



Incorporation of the equilibrium temperature approach in a Soil and Water Assessment Tool hydroclimatological stream temperature model

Xinzhong Du¹; Narayan Kumar Shrestha¹; Darren L. Ficklin²; Junye Wang^{1*}

5 **1 Athabasca River Basin Research Institute (ARBRI), Athabasca University, 1 University Drive, Athabasca, Alberta T9S 3A3, Canada**

2 Department of Geography, Indiana University, Bloomington, Indiana, USA

*Correspondence to: junyew@athabascau.ca

Abstract

10 Stream temperature is an important indicator for biodiversity and sustainability in aquatic ecosystems. The stream temperature model currently in the Soil and Water Assessment Tool (SWAT) only considers the impact of air temperature on stream temperature, while the hydroclimatological stream temperature model developed within SWAT model considers hydrology and the impact of air temperature in
15 simulating the water-air heat transfer process. In this study we propose using the equilibrium temperature approach to model complex heat transfer processes at the water-air interface, which reflects the influences of air temperature, solar radiation, wind speed and stream water depth on the heat transfer process. The thermal capacity of the streamflow is modelled by the variation of the stream water depth. An advantage of this equilibrium temperature model is the simple parameterization, with only two added parameters to model the heat transfer processes. The equilibrium temperature model is applied and tested in the
20 Athabasca River Basin (ARB) in Alberta, Canada. The model is calibrated and validated at five stations throughout different parts of the ARB for which high-frequency observed stream temperature data are available. The results indicate that the equilibrium temperature model provided better and more consistent performances for the different regions of the ARB with the values of Nash-Sutcliffe Efficiency (> 0.67) greater than those of the original SWAT model and the hydroclimatological model. Overall, the
25 equilibrium temperature model uses existing SWAT meteorological data as input, can be calibrated using fewer parameters and less effort, and has an overall better performance for the simulation of daily stream temperatures. Thus, it can be used as an effective tool for predicting the change in stream temperature regimes under varying hydrological and meteorological conditions. In addition, the impact of the stream temperature simulations on chemical reaction rates and concentrations was tested. The results indicate
30 that the improved performance of the stream temperature simulation could significantly affect chemical reaction rates and the simulated concentrations and the equilibrium temperature model could be a potential tool to model stream temperature for water quality simulations.

Keywords: SWAT model, stream water temperature, equilibrium temperature, Athabasca River Basin

1. Introduction

35 Stream temperature is an important factor in assessing the water quality condition and biodiversity health. Stream temperature can alter physical and chemical properties of the water bodies. It has effects on water density, conductivity, pH, dissolved oxygen concentration, compound toxicity, chemical reaction rates, biological activity and biological habitats. All aquatic species has a specific range of water temperature that they can tolerate and any changes in water temperature may have an adverse impact on
40 the habitat of aquatic species (Caissie et al., 2007). For example, a fish species in a stream is likely to



migrate if the maximum weekly stream temperature exceeds its temperature tolerance (Eaton et al., 1995). Also, a fish species could perish due to osmoregulatory dysfunction if weekly stream temperature drops below a threshold temperature (Mohseni et al., 1998). Stream temperature regimes have been and will continue to be affected by anthropogenic activities, especially landuse and climate change. Land use changes, such as deforestation and urbanization have an impact on watershed hydrological conditions that can lead to stream temperature changes (Cao et al., 2016). Moreover, the possible rise of water temperature due to global warming caused by climate change is expected to affect aquatic species directly and indirectly (Hardenbicker et al., 2017; Ducharme, 2008). Therefore, it is important to model stream temperature for predicting the changes in temperature under varying hydrological and meteorological conditions.

Many stream temperature models have been developed over the past years, which can be classified into mechanistic and statistical models. A mechanistic model is based on energy balance while a statistical model uses regression techniques between stream temperature and meteorological or other physical variables such as geology. Statistical models are easy to use with less input data required but several drawbacks exist. Firstly, the statistical models of stream temperature are highly dependent upon model assumptions and curve regression techniques. It is well known that the statistical methods are problematic because different combinations of the parameters could yield similar curves. For example, widely used statistical models of stream temperature are regressed linearly or nonlinearly using only air temperature as an input parameter. Stefan et al. (1993) used a linear model between the stream and air temperatures with time lags to simulate daily and weekly water temperatures in 11 streams in the Mississippi River basin in the central US. Mohseni et al. (1998) developed a four-parameter nonlinear function using air temperature as the input to model weekly stream temperatures based on temperatures recorded over a 3-year period (1978-1980) at 584 U.S. Geological Survey gauging stations in the contiguous United States. Sohrabi et al. (2017) developed a parsimonious Bayesian regression approach to model daily stream temperatures accounting for the temporal autocorrelation, linear and nonlinear relationships with air temperature and discharge. However, stream temperature is clearly subject to other meteorological and hydrological constraints, such as solar radiation, wind speed and water depth, which cannot be reflected by the simple regression approach. Moreover, the impact of watershed hydrological conditions are not included in these regression models (Ficklin et al., 2012). Therefore, the statistical models of stream temperature may not be reliable when interpreting and predicting the impact of environmental and anthropological drivers, such as climate and landuse change.

