Rainfall disaggregation for hydrological modeling: Is there a need for spatial consistence?

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Abstract.

In this investigation, the influence of disaggregated rainfall products with different degrees of spatial consistence on rainfall runoff modeling results is analyzed for three meso-scale catchments in Lower Saxony, Germany. For the disaggregation of daily rainfall time series into hourly values a multiplicative random cascade model is applied. The disaggregation is applied on a per station basis without consideration of surrounding stations, hence subsequent steps are then required to implement spatial consistence. Spatial consistence is here represented by three bivariate spatial rainfall characteristics, complementing each other. A resampling algorithm and a parallelization approach are evaluated against the disaggregated time series without any subsequent steps. With respect to rainfall, clear differences between these three approaches can be identified regarding bivariate spatial rainfall characteristics, areal rainfall intensities and extreme values. The resampled time series lead to the best agreement with the observed ones. Using these different rainfall products as input to hydrological modeling, we hypothesize that derived runoff statistics are subject to similar differences as well. However, an impact on the runoff statistics summer and winter peak flows, monthly average discharge and flow duration curve of the simulated runoff time series cannot be detected. Several modifications of the investigation using rainfall runoff models with and without parameter calibration or using different rain gauge densities lead to similar results in runoff statistics. Only if the spatially highly resolved rainfall-runoff WaSiM-model is applied instead of the semi-distributed HBV-IWW-model, slight differences regarding the seasonal peak flows can be identified. Hence, the hypothesis formulated before is rejected in this case study. These findings suggest that (i) simple model structures might compensate for deficiencies in spatial representativeness through parameterization and (ii) highly resolved hydrological models benefit from improved spatial modeling of rainfall.

1. Introduction

Flood quantiles are important information for the creation of flood hazard maps, the construction of riverfront buildings and landscape development plans, for example. For ungauged catchments and catchments with short discharge observation periods, rainfall-runoff modeling is a possibility to obtain long, simulated discharge time series which can then be used for derived flood frequency analysis.

The most important data input for rainfall-runoff modeling are rainfall time series (Beven, 2001). Melsen et al. (2015) gave an overview of typical processes for different catchment sizes and corresponding temporal resolutions. For catchments with areas of a few hundred square kilometers, time series with hourly resolutions are required for the simulation of instantaneous flood peaks. In most of these cases, observed rainfall time series of that kind are i) too short or ii) the network density is too low. Both are issues-, because i) limits the length of the simulation period and hence the derivable flood frequencies and ii) effects the representationof spatial rainfall patterns (Krajewski et al. (1991), Ogden and Julien (1993), Obled et al. (1994) and Nicotina et al. (2008)) and hence the areal rainfall used as input for the rainfall-runoff simulations.

Usually, time series of daily stations have much longer observation periods and a higher network density. Daily time series can be disaggregated to hourly time series by usinginformation from observed, hourly time series. One possible method for the disaggregation of rainfall is the multiplicative random cascade model (e.g. Olsson, 1998), which was originally introduced within the field of turbulence theory (Mandelbrot, 1974). The use of observed daily time series as input is a strong advantage of the cascade model, since starting with "true" rainfall amounts and intermittency facilitates their conservation to finer temporal resolutions, while other rainfall generators (e.g. Poisson-cluster models (Rodriguez-Iturbe et al., 1987, Onof et al., 2000)) try to generate time series with a certain temporal resolution and target statistics without any temporal reference to observations.

With the micro-canonical cascade model, the rainfall amount of a coarse time step (e.g. a day) is conserved exactly through the disaggregation process, so that an aggregation of the disaggregated time series would result exactly to the original observed time series. Starting from a daily resolution, an hourly temporal resolution is achieved, which is a convenient input resolution for many rainfall-runoff models. However, this disaggregation method is a univariate process, carried out for single time series only which are independent from the time series of surrounding stations. Through the systematically random distribution of the rainfall amount within a day, unrealistic patterns of rainfall are generated and the spatial consistence of rainfall is missing. If an unrealistic spatial distribution of rainfall is used within a rainfall-runoff simulation, it can be assumed that this affects the simulated runoff. However, a realistic spatial representation of rainfall is essential if the time series serve as input for rainfall-runoff modeling (e.g. Gires et al., 2013, Paschalis et al., 2014, Ochoa Rodriguez et al., 2015, Peleg et al., 2017).)

Müller and Haberlandt (2015) have introduced a resampling scheme as a subsequent step after the disaggregation process, which can be used for the implementation of spatial consistence within disaggregated time series. Spatial consistence is hereby defined by three bivariate rainfall characteristics: the probability of occurrence, the coefficient of correlation after

Pearson, and the continuity ratio (Wilks, 1998). The implementation of spatial consistence for hourly time series was proven by the above mentioned bivariate characteristics in addition to areal rainfall intensities resulting from the disaggregated time series. Without resampling, areal rainfall intensities were underestimated. The resampling algorithm was additionally tested for time series of 5 min resolution by Müller and Haberlandt (2016). Bivariate rainfall characteristics as well as the simulated

5   runoff from an artificial sewage system were positively validated against observed rainfall time series and its resulting simulated runoff.

Haberlandt and Radtke (2014) overcame the lack of spatial consistence using a parallelization approach, which leads to an overestimation of simulated floods, but is preferred in comparison to a possible underestimation. However, Ding et al. (2016) also used disaggregated time series for their rainfall-runoff analyzes with a focus on instantaneous peak flows, but

10   without any subsequent changes to the disaggregated time series. Neither a systematic over- or underestimation of simulated discharge and flood peaks can be found in both investigations.

It can be questioned, why the simulation results from both studies, based both upon unrealistic spatial rainfall behavior, leads to an acceptable representation of observed discharge characteristics. The hypothesis of this study is that rainfall products with different degrees of spatial consistence will result in different areal rainfall intensities and hence influence runoff

15   statistics derived from simulated runoff time series. Therefore, three different rainfall products are used as input for rainfall runoff modeling: disaggregated time series with (Müller and Haberlandt, 2015) and without (Ding et al., 2016) implemented spatial consistence, and thirdly time series with an "overestimated spatial consistence" by parallelization (Haberlandt and Radtke, 2014). A systematic comparison is carried out including rainfall-runoff simulations with and without calibration, differing station densities and different rainfall-runoff models.

20   In general, calibration and validation of rainfall-runoff model parameters are carried out by a quantitative comparison of simulated and observed time series. This strategy is not applicable by using disaggregated rainfall time series as input, since the daily rainfall amount is distributed randomly in time during a day. Hence, the temporal connection between rainfall and runoff is missing. An alternative strategy is the calibration on runoff statistics and has been applied before by others, as Yu and Yang (2000), Westerberg et al. (2011), Haberlandt and Radtke (2014), Wallner and Haberlandt (2015) and Ding et al.

25   (2015). Runoff statistics are time-independent, but contain useful information about the hydrograph and hence about the hydrological regime and its characteristics. It is assumed, that by a simultaneous consideration of different complimentary runoff statistics, the runoff behavior can be represented sufficiently. Possible runoff statistics are: runoff extremes for different seasons of a year (to take into account e.g. summer and winter floods with their different genesis and resulting runoff behavior), flow duration curves (to describe the overall behavior), and average monthly values (to describe the inter-

30   annual variability).

The manuscript is organized as follows: after a brief description of the study area and the data in section 2, the rainfall generation including the implementation of spatial consistence and the applied rainfall-runoff models including the calibration technique are explained in section 3. Section 4 includes the results for both the rainfall generation and rainfall-

runoff-modeling. A summary of the rainfall-runoff model results is provided in section 5 and general conclusions and a brief outlook are provided in section 6.

2. Data & Investigation area

2.1 Catchments

5   The investigation is carried out for three catchments in the Aller-Leine river basin, namely Reckershausen, Pionierbrücke and Tetendorf (see Fig. 1). The river basin is situated in Lower Saxony, Northern Germany. Based on the Köppen-Geiger climate classification, the river basin can be divided into a temperate oceanic climate in the north and a temperate continental climate in the south (Peel et al. 2007). For Reckershausen an additional investigation regarding rain gauge network density is carried out. All hourly and daily stations for Reckershausen are shown in Fig. 2.
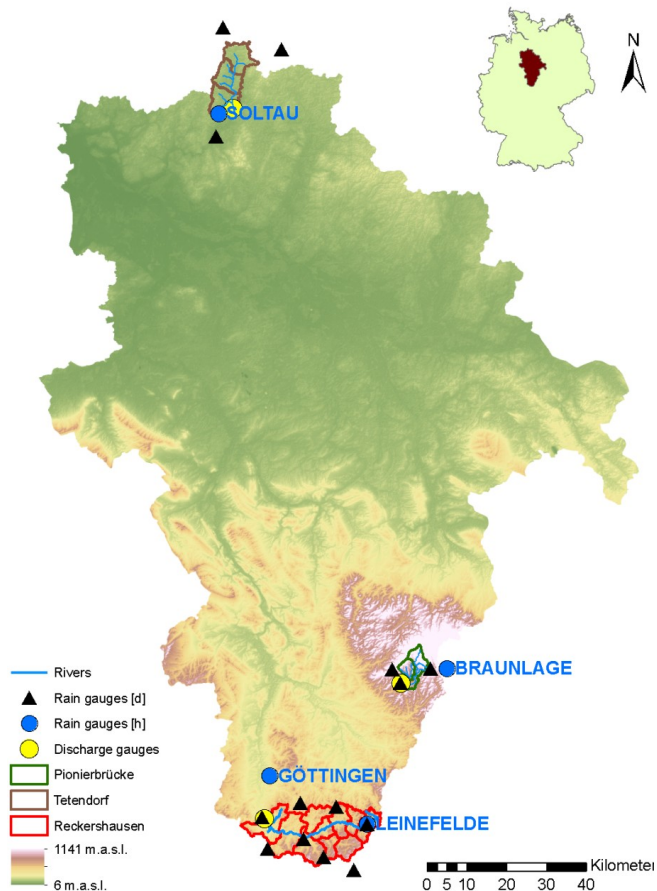
Fig. 1. Location of all three catchments in the Aller-Leine-river basin and its location in Germany.
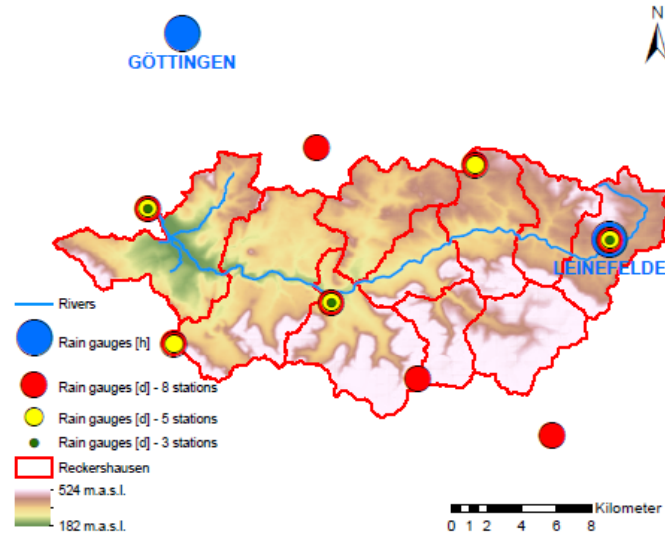
Fig. 2. Catchment Reckershausen including sets of 3, 5 and 8 daily stations used for network density analysis.

The catchments differ concerning area and elevation as well as land use and soil conditions. A brief description can be found in Table 1. The soil information is extracted from the soil map BÜK1000 of the Federal Republic of Germany with a scale of
5   1:1,000,000 (Hartwich et al., 1998). Information regarding the land use is extracted from the CORINE database (Federal Environment Agency, 2009). The time of concentration has been estimated as per Kirpich (1940).

Table 1. Brief description of the investigated catchments with fraction of dominant soil type and land use

Catchment	River	Area [km²]	Sub-catch-ments	Time of concen-tration [h]	Dominant soil type	Dominant land use
Pionierbrücke	Sieber	44	2	1.8	Spodic Cambisols (77 %)	Coniferous forest (81 %)
Tetendorf	Böhme	110	3	7.2	Haplic Podzols / Dystric Regosols (40 %)	Non-irrigated arable land (39 %)
Reckers-hausen	Leine	321	10	7.4	Dystric Cambisols (37 %)	Non-irrigated arable land (59 %)

2.2 Climate data

10   For the rainfall disaggregation, time series of hourly and daily stations are required. Time series of the hourly stations are used for the parameter estimation of the cascade model (described in section 3.1 a), which is in turn used for the

disaggregation of the time series of the daily stations. An overview of rain gauges used in this study is given in Fig. 1 while their measuring periods in Tab. 2 For the daily stations, the chosen period is the longest available period with data for all stations in a catchment. From Table 2 it can be seen, that time series lengths have a longer duration for daily stations in comparison to those from hourly stations for all catchments (up to 2.7 times for Pionierbrücke). Additionally, the number of daily-stations is higher.

Table 2. Rain gauges and time series lengths used for each catchment

Catchment	Type	Rain gauges	Start	End
Pionierbrücke	Daily	3	1950	2004
	Hourly	1	1993	2013
Tetendorf	Daily	3	1984	2006
	Hourly	1	1993	2013
Reckershausen	Daily	8	1972	2006
	Hourly	2	1993	2013

For the rainfall-runoff-model HBV (see section 3.2), time series of precipitation, temperature and potential evaporation are needed. The following description of data processing of temperature and potential evaporation is based on Wallner et al. (2013) and was carried out for the whole Aller-Leine basin. The temperature time series were derived through an interpolation using External Drift Kriging of 38 hourly stations with hourly resolution, whereby the additional information is elevation.

The calculation of the potential evaporation is carried out using the Turc-Wendling method on a daily basis (DVWK, 1996). The required sunshine duration per day was derived through Ordinary Kriging using 29 stations. To achieve an hourly resolution, daily values have been divided by 24, since the inter-daily distribution of potential evaporation has been shown not to be that sensitive as model input. Different land use types have been taken into account by using an average land use parameter (DVWK, 2002) similar to the crop coefficient. All input data were interpolated and subsequently aggregated to subcatchment scale.

For the WaSiM model, which is applied only for the catchment Pionierbrücke, climate time series are needed as point or gridded information on an hourly basis. From the climate station Braunlage, time series of temperature, relative air humidity, and wind speed are available with an hourly resolution. Global radiation was only available on a daily basis, but has been disaggregated to hourly values using an approach as in Förster et al. (2016).

