



- 1 Effects of Micro-Arrangement of Solid Particles on
- 2 PCE Migration and Its Remediation in Porous Media
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21 ABSTRACT

22 Groundwater can be stored abundantly in granula-composed aquifers with high permeability. The micro-structure of granular materials has important effect on aquifer 23 permeability; and the contaminant migration and remediation in aquifers is also 24 25 influenced by the characteristics of porous media. In this study, two different microscale 26 arrangements of sand particles are examined to reveal the effects of micro-structure on the contaminant migration and remediation. With the help of fractal theory, the 27 mathematical expressions of permeability and entry pressure are conducted to delineate 28 29 granular materials with regular triangle arrangement (RTA) and square pitch arrangement 30 (SPA) at microscale. Using Sequential Gaussian Simulation (SGS) method, a synthetic 31 heterogeneous site contaminated by Perchloroethylene (PCE) is then used to investigate 32 the migration and remediation affected by the two different micro-scale arrangements. 33 PCE is released from an underground storage tank into the aquifer and the surfactant is 34 used to clean up the subsurface environment. Results suggest that RTA not only can 35 cause larger range of groundwater contamination, but also can cause harder remediation 36 for contaminated aquifer. The PCE remediation efficiency of 60.01% -99.78% with a 37 mean of 92.52% and 65.53% -99.74% with a mean of 95.83% are achieved for 200 individual heterogeneous realizations based on the RTA and SPA, respectively, 38 39 indicating that the cleanup of PCE in aquifer with SPA is significantly easier. This study leads to a new understanding of the microstructures of porous media and demonstrates 40 41 how micro-scale arrangements control contaminant migration in aquifers, which is





- 42 helpful to design successful remediation scheme for underground storage tank spill.
- 43 Keywords: microscale arrangement; regular triangle; square pitch; contaminant
- 44 migration and remediation; cumulative PCE removal; macroscopic scale
- 45

46 **1. Introduction**

Groundwater is an essential natural resource for water supply to domestic, agricultural, 47 48 industrial activities and ecosystem health (Boswinkel, 2000; Valipour, 2012; Valipour, 2015; Yannopoulos et al., 2015; Valipour and Singh, 2016). Unfortunately, with the rapid 49 development of economic activities such as mining, agriculture, landfills and industrial 50 activities (Bakshevskaia and Pozdniakov, 2016; Cui et al., 2016; Liu et al., 2016), more 51 52 and more contaminants released from human activities are contaminating the precious 53 groundwater resource and subsurface environment (Dawson and Roberts, 1997; Liu, 2005; Hadley and Newell, 2014; C.Carroll et al., 2015; Essaid et al., 2015; Huang et al., 54 55 2015; Liu et al., 2016; Schaefer et al., 2016; Weathers et al., 2016). Out of the contaminants detected in groundwater, dense nonaqueous phase liquids (DNAPLs) 56 such as perchloroethylene (PCE) and other polycyclic aromatic hydrocarbons (PAHs), 57 58 are highly toxic and carcinogenic (Dawson and Roberts, 1997; Hadley and Newell, 2014). 59 When DNAPLs are released into aquifer from underground storage tank, they will infiltrate through the entire aquifer and form residual ganglia and pools of DNAPLs due 60 to their large densities, high interfacial tension, and low solubility. The residual 61 ganglia and pools of DNAPLs can serve as long-term sources of groundwater 62 contamination that is harmful to subsurface environment and human beings (Bob et al., 63





2008; Liang and Lai, 2008; Liang and Hsieh, 2015). Consequently, it is very important
 to explore DNAPL migration in aquifer and mitigate groundwater contamination by
 appropriate remediation.

67 When DNAPL migrates in aquifers at macroscopic scale, the transport properties such 68 as permeability, diffusivity and dispersivity are closely related to the aquifer's microstructures (Yu and Li, 2004; Yu, 2005; Yun et al., 2005; Feng and Yu, 2007; Yu et 69 70 al., 2009). Therefore, characterizing the effect of microstructures on macroscopic 71 properties is a key point of heterogeneity of porous media. In the classical 72 Kozeny–Carman equation, the permeability K is related to porosity n, surface area S 73 and the Kozeny constant c, where c is affected by the porosity, solid particles and micro geometric structures (Bear 1972; Yu et al. 2009). According to fractal theory, 74 75 natural porous media can be treated as fractal objects (Pfeifer and Avnir 1983; Katz and Thompson 1985; Krohn 1988). For example, the tortuosity of flow path in porous media 76 is deeply studied by various proposed fractal models (Yu and Cheng 2002; Yu et al. 2009; 77 Cai et al. 2010), indicating the effectiveness of fractal methods compared to experimental 78 79 observations. Based on fractal concepts, mathematic models are proposed to depict the permeability and invasion of fluids in some special porous media (Yu and Cheng 2002; 80 Yu et al. 2009; Cai et al. 2010). Furthermore, fractal method is also used to explore the 81 effect of microstructure of biological media on associated thermal conductivity while this 82 83 kind of material has a complex randomly distributed vascular trees structure at microscale (Li and Yu 2013). 84

85 In this study, we focus on the effect of micro-arrangement of sand particles on





macroscopic DNAPL migration and associated remediation for underground storage 86 tank spill. With the help of fractal theory, the microstructures of two different microscale 87 arrangements of sand particles are explored. Afterwards, the mathematical relationships 88 between porosity and permeability, entry pressure are derived for regular triangle 89 90 arrangement (RTA) and square pitch microscale arrangement (SPA). Idealized heterogeneous contaminated site is generated using Sequential Gaussian Simulation 91 92 (SGS) method. Underground storage tank releases PCE into heterogeneous aquifer 93 composed of granular material and migrates freely. After long time migration, PCE 94 contamination is alleviated using surfactant remediation method. A multicomponent, 95 multiphase model simulator UTCHEM is then used to simulate the entire process of DNAPL migration and remediation. Effects of arrangements of sand particles on 96 97 migration and remediation of DNAPLs are comparatively analyzed based on the simulations to reveal how the microstructure of porous media controls the contaminant 98 99 migration and remediation at macroscopic scale.

