## Time varying parameter models for catchments with land use

## change: the importance of model structure

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#### 1 Abstract

2 Rapid population and economic growth in South-East-Asia has been accompanied by extensive land 3 use change with consequent impacts on catchment hydrology. Modelling methodologies capable of 4 handling changing land use conditions are therefore becoming ever more important, and are 5 receiving increasing attention from hydrologists. A recently developed Data Assimilation based 6 framework that allows model parameters to vary through time in response to signals of change in 7 observations is considered for a medium sized catchment (2880 km<sup>2</sup>) in Northern Vietnam 8 experiencing substantial but gradual land cover change. We investigate the efficacy of the method 9 as well as the importance of the chosen model structure in ensuring the success of a time varying 10 parameter method. The method was used with two lumped daily conceptual models (HBV and 11 HyMOD) that gave good quality streamflow predictions during pre-change conditions. Although both 12 time varying parameter models gave improved streamflow predictions under changed conditions 13 compared to the time invariant parameter model, persistent biases for low flows were apparent in 14 the HyMOD case. It was found that HyMOD was not suited to representing the modified baseflow 15 conditions, resulting in extreme and unrealistic time varying parameter estimates. This work shows 16 that the chosen model can be critical for ensuring the time varying parameter framework 17 successfully models streamflow under changing land cover conditions. It can also be used to 18 determine whether land cover changes (and not just meteorological factors) contribute to the 19 observed hydrologic changes in retrospective studies where the lack of a paired control catchment 20 precludes such an assessment.

#### 21 **1. Introduction**

22 Population and economic growth in South-East Asia has led to significant land use change, with rapid 23 deforestation occurring largely for agricultural purposes [Kummer and Turner, 1994]. Forest cover in 24 the Greater Mekong Sub-region (comprising Myanmar, Thailand, Cambodia, Laos, Vietnam, and 25 South China) has decreased from about 73% in 1973 to about 51% in 2009 [WWF, 2013]. Vietnam in 26 particular has had the second highest rate of deforestation of primary forest in the world, based on 27 estimates from the Forest Resource Assessment by the United Nations Food and Agriculture 28 Organization [FAO, 2005]. Such extensive land use change has the potential to significantly alter 29 catchment hydrology (in terms of both quantity and quality), with its effects sometimes not 30 immediate but occurring gradually over a lengthy period of time. Recent estimates from satellite 31 measurements indicate that rapid deforestation continues in the region, although at lower rates [e.g. 32 Kim et al., 2015]. Persistent land use change necessitates modelling methodologies that are capable 33 of providing accurate hydrologic forecasts and predictions, despite non-stationarity in catchment 34 processes. This is also particularly relevant for water resource management which requires reliable 35 estimates of water availability, both in terms of volume and timing, to properly allocate the resource 36 between different water uses and to prevent flood damages. Vietnam has built many reservoirs in 37 the last decades and more are planned because they are considered to be fundamentally important 38 for electricity production, flood control, water supply and irrigation, ultimately contributing to the 39 development of the country [Giuliani et al., 2016].

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The literature on land-use change and its impacts on catchment hydrology is extensive, with studies
examining the effects of 1) conversion to agricultural land-use [*Thanapakpawin et al*, 2007; *Warburton et al.*, 2012]; 2) deforestation [*Costa et al.*, 2003; *Coe et al*, 2011]; 3) afforestation [e.g. *Yang et al.*, 2012; *Brown et al*, 2013] and 4) urbanization [*Bhaduri et al.*, 2001; *Rose & Peters*, 2001].
Fewer studies have examined how traditional modelling approaches must be modified to handle

46 non-stationary conditions, or how modelling methods can be used to assess impacts of land use 47 change. Split sample calibration has been used frequently to retrospectively examine changes to 48 model parameters due to land use or climatic change [Seibert & McDonnell, 2010; Coron et al., 2012; 49 McIntyre & Marshall, 2010; Legesse et al, 2003]. Several other studies have employed scenario 50 modelling, whereby hydrologic models are parameterized to represent different possible future land 51 use conditions [e.g. Niu & Sivakumar, 2013; Elfert & Borman, 2010]. A related approach involves 52 combining land use change forecast models with hydrologic models [e.g. Wijesekara et al., 2012]. 53 However, the aforementioned approaches are unsuited to hydrologic forecasting in changing 54 catchments, as the predicted land use change may not reflect actual changes. A potentially more 55 suitable approach in such a setting is to allow model parameters to vary in time, rather than 56 assuming a constant optimal value or stationary probability distribution. Many existing methods 57 utilising such a framework require some apriori knowledge of the land use change in order to inform 58 variations in model parameters (see for instance *Efstratiadis*, 2015; *Brown et al.*, 2006; and *Westra et* 59 al., 2014). Recent efforts have examined the potential for time varying parameter models to 60 automatically adapt to changing conditions using information contained in hydrologic observations 61 and sequential Data Assimilation, without requiring explicit knowledge of the changes [see for 62 example Taver et al., 2015, Pathiraja et al., 2016a&b]. Such approaches can objectively modify 63 model parameters in response to signals of change in observations in real time, whilst simultaneously 64 providing uncertainty estimates of parameters and streamflow predictions. They can also be used to 65 determine whether land cover changes (and not solely meteorological factors) contribute to 66 observed changes in streamflow dynamics in retrospective studies where the lack of a paired control 67 catchment precludes such an assessment.

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Pathiraja et al. [2016a] presented an Ensemble Kalman Filter based algorithm (the so-called Locally
 Linear Dual EnKF) to estimate time variations in model parameters. The method sequentially
 assimilates observations into a numerical model in real time to generate improved estimates of

72 model states, fluxes and parameters based on their respective uncertainties. Its purpose is to infer 73 changes to catchment properties (e.g. land cover change) from hydrologic observations, without 74 prior knowledge of such changes, at the time scale of the available observations. It can therefore be 75 used for various applications: 1) to retrospectively estimate time variations in model parameters; 2) 76 for short-term predictive modelling (days to weeks), e.g. flood forecasting; and 3) for on-line/real 77 time water resource management, e.g. determining releases from reservoirs in catchments with 78 changing land cover conditions. In retrospective mode, the method is advantageous compared to 79 split-sample calibration type approaches since no apriori knowledge of land use change is needed, 80 and the modeller does not have to make somewhat arbitrary decisions about how to segregate the 81 data. When used for prediction or forecasting, states and parameters are updated sequentially using 82 all available observations up until the current time. These updated states and parameters are then 83 used along with the prior parameter generating model to produce hydrologic predictions over a short 84 time horizon. This allows one to seamlessly obtain predictions without the modeller needing to 85 explicitly modify the model to account for any catchment changes. The efficacy of the method was 86 demonstrated in Pathiraja et al. [2016b] through an application to small experimental catchments (< 87 350 ha) with drastic land cover changes and strong signals of change in streamflow observations. 88 89 Here we investigate two issues related to the use of time varying parameter models for prediction in

90 realistic catchments with changing land cover conditions. Firstly, we investigate the efficacy of the 91 time varying parameter method for sparsely observed, medium-sized catchments with spatially 92 complex and gradual land use change (occurring over months/years). Several authors have 93 demonstrated that impacts of land use change on the hydrologic response are dependent on many 94 factors including the type and rate of land cover conversion as well the spatial pattern of different 95 land uses within the catchment [Dwarakish & Ganasri, 2015; Warburton et al., 2012]. In such 96 situations, the effects of unresolved spatial heterogeneities in model inputs (e.g. rainfall) and the 97 relatively less pronounced changes in land surface conditions make time varying parameter detection

and accurate hydrologic prediction more difficult. The second objective is to examine the role of
the hydrologic model in determining the ability of the time varying parameter framework to provide
high quality predictions in changing conditions. Often there may be several candidate hydrologic
models (with time invariant parameters) that have similar predictive performance for a catchment
when calibrated and validated over a time series of static land cover conditions [*Marshall et al.,*2006]. This work examines whether all such candidate models in time varying parameter mode are
also capable of providing accurate predictions under changing conditions.

