1 A large sample analysis of European rivers on seasonal river flow correlation

2 and its physical drivers

- 3 Theano Iliopoulou^{1*}, Cristina Aguilar², Berit Arheimer³, María Bermúdez⁴, Nejc Bezak⁵, Andrea
- 4 Ficchì⁶, Demetris Koutsoyiannis¹, Juraj Parajka⁷, María José Polo², Guillaume Thirel⁸ and
- 5 Alberto Montanari⁹
- 6 (1) Department of Water Resources and Environmental Engineering, School of Civil Engineering,
- 7 National Technical University of Athens, Zographou, 15780, Greece
- 8 (2) Fluvial dynamics and hydrology research group, Andalusian Institute of Earth System
- 9 Research, University of Cordoba, Cordoba, 14071, Spain
- 10 (3) Swedish Meteorological and Hydrological Institute, 601 76 Norrköping, Sweden
- 11 (4) Water and Environmental Engineering Group, Department of Civil Engineering, Universidade
- da Coruña, 15071 A Coruña, , Spain
- 13 (5) Faculty of Civil and Geodetic Engineering, University of Ljubljana, Jamova 2, SI-1000
- 14 Ljubljana, Slovenia
- 15 (6) Department of Geography and Environmental Science, University of Reading, Reading, RG6
- 16 6AB, United Kingdom; formerly, IRSTEA, Hydrology Research Group (HYCAR), F-92761,
- 17 Antony, France
- 18 (7) Vienna University of Technology, Institute of Hydraulic Engineering and Water Resources
- 19 Management, Karlsplatz 13/222, A-1040 Vienna, Austria
- 20 (8) IRSTEA, Hydrology Research Group (HYCAR), F-92761, Antony, France
- 21 (9) Department DICAM, University of Bologna, Bologna, 40136, Italy
- * * Correspondence to: Theano Iliopoulou (anyily@central.ntua.gr)

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Abstract

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- 28 The geophysical and hydrological processes governing river flow formation exhibit persistence 29 at several timescales, which may manifest itself with the presence of positive seasonal 30 correlation of streamflow at several different time lags. We investigate here how persistence 31 propagates along subsequent seasons and affects low and high flows. We define the High Flow 32 Season (HFS) and the Low Flow Season (LFS) as the three-month and the one-month periods which usually exhibit the higher and lower river flows, respectively. A dataset of 224 rivers from 33 34 six European countries spanning more than 50 years of daily flow data is exploited. We compute 35 the lagged seasonal correlation between selected river flow signatures, in HFS and LFS, and the 36 average river flow in the antecedent months. Signatures are peak and average river flow for HFS 37 and LFS, respectively. We investigate the links between seasonal streamflow correlation and 38 various physiographic catchment characteristics and hydro-climatic properties. We find 39 persistence to be more intense for LFS signatures than HFS. To exploit the seasonal correlation in the frequency estimation of high and low flows, we fit a bivariate Meta-Gaussian probability 40 41 distribution to the selected flow signatures and average flow in the antecedent months in order to 42 condition the distribution of high and low flows in the HFS and LFS, respectively, upon river 43 flow observations in the previous months. The benefit of the suggested methodology is 44 demonstrated by updating the frequency distribution of high and low flows one season in 45 advance in a real-world case. Our findings suggest that there is a traceable physical basis for 46 river memory which in turn can be statistically assimilated into high- and low-flow frequency 47 estimation to reduce uncertainty and improve predictions for technical purposes.
- 49 **Keywords**: seasonal streamflow correlation, river memory, persistence, real-time flow
- 50 forecasting, floods, low flows, meta-Gaussian

1. Introduction

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Recent analyses for the Po River and the Danube River highlighted that catchments may exhibit significant correlation between peak river flows and average flows in the previous months (Aguilar et al., 2017). Such correlation is the result of the behaviours of the physical processes involved in the rainfall-runoff transformation that may induce memory in river flows at several different time scales. The presence of long-term persistence in streamflow has been known for a long time since the pioneering works of Hurst (1951) and has been actively studied ever since (e.g. Koutsoviannis, 2011; Montanari, 2012; O'Connell et al., 2016 and references therein). While a number of seasonal flow forecasting methods have been explored in the literature (e.g. Bierkens and van Beek, 2009; Dijk et al., 2013), attempts to explicitly exploit streamflow persistence in seasonal forecasting through information from past flows have been in general limited. Koutsoyiannis et al. (2008) proposed a stochastic approach to incorporate persistence of past flows into a prediction methodology for monthly average streamflow and found the method to outperform the historical analogue method (see also Dimitriadis et al., 2016 for theory and applications of the latter) and artificial neural network methods in the case of the Nile River. Similarly, Syensson (2016) assumed that the standardized anomaly of the most recent month will not change during future months to derive monthly flow forecasts for 1-3 months lead time and found the predictive skill to be superior to the analogue approach for 93 UK catchments. The abovementioned persistence approach has also been used operationally in the production of seasonal streamflow forecasts in the UK since 2013, within the framework of the Hydrological Outlook UK (Prudhomme et al. 2017). A few other studies have included past flow information in prediction schemes along with teleconnections or other climatic indices (Piechota et al., 2001; Chiew et al., 2003; Wang et al., 2009). Recently, it was shown that streamflow persistence, revealed as seasonal correlation, may also be relevant for prediction of extreme events by allowing one to update the flood frequency distribution based on river flow observations in the pre-flood season and reduce its bias and variability (Aguilar et al., 2017). The above previous studies postulated that seasonal streamflow correlation may be due to the persistence of the catchments storage and/or the weather, but no attempt was made to identify the physical drivers.

The present study aims to further inspect seasonal persistence in river flows and its determinants, by referring to a large sample of catchments in 6 European countries (Austria, Sweden, Slovenia, France, Spain and Italy). We focus on persistence properties of both high and low flows by investigating the following research questions: (i) what are the physical conditions, in terms of catchment properties, i.e. geology and climate, which may induce seasonal persistence in river flow? And, (ii) can floods and droughts be predicted, in probabilistic terms, by exploiting the information provided by average flows in the previous months? These questions are relevant for gaining a better comprehension of catchment dynamics and planning mitigation strategies for natural hazards. To reach the above goals, we identify a set of descriptors for catchment behaviours and climate, and inspect their impact on correlation magnitude and predictability of river flows.

A few studies have analysed physical drivers of streamflow persistence on annual and deseasonalized monthly and daily timeseries (Mudelsee, 2007; Hirpa et al., 2010; Gudmundsson et al., 2011; Zhang et al., 2012; Szolgayova et al., 2014; Markonis et al., 2018) but the topic has been less studied on intra-annual scales relevant to seasonal forecasting of floods and droughts.

To demonstrate the high practical relevance of the identified seasonal correlations we present a technical experiment for one of the studied rivers (Section 7) in which the frequency distribution of both high and low flows is updated one season in advance by exploiting real-time information on the state of the catchment.

2. Methodology

The investigation of the persistence properties of river flows focuses separately on both high and low discharges and is articulated in the following steps: (a) identification of the high- and low-flow seasons; (b) correlation assessment between the peak flow in the high flow season (average flow in the low-flow season) and average flows in the previous months; (c) analysis of the physical drivers for streamflow

persistence and its predictability through a Principal Component Analysis; (d) real-time updating of the frequency distribution of high and low flows for a selected case study with significant seasonal correlation by employing a Meta-Gaussian approach. The above steps are described in detail in the following sections.

2.1 Season Identification

Season identification is performed algorithmically to identify the High Flow Season (HFS) and Low Flow Season (LFS) for each river time series. For the estimation of HFS, we employ an automated method recently proposed by Lee et al. (2015), which identifies the high flow season as the three-month period centred around the month with the maximum number of occurrences of Peaks Over Threshold (POT), with the threshold set to the highest 5% of the daily flows. To evaluate the selection of HFS, a metric constructed as the Percentage of Annual Maximum Flows (PAMF) captured in the HFS is used. The PAMFs are classified in subjective categories of "poor" (<40%), "low" (40–60%), "medium" (60–80%) and "high" (>80%) values, denoting the probability that the identified HFS is the dominant high-flow season in the record. If the identified peak month alone contains 80% or more of annual maxima flows, a uni-modal regime is assumed and the identification procedure is terminated. In all other cases, the method allows for the search of a second peak month and the identification of a minor HFS but we do not further elaborate on this analysis here because we are only interested in the most extreme seasons for the purpose of predicting high and low flows.