100 2. Methodology

101 **2.1 Fractal models of two different microscale arrangements of sand**

102 particles

The porous media can be treated as the bundle of tortuous capillary tubes, the
relationship between the diameter and the length of capillary tube are (Yu and Cheng,
2002):

106
$$L_t(\lambda) = \lambda^{1-D_t} L_s^{D_t}$$
(1)





- 107 where L_s is the straight length between the tortuous flow path's end point; λ is the
- 108 diameter of capillary tube; D_t is the fractal dimension of tortuosity for porous media,
- 109 $1 \le D_t \le 2$ (Yu and Cheng, 2002).
- 110 Select an infinitesimal element consisting of a bundle of tortuous capillary tubes
- 111 form porous media, the total number of capillary tubes in infinitesimal element can be
- 112 calculated by the power-law relation:

113
$$N(L \ge \lambda) = \left(\frac{\lambda_{\max}}{\lambda}\right)^{D_f}$$
(2)

114 where D_f is the fractal dimension for pore areas in porous media, $1 < D_f < 2$ (Yu and

115 Cheng, 2002); λ_{max} is the maximum diameter of capillary tubes.

116 Afterward, the derivative of Equation (2) can be achieved:

117
$$-dN(L \ge \lambda) = D_f \lambda_{\max}^{D_f} \lambda^{-(D_f+1)} d_{\lambda}$$
(3)

118 The total number of capillary tubes in infinitesimal element can be derived from

119 Equation (3):

120
$$N_t (L \ge \lambda_{\min}) = \left(\frac{\lambda_{\max}}{\lambda_{\min}}\right)^{D_f}$$
(4)

121 where λ_{min} is the minimum diameter of capillary tubes.

122 Dividing Equation (3) by Equation (4) can achieve:

123
$$-\frac{d_{N(L\geq\lambda)}}{N_t} = D_f \lambda_{\min}^{D_f} \lambda^{-(D_f+1)} d_\lambda = f(\lambda) d_\lambda$$
(5)

124 where $f(\lambda)$ is the probability density function, $f(\lambda) = D_f \lambda_{\min}^{D_f} \lambda^{-(D_f+1)}$, it should satisfy

125 $\int_{-\infty}^{+\infty} f(\lambda) d_{\lambda} = 1 - \left(\frac{\lambda_{\min}}{\lambda_{\max}}\right)^{D_{f}} . \text{If } \left(\frac{\lambda_{\min}}{\lambda_{\max}}\right)^{D_{f}} = 0.$

126 The probability density function satisfies the relationship:





127
$$\int_{-\infty}^{+\infty} f(\lambda) d_{\lambda} = 1 - \left(\frac{\lambda_{\min}}{\lambda_{\max}}\right)^{D_{f}}$$
(6)

128 Considering $\left(\frac{\lambda_{min}}{\lambda_{max}}\right)^{D_f} = 0$, the above Equation (6) becomes:

129
$$\int_{-\infty}^{+\infty} f(\lambda) d_{\lambda} = \int_{\lambda_{\min}}^{\lambda_{\max}} f(\lambda) d_{\lambda} = 1 - \left(\frac{\lambda_{\min}}{\lambda_{\max}}\right)^{D_{f}} = 1$$
(7)

130 When fluid flow in capillary tubes, the flow rate Q can be calculated by the

131 Hagen–Poiseulle equation:

132
$$Q = \frac{\pi^4 \Delta P}{8\mu L_s} = \frac{\pi (\frac{\lambda}{2})^4 \Delta P}{8\mu L_s} = \frac{\pi \lambda^4 \Delta P}{128\mu L_s}$$
(8)

133 where μ is fluid's viscosity; ΔP is the pressure gradient across the capillary tube.

134 The differentiation of flow rate of capillary tubes is (Yu and Cheng, 2002):

$$d_{q} = \left[-d_{N(L \ge \lambda)}\right] \frac{\pi \lambda^{4} \Delta P}{128 \mu L_{t}(\lambda)} = D_{f} \lambda_{\max}^{D_{f}} \lambda^{-(D_{f}+1)} d_{\lambda} \cdot \frac{\pi \lambda^{4} \Delta P}{128 \mu L_{t}(\lambda)}$$

$$= \frac{\pi}{128} \frac{\Delta P}{\mu} \frac{D_{f} \lambda_{\max}^{D_{f}}}{L_{t}(\lambda)} \lambda^{3-D_{f}} d_{\lambda} = \frac{\pi}{128} \frac{\Delta P}{\mu} \frac{D_{f} \lambda_{\max}^{D_{f}}}{\lambda^{1-D_{t}} L_{s}^{D_{f}}} \lambda^{3-D_{f}} d_{\lambda}$$

$$= \frac{\pi}{128} \frac{\Delta P}{\mu} \frac{D_{f} \lambda_{\max}^{D_{f}}}{L_{s}^{P_{f}}} \lambda^{2+D_{t}-D_{f}} d_{\lambda}$$
(9)

136 Integrating the individual flow rate from λ_{min} to λ_{max} can achieve the total flow rate

137 (Yu and Cheng, 2002):

$$Q = \int d_{q} = \int_{\lambda_{\min}}^{\lambda_{\max}} \frac{\pi}{128} \frac{\Delta P}{\mu} \frac{D_{f} \lambda_{\max}^{D_{f}}}{L_{s}^{D_{f}}} \lambda^{2+D_{t}-D_{f}} d_{\lambda}$$

$$= \frac{\pi}{128} \frac{\Delta P}{\mu} \frac{D_{f}}{3-D_{f}+D_{t}} \frac{1}{L_{s}^{D_{f}}} \lambda^{D_{f}}_{\max} (\lambda_{\max}^{3-D_{f}+D_{t}} - \lambda_{\min}^{3-D_{f}+D_{t}})$$

$$= \frac{\pi}{128} \frac{\Delta P}{\mu} \frac{D_{f}}{3-D_{f}+D_{T}} \frac{1}{L_{s}^{D_{f}}} \lambda^{3+D_{t}}_{\max} [1 - (\frac{\lambda_{\min}}{\lambda_{\max}})^{D_{f}} (\frac{\lambda_{\min}}{\lambda_{\max}})^{3+D_{t}-2D_{f}}]$$
(10)

138

139 Due to $1 \le D_t \le 2$ and $1 \le D_f \le 2$, then $3 + D_T - 2D_f \ge 0$. Simultaneously, $(\frac{\lambda_{\min}}{\lambda_{\max}})^{D_f} \cong 0$,





140
$$0 < (\frac{\lambda_{\min}}{\lambda_{\max}})^{3+D_T-D_f} < 1$$
. Therefore, Equation (10) can be simplified as:

141
$$Q = \int d_q = \frac{\pi}{128} \frac{\Delta P}{\mu} \frac{D_f}{3 - D_f + D_T} \frac{1}{L_0^{D_T}} \lambda_{\max}^{3 + D_T}$$
(11)

142 Substituting Darcy's law $Q = \frac{kA\Delta P}{\mu L_0}$ in Equation (11) will obtain the permeability

143 of porous media:

144
$$k = \frac{\pi}{128} \frac{D_f}{3 + D_T - D_f} \frac{L_0^{1 - D_T}}{A} \lambda_{\max}^{3 + D_T}$$
(12)

145 To obtain the fractal dimension of tortuosity D_t , the expression of tortuosity (τ)

146 can be obtained from Equation (1):

147
$$\tau = \frac{L_t(\lambda)}{L_s} = \frac{\lambda^{1-D_t} L_s^{D_t}}{L_s} = (\frac{L_s}{\lambda})^{D_t - 1}$$
(13)