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106 These issues are investigated for the Nammuc catchment (2880 km<sup>2</sup>) in Northern Vietnam which has 107 experienced deforestation largely due to increasing agricultural development. It serves as an ideal 108 test catchment to study the efficacy of the time varying parameter algorithm due to its size, spatially 109 complex pattern of land use changes, and lack of information on the precise timing of such changes. 110 Land cover change is estimated to have occurred at varying rates, with cropland accounting for 111 roughly 23% between 1981 and 1994, and 52% by 2000. We also consider two lumped conceptual 112 hydrologic models (given the availability of point rainfall, temperature, and streamflow data) 113 operating at daily time step to address the second objective. Both models demonstrate similar 114 performance in representing streamflow at the outlet during the pre-change calibration period 115 (1975-1979), although their performance during/after land use change is unknown. Therefore, the 116 effect of the model structure (i.e. model equations) on hydrologic predictions from the time varying 117 parameter models is studied. This work represents the first application of a continuously time 118 varying parameter approach for modelling a real medium sized catchment with no apriori (or partial) 119 knowledge of the type and timing of land use change.

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121 The remainder of this paper is structured as follows. Details of the study catchment and the impact 122 of land cover change are analysed in Section 2. Section 3 summarizes the experimental setup 123 including the hydrological models and the time varying parameter estimation method used. Results

are provided in Section 4, along with an analysis of whether the time varying model structures reflect
 the observed catchment dynamics. Finally, we conclude with a summary of the main outcomes of
 the study as well as proposed future work.

#### 127 **2. The Nammuc Catchment**

128 The Nammuc catchment (2880 km<sup>2</sup>) is located in the Red River Basin, the second largest drainage 129 basin in Vietnam which also drains parts of China and Laos. The local climate is tropical monsoon 130 dominated with distinct wet (May to October) and dry (November to April) seasons. The wet season 131 tends to have high temperatures (on average 27 to 29 °C) due to south-south easterly winds that 132 bring humid air masses. Conversely, during the dry season, circulation patterns reverse carrying 133 cooler dry air masses to the basin (leading to average temperatures of 16 to 21°C). Streamflow 134 response is consequently monsoon driven, with high flows occurring between June and October 135 (generally peaking in July/August) and low flows in the December to May period (Vu, 1993). Average 136 annual rainfall at Nammuc varies between 1300 and 2000 mm (on average 1600 mm) and catchment 137 elevation ranges between 350 and 1500 m asl. A summary of catchment properties is provided in 138 Table 1 for pre-change (prior to 1994) and post-change (after 1994) conditions. This separation was based on available land cover information as described below. 139

#### 140 2.1.Data & Land Cover Change

141 Figure 1 shows the available land cover information for the Nammuc catchment. Land cover

142 information for the catchment is scant, we were able to locate only two sources which unfortunately

- 143 do not give a complete picture over the entire time period of interest (1970 to 2004). The first land
- 144 cover map refers to the period 1981-1994 and was obtained by the Vietnamese Forest Inventory and
- 145 Planning Institute (<u>http://fipi.vn/Home-en.htm</u>). The second land cover map refers to year 2000 and
- 146 was obtained from the FAO Global Land Cover database
- 147 (http://www.fao.org/geonetwork/srv/en/metadata.show?id=12749&currTab=simple). A comparison

of the two maps shows a reduction in forest cover in favor of cropland; Evergreen Leaf decreases from about 60% to 30% whilst cropland increases from about 23% to 52%. The change in land cover is patchy, although mostly concentrated in the northern part of the catchment. Because of the scant information available, it is not easy to identify the precise time period of these changes. Based on the available land cover map information and the changes to observed runoff (see Section 2.2), we posit that a period of rapid extensive deforestation occurred in early to mid-1990s.

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155 Daily point rainfall data is available at four precipitation stations surrounding the catchment (Dien 156 Bien, Tuan Giao, Quynh Nhai and Nammuc, see Figure 1). Catchment averaged rainfall was 157 developed as a weighted sum of the four stations with weights determined by Thiessen Polygons. 158 Daily mean temperature was calculated in a similar fashion using temperature records from the 2 159 closest gauges (Lai Chau and Quynh Nhai, see Figure 1). This was used to estimate Potential 160 Evapotranspiration through the empirical temperature-latitude based Hamon PET method [Hamon, 161 1961]. Daily rainfall, temperature and streamflow data was provided by the Vietnamese Institute of 162 Water Resources Planning.

#### 163 **2.2.Impact of Land Cover Change on Streamflow**

The annual runoff/direct runoff coefficient and Baseflow Index were used to assess the impact of land cover change on the hydrologic regime. Baseflow was estimated using the two parameter recursive baseflow filter of *Eckhardt* [2005] (see equation 1), with on-line updating of baseflow estimates to match low flows:

$$b_{k} = \frac{1}{(1 - a.BFI_{max})} [(1 - BFI_{max}).a.b_{k-1} + (1 - a).BFI_{max}.y_{k}]$$
(1)

where  $b_k$  is the estimated baseflow at time k,  $y_k$  is the total observed streamflow at time k,  $BFI_{max}$ is the maximum value of the BFI (long term ratio of baseflow to total streamflow) and a is a filter parameter. In this study, we adopt  $BFI_{max} = 0.5$  and a = 0.988 based on manual optimization.