Mechanistic stream temperature models simulate the change of stream temperature based on energy balances of heat fluxes and water mass balance in a river system (Brennan, 2015). Heat transfer and stream temperature are calculated at the water-air interface and water-sediment interface. Heat exchange between sediment and water is generally small compared to air-water heat exchange (Caissie et al., 2007) and can often be negligible. At the water-air interface, heat flux can be calculated using solar radiation, net long-wave radiation, evaporation, and convective heat transfer. As stream temperatures impact the chemical reaction rates in the aquatic environment, widely used water quality models, such as QUAL2K (Chapra et al., 2012) and CE-QUAL-W2 (Cole et al., 2016), have the capability to model stream temperature based on a full energy balance approach. These models require hydrological conditions represented by flow rates and stream temperature from tributaries as input boundary conditions to model stream temperature in the mainstream based on a full energy balance approach, and therefore, they cannot directly project the effects of watershed hydrological conditions on stream temperature. Some researchers have tried to incorporate physical based energy balances into the hydrological models to simulate stream temperature. For example, Ozaki et al. (2008) developed a river temperature model based on a multi-layer mesh-type runoff model to calculate the heat budget in the landscape and river system. Battin et al. (2007)



added a heat balance module to the Distributed Hydrology-Soil-Vegetation Model (DHSVM) to model stream temperatures in the Snohomish Basin. However, because of their complexity, these mechanistic models require intensive data and calibration effort, which to some extent, can limit their applicability (Du et al., 2014).

5 Ficklin et al. (2012) developed a hydroclimatological stream temperature model within the Soil and
Water Assessment Tool (SWAT) hydrological model (Arnold et al., 1998), which includes the combined
effects of watershed hydrological conditions and air temperature. The effects of watershed hydrological
conditions are modelled by mixing local subbasin runoff components (surface runoff, lateral flow,
10 snowmelt and groundwater flow) and upstream inflow to calculate the initial temperature in the stream.
Then, the heat transfer at water-air interface was calculated using the difference between initial stream
temperature and air temperature. This model was tested and validated in seven coastal and mountainous
basins in the western U.S., showing much better stream temperature simulation performance compared to
the original linear regression approach of SWAT (Ficklin et al., 2012). It had also been used to assess the
15 impact of climate change on stream temperature in the Columbia River basin in North America (Ficklin et
al., 2014) and Sierra Nevada mountain range in California (Ficklin et al., 2013). Zeiger et al. (2016)
applied the hydroclimatological model in a mixed-use, urbanizing watershed in the central U.S. and
compared the model performance with the linear and non-linear regression models. Their results showed
that it had a better and more consistent performance both in lower and higher stream temperature ranges.
20 The hydroclimatological model explicitly describes the effects of hydrological inputs (local runoff
components and upstream inflow) on stream temperature for evaluating the impact of hydrological
changes caused by climate or landuse changes on stream temperature. However, the process of water-air
heat transfer is modelled by considering only the impact of air temperature. The water-air heat transfer
can be simulated based on the full energy balance, but more input data and calibration will be required
because of the model complexity. The equilibrium temperature approach, which includes the impact of air
25 temperature, solar radiation, and wind speed and stream water depth (Bogan et al., 2003; Mohseni and
Stefan, 1999) is an alternative for simulating heat transfer processes. Although many studies have used the
equilibrium temperature concept to interpret thermal processes in rivers, it has rarely used for the
simulation of stream temperature (Caissie et al., 2005). The equilibrium temperature approach is a
compromise between an empirical statistical and a complex mechanistic model. It has moderate data input
30 requirements and has potential to be an effective modelling tool for stream temperature. Therefore, the
equilibrium temperature approach is incorporated into this hydroclimatological model to improve the
simulation of heat transfer process at the water-air interface.

The primary objective of this paper is to develop a stream temperature model in the SWAT framework
to improve the simulation of heat transfer processes and stream temperature by using an equilibrium
35 temperature approach. The equilibrium temperature model uses existing SWAT meteorological input data
and a simple parameterization scheme with only two added parameters to model heat transfer processes at
water-air interface. It not only includes the effects of air temperature, solar radiation and wind speed, but
also incorporates variations in thermal capacity of streamflow represented by stream water depth. The
SWAT model is calibrated for hydrology and the equilibrium model is then calibrated and validated
40 against observed daily stream temperature data at five different stations throughout the upper, middle and
lower regions of the Athabasca River Basin (ARB), located Alberta and Saskatchewan, Canada.

2. Materials and Methods

2.1 Study area



The Athabasca River originates in the Rocky Mountains of Alberta and travels northeast across Alberta (Figure 1). The ARB includes the urban centers of Jasper, Hinton, Whitecourt, Athabasca and Fort McMurray before draining into Lake Athabasca. The entire ARB is approximately 159000 km², which is about 24% of Alberta's landmass. Forest is the dominating land cover accounting for about 82% of the whole basin area, and agriculture land (9.5%) stands at a second. Major activities in the basin include forestry, agriculture, tourism, pulp mills, coal mining, traditional oil and gas extraction, and oil sands mining. Within the ARB, fish species can be broadly grouped into two primary types: those tolerant of cold waters and those which require relatively warmer water temperatures (Wallace and McCart, 1984). The main fish species include walleye, lake whitefish, northern pike, and burbot (Lebel et al., 2011).