The method proposed by Lee et al. (2015) has several advantages that make it suitable for the purpose of this research. Most importantly, it is capable of handling conditions of bi-modality, which is usually a major issue for traditional methods like, e.g., directional statistics (Cunderlik et al., 2004). A potential limitation is the assumption of symmetrical extension of HFS around the peak month, along with the uniform selection of its length (3-month period). The degree of subjectivity in the evaluation of the second HFS is another limitation, which is not relevant here as we focus on the main HFS.

LFS is herein identified as the one-month period with the lowest amount of mean monthly flow. An alternative approach of estimating the relative frequencies of annual minima of monthly flow and selecting the month with the highest frequency as LFS is also considered.

2.2 Correlation analysis and physical interpretation through Principal Component Analysis

127 2.2.1 Correlation analysis

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- In the case of HFS, a correlation is sought between the maximum daily flow occurring in the HFS period
- and the mean flow in the previous months, before the onset of HFS. For LFS, correlation is computed
- between the mean flow in the LFS itself and the mean flow in the previous months. We use the mean flow
- in the previous month as a robust proxy of 'storage' in the catchment that is expected to reflect the state of
- the catchment, i.e., wetter/drier than usual. Since we are interested in seasonal persistence, we compute the
- Pearson's correlation coefficient up to 9-month lag for HFS and 11-month lag for LFS.
- 134 2.2.2 Analysis of physical drivers
- a. Catchment, geological and climatic descriptors
- An extensive investigation is carried out to identify physical drivers of seasonal streamflow correlation, in
- terms of catchment, geological and climatic descriptors.
- As catchment descriptors, we consider the basin area (A), the Baseflow Index (BI), the mean specific
- 139 runoff (SR), the percentage of basin area covered by lakes (percentage of lakes, PL) and glaciers
- 140 (percentage of glaciers, PG) and altitude as candidate explanatory variables for streamflow correlation.
- The area A (km²) is primarily investigated as it is representative of the scale of the catchment, under
- the assumption that in larger basins the impact of the climatological and geophysical processes affecting
- river flow becomes more significant and may lead to a magnified seasonal correlation.
- BI is considered based on the assumption that high groundwater storage may be a potential driver of
- 145 correlation. BI is calculated from the daily flow series of the rivers following the hydrograph separation
- procedure detailed in Gustard et al. (2009). Flow minima are sampled from non-overlapping 5-day blocks
- of the daily flow series and turning points in the sequence of minima are sought and identified when the

90% value of a certain minimum is smaller or equal to its adjacent values. Subsequently, linear interpolation is used in between the turning points to obtain the baseflow hydrograph. The BI is obtained as the ratio of the volume of water beneath the baseflow separation curve versus the total volume of water from the observed hydrograph, and an average value is computed over all the observed hydrographs for a given catchment. A low index is indicative of an impermeable catchment with rapid response, whereas a high value suggests high storage capacity and a stable flow regime.

SR (m³ s⁻¹ km⁻²) is computed as the mean daily flow of the river standardized by the size of its basin area. It may be an important physical driver as it is an indicator of the catchment's wetness. PL (%) and PG (%) are investigated for the Swedish and Austrian catchments, respectively, as lakes and glaciers are expected to increase catchment storage thus affecting persistence. Lake coverage data are based on cartography and available from the Swedish Water Archive (https://www.smhi.se/), while glacier coverage data are estimated from the CORINE land cover database (https://www.eea.europa.eu/publications/COR0-landcover).

The effect of catchment altitude is also inspected using relief maps from the Shuttle Radar Topography Mission (SRTM) data (http://srtm.csi.cgiar.org/). The data are available for the whole globe and are sampled at 3 arch-seconds resolution (approximately 90 meters). Topographic information is available for all catchments located at latitude lower than 60 degrees north while a 1 km resolution digital elevation model is available for Austria.

As geological descriptors we consider the percentage of catchment area with the presence of flysch (percentage of flysch, PF) and karstic formations (percentage of karst, PK) for Austrian and Slovenian catchments, respectively, for which this type of information is available. A subset of Austrian catchments is characterised by the dominant presence of flysch, a sequence of sedimentary rocks characterized by low permeability, which is known to generate a very fast flow response. Karstic catchments, characterized by the irregular presence of sinkholes and caves, are also known for having rapid response times and complex behaviour; e.g. initiating fast preferential groundwater flow and intermittent discharge via karstic springs

(Ravbar, 2013; Cervi et al., 2017). Geological features are presumed to be linked to persistence properties also because geology is the main control for the baseflow index across the European continent (Kuentz et al. 2017). PK (%) and PF (%) are estimated from geological maps of Slovenia and Austria, respectively.

As climatic descriptors, the mean annual precipitation P (mm year⁻¹) and the mean annual temperature T (°C) are selected. Corresponding gridded data are retrieved from the Worldclim database (http://www.worldclim.org/) at a spatial resolution of 10 minutes of degree (approximately 18.55 km). We note that low mean temperature regimes are also associated with snow, the presence of which is also considered in the interpretation of the results. We also adopt as climatic descriptor the De Martonne index (De Martonne, 1926), IDM, which is given by IDM = P/(T+10), and enables classification of a region into one of the following 6 climate classes, i.e., arid (IDM \leq 5), semi-arid ($5 < \text{IDM} \leq 10$), dry sub-humid ($10 < \text{IDM} \leq 20$), wet sub-humid ($20 < \text{IDM} \leq 30$), humid ($30 < \text{IDM} \leq 60$) and very humid ($10 < \text{IDM} \leq 60$). Additionally, the Köppen-Geiger climatic classification (Kottek et al., 2006) of the rivers is assessed.

b. Principal Component Analysis

To identify what catchment, physiographic and climatic characteristics may explain river memory we attempt to regress the seasonal streamflow correlation against the physical descriptors introduced above. We expect the presence of multi-collinearity among the explaining variables and therefore Principal Component Analysis (PCA; Pearson, 1901; Hotelling, 1933) was applied to construct uncorrelated explanatory variables. In essence, PCA is an orthonormal linear transformation of p data variables into a new coordinate system of $q \le p$ uncorrelated variables (principal components, PCs) ordered by decreasing degree of variance retained when the original p variables are projected into them (Jolliffe, 2002). Therefore, the first principal axis contains the greatest degree of variance in the data, while the second principal axis is the direction which maximizes the variance among all directions orthogonal to the first principal axis and so on. Specifically, let x be a random vector with mean μ and correlation matrix Σ , then the principal component transformation of x is obtained as follows:

 $197 \mathbf{y} = \mathbf{C}^T \mathbf{x}' (1)$

where y is the transformed vector whose kth column is the kth principal component (k = 1, 2..p), C is the $p \times p$ matrix of the coefficients or loadings for each principal component and x' is the standardized x vector. Standardization is applied in order to avoid the impact of the different variable units on selecting the direction of maximum variance, when forming the PCs. The y values are the scores of each observation, i.e. the transformed values of each observation of the original p variables in the kth principal component direction.

PCA has useful descriptive properties of the underlying structure of the data. These properties can be efficiently visualized in the biplot (Gabriel, 1971), which is the combined plot of the scores of the data for the first two principal components along with the relative position of the *p* variables as vectors in the two-dimensional space. Herein, the distance biplot type (Gower and Hand, 1995), which approximates the Euclidean distances between the observations, is used. Variable vectors coordinates are obtained by the coefficients of each variable for the first two principal components. After construction of the PCs, a linear regression model is explored for the case of HFS and LFS lag-1 correlation.

2.3 Technical experiment: Real-time updating of the frequency distribution of high and low flows

In order to evaluate the usefulness of the information provided by the one-month-lag seasonal correlation for flow signatures in HFS and LFS, we perform a real-time updating of the frequency distribution of high and low flows based on the average river flow in the previous month. A similar analysis for the high flows was carried out by Aguilar et al. (2017) for the Po and Danube Rivers. In principle, this is a data assimilation approach, since real-time information, i.e. observations of the average river flow, is used in order to update a probabilistic model and inform the forecast of the flow signature of the upcoming season.