2.3 Runoff data

The available discharge data of the three catchments is listed in Table 3. While observed hourly time series are only available since 2000 (Pionierbrücke) and 2004 (Tetendorf and Reckershausen), observed extreme values exist for much longer periods. Daily discharge time series exist for at least as long as the period of the hourly extreme values on a monthly
5 basis.

For the calibration, a special focus is given to the extreme values of the summer (01.05.-31.10.) and winter period (01.11.-30.04.). Therefore, the maximum observed value of each half year were extracted from both data sources, observed hourly time series and monthly extreme values, to generate periods as long as possible.

Table 3. Available periods of runoff data types

Catchment	Hourly discharge time series	Daily discharge time series	Monthly extreme values
Pionierbrücke	2000-2013	1929-2006	1952-2005
Tetendorf	2004-2013	1986-2000	1986-2000
Reckershausen	2004-2009	1964-2006	1974-2005

3. Methods

The method section consists of two subsections. In the sub section 3.1, the multiplicative cascade model for the disaggregation of rainfall time series is explained. Additionally, two methods for the implementation of spatial consistence in the disaggregated time series are presented. The descriptions of the two rainfall-runoff models HBV and WaSim and the
15 calibration procedure for HBV can be found in subsection 3.2.

3.1 Rainfall generation

a) Rainfall disaggregation

 The multiplicative random cascade model (Müller and Haberlandt, 2015) is applied for the disaggregation of time series of
20 the daily stations. A general scheme of this model is shown in Fig. 3. One coarse time step is divided into b finer time steps of equal length. The branching number b determines the number of finer time steps and is in the first disaggregation time step $b=3$ and in all following disaggregation steps down to 1 h resolution $b=2$. The cascade-model is micro-canonical, so the rainfall amount of each time step is conserved exactly. A re-aggregation of the disaggregated time series yield the observed time series used for the disaggregation. Since the focus of this investigation is not on the disaggregation itself,the interested
25 reader is referred to Müller and Haberlandt (2015) for a more detailed explanation,. However, the main results are a slight underestimation of dry spell duration (relative error of -6 %), fraction of dry intervals (-3 %), wet spell duration (-12 %) and

amount (-9 %), while average intensity is slightly overestimated (4 %). While the autocorrelation function also shows underestimations, the extreme values are well represented.
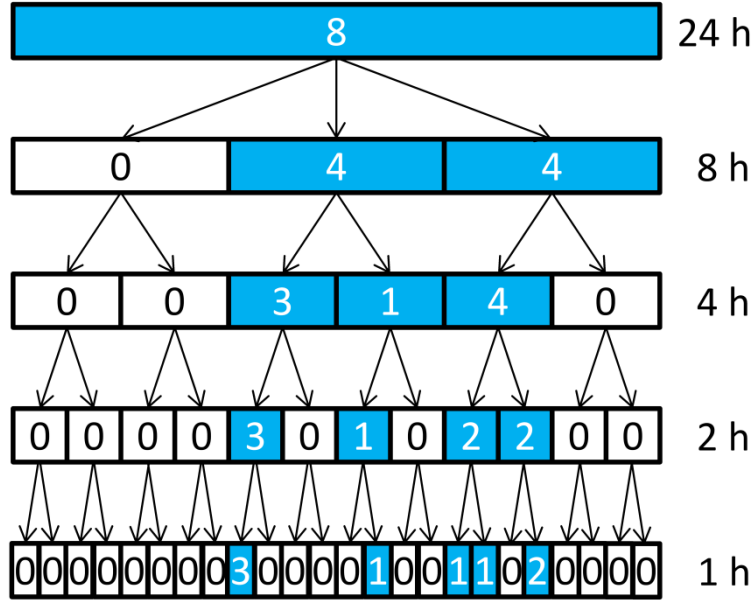
Fig. 3. General disaggregation scheme of the applied multiplicative cascade model (values inside the boxes represent rainfall amount, blue or white box color indicates wet or dry time steps, respectively)

b) Bivariate characteristics

For the definition of spatial consistence applied in this study the bivariate rainfall characteristics are following the ones used by Haberlandt (2008) and are briefly described in the following:

The probability of occurrence $P_{k,l}$ describes the probability of rainfall occurrence at the same time at two stations k and l:

$$P_{k,l}\left(z_k > 0 \mid z_l > 0\right) \approx \frac{n_{11}}{n} \quad , \tag{1}$$

where n is the total number of non-missing observation hours at both stations, z_i is the rainfall intensity and the number of simultaneous rainfall occurrence at both stations is represented by n_{11}.

The Pearson's coefficient of correlation ρ describes the relationship between simultaneously occurring rainfall at two stations k and l as a measure of the linear relation between both rainfall time series (Eq. (2)). Breinl et al. (2014) used this coefficient before for multisite rainfall generation:

$$\rho_{k,l} = \frac{cov(z_k, z_l)}{\sqrt{var(z_k) \times var(z_l)}}, \ z_k > 0, z_l > 0 \quad . \tag{2}$$

Müller and Haberlandt (2015) found an intensity-dependency for Pearson's coefficient of correlation and distinguished between $\rho(k \leq 4\ mm)$ and $\rho(k > 4\ mm)$, which is adopted here.

The continuity ratio $C_{k,l}$ compares the expected rainfall amount at one station for times with and without rain at the neighboring station ($E.$ is the expectation operator):

5    $$C_{k,l} = \frac{E(z_k|z_k>0, z_l=0)}{E(z_k|z_k>0, z_l>0)} \tag{3}$$

These characteristics are distance-dependent and prescribed values can be estimated as functions of the separation distance between two stations from observed data (see regression lines in Fig. 4 for each characteristic).

c) Implementation of spatial consistence

10   As mentioned before, the disaggregation of single time series is a point-process with no surrounding stations taken into account. Input rainfall products for the rainfall-runoff models consisting of just the disaggregated time series without subsequent steps to implement spatial consistence are referred to as V1 (no implementation of spatial consistence). Two methods for the implementation of spatial consistence and resulting in the rainfall products V2 and V3, are applied in this investigation.

15   The first method, resulting in V2, is based on simulated annealing (Aarts and Korst, 1965, Kirkpatrick et al., 1983), a non-linear optimization method from the group of resampling algorithms. The aim of simulated annealing is to modify the disaggregated time series and in doing so minimizing an objective function including the deviations between the observed bivariate rainfall characteristics and those from the disaggregated time series.Relative diurnal cycles are swapped without changing the structure of the time series or the absolute daily totals of rainfall amounts.The interested reader is referred to

20   Müller and Haberlandt (2015) for further details.

The second method, resulting in rainfall product V3, is a more pragmatic solution. It was introduced by Haberlandt and Radtke (2014) and is also based on the already disaggregated time series of V1. For each day, the station with the highest rainfall amount is identified. The relative diurnal cycle of this station is transferred to all other stations for this day. This parallelization is carried out for all days of the disaggregated time series. The varying diurnal distributions of rainfall at each

25   station without spatial patterns, leading to an underestimation of spatial consistence, is instead transformed to a simultaneous occurrence of rainfall at all stations with an overestimation of spatial consistence.

Both methods are compared against using the disaggregated time series without any subsequent steps. For analyzes and discussion of the impacts of these methods, the designations listed in the summarizing Table 4 are used.

Table 4. Short characterization of the three rainfall products

Starting point	Subsequent step	Rainfall occurence at different stations	Designation
Disaggregated	none	Random	V1
time series	Resampling	Intersecting	V2

3.2 Hydrological Models

For analyzing the impact of rainfall products with different spatial consistencies, two models, HBV-IWW (Wallner et al., 2013) and WaSiM (Schulla, 1997, 2015), are used. All simulations are carried out continuously. This enables the derivation

5 of flood frequency analyzes and avoids uncertainties from unknown initial conditions resulting from event-based modeling (Pathiraja et al., 2016). Additionally, an initial phase of one year is used as a spin-up period to achieve plausible initial conditions for all storages.

a) HBV-IWW including calibration procedure

The HBV-IWW model is based on the HBV model that was originally developed at the Swedish Meteorological and

10 Hydrological Institute (SMHI) in early 1970s (SMHI, 2008) and was modified by Wallner et al. (2013). HBV-IWW, for simplification titled HBV, is a conceptual model, where runoff generation and runoff transformation are represented by simple relationships between storage and effective precipitation, respectively runoff (see flow chart of the model in the supplementary material S1). For the spatial discretization of the study areas subcatchments (see Fig. 2) with an approx. area of 20 km² are applied. It could be questioned, if a rainfall-runoff model with subcatchments is useful for the validation of the

15 spatial consistence of rainfall. A daily station covers an area of 65 km² on average in Germany (Müller, 2016). This spatial resolution is not increased by the cascade model in this study, since only a temporal disaggregation is applied. Also, no additional information is gained by a model with higher spatial resolution. So the only disadvantage could be sort of numerical diffusion due to the spatial resolution. However, since subcatchments of this size are used throughout a number of studies, the HBV with this spatial resolution represents the state-of-the-art and is applied for the actual investigation.

20 For the estimation of the areal rainfall of each subcatchment, a two-step approach was chosen. First, rainfall is interpolated with a Nearest-Neighborhood approach on a raster basis with cell widths of 1 km. In the second step, areal rainfall for each subcatchment is calculated by an arithmetic mean of all raster cells within the subcatchment. If the areal rainfall of a subcatchment is dominated by one station, it could be questioned if areal rainfall intensities should be reduced (by e.g. areal reduction factors (Sivapalan and Blöschl, 1998, Veneziano and Langousis, 2005, Wright et al., 2013)) to avoid an

25 overestimation (e.g. Peleg et al., 2018). Since also underestimations occur in the continuous simulation if this station was not in the center of the storm, no areal reduction was carried out.

Snow accumulation and melt is based by a threshold temperature and the degree day method. After the snow storage, all precipitation and snow melt is entering the soil storage where actual evaporation is considered. Depending on the state of the soil storage, water is released to the upper groundwater layer from where surface runoff and interflow can occur. Both are

30 controlled by a storage coefficient. Water from the upper groundwater layer can also percolate to the lower groundwater layer. The outflow from the latter is representing the baseflow component. Surface runoff, interflow and baseflow are finally

summarized and transformed via a triangular unit hydrograph. River routing is carried out via the Muskingum method. Further details about the model parameters can be found in Wallner et al. (2013) and in the supplementary material S2.

For the calibration, the following runoff statistics are used: quantiles of the distribution functions fitted to the extreme values of i) summer (Extr-Su, May to October) and ii) winter (Extr-Wi, November to April), iii) quantiles of the flow duration

5 curve (FDC), and iv) monthly averages (Q-mon). The calibration is carried out for each rainfall product separately, but for all 10 realizations.at the same time (resulting in one parameter set for 10 realizations) The calibration procedure is also illustrated the supplementary material S1..

For Extr-Su and Extr-Wi, a two-parametric Gumbel-distribution is fitted to the annual series of extreme values. L-moments are used for parameter estimation to reduce the sensitivity against outliers (Hosking and Wallis, 1997). Although extreme

10 values occur only in a few time steps, their reproduction in the discharge time series is the main aim of the simulation on an hourly basis. However, since the extreme values represent only a small fraction of the discharge time series, also FDC and Q-mon are used to represent the more frequent discharge values. Q-mon accounts for the temporal dependency on the inter-annual variation of the discharge. As mentioned before, the analyzes of FDC and Q-mon allows no direct validation of the rainfall products, but enables an overall plausible simulation of rainfall-runoff processes. Hence, FDC and Q-mon are

15 calculated from averaged daily discharge values in order to reduce computation time.

For the goodness-of-fit analyzes of simulated (Sim) and observed (Obs) statistics, the Nash-Sutcliffe-efficiency NSE (Nash and Sutcliffe, 1970) is used. A perfect fit would result in *NSE=1*, while assuming the average of the observed data for all time steps would result in *NSE=0*. The equation for the *NSE* is given in Eq. 4 and the corresponding quantiles for Extr-Su, Extr-Wi and FDC and months for the Q-mon, respectively, are given in Eq. 5.

20 $$NSE = 1 - \frac{\sum_{t=1}^{n}(Q_{Obs}(t) - Q_{Sim}(t))^2}{\sum_{t=1}^{n}(Q_{Obs}(t) - \overline{Q_{Obs}})^2} \tag{4}$$

$$t = \begin{cases} \{0.05, 0.25, 0.5, 0.75, 0.95, 0.975\} & for\ FDC \\ \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\} & for\ Q - mon \\ \{0.2, 0.5, 0.8, 0.9, 0.95, 0.98, 0.99\} & for\ Extr - Su\ and\ Extr - Wi \end{cases} \tag{5}$$

The goodness-of-fit of all runoff statistics are summarized in the objective function O_{stat}, which should be minimized during the calibration:

$$O_{stat} = 1 - (0.275 \cdot NSE_{Extr-Su} + 0.275 \cdot NSE_{Extr-Wi} + 0.2 \cdot NSE_{FDC} + 0.25 \cdot NSE_{Q-mon}) \tag{6}$$

25 For the optimization simulated annealing is used. The parameters modified during the optimization with the corresponding ranges are given in the supplementary material S2.. The periods for calibration and validation are listed in Table 6 for each catchment.

Table 6. Calibration and validation period for all catchments

Gauge	Calibration period		Validation period	
	Start	End	Start	End

Pionierbrücke	01.11.1952	31.10.1977	01.11.1977	31.10.2003
Tetendorf	01.11.1986	31.10.1993	01.11.1993	31.10.2000
Reckershausen	01.11.1974	31.10.1990	01.11.1990	31.10.2006

b) WaSiM

WaSiM (Schulla, 1997, 2015) is a physically based and distributed hydrological model which has been designed to study climate change and land-use change impacts on the water balance and floods in meso-scale catchments (e.g., Niehoff et al.

5 2002, Bormann and Elfert, 2010). WaSiM was formerly known as WaSiM-ETH, but has since been renamed (Schulla, 2015) and hence the new abbreviation is used throughout the manuscript. WaSiM is flexible regarding the resolution of spatial input data. In general, elevation, land-use, and soil data need to be prepared as gridded raster datasets. The spatial resolution of WaSiM applications covers several scales ranging from tens of meters to a few kilometers. For this study a spatial resolution of 150 m x 150 m was chosen.