172 An examination of the observed streamflow and rainfall records shows that distinct changes to the hydrologic regime are evident after the mid-1990s. The annual runoff coefficient  $\left(\frac{runoff}{rainfall}\right)$  varies 173 174 between 0.4 and 0.6 prior to 1994, after which it increases to between 0.6 and 0.8 until 2004 (see 175 Figure 2a). However, increases to annual yields are driven mostly by changes to baseflow volume. 176 This is evident in Figure 2a, which shows that the increase in the annual direct runoff coefficient  $\left(\frac{runoff-baseflow}{rainfall}\right)$  is less than the increase in the total runoff coefficient (roughly 0.1 increase 177 compared to 0.2 respectively). A small increase in the Annual Baseflow Index  $\left(\frac{baseflow}{rumoff}\right)$  is apparent 178 179 also, from about 0.32 on average in the period 1970 to 1982 to 0.39 on average after 1994 (Figure 180 2b). This indicates that the annual increases to baseflow volume exceed the increases to direct 181 runoff volume. Similar changes were found by Wang et al. [2012] who analyzed records in the 182 entire Da River basin which drains the largest river in the Red River catchment. The exact physical 183 processes behind the observed increase in baseflow are not precisely known, particularly since 184 effects of land use change from forest to cropland are not unequivocal [Price, 2011]. Deforestation 185 may be associated to an increase in mean annual flow and baseflow because of lower interception 186 and evapotranspiration rates [e.g., Keppeler and Ziemer, 1990]. Nevertheless, permanent forest 187 removal may decrease baseflow because of soil compaction and lower infiltration rates [e.g., 188 Zimmermann et al., 2006; Bormann and Klaassen; 2008]. Some authors also show that tillage 189 practices, associated to forest conversion to cropland, can increase soil porosity, soil water content, 190 and infiltration, thus ultimately contributing to baseflow formation [e.g., Alam et al., 2014].

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At a seasonal time scale, it is apparent that both wet and dry season flows exhibit temporal variations. We utilized the Moving Average Shifting Horizon (MASH) [*Anghileri et al.,* 2014] and Mann-Kendall test to assess seasonal trends in observed streamflow, precipitation, and temperature data. The MASH tool can be used to qualitatively assess inter-annual variations in the seasonal pattern of a variable. It works by calculating a statistic of the data (e.g. mean) over the same block of

197 days in consecutive years. A steady increase in baseflow is again apparent (see February to April in 198 Figure 2c), as well as increases to wet season flows (see June to September in Figure 2c). Mann-199 Kendall test (with significance level equal to 5%) on annual and monthly streamflow time series 200 shows increasing trends in almost all months, i.e., from October to July. No concurrent increases are 201 apparent in rainfall (see Figure 2d). Also, the Mann-Kendall test applied to precipitation time series 202 does not show any statistically significant trend, except a decrease in September for Nammuc and 203 Quynh Nhai station and an increase in July for Dien Bien station. Temperature variations are not 204 evident from the MASH analysis (not shown) and no significant trend can be detected by applying the 205 Mann-Kendall test. These results indicate that changes in streamflow dynamics are likely due to land 206 use change rather than climatic impacts.

### 207 **3. Experimental Setup**

#### 208 3.1.Hydrologic Models

Conceptual lumped models operating at a daily time step were adopted due to the availability of point rather than distributed hydro-meteorological data of sufficient length. We considered the HyMOD [*Boyle*, 2001] and Hydrologiska Byrans Vattenbalansavdelning (HBV) [*Bergstrom et al.*, 1995] models. They differ mainly in the way components of the response flow are separated (HBV has near surface flow, interflow, and baseflow components whilst HyMOD has a quickflow and slow flow component only) and how these flows are routed. A schematic of the models is shown in Figure 3.

216 In the HyMOD model, spatial variations in catchment soil storage capacity are represented by a 217 Pareto distribution with shape parameter *b* and maximum point soil storage depth  $c_{max}$ . Excess 218 rainfall (*V*) is partitioned into three cascading tanks representing quick flow and a single slow flow 219 store through the splitting parameter  $\alpha$ . Outflow from these linear routing tanks is controlled by parameters  $k_q$  (for the quick flow stores) and  $k_s$  (for the slow flow store). The model has a total of 5 states and 5 parameters.

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223 In the HBV model, input to the soil store is represented by a power-law function (see Figure 3, note 224 the snow store is neglected for this study). Excess rainfall enters a shallow layer store which 225 generates: 1) near surface flow  $(q_0)$  whenever the shallow store state (stw1) is above a threshold 226 (hl1) and 2) interflow  $(q_1)$  by a linear routing mechanism controlled by the K1 parameter. 227 Percolation from the shallow layer store to the deep layer store (controlled by *perc* parameter) then 228 leads to the generation of baseflow also via linear routing (controlled by the K2 parameter). Finally, a 229 triangular weighting function of base length *Maxbas* is used to route the sum of all three flow 230 components. There are a total of 9 parameters and 3 states. 231 232 The Shuffled Complex Evolution Algorithm (SCE-UA) [Duan et al., 1993] was used to calibrate HyMOD 233 and the Borg Evolutionary Algorithm [Hadka & Reed, 2013] was used to calibrate HBV. The 234 calibration algorithms were selected based on previous studies that had successfully used them for 235 calibration of these models [Reed et al., 2013; Moradkhani et al., 2005]. The calibration procedure 236 itself is however not critical in our study, because the optimal parameter values are only used as 237 initial values for the time varying parameter method. Both models were calibrated to pre-change 238 conditions. The period 1973 to 1979 was selected for calibration (with 2 years for spin-up) as it was 239 expected to have minimal land cover changes (and is therefore representative of pre-change 240 conditions), and also to ensure sufficient data on pre-change conditions is available for assimilation. 241 Both models had very similar performance in terms of reproducing observed runoff (an NSE of 0.75 242 and 0.77 for HyMOD and HBV respectively). HBV was slightly better at reproducing low flows whilst 243 HyMOD was slightly better at mid-range flows (see Table 2). Here the low flow threshold was 244 defined as the average annual 50<sup>th</sup> percentile flow and the high flow threshold as the average annual 245 85<sup>th</sup> percentile flow.

#### 246 **3.2.Time Varying Parameter Estimation**

247 A Data Assimilation based framework for estimating time varying parameters was presented in 248 Pathiraja et al. [2016a]. The approach relies on an Ensemble Kalman Filter (EnKF) [Evensen, 1994] to 249 perform sequential joint state and parameter updating. EnKFs were developed to extend the 250 applicability of the celebrated Kalman Filter [Kalman, 1960] to non-linear systems, although they 251 provide a sub-optimal update as only the mean and covariance are considered in generating the 252 posterior. However, they have been used with much success in many hydrologic applications [see for 253 example Reichle et al., 2002; Gu et al., 2005; Komma et al., 2008; Sun et al., 2009; Xu et al., 2016]. 254 EnKFs offer a practical alternative to Sequential Monte Carlo/Particle Filter methods that propagate 255 the full probability density through time, but suffer from several implementation issues even in 256 moderate dimensional systems. The Locally Linear Dual EnKF method of Pathiraja et al. [2016a] 257 works by sequentially proposing parameters, updating these using the Ensemble Kalman filter and 258 available observations, and subsequently using these updated parameters to propose and update 259 model states. An approach for proposing parameters in the time varying setting was also presented, 260 for cases where no prior knowledge of parameter variations is available. The method was verified 261 against multiple synthetic case studies as well as for 2 small experimental catchments experiencing 262 controlled land use change [Pathiraja et al., 2016a and Pathiraja et al., 2016b]. The algorithm is 263 summarised below, for full details refer to Pathiraja et al. [2016a].