In detail, a bi-variate meta-Gaussian probability distribution (Kelly and Krzysztofowicz, 1997; Montanari and Brath, 2004) is fitted between the observed flow signatures, i.e., peak flow in the HFS, Q_P and average flow in the LFS, Q_L , and the average flow in the pre-HFS and LFS months, Q_m , respectively. The peak HFS flow and the average LFS flow are the dependent variables and are extracted as the peak

river discharge observed in the previously identified HFS and the average river discharge observed in the previously identified LFS, respectively. The average flow in the month preceding the HFS and the LFS is the explanatory variable in both cases. In the following, random variables are denoted by underscore and their outcomes are written in plain form.

The normal quantile transform, NQT (Kelly and Krzysztofowicz, 1997), is used in order to make the marginal probability distribution of dependent and explanatory variables Gaussian. This is achieved as follows: a) the sample quantiles Q are sorted in increasing order e.g. Q_{m_1} , Q_{m_2} ... Q_{m_n} , b) the cumulative frequency, e.g. FQ_{m_i} is computed via a Weibull plotting position, and c) the standard normal quantile, e.g., NQ_{m_i} is obtained as the inverse of the standard normal distribution for each cumulative frequency, e.g., $G^{-1}(FQ_{m_i})$. Therefore, all sample quantiles are discretely mapped into the Gaussian domain. To get the inverse transformation for any normal quantile, we connect the points in the above mapping with linear segments. The extreme segments are extended to allow extrapolation outside the range covered by the observed sample.

In the Gaussian domain, a bivariate Gaussian distribution is fitted between the random explanatory variable $\underline{NQ_m}$ and the dependent variables $\underline{NQ_P}$ and $\underline{NQ_L}$ by assuming stationarity and ergodicity of the variables. We define the generic random variable $\underline{NQ_{fs}}$ to represent any dependent flow signature, i.e.; $\underline{NQ_P}$ and $\underline{NQ_L}$ in our case. Then, the predicted signature at time t can be written as:

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$$NQ_{fs}(t) = \rho(\underline{NQ_{m,}} \underline{NQ_{fs}}) NQ_{m}(t-h) + N\varepsilon(t)$$
 (2)

where $\rho(\underline{NQ_m}, \underline{NQ_{fs}})$ is the Pearson's cross correlation coefficient between $\underline{NQ_m}$ and $\underline{NQ_{fs}}$, h is the selected correlation lag with h=1 in the present application, and $N\epsilon(t)$ is an outcome of the stochastic process $\underline{N\epsilon}$, which is independent, homoscedastic, stochastically independent of $\underline{NQ_m}$ and normally distributed with zero mean and variance $1-\rho^2(\underline{NQ_m}, \underline{NQ_{fs}})$. Then, the joint bivariate Gaussian probability distribution function is defined by the mean $(\mu(\underline{NQ_m}) = 0$ and $\mu(\underline{NQ_{fs}}) = 0$), the standard deviation $(\sigma(\underline{NQ_m}) = 1$ and $\sigma(\underline{NQ_{fs}}) = 1$) of the standardized normalized series, and the Pearson's cross correlation coefficient between the normalized series, $\rho(\underline{NQ_m}, \underline{NQ_{fs}})$. From the Gaussian bivariate probability properties, it follows that for

any observed $NQ_m(t-h)$ the probability distribution function of $\underline{NQ_{fs}}(t)$ conditioned on NQ_m is Gaussian,

with parameters given by:

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$$\mu(\underline{NQ}_{fs}(t)) = \rho(\underline{NQ}_{m}, \underline{NQ}_{fs}) NQ_{m}(t-h)$$
(3)

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$$\sigma(\underline{NQ_{fs}}(t)) = (1 - \rho^2(\underline{NQ_{m,}}, \underline{NQ_{fs}}))^{0.5}$$
 (4)

To derive the probability distribution of $Q_{fs}(t)$ conditioned to the observed $Q_{m}(t-h)$, we first apply the inverse NQT, i.e., we use linear segments to connect the points of the previous discrete quantile mapping of the original quantiles into the Gaussian domain, and accordingly, obtain $Q_{fs}(t)$ for any $NQ_{fs}(t)$. Subsequently, we estimate the parameters of an assigned probability distribution for the obtained quantiles in the untransformed domain. This is referred to as the updated probability distribution of the considered flow signature (NQ_P and NQ_L in our case). We use the Extreme Value Type I distribution for the peak flows and calculate the differences in the magnitude of estimated maxima for a given return period between the unconditioned and the updated distribution. The latter is conditioned by the 95% sample quantile of the observed mean flow in the previous month. To model the low flows we use the lognormal distribution, which was found to exhibit the best fit for the river in question among other typical candidates for average flows, i.e. the Weibull and the Gamma distribution. The low flows are conditioned by the lower 5% sample quantile of the observed mean flow in the previous month.

3. Data and catchments description

The dataset includes 224 records spanning more than 50 years of daily river flow observations from gauging stations, mostly from non-regulated streams. A few catchments are impacted by regulation. Among the 224 rivers, 108 are located in Austria, 69 in Sweden, 31 in Slovenia, 13 in France, 2 in Spain and one in Italy. Catchment areas vary significantly, the largest being the Po River basin in Italy (70 091 km²) and the smaller being the Hålabäck River basin in Sweden (4.7 km²). The geographical location of the river gauge stations as well as their climatic classification are shown in Fig. 1. Most of the examined rivers belong to either a warm temperate (C) or a boreal/snow climate (D) with a subset impacted by polar climatic conditions (E), according to the updated World Map of the Köppen-Geiger climate classification

(Fig. 1) based on gridded temperature and precipitation data for the period 1951-2000 (Kottek et al., 2006). More specifically, the majority of French, Slovenian and approximately one third of the Swedish basins belong to the warm temperate Cfb category characterized by precipitation distributed throughout the year (fully humid) and warm summers. The rest of the Swedish catchments are impacted by a Dfc climatic type, i.e. a snow climate, fully humid with cool summers. The Austrian catchments belonging to the region impacted by the European Alps have the most complicated regime due to their topographic variability. At the lowest altitudes, Cfb is the prevailing regime, but as proximity to the Alps increases, a Dfc regime dominates and progressively, in the highest altitude basins, the climate becomes a polar tundra type (Et), characterized primarily by the very low temperatures present. The characteristics of all the climatic regimes of the studied rivers are given in the legend of Fig. 1. A summary of the river basins under study in terms of the selected descriptors is also provided in Table 1, showing that the investigated rivers cover a wide range of catchment area sizes, flow regimes and climatic conditions.

It is relevant to note that 16 of the Austrian rivers are subject to regulation, which may alter the persistence properties of river flows. This relates to generally 'mild' forms of regulation, i.e. upstream regulation with very low degree of flow attenuation, hydropower operations and flow diversions to and from the basin. A preliminary examination of these rivers did not reveal any significant change during time of the flow regime. The presence of regulation does not preclude the exploitation of correlation for predicting river flows in probabilistic terms, but may affect the analysis of physical drivers, as it may enhance or reduce persistence in the natural river flow regime. Given that detailed information is generally lacking on the impact of regulation (Kuentz et al. 2017), we assume stationarity of the river flows for all the catchments herein considered and additionally, assume that river management does not significantly affect the identification of the physical drivers.

4. River memory analysis for the considered case studies

4.1 Season Identification

Approximately half of the 224 rivers are characterized by at least one high-flow season with medium or higher significance (PAMF(HFS) \geq 60%). Among them, very strong unimodal regimes (PAMF(HFS) \geq 80%) are observed in 63 rivers, the majority of which are located in Sweden. For 25% of the rivers, a high-flow season of low significance is found (PAMF(HFS) between 40–60%), while for the remaining 25% the high-flow distribution looks uniform along the year. Bi-modality regimes are found with low and moderate significance in rivers located mostly in Austria and Sweden, but we focus here on the major high-flow season, as we are interested in the most extreme events. A minor HFS analysis would be perhaps relevant in other regions of the world where bimodal flood regimes are more prominent, as suggested by the analysis of Lee et al. (2015).

Regarding the LFS identification, the two considered approaches (see Section 2.1) agree for 139 out of 224 stations but the first method, i.e. the one-month period with the lowest amount of mean monthly flow is selected as being more relevant to the purpose of computing mean flow correlations.