10 For the areal rainfall estimation a combined Inverse Distance Weight (IDW) and elevation dependent regression approach is applied. This approach does not only account for a horizontal interpolation but also addresses the typically observed increase in precipitation with increasing elevation which proves helpful given that the catchment spans an altitudinal range of several hundred meters.

A set of alternative hydrological process representations for each of the following sub-models is included in the model in

15 order to cover different user needs and meteorological data requirements: (i) evapotranspiration, (ii) snow, (iii) interception, and (iv) soil water. This list is not exhaustive since other processes can be also addressed using the model. Here, only the processes utilized in this study are described. Potential evapotranspiration is computed using the Penman-Monteith approach (e.g., Monteith, 1965) taking into account look-up tables of parameters defined for different land-use classes. Seasonal snow cover dynamics is simulated using a temperature threshold for phase partitioning and a temperature index model for

20 snowmelt calculations. A bucket approach is applied to consider interception of rainwater. The soil water dynamics including actual evapotranspiration, infiltration, lateral outflow (interflow), and percolation is simulated in a numerical scheme which is based on the Richards equation. The lowermost nodes in each grid cell which are subject to saturation represent the groundwater storage in the model. A linear storage approach is applied here to simulate the outflow from the groundwater.

25 Since WaSiM is more complex than HBV with respect to computational needs, a different strategy for model calibration was chosen. As the number of both adjustable parameters and iterations is limited due to limited computational resources, a lexicographical approach was set-up for model calibration (Gelleszun et al., 2015). In this way, the optimization of parameters is divided into subsequent steps that are associated to different processes. In a first step, the parameters of the soil water balance and runoff generation (i.e. recession of hydraulic conductivity along the soil profile and the flow density) have

30 been calibrated through maximizing *NSE*. Then, the baseflow recession is improved through minimizing the root mean

square error *RMSE* of the lowermost part of the flow duration curve (two parameters). Both calibration steps have been performed using hourly meteorological time series and observed discharge time series from the period 2009-2012. As highly resolved meteorological observations are only available from 2000 onwards, an additional calibration step has been carried out using disaggregated rainfall time series in order to better match the long-term water balance characteristics through slightly modifying canopy resistance parameters of the evapotranspiration model. Without these pre-calibration steps an underestimation of the mean discharge and hence the water balance was identified. An incorrect representation of the water balance introduces other uncertainty sources which hence superpose the effects of the different versions of spatial rainfall. However, these pre-calibration was focused only on the water balance itself and not on the objectives used in Eq. (6).

4. Results & Discussion

For the discussion of the results, the section is divided into two parts. The first part deals with the interpretation of the rainfall spatial variability, while the influence on simulated discharges is discussed in the second part.

4.1 Rainfall

For the disaggregation of daily rainfall time series to hourly values, the micro-canonical cascade model of Müller and Haberlandt (2015) is used. This model was previously validated in the beforementioned study for the the Aller-Leine river basin, which is also considered in this study. Since the focus of this investigation is the spatial variability of the generated rainfall, the interested reader is referred to their investigation for a detailed analyzes of point results. In Fig. 4 the bivariate characteristics are shown for V1, V2 and V3 in comparison with the observations for Pionierbrücke (results for the other two catchments are in the supplementary material S3 and S4). For the V1 case (the disaggregated time series without any subsequent steps), the probability of occurrence and the correlation coefficients are underestimated, whereas the continuity ratio is overestimated.

For the V2 case, the probability of occurrence and the correlation coefficients could be improved. While values for the probability of occurrence and correlation coefficient for rainfall intensities > 4 mm are similar to observations, a slight underestimation can be identified for correlation coefficients for rainfall intensities ≤ 4 mm for some station pairs. For the continuity ratio, V2 results are varying. This is due to the definition of the criterion, taking into account station k with respect to station l, but not vice versa. This definition leads to different values for the same station pair, because different time steps are taken into account. Therefore, for $C_{k,l}$ an improvement can be identified during simultaneous worsening of $C_{l,k}$.

It should be noted that the resampling algorithm has not been validated in the context of distances smaller than 20 km and temporal resolution of 1 h. Although the spatial rainfall characteristics are underestimated after the disaggregation (V1), a major improvement can be identified moving all station pairs into the cloud of observations (except some of the continuity ratio).

The simultaneous rainfall of V3 leads to the best values for the continuity ratio, comparable to those from observations. However, slight overestimations can be identified for both coefficients of correlation. For the probability of occurrence, high overestimations can be identified (approximately 50 %). Although the same diurnal cycles are used for all stations, probability of occurrence is less than 1 due to the fact that rainfall does not necessarily occur at all stations on a wet day.
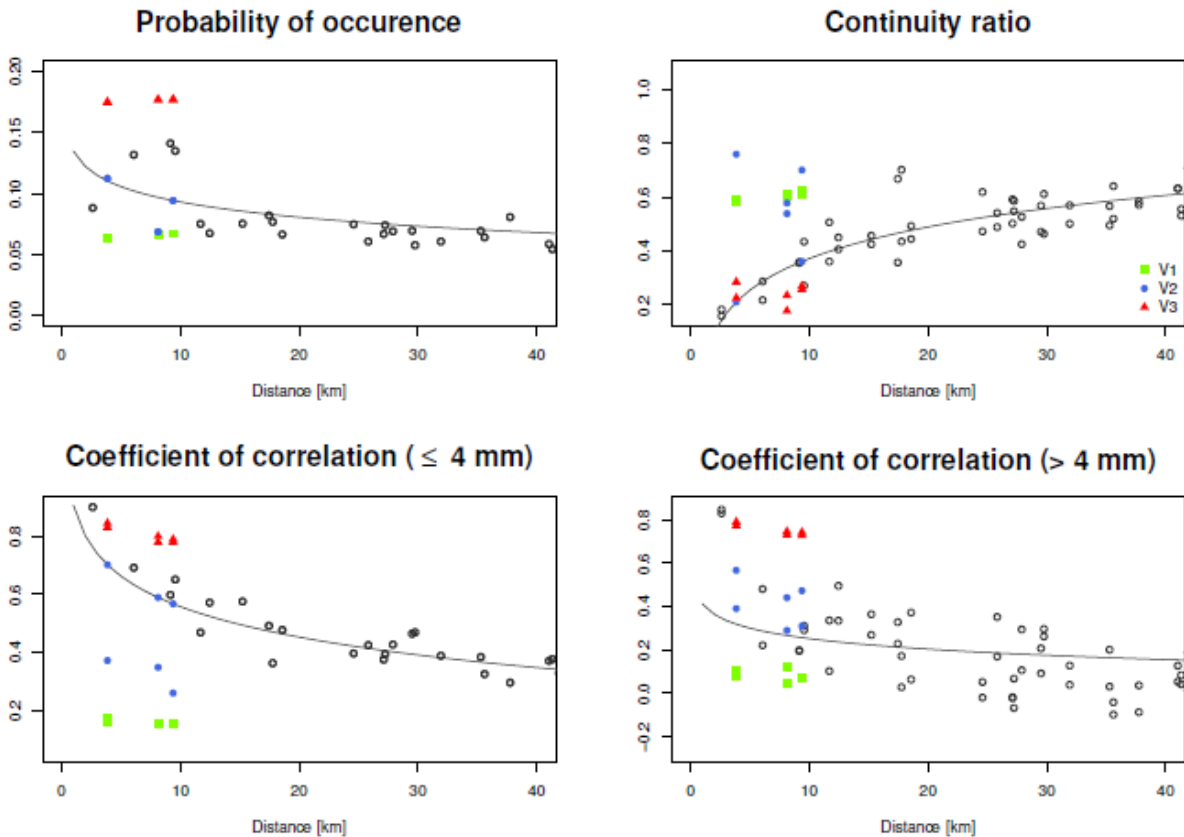
Fig. 4. Bivariate spatial rainfall characteristics of V1, V2 and V3 in comparison to observations for the catchment Pionierbrücke (for one realization, black circles represent observations - for details the reader is referred to Müller and Haberlandt (2015)).

Additionally, the influence of the spatial consistence on resulting areal rainfall intensities is investigated. In the supplementary material S5, areal rainfall intensities resulting from V1, V2 and V3 are shown for one subcatchment of

10   Pionierbrücke. Since only one observed high-resolution time series (Reckershausen: two) is available for each catchment, no comparison between areal rainfall intensities between observed and disaggregated time series (resulting from three stations for each catchment) can be carried out. Areal rainfall intensities resulting from disaggregated time series can only be compared among each other. V1 leads to the lowest rainfall intensities, V3 to the highest. Areal rainfall intensities of V2 lie between V1 and V2. The "random" rainfall occurrence in V1 leads to smaller rainfall intensity values as was indicated by

15   the probability of occurrence (see Fig. 5). Accordingly, the parallelization of V3 leads to the highest areal rainfall intensities.

Therefore, the results for the spatial bivariate characteristics and the areal rainfall intensities are consistent. The findings are similar for the other subcatchments in Tetendorf and Reckershausen.

Additionally, the extreme values of the areal rainfall intensities have been analyzed, since those can have a significant influence on the resulting runoff. In Fig. 5, the annual rainfall extremes for another subcatchment in Pionierbrücke are illustrated using the Weibull-plotting position (similar for all subcatchments). As identified for all areal rainfall intensities, V1 also leads for the extreme values to the lowest values for each return period. V2 and V3 result in similar values for return periods < 18 years. The clear difference of higher values for V3 over the whole spectrum of non-exceedance probability cannot be identified for the extreme values (see S5). Although for V3, where the diurnal cycle of the station with the highest daily rainfall amount is transferred to the time series of all other stations, V3 does not lead to the highest extreme values. The reason for this is that the highest daily rainfall amount does not necessarily lead to the highest rainfall intensity on the final disaggregation level with an hourly time step. As an example, a rainfall station A with a daily total rainfall amount of 50 mm has a maximum intensity during this day of 8 mm/h, whereas station B with a daily total rainfall of 40 mm has a higher maximum intensity of 15 mm/h. As such, V3 can also lead to a smoothing of the rainfall intensities, at least for peak intensities. However, for higher return periods (> 18 years), V3 leads to higher values than V2.
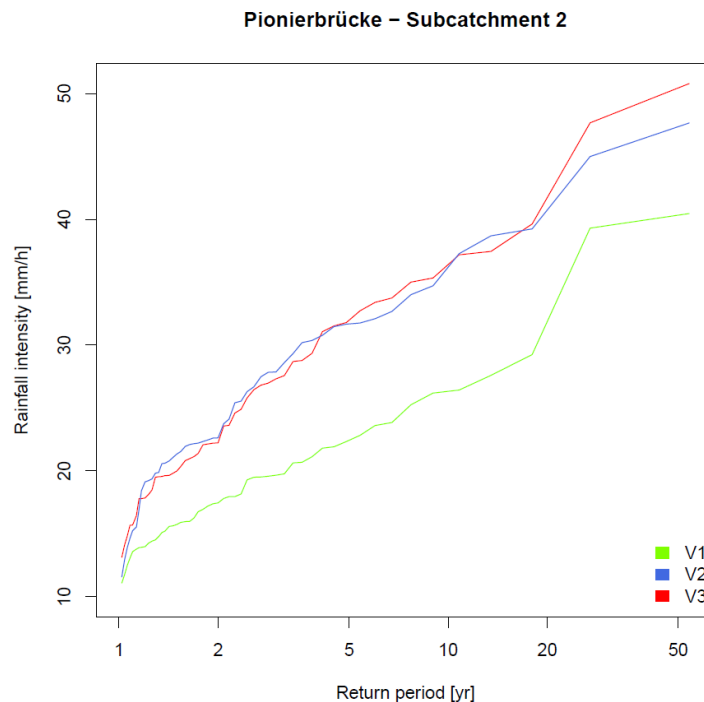
Fig. 5. Annual rainfall extremes of the areal rainfall intensities for subcatchment 2 in Pionierbrücke (for one realization, based on n=53 annual extreme values from 01.11.1950-31.10.2003).

It can be summarized that V1, V2 and V3 lead to different results regarding spatial characteristics and areal rainfall intensities

4.2 Rainfall-runoff-model results

5   In this section, all rainfall-runoff simulation results are presented. The section is organized as follows: in a) the rainfall runoff-model results using HBV are shown for all catchments for V1, V2 and V3 with three rain gauges as input for each. In b) HBV-model results for different station densities for catchment Reckershausen are presented. HBV-model results without parameter calibration are shown for all catchments in c), while WaSiM-model results are presented in d) for catchment Pionierbrücke.

a) HBV- simulation results with calibration using three rain gauges as input

The parameterization was carried out by a split-sampling with a calibration and validation period for each catchment. The results for Reckershausen, Pionierbrücke and Tetendorf are shown in Fig. 6, 8 and 9 for the calibration period. For Reckershausen, only results using three rain gauges as input are shown here. For Extr-Su and Extr-Wi, flood quantiles are

15   shown for a return period of 100 years. However, the extrapolation is limited by the length of the simulated runoff time series. As per Maniak (2005), a maximum return period of three times the runoff time series length should be used to avoid too high statistical uncertainties caused by extrapolation. This results in 75 years for Pionierbrücke, 21 years for Tetendorf and 45 years for Reckershausen. The discussion of the results is limited to those and more frequent return periods. For a quantitative analysis, NSC-values for all criteria and for each catchment are given in Table 8. As mentioned before, NSC-

20   values are based on a few supporting points (see Eq. 5). Also, theoretical Gumbel-distribution functions with two parameters are compared, which can be similar although the population used of each distribution function are different. Hence, values of 0.99 or even 1.00 can be achieved. On the other hand, small deviations from the observations can lead to even negative NSC-values (see e.g. the discussion of the simulation results for Reckershausen).

For Reckershausen, the Extr-Su and Extr-Wi are similar to those from observations (Fig. 6). While for summer all observed

25   flood quantiles are within the range of Extr-Su ($0.99 \leq NSC \leq 1.00$), for Extr-Wi a slight overestimation occurs for V2 and V3.