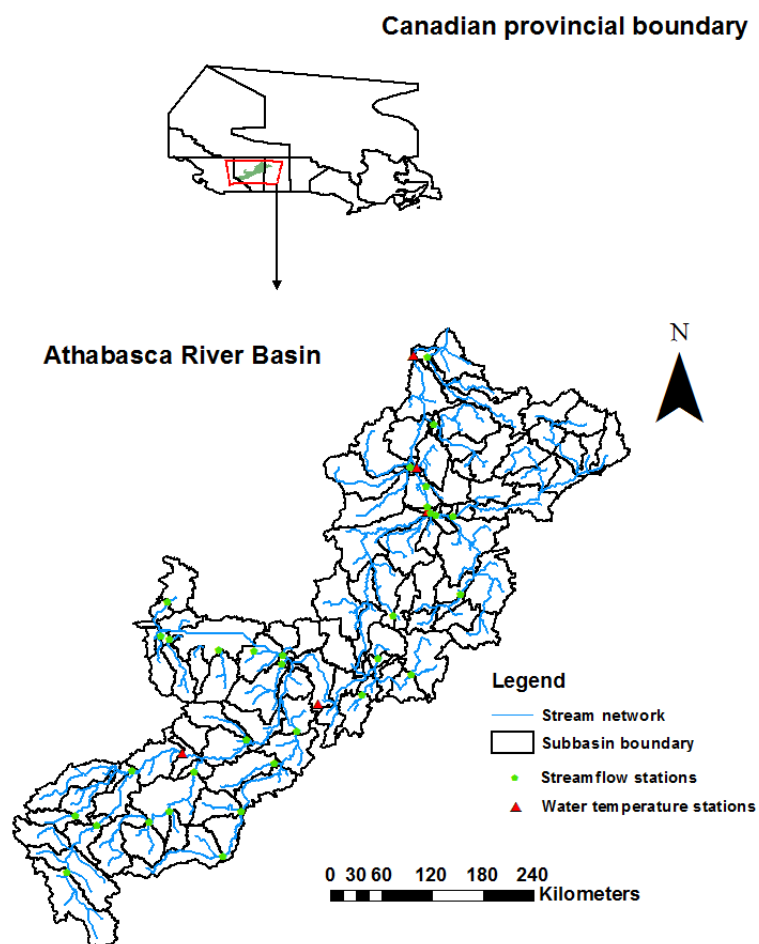


Fig. 1. Location of Athabasca River Basin with streamflow and water temperature stations.



2.2 SWAT hydrological and stream temperature model

Meteorological data and spatial dataset are required for setting up the SWAT model in ARB. The spatial datasets include a digital elevation model (DEM), landuse data and soil data. The Shuttle Radar Topography Mission (SRTM) DEM data (90m×90m), Global Land Cover Characterization based land use map of 1km × 1km spatial resolution (Loveland et al., 2000) and 1:1 million scale soil map from the Agriculture and Agri-Food Canada were used as model input. The DEM was used to delineate subbasin and stream networks, where a total of 131 subbasins were delineated in the ARB. Eleven different landuse classes and 320 different soil types were defined for the model setup. A total of 1370 HRUs were defined based on the landuse, soil and slope classifications. For meteorological data input, daily precipitation, maximum air temperature and minimum air temperature were obtained from 73 stations recorded by Environmental Canada and Climate Change. Relative humidity, solar radiation, and wind speed data at 230 stations recorded by Climate Forecast System Reanalysis (Dile and Srinivasan, 2014) were also used as the model input data.

The SWAT model is a river basin or watershed scale model used to predict the impact of land management practices on water, sediment and agricultural chemical yields in large complex watersheds with varying conditions over long periods of time (Neitsch et al., 2011). The hydrological cycle simulated by SWAT is based on water balance, and the simulated processes include canopy interception, surface runoff, infiltration, lateral flow, snowmelt flow, evapotranspiration, deep percolation, groundwater flow and water routing in the stream and other water bodies. Snowpack accumulation and snowmelt processes are modelled using a temperature index-based approach. More detailed description of SWAT theory is available from Neitsch et al. (2011).

The SWAT model uses a linear equation developed by Stefan and Preudhomme (1993) to calculate average daily temperature for a well-mixed stream:

$$T_{water} = 5.0 + 0.75 \cdot T_{air} \quad (1)$$

where T_{water} is the stream temperature for the day (°C), and T_{air} is the average air temperature on the day (°C). This equation assumes that the lag time between air and stream temperatures is less than one day. However, aside from air temperature, the stream temperature is influenced by other factors, such as solar radiation, wind speed, relative humidity, water depth, artificial heat inputs, groundwater inflow and thermal conductivity of the sediments. The impacts of these factors on stream temperature are not taken into account in the existing SWAT model versions. Therefore, this simple linear equation may lead to unrealistic estimates of stream water temperature when the air temperature is low during winter in cold regions like the ARB.

2.3 SWAT hydroclimatological stream temperature model

The hydroclimatological stream temperature model developed by Ficklin et al. (2012) is used to simulate the combined impacts of air temperature and hydrological inputs (streamflow, snowmelt, groundwater, surface runoff, and lateral soil flow) on stream temperature. Three components are considered in this stream temperature model, including temperature and water contribution within the subbasin, the temperature and volume of inflows from upstream subbasin(s) and heat transfer at the water-air interface during the streamflow transport in the subbasin. In the first step, the temperature of the local water contribution is calculated within the local subbasin using a basic mixing model of the volumes and temperatures of surface runoff, lateral flow, and groundwater, and snowmelt runoff to the stream water:



$$T_{w,local} = \frac{(T_{snow} \cdot sub_snow) + (T_{gw} \cdot sub_gw) + (\lambda T_{air,lag})(sub_surq + sub_latq)}{sub_wyld} \quad (2)$$

where sub_snow is the snowmelt runoff contribution to streamflow within the subbasin (m^3d^{-1}), sub_gw is the groundwater flow contribution to streamflow within the subbasin (m^3d^{-1}), sub_surq is the surface runoff contribution to streamflow within the subbasin (m^3d^{-1}), sub_latq is the soil lateral flow contribution to streamflow within the subbasin (m^3d^{-1}), sub_wyld is the total water yield contribution to streamflow within the subbasin (m^3d^{-1}), T_{snow} is the temperature of snowmelt runoff ($0.1^\circ C$), T_{gw} is the groundwater flow temperature ($^\circ C$), $T_{air,lag}$ is the average daily air temperature with a lag ($^\circ C$), and λ is a calibration coefficient.

