

Dear Dr. Hrachowitz,

Thank you for the prompt evaluation of our revised manuscript and the positive assessment. In regards to your response regarding the benchmark: yes, we do indeed briefly compare to the time invariant parameter case and this can be considered a benchmark. We apologise for the confusion here; our intent was that no benchmark was used in investigating the impact of the model structure on the performance of the time varying parameter model, which is the main focus of the paper. The majority of the discussion is devoted to comparing the output from state and parameter updating (so called LL Dual EnKF with HBV or HyMOD) and time varying parameter model with no state updating (TVP-HBV and TVP-HyMOD).

We have added in the following statements as per your requests. Specifically, additional discussion has been provided to make clear that the time invariant parameter models were calibrated on pre-1979, and that the comparisons have been made for the time invariant parameter model evaluated over the post 1979 period. Additionally, the improvement has been quantified using the NSE.

In the methods section (Section 3.2.2, lines 348-351 of manuscript with tracked changes):

“Joint state and parameter estimation was undertaken for the Nammuc Catchment over the period 1980 to 2004 by assimilating streamflow observations into the HyMOD and HBV models at a daily time step. Additionally, simulations using the time invariant parameters obtained from calibration over the period 1973-1979 were generated for 1980 to 2004, for comparison.”

In the results section (Section 4, lines 463-470 of manuscript with tracked changes):

“Streamflow predictions from the LL Dual EnKF (i.e. with state and parameter updating) for both the HyMOD and HBV are generally of similar quality and superior to those from the respective time invariant parameter models that have been calibrated on pre-change data (1975-1979), although a slight bias in baseflow predictions from HyMOD is evident (see for example Figure 6). The Nash Sutcliffe Efficiency of one step ahead streamflow predictions over the period 1980 – 2004 from the LL Dual EnKF is 0.87 when using HyMOD or HBV, compared to 0.76 and 0.72 for the respective time invariant parameter models evaluated over the same period. However, differences in predictions from TVP-HBV and TVP-HyMOD are more striking due to the lack of state updating.”

We hope this clarifies any ambiguities, and we look forward to your response. Thank you for your time and consideration.

Best Regards,

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Time varying parameter models for catchments with land use

change: the importance of model structure

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1 **Abstract**

2 Rapid population and economic growth in South-East-Asia has been accompanied by extensive land
3 use change with consequent impacts on catchment hydrology. Modelling methodologies capable of
4 handling changing land use conditions are therefore becoming ever more important, and are
5 receiving increasing attention from hydrologists. A recently developed Data Assimilation based
6 framework that allows model parameters to vary through time in response to signals of change in
7 observations is considered for a medium sized catchment (2880 km²) in Northern Vietnam
8 experiencing substantial but gradual land cover change. We investigate the efficacy of the method
9 as well as the importance of the chosen model structure in ensuring the success of a time varying
10 parameter method. The method was used with two lumped daily conceptual models (HBV and
11 HyMOD) that gave good quality streamflow predictions during pre-change conditions. Although both
12 time varying parameter models gave improved streamflow predictions under changed conditions
13 compared to the time invariant parameter model, persistent biases for low flows were apparent in
14 the HyMOD case. It was found that HyMOD was not suited to representing the modified baseflow
15 conditions, resulting in extreme and unrealistic time varying parameter estimates. This work shows
16 that the chosen model can be critical for ensuring the time varying parameter framework
17 successfully models streamflow under changing land cover conditions. It can also be used to
18 determine whether land cover changes (and not just meteorological factors) contribute to the
19 observed hydrologic changes in retrospective studies where the lack of a paired control catchment
20 precludes such an assessment.

21 **1. Introduction**

22 Population and economic growth in South-East Asia has led to significant land use change, with rapid
23 deforestation occurring largely for agricultural purposes [Kummer and Turner, 1994]. Forest cover in
24 the Greater Mekong Sub-region (comprising Myanmar, Thailand, Cambodia, Laos, Vietnam, and
25 South China) has decreased from about 73% in 1973 to about 51% in 2009 [WWF, 2013]. Vietnam in
26 particular has had the second highest rate of deforestation of primary forest in the world, based on
27 estimates from the Forest Resource Assessment by the United Nations Food and Agriculture
28 Organization [FAO, 2005]. Such extensive land use change has the potential to significantly alter
29 catchment hydrology (in terms of both quantity and quality), with its effects sometimes not
30 immediate but occurring gradually over a lengthy period of time. Recent estimates from satellite
31 measurements indicate that rapid deforestation continues in the region, although at lower rates [e.g.
32 Kim et al., 2015]. Persistent land use change necessitates modelling methodologies that are capable
33 of providing accurate hydrologic forecasts and predictions, despite non-stationarity in catchment
34 processes. This is also particularly relevant for water resource management which requires reliable
35 estimates of water availability, both in terms of volume and timing, to properly allocate the resource
36 between different water uses and to prevent flood damages. Vietnam has built many reservoirs in
37 the last decades and more are planned because they are considered to be fundamentally important
38 for electricity production, flood control, water supply and irrigation, ultimately contributing to the
39 development of the country [Giuliani et al., 2016].

40

41 The literature on land-use change and its impacts on catchment hydrology is extensive, with studies
42 examining the effects of 1) conversion to agricultural land-use [Thanapakpawin et al, 2007;
43 Warburton et al., 2012]; 2) deforestation [Costa et al., 2003; Coe et al, 2011]; 3) afforestation [e.g.
44 Yang et al., 2012; Brown et al, 2013] and 4) urbanization [Bhaduri et al., 2001; Rose & Peters, 2001].
45 Fewer studies have examined how traditional modelling approaches must be modified to handle

46 non-stationary conditions, or how modelling methods can be used to assess impacts of land use
47 change. Split sample calibration has been used frequently to retrospectively examine changes to
48 model parameters due to land use or climatic change [Seibert & McDonnell, 2010; Coron et al., 2012;
49 McIntyre & Marshall, 2010; Legesse et al, 2003]. Several other studies have employed scenario
50 modelling, whereby hydrologic models are parameterized to represent different possible future land
51 use conditions [e.g. Niu & Sivakumar, 2013; Elfert & Borman, 2010]. A related approach involves
52 combining land use change forecast models with hydrologic models [e.g. Wijesekara et al., 2012].
53 However, the aforementioned approaches are unsuited to hydrologic forecasting in changing
54 catchments, as the predicted land use change may not reflect actual changes. A potentially more
55 suitable approach in such a setting is to allow model parameters to vary in time, rather than
56 assuming a constant optimal value or stationary probability distribution. Many existing methods
57 utilising such a framework require some *a priori* knowledge of the land use change in order to inform
58 variations in model parameters (see for instance Efstratiadis, 2015; Brown et al., 2006; and Westra et
59 al., 2014). Recent efforts have examined the potential for time varying parameter models to
60 automatically adapt to changing conditions using information contained in hydrologic observations
61 and sequential Data Assimilation, without requiring explicit knowledge of the changes [see for
62 example Taver et al., 2015, Pathiraja et al., 2016a&b]. Such approaches can objectively modify
63 model parameters in response to signals of change in observations in real time, whilst simultaneously
64 providing uncertainty estimates of parameters and streamflow predictions. They can also be used to
65 determine whether land cover changes (and not solely meteorological factors) contribute to
66 observed changes in streamflow dynamics in retrospective studies where the lack of a paired control
67 catchment precludes such an assessment.

68

69 Pathiraja et al. [2016a] presented an Ensemble Kalman Filter based algorithm (the so-called Locally
70 Linear Dual EnKF) to estimate time variations in model parameters. The method sequentially
71 assimilates observations into a numerical model in real time to generate improved estimates of

72 model states, fluxes and parameters based on their respective uncertainties. Its purpose is to infer
73 changes to catchment properties (e.g. land cover change) from hydrologic observations, without
74 prior knowledge of such changes, at the time scale of the available observations. It can therefore be
75 used for various applications: 1) to retrospectively estimate time variations in model parameters; 2)
76 for short-term predictive modelling (days to weeks), e.g. flood forecasting; and 3) for on-line/real
77 time water resource management, e.g. determining releases from reservoirs in catchments with
78 changing land cover conditions. In retrospective mode, the method is advantageous compared to
79 split-sample calibration type approaches since no *a priori* knowledge of land use change is needed,
80 and the modeller does not have to make somewhat arbitrary decisions about how to segregate the
81 data. When used for prediction or forecasting, states and parameters are updated sequentially using
82 all available observations up until the current time. These updated states and parameters are then
83 used along with the prior parameter generating model to produce hydrologic predictions over a short
84 time horizon. This allows one to seamlessly obtain predictions without the modeller needing to
85 explicitly modify the model to account for any catchment changes. The efficacy of the method was
86 demonstrated in *Pathiraja et al.* [2016b] through an application to small experimental catchments (<
87 350 ha) with drastic land cover changes and strong signals of change in streamflow observations.