For the validation period, flood quantiles for both, Extr-Su and Extr-Wi, are overestimated. The overestimation is higher in winter (approx. 20 m³/s for HQ_{50}) than in summer (approx. 10 m³/s). One possible cause can be the higher yearly maximums in the calibration period. It is assumed that parameters, calibrated to achieve high floods, tend to generate larger discharges

30   even if lower yearly maxima are observed. This is also indicated by the results for FDC and Q-mon. Although both are represented well in the calibration period ($0.88 \leq NSC_{FDC} \leq 0.90$, $0.96 \leq NSC_{Q\text{-}mon} \leq 0.99$), both criteria are overestimated in

the validation period ($0.57 \le NSC_{FDC} \le 0.63$, $0.81 \le NSC_{Q-mon} \le 0.89$). In the validation period the range and hence the uncertainty for both, Extr-Su and Extr-Wi, is smaller for V2 and V3 in comparison to V1.

The simulation results of Extr-Su of the validation period for the catchment Reckershausen show the sensitivity of the *NSC* as a goodness-of-fit criterion. V1 and V3 lead to positive *NSC*-values (0.60 and 0.31), while V2 leads to a negative value of *NSC*=-0.05. However, from a visual inspection (see Fig. 7), differences between all three approaches are small and less intense as one might expect from the *NSC*-value itself. The high sensitivity of the *NSC* makes a direct interpretation of its values more difficult (Schaefli and Gupta, 2007, Criss and Winston, 2008). However, for the calibration process, a high sensitivity leads to an improvement of the simulation results.

Values for the objective function are given in Tab. 9. For Reckershausen, the objective function values are very similar for V1, V2 and V3 for both, calibration and validation period. Especially by taking into account that the value for the objective function depends on four *NSC*-values.
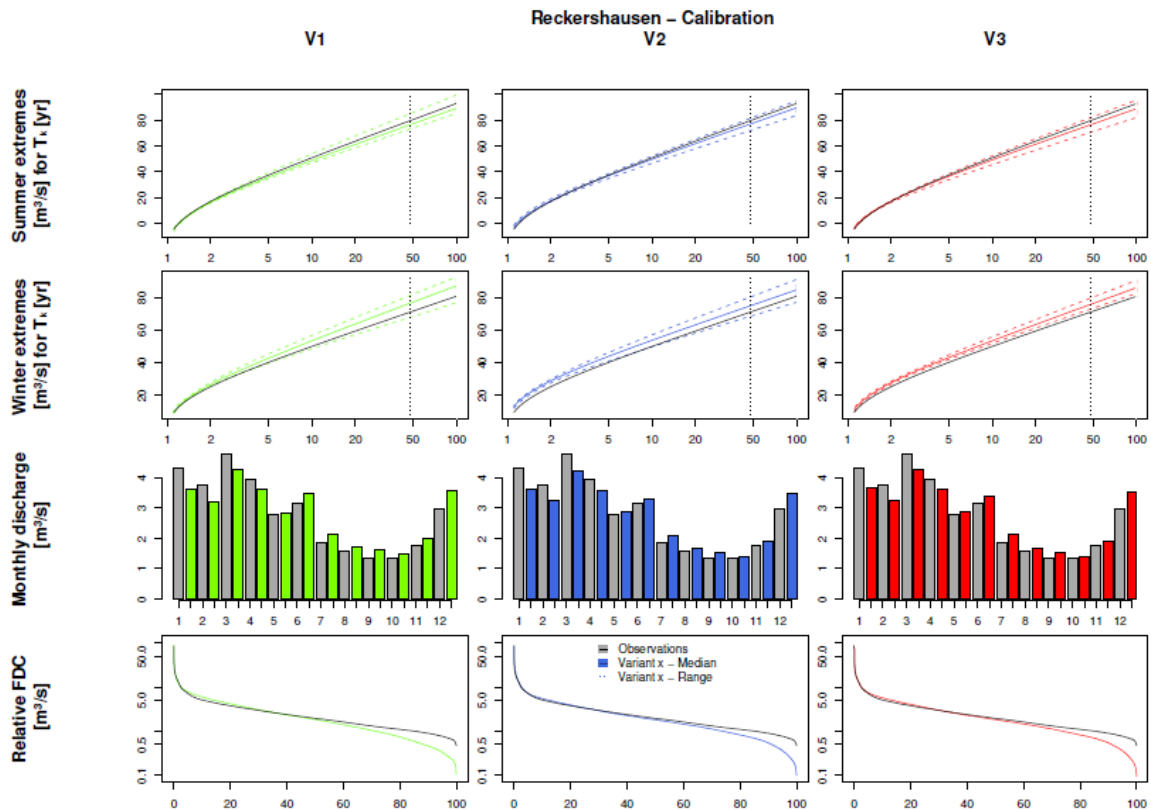
Fig. 6. Runoff simulation results with HBV for Reckershausen, calibration period
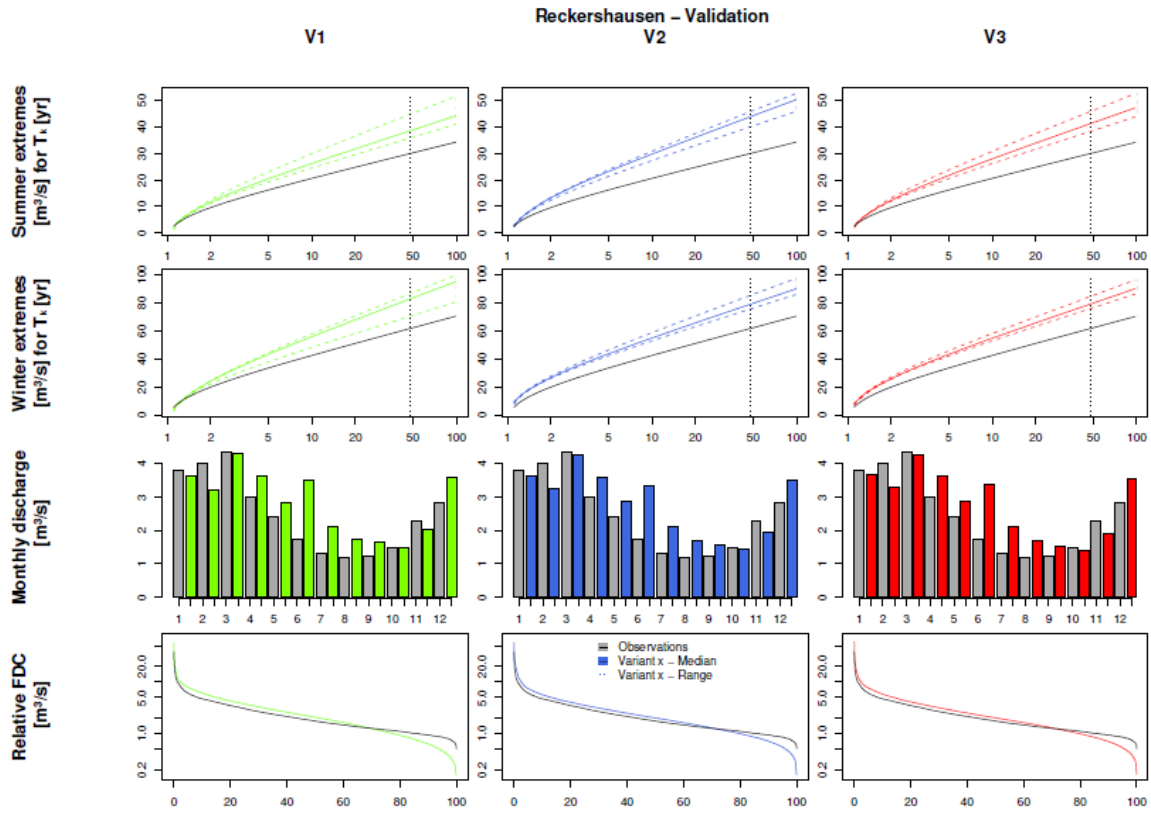
Fig. 7. Runoff simulation results with HBV for Reckershausen, validation period

For Pionierbrücke it should be mentioned that at points during the calibration (see the FDC in Fig. 8) and validation periods a simulated discharge of $Q = 0$ m³/s was obtained. Zero discharge implies that all storages have been emptied. This occurs only for Pionierbrücke and is due to the very steep conditions in the mountainous catchment (see Fig. 1) and hence the low soil depth and storage capacity. In the observed time series the minimum value is $Q = 0.1$ m³/s. The underestimation is as well caused by the selection of criteria selected for the objective function used for calibration. The main aim is to represent the extreme flows, while the shape of the intra-annual cycle of monthly average discharges and of the FDC are only implemented to achieve an overall realistic mean discharge behavior. For the FDC, four quantiles greater than 0.5 and only two quantiles smaller than 0.5 are used. Smaller quantiles are not of interest in these simulations, since discharge values in that range belong to dry periods with low flows, for which daily values of rainfall are sufficient for simulations and hence no rainfall disaggregation would be necessary. For the FDC, V3 leads to a slightly better fit to observations for non-exceedance probabilities smaller than 35 %, but to a worse fit between 35 % and 60 % non-exceedance probability. However, FDC is underestimated, independent from the applied rainfall product, for non-exceedance probabilities higher than 60 %. The

underestimation identified by the FDC can also be identified for Q-mon in winter and in the underestimation of the Extr-Su and Extr-Wi. The results for the validation period are very similar and not shown here.
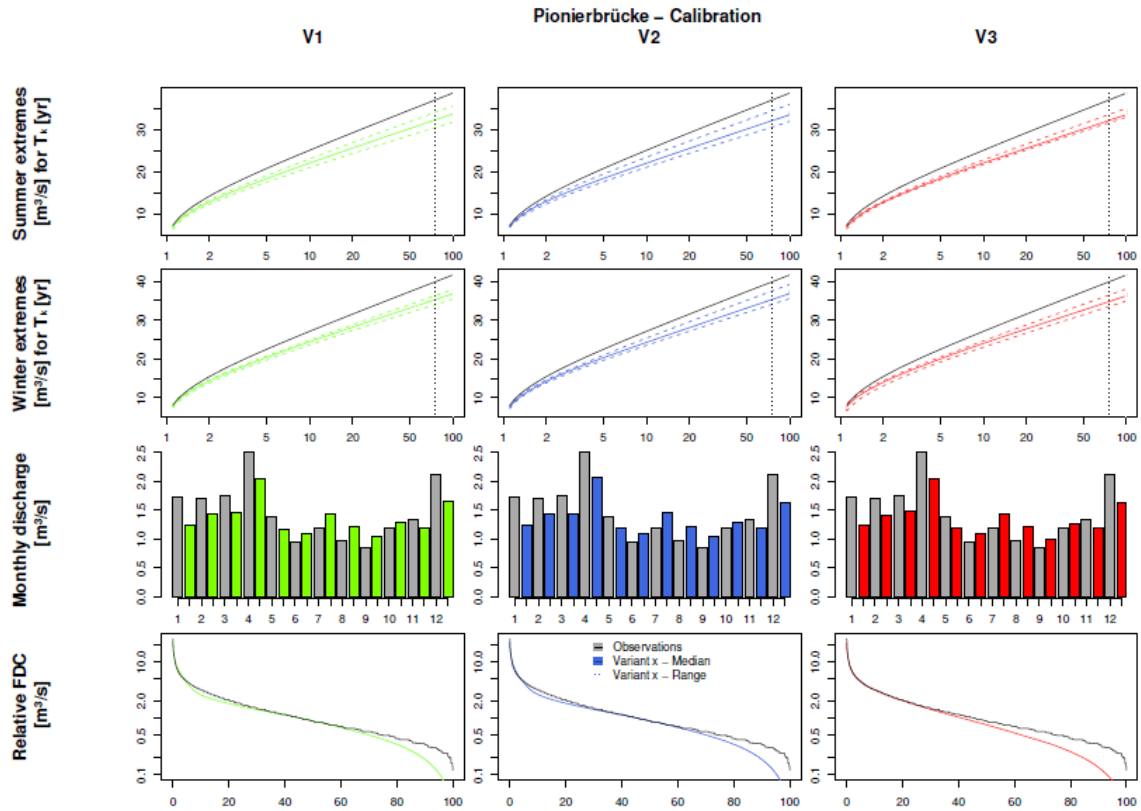
Fig. 8. Runoff simulation results with HBV for Pionierbrücke, calibration period

On the contrary, for Tetendorf FDC and Q-mon (except September and October) are overestimated by all rainfall products (Fig. 9). However, for Q-mon the shape of the intra-annual cycle is well-represented. For the extreme values it should be mentioned again, that the analyzes are only valid for return periods more frequent than 21 years. For Extr-Su, underestimations occur for return periods more frequent than 5 years for all variants in the calibration period (less than 2 years in the validation period). For Extr-Wi, the median of V1 represents the observed values well, while for V2 and V3 the median leads to overestimations for return periods frequent than 5 years. However, observations are still in the range of the simulation results, whereby the range is wider for V1 and V3 in comparison to V2. In total, the resampling in V2 leads to a reduction of the overestimation of the observed summer extreme values, but to a stronger overestimation for winter extremes in comparison to V1 and V3.

Since for Tetendorf seasonal differences regarding V2 were identified, the spatial rainfall characteristics of the objective function applied for the resampling process have been re-analyzed, differing between the summer and winter half years. The results regarding both periods as well as the estimation over the complete year are shown in Fig. 10 for all bivariate spatial rainfall characteristics based on all 24 hourly stations in Lower Saxony that have been used before for the estimation of these

5   characteristics (Müller, 2016). For the continuity ratio, probability of occurrence and both volume classes of correlation coefficients, differences can be identified, based on the different geneses of rainfall in summer and winter. The probability of rainfall occurrence is lower in summer due to a higher amount of convective rainfall events. However, the distance-dependent curve progression is very similar between the seasonal and annual estimated spatial characteristics. Since spatial characteristics are just moved closer to the regression line by V2 (without a perfect fit, see Fig. 4), an improvement of the

10   spatial rainfall characteristics by introducing slightly different season-dependent regression lines cannot be expected and is hence not applied.

As main reasons for the seasonal differences, the short validation and calibration period are considered. Short periods mean a small amount of days with rain and hence a small amount of relative diurnal cycles to swap during the resampling, limiting the ability of the algorithm to improve the spatial characteristics. The usage of time series of V2 as input for HBV and the

15   additional short time for the calibration process lead to the seasonal differences.

For longer calibration and validation periods (Reckershausen and Pionierbrücke) the results for V1, V2 and V3 are very similar regarding the runoff statistics. An influence of the chosen method for the implementation of spatial consistence cannot be recognized.