#### 264 **3.2.1. Locally Linear Dual EnKF**

Suppose a dynamical system can be described by a vector of states  $x_t$  and outputs  $y_t$  and a vector of associated model parameters  $\theta_t$  at any given time t. The uncertain system states and parameters are represented by an ensemble of states  $\{x_t^i\}_{i=1:n}$  and parameters  $\{\theta_t^i\}_{i=1:n}$  each with n members. The prior state and parameter distributions  $\{x_t^{i-}\}_{i=1:n}$  and  $\{\theta_t^{i-}\}_{i=1:n}$  respectively represent our prior knowledge of the system, usually derived as the output from a numerical model. Suppose also that the system outputs are observed  $(y_t^o)$  but that there is also some uncertainty associated with these observations. The purpose of the data assimilation algorithm (here the EnKF) is to combine the prior estimates with measurements, based on their respective uncertainties, to obtain an improved estimate of the system states and parameters. A single cycle of the Locally Linear Dual EnKF procedure for a given time *t* is undertaken as follows. Note in the following, the overbar notation is used to indicate the ensemble mean.

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1. **Propose a prior parameter ensemble.** This involves generating a parameter ensemble using prior knowledge. In this case, our prior knowledge comes from the updated parameter ensemble from the previous time  $(\theta_{t-1}^{i+})$  and how it has changed over recent time steps. The assumed parameter dynamics is a Gaussian random walk with time varying mean and variance, given by:

$$\boldsymbol{\theta}_{t}^{i-} \sim N\left(\boldsymbol{\theta}_{t-1}^{i+} + \boldsymbol{m}_{t}.\Delta t, s^{2}\boldsymbol{\Sigma}_{t-1}^{\theta}\right) \text{ for } i = 1:n$$
(2)

$$\boldsymbol{\Sigma}_{t-1}^{\theta} = \frac{1}{n-1} \sum_{i=1}^{n} \left( \boldsymbol{\theta}_{t-1}^{i+} - \overline{\boldsymbol{\theta}_{t-1}^{+}} \right) \left( \boldsymbol{\theta}_{t-1}^{i+} - \overline{\boldsymbol{\theta}_{t-1}^{+}} \right)^{\mathrm{T}}$$
(3)

where  $\Sigma_{t-1}^{\theta}$  is the sample covariance matrix of the updated parameter ensemble at time t - 2831;  $\overline{\theta_{t-1}^+}$  indicates the ensemble mean of the updated parameters at time t - 1; ()<sup>T</sup> represents the transpose operator; and  $s^2$  is a tuning parameter. The prior ensemble mean is determined as the linear extrapolation of the updated ensemble means from the previous two time steps, i.e.:

$$\boldsymbol{m}_{t}[k] = \begin{cases} \boldsymbol{m}_{t-1}[k], & |\boldsymbol{m}_{t-1}[k]| \leq m_{max} \\ \boldsymbol{m}_{t-2}[k], & |\boldsymbol{m}_{t-1}[k]| > m_{max} \end{cases}$$
(4)

$$\boldsymbol{m}_{t-1} = \frac{\overline{\boldsymbol{\theta}_{t-1}^+} - \overline{\boldsymbol{\theta}_{t-2}^+}}{\Delta t}$$
(5)

$$\boldsymbol{m}_{t-2} = \frac{\overline{\boldsymbol{\theta}_{t-2}^+} - \overline{\boldsymbol{\theta}_{t-3}^+}}{\Delta t}$$
(6)

287 where  $m_t[k]$  indicates the kth component of the vector  $m_t$ , the estimated rate of change. 288 Note that the extrapolation is forced to be less than a pre-defined maximum rate of change 289  $m_{max}$  to minimise overfitting and avoid parameter drift due to isolated large updates. The 290 maximum rate of change is model specific and will depend on the modeller's judgement

291 regarding expected extreme changes.

2. Consider observation and forcing uncertainty. This is done by perturbing measurements of 23 forcings and system outputs with random noise sampled from a distribution representing the 294 uncertainty in those measurements. The result is an ensemble of forcings ( $u_t^i$ ) and 295 observations ( $y_t^i$ ) each with *n* members. For example, if random errors in measurements of 296 system outputs (herein also referred as observations) are characterized by a zero mean

297 Gaussian distribution, the ensemble of observations is given by:

$$\mathbf{y}_{t}^{i} \sim N\left(\mathbf{y}_{t}^{o}, \mathbf{\Sigma}_{t}^{y^{o}y^{o}}\right) \quad for \ i = 1:n$$
 (7)

298 where  $y_t^o$  is the recorded measurement at time t and  $\Sigma_t^{y^o y^o}$  is the error covariance matrix of 299 the measurements.

3. *Generate simulations using prior parameters*. The prior parameters from Step 1,  $\theta_t^{i-}$  and 301 updated states from the previous time,  $x_{t-1}^{i+}$  are forced through the model equations to 302 generate an ensemble of model simulations of states ( $\hat{x}_t^i$ ) and outputs ( $\hat{y}_t^i$ ):

$$\widehat{\boldsymbol{x}}_{t}^{i} = f\left(\boldsymbol{x}_{t-1}^{i+}, \boldsymbol{\theta}_{t}^{i-}, \boldsymbol{u}_{t}^{i}\right) \text{ for } i = 1:n$$
(8)

$$\widehat{\mathbf{y}}_{t}^{i} = h(\widehat{\mathbf{x}}_{t}^{i}, \boldsymbol{\theta}_{t}^{i-}) \text{ for } i = 1:n$$
(9)

#### 303 4. *Perform the Kalman update of parameters.* Parameters are updated using the Kalman

304 update equation and the prior parameter and simulated output ensemble from Step 1 and 3:

$$\boldsymbol{\theta}_t^{i+} = \boldsymbol{\theta}_t^{i-} + \mathbf{K}_t^{\theta} (\boldsymbol{y}_t^i - \,\widehat{\boldsymbol{y}}_t^i) \ for \ i = 1:n$$
(10)

$$\mathbf{K}_{t}^{\theta} = \boldsymbol{\Sigma}_{t}^{\theta \hat{\boldsymbol{\mathcal{Y}}}} \left[ \boldsymbol{\Sigma}_{t}^{\hat{\boldsymbol{\mathcal{Y}}} \hat{\boldsymbol{\mathcal{Y}}}} + \boldsymbol{\Sigma}_{t}^{\boldsymbol{\mathcal{Y}}^{o} \boldsymbol{\mathcal{Y}}^{o}} \right]^{-1}$$
(11)

305 where  $\Sigma_t^{\hat{\theta}\hat{y}}$  is a matrix of the sample cross covariance between errors in parameters  $\theta_t^{i-}$  and 306 simulated output  $\hat{y}_t^i$ ; and  $\Sigma_t^{\hat{y}\hat{y}}$  is the sample error covariance matrix of the simulated output:

$$\boldsymbol{\Sigma}_{t}^{\boldsymbol{\theta}\boldsymbol{\hat{y}}} = \frac{1}{n-1} \sum_{i=1}^{n} \left(\boldsymbol{\theta}_{t}^{i-} - \overline{\boldsymbol{\theta}_{t}^{-}}\right) \left(\boldsymbol{\hat{y}}_{t}^{i} - \overline{\boldsymbol{\hat{y}}_{t}}\right)^{\mathrm{T}}$$
(12)

$$\boldsymbol{\Sigma}_{t}^{\hat{y}\hat{y}} = \frac{1}{n-1} \sum_{i=1}^{n} \left( \hat{\boldsymbol{y}}_{t}^{i} - \overline{\hat{\boldsymbol{y}}_{t}} \right) \left( \hat{\boldsymbol{y}}_{t}^{i} - \overline{\hat{\boldsymbol{y}}_{t}} \right)^{\mathrm{T}}$$
(13)

