



Inference of analytical flow duration curves in Swiss alpine environments

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Abstract. This paper assesses the performance of an analytical modeling framework for streamflow probability distributions for summer streamflow of 26 Swiss catchments characterized by negligible anthropic influence. These catchments show a wide range of hydroclimatic regimes, including snow- and icemelt influenced streamflows. The model parameters are estimated from a gridded daily precipitation data set and observed daily discharge time series. The performance of the linear and nonlinear model version is assessed in terms of reproducing observed flow duration curves and their natural variability. The results show that the model performs well for summer discharges under all analyzed regimes and that there is a clear model performance increase with mean catchment elevation (i.e. with transition from rainfall-dominated to snow-influenced regimes). The nonlinear model version outperforms the linear model for all regimes but the performance difference decreases also with mean catchment elevation. Future work will focus on the extension of the modeling framework, addressing snowmelt and snowfall onset.

10 1 Introduction

Knowledge of the availability and variability of daily discharges in a given stream section proves useful for many engineering applications (e.g. the design of hydro-power plants or water supply systems), as well as for studies about water quality and allocation, or about stream ecology alterations and sediment transport (Vogel and Fennessey, 1995; Searcy, 1959; Ceola et al., 2010; Basso et al., 2015). For many such applications, knowledge of the probability distribution of daily discharges rather than of the serial structure of their occurrence is sufficient, i.e. daily discharges can be treated as a random variable.

The probability distribution of daily discharges is traditionally not represented as a probability density function (pdf) but in terms of flow duration curves (FDCs) that associate an exceedance probability to each discharge value (Vogel and Fennessey, 1994), which corresponds to the complement of the cumulative distribution function (cdf).

FDCs or other representations of the probabilistic distributions of daily discharges can be obtained in different manners, the most straightforward method being the assignment of empirical probabilities to observed ranked data (yielding empirical FDCs) (Vogel and Fennessey, 1994). Quite frequently, however, there are no discharge data available for the exact location of interest or, if there are, the length of the time series is insufficient, requiring other solutions for FDC estimation.



According to Castellarin et al. (2013), there exist several ways to estimate FDCs in the absence of sufficient streamflow data, including statistical and process-based methods. Statistical methods include regression methods that generate FDCs independently of the characteristics of the catchment and of climate (e.g. Franchini and Suppo (1996)) but generally use geological and topographic characteristics as predictor variables. Geostatistical methods are also relatively popular (Pugliese et al., 2014) to regionalize FDCs according to geographic proximity and topography.

Another group of statistical methods are so-called index flow methods that consist in some form of re-scaling of a reference FDC (Castellarin et al., 2004), which can be obtained by regionalizing the parameters of the reference curve to each location of interest (Ganora et al., 2009) or by using standard representations of FDCs for homogeneous regions and rescaling them to an index-flow (typically the mean annual runoff or the median daily runoff). Finally, there are also methods that propose to correct a relatively small series of data observations to generate a more reliable FDC using resampling experiments like the one suggested by Castellarin et al. (2004).

Process-based methods, instead, try to combine climate controls and catchment characteristics to estimate the shape of FDCs at ungauged locations. They consist of models that are approximations of the behavior of the given hydrological system, providing mathematical or simulation-based descriptions of FDCs based on observed data other than daily discharges. Simulation-based methods use long-term numerical simulations of the climatic and hydrological processes in a catchment to describe discharge and build FDCs. Being generally relatively complex, simulation-based methods can provide a detailed description of the hydrological system, but are demanding in terms of model development time and necessary data (Viviroli et al., 2009). Derived distribution models, in exchange, derive the FDCs from precipitation and catchment characteristics analytically. One of those models is the one proposed by Botter et al. (2007c) later extended in a variety of ways (Botter et al., 2008, 2009; Schaeffli et al., 2013; Müller et al., 2014), that will be explored in this paper.