88

89 Here we investigate two issues related to the use of time varying parameter models for prediction in
90 realistic catchments with changing land cover conditions. Firstly, we investigate the efficacy of the
91 time varying parameter method for sparsely observed, medium-sized catchments with spatially
92 complex and gradual land use change (occurring over months/years). Several authors have
93 demonstrated that impacts of land use change on the hydrologic response are dependent on many
94 factors including the type and rate of land cover conversion as well the spatial pattern of different
95 land uses within the catchment [*Dwarakish & Ganasri, 2015; Warburton et al., 2012*]. In such
96 situations, the effects of unresolved spatial heterogeneities in model inputs (e.g. rainfall) and the
97 relatively less pronounced changes in land surface conditions make time varying parameter detection

98 and accurate hydrologic prediction more difficult. The second objective is to examine the role of
99 the hydrologic model in determining the ability of the time varying parameter framework to provide
100 high quality predictions in changing conditions. Often there may be several candidate hydrologic
101 models (with time invariant parameters) that have similar predictive performance for a catchment
102 when calibrated and validated over a time series of static land cover conditions [Marshall *et al.*,
103 2006]. This work examines whether all such candidate models in time varying parameter mode are
104 also capable of providing accurate predictions under changing conditions.

105
106 These issues are investigated for the Nammuc catchment (2880 km²) in Northern Vietnam which has
107 experienced deforestation largely due to increasing agricultural development. It serves as an ideal
108 test catchment to study the efficacy of the time varying parameter algorithm due to its size, spatially
109 complex pattern of land use changes, and lack of information on the precise timing of such changes.
110 Land cover change is estimated to have occurred at varying rates, with cropland accounting for
111 roughly 23% between 1981 and 1994, and 52% by 2000. We also consider two lumped conceptual
112 hydrologic models (given the availability of point rainfall, temperature, and streamflow data)
113 operating at daily time step to address the second objective. Both models demonstrate similar
114 performance in representing streamflow at the outlet during the pre-change calibration period
115 (1975-1979), although their performance during/after land use change is unknown. Therefore, the
116 effect of the model structure (i.e. model equations) on hydrologic predictions from the time varying
117 parameter models is studied. This work represents the first application of a continuously time
118 varying parameter approach for modelling a real medium sized catchment with no *a priori* (or partial)
119 knowledge of the type and timing of land use change.

120
121 The remainder of this paper is structured as follows. Details of the study catchment and the impact
122 of land cover change are analysed in Section 2. Section 3 summarizes the experimental setup
123 including the hydrological models and the time varying parameter estimation method used. Results

124 are provided in Section 4, along with an analysis of whether the time varying model structures reflect
125 the observed catchment dynamics. Finally, we conclude with a summary of the main outcomes of
126 the study as well as proposed future work.

127 **2. The Nammuc Catchment**

128 The Nammuc catchment (2880 km²) is located in the Red River Basin, the second largest drainage
129 basin in Vietnam which also drains parts of China and Laos. The local climate is tropical monsoon
130 dominated with distinct wet (May to October) and dry (November to April) seasons. The wet season
131 tends to have high temperatures (on average 27 to 29 °C) due to south-south easterly winds that
132 bring humid air masses. Conversely, during the dry season, circulation patterns reverse carrying
133 cooler dry air masses to the basin (leading to average temperatures of 16 to 21°C). Streamflow
134 response is consequently monsoon driven, with high flows occurring between June and October
135 (generally peaking in July/August) and low flows in the December to May period (Vu, 1993). Average
136 annual rainfall at Nammuc varies between 1300 and 2000 mm (on average 1600 mm) and catchment
137 elevation ranges between 350 and 1500 m asl. A summary of catchment properties is provided in
138 [Table 1](#) for pre-change (prior to 1994) and post-change (after 1994) conditions. This separation was
139 based on available land cover information as described below.

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140 **2.1.Data & Land Cover Change**

141 [Figure 1](#) shows the available land cover information for the Nammuc catchment. Land cover
142 information for the catchment is scant, we were able to locate only two sources which unfortunately
143 do not give a complete picture over the entire time period of interest (1970 to 2004). The first land
144 cover map refers to the period 1981-1994 and was obtained by the Vietnamese Forest Inventory and
145 Planning Institute (<http://fipi.vn/Home-en.htm>). The second land cover map refers to year 2000 and
146 was obtained from the FAO Global Land Cover database
147 (<http://www.fao.org/geonetwork/srv/en/metadata.show?id=12749&currTab=simple>). A comparison

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150 of the two maps shows a reduction in forest cover in favor of cropland; Evergreen Leaf decreases
151 from about 60% to 30% whilst cropland increases from about 23% to 52%. The change in land cover
152 is patchy, although mostly concentrated in the northern part of the catchment. Because of the scant
153 information available, it is not easy to identify the precise time period of these changes. Based on the
154 available land cover map information and the changes to observed runoff (see Section 2.2), we posit
155 that a period of rapid extensive deforestation occurred in early to mid-1990s.

156

157 Daily point rainfall data is available at four precipitation stations surrounding the catchment (Dien

158 Bien, Tuan Giao, Quynh Nhai and Nammuc, see [Figure 1](#)). Catchment averaged rainfall was

159 developed as a weighted sum of the four stations with weights determined by Thiessen Polygons.

160 Daily mean temperature was calculated in a similar fashion using temperature records from the 2

161 closest gauges (Lai Chau and Quynh Nhai, see [Figure 1](#)). This was used to estimate Potential

162 Evapotranspiration through the empirical temperature-latitude based Hamon PET method [*Hamon*,

163 1961]. Daily rainfall, temperature and streamflow data was provided by the Vietnamese Institute of

164 Water Resources Planning.

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165 **2.2. Impact of Land Cover Change on Streamflow**

166 The annual runoff/direct runoff coefficient and Baseflow Index were used to assess the impact of
167 land cover change on the hydrologic regime. Baseflow was estimated using the two parameter
168 recursive baseflow filter of *Eckhardt* [2005] (see equation 1), with on-line updating of baseflow
169 estimates to match low flows:

$$b_k = \frac{1}{(1 - a \cdot BFI_{max})} [(1 - BFI_{max}) \cdot a \cdot b_{k-1} + (1 - a) \cdot BFI_{max} \cdot y_k] \quad (1)$$

170 where b_k is the estimated baseflow at time k , y_k is the total observed streamflow at time k , BFI_{max}

171 is the maximum value of the BFI (long term ratio of baseflow to total streamflow) and a is a filter

172 parameter. In this study, we adopt $BFI_{max} = 0.5$ and $a = 0.988$ based on manual optimization.

173

176 An examination of the observed streamflow and rainfall records shows that distinct changes to the
177 hydrologic regime are evident after the mid-1990s. The annual runoff coefficient ($\frac{\text{runoff}}{\text{rainfall}}$) varies
178 between 0.4 and 0.6 prior to 1994, after which it increases to between 0.6 and 0.8 until 2004 (see
179 [Figure 2a](#)). However, increases to annual yields are driven mostly by changes to baseflow volume.
180 This is evident in [Figure 2a](#), which shows that the increase in the annual direct runoff coefficient
181 ($\frac{\text{runoff} - \text{baseflow}}{\text{rainfall}}$) is less than the increase in the total runoff coefficient (roughly 0.1 increase
182 compared to 0.2 respectively). A small increase in the Annual Baseflow Index ($\frac{\text{baseflow}}{\text{runoff}}$) is apparent
183 also, from about 0.32 on average in the period 1970 to 1982 to 0.39 on average after 1994 ([Figure](#)
184 [2b](#)). This indicates that the annual increases to baseflow volume exceed the increases to direct
185 runoff volume. Similar changes were found by *Wang et al.* [2012] who analyzed records in the
186 entire Da River basin which drains the largest river in the Red River catchment. The exact physical
187 processes behind the observed increase in baseflow are not precisely known, particularly since
188 effects of land use change from forest to cropland are not unequivocal [*Price*, 2011]. Deforestation
189 may be associated to an increase in mean annual flow and baseflow because of lower interception
190 and evapotranspiration rates [e.g., *Keppeler and Ziemer*, 1990]. Nevertheless, permanent forest
191 removal may decrease baseflow because of soil compaction and lower infiltration rates [e.g.,
192 *Zimmermann et al.*, 2006; *Bormann and Klaassen*; 2008]. Some authors also show that tillage
193 practices, associated to forest conversion to cropland, can increase soil porosity, soil water content,
194 and infiltration, thus ultimately contributing to baseflow formation [e.g., *Alam et al.*, 2014].

195
196 At a seasonal time scale, it is apparent that both wet and dry season flows exhibit temporal
197 variations. We utilized the Moving Average Shifting Horizon (MASH) [*Anghileri et al.*, 2014] and
198 Mann-Kendall test to assess seasonal trends in observed streamflow, precipitation, and temperature
199 data. The MASH tool can be used to qualitatively assess inter-annual variations in the seasonal
200 pattern of a variable. It works by calculating a statistic of the data (e.g. mean) over the same block of

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204 days in consecutive years. A steady increase in baseflow is again apparent (see February to April in
205 [Figure 2c](#)), as well as increases to wet season flows (see June to September in [Figure 2c](#)). Mann-
206 Kendall test (with significance level equal to 5%) on annual and monthly streamflow time series
207 shows increasing trends in almost all months, i.e., from October to July. No concurrent increases are
208 apparent in rainfall (see [Figure 2d](#)). Also, the Mann-Kendall test applied to precipitation time series
209 does not show any statistically significant trend, except a decrease in September for Nammuc and
210 Quynh Nhai station and an increase in July for Dien Bien station. Temperature variations are not
211 evident from the MASH analysis (not shown) and no significant trend can be detected by applying the
212 Mann-Kendall test. These results indicate that changes in streamflow dynamics are likely due to land
213 use change rather than climatic impacts.