#### 307 5. *Generate simulations using updated parameters.* Step 3 is repeated with the updated

308 parameter ensemble  $\theta_t^{i+}$  to generate the prior ensemble of model simulations of states  $(x_t^{i-})$ 309 and outputs  $(\tilde{y}_t^i)$ :

$$\boldsymbol{x}_{t}^{i-} = f(\boldsymbol{x}_{t-1}^{i+}, \boldsymbol{\theta}_{t}^{i+}, \boldsymbol{u}_{t}^{i}) \ for \ i = 1:n$$
(14)

$$\widetilde{\boldsymbol{y}}_t^i = h(\boldsymbol{x}_t^{i-}, \boldsymbol{\theta}_t^{i+}) \text{ for } i = 1:n$$
(15)

# 6. **Perform the Kalman update of states and outputs**. Use the Kalman update equation for correlated measurement and process noise (equations 16 to 19) and the simulated state $(x_t^{i-})$ and output $(\tilde{y}_t^i)$ ensembles from Step 5 to update them. Since the measurements have already been used to generate $\tilde{y}_t^i$ , the errors in model simulations and measurements are now correlated. The standard Kalman update equation (as in the form of equations 10 and 11) can no longer be used as it relies on the assumption that errors in measurements and model simulations are independent.

$$\boldsymbol{x}_{t}^{i+} = \boldsymbol{x}_{t}^{i-} + \mathbf{K}_{t}^{x} (\boldsymbol{y}_{t}^{i} - \widetilde{\boldsymbol{y}}_{t}^{i}) \text{ for } i = 1:n$$
(16)

$$\mathbf{K}_{t}^{x} = \left[ \boldsymbol{\Sigma}_{t}^{x\tilde{y}} + \boldsymbol{\Sigma}_{t}^{\varepsilon_{x}y^{o}} \right] \left[ \boldsymbol{\Sigma}_{t}^{\tilde{y}\tilde{y}} + \boldsymbol{\Sigma}_{t}^{\varepsilon_{\tilde{y}}y^{o}} + \left( \boldsymbol{\Sigma}_{t}^{\varepsilon_{\tilde{y}}y^{o}} \right)^{\mathrm{T}} + \boldsymbol{\Sigma}_{t}^{y^{o}y^{o}} \right]^{-1}$$
(17)

$$\boldsymbol{\varepsilon}_{\boldsymbol{x}_t^i} = \boldsymbol{x}_t^{i-} - \boldsymbol{\widehat{x}}_t^i \tag{18}$$

$$\boldsymbol{\varepsilon}_{\boldsymbol{\tilde{y}}_{t}^{i}} = \boldsymbol{\tilde{y}}_{t}^{i} - \boldsymbol{\hat{y}}_{t}^{i}$$
(19)

317 where  $\Sigma_t^{x\tilde{y}}$  is a matrix of the sample cross covariance between simulated states  $\{x_t^{i-}\}_{i=1:n}$ 

318 and outputs  $\{\tilde{y}_t^i\}_{i=1:n}$  from Step 5;  $\Sigma_t^{\varepsilon_x y^o}$  represents the sample covariance between

319 
$$\{\varepsilon_{x_{t}}^{i}\}_{i=1:n}$$
 and the observations; and  $\Sigma_{t}^{\varepsilon_{\tilde{y}}y^{o}}$  represents the sample covariance between the  
320  $\{\varepsilon_{\tilde{y}_{t}}^{i}\}_{i=1:n}$  and the observations.

## 321 The above algorithm specifies the updating of states and parameters at any given time, based on 322 available observations. This allows one to retrospectively estimate time variations in model 323 parameters, as well as provide one time step ahead forecasts of states & outputs (as per equations 8 324 and 9). Forecasts at longer time horizons (i.e. longer than one time step ahead) would be made by

- 325 generating prior parameters and states as detailed in Steps 1 to 3, although the local linear
- 326 extrapolations are only valid close to the current time point.

#### 327 **3.2.2.** Application to the Nammuc Catchment

328 Joint state and parameter estimation was undertaken for the Nammuc Catchment over the period 329 1979 to 2004 by assimilating streamflow observations into the HyMOD and HBV models at a daily 330 time step. Estimating a large number of parameters from limited data is problematic in that the 331 system is highly under-determined, making it difficult to ensure the estimated parameters are 332 meaningful. Given the fairly low parameter dimensionality of HyMOD, all model parameters were 333 allowed to vary in time whilst for HBV we applied the Sobol method to identify the most sensitive 334 parameters to be included in the time varying parameter estimation. The Sobol method is a global 335 sensitivity analysis method based on variance decomposition. It identifies the partial variance 336 contribution of each parameter to the total variance of the hydrological model output [see for 337 example Saltelli et al., 2008, Nossent et al. 2011]. The method, implemented through the SAFE 338 toolbox [Pianosi et al., 2015], found the lp and Maxbas parameters to be the least sensitive and 339 least important in defining variations to catchment hydrology (see Table 3). These were held fixed (lp340 = 1 and Maxbas = 1 day) in the following analysis. Note that although the hl1 parameter was found 341 to have low sensitivity, it was retained as a time varying parameter due to its conceptual importance 342 in separating interflow and near surface flow (refer Figure 3).

343

Unbiased normally distributed ensembles of the parameters and states are required to initialise the LL Dual EnKF. Initial parameter ensembles were generated by sampling from a Gaussian distribution with mean equal to the calibrated parameters over the pre-change period and variance estimated from parameter sets with similar objective function values. Parameter sets with similar objective function values were obtained when using different starting points to the optimization algorithm during the model calibration stage. Initial state ensembles were also sampled from normal

350 distributions with mean equal to the simulated state at the end of the calibration period. An 351 ensemble size of 100 members was adopted and assumed sufficiently large based on the findings of 352 Moradkhani et al. [2005] and Aksoy et al. [2006]. Due to the stochastic-dynamic nature of the 353 method, ensemble statistics were calculated over 20 separate realisations of the LL Dual EnKF. The 354 prior parameter generating method described in Step 1 of Section 3.2 requires specification of the tuning parameter  $s^2$  to define the variance of the perturbations. This was tuned by selecting the  $s^2$ 355 356 value that optimized the quality of forecast streamflow over the calibration period. Forecast quality 357 was assessed using the logarithmic score (LS) [Good, 1952] of background streamflow predictions 358  $(\tilde{y}_{t}^{i})$  using updated parameters (equation 15), which was averaged over the calibration period of 359 length T:

$$\overline{LS} = \sum_{t=1}^{T} LS_t \tag{20}$$

$$LS_t = \log\left(f(y = y_t^o)\right) \tag{21}$$

where f(y) is the probability density function of the background streamflow predictions (represented by the empirical pdf of the sample points  $\{\tilde{y}_t^i\}_{i=1:n}$ ); and  $y_t^o$  is the measurement of the system outputs. The  $s^2$  value that gave the largest  $\overline{LS}$  was adopted for the assimilation period. The maximum allowable daily rate of change in the ensemble mean was based on assuming a linear rate of change within the entire feasible parameter space over a three year period.