The discharge in a river section depends on various factors, including climate, geomorphology and land use. Precipitated water can be released and stored in different ways, but the main climate control for discharge production is the precipitation event itself (Wagener et al., 2007), which, in Alpine regions, mostly occurs in form of rain or snow. Botter et al. (2007c) assumed rainfall as the trigger for discharge production and proposed an analytical model to obtain probabilistic distributions of discharge by considering daily discharge as the result of "the superposition of a sequence of subsurface water flow pulses, triggered by a stochastic precipitation and censored by the soil moisture dynamics" (Botter et al., 2013).

Describing rainfall as a stochastic process (a marked Poisson process with exponentially distributed rainfall depths), Botter et al. (2007c) showed that the FDC of rainfall-dominated catchments that present a linear decay of discharge due to the release of water from the subsoil can be described by a gamma distribution characterized by the mean depth of precipitation, the frequency of precipitation events that produce discharge, the area of a catchment and the mean residence time of the catchment. This model framework has been applied successfully in Europe, in Italy (Botter et al., 2007c, 2009; Ceola et al., 2010; Schaeffli et al., 2013) and Switzerland (Schaeffli et al., 2013; Basso et al., 2015), and in the US (Botter et al., 2007a; Ceola et al., 2010; Botter et al., 2013).

Based on the same theoretical framework, some extensions of the model have already been proposed to make it more suitable for different hydrological conditions, in particular for situations where the decay of discharge due to the release of water from



the soil is considered to be nonlinear (Botter et al., 2009), for winter flow in snow-dominated catchments (Schaeffli et al., 2013) and for seasonally dry climates (Müller et al., 2014):

In the previous applications of the model, the focus was generally on the study of signatures of discharge regimes under different climates and landscape conditions (Botter et al., 2007a, 2013), where the shape of the pdf is more important than the accuracy of the obtained discharge probabilities. It is important to emphasize that except for the work of Schaeffli et al. (2013) that adapts the model to conditions of snow accumulation, previous applications deliberately exclude catchments and/or seasons where snow accumulation and melt affect the discharges (Botter et al., 2007a; Ceola et al., 2010; Botter et al., 2013; Doulatyari et al., 2015). A detailed analysis of how well the modeling framework can reproduce observed FDCs is presented in the work of Botter et al. (2008) and in particular in the work of Ceola et al. (2010), who presents a detailed analysis of different parameter estimation methods and of model performance assessment for the linear and the non-linear model version.

The objective of this research is to assess the model performance (linear and non-linear form) for a set of 26 Swiss catchments for summer flows, including rainfall-dominated catchments with typical summer low flows and catchments with snowmelt-driven summer high flows. Particular attention is paid hereby to a detailed analysis of the model parameters and their seasonality.

Switzerland is a mountainous, relatively humid country, with precipitation approximately evenly distributed during the seasons, but varying according to the region (Schwarb et al., 2001), which results in a relatively high diversity of hydrologic regimes within this small country (41.285 km²) (Weingartner and Aschwanden, 1992). Very intense precipitation events are not common, especially not in higher areas, with the exception of the south of Alps region (Spreafico and Weingartner, 2005). These conditions are ideal for the application of the analytical streamflow distribution model of Botter et al. (2007c) because most of the discharge can be assumed to result from subsurface flow, one of the necessary assumptions underlying this model. This assumption in particular also holds in the presence of snowmelt, which plays a major role in several of the studied catchments even in summer (see Section 3), most of the discharge can be assumed to result from subsurface flow, one of the necessary assumptions underlying this model. It is noteworthy, however, that the travel time distributions underlying the hydrologic response at a chosen control section (stream flow gauge) cannot be considered to be stationary, an issue which is of major concern when transport processes are investigated (Rinaldo et al., 2011, 2015)

The paper is organized as follows: Section 2 provides a description of the analytical model, together with the methods adopted in this paper to estimate the model parameters and to assess the model performance, followed by a presentation of the Swiss case studies (Section 3). The obtained results for the linear and the nonlinear model version (Section 4) are discussed in Section 5 with a particular focus on the model performance under different hydrological regimes. The conclusions are summarized in Section 6.