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214 3. Experimental Setup

215 3.1. Hydrologic Models

216 Conceptual lumped models operating at a daily time step were adopted due to the availability of
217 point rather than distributed hydro-meteorological data of sufficient length. We considered the
218 HyMOD [Boyle, 2001] and Hydrologiska Byrans Vattenbalansavdelning (HBV) [Bergstrom et al., 1995]
219 models. They differ mainly in the way components of the response flow are separated (HBV has near
220 surface flow, interflow, and baseflow components whilst HyMOD has a quickflow and slow flow
221 component only) and how these flows are routed. A schematic of the models is shown in [Figure 3](#).

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222
223 In the HyMOD model, spatial variations in catchment soil storage capacity are represented by a
224 Pareto distribution with shape parameter b and maximum point soil storage depth c_{max} . Excess
225 rainfall (V) is partitioned into three cascading tanks representing quick flow and a single slow flow
226 store through the splitting parameter α . Outflow from these linear routing tanks is controlled by

231 parameters k_q (for the quick flow stores) and k_s (for the slow flow store). The model has a total of 5
232 states and 5 parameters.

233

234 In the HBV model, input to the soil store is represented by a power-law function (see [Figure 3](#), note
235 the snow store is neglected for this study). Excess rainfall enters a shallow layer store which
236 generates: 1) near surface flow (q_0) whenever the shallow store state ($stw1$) is above a threshold
237 ($hl1$) and 2) interflow (q_1) by a linear routing mechanism controlled by the $K1$ parameter.
238 Percolation from the shallow layer store to the deep layer store (controlled by $perc$ parameter) then
239 leads to the generation of baseflow also via linear routing (controlled by the $K2$ parameter). Finally, a
240 triangular weighting function of base length $Maxbas$ is used to route the sum of all three flow
241 components. There are a total of 9 parameters and 3 states.

242

243 The Shuffled Complex Evolution Algorithm (SCE-UA) [Duan *et al.*, 1993] was used to calibrate HyMOD
244 and the Borg Evolutionary Algorithm [Hadka & Reed, 2013] was used to calibrate HBV. The
245 calibration algorithms were selected based on previous studies that had successfully used them for
246 calibration of these models [Reed *et al.*, 2013; Moradkhani *et al.*, 2005]. The calibration procedure
247 itself is however not critical in our study, because the optimal parameter values are only used as
248 initial values for the time varying parameter method. Both models were calibrated to pre-change
249 conditions. The period 1973 to 1979 was selected for calibration (with 2 years for spin-up) as it was
250 expected to have minimal land cover changes (and is therefore representative of pre-change
251 conditions), and also to ensure sufficient data on pre-change conditions is available for assimilation.

252 Both models had very similar performance in terms of reproducing observed runoff (a [Nash Sutcliffe](#)
253 [Efficiency](#) of 0.75 and 0.77 for HyMOD and HBV respectively). HBV was slightly better at reproducing
254 low flows whilst HyMOD was slightly better at mid-range flows (see [Table 2](#)). Here the low flow
255 threshold was defined as the average annual 50th percentile flow and the high flow threshold as the
256 average annual 85th percentile flow.

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260 3.2. Time Varying Parameter Estimation

261 A Data Assimilation based framework for estimating time varying parameters was presented in
262 *Pathiraja et al.* [2016a]. The approach relies on an Ensemble Kalman Filter (EnKF) [Evensen,1994] to
263 perform sequential joint state and parameter updating. EnKFs were developed to extend the
264 applicability of the celebrated Kalman Filter [Kalman, 1960] to non-linear systems, although they
265 provide a sub-optimal update as only the mean and covariance are considered in generating the
266 posterior. However, they have been used with much success in many hydrologic applications [see for
267 example *Reichle et al.*, 2002; *Gu et al.*, 2005; *Komma et al.*, 2008; *Sun et al.*, 2009; *Xu et al.*, 2016].
268 EnKFs offer a practical alternative to Sequential Monte Carlo/Particle Filter methods that propagate
269 the full probability density through time, but suffer from several implementation issues even in
270 moderate dimensional systems. The Locally Linear Dual EnKF method of *Pathiraja et al.* [2016a]
271 works by sequentially proposing parameters, updating these using the Ensemble Kalman filter and
272 available observations, and subsequently using these updated parameters to propose and update
273 model states. An approach for proposing parameters in the time varying setting was also presented,
274 for cases where no prior knowledge of parameter variations is available. The method was verified
275 against multiple synthetic case studies as well as for 2 small experimental catchments experiencing
276 controlled land use change [*Pathiraja et al.*, 2016a and *Pathiraja et al.*, 2016b]. The algorithm is
277 summarised below, for full details refer to *Pathiraja et al.* [2016a].

278 3.2.1. Locally Linear Dual EnKF

279 Suppose a dynamical system can be described by a vector of states \mathbf{x}_t and outputs \mathbf{y}_t and a vector of
280 associated model parameters $\boldsymbol{\theta}_t$ at any given time t . The uncertain system states and parameters
281 are represented by an ensemble of states $\{\mathbf{x}_t^i\}_{i=1:n}$ and parameters $\{\boldsymbol{\theta}_t^i\}_{i=1:n}$ each with n members.
282 The prior state and parameter distributions $\{\mathbf{x}_t^{i-}\}_{i=1:n}$ and $\{\boldsymbol{\theta}_t^{i-}\}_{i=1:n}$ respectively represent our
283 prior knowledge of the system, usually derived as the output from a numerical model. Suppose also
284 that the system outputs are observed (\mathbf{y}_t^o) but that there is also some uncertainty associated with

285 these observations. The purpose of the data assimilation algorithm (here the EnKF) is to combine the
 286 prior estimates with measurements, based on their respective uncertainties, to obtain an improved
 287 estimate of the system states and parameters. A single cycle of the Locally Linear Dual EnKF
 288 procedure for a given time t is undertaken as follows. Note in the following, the overbar notation is
 289 used to indicate the ensemble mean.

290

291 1. **Propose a prior parameter ensemble.** This involves generating a parameter ensemble using
 292 prior knowledge. In this case, our prior knowledge comes from the updated parameter
 293 ensemble from the previous time (θ_{t-1}^{i+}) and how it has changed over recent time steps. The
 294 assumed parameter dynamics is a Gaussian random walk with time varying mean and
 295 variance, given by:

$$\theta_t^{i-} \sim N(\theta_{t-1}^{i+} + \mathbf{m}_t \Delta t, s^2 \Sigma_{t-1}^\theta) \text{ for } i = 1:n \quad (2)$$

$$\Sigma_{t-1}^\theta = \frac{1}{n-1} \sum_{i=1}^n (\theta_{t-1}^{i+} - \overline{\theta_{t-1}^+}) (\theta_{t-1}^{i+} - \overline{\theta_{t-1}^+})^T \quad (3)$$

296 where Σ_{t-1}^θ is the sample covariance matrix of the updated parameter ensemble at time $t -$
 297 1; $\overline{\theta_{t-1}^+}$ indicates the ensemble mean of the updated parameters at time $t - 1$; $()^T$
 298 represents the transpose operator; and s^2 is a tuning parameter. The prior ensemble mean
 299 is determined as the linear extrapolation of the updated ensemble means from the previous
 300 two time steps, i.e.:

$$\mathbf{m}_t[k] = \begin{cases} \mathbf{m}_{t-1}[k], & |\mathbf{m}_{t-1}[k]| \leq m_{max} \\ \mathbf{m}_{t-2}[k], & |\mathbf{m}_{t-1}[k]| > m_{max} \end{cases} \quad (4)$$

$$\mathbf{m}_{t-1} = \frac{\overline{\theta_{t-1}^+} - \overline{\theta_{t-2}^+}}{\Delta t} \quad (5)$$

$$\mathbf{m}_{t-2} = \frac{\overline{\theta_{t-2}^+} - \overline{\theta_{t-3}^+}}{\Delta t} \quad (6)$$

301 where $\mathbf{m}_t[k]$ indicates the k th component of the vector \mathbf{m}_t , the estimated rate of change.

302 Note that the extrapolation is forced to be less than a pre-defined maximum rate of change

303 m_{max} to minimise overfitting and avoid parameter drift due to isolated large updates. The

304 maximum rate of change is model specific and will depend on the modeller's judgement
 305 regarding expected extreme changes.

306 2. **Consider observation and forcing uncertainty.** This is done by perturbing measurements of
 307 forcings and system outputs with random noise sampled from a distribution representing the
 308 uncertainty in those measurements. The result is an ensemble of forcings (\mathbf{u}_t^i) and
 309 observations (\mathbf{y}_t^i) each with n members. For example, if random errors in measurements of
 310 system outputs (herein also referred as observations) are characterized by a zero mean
 311 Gaussian distribution, the ensemble of observations is given by:

$$\mathbf{y}_t^i \sim N(\mathbf{y}_t^o, \Sigma_t^{y^o y^o}) \text{ for } i = 1:n \quad (7)$$

312 where \mathbf{y}_t^o is the recorded measurement at time t and $\Sigma_t^{y^o y^o}$ is the error covariance matrix of
 313 the measurements.