148 Then the D_f is given by (Yu and Li, 2001):

149
$$D_{t} = 1 + \frac{\ln \tau}{\ln(\frac{L_{s}}{\lambda})}$$
(14)

150 RTA and SPA are shown in Fig. 1. An equilateral triangle and a square are

selected from the two micro-structures as unit cells (Fig. 1a and Fig. 1b). The unit cell

152 of equilateral triangle is composed of three solid particles and the pore among them,

153 while the unit cell of square is composed of four solid particles. For the unit cell of

154 RTA in Fig. 1a, corresponding porosity is given by:

155
$$n = \frac{A_a - \pi R_v^2 / 2}{A_a}$$
(15)

156 where *n* is porosity; A_a is the total area of equilateral triangle; R_v is the average radius

157 of solid particles. The total area of equilateral triangle can be achieved:

158
$$A_a = \frac{\pi R_v^2}{2(1-n)}$$
(16)





159 The side length of the equilateral triangle in Fig. 1a can be calculated as:

160
$$L_{a} = R_{v} \sqrt{\frac{2\pi}{\sqrt{3}(1-n)}}$$
(17)

161 where L_a is the side length.

162 The area of irregular pore among solid particles is given by:

163
$$A_{ap} = A_a - \frac{\pi R_v^2}{2} = \frac{\pi R_v^2 n}{2(1-n)}$$
(18)

164 where A_{ap} is the area of pore in the unit cell.

165 Approximate the pore in the equilateral triangle as a circle, then the maximum

166 diameter of pore can be obtained:

167
$$\lambda_{max,a} = R_{\nu} \sqrt{\frac{2n}{1-n}}$$
(19)

where $\lambda_{max,a}$ is the diameter of capillary tube in equilateral triangle. The fluid passes not only the central-pore of the unit cell, but also the gap between adjacent particles. The gap length and the average diameter of capillary tube perpendicular to the plane

171 of equilateral triangle are calculated as follows:

172
$$\Delta L_a = L_a - 2R_v = R_v \left(\sqrt{\frac{2\pi}{\sqrt{3}(1-n)}} - 2 \right)$$
(20)

173
$$\lambda_a = \frac{\lambda_{\max,a} + \Delta L_a}{2} = \frac{R_v}{2} \left(\sqrt{\frac{2n}{1-n}} + \sqrt{\frac{2\pi}{\sqrt{3}(1-n)}} - 2 \right)$$
(21)

174 where ΔL_a is the gap length between solid particles; λ_a is the average diameter of

175 capillary tubes in the equilateral triangle.

Generally, the tortuosity of flow path in porous media is the ratio of the length of
tortuous flow path to the straight length of flow path along the flow direction (Taiwo et al.,
2016):





179
$$\tau = \frac{L_t}{L_s}$$
(22)

- 180 where L_t is the length of tortuous flow path; and L_s is the straight length of flow path
- 181 along the flow direction.
- 182 For the flow path shown in Fig. 1a, the L_t and L_s respectively are:

183
$$L_{t} = (h_{o} - R_{v}) + \frac{\pi R_{v}}{2} = R_{v} (\sqrt{\frac{\sqrt{3}\pi}{2(1-n)}} + \frac{\pi}{2} - 1)$$
(23)

184
$$L_{s} = h_{o} = R_{v} \sqrt{\frac{\sqrt{3}\pi}{2(1-n)}}$$
(24)

185 where h_o is the altitude of the equilateral triangle, $h_o = \frac{\sqrt{3}}{2} L_a = R_v \sqrt{\frac{\sqrt{3}\pi}{2(1-n)}}$

186 Consequently, the tortuosity of RTA is yielded:

187
$$\tau = \frac{L_t}{L_s} = 1 + \frac{\frac{\pi}{2} - 1}{\sqrt{\frac{\sqrt{3}\pi}{2(1 - n)}}}$$
(25)

The
$$D_f$$
 is determined using Sierpinkski gasket (Fig. 2) in fractal theory (Yu and
Cheng, 2002). The shaded area represents solid of porous media and the white area
represents pore. The pore area fractal dimension in Figs. 2a-c are 0.000, 1.000 and 1.594,
respectively $(1 = L_a^{D_f} = 2^{D_f}, 3 = L_a^{D_f} = 3^{D_f}, 13 = L_a^{D_f} = 5^{D_f})$. Based on the Sierpinkski gasket,

192 the dimensionless pore area in RTA (Fig. 1a) is approximated as:

$$A_{apd} = \left(L_a^+\right)^{D_f} \tag{26}$$

where A_{apd} is the dimensionless pore area of RTA; $L_a^+ = L_a / \lambda_{min}$. Equation (26) can be solved to achieve D_{f} :

$$D_f = \frac{\ln A_{apd}}{\ln L_a^+} \tag{27}$$





- 197 The porosity equals to the ratio of the dimensionless pore area of RTA (A_{apd}) to
- 198 the dimensionless total area of RTA (A_a^+):

199
$$n = \frac{A_{apd}}{A_a^+}$$
(28)

200 where
$$A_a^+ = \frac{A_a}{\pi \lambda_{\min}^2 / 4} = \frac{\frac{\pi R_v^2}{2(1-n)}}{\pi \frac{\lambda_{\min}^2}{4}} = \frac{2R_v^2}{\lambda_{\min}^2} \frac{1}{1-n} = \frac{(d^+)^2}{2} \frac{1}{1-n}; d^+ = \frac{2R_v}{\lambda_{\min}}, \quad L_a^+ = \sqrt{A_a^+}.$$

From Equation (28), the dimensionless pore area of RTA (A_{apd}) is given by:

$$A_{apd} = n \cdot A_a^+ \tag{29}$$

203 The dimensionless total area of RTA (A_a^+) can be written as:

204
$$A_a^+ = (L_a^+)^2$$
 (30)

205 Afterward, L_a^+ is calculated as:

206
$$L_{a}^{+} = \sqrt{A_{a}^{+}} = \sqrt{\frac{(d^{+})^{2}}{2} \frac{1}{1-n}} = d^{+} \sqrt{\frac{1}{2(1-n)}}$$
(31)

207 Substituting Equation (29) and Equation (31) into Equation (27) will derive D_f of

208 RTA:

209
$$D_{f} = \frac{\ln A_{apd}}{\ln L_{a}^{+}} = \frac{\ln(n \cdot A_{a}^{+})}{\ln(\sqrt{A_{a}^{+}})} = 2 + \frac{\ln(n)}{\ln(\sqrt{A_{a}^{+}})} = 2 + \frac{\ln(n)}{\ln(d^{+}\sqrt{\frac{1}{2(1-n)}})}$$
(32)

210 For the unit cell of square shown in Fig. 1b, the porosity is:

211
$$n = \frac{A_b - \pi R_v^2}{A_b}$$
(33)

where A_b is the total area of the square. Equation (33) can also be expressed as the

area of unit cell:

$$A_b = \frac{\pi R_v^2}{1-n} \tag{34}$$





215 Again, the side length of the square is:

216
$$L_b = \sqrt{A_b} = R_v \sqrt{\frac{\pi}{1-n}}$$
(35)

217 Consequently, the area of irregular pore in the square is given by:

218
$$A_{bp} = A_b - \pi R_v^2 = \frac{n\pi R_v^2}{1-n}$$
(36)

219 where A_{bp} is the area of pore in the square.