2 Methods

Hereafter, we first give a short overview over the used analytic model framework, followed by the two different methods used for parameter estimation and for model performance assessment. All model methods are applied only to the summer season



(June 1st to August 31st, see also Section 3). The sequence of calculations required to estimate all model parameters in this work is synthesized in Figure 1.

2.1 Model framework

The analytical model framework for probabilistic characterization of rainfall-drive daily discharges developed by Botter et al. (2007c) is based on a previous model proposed by Rodriguez-Iturbe et al. (1999), which model represents the dynamics of soil moisture at a point as a result of a deterministic state-dependent loss function, combined with stochastic increments triggered by rainfall events. Following Botter et al. (2007c), the spatially averaged soil moisture $s(t)$ can be obtained based on the water balance equation:

$$\frac{ds(t)}{dt} = -\rho[s(t)] + \xi_t, \quad (1)$$

where $-\rho[s(t)]$ is the loss function, due to evapotranspiration, surface runoff and deep percolation, and where ξ_t represents the stochastic instantaneous inputs due to rainfall infiltration from rainfall.

Botter et al. (2007c) proposed to describe the dynamics of daily streamflow with a similar stochastic differential equation, supposing that some precipitation events can act as a stochastic forcing for discharge production and that water will be released from the soil producing discharge according to a deterministic decay :

$$\frac{dQ(t)}{dt} = -kQ(t) + \xi_t'', \quad (2)$$

where (Q) is the daily streamflow, k is the inverse of the time constant associated with the loss function and ξ_t'' is the stochastic rate due to discharge producing precipitation events.

It is assumed hereby that discharge (Q) is the result of a sequence of subsurface inputs triggered by events of precipitation that deliver enough water to fill the water deficit in the soil and to raise its level of moisture above its retention capacity. The excess of water becomes discharge and is removed from the soil as subsurface run-off. As it can be seen in Equation 2, the subsurface storage is assumed to behave like a linear reservoir with a constant k . This description comprises only the dynamics of the sub-surface runoff, neglecting any surface runoff.

The overall rainfall forcing can be modeled as a marked Poisson process with frequency λ_P and exponentially distributed rainfall depths with average α . But not all the rainfall events are able to force discharge production. Accordingly, the frequency is reduced to λ , the frequency of discharge-producing events, i.e. of events that raise the soil moisture above its retention capacity. In rainfall-driven environments, this reduced frequency λ can be understood as the frequency of rainfall events that are unusable by plants; λ is influenced by the soil storage capacity and soil drying time (Botter et al., 2007b). The corrected frequency λ can be written as (Botter et al., 2007a).

$$\lambda = \eta \frac{\exp(-\gamma) \gamma^{\frac{\lambda_P}{\eta}}}{\Gamma(\lambda_P/\eta, \gamma)}, \quad (3)$$



where $\Gamma(a, b)$ is the lower incomplete Gamma function with parameters a and b , $\eta = E/(nZ_r(s_1 - s_w))$, $\gamma = \gamma_P n Z_r (s_1 - s_w)$ and $\gamma_P = 1/\alpha$. E is the maximum evapotranspiration rate and $nZ_r(s_1 - s_w)$ synthesizes the volume in the soil that can be filled by water, where n is the porosity of the soil and Z_r is the effective depth of the soil. The multiplication of these two variables represents a normalizing factor. Accordingly, s_1 is the soil moisture threshold above which water starts to move in the soil and s_w is the wilting point. The difference represents the volume in the soil that can be filled before drainage starts.

As discussed in detail by Botter et al. (2007c), this framework results in the following probability distribution of daily discharges at the catchment outlet:

$$p(Q, t \rightarrow \infty) = \frac{1}{\Gamma(\frac{\lambda}{k})} \frac{1}{Q} \left(\frac{Q}{\alpha k A} \right)^{\frac{\lambda}{k}} \exp\left(-\frac{Q}{\alpha k A}\right), \quad (4)$$

where Q is the daily discharge, k is the inverse of the mean residence time in the subsurface ($\tau = k^{-1}$), α is the average of precipitation depths and A is the area of the catchment. This corresponds to a Gamma distribution with shape parameter λ/k and a scale parameter $\alpha k A$.