314 3. **Generate simulations using prior parameters.** The prior parameters from Step 1, θ_t^{i-} and
 315 updated states from the previous time, \mathbf{x}_{t-1}^{i+} are forced through the model equations to
 316 generate an ensemble of model simulations of states ($\hat{\mathbf{x}}_t^i$) and outputs ($\hat{\mathbf{y}}_t^i$):

$$\hat{\mathbf{x}}_t^i = f(\mathbf{x}_{t-1}^{i+}, \theta_t^{i-}, \mathbf{u}_t^i) \text{ for } i = 1:n \quad (8)$$

$$\hat{\mathbf{y}}_t^i = h(\hat{\mathbf{x}}_t^i, \theta_t^{i-}) \text{ for } i = 1:n \quad (9)$$

317 4. **Perform the Kalman update of parameters.** Parameters are updated using the Kalman
 318 update equation and the prior parameter and simulated output ensemble from Step 1 and 3:

$$\theta_t^{i+} = \theta_t^{i-} + \mathbf{K}_t^\theta (\mathbf{y}_t^i - \hat{\mathbf{y}}_t^i) \text{ for } i = 1:n \quad (10)$$

$$\mathbf{K}_t^\theta = \Sigma_t^{\theta \hat{\mathbf{y}}} \left[\Sigma_t^{\hat{\mathbf{y}} \hat{\mathbf{y}}} + \Sigma_t^{y^o y^o} \right]^{-1} \quad (11)$$

319 where $\Sigma_t^{\theta \hat{\mathbf{y}}}$ is a matrix of the sample cross covariance between errors in parameters θ_t^{i-} and
 320 simulated output $\hat{\mathbf{y}}_t^i$; and $\Sigma_t^{\hat{\mathbf{y}} \hat{\mathbf{y}}}$ is the sample error covariance matrix of the simulated output:

$$\Sigma_t^{\theta \hat{\mathbf{y}}} = \frac{1}{n-1} \sum_{i=1}^n (\theta_t^{i-} - \bar{\theta}_t) (\hat{\mathbf{y}}_t^i - \bar{\hat{\mathbf{y}}}_t)^\top \quad (12)$$

$$\Sigma_t^{\hat{\mathbf{y}} \hat{\mathbf{y}}} = \frac{1}{n-1} \sum_{i=1}^n (\hat{\mathbf{y}}_t^i - \bar{\hat{\mathbf{y}}}_t) (\hat{\mathbf{y}}_t^i - \bar{\hat{\mathbf{y}}}_t)^\top \quad (13)$$

321 5. **Generate simulations using updated parameters.** Step 3 is repeated with the updated
 322 parameter ensemble θ_t^{i+} to generate the prior ensemble of model simulations of states (x_t^{i-})
 323 and outputs (\tilde{y}_t^i):

$$x_t^{i-} = f(x_{t-1}^{i+}, \theta_t^{i+}, u_t^i) \text{ for } i = 1:n \quad (14)$$

$$\tilde{y}_t^i = h(x_t^{i-}, \theta_t^{i+}) \text{ for } i = 1:n \quad (15)$$

324 6. **Perform the Kalman update of states and outputs.** Use the Kalman update equation for
 325 correlated measurement and process noise (equations 16 to 19) and the simulated state
 326 (x_t^{i-}) and output (\tilde{y}_t^i) ensembles from Step 5 to update them. Since the measurements have
 327 already been used to generate \tilde{y}_t^i , the errors in model simulations and measurements are
 328 now correlated. The standard Kalman update equation (as in the form of equations 10 and
 329 11) can no longer be used as it relies on the assumption that errors in measurements and
 330 model simulations are independent.

$$x_t^{i+} = x_t^{i-} + K_t^x (y_t^i - \tilde{y}_t^i) \text{ for } i = 1:n \quad (16)$$

$$K_t^x = [\Sigma_t^{x\tilde{y}} + \Sigma_t^{\varepsilon_x y^o}] [\Sigma_t^{\tilde{y}\tilde{y}} + \Sigma_t^{\varepsilon_{\tilde{y}} y^o} + (\Sigma_t^{\varepsilon_{\tilde{y}} y^o})^T + \Sigma_t^{y^o y^o}]^{-1} \quad (17)$$

$$\varepsilon_{x_t}^i = x_t^{i-} - \hat{x}_t^i \quad (18)$$

$$\varepsilon_{\tilde{y}_t}^i = \tilde{y}_t^i - \hat{y}_t^i \quad (19)$$

331 where $\Sigma_t^{x\tilde{y}}$ is a matrix of the sample cross covariance between simulated states $\{x_t^{i-}\}_{i=1:n}$
 332 and outputs $\{\tilde{y}_t^i\}_{i=1:n}$ from Step 5; $\Sigma_t^{\varepsilon_x y^o}$ represents the sample covariance between
 333 $\{\varepsilon_{x_t}^i\}_{i=1:n}$ and the observations; and $\Sigma_t^{\varepsilon_{\tilde{y}} y^o}$ represents the sample covariance between the
 334 $\{\varepsilon_{\tilde{y}_t}^i\}_{i=1:n}$ and the observations.

335 The above algorithm specifies the updating of states and parameters at any given time, based on
 336 available observations. This allows one to retrospectively estimate time variations in model
 337 parameters, as well as provide one time step ahead forecasts of states & outputs (as per equations 8
 338 and 9). Forecasts at longer time horizons (i.e. longer than one time step ahead) would be made by

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345 generating prior parameters and states as detailed in Steps 1 to 3, although the local linear
346 extrapolations are only valid close to the current time point.

347 3.2.2. Application to the Nammuc Catchment

348 Joint state and parameter estimation was undertaken for the Nammuc Catchment over the period
349 1980 to 2004 by assimilating streamflow observations into the HyMOD and HBV models at a daily
350 time step. Additionally, simulations using the time invariant parameters obtained from calibration

351 over the period 1973-1979 were generated for 1980 to 2004, for comparison. Estimating a large
352 number of parameters from limited data is problematic in that the system is highly under-

353 determined, making it difficult to ensure the estimated parameters are meaningful. Given the fairly

354 low parameter dimensionality of HyMOD, all model parameters were allowed to vary in time whilst

355 for HBV we applied the Sobol method to identify the most sensitive parameters to be included in the

356 time varying parameter estimation. The Sobol method is a global sensitivity analysis method based

357 on variance decomposition. It identifies the partial variance contribution of each parameter to the

358 total variance of the hydrological model output [see for example *Saltelli et al., 2008, Nossent et al.*

359 *2011*]. The method, implemented through the SAFE toolbox [*Pianosi et al., 2015*], found the *lp* and

360 *Maxbas* parameters to be the least sensitive and least important in defining variations to catchment

361 hydrology (see Table 3). These were held fixed (*lp* = 1 and *Maxbas* = 1 day) in the following analysis.

362 Note that although the *hl1* parameter was found to have low sensitivity, it was retained as a time

363 varying parameter due to its conceptual importance in separating interflow and near surface flow

364 (refer [Figure 3](#)).

365

366 Unbiased normally distributed ensembles of the parameters and states are required to initialise the

367 LL Dual EnKF. Initial parameter ensembles were generated by sampling from a Gaussian distribution

368 with mean equal to the calibrated parameters over the pre-change period and variance estimated

369 from parameter sets with similar objective function values. Parameter sets with similar objective

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373 function values were obtained when using different starting points to the optimization algorithm
374 during the model calibration stage. Initial state ensembles were also sampled from normal
375 distributions with mean equal to the simulated state at the end of the calibration period. An
376 ensemble size of 100 members was adopted and assumed sufficiently large based on the findings of
377 *Moradkhani et al.* [2005] and *Aksoy et al.* [2006]. Due to the stochastic-dynamic nature of the
378 method, ensemble statistics were calculated over 20 separate realisations of the LL Dual EnKF. The
379 prior parameter generating method described in Step 1 of Section 3.2 requires specification of the
380 tuning parameter s^2 to define the variance of the perturbations. This was tuned by selecting the s^2
381 value that optimized the quality of forecast streamflow over the calibration period. Forecast quality
382 was assessed using the logarithmic score (LS) [*Good, 1952*] of background streamflow predictions
383 (\tilde{y}_t^i) using updated parameters (equation 15), which was averaged over the calibration period of
384 length T :

$$\overline{LS} = \sum_{t=1}^T LS_t \quad (20)$$

$$LS_t = \log (f(y = y_t^o)) \quad (21)$$

385 where $f(y)$ is the probability density function of the background streamflow predictions
386 (represented by the empirical pdf of the sample points $\{\tilde{y}_t^i\}_{i=1:n}$); and y_t^o is the measurement of the
387 system outputs. The s^2 value that gave the largest \overline{LS} was adopted for the assimilation period. The
388 maximum allowable daily rate of change in the ensemble mean was based on assuming a linear rate
389 of change within the entire feasible parameter space over a three year period.