220 Approximate the pore as a circle and obtain corresponding maximum diameter:

221
$$\lambda_{max,b} = 2R_{\nu}\sqrt{\frac{n}{1-n}}$$
(37)

where $\lambda_{max,b}$ is the maximum diameter of capillary tube perpendicular to the plane of the square. Similarly, fluid flows through the central-pore in the square and the gap between adjacent particles. As a result, the gap and average diameter of capillary tube are expressed as:

226
$$\Delta L_{b} = L_{b} - 2R_{v} = R_{v} \left(\sqrt{\frac{\pi}{1 - n}} - 2 \right)$$
(38)

227
$$\lambda_{b} = \frac{\lambda_{max,b} + \Delta L_{b}}{2} = \frac{R_{v}}{2} \left(2\sqrt{\frac{n}{1-n}} + \sqrt{\frac{\pi}{1-n}} - 2 \right)$$
(39)

where ΔL_b is the gap length between the adjacent two solid particles; λ_b is the average

diameter of capillary tube.

For the tortuous flow path in Fig. 1b, the L_t and L_s respectively are given by:

231
$$L_{t} = \Delta L_{b} + \pi R_{v} = R_{v} \left(\sqrt{\frac{\pi}{1 - n}} - 2 + \pi \right)$$
(40)

$$L_s = L_b = R_v \sqrt{\frac{\pi}{1 - n}} \tag{41}$$

233 Afterward, the tortuosity of SPA yields:



(47)



234
$$\tau = \frac{L_{t}}{L_{s}} = 1 + \frac{\pi - 2}{\sqrt{\frac{\pi}{1 - n}}}$$
(42)

- The procedure of deriving D_f of SPA is similar to the procedure of calculating D_f of
- 236 RTA. Similarly, the *D_f* and porosity of SPA (Fig. 1b) are given by:

$$D_f = \frac{\ln A_{bpd}}{\ln L_b^+} \tag{43}$$

238
$$n = \frac{A_{bpd}}{A_b^+} \tag{44}$$

239 where A_{bpd} is the dimensionless pore area of SPA; $L_b^+ = L_b / \lambda_{min}$, A_b^+ is the

240 dimensionless total area of SPA,
$$A_b^+ = \frac{A_b}{\pi \lambda_{\min}^2 / 4} = \frac{\frac{\pi R_v^2}{1 - n}}{\pi \frac{\lambda_{\min}^2}{4}} = \frac{4R_v^2}{\lambda_{\min}^2} \frac{1}{1 - n} = (d^+)^2 \frac{1}{1 - n}.$$

241 The dimensionless pore area of SPA (A_{bpd}) can be yielded from Equation (44):

 $A_{bpd} = n \cdot A_b^+ \tag{45}$

243 L_b^+ can be calculated as:

244
$$L_b^+ = \sqrt{A_b^+} = \sqrt{(d^+)^2 \frac{1}{1-n}} = d^+ \sqrt{\frac{1}{1-n}}$$
(46)

Substituting Equation (45) and Equation (46) into Equation (43),
$$D_f$$
 of SPA can
be derived:

247
$$D_f = \frac{\ln A_{bpd}}{\ln L_b^+} = \frac{\ln(n \cdot A_b^+)}{\ln(\sqrt{A_b^+})} = 2 + \frac{\ln(n)}{\ln(\sqrt{A_b^+})} = 2 + \frac{\ln(n)}{\ln(d^+\sqrt{\frac{1}{1-n}})}$$

The entry pressure of tortuous capillary tube (P_c) is defined by Yong-Laplace equation as follows (Ahn and Seferis, 1991):

$$P_c = \frac{\omega}{\lambda} \frac{1-n}{n}$$
(48)

251 where P_c is the entry pressure; λ is the diameter of capillary tube; ω equals to $F\sigma \cos\theta$





- in which θ is the contact angle between fluid and solid, σ is the surface tension of the
- wetting fluid, and F is the form factor depending on the capillary tube alignment and
- the flow direction.

255 **2.2 Dealing with the heterogeneity of porous media**

256 In this study, Sequential Gaussian Simulation (SGS) is used to generate random realization of heterogeneous porosity field. SGS is a stochastic simulation method 257 258 combining sequential principle and Gaussian method. It assumes variable fit to Gaussian 259 random field. The gauss distribution function is constructed at the each simulated spatial 260 location based on the characteristics of variation function, afterward, randomly selects a 261 value as the variable at the location. In SGS method, observation data are transformed to 262 Gaussian distribution or normal distribution. Based on current sample data, the conditional probability distribution of points to be simulated is calculated by SGS 263 264 method and then simulation is performed based on semivariogram model. Each simulated value, together with measured data and previous simulation data, becomes the 265 conditional data set for the next step. As simulation proceeds, the conditional data set 266 increases. Pervious researches suggested 50-400 realizations are required to obtain a 267 268 statistically stable mean realization (Eggleston et al., 1996; Hu et al., 2007).

269 2.3 Modeling PCE migration and its remediation

The DNAPL migration and remediation are modeled using a multi-component, multi-phase, and multi-composition of contaminant-transport processes simulator named





272 UTCHEM (University of Texas Chemical Compositional Simulator) (Delshad et al., 273 1996). As an extension to Delshad's work, UTCHEM was developed by University of 274 Texas as a comprehensive and practical tool. In numerous applications, UTCHEM has proved to be particularly useful and has been a popular multi-phase flow and 275 276 multi-constituent, reactive transport model used widely in groundwater simulations. UTCHEM account for chemical, physical and biological reactions, complex 277 278 non-equilibrium sorption, decay and geochemical reactions and surfactant-enhanced 279 solubilization and mobilization of DNAPLs, moreover, heterogeneous properties of 280 porous media is addressed. As a result, UTCHEM has been adapted for a variety of 281 environmental applications such as surfactant-enhanced aquifer remediation (SEAR). In 282 this study, DNAPL migration and remediation for cleaning up DNAPL contamination in 283 idealized heterogeneous site are simulated by UTCHEM.