365

As detailed in Section 3.2, observation and forcing uncertainty is considered by perturbing
measurements with random noise. Here streamflow errors were assumed to be zero-mean normally
distributed (truncated to ensure positivity) and heteroscedastic. The variance is defined as a
proportion of the observed streamflow, to reflect the fact that larger flows tend to have greater
errors than low flows:

$$y_t^i \sim TN(y_t^o, d. y_t^o) \text{ for } i = 1:n$$
 (22)

371 where TN indicates the truncated normal distribution to ensure positive flows and d = 0.1. A

372 multiplier of 0.1 was chosen based on estimates adopted for similar gauges in hydrologic DA studies

373 [e.g. Clark et al., 2008; Weerts & Serafy, 2006; Xie et al., 2014].

374

Several studies have noted that a major source of rainfall uncertainty arises from scaling point
rainfall to the catchment scale [*Villarini & Krajewski*, 2008; *McMillan et al.*, 2011] and that
multiplicative errors models are suited to describing such errors [e.g. *Kavetski et al.*, 2006]. Rainfall
uncertainties were therefore described using unbiased, lognormally distributed multipliers:

$$P_t^i = P_t.M^i \tag{23}$$

$$M^i \sim LN(m, v)$$
 and  $X^i = \log(M^i) \sim N(\mu, \sigma^2)$  for  $i = 1:n$ 
  
(24)

379 where  $P_t$  is the measured rainfall at time t; m and v are the mean and variance of the lognormally distributed rainfall multipliers M respectively; and  $\mu$  and  $\sigma^2$  are the mean and variance of the 380 381 normally distributed logarithm of the rainfall multipliers M. For unbiased perturbations, we let m =382 1. The variance of the rainfall multipliers (v) was estimated by considering upper and lower bound 383 error estimates in the Thiessen weights assigned to the four rainfall stations (see Section 2.1 for 384 calculation of catchment averaged rainfall,  $P_t$ ). The resulting upper and lower bound catchment 385 averaged rainfall data were then used to estimate error parameters due to spatial variation in 386 rainfall:

$$v = e^{(2\mu + \sigma^2)} \cdot (e^{\sigma^2} - 1)$$
(25)

$$\sigma^{2} = \widehat{\sigma^{2}} = var\left(\log\left[\frac{P_{upper,10}}{P_{lower,10}}\right]\right)$$
(26)

$$\mu = \log(m) - \frac{\sigma^2}{2} = -\frac{\sigma^2}{2}$$
(27)

where  $P_{upper,10}$  indicates catchment averaged rainfall data estimated using the upper bound Thiessen weights with daily depth greater than 10mm (similar for  $P_{lower,10}$ ). A 10mm rainfall depth threshold was chosen to avoid large rainfall fractions due to small rainfall depths.  $\hat{\sigma^2}$  was found to be 0.05 in this case study. Similarly, we assume the dominant source of uncertainty in temperature data arises from spatial variation. Differences in temperature records at Lai Chau and Quynh Nhai
(only available gauges with temperature records) were analysed and found to be approximately
normally distributed with sample mean 0.2 deg C and variance of 1.4 deg C. A perturbed
temperature ensemble was then generated according to equation 28:

$$T_t^i \sim TN(T_t^{avg}, 1.4) \quad for \ i = 1:n \tag{28}$$

where  $T_t^{avg}$  represents catchment averaged temperature data (see Section 2.1). Note that perturbations were taken to be unbiased (zero mean) as the sample mean of the differences in the temperature records was close to zero. The same perturbed input and observation sequences were used for the HyMOD and HBV runs for the sake of comparison. A summary of the values adopted for the various components of the Locally Linear Dual EnKF for each model is provided in Table 4 and Table 5.

#### 401 **4. Results and Discussion**

402 Temporal variations in the estimated parameter distributions from the LL Dual EnKF are evident for 403 both models (see Figure 4 and 5). In the case of the HBV model, changes at an inter-annual time 404 scale are evident for the *perc* and  $\beta$  (see Figure 4). The decrease in the  $\beta$  parameter means that a 405 greater proportion of rainfall is converted to runoff (i.e. more water entering the shallow layer 406 storage). Additionally, the increase in the *perc* parameter means that a greater volume of water is 407 made available for baseflow generation. These changes correspond with the observed increase in 408 the annual runoff coefficient (Figure 2) and increase in baseflow volume (as discussed in Section 2.2). 409 From an algorithm perspective, these parameters are most strongly correlated with streamflow (as 410 well as the most sensitive, see Table 3), meaning that they will receive the greatest proportional 411 updates. Similar parameter adjustments are seen for HyMOD, at least at a qualitative level (see 412 Figure 5). The sharp increase in the b parameter during the post-change period means that a greater 413 volume of water is available for routing (as larger b values mean that a smaller proportion of the

414 catchment has deep soil storage capacity) and the downward inter-annual trend in  $\alpha$  means that a 415 greater portion of excess runoff is routed through the baseflow store. Intra-annual variations in 416 updated model parameters for both HyMOD and HBV are also apparent (refer Figure 4 and Figure 5). 417 This is due to the inability of a single parameter distribution to accurately model both wet and dry 418 season flows. Such variations were not observed when using the time varying parameter framework 419 for small deforested catchments (< 350ha) [see Pathiraja et al., 2016b]. The comparatively less clear 420 parameter changes for the Nammuc catchment are due to a combination of the increased difficulty 421 in accurately modelling the hydrologic response (even in pre-change conditions) and due to the 422 relatively more subtle and gradual changes to land cover. Nonetheless, the method is shown to 423 generate a temporally varying structure that is conceptually representative of the observed changes.

424

425 Despite the overall correspondence between changes to model parameters and observed 426 streamflow, a closer examination shows that the hydrologic model structure is critical in determining 427 whether the time varying parameter models accurately reflect changes in all aspects of the 428 hydrologic response (not just total streamflow). In order to examine the impact of parameter 429 variations on the model dynamics, we generated model simulations with the time varying parameter 430 ensemble from the LL Dual EnKF, but without state updating (hereafter referred to as TVP-HBV and 431 TVP-HyMOD). Streamflow predictions from the LL Dual EnKF (i.e. with state and parameter updating) 432 for both the HyMOD and HBV are generally of similar quality and superior to those from the 433 respective time invariant parameter models, although a slight bias in baseflow predictions from 434 HyMOD is evident (see for example Figure 6). However, differences in predictions from TVP-HBV and 435 TVP-HyMOD are more striking due to the lack of state updating. Figure 7 shows annual statistics of 436 simulated streamflow from the TVP-HBV and TVP-HyMOD models and observed runoff. The TVP-437 HBV gives direct runoff and baseflow predictions that are consistent with runoff observations, 438 meaning that the parameter adjustments reflect the observed changes in the runoff response. This 439 however is not the case for the TVP-HyMOD. The annual runoff coefficient and annual direct runoff

440 coefficient are severely under-estimated in the post-change period by the TVP-HyMOD, whilst the
441 Annual Baseflow Index has an increasing trend of magnitude far greater than observed (Figure 7c).
442 All three quantities on the other hand are well represented by the TVP-HBV (Figure 7). Similar
443 conclusions can be drawn from Figure 8, which shows the results of a Moving Average Shifting
444 Horizon (MASH) analysis (see Section 2.2) on total and direct runoff (observed and simulated).
445 Observed increases in January to April flows (see Figure 8a) and wet season direct flows (July to
446 September) (see Figure 8e) are well represented by the TVP-HBV but not TVP-HyMOD.