In the second step, the initial stream temperature before calculating heat transfer between air and water is then calculated as a weighted average of contributions within the subbasin and the contribution from the upstream subbasin(s):

$$T_{w,initial} = \frac{T_{w,up}(Q_{outlet} - sub_wyld) + T_{w,local} \cdot sub_wyld}{Q_{outlet}} \quad (3)$$

where $T_{w,up}$ is the temperature of the streamflow entering the subbasin from upstream subbasin(s) and Q_{outlet} is the streamflow discharge at the outlet of the subbasin. In the case of headwater streams without inflow, $T_{w,up} = T_{w,initial}$.

In the third step, the final stream temperature is calculated by adding a change caused by heat transfer to the initial stream temperature. This change is calculated based on the temperature difference between the stream and air, and the water travel time through the reach in the subbasin. It is given by the following equations, depending on T_{air} :

$$T_w = T_{w,initial} + (T_{air} - T_{w,initial}) \cdot K \cdot TT \quad \text{if } T_{air} > 0 \quad (4)$$

$$T_w = T_{w,initial} + [(T_{air} + \varepsilon) - T_{w,initial}] \cdot K \cdot TT \quad \text{if } T_{air} < 0 \quad (5)$$

where T_{air} is average daily temperature, K (1/h) is a bulk coefficient of the heat transfer and ranges from 0 to 1, TT is the water travel time in the stream (hour) and is simulated by the SWAT stream routing module, and ε is air temperature addition coefficient, which is included to account for water temperature pulses when air temperature is below $0^\circ C$. ε allows the simulated stream temperature to rise above $0^\circ C$ when air temperature is below $0^\circ C$. K is the critical parameter for calculating the heat transfer, which is dependent on the relationship between stream and air temperature within a subbasin.

2.4 Incorporating the equilibrium temperature approach into Ficklin et al. (2012)

The change of stream temperature can be modelled based on an energy balance accounting for the heat exchange between water-air and water-sediment interface. Stream temperature increases or decreases with time according to the net heat flux:

$$\rho_w C_{pw} \frac{\partial T_w}{\partial t} = \frac{q_{net}}{H} \quad (6)$$

where ρ_w is the density of water (kg/m^3), C_{pw} is the specific heat capacity of water, q_{net} is the net heat flux (W/m^2) and H is the water depth (m), which is calculated by the SWAT stream routing module.



The equilibrium temperature is defined as a hypothetical water temperature at which the net heat flux is zero. The net heat input is assumed to be proportional to the difference between the stream temperature and the equilibrium temperature:

$$\rho_w C_{pw} \frac{\partial T_w}{\partial t} = \frac{K_T (T_e - T_w)}{H} \quad (7)$$

5 where K_T is overall heat exchange coefficient ($\text{W}/\text{m}^2/^\circ\text{C}$) and T_e is the equilibrium temperature ($^\circ\text{C}$).

The overall heat exchange coefficient can be calculated from the empirical relationships that include wind velocity, dew point temperature and initial stream temperature $T_{w,initial}$ (Edinger et al., 1974).

$$K_T = 4.5 + 0.05 T_w + \beta \cdot f(wnd) + 0.47 f(wnd) \quad (8.a)$$

$$f(wnd) = 9.2 + 0.46 wnd^2 \quad (8.b)$$

$$10 \quad \beta = 0.35 + 0.015 \left(\frac{T_d + T_w}{2} \right) + 0.0012 \left(\frac{T_d + T_w}{2} \right)^2 \quad (8.c)$$

where T_d is the dew point temperature ($^\circ\text{C}$), wnd is the wind speed (m/s), which is an input meteorological data of the SWAT model. The equilibrium temperature can be calculated by the empirical relationship of the overall heat exchange coefficient, the dew point temperature and the solar radiation (below) (Edinger et al., 1974):

$$15 \quad T_e = T_d + \frac{slr}{K_T} \quad (9)$$

where slr is the solar radiation, which is also an input meteorological data of the SWAT model.

In equations 8 and 9, the dew point temperature is required when calculating the heat exchange coefficient and equilibrium temperature. Because the dew point temperature is not an input meteorological data of the SWAT model, it can be estimated by air temperature and relative humidity using a simple linear equation or non-linear equation (Lawrence, 2005). Also, Dingman (1972) used air temperature and solar radiation to calculate the equilibrium temperature instead of the dew point temperature in equation 9. In this study, air temperature and an additive parameter ($T_{air} + \eta$) are used to replace the dew point temperature T_d in equation 8 and 9, therefore the dew point temperature is not required as an input data. The η is an additive parameter, which is subject to model calibration using observed stream temperature data. Therefore, the equilibrium temperature approach proposed here can calculate the water-air heat transfer using SWAT existing input data, which considers the impact of air temperature, solar radiation, wind speed and water depth. The final stream temperature is corrected using the equilibrium temperature of the influence of heat transfer to the initial stream temperature. Combining equations 8 and 9 into equation 4 yields:

$$30 \quad T_w = T_{w,initial} + \frac{K_T (T_e - T_{w,initial})}{\rho_w C_{pw} H} \cdot TT \quad (10)$$

where T_w is the stream temperature after the water-air heat transfer calculation using the equilibrium temperature, $T_{w,initial}$ is the initial stream temperature by mixing water from upstream and the local subbasin. The equilibrium temperature T_e is calculated in the below formula using the air temperature rather than the dew point temperature:



$$T_e = (T_{air} + \eta) + \frac{slr}{K_T} \quad (11)$$

where η is the additive parameter for the water-air heat transfer process. Heat exchange coefficient K_T is calculated using equation 8 with $(T_{air} + \eta)$ replacing dew point temperature T_d .