20   **Table 8.** *NSC-values for all catchments and all criteria for calibration (Cal) and validation (Val) period*

Catchment	Criteria	V1		V2		V3	
		Cal	Val	Cal	Val	Cal	Val
Reckershausen	*Extr-Su*	0.99	0.60	1.00	-0.05	0.99	0.31
	Extr-Wi	0.97	0.43	0.97	0.58	0.97	0.58
	FDC	0.88	0.57	0.90	0.63	0.90	0.61
	Q-mon	0.96	0.81	0.99	0.89	0.98	0.85
Pionierbrücke	*Extr-Su*	0.89	0.95	0.88	0.91	0.89	0.94
	Extr-Wi	0.91	0.88	0.91	0.86	0.89	0.83
	FDC	0.61	0.17	0.61	0.16	0.61	0.17
	Q-mon	0.99	1.00	0.99	1.00	0.99	0.99
Tetendorf	*Extr-Su*	0.32	-0.79	0.68	0.78	0.21	-0.61
	Extr-Wi	0.87	0.70	0.64	-4.36	0.47	0.88
	FDC	0.79	0.82	0.84	0.65	0.71	0.78

| *Q-mon* | 0.86 | 0.93 | 0.78 | 0.92 | 0.83 | 0.92 |
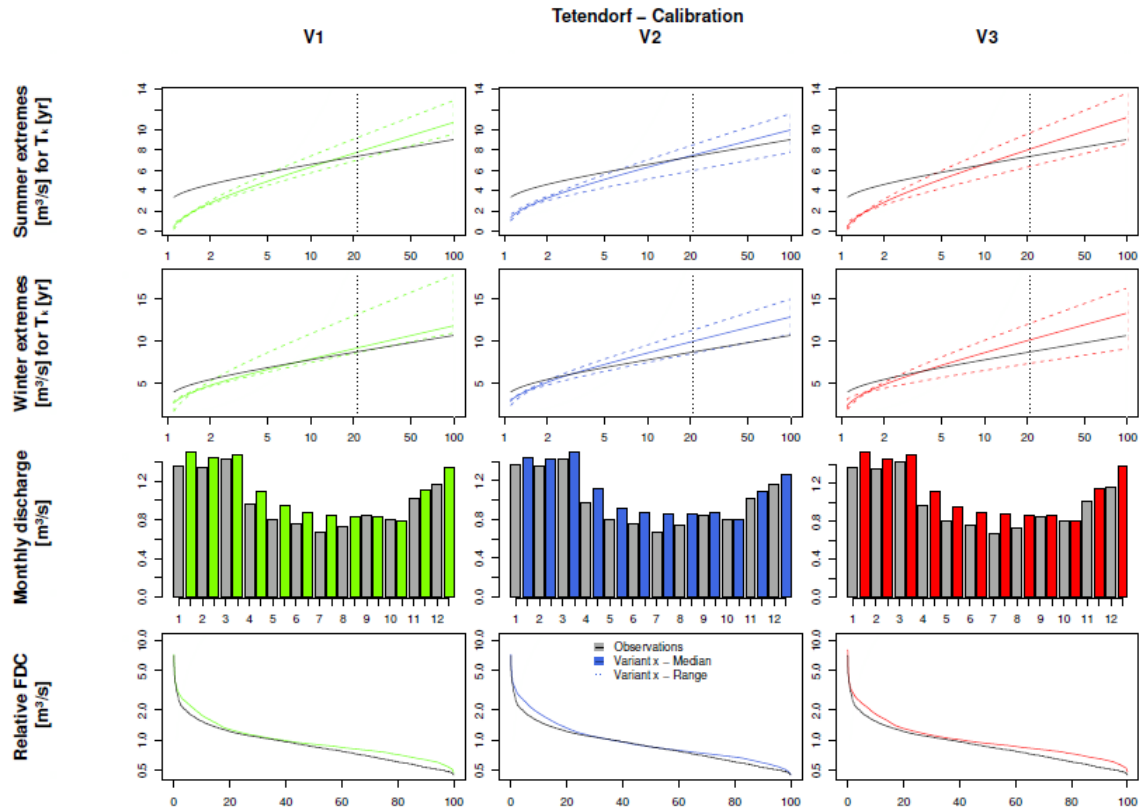
Fig. 9. Runoff simulation results with HBV for Tetendorf, calibration period

Table 9. O_{stat}-values for all catchments and all criteria for calibration (Cal) and validation (Val) period

Catchment	V1		V2		V3	
	Cal	Val	Cal	Val	Cal	Val
Reckershausen	0.04	0.39	0.03	0.48	0.03	0.40
Pionierbrücke	0.13	0.21	0.13	0.23	0.14	0.23
Tetendorf	0.29	0.58	0.27	1.49	0.44	0.50
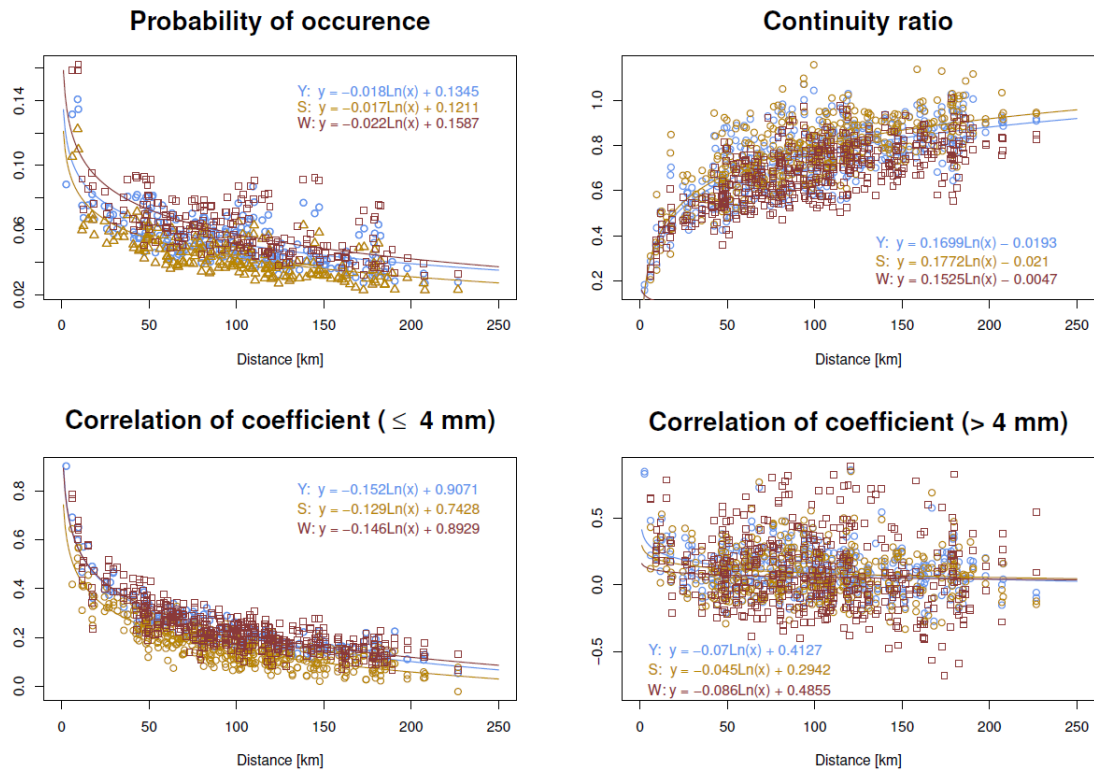
Fig. 10. Bivariate spatial characteristics estimated for summer (S) and winter (W) seasonal as well as over the whole year (Y)

b) HBV- simulation results calibration using different numbers of rain gauges as input

A possible reason for the non-visible influence of the chosen method for the implementation of spatial consistence in the simulated runoff statistics is the low rain gauge network density. With a low network density, it is not possible to reflect the spatial rainfall variability and hence the influence of V1, V2 and V3 cannot be identified. The influence of the spatial rainfall variability on the runoff can only be determined by rainfall-runoff simulations.

Therefore, for Reckershausen, different numbers of rain gauges are applied for the calculation of the areal rainfall used as input for HBV. Areal rainfall is estimated by 3 rain gauges (representing a network density of 0.9 gauges per 100 km²) as carried out in a), 5 (1.6 gauges/100 km²) and 8 rain gauges (2.5 gauges/100 km²). The results are shown for V2 in Fig. 11 for the calibration and in Fig. 13. for the validation period. The results for V1 and V3 are very similar and not shown here. However, for a quantitative analysis the *NSC*- and O_{stat}-values are shown in Table 10 and Table 11.
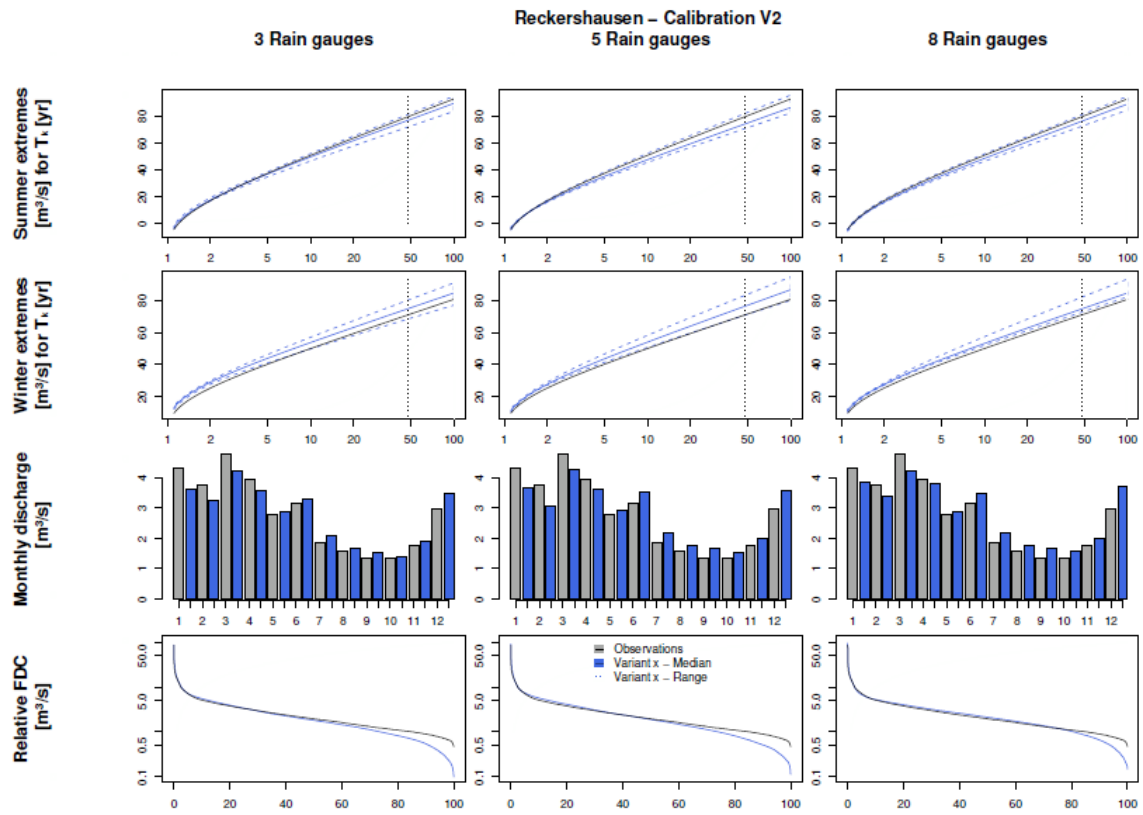
Fig. 11. Runoff simulation results for V2 with 3, 5 and 8 rain gauges with HBV for Reckershausen, calibration period
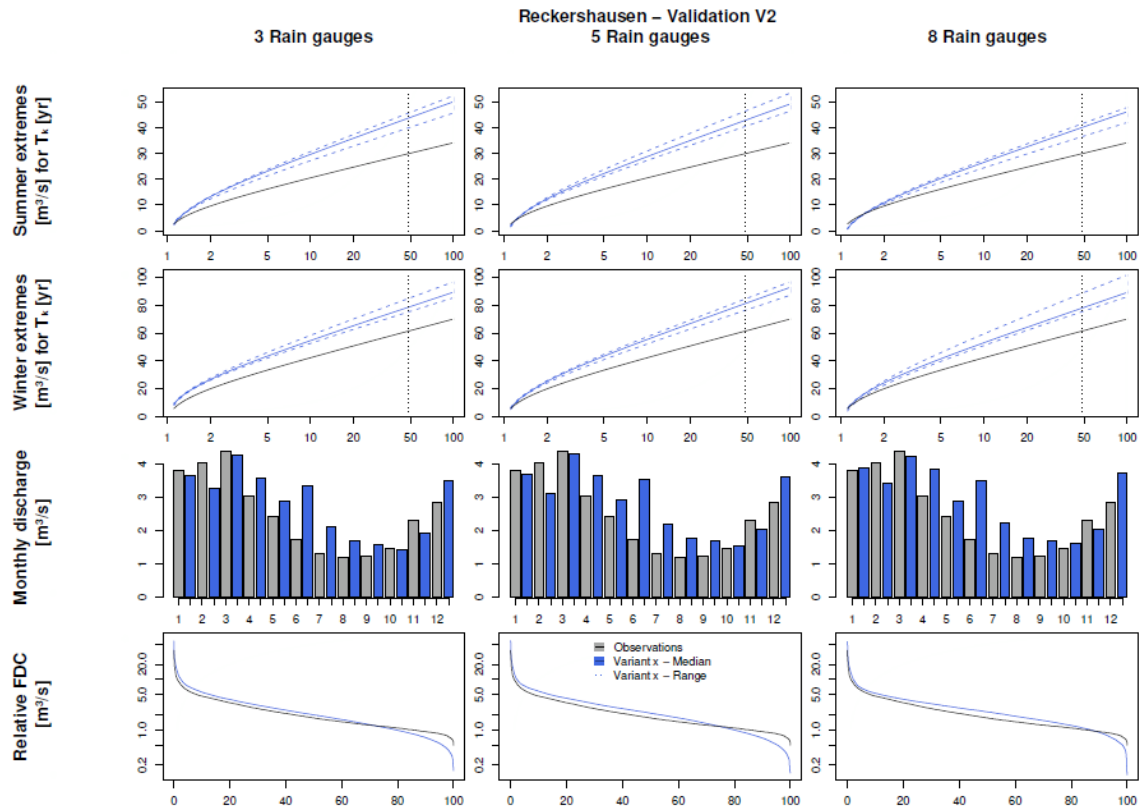
Fig. 12. Runoff simulation results for V2 with 3, 5 and 8 rain gauges with HBV for Reckershausen, validation period

Again, independent of the number of rain gauges used for the estimation of the areal rainfall, the results from the calibration period (Fig.11) represent the observations better than those from the validation period (Fig. 12). In the validation period, Extr-Su and Extr-Wi are overestimated as well as the majority of Q-mon and the FDC. Minor differences can be identified between the different rain gauge network densities, but no general conclusion is possible, e.g. the overestimation of Extr-Wi in the calibration period is increasing with an increasing network density. However, in the validation period the overestimation is decreasing with an increasing number of rain gauges from 3 to 8. Also for Q-mon or the FDC, no systematic improvement can be identified. This is an unexpected finding, because with the additional information from the daily total rainfall amounts, an improvement of at least the continuum characteristics was expected. Also for the *NSC-* and O_{stat}-values no systematical improvement can be identified: O_{stat}(V2, 3 rain gauges)= 0.03, O_{stat}(V2, 5 rain gauges)= 0.04, O_{stat}(V2, 8 rain gauges)= 0.03 (see Table 10 and Table 11).