The model is suitable for steady state conditions, at the annual or seasonal scale, depending on the temporal variability of the model parameters (Botter et al., 2007a).

Nonlinear storage-discharge relations in subsurface are common due to changes in the hydraulic properties of the soil under different soil moisture levels (Botter et al., 2009; Brutsaert and Nieber, 1977; Mutzner et al., 2013). Accordingly, Botter et al. (2009) proposed an extension of the above modeling framework assuming that:

$$\frac{dQ(t)}{dt} = -k_n Q(t)^a + \xi_t, \quad (5)$$

where k_n and a are the constants of the nonlinear recession.

As previously, with this new storage discharge relation, it is possible to obtain an equation for the pdf of the daily discharges:

$$p(Q, t \rightarrow \infty) = C \left\{ \frac{1}{Q^a} \exp\left[-\frac{Q^{2-a}}{\alpha k_n (2-a)} + \frac{Q^{1-a} \lambda}{k_n (1-a)}\right] \right\}, \quad (6)$$

where C is a normalizing constant (Botter et al., 2009).

According to Castellarin et al. (2013), the proposed method can be classified as a process-based derived distribution method, because it derives a distribution for daily discharges analytically based on underlying catchment properties and some key precipitation characteristics.

2.2 Parameter estimation 1: forward estimation

In this work, we use the term "forward parameter" estimation to emphasize that the parameters are estimated directly from observed data before any model is actually applied. Such method is generally used in the context of this model framework for the estimation of the precipitation parameters λ_P and α . In the present work, the mentioned parameters were always estimated



in a forward mode; however, between the soil-dependent parameters (λ , k , k_n and a) the recession parameters (k , k_n and a) are either estimated in a forward mode (Botter et al., 2007c, 2009; Ceola et al., 2010; Schaeffli et al., 2013) or in an inverse mode (Ceola et al., 2010) (see Section 2.3).

Prior to the calculation of the precipitation parameters λ_P and α , it is necessary to subtract interception losses (I) from the observed daily precipitation depths. These losses are in fact evaporated (or sublimated in case of snow) before participating to soil moisture dynamics. Following Rodriguez-Iturbe et al. (1999), previous model applications generally assumed that these losses are accounted for when the frequency of precipitation events is corrected to the frequency of discharge producing events. In view of understanding how the model parameters vary in space, in this work it was decided to treat this interception losses explicitly with minimal assumptions about this process: different maximum interception depths are attributed to four different land covers (4 mm for forests, 2 mm, for low vegetation, 1 mm for impervious areas, 0 mm for water bodies (Gerrits, 2010)). The catchment-scale maximum interception depth is obtained as the area-average of these values but a minimum interception depth of 1 mm is imposed. This catchment-scale interception depth is subtracted from daily precipitation observations, assuming that at a daily time step, all intercepted water evaporates.

The recession parameter for the linear model is calculated directly from observed daily discharge based on a classical Brutsaert-Nieber recession analysis (Brutsaert and Nieber, 1977; Biswal and Marani, 2010, 2014; Mutzner et al., 2013), considering, however, only discharges below a certain threshold, fixed to 95%. (see the work of Doulatyari et al. (2015) for a method to estimate this parameter from a geomorphic recession model). The nonlinear recession parameters, k_n and a are also obtained based from a recession analysis, using the same discharge threshold via linear regression of the logarithm of $(-dQ/dt)$ versus the logarithm of Q , where a is the slope and k_n the intercept. In forward estimation, the frequency of precipitation events, λ_P is corrected to the discharge-producing frequency λ using the following relationship:

$$\bar{Q} = \lambda \alpha, \quad (7)$$

where \bar{Q} is the average of the observed daily discharges \tilde{Q} . Estimating λ from the above equation rather than directly from the soil properties as in Equation 7, has been shown by Ceola et al. (2010) to provide much better results, and this method is used by the majority of studies since then (e.g. Ceola et al., 2010; Botter et al., 2013; Basso et al., 2015).