4.2 Seasonal correlation

LFS correlation is markedly higher than the corresponding HFS correlation for lags 1–5 and its median remains higher than 0 for more lags (see Fig. 2). For the case of HFS correlation, we focus only on the most significant first lag, for which 73 rivers are found to have correlation significantly higher than 0 at 5% significance level. In Fig. 3, the autocorrelation of the whole monthly series is compared to the LFS correlation for lag of 1 and 2 months, in order to prove that the seasonal correlation for LFS is significantly higher than its counterpart computed by considering the whole year. The latter is also confirmed by the Kolmogorov-Smirnov test for both LFS lags (corresponding p-values, $p_{lag1} < 2.2 \times 10^{-6}$ and $p_{lag2} < 2.2 \times 10^{-6}$ for the null hypothesis that the LFS correlation coefficients are not higher than the corresponding values for the monthly series autocorrelation; Conover, 1971).

Figure 4 shows the spatial pattern of HFS and LFS streamflow correlations. It is interesting to notice the emergence of spatial clustering in the correlation magnitude, which implies its dependence on different spatially varying physical mechanisms. For example, for HFS, a geographical pattern emerges within France, since the highest correlation coefficients are located in the northern part of the country, which is characterized by oceanic climate and higher baseflow indexes.

5. Physical interpretation of correlation

- To attribute the detected correlations to physical drivers, we define 6 groups of potential drivers of seasonal correlation magnitude, which are: basin size, flow indices, presence of lakes and glaciers, catchment elevation, catchment geology, and hydro-climatic forcing. For some of the descriptors the information is available for a few countries only.
- In what follows, we will use the term "positive (negative) impact on correlation" to imply that an increasing value of the considered descriptor is associated to increasing (decreasing) correlation. For each descriptor, we also report between parentheses the Spearman's rank correlation coefficient r_s (Spearman, 1904) between its value and the considered (LFS or HFS) correlation, and the p-value of the null hypothesis $r_s = 0$. Spearman's coefficient is adopted in view of its robustness to the presence of outliers and its capability of capturing monotonic relationships of non-linear type.

5.1 Catchment area – Descriptor A

- Figure 5 shows that there is only a weak positive impact of the catchment area (log-transformed) on
- correlation for HFS ($r_s = 0.17$, p = 0.01) but a more significant positive one for LFS ($r_s = 0.27$, $p = 5.5 \times 10^-$
- 338 ⁵). The presence of relevant scatter in the plots also indicates that it is not a key determinant of correlation.

5.2 Flow indices – Descriptors BI and SR

- The effect of the BI and SR is shown in Fig. 6. BI (Fig. 6a) appears to be a marked positive driver for LFS
- 341 ($r_s = 0.6$, $p = 1.8 \times 10^{-23}$) while its effect for HFS is less clear, being weakly positive ($r_s = 0.21$, p = 0.001).

For SR (Fig. 6b), it appears that both LFS and HFS streamflow correlations drop for increasing wetness (r_s

343 = -0.4, p = 4×10^{-10} and $r_s = -0.28$, p = 2.8×10^{-5} respectively).

5.3 Presence of lakes and glaciers – Descriptors PL and PG

Detailed information on the presence of lakes is available for the 69 Swedish catchments while areal extension of glaciers is known for the 108 Austrian catchments. Figure S1 in the Supplement shows that the impact of lake area (Fig. S1a) on correlation for LFS and HFS is not significant but positive ($r_s = 0.10$, p = 0.399 and $r_s = 0.12$, p = 0.347). The results for glaciers show a positive impact for LFS ($r_s = 0.28$, p = 0.081) but negative for HFS ($r_s = -0.34$, p = 0.032). For a meaningful interpretation, these results should be considered in conjunction with the seasonality of flows for the Austrian catchments. Low flows for the glacier-dominated catchments are typically occurring in winter months, when glaciers are not contributing to the flow (Parajka et al., 2009). Thus the observed result for LFS is more likely portraying the impact of low temperature (low evapotranspiration) and snow accumulation, the latter generally being a slowly varying process. For HFS, which is typically occurring in the summer months for the considered catchments, flows are mainly determined by snowmelt which is associated to large variability and reduced persistence (Fig. S1b).

5.4 Catchment elevation

The areal coverage of the SRTM data is limited to 60 degrees north and 54 degrees south and therefore, data for the northern part of the Swedish catchments are not available. The rest of the rivers are divided in three regions based on proximity: Region I including the central and eastern part of the Alps and encompassing Austrian, Slovenian and Italian catchments; Region II showing the western part of the Alps and encompassing French and Spanish territory; and Region III including the southern part of Sweden. Figure 8 shows elevation maps along with the location of gauge stations and magnitude of correlations. Elevation seems to enhance LFS correlation which is more evident in the mountainous Region I (Fig. 7). For HFS correlation there is not a prevailing pattern.

In the case of Austrian catchments, a 1 km resolution digital model is also used to extract information on elevation. Figure 8 confirms that there is a positive correlation pattern emerging with elevation for LFS. Based on local climatological information, it can be concluded that the spatial pattern for LFS correlation is reflective of the timing and strength of seasonality of the low flows in Austria, where dry months occur in lowlands during the summer due to increased evapotranspiration and in the mountains during winter (mostly February) due to snow accumulation which is characterised by stronger seasonality compared to the lowlands flow regime (Parajka et al., 2016; see Fig. 1). Concerning HFS in the same region, high flows are significantly impacted by the seasonality of extreme precipitation (Parajka et al., 2010), which is highly variable, with the exception of the rivers where high flows are generated by snowmelt. Therefore, a spatially consistent pattern does not clearly emerge.

5.5 Catchment geology – Descriptors PK and PF

Two different geological behaviours are identified which may impact river correlation. We first focus on 21 Slovenian catchments (out of 31) where more than 50% of the basin area is characterised by the presence of karstic aquifers (percentage of karstic areas $PK \ge 50\%$). Figure 9 shows boxplots of the estimated lag-1 correlation coefficient for both HFS and LFS against rivers where PK < 50%. It is clear that there is a significant decrease in correlation where karstic areas dominate for both for HFS and LFS.

In a second analysis, we focus on Austrian catchments and investigate the relationship between correlation and percentage of Flysch coverage, PF. Figure S2 in the Supplement shows that there is not a prevailing pattern in either case ($r_s = 0.13$, p = 0.6 for LFS and $r_s = -0.19$, p = 0.446 for HFS).

5.6 Atmospheric forcing – Descriptors *P* and *T*

Figure 10 shows the lag-1 HFS and LFS correlations against estimates of the annual precipitation P and annual mean temperature T as well as the De Martonne index IDM. LFS correlation appears to be more sensitive than HFS to the above climatic indices, showing a decrease with increasing temperature and also a

decrease with increasing precipitation ($r_s = -0.44$, $p = 3.1 \times 10^{-12}$ for P and $r_s = -0.57$, $p = 1.8 \times 10^{-20}$ for 390 391 T). **HFS** correlation scarcely sensitive is to these variables (r_s) 392 -0.17, p = 0.011 for P and $r_s = 0.08$, p = 0.208 for T). The IDM (Fig. 10 c) shows a mild decrease of both 393 LFS ($r_s = -0.06$, p = 0.368) and HFS correlation with increasing IDM ($r_s = -0.17$, p = 0.01), while for the 394 latter there seems to be a clearer trend (lower correlation with higher IDM) in very humid areas (dark blue 395 points in Fig. 10c).

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5.7 Physical drivers of high correlation

To gain further insights into the results we select the 20 catchments with the highest streamflow seasonal correlation coefficients for both HFS and LFS periods in order to investigate their physical characteristics in relation to the remaining set of rivers. Table 2 summarizes statistics for selected descriptors in order to identify dominant behaviours. We also compare the number of rivers with distinctive features, i.e. lakes N_L (number of rivers with lakes), glaciers N_G (number of river with glaciers), flysch N_F (number of rivers with flysch formations) and karst N_K (number of rivers with karstic areas) for the highest correlation group with those obtained from 1000 randomly sampled 20-catchment groups from the whole set of considered catchments to assess whether higher correlation implies distinctive features.

By focusing on HFS, one can notice that the catchments with higher seasonal correlation are characterised by larger catchment area, higher baseflow index and temperature with respect to the remaining catchments, and lower specific runoff, precipitation and wetness. Presence of lake, glaciers, karstic and Flysch areas do not appear significantly effective at a 5% significance level. More robust considerations can be drawn for the LFS: higher seasonal correlation is found for larger catchments with higher baseflow index and lower specific runoff, precipitation and wetness. Decreasing temperature is strongly associated with higher correlation for the LFS. The presence of lakes plays a significant role both for lag-1 and lag-2 correlations with the latter being also significantly influenced by presence of glaciers.