3. Application to a synthetic heterogeneous PCE contaminated site

285 **3.1 Site description**

The idealized domain synthetic application is a two-dimensional confined aquifer saturated by water (Fig. 3). The length, width and depth of aquifer are 101 m, 25 m and 25 m, respectively. Idealized aquifer is discretized into 101 grids horizontally and 25 layers vertically (Fig. 3b). The spacing of each grid is uniformly 1 m along x and zdirections, and the longitudinal and transverse dispersivities are set as to 1.0 m and 0.1 m, respectively. Horizontal and vertical correlation length values is 5 m. The top and bottom borders of aquifer are defined as no-flow boundaries, while the left and right





borders are defined as constant potential boundaries to create a groundwater flow from
left to right under a low hydraulic gradient of 0.005 m/m (Liu et al., 2003; Liu, 2005; Qin
et al., 2007). The porous media of idealized aquifer is assumed to be heterogeneous and
mixed by different grades of sands.

297 The porosity of aquifer is assumed spatially and uniformly distributed with average 298 value of 0.220 and standard deviation of 0.060. In this study, porosity follows normal 299 distribution and its standard deviation (SD) represents the enhanced geological 300 heterogeneity. 200 realizations porosity field are generated using Sequential Gaussian Simulation (SGS). One of the 200 realizations of heterogeneous field is shown in Fig. 4a. 301 302 Simultaneously, statistical assessment is taken on the individual realization of porosity 303 field and corresponding histograms are shown in Fig. 4b. We can find the frequency of 304 the individual realization of porosity field is close to normal distribution, which conform 305 to the fact that most characteristic of natural aquifer can be expressed as normal 306 distribution (Montgomery et al, 1987). Based on the heterogeneous porosity field, the 307 fractal dimension of tortuosity D_t , the fractal dimension for pore areas D_f and the 308 diameter of capillary tube in porous media, permeability is obtained by the Equation (12). Fig. 4c shows the individual heterogeneous permeability field selected from the 309 310 200 realizations of RTA, besides, the result of associated frequency analysis is shown in 311 Fig. 4d. The permeability field fits the lognormal distribution obviously, which has been 312 presented by many researches that the parameter of aquifer penetrability is lognormal 313 distribution field (Montgomery et al., 1987; Veneziano and Tabaei, 2004). Compared to 314 histogram of porosity field in Fig. 4b, the shape of permeability is similar. The individual





heterogeneous permeability field of SPA is shown in Fig. 4e. Corresponding frequency analysis of SPA reveals the permeability field is lognormal distribution, while some difference appears compared with RTA (Fig. 4f). The average permeability of individual realization of RTA is 2.012×10^{-12} m² and the average permeability of individual realization of SPA is 1.618×10^{-12} m². For 200 realizations, the average permeability of RTA and SPA are 2.120×10^{-12} m² and 1.706×10^{-12} m², indicating the permeability of RTA is bigger than SPA slightly.

322 The average pore diameters of two different microscale arrangements of particles 323 are derived using corresponding fractal models. In detail, average diameter of RTA is 324 calculated by Equation (21) and average diameter of SPA is calculated by Equation 325 (39). Consequently, the entry pressure of the two kinds of microscale arrangements 326 can be obtained by Equation (48), respectively. The individual entry pressure fields of 327 two microscale arrangements and associated frequency analysis are shown in Figs. 4g-i. 328 From the frequency of entry pressure in Fig. 4h and Fig. 4j, the entry pressures of both 329 RTA and SPA are the lognormal distributions. However, the average entry pressure of 330 individual realization of RTA is 1.980 kPa, while the average entry pressure of SPA is 331 1.481 kPa. For 200 realizations of entry pressure field, the average entry pressure of RTA is 1.922 kPa and the average entry pressure of SPA is 1.442 kPa. The differences of 332 333 average entry pressure and the entry pressure distributed range between RTA and SPA 334 imply the micro-structure of aquifer has effect on the macroscopic characteristics.

The purpose of this study is to explore the effects of micro-structure of aquifer on DNAPL migration and remediation. A PCE spill event (the leaking of underground





337 storage tank) occurs on the top of the aquifer and a surfactant remediation is desired to 338 clean up the contaminated aquifer. The total duration of 300 days is divided into four 339 stages: (1) 300 m³ PCE is released from underground storage tank into aquifer at the top layer of spill position shown in Fig. 3a during 0~30 days; (2) PCE migrates in aquifer 340 341 freely during 30~100 days; (3) surfactant is injected into aquifer during 100~150 days; and (4) water flushing during 150~300 days. In the first stage, PCE is released as a point 342 343 pollution source in the center grid block at the top layer of the aquifer, which spill is at a 344 constant rate of 10 m³/day. After PCE coming into heterogeneous aquifer, PCE is 345 migrating freely under the effects of gravity and the natural hydraulic gradient condition. 346 The PCE not only migrates downward through the aquifer, but also can be trapped by capillary forces as residual ganglia and globules. During the long-term PCE migration 347 348 period, PCE is contaminating groundwater and expanding plume. To clean up the 349 contaminated aquifer, 4% surfactant solution is injected into aquifer through the two 350 injection wells (Fig. 3b) at a constant rate of 80 m³/day, simultaneously, contaminated groundwater is extracted through production well at constant rate of 160 m³/day. 351 352 Surfactant can reduce the interfacial tension between DNAPL and aqueous phase to promote solubilization and mobilization of DNAPL in aquifer. After surfactant injection, 353 the contaminated aquifer is flushed by water over a long time of 150 days. Based on the 354 355 distributions of porosity, permeability and entry pressure of two microscale arrangements, 356 the entire PCE migration and remediation process is simulated by a multicomponent, 357 multiphase model simulator UTCHEM (Delshad et al., 1996). The parameters used in simulation are listed in Table 1. Simulation results of two different microscale 358





359 arrangements are compared to reveal the effect of microstructure on the DNAPL

360 migration and remediation.

361 **3.2 Results and discussion**

362 **3.2.1 PCE migration and its remediation based on single realizations**

The simulation results of PCE migration for individual realization of porosity field 363 for RTA are shown in Fig. 5a-f. When PCE is released into aquifer into aquifer at the top 364 layer of spill position, PCE almost infiltrates vertically under the effect of gravity force 365 (Fig. 5a). Due to the heterogeneity of aquifer, some preferential flow appears and PCE 366 367 plume becomes irregular (Fig. 5b). After 30 days, PCE plume almost touches the 368 bottom of aquifer (Fig. 5c). When the PCE leakage is stopped, PCE continues to migrate freely in aquifer for 70 days (Fig. 5d-f). The released PCE is migrating 369 370 downward and entrapped by capillary forces as residual ganglia and globules. 371 Heterogeneity of aquifer makes PCE migrate along preferential pathway. When PCE 372 plume touches the zones of low permeability and high entry pressure, it will bypass these zones and migrate continuously, which leads to an increasing variability in PCE 373 374 distribution. After PCE plume reaches the bottom of aquifer, PCE begins accumulate 375 and form contaminant pool at the bottom. At t=100 days, A PCE pool has been formed at the bottom of aquifer, moving toward the right boundary. 376

Figs. 6a-f show the simulated PCE saturation for individual realization of porous media for SPA during migration period. Under the effects of gravity force and natural hydraulic gradient, PCE is migrating and spreading contaminant plume. Heterogeneity





380 of aquifer significantly changes the migration paths and leads to irregular morphology 381 of the PCE plume (Figs. 6a-c). However, due to the different micro-arrangement of 382 aquifer, the entry pressure field also is different which leads to some differences. After the PCE injection, the simulated PCE saturation in Figs. 6d-f indicates that further 383 384 trapping and spreading of the PCE occurs during this period. Compared with the simulation results of RTA in Fig. 5, the PCE plume slightly seems similar in Fig. 6. 385 386 Moreover, PCE infiltrate more quickly in porous media of RTA in Fig. 5. After 70 days, 387 PCE plume has touched the bottom for RTA (Fig. 5e), while PCE plume based on SPA 388 still keeps a significant distance from bottom (Fig. 6e).