It can be summarized, that the number of rain gauges has only a minor, but no systematic influence on runoff statistics for the catchments used in this investigation. This contradicts conclusions from other studies. Seliga et al. (1992) recommend for spatial rainfall applications information every 5 km² (20 rain gauges/ 100 km²). So an improvement by an increasing station

density up to this threshold should have been expected. For a French catchment with an area size of 71 km², Obled et al. (1994) investigated the influence of using 5 or 21 rain gauges, representing rain gauge network densities of 7 and 22 rain gauges/100 km². With 21 rain gauges Obled et al. improved their results significantly. Nevertheless, they conclude that the improvement is based on the better estimation of the total rainfall amount, not on its spatial distribution. Xu et al. (2013)

5 investigated the influence of station density on a Chinese catchment with an area size of 94 660 km² and daily rainfall time series, hence a direct comparison of network densities is not possible. Nevertheless, they point out that the distribution of rain gauges inside the catchment is of importance. A distribution covering regions with different rainfall behaviors in a catchment can lead to better simulation results with only a few rain gauges in comparison to a less efficiently distributed network with more rain gauges. In the actual study, the rain gauges for each network density scenario have been selected in a

10 way to cover the catchment area and its rainfall representatively (see Fig. 2). This could be one reason why an increase in rain gauge network density shows no systematic improvement in this study.

Table 10. *NSC*-values for all catchments and all criteria for calibration (Cal) and validation (Val) period

Number of rain gauges	Criteria	V1		V2		V3	
		Cal	Val	Cal	Val	Cal	Val
3	Extr-Su	0.99	0.6	1	-0.05	0.99	0.31
	Extr-Wi	0.97	0.43	0.97	0.58	0.97	0.58
	FDC	0.88	0.57	0.9	0.63	0.9	0.61
	Q-mon	0.96	0.81	0.99	0.89	0.98	0.85
5	Extr-Su	0.98	-0.24	0.98	0.09	0.99	-0.23
	Extr-Wi	0.97	0.68	0.96	0.48	0.98	0.65
	FDC	0.86	0.53	0.87	0.53	0.86	0.55
	Q-mon	0.99	0.91	0.98	0.86	0.99	0.91
8	Extr-Su	0.99	0.75	0.99	0.46	1	0.54
	Extr-Wi	0.96	0.62	0.98	0.64	0.97	0.59
	FDC	0.91	0.57	0.89	0.54	0.89	0.6
	Q-mon	0.99	0.88	0.99	0.94	0.98	0.88

Table 11. O_{stat}-values for all catchments and all criteria for calibration (Cal) and validation (Val) period

Number of rain gauges	V1		V2		V3	
	Cal	Val	Cal	Val	Cal	Val
3	0.04	0.39	0.03	0.48	0.03	0.40
5	0.05	0.51	0.04	0.49	0.04	0.51
8	0.04	0.28	0.03	0.34	0.04	0.33

c1) HBV-simulation results without calibration using three rain gauges as input

Another possible reason for the small differences between V1, V2 and V3 is the calibration of the rainfall-runoff model parameters for each of the rainfall products. Parameters are allowed to vary between V1, V2 and V3, and hence damp the

5 effects of the different degrees of spatial consistence. To exclude the calibration as a possible reason for the damping behavior, a calibration with a neutral rainfall product offering the same spatial rainfall coverage without giving preference to one of the investigated versions would be recommended. This would enable a direct comparison between V1, V2 and V3 without re-calibration of the models. Since high-resolution time series do not exist with the required spatial network density, radar data could be a possible solution. However, radar time series exist only for lengths which are too short for model

10 simulations and subsequent derived flood frequency analyses.

To avoid re-calibrations, a pragmatic solution is chosen. The arithmetic means of the lower and upper limit for each parameter in Table 5 have been applied as a neutral parameter set. For the validation period simulation results based on this neutral parameter set have been analyzed. Although a splitting in calibration and validation period is not necessary if no calibration is carried out, comparisons are possible between the simulation results with and without calibrated parameters.

15 The results are shown in Fig. 13 for Reckershausen, results are similar for Pionerbrücke and Tetendorf. For a quantitative evaluation *NSC*-values for all catchments are provided in the supplement material S6 and O_{stat}-values in S7.

For Pionierbrücke and Tetendorf simulation results are worse without calibration (e.g. for Pionierbrücke, V1: $O_{stat,not\ calibrated}$=1.14 and $O_{stat,calibrated}$=0.21). For Reckershausen a slight improvement can be identified without calibration. The calibrated parameters led in the validation period to an overestimation of extreme values for both seasons as well as an

20 overestimation of FDC and Q-mon (e.g. for V3: $O_{stat,not\ calibrated}$=0.28 and $O_{stat,calibrated}$=0.40). For all catchments, Extr-Su are underestimated by every version of spatial consistence. The Extr-Wi are also underestimated for Reckershausen and Pionierbrücke, but overestimated for Tetendorf. For all catchments, an intra-annual cycle of Q-mon can be identified. For Reckershausen, Q-mon is similar to observations, while for Pionierbrücke underestimations and for Tetendorf overestimations can be identified in winter. The FDC is not represented well for any of the catchments.

25 Although a neutral set of parameters has been applied, the differences in the simulation results between V1, V2 and V3 are still small. For Pionierbrücke the values of the objective function show the same range without and with calibration (1.10 (V2)$\leq O_{stat,not\ calibrated}\leq$1.14 (V1) respectively 0.21 (V1)$\leq O_{stat,calibrated}\leq$0.23(V2, V3)). The similarity of the simulation results exists even if the model parameters are not calibrated and a neutral parameter set is used.
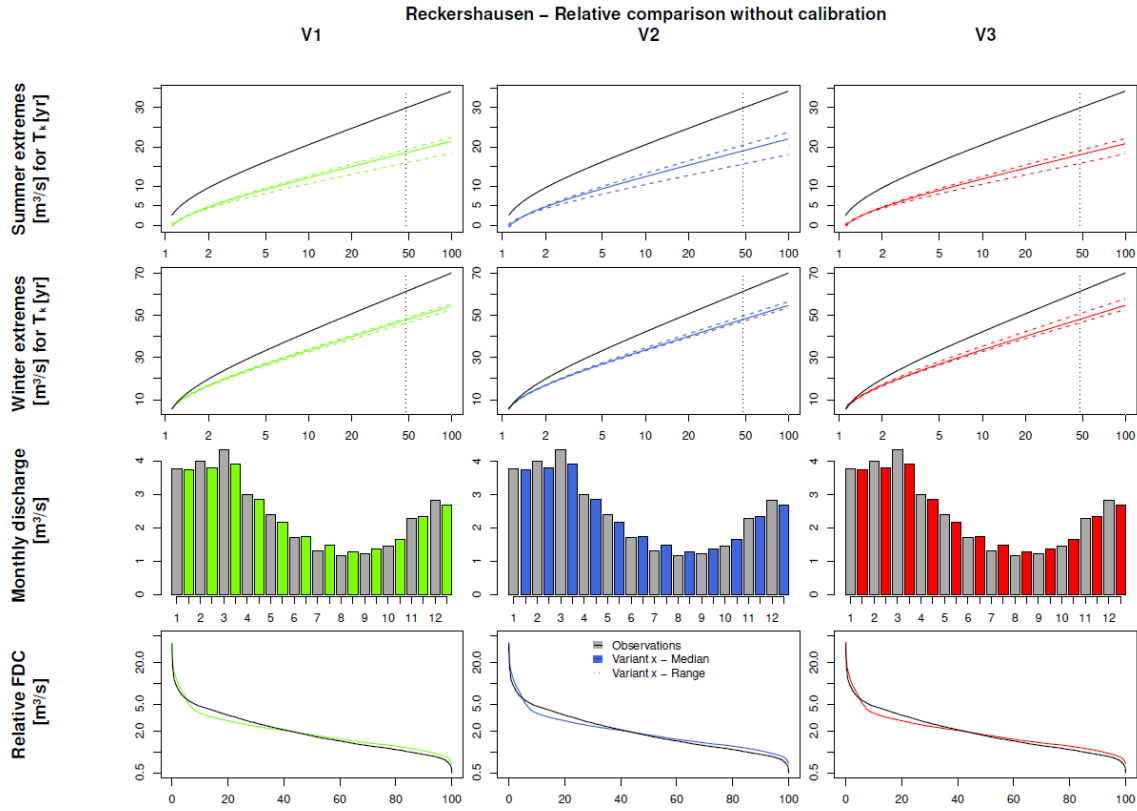
Fig. 13. Runoff simulation results with HBV without calibration for Reckershausen, validation period

c2)   WaSiM- simulation results without calibration using three rain gauges as input

5   For the comparison of V1, V2 and V3, WaSiM (Schulla, 1997, 2015) is used as an additional rainfall-runoff model. The application of more than one model increases the reliability of the simulation results and excludes the possibility of being model-dependent. As far as possible, the same parameter values as in HBV in the uncalibrated case (c1) have been applied. The investigation with WaSiM is carried out only for catchment Pionierbrücke, since here the highest differences in simulation results are expected due to the short reaction time of the catchment.

10 The results are shown in Fig. 14 for the calibration period, Fig. 15 for the validation period and a quantitative analysis is given in Table 12. For the calibration and the validation period Extr-Su and Extr-Wi are simulated slightly higher with V2 and V3 in comparison to V1. This is consistent with the areal rainfall extremes presented for Pionierbrücke in Fig. 5. In addition, the range for both criteria is higher for V2 and V3 in comparison to V1, whereby V2 leads to even wider ranges than V3 in some cases (e.g. Extr-Win the validation period). In this context it should be repeated, that a relative comparison

is carried out and under- or overestimations are not points of interest. The *NSE*-values for both Extr-Su and Extr-Wi are very similar for V2 and V3 (e.g. $NSC_{Extr-Wi,Cal,V2}$=0.98and $NSC_{Extr-Wi,Cal,V3}$=0.99), but show differences to V1 ($NSC_{Extr-Wi,Cal,V1}$=0.90). Hence, in WaSiM a slight effect of the spatial consistence of rainfall is visible from the simulation results. Possible reasons for the differences are the spatial resolution (150 m x 150 m for each raster cell). However, for FDC and Q_{mon}, values for V1, V2 and V3 are again very similar. While for the calibration period the O_{stat}-values are similar for all rainfall products, in the validation period the O_{stat}-values for V2 and V3 ($O_{stat, Val, V2}$=0.45 and $O_{stat, Val, V3}$=0.46) are much closer to each other than to V1 ($O_{stat, Val, V1}$=0.30).

Table 12. *NSC*- and O_{stat}-values for Pionierbrücke without parameter calibration using WaSiM