447

448 The reason for the differences in performance between the TVP-HBV and TVP-HyMOD lies in the 449 structure of the hydrologic model. The TVP-HyMOD is incapable of representing the observed 450 increase in annual runoff/direct runoff coefficient due to the increased baseflow during dry periods, 451 despite having an Annual Baseflow Index far greater than the observed. This occurs due to an 452 inability to generate flow volume during periods of no rain. In joint state-parameter updating using 453 HyMOD, underestimated runoff predictions during dry periods lead to adjustments to the  $k_s$  and  $\alpha$ 454 parameters to increase baseflow depth (since these are the only parameters that are associated to 455 an active store). Unlike HBV, HyMOD has no continuous supply of water to the routing stores (i.e. 456 the quick flow and slow flow stores) during recession periods (which typically have extended periods 457 of no rainfall, so that V in Figure 3 is zero). This means that  $k_s$  and  $\alpha$  are updated to extreme values 458 to compensate for the volumetric shortfall. The HBV structure, on the other hand, has a continuous 459 percolation of water into the deep layer store even during periods of no rain (so long as the shallow 460 water store is non-empty). In summary, the HyMOD model structure is poorly suited to simulating 461 streamflow dynamics in post-change conditions, although it gave reasonable simulations in pre-462 change conditions. This highlights that need to select a sufficiently flexible model structure prior to 463 undertaking forecasting/predictive modelling using the time varying parameter approach. In 464 particular, the model structure must be capable of effectively simulating all potential future 465 catchment conditions.

467 Having established that the TVP-HBV provided a good representation of the observed streamflow 468 dynamics, we used a modelling approach to determine whether the observed changes were solely 469 driven by forcings and which (if any) components of runoff were also affected by land use change. A 470 resampled rainfall and temperature time series was generated by sampling the data without 471 replacement across years for each day (for instance rainfall and temperature for 1<sup>st</sup> January 1990 is 472 found by randomly sampling from all records on 1<sup>st</sup> January). This maintains the intra-annual (e.g. 473 seasonal) variability but destroys any inter-annual trends in the meteorological data. Streamflow 474 simulations were then generated using this resampled meteorological sequence as inputs to the TVP-475 HBV (i.e. without state updating). If the resulting streamflow simulations do not reproduce the 476 observed changes to streamflow dynamics, then this indicates that changes to meteorological 477 forcings are the main contributor. However, if it is able to at least partially (or fully) reproduce the 478 observed streamflow changes, this means that land cover changes are impacting catchment 479 hydrology (but potentially in addition to forcing changes, due to the presence of ecosystem 480 feedbacks). Figure 8d&h show the results of a MASH undertaken on the resulting simulations of total 481 and direct runoff using the resampled forcing time series and TVP-HBV model. Observed increases in 482 baseflow during the January - April period (see Figure 8a) and increases in direct runoff in the June -483 September period (see Figure 8e) are reproduced. The magnitude of increase in direct runoff in July 484 is slightly lower, indicating the potential for some climatic influences also. This is consistent with 485 findings from the Mann-Kendall test which identified a statistically significant increase in July rainfall 486 (see Section 2.2). Overall however, these results lend further weight to the conclusion that land 487 cover change has impacted the hydrologic regime of the Nammuc catchment. These results also 488 demonstrate that parameter changes correspond to actual changes in catchment hydrology, and are 489 not just random fluctuations that reproduce the observed streamflow statistics only when the 490 observed forcing time series is used.

#### 491 **5. Conclusions**

492 As our anthropogenic footprint expands, it will become increasingly important to develop modelling 493 methodologies that are capable of handling changing catchment conditions. Previous work proposed 494 the use of models whose parameters vary with time in response to signals of change in observations. 495 The so-called Locally Linear Dual EnKF time varying parameter estimation algorithm [Pathiraja et al., 496 2016a] was applied to 2 sets of small (< 350 ha) paired experimental catchments with deforestation 497 occurring under experimental conditions (rapid clearing of 100% and 50% of land surface) [Pathiraja 498 et al., 2016b]. Here we demonstrate the efficacy of the method for a larger catchment experiencing 499 more realistic land cover change, whilst also investigating the importance of the chosen model 500 structure in ensuring the success of the time varying parameter estimation method. We also 501 demonstrate that the time varying parameter framework can be used in a retrospective fashion to 502 determine whether land cover changes (and not just meteorological factors) contribute to the 503 observed hydrologic changes.

504

505 Experiments were undertaken on the Nammuc catchment (2880 km<sup>2</sup>) in Vietnam, which experienced 506 a relatively gradual conversion from forest to cropland over a number of years (cropland increased 507 from roughly 23% of the catchment between 1981 and 1994 to 52% by 2000). Changes to the 508 hydrologic regime after the mid-1990s were detected and attributed mostly to an increase in 509 baseflow volume. Application of the LL Dual EnKF with two conceptual models (HBV and HyMOD) 510 showed that the time varying parameter framework with state updating improved streamflow 511 prediction in post-change conditions compared to the time invariant parameter case. However, 512 baseflow predictions from the LL Dual EnKF with HBV were generally superior to the HyMOD case 513 which tended to have a slight negative bias. It was found that the structure (i.e. model equations) of 514 HyMOD was unsuited to representing the modified baseflow conditions, resulting in extreme and 515 unrealistic time varying parameter estimates. This work shows that the chosen model is critical for

516 ensuring the time varying parameter framework successfully models streamflow in unknown future 517 land cover conditions, particularly when used in a real time forecasting mode. Appropriate model 518 selection can be a difficult task due to the significant uncertainty associated with future land use 519 change, and can be even more problematic when multiple models have similar performance in pre-520 change conditions (as was the case in this study). One possible way to ensure success of the time 521 varying parameter approach is to use models whose fundamental equations explicitly represent key 522 physical processes (for instance, modelling sub-surface flow using Richard's equation with hydraulic 523 conductivity allowed to vary with time). In this way, time variations in model parameters would 524 more closely reflect changes to physiographic properties, rather than also having to account for 525 missing processes. The drawback of such physically based models is that they are generally data 526 intensive, both in generating model simulations (i.e. detailed inputs) and specifying parameters. 527 Additionally, it may be necessary to reduce the dimensionality of the time varying parameter vector 528 by keeping less sensitive model parameters fixed in order to make the estimation problem tractable. 529 Models of intermediate complexity that have explicit process descriptions may be the most 530 promising, although this also remains to be demonstrated.