390
391 As detailed in Section 3.2, observation and forcing uncertainty is considered by perturbing
392 measurements with random noise. Here streamflow errors were assumed to be zero-mean normally
393 distributed (truncated to ensure positivity) and heteroscedastic. The variance is defined as a
394 proportion of the observed streamflow, to reflect the fact that larger flows tend to have greater
395 errors than low flows:

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$$y_t^i \sim TN(y_t^0, d, y_t^0) \text{ for } i = 1:n \quad (22)$$

397 where TN indicates the truncated normal distribution to ensure positive flows and $d = 0.1$. A
 398 multiplier of 0.1 was chosen based on estimates adopted for similar gauges in hydrologic DA studies
 399 [e.g. Clark et al., 2008; Weerts & Serafy, 2006; Xie et al., 2014].

400

401 Several studies have noted that a major source of rainfall uncertainty arises from scaling point
 402 rainfall to the catchment scale [Villarini & Krajewski, 2008; McMillan et al., 2011] and that
 403 multiplicative errors models are suited to describing such errors [e.g. Kavetski et al., 2006]. Rainfall
 404 uncertainties were therefore described using unbiased, lognormally distributed multipliers:

$$P_t^i = P_t \cdot M^i \quad (23)$$

$$M^i \sim LN(m, v) \text{ and } X^i = \log(M^i) \sim N(\mu, \sigma^2) \text{ for } i = 1:n \quad (24)$$

405 where P_t is the measured rainfall at time t ; m and v are the mean and variance of the lognormally
 406 distributed rainfall multipliers M respectively; and μ and σ^2 are the mean and variance of the
 407 normally distributed logarithm of the rainfall multipliers M . For unbiased perturbations, we let $m =$
 408 1. The variance of the rainfall multipliers (v) was estimated by considering upper and lower bound
 409 error estimates in the Thiessen weights assigned to the four rainfall stations (see Section 2.1 for
 410 calculation of catchment averaged rainfall, P_t). The resulting upper and lower bound catchment
 411 averaged rainfall data were then used to estimate error parameters due to spatial variation in
 412 rainfall:

$$v = e^{(2\mu + \sigma^2)} \cdot (e^{\sigma^2} - 1) \quad (25)$$

$$\sigma^2 = \widehat{\sigma^2} = \text{var} \left(\log \left[\frac{P_{upper,10}}{P_{lower,10}} \right] \right) \quad (26)$$

$$\mu = \log(m) - \frac{\sigma^2}{2} = -\frac{\sigma^2}{2} \quad (27)$$

413 where $P_{upper,10}$ indicates catchment averaged rainfall data estimated using the upper bound
 414 Thiessen weights with daily depth greater than 10mm (similar for $P_{lower,10}$). A 10mm rainfall depth
 415 threshold was chosen to avoid large rainfall fractions due to small rainfall depths. $\widehat{\sigma^2}$ was found to

416 be 0.05 in this case study. Similarly, we assume the dominant source of uncertainty in temperature
417 data arises from spatial variation. Differences in temperature records at Lai Chau and Quynh Nhai
418 (only available gauges with temperature records) were analysed and found to be approximately
419 normally distributed with sample mean 0.2 deg C and variance of 1.4 deg C. A perturbed
420 temperature ensemble was then generated according to equation 28;

$$T_t^i \sim TN(T_t^{avg}, 1.4) \text{ for } i = 1:n \quad (28)$$

421 where T_t^{avg} represents catchment averaged temperature data (see Section 2.1). Note that
422 perturbations were taken to be unbiased (zero mean) as the sample mean of the differences in the
423 temperature records was close to zero. The same perturbed input and observation sequences were
424 used for the HyMOD and HBV runs for the sake of comparison. A summary of the values adopted for
425 the various components of the Locally Linear Dual EnKF for each model is provided in [Table 4](#) and
426 [Table 5](#).

427 4. Results and Discussion

428 Temporal variations in the estimated parameter distributions from the LL Dual EnKF are evident for
429 both models (see Figure 4 and 5). In the case of the HBV model, changes at an inter-annual time
430 scale are evident for the $perc$ and β (see [Figure 4](#)). The decrease in the β parameter means that a
431 greater proportion of rainfall is converted to runoff (i.e. more water entering the shallow layer
432 storage). Additionally, the increase in the $perc$ parameter means that a greater volume of water is
433 made available for baseflow generation. These changes correspond with the observed increase in
434 the annual runoff coefficient ([Figure 2](#)) and increase in baseflow volume (as discussed in Section 2.2).
435 From an algorithm perspective, these parameters are most strongly correlated with streamflow (as
436 well as the most sensitive, see Table 3), meaning that they will receive the greatest proportional
437 updates. Similar parameter adjustments are seen for HyMOD, at least at a qualitative level (see
438 [Figure 5](#)). The sharp increase in the b parameter during the post-change period means that a greater

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445 volume of water is available for routing (as larger b values mean that a smaller proportion of the
446 catchment has deep soil storage capacity) and the downward inter-annual trend in α means that a
447 greater portion of excess runoff is routed through the baseflow store. Intra-annual variations in
448 updated model parameters for both HyMOD and HBV are also apparent (refer [Figure 4](#) and [Figure 5](#)).
449 This is due to the inability of a single parameter distribution to accurately model both wet and dry
450 season flows. Such variations were not observed when using the time varying parameter framework
451 for small deforested catchments (< 350ha) [see *Pathiraja et al.*, 2016b]. The comparatively less clear
452 parameter changes for the Nammuc catchment are due to a combination of the increased difficulty
453 in accurately modelling the hydrologic response (even in pre-change conditions) and due to the
454 relatively more subtle and gradual changes to land cover. Nonetheless, the method is shown to
455 generate a temporally varying structure that is conceptually representative of the observed changes.

456
457 Despite the overall correspondence between changes to model parameters and observed
458 streamflow, a closer examination shows that the hydrologic model structure is critical in determining
459 whether the time varying parameter models accurately reflect changes in all aspects of the
460 hydrologic response (not just total streamflow). In order to examine the impact of parameter
461 variations on the model dynamics, we generated model simulations with the time varying parameter
462 ensemble from the LL Dual EnKF, but without state updating (hereafter referred to as TVP-HBV and
463 TVP-HyMOD). Streamflow predictions from the LL Dual EnKF (i.e. with state and parameter updating)
464 for both the HyMOD and HBV are generally of similar quality and superior to those from the

465 respective time invariant parameter models [that have been calibrated on pre-change data \(1975-](#)
466 [1979\)](#), although a slight bias in baseflow predictions from HyMOD is evident (see for example [Figure](#)
467 [6](#)). [The Nash Sutcliffe Efficiency of one step ahead streamflow predictions over the period 1980 –](#)
468 [2004 from the LL Dual EnKF is 0.87 when using HyMOD or HBV, compared to 0.76 and 0.72 for the](#)
469 [respective time invariant parameter models evaluated over the same period.](#) However, differences
470 in predictions from TVP-HBV and TVP-HyMOD are more striking due to the lack of state updating.

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475 [Figure 7](#) shows annual statistics of simulated streamflow from the TVP-HBV and TVP-HyMOD models
476 and observed runoff. The TVP-HBV gives direct runoff and baseflow predictions that are consistent
477 with runoff observations, meaning that the parameter adjustments reflect the observed changes in
478 the runoff response. This however is not the case for the TVP-HyMOD. The annual runoff coefficient
479 and annual direct runoff coefficient are severely under-estimated in the post-change period by the
480 TVP-HyMOD, whilst the Annual Baseflow Index has an increasing trend of magnitude far greater than
481 observed ([Figure 7c](#)). All three quantities on the other hand are well represented by the TVP-HBV
482 ([Figure 7](#)). Similar conclusions can be drawn from [Figure 8](#), which shows the results of a Moving
483 Average Shifting Horizon (MASH) analysis (see Section 2.2) on total and direct runoff (observed and
484 simulated). Observed increases in January to April flows (see [Figure 8a](#)) and wet season direct flows
485 (July to September) (see [Figure 8e](#)) are well represented by the TVP-HBV but not TVP-HyMOD.
486
487 The reason for the differences in performance between the TVP-HBV and TVP-HyMOD lies in the
488 structure of the hydrologic model. The TVP-HyMOD is incapable of representing the observed
489 increase in annual runoff/direct runoff coefficient due to the increased baseflow during dry periods,
490 despite having an Annual Baseflow Index far greater than the observed. This occurs due to an
491 inability to generate flow volume during periods of no rain. In joint state-parameter updating using
492 HyMOD, underestimated runoff predictions during dry periods lead to adjustments to the k_s and α
493 parameters to increase baseflow depth (since these are the only parameters that are associated to
494 an active store). Unlike HBV, HyMOD has no continuous supply of water to the routing stores (i.e.
495 the quick flow and slow flow stores) during recession periods (which typically have extended periods
496 of no rainfall, so that V in [Figure 3](#) is zero). This means that k_s and α are updated to extreme values
497 to compensate for the volumetric shortfall. The HBV structure, on the other hand, has a continuous
498 percolation of water into the deep layer store even during periods of no rain (so long as the shallow
499 water store is non-empty). In summary, the HyMOD model structure is poorly suited to simulating
500 streamflow dynamics in post-change conditions, although it gave reasonable simulations in pre-

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508 change conditions. This highlights that need to select a sufficiently flexible model structure prior to
509 undertaking forecasting/predictive modelling using the time varying parameter approach. In
510 particular, the model structure must be capable of effectively simulating all potential future
511 catchment conditions.