Criteria	V1		V2		V3	
	Cal	Val	Cal	Val	Cal	Val
Extr-Su	0.95	0.96	0.97	0.95	0.96	0.95
Extr-Wi	0.90	0.77	0.98	0.21	0.99	0.26
FDC	0.86	-0.15	0.87	-0.20	0.88	-0.27
Q-mon	0.99	0.99	0.99	0.99	1.00	0.99
O_{stat}	0.07	0.30	0.04	0.45	0.04	0.46
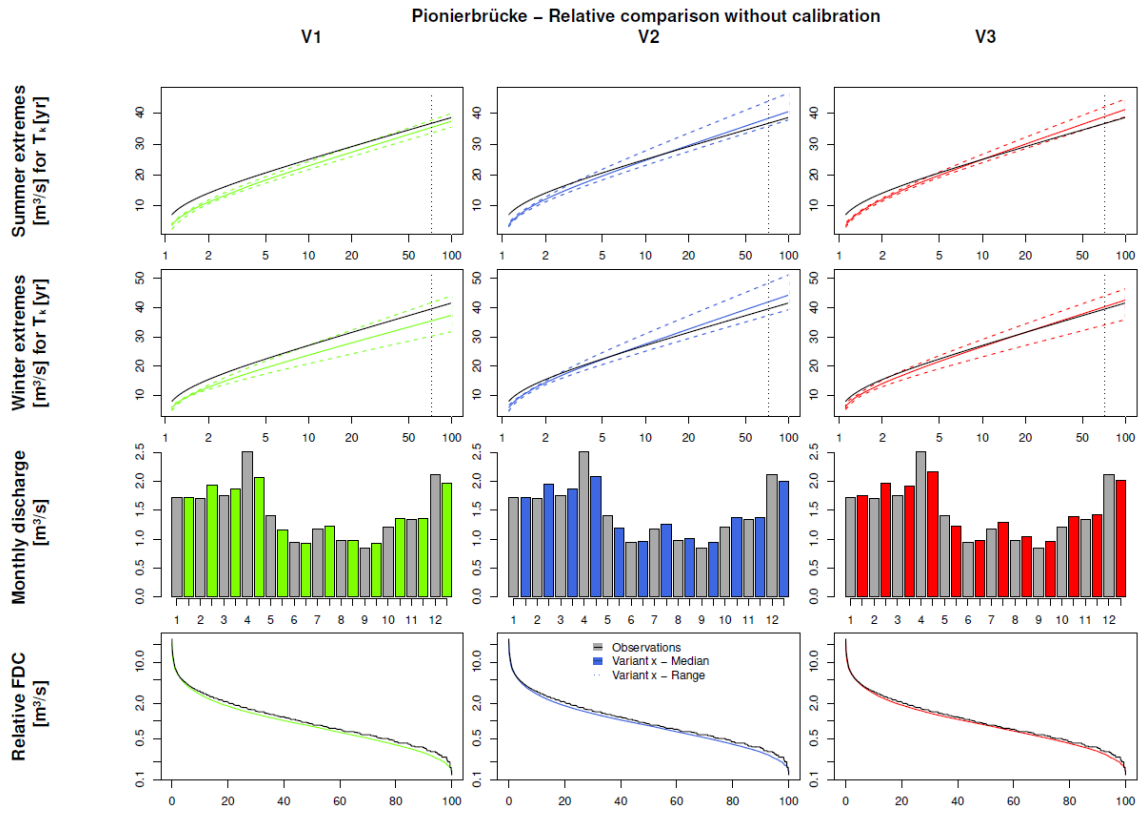
Fig. 14. Runoff simulation results with WaSiM without calibration for Pionierbrücke, calibration period
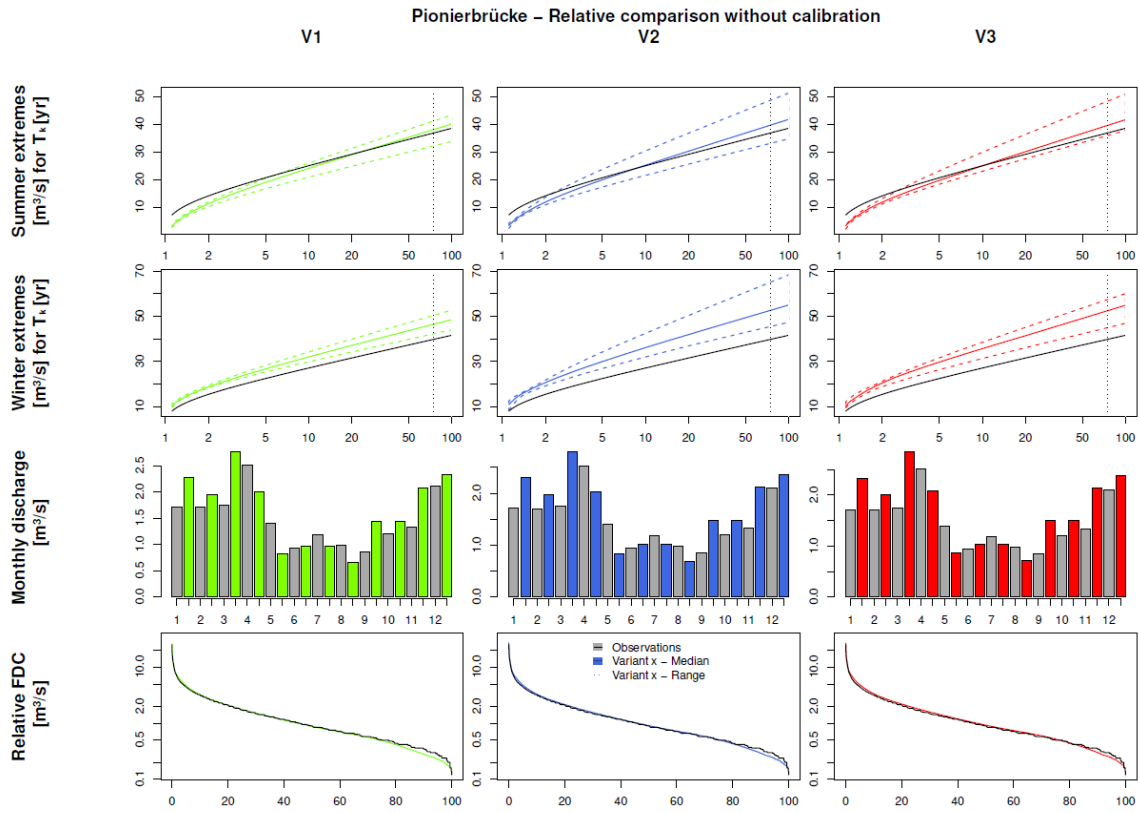
Fig. 15. Runoff simulation results with WaSiM without calibration for Pionierbrücke, validation period

5. Discussion of rainfall-runoff simulation results

The rainfall-runoff simulation results with HBV after calibration of the parameters show that with all three rainfall products, V1, V2 and V3, the Extr-Su and Extr-Wi, the FDC, and Q-mon can be represented with a comparable quality. The differences between the three methods are very small for the majority of all cases. Possible reasons for these small differences, which are discussed below, are:

- small differences between the three rainfall products
- dampening of those differences by the calibration of the rainfall-runoff model parameters
- dampening behavior of the catchments
- choice of the rainfall-runoff model and its ability to represent differences of the three rainfall products

Small differences between V1, V2 and V3 would lead to small differences in rainfall-runoff simulation results. However, the differences between the three methods are apparent. For the bivariate spatial characteristics (Fig. 4), the areal rainfall intensities (see S5) and the areal rainfall extremes (Fig. 5), differences can be identified among all three methods, which should as well be reflected by the runoff statistics results.

Another cause can be the separate calibration of the rainfall-runoff model parameters for each method. The applied calibration strategy has the capability to harmonize the different rainfall products with the runoff statistics used for calibration. For the discussion of this harmonization effect, the simulation results for Reckershausen during the calibration (Fig. 11) and validation periods (Fig. 12) are used. During the calibration period, higher values for Extr-Su and Extr-Wi can be found in the observed runoff data. Hence, the parameters calibrated in this period tend to lead to higher runoff values. This is proven by the simulation results of the validation period with an overestimation of all runoff statistics. Only by the usage of an uncalibrated parameter set the calibration can be excluded from the list of possible causes.

The dampening behavior of the investigated catchments depends on the size and the concentration time of a catchment (Andres-Domenech et al., 2015). Also, catchments act as a filter, so that rainfall as an input signal is dampened during its transformation to runoff by several processes (e.g. interception, losses due to storage filling, transport processes). Mandapaka et al. (2009) have analyzed for (sub-) catchments of different sizes the runoff response from different rainfall scenarios with a total amount of 10 mm. For catchments with an area less than 10 km², a strong dependence of the duration, the intensity and the spatial distribution of the rainfall is identified. With increasing area size, the influence of these factors is reduced and for catchments with 1000 km², it is almost completely dampened. Since the catchment areas in the actual study range between 44 km² and 321 km², i.e. considerably larger than 10 km², this could be a possible reason why the differences in the runoff results are so small. On the other hand, the results of Seliga et al. (1992) and Obled et al. (1994) show that an increasing station network density lead to an improvement of rainfall information and hence should also lead to an improvement of the runoff simulation results. Ogden and Julien (1993) investigate the time of concentration of a catchment as an influencing factor for the rainfall-runoff processes. If the duration of a rainfall event causing flooding is shorter than the time of concentration, the spatial distribution of the rainfall is influencing the discharge at the catchment outlet. If rainfall

events last longer than the concentration time, the influence decreases. However, Nicotina et al. (2008) identify an influence of spatial rainfall patterns only for catchments with areas > 1000 km², based on the travel time in the catchment. In the investigated catchments, the concentration time ranges from 1.8 h to 7.4 h, so the temporal and spatial variation should have an influence on the simulated discharges.In Müller and Haberlandt (2018) the rainfall products V1 and V2 and their

5   influence on simulated discharge have been analyzed for 5-minute time steps in an urban hydrological context. Significant differences could be identified between the simulated runoff statistics resulting from V1 and V2 for their artificial sewage system.

Another reason could be the choice of the rainfall-runoff model. Obled et al. (1994) raise the question if it is possible with semi-distributed models to transfer the information of the spatial rainfall patterns into the simulated discharge time series.

10   Obversely, if spatial rainfall patterns are necessary for rainfall-runoff simulations for a catchment with an area size of 71 km², as is used in their study, the spatial resolution of semi-distributed models may not be sufficient. Krajeski et al. (1991) also conclude that for the analysis of spatial problems, fully-distributed models may be more suitable and recommend those for further studies. Bárdossy and Das (2008) point out that with an increasing spatial resolution of the applied rainfall-runoff model, the sensitivity of for example the rain gauge density and hence the spatial rainfall patterns may increase as

15   well. The rainfall-runoff simulations were carried out with two models, the semi-distributed HBV model and the fully-distributed WaSiM-model. The spatial resolution is in WaSiM with 150 m x 150 m for each raster cell much higher than in HBV with approx. 20 km² per subcatchment. This higher spatial rainfall diversity and hence a numerical diffusion of the rainfall due to a too-coarse spatial resolution is thus avoided. Through the rainfall correction for altitude, an additional increase of the spatial diversity is achieved. While for the simulated discharge time series with HBV almost no differences

20   between the different rainfall products could be identified, for catchment Pionierbrücke in WaSiM slight differences between method V1 and methods V2 and V3 differences regarding the seasonal extreme values can be identified. For both, V2 and V3, subsequent steps after the rainfall disaggregation were applied to implement spatial consistence by simultaneous rainfall occurrence at different rain gauges. This affects the simulated runoff at least for instantaneous peak flows in the summer and winter period. However, the number of subcatchments in HBV and by that the spatial resolution of the rainfall-runoff model

25   can be increased, which is assumed to lead to more diverse results between V1, V2 and V3, similar as resulting from WaSiM.

For Pionierbrücke, as a fast-reacting, mountainous catchment, the absolute differences for the seasonal extreme flows resulting from V1 or the products V2 and V3 for a flood with a return period of 50 years are approx. 5-8 m³/s during both the calibration and validation periods (see Fig. 14 and 15) using WaSiM. For the other two catchments Reckershausen and

30   Tetendorf, the difference is expected to be smaller since both catchments are larger and cover a less steep area. Thus, no additional simulations with WaSiM have been carried out for these two catchments. In this context it should be mentioned, that WaSiM is a much more complex rainfall-runoff model than HBV with a high demand on meteorological input time series (e.g. precipitation, temperature, humidity, wind speed and global radiation), which has to be available for the whole simulation period on an hourly time step.

6. Summary, Conclusions & Outlook

The aim of this investigation is to investigate the influence of different degrees of spatial consistence in disaggregated time series on simulated runoff statistics. The investigation is carried out for three meso-scale catchments in Lower Saxony, Germany, which differ in terms of their size, land use, soil and slope. For the disaggregation, a multiplicative, micro-canonical cascade model after Müller and Haberlandt (2015) is used. Since the disaggregation process is performed on a per station basis without taking into account neighboring stations, spatial consistence must be implemented afterwards. Here, a resampling algorithm based on Müller and Haberlandt (2015) is applied (named V2) as well as a more pragmatic approach where the same relative diurnal cycle is used for all stations on the one day (Haberlandt and Radtke, 2014, named V3). Nevertheless, investigations without subsequent steps to implement spatial consistence exist as well (Ding et al., 2016) and have been included in this investigation (named V1). The hypothesis tested in this study is that these different rainfall products lead to differences in the derived runoff statistics as well. The following conclusions can be drawn regarding the rainfall product differences:

1. The resampling algorithm for the implementation of spatial consistence was applied on an hourly basis for the first time for distances smaller than 20 km for V2. The achieved values for the bivariate spatial rainfall characteristics are comparable to those from observations.

2. The bivariate spatial characteristics are underestimated by V1 and overestimated by V3 respectively.

3. While for the areal rainfall intensities, the exceedance curve leads to an expected order of V1<V2<V3, for the areal rainfall extremes, V2 and V3 result in similar values, both being higher than V1.

The generated rainfall products V1, V2 and V3 have been used as input for rainfall-runoff modeling to evaluate the influence of the above identified differences of rainfall characteristics. An application-based evaluation is important in terms of rainfall generation, since it provides a new perspective and hence new insights into the rainfall data (Müller and Haberlandt, 2016, Müller et al., 2018, Sikorska et al., 2018). For the simulations, the semi-distributed HBV model (Wallner et al., 2013) and the fully-distributed WaSiM model (Schulla, 1997, 2015) have been implemented. The essential findings are:

1. With the applied calibration process in HBV, a good representation of observed runoff statistics is possible for V1-V3 for the calibration period.

2. The rainfall products V1-V3 result in only small differences in the simulated runoff statistics using HBV. Differences do not increase whether a neutral parameter set without calibration is applied nor if the station density increases.

3. For peak flows in the summer and winter periods, slight differences resulting from V1 and both, V2 and V3, can be identified using WaSiM. V2 and V3 lead to comparable higher flood peaks than V1, which is consistent with extreme value analysis of areal rainfall for this catchment.

4. For the intra-annual cycle and the flow duration curve, no difference resulting from V1-V3 can be identified from either HBV nor WaSiM.

Ding et al. (2016) achieved a good representation of summer and winter peak flows with V1 as input rainfall data and HBV as rainfall-runoff model. Haberlandt and Radtke (2014) applied HEC-HMS as semi-distributed rainfall-runoff model with disaggregated and parallelized rainfall time series (V3) as input data. The continuously simulated runoff time series were analyzed regarding annual extreme flows, which could be reproduced well for all catchments. The findings of both investigations can be confirmed by the actual study.

However, no differences resulting from V1, V2 and V3 regarding the summer and winter extremes are detectable for HBV. On the other hand, WaSiM results in slight differences for seasonal extreme values for the investigated catchment Pionierbrücke which is in line with previous findings regarding the areal rainfall extreme values. However, the differences between the resulting seasonal peak flows simulated with WaSiM from V1, V2 and V3 are still small with approx. 5-8 m³/s (up to 15 %) for floods with return periods of 50 years. It should be noted that V1, V2 and V3 clearly differ regarding the investigated spatial bivariate characteristics of probability of occurrence, coefficient of correlation, continuity ratio and the resulting areal rainfall intensities, especially regarding their extreme values. Hence, the hypothesis formulated before is rejected in this case study. Although several possible causes regarding the applied rainfall-runoff models (parameter calibration, rainfall station density, type and spatial resolution of rainfall-runoff model) have been analyzed, no final conclusion about the reason for the similar runoff statistic can be drawn. It is assumed that the damping behavior of the catchments leads to these small differences in runoff statistics.

These findings suggest that (i) simple model structures might compensate for deficiencies in spatial representativeness through parameterization and (ii) highly resolved hydrological models benefit from improved spatial modeling of rainfall.