6. Principal component analysis of the predictors and linear regression

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We attempt to fit a linear regression model to relate correlation to physical drivers, in order to support correlation estimation for ungauged catchments. To avoid the impact of multicollinearity in the regression while additionally summarizing river information, we apply PCA (see Section 2.2). Although correlation effects are efficiently dealt with via the PCA, we avoid including highly correlated variables in the analysis. For example, the De Martonne Index, Precipitation and SR are mutually highly correlated (all Pearson's cross-correlations are higher than 0.6) and therefore we only consider the SR in the PCA because it shows a more robust linear relationship with correlation magnitude. We select A, BI, SR and T as the variables to be considered in the PCA. A log transformation is applied on the basin area to reduce impact of outliers. Table 3 shows the coefficients estimated for each component (the loadings) and the explained variance. The first principal component is primarily a measure of BI; the second principal component mostly accounts for T and the third principal component accounts for A. There is an evident geographical pattern emerging by the visualization of countries in the biplot (Fig. 11). Slovenian rivers cluster towards the direction of increasing SR and T, whereas Swedish rivers towards the opposite direction of increasing BI and decreasing T. Austrian rivers, which are the majority, are the most diverse. The first two components together explain the 70% of the total variability in the data.

Naturally, the statistical behaviour of the indices reflects the known local controls for certain rivers. For example, the observed lowest BI in Slovenia is consistent with the presence of karstic formations for the majority of the Slovenian rivers, as is the higher BI in Sweden and Austria, which is related to the presence of lakes and glaciers in both countries.

In the case of HFS, all the examined linear models (combinations of $\ln A$, SR, BI, P, T, IDM predictors) failed in explaining the streamflow correlation magnitude. On the contrary, the linear regression model performs fairly well in explaining the correlation for LFS, with an adjusted R^2 value of 0.58 and an F-test returning a p-value $< 2.2 \times 10^{-16}$. The coefficients for the first three PCs are found significantly different from zero at a 0.1% significance level and are included in the regression (see Table 4). The

highest coefficient is obtained for the first PC, which mostly accounts for BI importance. Diagnostic plots from linear regression for LFS are shown in Fig. 12. There is no clear violation of the homoscedasticity assumption in linear regression, apart from the presence of a limited number of outliers. There is a certain departure from normality in the lower tail of the residuals, which relates to the fact that the model performs better in the area of higher seasonal streamflow correlations and overestimates the lower correlations.

7. Real-time updating of the frequency distribution of high and low flows for the Oise River

We apply the technical experiment (see section 2.3) for high and low flows to the Oise River in France and assess the difference in the estimated flood and low-flow magnitudes. We update the probability distribution of high and low flows after the occurrence of the upper 95% and lower 5% sample quantile of the observed mean flow in the previous month, respectively.

The Oise River (55 years of daily flow values) at Sempigny in France has a basin area of 4320 km² and its gauging station at Sempigny is part of the French national real-time monitoring system (https://www.vigicrues.gouv.fr/), which is in place to monitor and forecast floods in the main French rivers. The selected river has a high technical relevance since it experiences both types of extremes with large impacts. For instance, a severe drought event in 2005 led to water restrictions impacting agriculture and water uses in the region (Willsher, 2005), while the river originated an inundation during the 1993 flood events in northern and central France, which was one of the most catastrophic flood-related disasters in Europe in the period 1950-2005 (Barreldo, 2007). It is characterized by HFS correlation $\rho = 0.54$, which is the 3rd largest lag-1 correlation for the HFS in our dataset and LFS correlation $\rho = 0.80$, which stands for the 70% quantile of the sample lag-1 correlation for LFS.

A visual inspection of the residuals plots is also performed (Fig. 13a, b) in order to evaluate the assumption of homoscedasticity of the residuals of the regression models given by Eq. (2). The residuals do not show any apparent trend and therefore the Gaussian linear model is accepted. Figure 13 (c, d) shows the conditioned and unconditioned probability distributions of peak and low flows in the Gaussian domain. As

follows from Eq. (3) and (4), the variance of the updated (conditioned) distributions decreases while the mean value increases.

After application of the inverse NQT the conditioned peak flows are modelled through the EV1 distribution and compared to the unconditioned (observed) peak flows. The corresponding Gumbel probability plot for conditioned and unconditioned distributions is shown in Fig. 13e. For the return period of 200 years, the updated distribution shows a 6% increase in the flood magnitude for the Oise River (307.7 m³ s⁻¹ to 326.44 m³ s⁻¹). Likewise, the conditioned low flows are modelled through the lognormal distribution. The two cumulative distribution functions are compared in Fig. 13f showing a major departure in the estimated quantiles for the updated distribution; the occurrence of the predefined 5% quantile flow in the pre-LFS month induces a decrease of the exceedance probability of an average LFS flow of 15 m³ s⁻¹ from a prior 43% (according to the unconditioned model) to 1%.

8. Discussion

The methodology presented herein aims to progress our physical understanding of seasonal river flow persistence for the sake of exploiting the related information to improve probabilistic prediction of high and low flows. The correlation of average flow in the previous months with LFS flow and HFS peak flow was found to be relevant, with the former prevailing on the latter. This result was foreseen since the LFS correlation refers to average flow while the HFS correlation is related to rapidly occurring events. We also aim to investigate physical drivers for correlation and quantify their relative impact on correlation magnitude. Therefore, a thorough investigation of the geophysical and climatological features of the considered catchments was carried out.

We found that increasing basin area and baseflow index are associated with increasing seasonal streamflow correlation, yet the latter has a stronger impact. To this respect, Mudelsee (2007), Hirpa et al. (2010) and Szolgayova et al. (2014a) also found positive dependencies of long-term persistence on basin area, Markonis et al. (2018) found a positive impact too but for larger spatial scales ($> 2 \times 10^4 \text{ km}^2$), while Gudmunsson et al. (2011) found basin area to have negligible to no impact to the low-frequency

components of runoff. Our results additionally point out that catchment storage induces mild positive correlation, not only for low discharges which are directly governed by base flow, but also for high flows, which is less anticipated.

Previous studies also pointed out that correlation increases for groundwater-dominated regimes (Yossef et al., 2013; Dijk et al., 2013; Svensson, 2016) and slower catchment response times (Bierkens and van Beek, 2009), which concurs with the impact of baseflow index found herein as well as with the observed impact of fast responding karst areas. The latter findings are also in agreement with our conclusion that correlation decreases for increasing rapidity of river flow formation, which for instance occurs in the presence of karstic areas and wet soils, which explains why persistence decreases with high specific runoff; as also confirmed by other studies (Gudmundsson et al., 2011; Szolgayova et al., 2014).

Other contributions also reported higher streamflow persistence in drier conditions, either relating to lower specific runoff or mean areal precipitation estimates (Szolgayova et al., 2014; Markonis et al., 2018). It was postulated that this is due to wet catchments showing increased short-term variability compared to drier catchments (Szolgayova et al., 2014) and having a faster response to rainfall due to saturated soil. A similar conclusion has been reached by other previous studies reporting that low humidity catchments are more sensitive to inter-annual rainfall variability (Harman et al., 2011), therefore leading to enhanced persistence. Yet, these studies refer to generally humid regions and cannot be extrapolated to more arid climates. A related conclusion is proposed by Seneviratne et al. (2006) who found the highest soil moisture memory for intermediate soil wetness. These results do not contrast with our findings, which refer to a wide range of climatic conditions. In fact, our finding that increased wetness has a negative impact on seasonal memory of both high and low flows, extends the above results to the seasonal scale and interestingly, to both types of extremes.

We also confirm the role of lakes in determining higher catchment storage and therefore positive correlations for the LFS, which has only been reported for annual persistence in a few sites (Zhang et al., 2012).