512
513 Having established that the TVP-HBV provided a good representation of the observed streamflow
514 dynamics, we used a modelling approach to determine whether the observed changes were solely
515 driven by forcings and which (if any) components of runoff were also affected by land use change. A
516 resampled rainfall and temperature time series was generated by sampling the data without
517 replacement across years for each day (for instance rainfall and temperature for 1st January 1990 is
518 found by randomly sampling from all records on 1st January). This maintains the intra-annual (e.g.
519 seasonal) variability but destroys any inter-annual trends in the meteorological data. Streamflow
520 simulations were then generated using this resampled meteorological sequence as inputs to the TVP-
521 HBV (i.e. without state updating). If the resulting streamflow simulations do not reproduce the
522 observed changes to streamflow dynamics, then this indicates that changes to meteorological
523 forcings are the main contributor. However, if it is able to at least partially (or fully) reproduce the
524 observed streamflow changes, this means that land cover changes are impacting catchment
525 hydrology (but potentially in addition to forcing changes, due to the presence of ecosystem

526 feedbacks). [Figure 8d&h](#) show the results of a MASH undertaken on the resulting simulations of total
527 and direct runoff using the resampled forcing time series and TVP-HBV model. Observed increases in
528 baseflow during the January – April period (see [Figure 8a](#)) and increases in direct runoff in the June –
529 September period (see [Figure 8e](#)) are reproduced. The magnitude of increase in direct runoff in July
530 is slightly lower, indicating the potential for some climatic influences also. This is consistent with
531 findings from the Mann-Kendall test which identified a statistically significant increase in July rainfall
532 (see Section 2.2). Overall however, these results lend further weight to the conclusion that land
533 cover change has impacted the hydrologic regime of the Nammuc catchment. These results also

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537 demonstrate that parameter changes correspond to actual changes in catchment hydrology, and are
538 not just random fluctuations that reproduce the observed streamflow statistics only when the
539 observed forcing time series is used.

540 **5. Conclusions**

541 As our anthropogenic footprint expands, it will become increasingly important to develop modelling
542 methodologies that are capable of handling changing catchment conditions. Previous work proposed
543 the use of models whose parameters vary with time in response to signals of change in observations.
544 The so-called Locally Linear Dual EnKF time varying parameter estimation algorithm [*Pathiraja et al.,*
545 2016a] was applied to 2 sets of small (< 350 ha) paired experimental catchments with deforestation
546 occurring under experimental conditions (rapid clearing of 100% and 50% of land surface) [*Pathiraja*
547 *et al., 2016b*]. Here we demonstrate the efficacy of the method for a larger catchment experiencing
548 more realistic land cover change, whilst also investigating the importance of the chosen model
549 structure in ensuring the success of the time varying parameter estimation method. We also
550 demonstrate that the time varying parameter framework can be used in a retrospective fashion to
551 determine whether land cover changes (and not just meteorological factors) contribute to the
552 observed hydrologic changes.

553

554 Experiments were undertaken on the Nammuc catchment (2880 km²) in Vietnam, which experienced
555 a relatively gradual conversion from forest to cropland over a number of years (cropland increased
556 from roughly 23% of the catchment between 1981 and 1994 to 52% by 2000). Changes to the
557 hydrologic regime after the mid-1990s were detected and attributed mostly to an increase in
558 baseflow volume. Application of the LL Dual EnKF with two conceptual models (HBV and HyMOD)
559 showed that the time varying parameter framework with state updating improved streamflow
560 prediction in post-change conditions compared to the time invariant parameter case. However,
561 baseflow predictions from the LL Dual EnKF with HBV were generally superior to the HyMOD case

562 which tended to have a slight negative bias. It was found that the structure (i.e. model equations) of
563 HyMOD was unsuited to representing the modified baseflow conditions, resulting in extreme and
564 unrealistic time varying parameter estimates. This work shows that the chosen model is critical for
565 ensuring the time varying parameter framework successfully models streamflow in unknown future
566 land cover conditions, particularly when used in a real time forecasting mode. Appropriate model
567 selection can be a difficult task due to the significant uncertainty associated with future land use
568 change, and can be even more problematic when multiple models have similar performance in pre-
569 change conditions (as was the case in this study). One possible way to ensure success of the time
570 varying parameter approach is to use models whose fundamental equations explicitly represent key
571 physical processes (for instance, modelling sub-surface flow using Richard's equation with hydraulic
572 conductivity allowed to vary with time). In this way, time variations in model parameters would
573 more closely reflect changes to physiographic properties, rather than also having to account for
574 missing processes. The drawback of such physically based models is that they are generally data
575 intensive, both in generating model simulations (i.e. detailed inputs) and specifying parameters.
576 Additionally, it may be necessary to reduce the dimensionality of the time varying parameter vector
577 by keeping less sensitive model parameters fixed in order to make the estimation problem tractable.
578 Models of intermediate complexity that have explicit process descriptions may be the most
579 promising, although this also remains to be demonstrated.

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585

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590
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Tables

	Pre 1994	Post 1994
Land Use		
Evergreen Forest (including evergreen needle and evergreen leaf) (%)	77%	48%
Cropland (%)	23%	52%
Hydro-Meteorological Properties		
Mean Annual Rainfall (mm)	1630	1660
Mean Annual Runoff (mm)	838	1190
Mean Annual Runoff Coefficient	0.5	0.7
Mean Annual PET (mm)	1300	1300
Estimated Mean Annual BFI	0.33	0.39

Table 1 Study catchment properties

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	HYMOD	HBV
NSE []	0.77	0.75
<i>Peak flows ($q > 5\text{mm/d}$)</i>		
MAE [mm/d]	3.11	2.85
RMSE [mm/d]	4.55	4.72
<i>Medium flows ($1\text{ mm/d} \leq q \leq 5\text{mm/d}$)</i>		
MAE [mm/d]	0.66	0.80
RMSE [mm/d]	0.86	1.09
<i>Low flows ($q < 1\text{mm/d}$)</i>		
MAE [mm/d]	0.35	0.20
RMSE [mm/d]	0.42	0.34

790 **Table 2 Model performance in pre-change conditions used for calibration (1975 – 1979). Bold face**
791 **numbers correspond to the model with superior performance for the particular metric. NSE = Nash**
792 **Sutcliffe Efficiency; MAE = Mean Absolute Error; RMSE = Root Mean Squared Error.**

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	Sensitivity Index
<i>h1</i>	0.10
<i>lp</i>	0.12
<i>Maxbas</i>	0.14
<i>fcap</i>	0.18
<i>k0</i>	0.23
<i>k2</i>	0.23
<i>k1</i>	0.38
<i>beta</i>	0.41
<i>perc</i>	0.47

797 **Table 3 Variance Based Sensitivity Analysis Results for HBV parameters: first order sensitivity index**
798 **representing the contribution of varying a single parameter to the variance of the model output.**
799 **Lower values indicate lower sensitivity.**

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Parameters						
	Description	Units	Initial Sampling Distribution	Feasible Range	s^2	Max allowable daily rate of change (m_{max})
β	Soil Moisture exponent	[]	$N(2, 0.1)$	0 – 7	0.003	1.8×10^{-3}
f_{cap}	Maximum soil moisture store depth	[mm]	$N(467, 10)$	10 – 2000	0.003	0.4
$hl1$	Threshold for generation of near surface flow	[mm]	$N(120, 10)$	0 – 400	0.003	0.1
$K0$	Near Surface Flow Routing Coefficient	[]	$N(0.3, 0.005)$	0.0625 – 1	0.003	2×10^{-4}
$K1$	Interflow Routing Coefficient	[]	$N(0.09, 5 \times 10^{-4})$	0.02 – 0.1	0.003	9×10^{-6}
$perc$	Percolation rate	[mm/d]	$N(1.3, 10^{-4})$	0 – 3	0.003	10^{-3}
$K2$	Baseflow Routing Coefficient	[]	$N(0.01, 10^{-6})$	5×10^{-5} – 0.02	0.003	9×10^{-6}
States						
$sowat$	Soil Moisture Store	[mm]	$N(0,1)$	$(0, f_{cap})$		
$stw1$	Shallow Layer Store	[mm]	$N(0,1)$	$(0, \infty)$		
$stw2$	Deep Layer Store	[mm]	$N(0,0.1)$	$(0, \infty)$		

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Table 4 Locally Linear EnKF inputs for the HBV model case