Of course, the similarity of the simulated runoff statistics from V1, V2 and V3 is only valid for the investigated catchments. For catchments with other climatic or physiographic attributes, results can be different. Therefore, a systematic investigation of catchments with different hydrological behavior in climates and with different rainfall-runoff models would be necessary (comparative hydrology) to identify catchments, for which the degree of spatial rainfall consistence matters. The actual study could be a starting point for that.

However, the main intention of the actual study was to analyze the impact of rainfall products with different degrees of spatial consistence on simulated runoff statistics. The application of the resampling algorithm (V2) is recommended for spatial application of disaggregated rainfall data since this method leads to the best agreement with the observed spatial rainfall characteristics.

Competing interests

The authors declare that they have no conflict of interest.

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References

Aarts, E. and Korst, J.: Simulated Annealing and Boltzmann Machines: A stochastic approach to combinatorial optimization and neural computing, John Wiley & Sons, Chichester, 1965.

Andres-Domenech, I., Garcia-Bartual, R., Montanari, A. and Marco, J.B.: Climate and hydrological variability: the catchment filtering role. Hydrol. Earth Syst. Sci. 19, 379–387, 2015.

Bárdossy, A. and Das, T.: Influence of rainfall observation network on model calibration and application. Hydrol. Earth Syst. Sci. 12, 77–89, 2008.

Beven, K. J.: Rainfall-Runoff Modelling: The Primer. John Wiley and Sons, Chichester, 2001.

Breinl, K., Turkington, T., and Stowasser, M.: Simulating daily precipitation and temperature: A weather generation framework for assessing hydrometeorological hazards. Meteorol. Appl., 22 (3), 334-347, 2014.

Bormann, H. and Elfert, S.: Application of WaSiM-ETH model to Northern German lowland catchments: model performance in relation to catchment characteristics and sensitivity to land use change. Adv. Geosci. 27, 1–10. doi:10.5194/adgeo-27-1-2010, 2010.

Buishand, T. A.: Stochastic modeling of daily rainfall sequences, H. Veenmann and Zonen B. V., Wageningen, Netherlands, 1977.

Carsteanu, A. and Foufoula-Georgiou, E.: Assessing dependence among weights in a multiplicative cascade model of temporal rainfall. J. Geophys. Res., 101(D21), 26363–26370. Federal Environment Agency (2009). CORINE Land Cover. DLR-DFD, Hannover, 1996.

Criss, R. E. and Winston, W. E.: Do Nash values have value? Discussion and alternate proposals. Hydrol. Process., 22, 2723-2725, 2008.

Ding, J., Wallner, M., Müller, H. and Haberlandt, U.: Estimation of instantaneous peak flows from maximum mean daily flows using the HBV hydrological model. Hydrol. Process. 30 (9), 1431–1448, 2016.

DVWK: Ermittlung der Verdunstung von Land- und Wasserflächen. In: ATVDVWK-Regelwerk (Ed.), DVWK-Merkblatt 238/1996. Deutscher Verband für Wasserwirtschaft und Kulturbau e.V. (DVWK), Bonn, 1996.

DVWK: Verdunstung in Bezug zu Landnutzung, Bewuchs und Boden. Merkblatt ATV-DVWK-M 504. Deutsche Vereinigung für Wasserwirtschaft, Abwasser und Abfall, 2002.

Feldman, A. D.: Hydrological Modeling System HEC-HMS – Technical Reference Manual, US Army Corps of Engineers, 2000.

Förster, K., Hanzer, F., Winter, B., Marke, T. and Strasser, U.: An open-source MEteoroLOgical observation time series DISaggregation Tool (MELODIST v0.1.1). Geosci. Model Dev. 9 (7), 2315-2333, 2016.

Gelleszun, M., Kreye, P. and Meon, G.: Lexikografische Kalibrierungsstrategie für eine effiziente Parameterschätzung in hochaufgelösten Niederschlag-Abfluss-Modellen (Lexicographic calibration strategy for efficient parameter estimation in highly resolved rainfall-runoff models). Hydrol. Wasserbewirtsch. 59, 84–95. doi:10.5675/HyWa_2015,3_1, 2015.

Gires, A., Giangola-Murzyn, A., Abbes, J.-B., Tchiguirinskaia, I., Schertzer, D. und Lovejoy, S: „Impacts of small scale rainfall variability in urban areas: a case study with 1D and 1D/2D hydrological models in a multifractal framework". *Urban Water Journal* 12 (8), 607–617, 2014.

Haberlandt, U., Ebner von Eschenbach, A.D. and Buchwald, I.: A space-time hybrid hourly rainfall model for derived flood frequency analysis. Hydrol. Earth Syst. Sci. 12 (6), 1353–1367, 2008.

Haberlandt, U. and Radtke, I.: Hydrological model calibration for derived flood frequency analysis using stochastic rainfall and probability distributions of peak flows. Hydrol. Earth Syst. Sci. 18 (1), 353–365, 2014.

Hartwich, R., Behrens, J., Eckelmann, W., Haase, G., Richter, A., Roeschmann, G. and Schmidt, R.: Bodenübersichtskarte der Bundesrepublik Deutschland. Bundesanstalt für Geowissenschaften und Rohstoffe, Hannover, 1998.

Hosking, J. and Wallis, J.: Regional Frequency Analysis: an approach based on L-moments. Cambridge University Press, New York, 1997.

Kirkpatrick, S., Gelatt, C. D. and Vecchi, M. P.: Optimization by simulated annealing, Science, 220 (4598), 671-680, 1983.

Kirpich, Z. P.: Time of concentration of small agricultural watersheds. Civil Eng. 10 (6), 362, 1940.

Krajewski, W. F., Lakshmi, V., Georgakakos, K. P. and Jain, S. C.: A Monte Carlo study of rainfall sampling effect on a distributed catchment model. Water Resour. Res. 27 (1), 119–128, 1991.

Maniak, U.: Hydrologie und Wasserwirtschaft. Springer Verlag, Berlin, 2005.

Mandapaka, P. V., Krajewski, W. F., Mantilla, R. and Gupta, V. K.: Dissecting the effect of rainfall variability on the statistical structure of peak flows. Adv. Water Resour. 32, 1508–1525, 2009.

Mandelbrot, B. B.: Intermittent turbulence in self-similar cascades: divergence of high moments and dimension of the carrier. J. Fluid Mech. 62 (2), 331–358, 1974.

Marshak, A., Davis, A., Cahalan, R., and Wiscombe,W.: Bounded cascade models as nonstationary multifractals. Phys. Rev. E, 49(1), 55–69, 1994.

Melsen, L. A., Teuling, A. J., Torfs, P. J. J. F., Uijlenhoet, R., Mizukami, N. und Clark, M. P.: Hydrol. Earth Syst. Sci. Opinions: The need for process-based evaluation of large-domain hyper-resolution models. Hydrol. Earth Syst. Sci. 20, 1069–1079, 2015.

Monteith, J.L.: Evaporation and environment, in: Fogg, G.E. (Ed.), The State and Movement of Water in Living Organisms, Symposia of the Society for Experimental Biology. Cambridge University Press, Cambridge, 205–234, 1965.

Müller, H.: Rainfall disaggregation for hydrological modeling, PhD-thesis, Faculty of Civil Engineering and Geosciences, Institute of Water Resources Management, Hydrology and Agricultural hydraulic Engineering (in German), 2016.

Müller, H. and Haberlandt, U.: Temporal Rainfall Disaggregation with a Cascade Model: From Single-Station Disaggregation to Spatial Rainfall. J. Hydrol. Eng. 20 (11), 04015026, 2015.

Müller, H. and Haberlandt, U.: Temporal rainfall disaggregation using a multiplicative cascade model for spatial application in urban hydrology. J. Hydrol. 556, 847-864 556, , 2018.

Müller, T., Schütze, M. and Bárdossy, A.: Temporal asymmetry in precipitation time series and its influence on flow simulations in combined sewer systems. Adv. Water Resour. 107, 56-64, 2017.

Nash, J. E. and Sutcliffe, J. V.: River flow forecasting through conceptual models part I - a discussion of principles. J. Hydrol. 10, 282–290, 1970.

Nicotina, L. E., Celegon, E. Alessi, Rinaldo, A. and Marani, M.: On the impact of rainfall patterns on the hydrologic response. Water Resour. Res. 44, W12401, 2008.

Niehoff, D., Fritsch, U. and Bronstert, A.: Land-use impacts on storm-runoff generation: scenarios of land-use change and simulation of hydrological response in a meso-scale catchment in SW-Germany. J. Hydrol. 267, 80–93, 2002.

Obled, C., Wendling, J. and Beven, K.: The sensitivity of hydrological models to spatial rainfall patterns: an evaluation using observed data. J. Hydrol. 159 (1 4), 305–333, 1994.

Ochoa-Rodriguez, S., Wang, L.-P., Gires, A., Pina, R. D., Reinoso-Rondinel, R., Bruni, G., Ichiba, A., Gaitan, S., Cristiano, E., Assel, J. v., Kroll, S., Murla-Tuyls, D., Tisserand, B., Schertzer, D., Tchiguirinskaia, I., Onof, C., Willems, P. und Veldhuis, M.-C. ten (2015). „Impact of Spatial and Temporal Resolution of Rainfall Inputs on Urban Hydrodynamic Modelling Outputs: A Multi-Catchment Investigation". *Journal of Hydrology* 531 (2), 389–407, 2015.

Ogden, F. L. and Julien, P. Y.: Runoff sensitivity to temporal and spatial rainfall variability at runoff plane and small basin scales. Water Resour. Res. 29 (8), 2589–2597, 1993.

Onof, C., Chandler, R. E. und Kakou, A.: Rainfall modelling using Poisson-cluster processes: a review of developments. Stoch. Env. Res. Risk A. 6 (14), 384–411, 2000.

Paschalis, A., Fatichi, S., Molnar, P., Rimkus, S., Burlando, P.: On the effects of small scale space–time variability of rainfall on basin flood response. J. Hydrol. 514, 313-327, 2014.

Pathiraja, S., Westra, S. and Sharma, A.: Why continuous simulation? The role of antecedent moisture in design flood estimation. Water Resour. Res. 48 (6), W06534, 2012.

Peel, M. C., Finlayson, B. L. and McMahon, T. A.: Updated world map of the Köppen-Geiger climate classification. Hydrol. Earth Syst. Sci. 11 (5), 1633–1644, 2007.

5 Peleg, N., Blumensaat, F., Molnar, P., Fatichi, S., Burlando, P.:Partitioning the impacts of spatial and climatological rainfall variability in urban drainage modelling. Hydrol. Earth Syst. Sci. 21, 1559-1572, 2017.

Peleg, N., Marra, F., Fatichi, S., Paschalis, A., Molnar, P., Burlando, P.: Spatial variability of extreme rainfall at radar subpixel scale. J. Hydrol. 556, 922-933, 2018.

Rodriguez-Iturbe, I., Cox, D. R. and Isham, V.: Some models for rainfall based on stochastic point-processes. P. R. Soc.
10 London A410, 269-288, 1987.

Rossman, L.A.: Storm water management model – User's manual version 5.0. Environmental Protection Agency, EPA/600/R-05/040, 2010.

Rupp, D. E., Keim, R. F., Ossiander, M., Brugnach, M. and Selker, J. S.: Time scale and intensity dependency in multiplicative cascades for temporal rainfall disaggregation. Water Resour. Res. 45 (7), W07409, 2009.

15 Schaefli, B., Gupta, H. V.: Do Nash Values have value?. Hydrol. Process., 21, 2075-2080, 2007.

Seliga, T. A., Aron, G., Aydin, K. and White, E.: Storm runoff simulation using radar-estimated rainfall rates and a Unit Hydrograph model (SYN-HYD) applied to GREVE watershed. American Meteorological Society, 25th International Conference on Radar Hydrology, 587–590, 1992.

Schulla, J.: Hydrologische Modellierung von Flussgebieten zur Abschätzung der Folgen von Klimaänderungen
20 (Dissertation). ETH Zürich, 1997.

Schulla, J.: Model Description WaSiM (Water balance Simulation Model) - completely revised version of 2012 with 2013 to 2015 extensions. Hydrology Software Consulting J. Schulla, 2015.

Veneziano, D., Furcolo, P., and Iacobellis, V. (2006). Imperfect scaling of time and space-time rainfall. J. Hydrol. 322(1–4), 105–119.

25 Sikorska, A. E., Vivrioli, D., Seibert, J. (2017). Effective precipitation duration for runoff peaks based on catchment modelling. J. Hydrol., 556, 510-522..

Sivapalan, M., Blöschl, G.: Transformation of point to areal rainfall: Intensityduration-frequency curves. J. Hydrol. 204 (1–4), 150–167, 1998.

Thober, S., Mai, J., Zink, M. and Samaniego, L.: Stochastic temporal disaggregation of monthly precipitation for regional
30 gridded data sets. Water Resour. Res. 50 (11), S. 8714–8735, 2014.

Veneziano, D., Langousis, A.: The areal reduction factor: a multifractal analysis. Water Resour. Res. 41 (7), W07008, 2005.

Wallner, M., Haberlandt, U. and Dietrich, J.: A one-step similarity approach for the regionalization of hydrological model parameters based on Self-Organizing Maps. J. Hydrol. 494 (0), S. 59–71, 2013.

Wallner, M. and Haberlandt, U.: Klimabedingte Änderung von Hochwasserabflüssen im Aller-Leine-Einzugsgebiet - Eine Fallstudie mit HBV-IWW. Hydrol. Wasserbewirtsch. 59 (4), 174–183, 2015.

Westerberg, I. K., Guerrero, J.-L., Younger, P. M., Beven, K. J., Seibert, J., Halldin, S., Freer, J. E. and Xu, C.-Y.: Calibration of hydrological models using flow-duration curves. Hydrol. Earth Syst. Sci. 15 (7), 2205–2227, 2011.

5   Wilks, D. S.: Multisite generalization of a daily stochastic precipitation generation model. J. Hydrol. 210 (1-4), 178–191, 1998.

Wright, D.B., Smith, J.A., Baeck, M.L.: A critical examination of area reduction factors. J. Hydrol. Eng. 19 (4), 769–776, 2013.

Xu, H., Chong-Yu, X., Zhang, Z. and Li, L.: Assessing the influence of rain gauge density and distribution on hydrological model performance in a humid region of China. J. Hydrol. 505, 1–12, 2013.

Yu, P. S. and Yang, T. C.: Using synthetic flow duration curves for rainfall-runoff model calibration at ungauged sites. Hydrol. Process. 14 (1), 117–133, 2000.