2.5 Model calibration and validation

5 The SWAT model was used for the simulation of streamflow and stream temperatures for a 34 year period, from 1980 to 2013. The first two years (1980-1981) were used as a warm up period to minimize the impact of initial conditions. The model calibration period was from 1990 to 2005 (16 years) including both wet and dry periods. The years of 1982 to 1989 and 2006 to 2013 were used for the model validation. SWAT-CUP and its SUFI-2 algorithm were used for streamflow calibration and validation (Shrestha et al.,
10 2017). For streamflow, daily time series data from 35 stations collected from Environmental Canada and Climate Change were used for the hydrological calibration and validation. The streamflow was calibrated from upstream to downstream according to the locations of 35 flow gauging stations. The Nash-Sutcliffe Efficiency (NSE) was selected as the objective function for the model calibration. In addition, the coefficient of determination (R^2) and relative error (RE) were also used to evaluate the model
15 performance. The definitions of NSE, R^2 and RE can refer to Du et al. (2016).

The same calibration and validation period were used for the stream temperature. The daily stream temperature data from Environmental Canada and Climate Change was used for the stream temperature calibration. The sampling frequencies of stream temperature varied from monthly to seasonal, and five stations with higher sampling frequency were chosen for the model calibration. These five stations were
20 located from upstream to downstream reflecting stream temperature conditions in different parts of the ARB (Figure 1). Additional information for the five stream temperature observed stations can be found in Table 1. As there was no stream temperature data at Athabasca River near Windfall during the validation period, model validation was performed at other four stations. The equilibrium and hydroclimatological stream temperature models were manually calibrated. To test the model performance and validity with
25 less calibration effort, one set of the stream temperature parameters for the ARB were used for the calibration processes. The average NSE value of the five stations was chosen as the objective function for the stream temperature calibration, and their parameter values were adjusted to obtain the maximum average NSE value. The average values of R^2 and RE were also calculated to evaluate the performance. The RE can be positive in case of overestimation or negative in case of underestimation. Therefore, the
30 absolute value of RE was calculated for each station, and then these absolute values were averaged. For the hydroclimatological stream temperature model, it is possible to use different parameters for different seasons which can account for the influence of seasonal variation on the stream temperature. In this study, three periods were defined to represent seasonal variations, and different parameters were given for each period.

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Table 1 Detailed information for the five stream temperature stations in the Athabasca River Basin

Stations	Drainage area (km ²)	Watershed Location	Number of water temperature samples	
			Calibration	Validation
Athabasca river at Old Fort	154800	downstream	97	71
Muskeg River near Fort Mackay	1715	downstream	102	39
Athabasca River near Horse River	98270	downstream	103	99
Athabasca River at Athabasca	73580	midstream	187	117
Athabasca River near Windfall	19650	upstream	60	/

3. Results and Discussion

3.1 SWAT streamflow calibration and validation

5 To examine the performance of the equilibrium temperature model, a SWAT model calibrated for hydrology is imperative in order to perform an accurate simulation of the stream temperature. The SWAT hydrological model was calibrated and validated using daily streamflow data for 35 stations in the ARB (Figure 1). The average values of NSE for the 35 stations were 0.57 and 0.49, respectively, during calibration and validation
 10 period. The average values of RE were 5.3% and 12.4%, respectively, during calibration and validation period. Detailed results from the ARB SWAT streamflow calibration and validation can be found in Shrestha et al. (2017). Overall, the accuracy of streamflow results at 35 stations across the basin suggests that the SWAT model could simulate the streamflow at headwaters, foothills, and prairie regions reasonably well, and the model's accuracy at downstream parts of the boreal plain region was satisfactory
 15 (Shrestha et al., 2017). This well calibrated SWAT hydrological model is further used for the simulation of stream temperature based on the hydroclimatological and equilibrium temperature models.

3.2 Stream temperature calibration and validation

For the equilibrium temperature model, a range of 0.5 to 1.5 for the multiplicative factor parameter λ_{kt} was used for calibration. η was the most sensitive parameter for the equilibrium temperature model and therefore, it was the main parameter that was manipulated. η was the first parameter to be calibrated, and it was optimized to 3.2 to obtain the maximum average NSE value of 0.79. Other parameters (Lag, λ and λ_{kt}) had little effect on NSE and R^2 value, but they did, however, have an impact on the average RE value. After η was calibrated, Lag, λ and λ_{kt} were calibrated as 2, 1.1 and 1.15, respectively, to minimize the average RE value. For the hydroclimatological model, three different seasons (Table 2) with different
 25 parameter sets were used for model calibration. It is found that the heat transfer coefficient K is the most sensitive parameter for hydroclimatological model and was the main parameter calibrated. The calibrated parameter values are given in Table 2.