2.3 Parameter estimation 2: inverse estimation

To objectively compare the potential of different model formulations to capture observed flow-duration curves, the recession parameters for the linear and the nonlinear model are also estimated in a classical inverse estimation mode where the model parameters are obtained by maximizing the likelihood function formulated for the model. For the linear model, the likelihood function is obtained from the model as follows:

$$\mathcal{L}(k|\tilde{\mathbf{Q}}, \alpha, \lambda) = \prod_{j=1}^N p(\tilde{Q}_j), \quad (8)$$



where $\tilde{Q}_j, j = 1, \dots, N$ are the observed daily discharges at all time steps j , $p(\tilde{Q}_j)$ is the probability of these observed discharges obtained from the model (Equation 4) and $\mathcal{L}(k|\tilde{Q}, \alpha, \lambda)$ is the likelihood function given observed data and the previously estimated model parameters α, λ . For the nonlinear model, the likelihood $\mathcal{L}(k_n, a|\tilde{Q}, \alpha, \lambda)$ is obtained analogously.

2.4 Model evaluation criteria

5 To objectively compare different models, we propose to use here the Kolmogorov-Smirnov distance between the cdfs corresponding to different models (Ceola et al., 2010; Schaeffli et al., 2013), i.e. the maximum difference between the values of the empirical and the modeled cumulative distributions. This comparison of the cdfs overcomes an important limitation inherent in the comparison of analytic pdfs and empirical pdfs: namely the question of the choice of the number of classes for the calculation of the empirical pdf from observed data (i.e. via a so-called frequency polygone Naghettini, 2016). The problem
 10 does not arise for cdfs given their cumulative nature.

Given that the nonlinear model formulation has an additional parameter, the linear and the nonlinear models are also compared based on the Akaike information criterion (Burnham and Anderson, 2004):

$$c^{\text{AIC}} = 2n - \ln(\hat{\mathcal{L}}), \quad (9)$$

where n is the number of parameters of the model and $\ln(\hat{\mathcal{L}})$ is the logarithm of the maximum likelihood function obtained by
 15 maximizing Equation 8.

Based on the above criterion, we measure the relative performance increase from the linear to the nonlinear model as follows:

$$r^{\text{AIC}} = \frac{c_n^{\text{AIC}} - c_l^{\text{AIC}}}{c_l^{\text{AIC}}}, \quad (10)$$

where c_n^{AIC} is the Akaike criterion for the nonlinear model and c_l^{AIC} for the linear model.

In addition to assessing the performance difference between different models, we propose here to compare the obtained
 20 models to the natural variability of discharge cdfs obtained from observed data. Therefore, an empirical long term cdf is constructed, obtained by ranking the observed data in ascending order and dividing the rank numbers by the total sample size. Furthermore, to assess the natural yearly variability, individual cdfs are constructed for each summer season of each civil year (Vogel and Fennessey, 1994). From these curves, cdf envelopes are obtained based on the maximum and minimum values of discharge for each probability class. A reliable model should yield a cdf contained in these curves and be as close as possible
 25 to the long term cdf.

3 Case studies

In Switzerland, an important part of precipitation occurs in form of snow that might either build a seasonal snow cover (accumulation and melt within a single year) or, at elevations roughly beyond 3000m a.m.s.l., accumulate interannually in the



form of glaciers. They represent an important storage that influences the hydrological cycle. In the higher parts of Switzerland, discharges are thus strongly influenced by snow and ice accumulation and melt processes. In addition, this relatively small country (41.285 km²), represents a high variety of hydro-climatic conditions (Weingartner and Aschwanden, 1992; Gonseth et al., 2001).

5 Accordingly, Switzerland presents three main types of hydrological regimes, namely: pluvial, snow-dominated and glacier (Weingartner and Aschwanden, 1992). The hydrological regime is called pluvial if discharge is driven mostly by rainfall events. Snow-influenced regimes can be found in catchments that show a significant seasonal snow cover, i.e. in catchments with mean elevation above roughly 900m a.m.s.l. In these catchments, solid precipitation accumulates during most of the cold season (winter) and is released in spring when temperature raises above 0°C and snow melts. Depending on the extent and depth
10 of the snow cover, this snowmelt release can last throughout spring until early summer. For catchments where the cycles of accumulation and melting happen during a single year, the hydrological regime is called snow-dominated. For catchments that have a significant amount of glacier cover, snow is accumulated during the entire year and ice melt sustains high streamflows during the entire summer; resulting in glacier regimes.

