmark. Total means all

258 mismatch catchments; ‘N’ means not significant trends ( $p > 0.05$ ); ‘S’ means significant

259 trends ( $p \leq 0.05$ ). The bottom, middle and top of each box are the 25th, 50th and 75th

260 percentiles, and the bottom and top whiskers are the 5th and 95th percentiles.

261 Though the three groups of experiments show small trend direction changes (Figure 6), it is

262 not clear how the trend bias (Eq. 3) looks. To this end, Figure 7 further compares the trend

263 bias between the experiments. It is clear that the trend biases between 5% and 10% missing

264 experiments are similar. For GR4J, both have the trend bias varying from -1 to 1

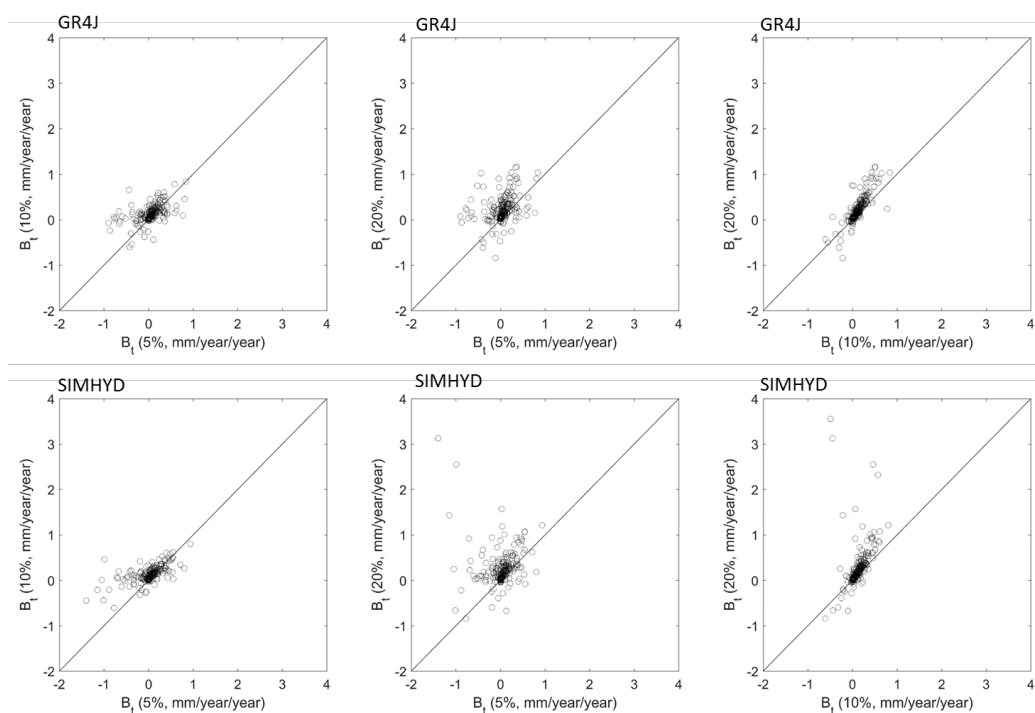
265 mm/year/year; For SIMHYD, the trend bias between the two is similar when it varies from -

266 0.5 to 1 mm/year/year, and the trend bias for 5% missing experiment is even larger than that

267 for 10% missing experiment. The trend bias for 20% missing experiment is noticeably larger



268 than that for 10% and 5% missing experiments for both models, and the underperformance is  
269 more noticeable from SIMHYD gap-filled than that from GR4J gap-filled. This result  
270 suggests that the trend bias is reasonable when the missing rate is less than 10%, and can be  
271 large for small number of catchments when the missing rate is to 20%.



272

273 **Fig. 7.** Trend biases comparison between the three groups of gap-filling experiments (5%,  
274 10% and 20%). Top three are for GR4J and bottom three are for SIMHYD.

#### 275 **4 Discussion and conclusions**

276 Researchers are keen to have a comprehensive understanding of rules for excluding  
277 catchments with gaps in the streamflow record. Our results indicate that when the streamflow  
278 data gaps are up to 10%, the gap-filled data obtained using hydrological modelling are very  
279 reasonable for annual trend analysis and annual streamflow estimates. Choosing the threshold  
280 of 10% missing rate will allow the use of many more catchments in modelling and data





281 analysis studies. For example, of the 780 unregulated Australian catchments available for  
282 modelling studies (Zhang et al., 2013), there are 237 catchments with the missing rate of 1-  
283 10% during 1981-2010, accounting for 38% of total available catchments (Figure 1). Of these  
284 237, 67 (~28%) also have gaps lasting more than one year (which we did not consider in this  
285 analysis), and therefore these may not be suitable for use. With an increased number of  
286 catchments, more reliable large-scale hydrological modelling studies can be carried out  
287 (Beck et al., 2016; Parajka et al., 2013; Zhang et al., 2016a).