The effect of snow cover for lag-1 LFS correlation is also revealed by the Austrian catchments. The mountainous rivers, directly affected by the process of snow accumulation, exhibit winter LFS and higher correlation than the rivers in the lowlands, which are more prone to drying out due to evapotranspiration in the hotter summer months. The inspection of elevation data confirmed the role of high altitudes in increasing LFS correlation, which is likely related to storage effects due to snow accumulation and gradual melting. In this respect, Kuentz et al. (2017) found that topography exerts dominant controls over the flow regime in the larger European region, controlling the flashiness of flow, and being a particularly important driver for other low flow signatures too. In fact, topography may affect the flow regime directly, through flow routing, but also indirectly, because of orographic effects in precipitation and hydroclimatic processes affected by elevation (e.g. snowmelt and evapotranspiration).

Regarding atmospheric forcing, we find LFS correlation to be negatively correlated to mean areal temperature and annual precipitation. The former result may be explained considering that increased evapotranspiration (higher temperature) is likely to dry out LFS flows while snow coverage (lower temperature) was found to be associated with higher LFS correlation. An apparently different conclusion was drawn by Szolgayova et al. (2014a) and Gudmundsson et al. (2011), who reported increasing persistence with increasing mean temperature postulating that snow-dominated flow regimes smooth out interannual fluctuations. Yet, it should be noted that they refer to interannual variability while we refer here to seasonal correlation and therefore to shorter time scales, which imply a different dynamic of snow accumulation and snowmelt; latitude may also play a relevant role in this, since in southern Europe the complete ablation of snow can occur more than once during the cold season, and sublimation may account for 20–30% of the annual snowfall (Herrero and Polo, 2016), decreasing the amount of snowmelt and impacting LFS flows in the summer season.

Snowmelt mechanisms are found to increase predictive skill during low-flow periods in some other studies (Bierkens and van Beek, 2009; Mahanama et al., 2011; Dijk et al., 2013). However, in the glacier-dominated regime of western Alpine and central Austrian catchments, it is unlikely that this is a relevant

driver of higher correlation, since low flow is occurring in the winter months. Yet the mountainous, glacier-dominated rivers still show increased LFS correlation compared to rivers in the lowlands, which agrees well with other studies that have found less uncertainty in the rainfall-runoff modelling in this regime owing to the greater seasonality of the runoff process and the decreased impact of rainfall compared to the rainfall-dominated regime of the lowlands (e.g Parajka et al., 2016).

Although the considerable uncertainty of areal precipitation estimates should be acknowledged, the contribution of annual precipitation interestingly complements the negative effect of increasing specific runoff –which is highly correlated to *P* estimates– on the correlation magnitude for both LFS and HFS. This outcome confirms that catchments receiving significant amount of rainfall do show less correlation than drier regimes as discussed before.

9. Conclusions and outlook

- This research investigates the presence of persistence in river flow at the seasonal scale, the associated physical drivers and the prospect for employing the related information to improve probabilistic prediction of high and low flows by exploring a large sample of European rivers. The main findings are summarized below:
- Rivers in Europe show persistent features at the seasonal timescale, manifested as correlation between high- and low-flow signatures, i.e. peak flows in HFS and average flows in LFS respectively, and average flows in the previous month. Correlation for LFS signatures is found consistently higher than HFS.
- Seasonal correlation shows increased spatial variability together with spatial clustering.
- Storage mechanisms, groundwater-dominated basins and slower catchment response time, as reflected by large basin areas, high baseflow index and the presence of lakes, amplify seasonal correlation. On

the contrary, correlation is lower in quickly responding karstic basins, and increased wetness conditions, as revealed by high specific runoff.

- Low mean areal temperature is associated with higher LFS correlation owing to the weaker drying-out evapotranspiration force and the mechanism of snow accumulation in higher altitudes. Higher mean areal precipitation is associated with lower LFS predictability, possibly due to the presence of saturated conditions and increased short-term variability in wetter climates.
- The drivers of LFS predictability are easier to identify and allow for the opportunity to construct regression models for possible application to ungauged basins (see Section 6).
- HFS and LFS correlation may directly serve for the probabilistic prediction of 'extremes', i.e. high and low flows, as increased correlation can be exploited in various stochastic models. Such an application was performed in Section 7 in a data assimilation setting for a river of marked technical relevance.

Regarding the latter, once a significant correlation is identified, it may be exploited in other model variants as well, e.g. adding more dependent variables of lagged flow and/or coupling with other relevant explanatory variables, such as teleconnections or antecedent rainfall, in multivariate prediction schemes. Indeed, the presence of river memory at the seasonal scale represents a possible opportunity to improve the prediction of water-related natural hazards by reducing uncertainty of associated estimates and allowing significant lag time for decision-making and hazard prevention. Besides the high relevance for extremes, this type of seasonal predictability could also be of interest to water resources management by, for instance, exploring the memory properties of a minor HFS.

The inspection of the physical basis, apart from advancing our understanding of the catchment dynamics and enabling predictions in ungauged basins, is highly important as it may guide the search for other dependent variables and build confidence in the formation of process-based stochastic models (Montanari and Koutsoyiannis, 2012). A large sample of indices was herein inspected, yet data are majorly needed to allow for more certain and generalized conclusions worldwide. An important note is the presence of regulation, the effect of which, due to lack of objective data, is not completely understood. However, the

opportunity of exploiting correlation is not affected by the presence of regulation, provided that the management of river flow does not change in time.

We conclude that our results point out that river memory provides interesting information that holds both theoretical and operational potential to improve the understanding and prediction of extremes, support decision-making and increase the level of preparedness for water-related natural hazards.

Data and Code availability

- The data and code used in this study may be made available to the readers upon request to the corresponding author.
- **Competing interests**
- The authors declare that they have no conflict of interest.

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Tables

Table 1 Summary statistics of the river descriptors. Summary statistics for PL, PG and PF variables are computed only for the subset of catchments with positive values (the total number of catchments is also reported in brackets). PK is used as a categorical variable (PK is either higher or lower than 50% of catchment area), therefore sample statistics are not computed in this case, but the number of stations with $PK \ge 50\%$ is reported as 'positive' presence of karst.

Descriptor (Units)	A (km²)	BI (-)	$\begin{array}{c} SR \\ (m^3 \ s^{-1} \ km^{-2}) \end{array}$	PL (%)	PG (%)	PF (%)	PK (-)	P (mm year ⁻¹)	T (°C)	IDM (-)
Min	4.7	0.29	0.004	0.5	0.1	0.3	_	444	-1.8	29.41
Max	70091	0.99	0.088	19.5	56.5	100	_	1500	13.7	153.40
Standard deviation	5904.3	0.14	0.018	4.04	15.54	32.56	-	288.22	3.59	24.53
Sample size	224	224	224	69 [69]	39 [108]	18 [108]	21 [31]	224	224	224

Table 2 Differences in the mean values between the descriptors of the 20-highest correlation river group for HFS and LFS vs the remaining rivers (204). N_L , N_G , N_F and N_K columns contain the absolute number of rivers in the higher correlation group with the specific descriptor (presence of lake, glacier, flysch and karst) with * denoting significance at 5% significance level (two-sided test) and brackets containing the mean value from the 1000 resampled 20-catchment subsets.

Descriptor (Units)	A (km²)	BI (-)	SR $(m^3 s^{-1} km^{-2})$	<i>N</i> _L (–)	<i>N</i> _G (–)	<i>N</i> _F (–)	<i>N</i> _K (–)	P (mm year ⁻¹)	T (°C)	IDM (-)
HFS lag1	+38.7%	+9.6%	-36.5%	5 [6]	5 [3]	1 [2]	1 [2]	-6.7%	+11.7%	-11.3%
LFS lag1	+358%	+20.2%	-47.3%	17* [6]	3 [3]	0 [2]	0 [2]	-37.9%	-80%	-17.3%
LFS lag2	+139.7%	+18.9%	-40.8%	12* [6]	7* [3]	0 [2]	0 [2]	-26.5%	-64.2%	-8.8%

Table 3 Loadings of the three Principal Components for ln A, SR, BI and T. The explained variance of each PC is denoted in parenthesis.

Predictor variables	PC1 (42.5%)	PC2 (28.2%)	PC3 (17%)	PC4 (12.2%)
ln A	-0.486	-0.427	0.748	0.145
SR	0.48	0.483	0.652	-0.332
BI	-0.619	0.262	-0.11	-0.731
T	0.385	-0.718	-0.04	-0.577

Table 4 Summary of Linear Regression results for the LFS model. *** indicate a 0.1% significance level.