The strong seasonality in the Swiss hydrological regimes is illustrated in Figure 2 which shows the joint behavior of discharge
15 and air temperature during an average year for typical cases of the three main types of regimes (Goldach (GOL), Dischmabach (DIS), Rhône à Gletsch (RHG)); air temperature is shown here as a proxy for snow and evapotranspiration processes. The rainfall-driven Goldach river shows the typical summer low flow resulting from evapotranspiration; the Dischmabach shows a snow regime with high summer flows and the Rhône river a glacier regime, for which summer high flow peaks in the same month as air temperature.

20 Furthermore, for hydrological purposes, Switzerland is typically divided in three main biogeographical regions: "Plateau and Jura", "Alps" and "South of Alps" (see Figure 3). Jura designates the mountain region in the north of the country, not extending beyond 1679 a.m.s.l. in Switzerland. (i.e. low in comparison to the Alps) and where the predominant hydrological regime is pluvial, locally with important karst effects. It is included here in a single region together with the low lying Plateau area (roughly 400 - 1400m a.m.s.l.). The Alps region includes the highest Swiss summit [i.e. the Dufourspitze, at 4634m
25 a.m.s.l.] and the source areas of some major European rivers (Rhône, Rhine, Po, Danube) (Huss, 2011). Most snow-dominated catchments are located here. The "South of Alps" is also a mountainous region, but it has a warmer climate and presents higher precipitation.

For the present analysis, all catchments with unperturbed discharges (i.e. minimal anthropogenic influence) that are gauged by the Swiss Federal Office for the Environment (FOEN) (FOEN, 2017) are selected, resulting in 26 study catchments in all
30 three regions (see Figure 3 and Table 1 for their main characteristics). The corresponding regime classification is given by Weingartner and Aschwanden (1992). 23 of the chosen catchments are considered "hydrological study areas" and have an associated dataset with some key characteristics, such as their land use (Aschwanden, 1996). The provided land use data was used to calculate interception. For the other catchments (i.e. the Areuse, Rhône-Gletsch and Venoge), land use was obtained from spatial data (FOS, 2015). The proportions of land use for each catchment can be found in the supplementary information.



This set of catchments includes fourteen catchments in the Plateau and Jura region, seven in the Alps and five in the South of Alps. The areas of the catchments vary from 1.05km² to 377km² and their mean elevations from 383m to 1860m a.m.s.l.

Besides observed daily discharge, the model requires basin-scale daily precipitation as input.

Most of the previous applications of the models used precipitation from one or several meteorological stations as input
5 (Botter et al., 2007c, a, 2013; Ceola et al., 2010; Basso et al., 2015; Schaeffli et al., 2013). Here it was decided to make use of the relatively new spatial precipitation data set of MeteoSwiss with a resolution of 2,2km and an effective resolution between 15km and 20km and extending back to 1961 (MeteoSwiss, 2014a) which can be assumed to give relatively good estimates of area-averaged precipitation (Paschalis et al., 2014; Addor and Fischer, 2015), even in mountainous areas where there are only few meteorological stations.

10 In addition, we also used the corresponding spatial temperature data set (MeteoSwiss, 2014b) to support the analysis of parameter seasonality.

4 Results

4.1 Discharge regimes and parameter seasonality

A key aspect of the different Swiss discharge regimes is their strong seasonality, resulting from evapotranspiration and the
15 accumulation and melt of snow and ice. To gain further insights in the hydrological behavior of the different regimes, Figure 4 shows the within-year variability of the model parameters obtained by estimating the parameters in forward mode for moving and overlapping 90-day windows (to estimate the parameters for a given time window, the data points corresponding to this window in all civil years are pooled together). The precipitation parameters α and λ_P overall do not show strong seasonal patterns, except for a few catchments such as the Goldach river (Figure 4a). For snow and glacier regimes, the frequency of
20 discharge-producing events, λ , increases strongly at the beginning of spring (Figure 4b and c), which indicates the release of water from snow- or ice-melt.