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Parameters						
	Description	Units	Initial Sampling Distribution	Feasible Range	s^2	Max allowable daily rate of change (m_{max})
b	Pareto-distributed soil storage shape parameter	[]	$N(0.37, 10^{-4})$	0 – 0.3	0.004	3×10^{-4}
c_{max}	Maximum point soil storage depth	[mm]	$N(651, 10)$	300 – 1500	0.004	0.3
k_q	Quick flow Routing Coefficient	[]	$N(0.6, 5 \times 10^{-4})$	0.55 – 0.99	0.018	3×10^{-4}
k_s	Slow flow Routing Coefficient	[]	$N(0.04, 5 \times 10^{-4})$	0.001 – 0.54	0.018	4×10^{-5}
α	Excess Runoff Splitting Parameter	[]	$N(0.47, 5 \times 10^{-4})$	0.001 – 0.99	0.018	4×10^{-4}
States						
S	Soil Store	[mm]	$N(180, 0.1 \cdot 180)$	$(0, S_{max} = \frac{b c_{min} + c_{max}}{b+1})$		
$S_{q1,2,3}$	Quick Flow Stores	[mm]	$N(0,1)$	$(0, \infty)$		
S_s	Slow Flow Store	[mm]	$N(0,1)$	$(0, \infty)$		

808 **Table 5 Locally Linear EnKF inputs for the HYMOD model case**

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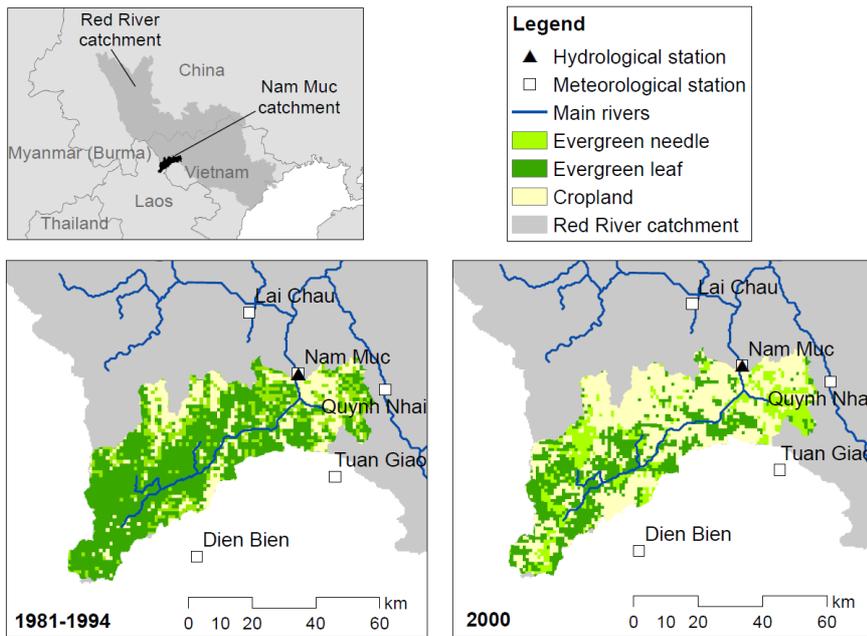
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814 **Figures**

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Figure 1 Study Catchment showing gauges and changes in land cover over time.

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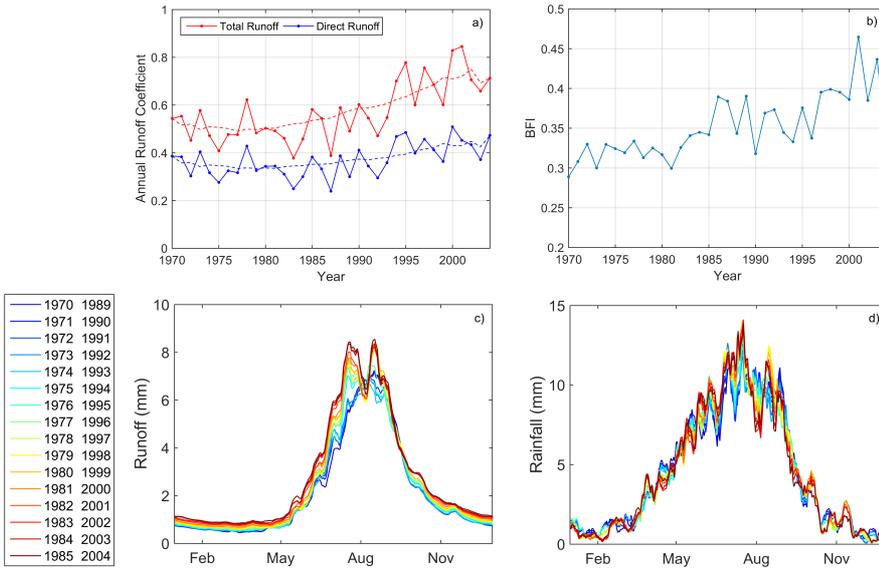
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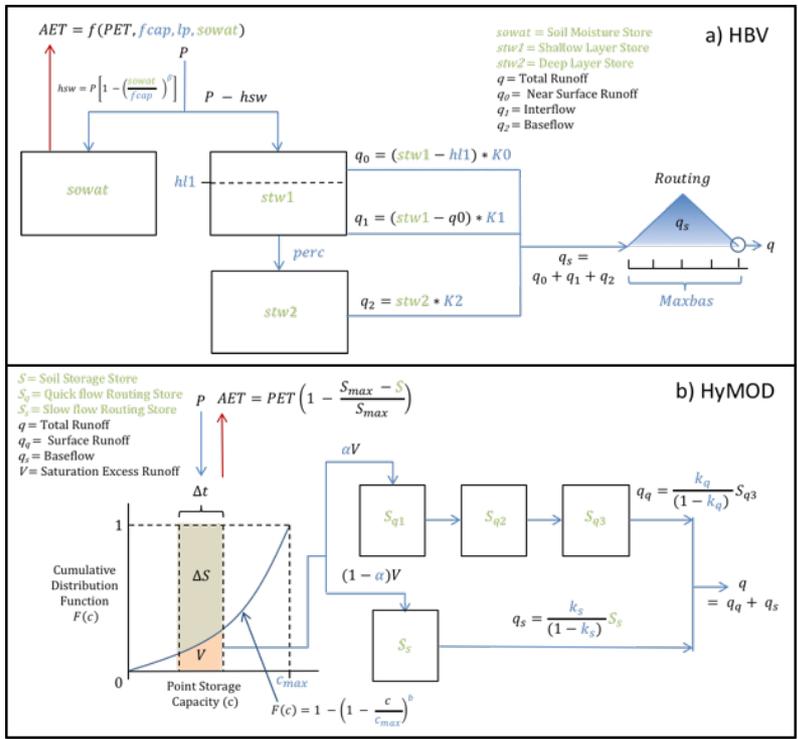
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834 **Figure 2 Impact of land use change on observed streamflow: a) Annual Runoff Coefficient, b)**
835 **Annual Baseflow Index (BFI), c) Moving Average Shifting Horizon (MASH) results for total observed**
836 **runoff, d) MASH for observed rainfall.**

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847 **Figure 3 Schematic of the models used in this study: a) HBV and b) HyMOD. Parameters are shown**
 848 **in blue and states are shown in green.**

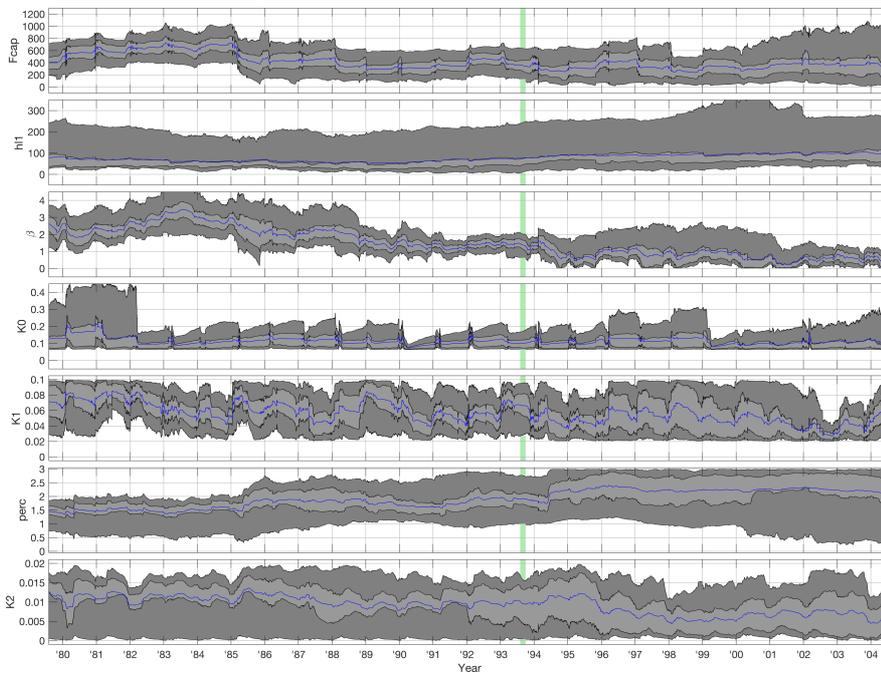
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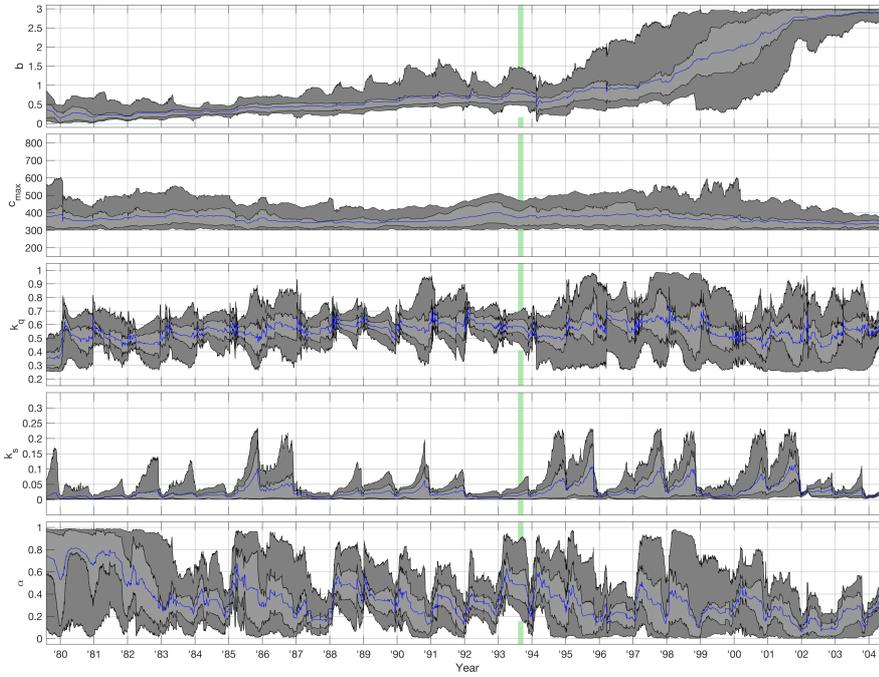
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Figure 4 Parameter Trajectories using the HBV model. The dark grey shaded areas indicate the middle 90% of the ensemble, bounded by the 5th and 95th percentiles. The light grey shaded areas indicate the middle 50% of the ensemble, bounded by the 25th and 75th percentiles. The ensemble mean is indicated by the blue line. The vertical green panel indicates the assumed time period of rapid deforestation.