389 To clean up the DNAPL, 4% surfactant solution is injected through two injection wells at a constant rate of 80 m^3/day over 50 days to evaluate the effectiveness of 390 391 surfactant flushing. Afterwards, following water-flush is applied during 150~300 day. The location of injection wells and production well are presented in Fig. 3b. The 392 393 production well is rightly installed at the location of the PCE spill position and two injection wells are located 39 m to the left and right of the production well. Figs. 5g-l 394 395 shows the PCE remediation results of individual realization for RTA. During the early remediation period, the effect of cleaning up DNAPL is not yet apparent (Figs. 5g-i). 396 397 When the water flushing begins, the surfactant solution circulates throughout the 398 contaminated aquifer (Figs. 5j-1). At t=200 days, there has been 237.01 m³ PCE 399 removal from contaminated aquifer, occupying 79.00% of the total released PCE (Fig. 5j). As time goes on, 268.30 m³ PCE is removed from aquifer and remediation 400 401 efficiency reaches 89.43%.





402	The same surfactant remediation is also conducted for individual realization of
403	porous media for SPA. Compare with the remediation for RTA, the remediation effect
404	is more apparent for SPA (Figs. 6g-1). As the remediation processes, more DNAPL is
405	removed and less DNAPL is remained as small contaminant pools at the bottom of
406	aquifer. At t=200 day, 267.68 m ³ PCE is removed from contaminated aquifer,
407	corresponding remediation efficiency rise to 89.23%. At t=300 day, 285.32 m ³ PCE is
408	cleaned up and remediation efficiency reaches 95.11%. From results of remediation, it
409	is obvious that microstructure has effect on remediation of macroscopic scale aquifer.
410	Results suggest contaminated aquifer of RTA is hard to clean up by surfactant
411	remediation while SPA can improve DNAPL remediation efficiency.

412 **3.2.2 PCE migration and SGS realizations**

413 PCE migration and remediation processes are simulated for 200 realizations of porosity field for porous media of RTA and SPA. The variations of contaminant mass, 414 415 the ganglia-to-pool ratio (GTP) and moments of PCE plume versus time are presented 416 in Figs. 7a-h. During $0 \sim 30$ day, the PCE in aquifer increases linearly at a constant rate of 10 m3/day (Fig. 7a), which corresponding to contaminant spill stage. Afterward, PCE 417 418 volume keep constant during the second stage ranged 30~100 day, while PCE in 419 aquifer is reduced when surfactant is injected into aquifer. After surfactant and water 420 flushing the contaminated aquifer, most DNAPL is cleaned up. The residual DNAPL mass remained in aquifer of 0.67 m³-119.89 m³ with a mean of 22.42 m³ and 0.79 421 m³-103.33 m³ with a mean of 12.51 m³ are achieve for 200 individual heterogeneous 422





423 realizations based on the RTA and SPA, respectively. The average remediation 424 efficiency of SPA is undoubtedly higher than RTA, indicating the aquifer of SPA is easier 425 to clean up. PCE plume architectures are quantified by measuring the ganglia-to-pool ratio (GTP) in Fig. 7b. Over entire periods, curves of GTP value appear obvious 426 427 oscillations. Surfactant has the ability of promoting solubilization and mobilization of 428 DNAPL can reduce GTP value. As a result, when surfactant is injected at t=100 day, the 429 GTP value reduces quickly. When surfactant injection is end and water flushing begins, 430 the GTP value increases with steep flank slope. At last, GTP values reach 0.10-0.41 with 431 a mean of 0.21 and 0.15-0.42 with a mean of 0.28 for 200 individual heterogeneous 432 realizations based on the RTA and SPA, respectively.

433 Fig. 7c shows cumulative PCE removal from contaminated aquifer versus flushing 434 time for RTA and SPA. During the surfactant injection period ranged 100~150 day, the 435 DNAPL removal is not apparent, However, DNAPL is removed effectively and quickly during water flushing period. Through long time remediation, the removal PCE from 436 contaminated aquifer reach 179.89 m³-298.98 m³ with a mean of 277.29 m³ and 196.45 437 m³-298.87 m³ with a mean of 287.21 m³ for 200 realizations based on RTA and SPA, 438 respectively. Average remediation efficiency of SPA (95.83%) is obvious higher than 439 average remediation efficiency of RTA (92.52%). 440

Fig. 7d shows the GTP value as a function of cumulative PCE removal for contaminated aquifer. The GTP remains at a relatively low level before 30% of the DNAPL is removed from aquifer. When 40% of the total 300 m³ PCE are removed, GTP values are increasing and corresponding curves appear a wave crest because the high





- saturation zone of PCE plume are dissolved and turned into ganglia state. After the wave
 crest, the GTP values decline quickly with steep flank slope due to PCE ganglia removal
 through water flushing. At last, GTP values increase at the end of remediation process for
 200 realizations, indicating most of PCE is removed and most of residual PCE turn to
 ganglia state.
- 450 For the center of PCE plume in horizontal axis, associated variations versus time are 451 similar for 200 realizations based on RTA and SPA (Fig. 7e). Significantly, the PCE 452 plume vertical infiltration rate in aquifer of RTA is slightly faster than PCE infiltration in 453 aquifer of SPA for 200 realizations (Fig. 7f). Simultaneously, the second PCE plume 454 moments in horizontal direction of RTA are different from SPA (Fig. 7g). After PCE migration at natural condition at 100 day, the second PCE plume moments in horizontal 455 456 direction are 10.61 m²-40.50 m² with a mean of 21.51 m² and 10.99 m²-36.38 m² with a mean of 20.75 m² for 200 realizations based on RTA and SPA, respectively. At t=300 day, 457 the second PCE plume moments in horizontal direction change to 0.81 m^2 -34.88 m² with 458 a mean of 5.79 m² and 1.03 m²-24.57 m² with a mean of 4.64 m² for RTA and SPA, 459 460 respectively. The horizontal second moment of RTA is always larger than horizontal second moment of SPA, indicating the PCE plume in aquifer of RTA is wider than PCE 461 plume in aquifer of SPA and RTA can cause larger range of groundwater contamination. 462 Similarly, the second moments in vertical direction of RTA are larger than the second 463 464 moments in vertical direction of SPA.
- 465 **4. Conclusions**