Predictor	Estimate	Standard Error	t value	Pr(> t)	Adjusted	F-statistic
variables					\mathbb{R}^2	
intercept	0.659407	0.008557	77.065	< 2 ×10 ⁻¹⁶ ***	0.5834	104.2
PC1	-0.110632	0.006577	-16.820	$< 2 \times 10^{-16}***$		p-value:
PC2	0.031761	0.008070	3.936	0.000111***		$< 2.2 \times 10^{-16}$
PC3	-0.038999	0.010388	-3.754	0.000223***		

Figures

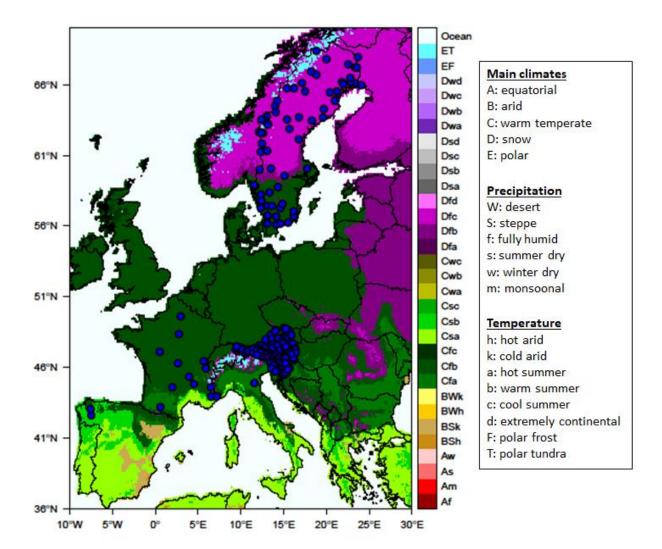


Figure 1. Updated Köppen-Geiger climatic map for period 1951–2000 (Kottek et al., 2006) showing the location of the 224 river gauge stations.

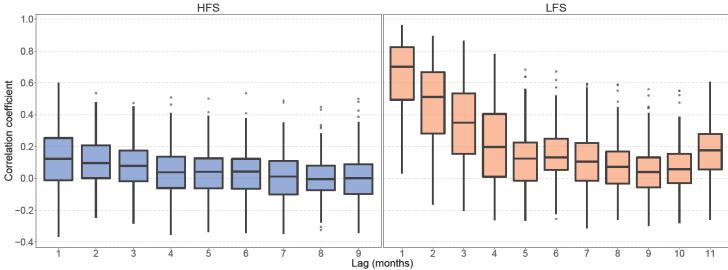


Figure 2. Boxplots of seasonal correlation coefficient against lag time for HFS (left panel) and LFS (right panel) analysis for the 224 rivers. The lower and upper ends of the box represent the 1st and 3rd quartiles, respectively, and the whiskers extend to the most extreme value within 1.5 IQR (interquartile range) from the box ends; outliers are plotted as filled circles.

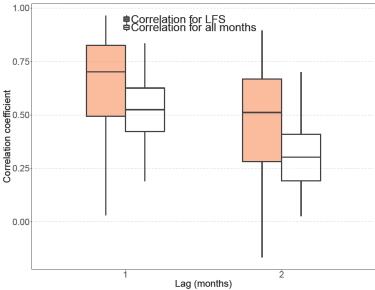


Figure 3. Boxplots of lag-1 and lag-2 correlation coefficients for LFS analysis (orange) and the whole monthly series (white) for the 224 rivers. The lower and upper ends of the box represent the 1st and 3rd quartiles, respectively, and the whiskers extend to the most extreme value within 1.5 IQR (interquartile range) from the box ends.

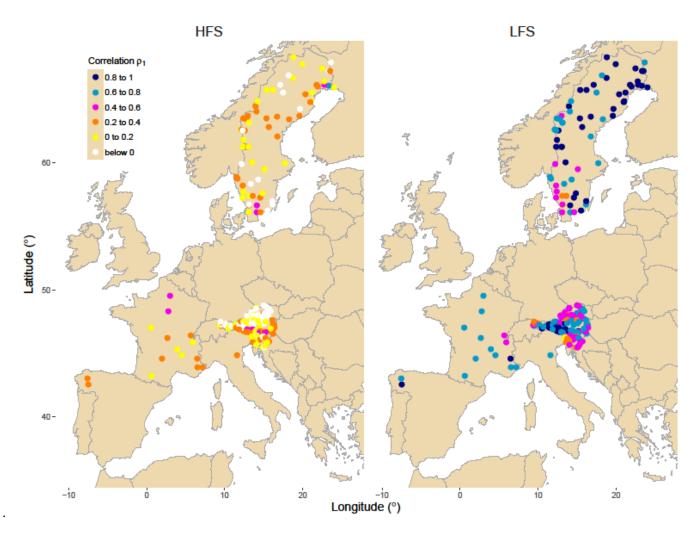


Figure 4. Spatial distribution of the lag-1 correlation coefficients for HFS (left) and LFS (right) analysis. Legend shows the color assigned to each class of correlation for the data.

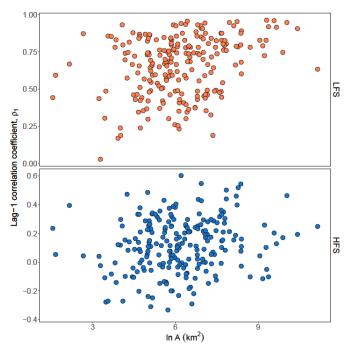


Figure 5. Scatterplots of lag-1 HFS (bottom panel) and LFS (top) streamflow correlation versus the natural logarithm of basin area ln *A*.

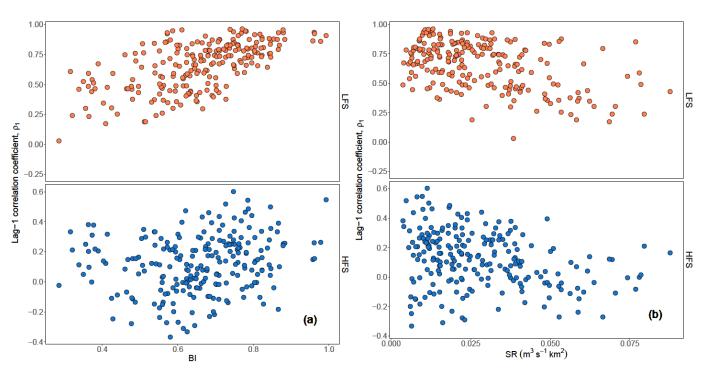


Figure 6. Scatterplots of lag-1 HFS (bottom panels) and LFS streamflow correlation (top panels) versus baseflow index BI (a) and specific runoff SR (b).

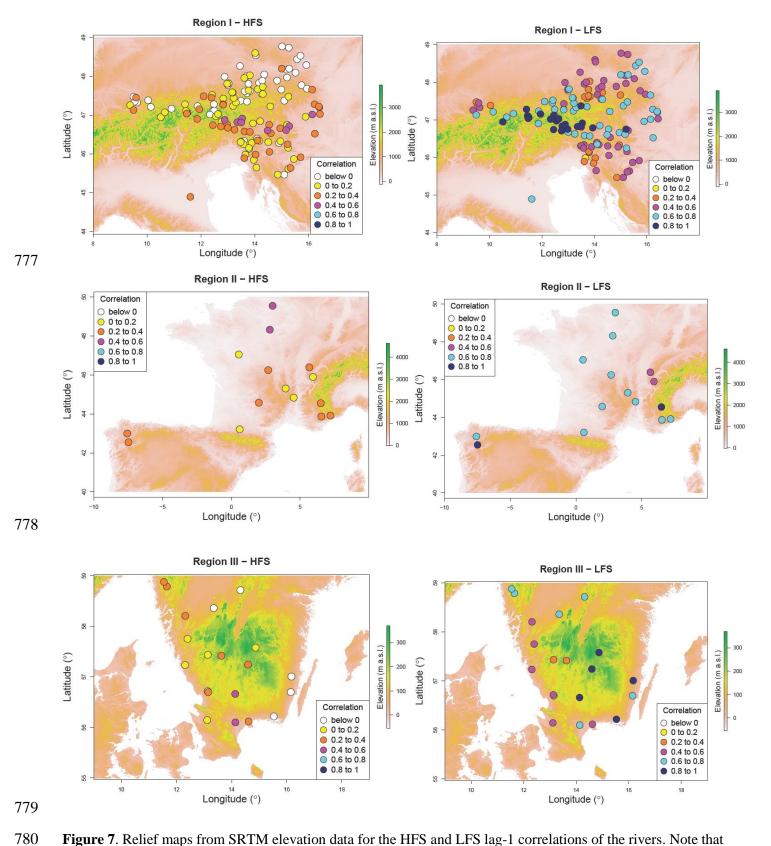


Figure 7. Relief maps from SRTM elevation data for the HFS and LFS lag-1 correlations of the rivers. Note that elevation scale is different for each region. Legend shows the colour assigned to each class of correlation for the data.