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865 **Figure 5 Parameter Trajectories using the HyMOD model. The dark grey shaded areas indicate the**
866 **middle 90% of the ensemble, bounded by the 5th and 95th percentiles. The light grey shaded**
867 **areas indicate the middle 50% of the ensemble, bounded by the 25th and 75th percentiles. The**
868 **ensemble mean is indicated by the blue line. The vertical green panel indicates the assumed time**
869 **period of rapid deforestation.**

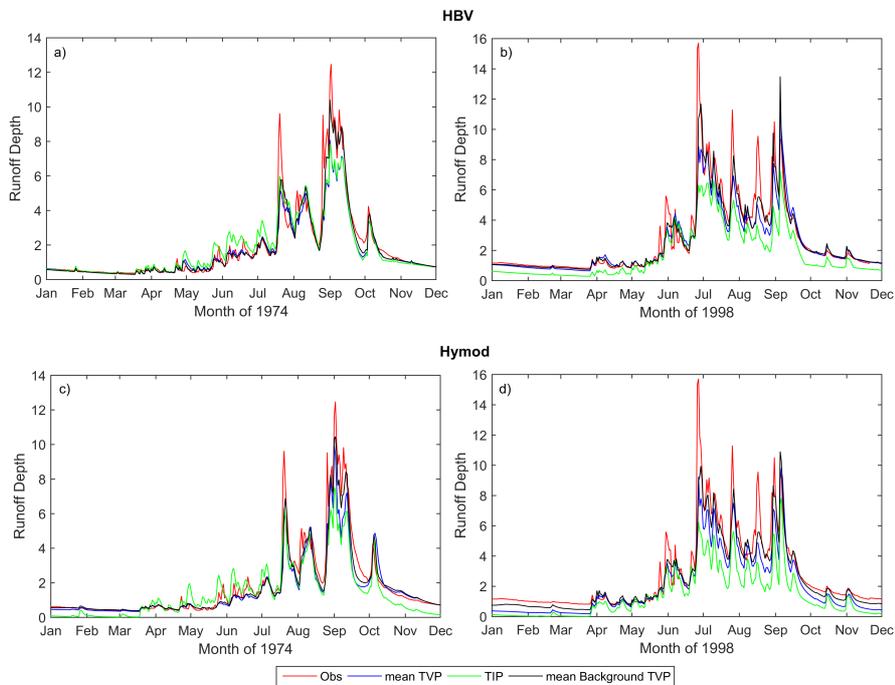
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876 **Figure 6 Representative Hydrographs of background streamflow from the LL Dual EnKF (black line),**
 877 **Time varying parameter model with no state updating (blue line), time invariant parameter model**
 878 **with no DA (green line) and observed streamflow (red line). Results for HBV are shown in the top**
 879 **row and HyMOD in the bottom row. A pre-change year (1974) is shown on the left and a post**
 880 **change year (1998) on the right.**

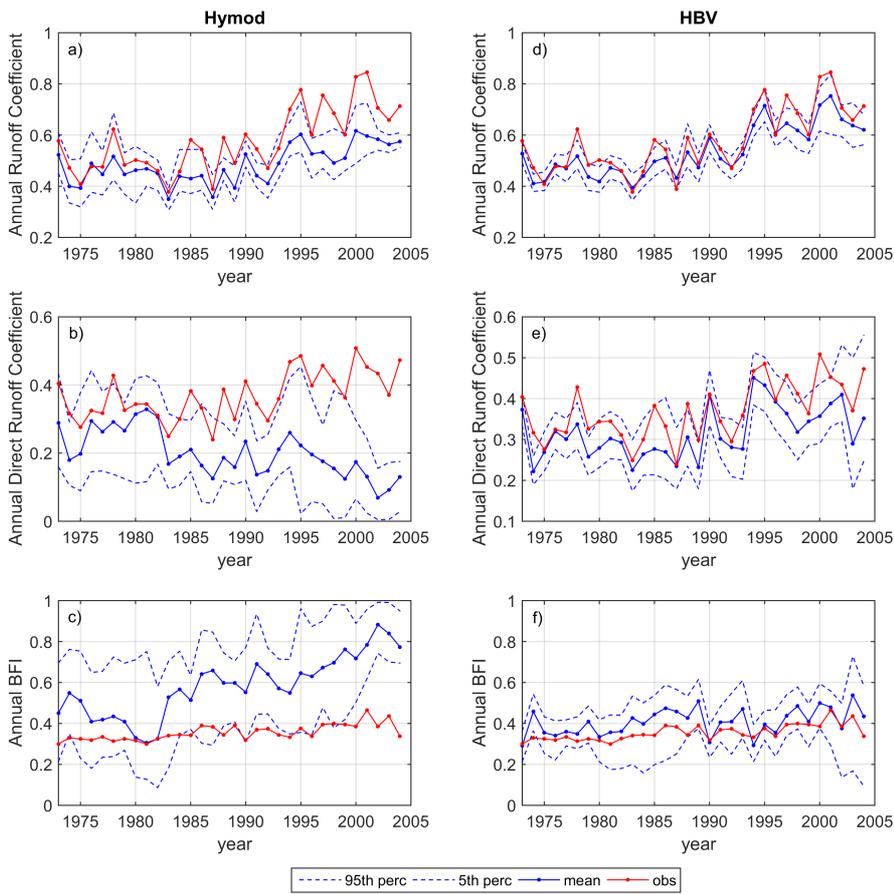
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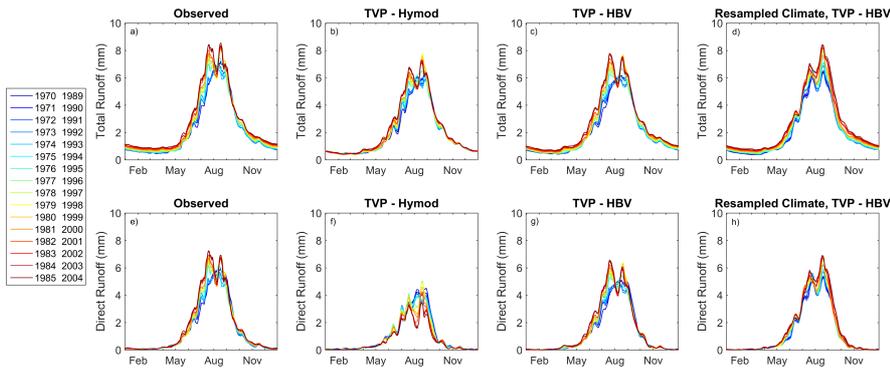
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Figure 7 Influence of time varying parameters on model output (i.e. without state updating) summarized in terms of the Annual Runoff Coefficient (top row), Annual Direct Runoff Coefficient (second row) and Annual Baseflow Index (BFI) (third row). Results for HyMOD are shown in the first column, HBV are shown in the second column.

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895 **Figure 8 Moving Average Shifting Horizon (MASH) results for observed streamflow (first column),**
896 **simulated streamflow from time varying parameter model (without state DA) for HYMOD (2nd**
897 **column), HBV (third column), resampled climate HBV (fourth column). These are split into total**
898 **runoff (first row) and direct runoff or surface runoff (2nd row).**

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