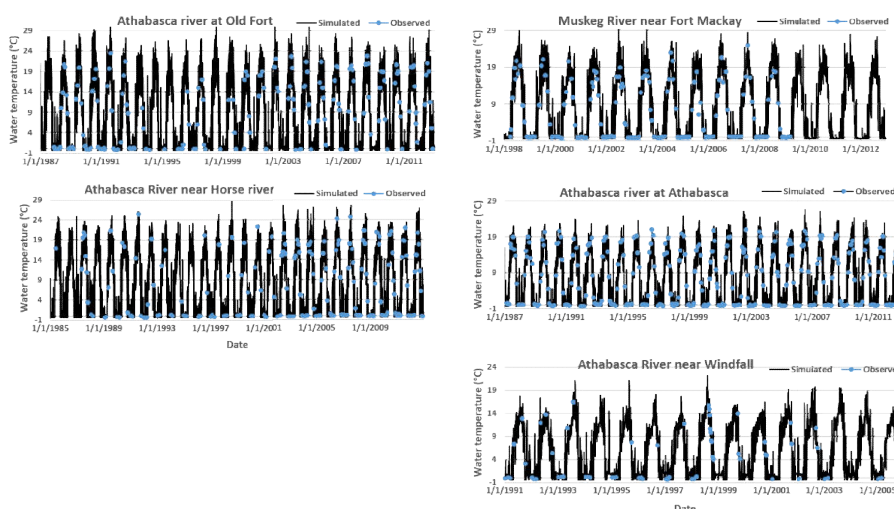


Table 2 Calibrated parameters of the hydroclimatological stream temperature model for the Athabasca River Basin

Julian Day		λ	K (1/h)	ϵ (°C)	Lag (days)
From	To				
1	90	1.1	0.1	12	5
91	300	1.1	0.05	0	3
301	366	1.1	0.1	9	5

3.3 Performance of the equilibrium temperature model

To evaluate the performance of the equilibrium temperature model, we performed a comparison of the model simulation results with observed daily water temperature (Figure 2). The results of equilibrium temperature model are in good agreement with the observed data for all five stations. Furthermore, the simulated results of the equilibrium temperature model were compared with that of the original SWAT temperature model and that of the hydroclimatological stream temperature model. Table 3 shows the results of statistical performance for the three different stream temperature models. For all five stations, the equilibrium temperature model improved the performance of stream temperature simulations compared to that of other two models. The original SWAT stream temperature model had average NSE, R^2 and RE as 0.51, 0.66 and 10.1%, respectively, during the calibration period and 0.56, 0.67 and 8.4%, respectively, during the validation period. The hydroclimatological model had average NSE, R^2 and RE as 0.50, 0.61 and 16.5%, respectively, during the calibration period and 0.50, 0.62 and 19.7%, respectively, during the validation period. The equilibrium temperature model had as average NSE, R^2 and RE as 0.79, 0.82 and 9.6%, respectively, during the calibration period and 0.76, 0.80 and 7.4%, respectively, during the validation period. Furthermore, the equilibrium temperature showed good performances for all regions of the ARB, with NSE values all greater than 0.67. In contrast, the performances of other two models are not consistent among different regions, especially for Athabasca River Station near Windfall with NSE values less than 0.1.



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Figure 2 Comparisons of simulated stream temperature using the equilibrium temperature model with observed stream temperature

**Table 3** Calibration and validation statistics for the three stream temperature models for the five stations in the Athabasca River Basin

Station	Calibration			Validation		
	NSE	R ²	RE (%)	NSE	R ²	RE (%)
<u>Original SWAT stream temperature model</u>						
Athabasca River at old Fort	0.48	0.62	15.9	0.68	0.71	11.8
Muskeg River near Fort Mackay	0.60	0.69	11.1	0.54	0.67	16.8
Athabasca River near Horse river	0.52	0.62	-14.0	0.50	0.60	-4.8
Athabasca River at Athabasca	0.87	0.68	2.8	0.53	0.68	-3.5
Athabasca River near Windfall	0.09	0.68	-6.6	/	/	/
Average	0.51	0.66	10.1	0.56	0.67	8.4
<u>SWAT hydroclimatological stream temperature model</u>						
Athabasca River at old Fort	0.68	0.68	1.5	0.81	0.87	-15.7
Muskeg River near Fort Mackay	0.36	0.46	18.3	-0.03	0.30	47.0
Athabasca River near Horse river	0.6	0.61	-4.1	0.41	0.46	-0.3
Athabasca River at Athabasca	0.81	0.82	-11.9	0.8	0.83	-15.8
Athabasca River near Windfall	0.03	0.47	46.9	/	/	/
Average	0.50	0.61	16.5	0.50	0.62	19.7
<u>SWAT equilibrium stream temperature model</u>						
Athabasca river at old Fort	0.67	0.74	14.6	0.70	0.75	-0.8
Muskeg River near Fort Mackay	0.81	0.85	12.0	0.80	0.86	18.8
Athabasca River near Horse river	0.86	0.86	-0.9	0.74	0.76	7.8
Athabasca River at Athabasca	0.86	0.86	-3.3	0.80	0.81	-2.3
Athabasca river near Windfall	0.74	0.77	-17.2	/	/	/
Average	0.79	0.82	9.6	0.76	0.80	7.4

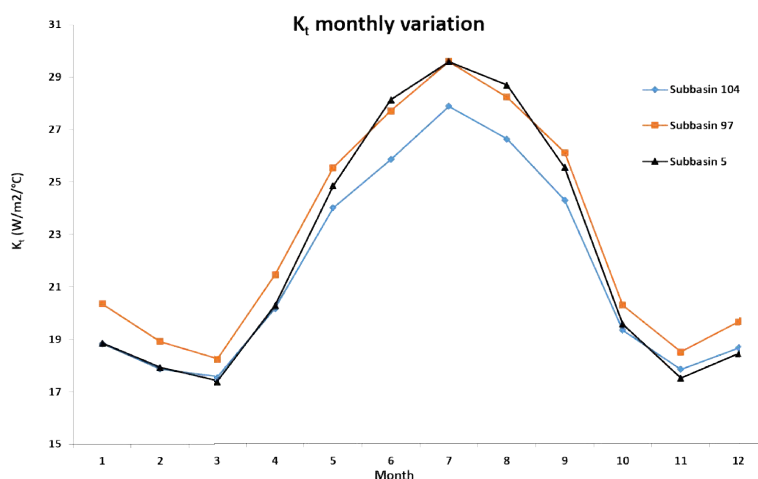


Figure 3 Monthly variations for heat exchange coefficient K_T at different parts of ARB