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## 730 Tables

	Pre 1994	Post 1994				
Land Use						
Evergreen Forest						
(including evergreen needle and	77%	48%				
evergreen leaf) (%)						
Cropland (%)	23%	52%				
Hydro-Meteorological Properties						
Mean Annual Rainfall (mm)	1630	1660				
Mean Annual Runoff (mm)	838	1190				
Mean Annual Runoff Coefficient	0.5	0.7				
Mean Annual PET (mm)	1300	1300				
Estimated Mean Annual BFI	0.33	0.39				

	HYMOD	HBV				
NSE [ ]	0.77	0.75				
Peak flows (q > 5mm/d)						
MAE [mm/d]	3.11	2.85				
RMSE [mm/d]	4.55	4.72				
Medium flows (1 mm/d <= q <= 5mm/d)						
MAE [mm/d]	MAE [mm/d] <b>0.66</b> 0.80					
RMSE [mm/d]	0.86	1.09				
Low flows (q < 1mm/d)						
MAE [mm/d] 0.35 0.20						
RMSE [mm/d]	0.42	0.34				

739Table 2 Model performance in pre-change conditions used for calibration (1975 – 1979). Bold face740numbers correspond to the model with superior performance for the particular metric.

	Sensitivity Index
hl1	0.10
lp	0.12
Maxbas	0.14
fcap	0.18
КО	0.23
К2	0.23
К1	0.38
beta	0.41
perc	0.47

Table 3 Variance Based Sensitivity Analysis Results for HBV parameters: first order sensitivity index
 representing the contribution of varying a single parameter to the variance of the model output.
 Lower values indicate lower sensitivity.

Parameters						
	Description	Units	Initial Sampling Distribution	Feasible Range	<i>s</i> <sup>2</sup>	Max allowable daily rate of change ( $m_{max}$ )
β	Soil Moisture exponent	[]	N(2, 0.1)	0-7	0.003	1.8x10 <sup>-3</sup>
fcap	Maximum soil moisture store depth	[mm]	N(467, 10)	10 – 2000	0.003	0.4
hl1	Threshold for generation of near surface flow	[mm]	N(120, 10)	0 – 400	0.003	0.1
KO	Near Surface Flow Routing Coefficient	[]	N(0.3, 0.005)	0.0625 – 1	0.003	2x10 <sup>-4</sup>
<i>K</i> 1	Interflow Routing Coefficient	[]	N(0.09, 5x10⁻⁴)	0.02 - 0.1	0.003	9x10 <sup>-6</sup>
perc	Percolation rate	[mm/d]	N(1.3, 10⁻⁴)	0-3	0.003	10-3
K2	Baseflow Routing Coefficient	[]	N(0.01, 10 <sup>-6</sup> )	5x10 <sup>-5</sup> 0.02	0.003	9x10 <sup>-6</sup>
States						
sowat	Soil Moisture Store	[mm]	N(0,1)	(0, fcap)		
stw1	Shallow Layer Store	[mm]	N(0,1)	(0, ∞)		
stw2	Deep Layer Store	[mm]	N(0,0.1)	(0, ∞)		

Table 4 Locally Linear EnKF inputs for the HBV model case

Parameters						
	Description	Units	Initial Sampling Distribution	Feasible Range	<i>s</i> <sup>2</sup>	Max allowable daily rate of change ( $m_{max}$ )
b	Pareto- distributed soil storage shape parameter	[]	N(0.37, 10 <sup>-4</sup> )	0-0.3	0.004	3x10 <sup>-4</sup>
C <sub>max</sub>	Maximum point soil storage depth	[mm]	N(651, 10)	300 – 1500	0.004	0.3
k <sub>q</sub>	Quick flow Routing Coefficient	[]	N(0.6, 5x10 <sup>-4</sup> )	0.55 – 0.99	0.018	3x10 <sup>-4</sup>
k <sub>s</sub>	Slow flow Routing Coefficient	[]	N(0.04, 5x10 <sup>-4</sup> )	0.001 – 0.54	0.018	4x10 <sup>-5</sup>
α	Excess Runoff Splitting Parameter	[]	N(0.47, 5x10 <sup>-4</sup> )	0.001 – 0.99	0.018	4x10 <sup>-4</sup>
States						
S	Soil Store	[mm]	N(180, 0.1*180)	$(0, S_{max} = \frac{bc_{min} + c_{max}}{b+1})$		
<i>S</i> <sub><i>q</i>1,2,3</sub>	Quick Flow Stores	[mm]	N(0,1)	(0, ∞)		
Ss	Slow Flow Store	[mm]	N(0,1)	(0, ∞)		

Table 5 Locally Linear EnKF inputs for the HYMOD model case

#### **Figures**



Figure 1 Study Catchment showing gauges and changes in land cover over time.







Figure 2 Impact of land use change on observed streamflow: a) Annual Runoff Coefficient, b) Annual Baseflow Index (BFI), c) Moving Average Shifting Horizon (MASH) results for total observed runoff, d) MASH for observed rainfall.



Figure 3 Schematic of the models used in this study: a) HBV and b) HyMOD. Parameters are shown in blue and states are shown in green.
 797



803Figure 4 Parameter Trajectories using the HBV model. The dark grey shaded areas indicate the<br/>middle 90% of the ensemble, bounded by the 5th and 95th percentiles. The light grey shaded<br/>areas indicate the middle 50% of the ensemble, bounded by the 25th and 75th percentiles. The<br/>ensemble mean is indicated by the blue line. The vertical green panel indicates the assumed time<br/>period of rapid deforestation.



Figure 5 Parameter Trajectories using the HyMOD model. The dark grey shaded areas indicate the middle 90% of the ensemble, bounded by the 5th and 95th percentiles. The light grey shaded areas indicate the middle 50% of the ensemble, bounded by the 25th and 75th percentiles. The ensemble mean is indicated by the blue line. The vertical green panel indicates the assumed time period of rapid deforestation.



Figure 6 Representative Hydrographs of background streamflow from the LL Dual EnKF (black line),
 Time varying parameter model with no state updating (blue line), time invariant parameter model
 with no DA (green line) and observed streamflow (red line). Results for HBV are shown in the top
 row and HyMOD in the bottom row. A pre-change year (1974) is shown on the left and a post
 change year (1998) on the right.





Figure 7 Influence of time varying parameters on model output (i.e. without state updating)
summarized in terms of the Annual Runoff Coefficient (top row), Annual Direct Runoff Coefficient
(second row) and Annual Baseflow Index (BFI) (third row). Results for HyMOD are shown in the
first column, HBV are shown in the second column.



Figure 8 Moving Average Shifting Horizon (MASH) results for observed streamflow (first column),
 simulated streamflow from time varying parameter model (without state DA) for HYMOD (2nd
 column), HBV (third column), resampled climate HBV (fourth column). These are split into total
 runoff (first row) and direct runoff or surface runoff (2nd row).