466 The micro-structure of aquifer has important effect on macroscopic scale





467 characteristics of aquifer and inner contaminant migration and remediation. In this study, 468 we focus on the DNAPL migration and remediation in heterogeneous aguifer composed of granular porous media with RTA and SPA. The microscale models of RTA and SPA 469 are developed to obtain the mathematical expressions of permeability and entry pressure 470 471 using fractal method. 200 realizations of porosity field are generated using SGS method 472 and PCE is released from underground storage tank into heterogeneous aquifer. To clean 473 up contamination caused by underground storage tank spill, surfactant remediation 474 technique is used to remove contaminants in aquifer. The entire process of DNAPL 475 migration and remediation is simulated by a multicomponent, multiphase model 476 simulator UTCHEM. Results suggest RTA not only cause larger range of groundwater contamination than RTA, but also the contaminated aquifer of RTA is harder to clean up 477 478 compared with SPA. The second PCE plume moments in horizontal direction are 10.61 m^2 -40.50 m^2 with a mean of 21.51 m^2 and 10.98 m^2 -36.38 m^2 with a mean of 20.75 m^2 479 for 200 realizations based on RTA and SPA after PCE natural migration at t=100 day, 480 respectively. Furthermore, the second PCE plume moments in horizontal direction at 481 482 t=300 day are 0.807 m²-34.88 m² with a mean of 5.79 m² and 1.025 m²-24.57 m² with a mean of 4.64 m² for RTA and SPA respectively after long time remediation. 483 Simultaneously, the residual DNAPL mass remained in aquifer are 0.67 m³-119.89 m³ 484 with a mean of 22.42 m³ and 0.79 m³-103.33 m³ with a mean of 12.51 m³ for RTA and 485 486 SPA respectively, indicating remediation efficiency of SPA (65.53%-99.74% with a mean of 95.83%) mostly is higher than remediation efficiency of RTA (60.01%-99.78% with a 487 488 mean of 92.52%). This study proves microstructure of aquifer has important effect on





- 489 contaminant movement and associated remediation efficiency in macroscopic scale
- 490 aquifer, which is very essential and significant for dealing with the accidental event of
- 491 underground storage tank spill and identifying subsurface contaminant source in the
- 492 future.
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498 **References**

- 499 Ahn, K.J., Seferis, J.C.: Simultaneous measurements of permeability and capillary
- pressure of thermosetting matrices in woven fabric reinforcements, Polym.
 Composite., 12, 146-152, 1991.
- 502 Bakshevskaia, V.A., Pozdniakov, S.P., Simulation of hydraulic heterogeneity and

503 upscaling permeability and dispersivity in Sandy-Clay foormations, Math.

- 504 Geosci., 48, 45-64, 2016.
- 505 Bear, J.: Dynamics of fluids in porous media, Dover, New York, 1972.
- 506 Bob, M.M., Brooks, M.C., Mravik, S.C., Wood, A.L.: A modified light transmission
- 507 visualization method for DNAPL saturation measurements in 2-D models, Adv.
- 508 Water Resour., 31, 727-742, 2008.
- 509 Boswinkel, J.A.: International Groundwater Resources Assessment Centre (IGRAC),





510	Netherland Institute of Applied Geoscience, Netherlands, 2000.
511	Cui, Q.L., Wu, H.N., Shen, S.L., Yin, Z.Y., Horpibulsuk, S.: Protection of neighbour
512	buildings due to construction of shield tunnel in mixed ground with sand over
513	weathered granite, Environ, Earth Sci., 75, 458, 2016.
514	C.Carroll, K., McDonald, K., Marble, J., Russo, A.E., Brusseau, M.L.: The impact of
515	transitions between two-fluid and three-fluid phases on fluid configuration and
516	fluid-fluid interfacial area in porous media, Water Resour. Res., 51, 7189-7201,
517	2015.
518	Dawson, H.E., Roberts, P.V.: Influence of Viscous, Gravitational, and Capillary Forces
519	on DNAPL Saturation, Groundwater, 35(2), 261-269, 1997.
520	Delshad, M., Pope, G.A., Sepehrnoori, K.: A compositional simulator for modeling
521	surfactant enhanced aquifer remediation, 1 Formation, J. Contam. Hydrol., 23,
522	303-327, 1996.
523	Eggleston, J.R., Rojstaczer, S.A., Peirce, J.J.: Identification of hydraulic conductivity
524	structure in sand and gravel aquifers: Cape Cod data set, Water Resour. Res., 32,
525	1209–1222, 1996.
526	Essaid, H.I., Bekins, B.A., Cozzarelli, I.M., Organic contaminant transport and fate in the
527	subsurface: Evolution of knowledge and understanding, Water Resour. Res., 51,
528	4861-4902, 2015.
529	Feng, Y.J., Yu, B.M.: Fractal dimension for tortuous streamtubes in porous media,
530	Fractals, 15, 385-390, 2007.
531	Hadley, P.W., Newell, C .: The New Potential for Understanding Groundwater





- 532 Contaminant Transport, Groundwater, 52(2), 174-186, 2014.
- 533 Hu, K., White, R., Chen, D., Li, B., Li, W.: Stochastic simulation of water drainage at the
- field scale and its application to irrigation management, Agr. Water Manage., 89,
- 535 123-130, 2007.
- 536 Huang, J.Q., Christ, J.A., Goltz, M.N., Demond, A.H.: Modeling NAPL dissolution
- from pendular rings in idealized porous media, Water Resour. Res., 51, 8182-8197,
- 538 2015.
- 539 Katz, A.J., Thompson, A.H.: Fractal sandstone: Implications for conductivity and pore
- 540 formation, Phys. Rev. Lett., 54, 325-332, 1985.
- 541 Krohn, C.E.: Sandstone fractal and Euclidean pore volume distributions, J. Geophys.
- 542 Res., 93, 3286-3296, 1988.
- 543 Liang, C., Hsieh, C.L.: Evaluation of surfactant flushing for remediating EDC-tar
- 544 contamination, J. Contam. Hydrol., 177-178, 158-166, 2015.
- 545 Liang, C., Lai, M.C.: Trichloroethylene degradation by zero valent iron activated
- 546 persulfate oxidation, Envrion. Eng. Sci., 25(7), 1071-1077, 2008.
- 547 Liu, H., Li, Y.X., He, X., Sissou, Z., Tong, L., Yarnes, C., Huang, X.: Compound-specific
- 548 carbon isotopic fractionation during transport of phthalate esters in sandy aquifer,
- 549 Chemosphere, 144, 1831-1836, 2016.
- 550 Liu, L.: Modeling for surfactant-enhanced groundwater remediation processes at
- 551 DNAPLs-contaminated sites, J. Environ. Inform., 5(2), 42-52, 2005.
- 552 Liu, L., Hao, R.X., Cheng, S.Y.: A possibilistic analysis approach for assessing
- 553 environmental risks from drinking groundwater at petroleum-contaminated sites,