Another advantage of the equilibrium temperature model is the simple parameterization scheme compared to the hydroclimatological model. The hydroclimatological model requires seasonally-varying parameters to reflect the variations in the impact of hydrological and meteorological conditions on stream temperature. The seasonal-varying parameters increase the model complexity and model calibration effort. The equilibrium temperature model uses the initial stream temperature and wind speed to calculate the initial value of K_T (heat exchange coefficient). Moreover, air temperature and solar radiation are used to calculate the equilibrium temperature, which is the critical variable for water-air heat transfer process. Therefore, the K_T and equilibrium temperature vary temporally and spatially as the meteorological input data, such as air temperature, solar radiation and wind speed, vary. Figure 3 illustrates temporal and spatial variations of monthly average K_T values in the subbasins of upper, middle and downstream of the ARB. It can be seen that the averaged K_T had an obvious seasonal variation for all the three subbasin in different parts of the ARB and spatial variations. As a result, the equilibrium temperature model does not need temporal and spatial varying parameters, which reduces the model complexity and calibration efforts. An additive parameter η and a multiplicative parameter λ_{kt} for the whole basin were used to adjust the magnitude of equilibrium temperature and heat exchange coefficient. The results showed that the equilibrium temperature model had consistent simulation performances (with NSE values all greater than 0.67) for different stations in different regions of the ARB, which proves the effectiveness of this simple parameterization scheme. In addition, the equilibrium temperature model considers the impact of water depth on the heat transfer process at the water-air interface. The variations of runoff from subbasin and inflow from upstream can be represented by the change of stream water depth. Therefore, the equilibrium temperature model can simulate the impact of variations in hydrological conditions on the water-air heat transfer processes by incorporating the water depth.

25 3.4 Impact of the stream temperature simulation on water quality modelling

Stream temperature simulation has an impact on water quality modelling in SWAT since the water temperature affects chemical reaction rates and oxygen saturation concentration. The water quality module of SWAT uses an exponential equation to correct chemical reaction rates based on the simulated daily stream temperature (Neitsch et al., 2011):

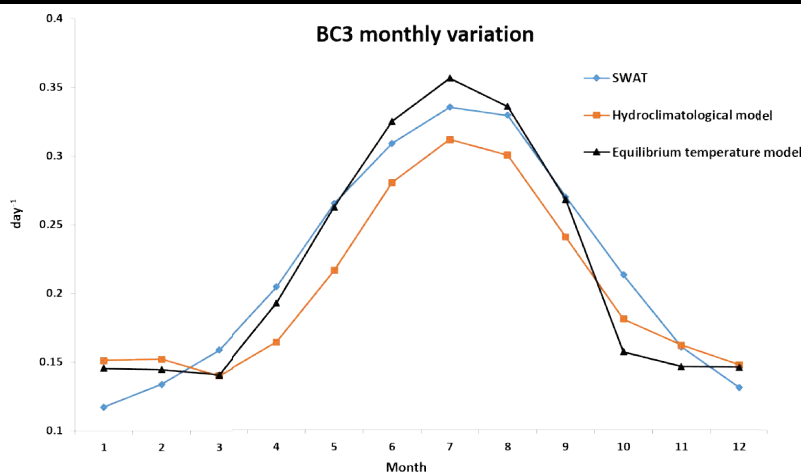


$$k(T) = k_{20} \cdot \theta^{T_w - 20} \quad (12)$$

where $K(T)$ is the reaction rate at a local temperature (d^{-1}), k_{20} is the reaction rate at 20 °C (d^{-1}), θ is temperature correction coefficient, and T_w is water temperature simulated by SWAT model (°C).

Table 4 Chemical reaction rates and their mean values under the different stream temperature models

Name	Description	K_{20} (/day)	θ	Mean value		
				Original SWAT	Hydroclimatological model	Equilibrium temperature model
RK1	CBOD deoxygenation rate	1.71	1.047	1.072	0.999	1.069
RK2	Oxygen reaeration rate	50	1.024	31.356	29.197	31.265
BC3	Organ N hydrolysis rate	0.21	1.047	0.132	0.123	0.131
BC4	Organic P mineralization rate	0.35	1.047	0.220	0.204	0.219



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Figure 4 Monthly variations for parameter BC3 using the different stream temperature models

The reaction rates at 20 °C are used as the input parameter, and the reaction rates at each day are corrected using the stream temperature simulated by the SWAT model. An inaccurate or uncalibrated stream temperature simulation may lead to uncertainties of the chemical reaction rates for water quality modelling. Four reaction rates that represent stream water quality in SWAT were chosen to analyze the impact of stream temperature simulation on water quality modelling. These reaction rates are related to carbonaceous biochemical oxygen demand (CBOD), dissolved oxygen (DO), nitrogen (N) and phosphorus (P) simulation in the stream (Table 4). The reaction rates at 20 °C and temperature correction coefficients are defined according to the default values in the SWAT manual (Arnold et al., 2013), and the mean values of chemical reaction rates for different stream temperature simulations are given in Table 4. Take BC3 and organic N concentration simulation as an example, the monthly average values of BC3

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were shown in Figure 4 to illustrate temporal variations under different water temperature models. The results showed that the chemical reaction rates differed in magnitude and temporal variation under different stream temperature simulations, which impacted the chemical concentration simulation within the stream. These differences in the reaction rates were caused by the different stream temperature simulations using the same reaction rates at 20 °C.