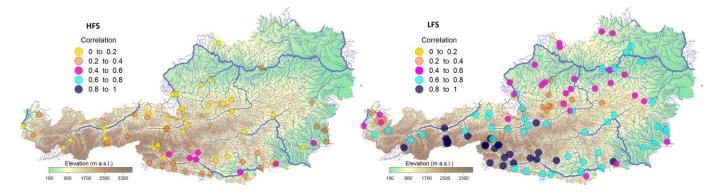


Figure 8. Digital elevation model of the Austrian river network depicting the spatial distribution of lag-1 positive correlation for HFS (left) and lag-1 positive correlation for LFS (right). Legend shows the colour assigned to each class of correlation for the data.

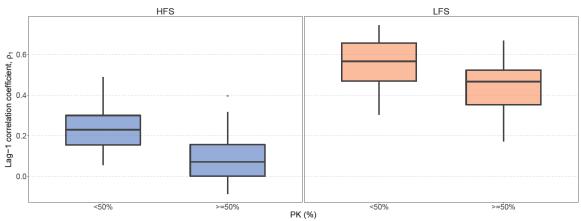


Figure 9. Boxplots of lag-1 correlation for Slovenian rivers with more than 50% presence of karstic formations PK and rivers with no or less presence for HFS analysis (left) and LFS analysis (right). The lower and upper ends of the box represent the 1st and 3rd quartiles, respectively, and the whiskers extend to the most extreme value within 1.5 IQR (interquartile range) from the box ends.

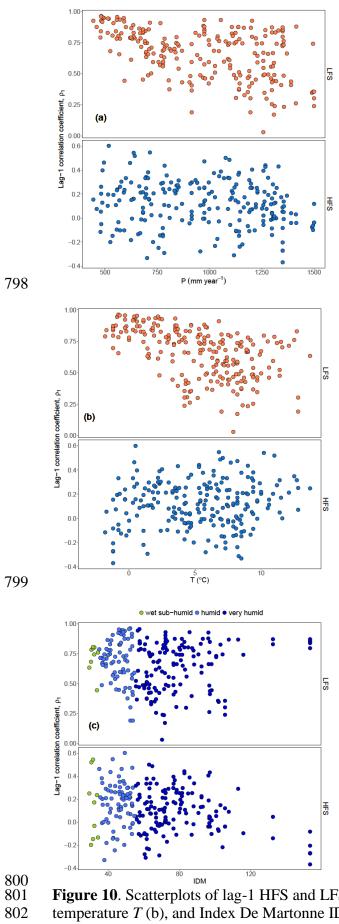


Figure 10. Scatterplots of lag-1 HFS and LFS correlation versus annual precipitation P (a), mean annual temperature T (b), and Index De Martonne IDM (c).

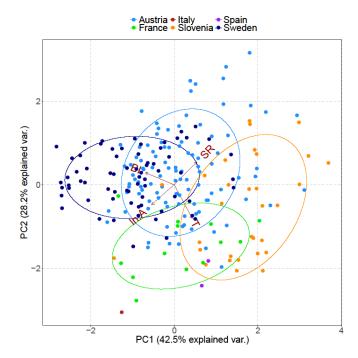


Figure 11. Principal component distance biplot showing the principal component scores on the first two principal axes along with the vectors (brown arrows) representing the coefficients of the baseflow index BI, specific runoff SR, natural logarithm of basin area ln *A* and mean annual temperature *T* variables when projected on the principal axes. Scores for the rivers are plotted in different colors corresponding to each country of origin and 68% normal probability contour plots are plotted for the countries.

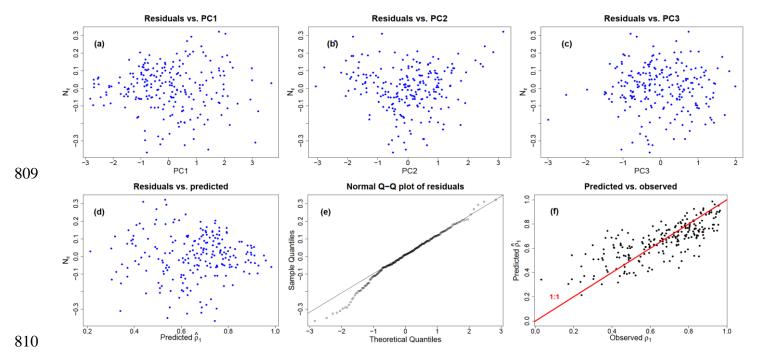


Figure 12. Diagnostic plots of linear regression for the LFS model. Residuals versus the first (a), the second (b) and the third principal component (c) and the predicted values (d). Normal Q-Q plot of the residuals (e). Plot of the predicted values from linear regression vs the observed ones; red line is the diagonal line 1:1 (f).

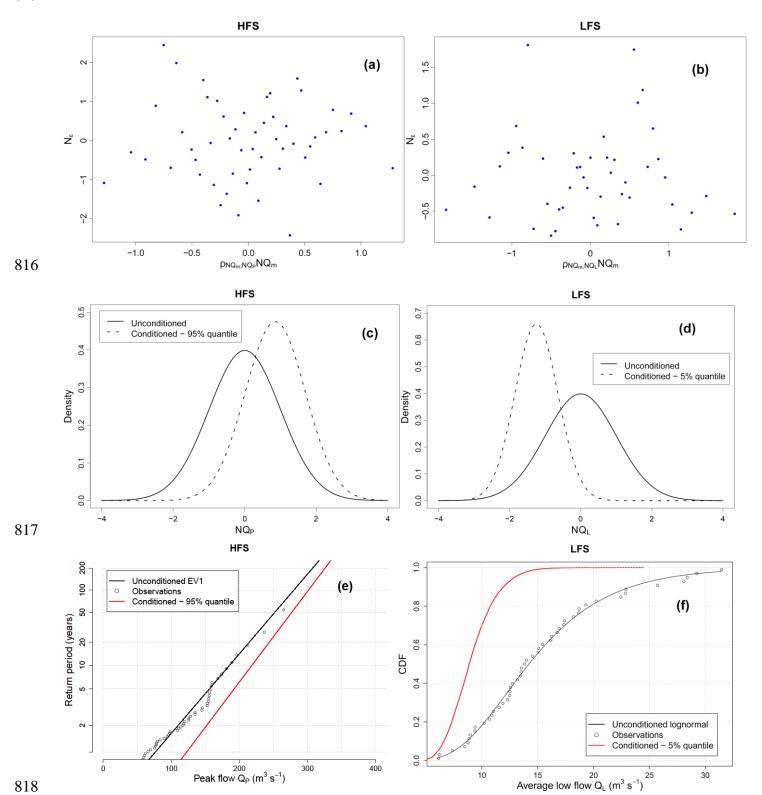


Figure 13. Conditioning the frequency distributions for high and low flows for the Oise River. Plots of the residuals of the linear regression given by Eq. (2) for the HFS (a) and LFS (b) models. Probability distribution of the unconditioned normalized peak flows NQ_P (solid line) and the normalized peak flows NQ_P conditioned to the occurrence of the 95% quantile (dotted line) for the HFS (c) and probability distribution of the unconditioned normalized low flows NQ_L (solid line) and the normalized low flows NQ_L conditioned to the occurrence of the 5% quantile (dotted line) for the LFS (d). Gumbel probability plots of the return period vs the unconditioned peak flows Q_P (black line) and the peak flows Q_P modelled by the EV1 distribution and conditioned to the occurrence of the 95% quantile (red line) for the HFS (e) and cumulative distribution function of the unconditioned low flows Q_L (black line) and the low flows Q_L modelled by the lognormal distribution and conditioned to the occurrence of the 5% quantile (red line) for the LFS (f).