554	J. Environ. Inform., 2(1), 31-37, 2003.
555	Liu, Y., Wang, S., McDonough, C.A., Khairy, M., Muir, D.C.G., Helm, P.A., Lohmann,
556	R.: Gaseous and freely-dissolved PCBs in the lower great lake based on passive
557	sampling: spatial trends and air-water exchange, Environ. Sci. Technol., 50,
558	4932-4939, 2016.
559	Pfeifer, P., Avnir, D.: Chemistry in Nonintegral dimensions between two and three. I .
560	Fractal theory of heterogeneous surface, J. Chem. Phys., 79, 3558-3565, 1983.
561	Qin, X.S., Huang, G.H., Chakma, A., Chen, B., Zeng, G.M.: Simulation-based process
562	optimization for surfactant-enhanced aquifer remediation at heterogeneous
563	DNAPL-contaminated sites, Sci. Total Environ., 381, 17-37, 2007.
564	Schaefer, C.E., White, E.B., Lavorgna, G.M., Annable, M.D.: Dense nonaqueous-phase
565	liquid architecture in fractured bedrock: implications for treatment and plume
566	longevity, Environ. Sci. Technol., 50, 207-213, 2016.
567	Valipour, M.: Comparison of surface irrigation simulation models: Full hydrodynamic,
568	zero inertia, kinematic wave, J. Agr. Sci., 4(12), 68-74, 2012.
569	Valipour, M.: Future of agricultural water management in Africa, Arch, Agron. Soil Sci.,
570	61(7), 907-927, 2015.
571	Valipour, M., Singh, V.P.: Global experiences on wastewater irrigation: challenges and
572	Prospects, in: Maheshwari, B., Singh, V.P., Thoradeniya, B., Balanced urban
573	development: options and strategies for liveable cities, Volume 72 of the series
574	Water Science and Technology Library, pp. 289-327, 2016.
575	Veneziano, D., Tabaei, A.: Nonlinear spectral analysis of flow through porous media with





- 576 isotropic lognormal hydraulic conductivity, J. Hydrol., 294, 4-17, 2004.
- 577 Weathers, T.S., Harding-Marjanovic, K., Higgins, C.P., Alvarez-Cohen, L., Sharp, J.O.:
- 578 Perfluoroalkyl acids inhibit reductive dechlorination of Trichloroethene by
- 579 repressing dehalococcoides, Environ. Sci. Technol., 50, 240-248, 2016.
- 580 Yannopoulos, S.I., Lyberatos, G., Theodossiou, N., Li, W., Valipour, M., Tamburrino, A.,
- 581 Angelakis, A.N.: Evolution of water lifting devices (pumps) over the centuries
- 582 worldwide, Water, 7, 5031-5060, 2015.
- 583 Yu, B.M.: Fractal character for tortuous streamtubes in porous media, CHIN. PHYS.
- 584 LETT., 22, 158-160, 2005.
- 585 Yu, B.M., Cai, J.C., Zou, M.Q.: On the physical properties of apparent two-phase fractal
- 586 porous media, Vadose Zone J., 8, 177-186, 2009.
- 587 Yu, B.M., Cheng, P.: Fractal models for the effective thermal conductivity of bidispersed
- 588 porous media, J. Thermophys. Heat Tr., 16, 22-29, 2002.
- 589 Yu, B.M., Li, J.H.: A geometry model for tortuosity of flow path in porous media, CHIN.
- 590 PHYS. LETT., 21, 1569-1571, 2004.
- 591 Yun, M.J., Yu, B.M., Zhang, B., Huang, M.T.: A geometry model for tortuosity of
- 592 streamtubes in porous media with spherical particles, CHIN. PHYS. LETT.,
- 593 22(6), 1464-1467, 2005.
- 594





595 **Table 1.** Parameters used in simulation

Parameter	Value
Average value of porosity	0.22
Standard deviation of porosity	0.06
Longitudinal dispersivity	1.0 m
Transverse dispersivity	0.1 m
Hydraulic gradient	0.005 m/m
Water density	1.00 g/cm ³
PCE density	1.63 g/cm ³
Surfactant density	1.15 g/cm^3
Water viscosity	1.00 cp
PCE viscosity	0.89 cp
PCE/ Water interfacial tension	45 dyn/cm
PCE solubility in water	240 mg/L
Residual water saturation	0.24
Residual PCE saturation	0.17
Endpoint of Water (BC model)	0.486
Endpoint of PCE (BC model)	0.65
Exponent of Water (BC model)	2.85
Exponent of PCE (BC model)	2.7
Exponent of capillary pressure	-0.52

596





598 599	Figure Captions
600	Figure 1. Two different microscale arrangements of solid particles: (a) RTA; and (b) SPA
601	Figure 2. Three kinds of Sierpinkski gasket [30]: (a) $L_a=2$; (b) $L_a=3$; and (c) $L_a=5$
602	Figure 3. (a) Two-dimensional view of contaminated domain; and (b) locations of
603	injection extraction wells
604	Figure 4. (a) The individual porosity field generated by Sequential Gaussian Simulation
605	(SGS) method; (b) the frequency of individual porosity field; (c) the individual
606	permeability field of RTA obtained from individual porosity field; (d) the
607	frequency of individual permeability field for RTA; (e) the individual
608	permeability field of SPA obtained from individual porosity field; (f) the
609	frequency of individual permeability field for SPA; (g) The obtained individual
610	entry pressure field of RTA; (h) the frequency of individual entry pressure field
611	of RTA; (i) the obtained individual entry pressure field of SPA; and (j) the
612	frequency of individual entry pressure of SPA
613	Figure 5. Simulated PCE saturation for individual realization of RTA over the entire
614	migration and remediation periods (0~300 day)
615	Figure 6. Simulated PCE saturation for individual realization of SPA over the entire
616	migration and remediation periods (0~300 day)
617	Figure 7. (a) PCE volume in aquifer versus time, RTA represents RTA and SPA
618	represents SPA; (b) Changes in GTP as a function of time; (c) Cumulative
619	DNAPL removal as a function of time; (d) Variation of GTP value as a function
620	of cumulative DNAPL removal percent; (e) the change of the center of PCE





621	plume during the entire periods of migration and remediation; (f) the change of
622	the depth of PCE plume center during the entire periods; (g) variation of second
623	PCE plume moment in horizontal axis; and (h) variation of second PCE plume
624	moment in vertical axis
625	
626	





























648 **Figure 5**

649







652 Figure 6

653







656 Figure 7