To investigate the impact of different stream temperature simulations on water quality concentration simulations, the simulated organic N concentrations at two streams (Table 5) by three different stream temperature models were output and analyzed. The stations of Muskeg River near Fort Mackay (MRFM) and Athabasca River at Old Fort (AROF) are in these two streams. The station of MRFM represents an upstream subbasin with no inflow impact, while the station of AROF is in the mainstream of downstream ARB representing the impact of inflow from upstreams. As can be seen from Table 5, annual average organic N concentrations simulated by three different stream temperature models at MRFM was very similar, but the simulated concentrations at AROF showed greater differences. Figure 5 shows the monthly average of simulated organic N concentrations from the three different stream temperature models at the MRFM and AROF stations. The results in Figure 5 indicate that monthly organic N concentrations simulated by different models showed greater variations at the AROF stations, especially from April to June when the concentrations are high. The results implied that the simulations of stream temperature has more impact on the simulated water quality concentrations in the downstream with upstream inflow impact than those locating in the upstream with no inflow impact.

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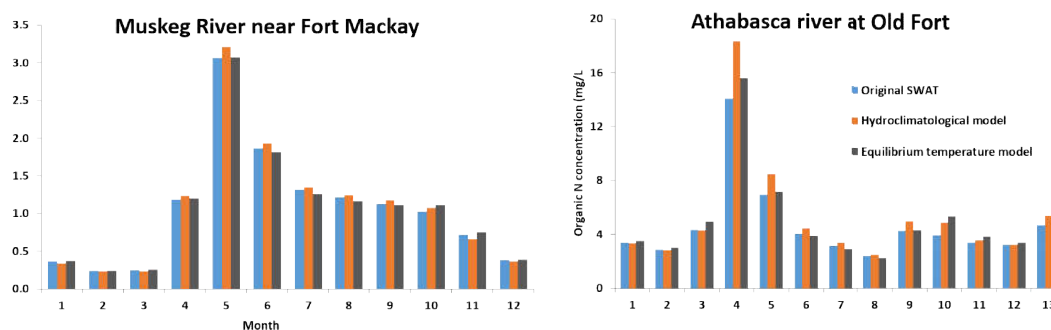


Figure 5 Monthly variations of organic N concentration simulated by the three different stream temperature models

Table 5 Annual average organic N concentrations simulated by the three different stream temperature models

Station	Average Organic N concentration (mg/L)		
	Original SWAT	Hydroclimatological model	Equilibrium temperature model
Muskeg River near Fort Mackay	1.064	1.087	1.063
Athabasca River at Old Fort	4.650	5.337	4.999

The SWAT model uses a linear relationship with air temperature to simulate water temperature, and the majority of SWAT applications for water quality modelling do not calibrate and validate stream temperature because of the fixed coefficients for the linear equations. Though water quality concentration

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can be calibrated by adjusting reaction rates at 20 °C without water temperature calibration, it might not reflect an accurate representation of chemical reactions and transformations. Therefore, the equilibrium temperature provides a potential tool for water quality concentration simulation.

4 Conclusions

5 The temperature of a river system is an important indicator for biodiversity and ecosystem sustainability. The original SWAT model uses a linear equation of air temperature to calculate the stream temperature and does not account for the impact of other meteorological and hydrological conditions. Thus, the linear equation may lead to an unrealistic prediction of the stream temperature when the air temperatures are very high or low. In this paper, we proposed a stream temperature model by
10 incorporating an equilibrium temperature approach to the hydroclimatological model developed by Ficklin et al. (2012). The equilibrium temperature approach accounts for the influence of air temperature, wind speed, solar radiation and water depth to calculate the water-air heat transfer. The hydroclimatological model considers the contribution of different runoff components and calculates the initial stream temperature by mixing runoff from subbasins and inflow from upstream. Then the final
15 stream temperature is calculated by simulating the water-air heat transfer. Compared to the hydroclimatological model, the equilibrium temperature model calculates heat transfer between water and air, including the impact of other meteorological conditions, such as wind speed and solar radiation. Also, the equilibrium temperature model considers the influence of water depth on the heat transfer, which reflects the impact of hydrological variations on water-air heat transfer. An additional advantage of this
20 model is the simple parameterization scheme requiring less calibration effort because it does not need spatial and temporal varying parameters. Also, the equilibrium temperature model uses the existing input data of the SWAT model with no additional inputs.

The equilibrium temperature model was applied to the ARB, and the model calibration and validation
25 were performed using daily water temperature data from five monitoring stations distributed throughout the ARB. The results show that the equilibrium temperature model had a better performance for the stream temperature simulation than the original SWAT and hydroclimatological models. The equilibrium temperature model showed a consistent performance for different regions in the ARB using fewer parameters and less calibration effort compared to the hydroclimatological model. In addition, the impact of the stream temperature on the water quality was analyzed through the variations of chemical reaction
30 rates and concentrations under three different stream temperature models. The results showed the chemical reaction rates and concentrations differed in magnitude and temporal variation under different water temperature simulations, which indicated the equilibrium temperature model can be a potential tool to simulate stream temperature for water quality concentration modelling. It is worth mentioning that the equilibrium temperature model can also be incorporated to other hydrological models with the required
35 runoff components and meteorological input data. Overall, the equilibrium temperature model, which accounts for the combined impact of meteorological and hydrological conditions, can be a useful tool for modelling the stream temperature.

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