The inverse of the recession coefficient k shows a strong coherent annual cycle for all catchments, independent of the underlying discharge regime (Figure 5). This seasonal pattern with consistently low τ values during summer for all catchments clearly justifies the choice of a common summer season (June, July, August) for all regimes. The annual cycle (the difference
25 between high and low τ values) is stronger for snow or glacier regime catchments, which reflects the fact that in these regimes, parts of the catchment are effectively dormant during the winter (Schaeffli et al., 2013).

4.2 Linear model

All estimated parameters for both forward and inverse estimations are summarized in Table 2. It can be noted that for 11 catchments (i.e. Rein da Sumvitg, Dischmabach, Alpbach, Grosstalbach, Rhône à Gletsch, Massa, Verzasca, Riale di Calneggia,
30 Krumbach, Poschiavino and Ova da Cluozza), λ is bigger than λ_P , contradicting the original description of the model that states that the discharge producing frequency is smaller than the precipitation frequency. This happens only in the catchments



with presence of snow processes, where snow- or glacier melt increases discharge production during the warmer seasons of the year (i.e. summer and spring), surpassing the losses by evapotranspiration that would cause a decreasing of λ as described by Botter et al. (2007b). Those results are further discussed in Section 5.

The cdfs obtained from these parameters are presented for three cases endowed with different hydrological regimes (see Figure 6). For the catchment with rainfall-driven discharges (GOL) it can be seen that for the forward estimation, probabilities of occurrence of low flows are largely overestimated (Figure 6a), a typical indication that the recession parameter is underestimated. The model values even exceed the envelopes that represent the natural variability of the discharges. Interestingly, in the presence of snow, the linear model tends to underestimate low flows, with satisfactory results for some cases, such as the Dischmabach. When the relative glacier cover increases, the quality of results start to decrease again as a result of the underestimation of low flows and overestimation of higher flows. This pattern is typical for overestimated recession parameters. It is interesting to notice that the values of the performance indicator (the Kolmogorov-Smirnov distance) are similar for the Goldach (GOL, pluvial regime) and the Rhone river (RHG, glacier regime), around 0.19, despite the difference in the nature of the inaccuracy.

The results are not satisfactory for the forward estimation method, not even for the catchments that are pluvial during all year. This originally motivated a deeper study of the recession parameter and its calculation using an inverse method (i.e. via parameter fitting with MLE). Results for the inverse estimation of parameters are also presented in the form of Kolmogorov-Smirnov distances in Table 2.

The inverse estimation of the model parameters improves the results significantly, but they are still not satisfying, the performance indicator has high values and the curves are visually not accurate specially for pluvial regimes. This suggest that the model with a linear discharge decay is overall not suitable for the studied catchments.

4.3 Nonlinear models

The nonlinear model formulation leads overall to a significant model performance increase, as can be verified comparing the indicators of performance c^{KS} and c^{AIC} presented for the linear and nonlinear models in Table 2 and also visually in Figure 7. The improvement is more noticeable for the catchments with low mean elevation and consequently rainfall-driven-regimes, as shown in Figure 8 and by comparing Figures 9a and 9b. Such behavior confirms that the recession observed in these catchments decays is in general better described by a nonlinear model. For some catchments (i.e. Murg-Wängi, Gürbe, Sense, Ilfis, and Grosstalbach), the forward estimation method gives very good results with KS distances below 0.1. In general, for the catchments where the discrepancies between modeled and observed cdfs are due to an underestimation of τ , the improvement of the results is very noticeable. For catchments where the recession time scale is overestimated with the linear model, the nonlinear model estimated in forward model leads to a performance decrease. The results obtained from inverse parameter estimation are very good for all catchments, validating the suitability of the nonlinear model for Swiss river regimes. Again, the nature of the discrepancies between modeled and observed cdf is different for the pluvial catchments than for the catchments where there is snow and glacier cover.