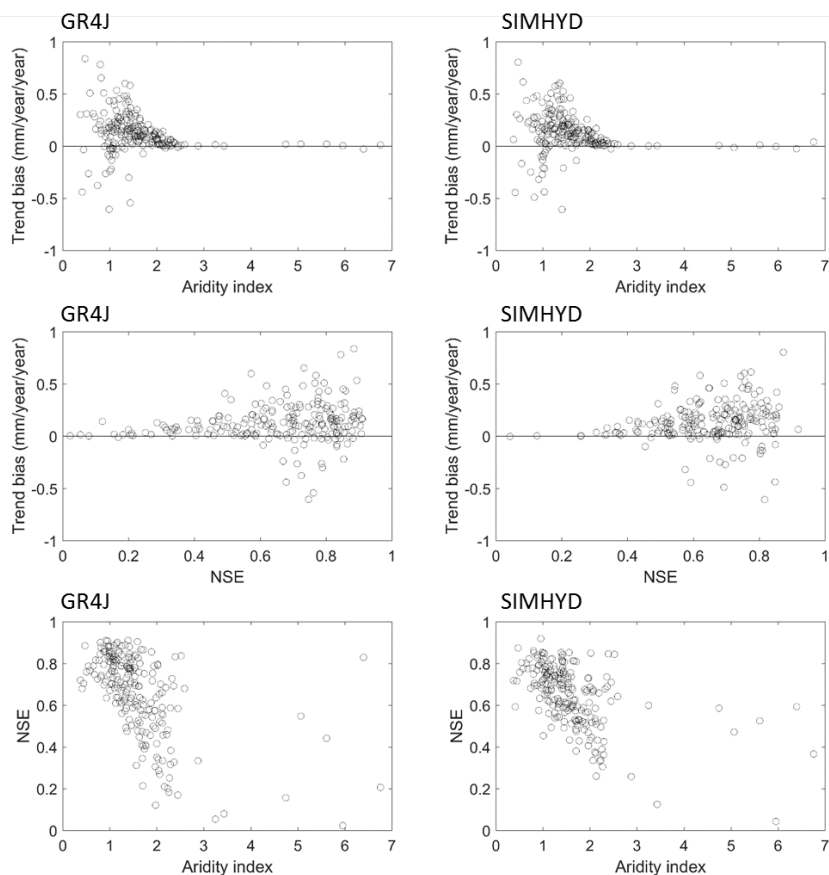
288 The ‘missing’ rate experiments designed in this study are based on the actual data missing  
289 patterns obtained from the 780 catchments. In most cases, the consecutive missing days are  
290 less than 10, as indicated by Figure 3, indicating brief periods of gauge malfunctions. It is  
291 however interesting to note that there are streamflow gaps lasting much longer than this in  
292 many catchments, with gaps of many months in some cases, noting that we excluded gaps  
293 lasting one year or more. It is highly likely that filling a gap of one year or more will result in  
294 biases larger than those presented here.

295 Furthermore, we also tested the quality of random gap-filled daily streamflow. In that case,  
296 the missing patterns were randomly selected using a random number generator. The results  
297 obtained from the random gap-filling (not shown) are similar to the results presented here.  
298 Thus, it is likely that the length of the gaps (as long as it is less than one year) is unlikely to  
299 impact the results of the gap-filling experiment. We would conclude from this that the use of  
300 hydrologic modelling for filling the substantially gapped data (up to 10% missing rate)  
301 described here for Australia will not impact annual trends of streamflow. Impacts on other  
302 streamflow characteristics also need to be examined, as well as seeing if the results obtained  
303 in Australia are comparable with those in other parts of the world, where the length of  
304 observational gaps may be quite different to those shown in Figure 3.



305 To understand if the quality of gap-filled streamflow is related to catchment attributes and  
306 calibration accuracy, we conducted further analysis among the trend bias, model calibration  
307 efficiency (i.e. *NSE*) and catchment aridity index (mean annual potential evaporation divided  
308 by mean annual precipitation) (Figure 8). The model calibration results at dry catchments are  
309 normally poorer than those at wet catchments. However, the trend bias (mm/year/year)  
310 obtained from dry catchments is usually smaller. The large biases are observed from the  
311 catchments with aridity index less than 2 and with the calibrated *NSE* being larger than 0.60.  
312 In part, this is to be expected since the streamflow is also lower in more arid catchments,  
313 meaning that the trend bias is also likely to be lower.

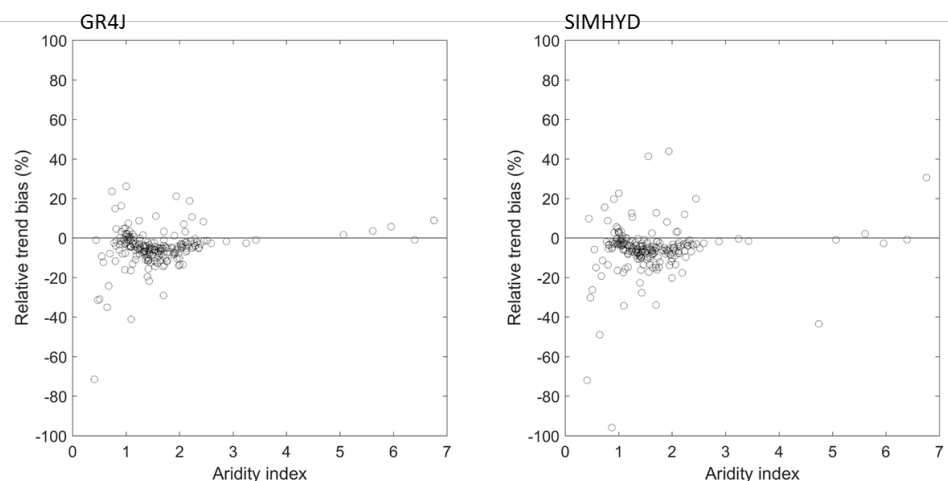
314 Figure 9 shows the relationship between relative trend bias (% , Eq. 4) and aridity index. It  
315 shows that not only is the actual trend bias lower in drier catchments, but so too is the relative  
316 (%) trend. This result suggests that the large bias in annual trends as a result of gap-filling is  
317 observed in relatively wet catchments where model calibrations are reasonably good. This  
318 result seems counter-intuitive and requires further exploration, which is beyond the scope of  
319 the current paper.



320

321 **Fig. 8.** Relationships among trend bias (mm/year/year), model calibration Nash-Sutcliffe

322 Efficiency and aridity index for each catchment and for the experiment of 10% missing rate.



323

324 **Fig. 9.** Relationships between relative trend bias (mm/year/year) and aridity index for each  
325 catchment and for the experiment of 10% missing rate.

326 This study focuses on evaluating annual streamflow and its trends. Therefore, we used the  
327 Nash-Sutcliffe Efficiency plus model bias (Eqs. 5 and 6) to calibrate the two hydrological  
328 models. If other hydrological response variables such as low flow metrics are required, other  
329 model calibration schemes should be used since the NSE model calibration scheme gives  
330 more weight to reproducing high flows at the expense of low-flows (Zhang et al., 2014). Low  
331 flow metrics have important ecological implications (Mackay et al., 2014; Smakhtin, 2001).  
332 In general however, it is challenging to use hydrological modelling for low flow simulations  
333 and predictions (Pushpalatha et al., 2012; Staudinger et al., 2011). To have credible low flow  
334 gap-filling, model calibrations should use an objective function that puts more weights on  
335 low flows, such as NSE of daily inverse streamflow and the direct low flow metrics. Another  
336 possible method is to combine hydrological modelling with other methods for gap-filling,  
337 such as using nearby gauges (Lopes et al., 2016) and statistical methods (Gedney et al.,  
338 2006b).



339 It is noted that the infilled data purely refers to the ‘missing’ data. All streamflow gauges are  
340 only rated to a certain flow. Once the flow exceeds that level during flooding, the results are  
341 interpolated using stage-discharge relationships (Peña-Arancibia et al., 2015). These  
342 interpolations could be a major source of observation error. However, investigating high flow  
343 interpolation and data quality is beyond the scope of this study.

344 In summary, our results clearly demonstrate that the gap-filled data is most accurate when  
345 examining trends at the annual scale, followed by monthly scale, and with least satisfaction at  
346 the daily scale. This gives researchers confidence for annual trend analysis, a hot topic in  
347 hydrological and climate sciences. Our results also clearly indicate that the gap-filling of  
348 Australian streamflow data using hydrological model is very reasonable when the missing  
349 rate is less than 10%, with only a small number of catchments showing a large trend bias  
350 when the missing rate is to 20%. The results also indicate that gap-filling drier catchments  
351 appears to be more successful than gap-filling wetter catchments.

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