4.4 Linear versus nonlinear model performance

As can be seen from the summary of results in Table 2, the nonlinear model outperforms the linear model for all catchments, both in terms of the KS performance and in terms of the Akaike criterion. Comparing the KS indicators to the mean catchment elevation, it can be seen that the performance increases with elevation for the linear model (Figure 9a) and decreases with elevation for the nonlinear model (Figure 9b). Elevation differences are more pronounced if the parameters are obtained by forward estimation than by inverse estimation. A plot of the relative performance increase r_{AIC} of the nonlinear model with respect to the linear model against mean catchment elevation (see Figure 8) shows that the nonlinear model performs significantly better for low-elevation catchments and that the difference decreases for high-elevation catchments.

5 Discussion

Our results for the 26 Swiss catchments show that the analytic flow distribution model presents very good performances for summer even in areas with snow- and glacier melt-driven summer high flows. Since the model parameters are obtained directly from observed data for each region and for each period, a traditional model validation procedure would not be suitable in this situation. The good performances in many different catchments with different regimes can, however, be considered as a validation of the model for Switzerland. The presence of ice melt in some catchments can be clearly seen comparing the precipitation frequency λ_p to the discharge-producing frequency λ : in fact, for some catchments, this frequency increases instead of decreasing, as it would be expected for rainfall driven regimes outlined in the original description of the model (Botter et al., 2007c). The increase of λ can be understood physically as the effect of an extra source of water contributing to the discharge production, in this case, snow- or glacier-melt that happens when temperature raises during warm seasons.

The augmentation of λ with respect to λ_p increases for catchments where ice melt has more influence on the discharges reaching values above 1 day^{-1} for the few strongly glaciated catchments (Table 2).

In general, considering the forward estimation of parameters, the results for the linear model are better for the catchments with summer high flows, while the results of the nonlinear model are better for catchments with rainfall-driven regimes. The departure of the model from the observed cdfs for catchments with or without a significant snow cover have different origins. For the summer high flows, the model in general underestimates the discharge variability, probably due to an overestimation of the recession parameter. For the lower catchments, the model in exchange overestimates the variability, resulting in cdfs that exceed the envelopes, probably due to an underestimation of the recession parameter. When the nonlinear model is applied, the recession becomes stronger, improving the results for the pluvial catchments but worsening them for the catchments with summer high flows. This worsening, however, only holds if the model parameters are estimated in forward mode.

A detailed comparison between the performance of the linear and the nonlinear models considering the optimized parameters obtained from the inverse approach shows that the results for nonlinear model are always better than for the linear model. This underlines that the nonlinear recession suits better the hydrological conditions of all study catchments and pinpoints the need to improve the method to estimate the recession parameters.



Very interesting additional insights can be obtained from the highlighted model performance increase with mean catchment elevation (Figures 9 and 8). This can in fact be explained by the evolution of the regimes with mean catchment elevation, from rainfall-dominated (pluvial) regimes with summer low flow to snowfall-dominated (nival) regimes with summer high flow. This result suggests, in fact, that mean catchment elevation is a very good proxy for this regime shift despite the fact that many other catchment characteristics vary strongly across the set of studied catchments (area, hypsometric curve, land use etc.). Given the strong link between mean catchment elevation and mean catchment air temperature, this opens very interesting perspectives for parameter regionalization.

In this context, it should be kept in mind that for the present study, λ is estimated directly from the relation between discharge and precipitation (see section 2.2). The question of how to estimate this parameter directly from catchment characteristics based on long term snow cover statistics and data on glacier cover remains to be answered in future work.

6 Conclusions

The application of an analytic model framework to 26 Swiss catchments showed that this framework can describe summer discharge distributions across a wide range of discharge regimes, including rainfall-driven regimes with summer flows, but also regimes with snow- and glacier melt-driven summer high flows. The detailed comparison between the performance of the linear and nonlinear model formulation shows that the description of summer low flows is strongly improved using a nonlinear storage-discharge relationship, whereas the discharge distribution of high summer flows can be well described with a linear relationship. In general, the linear model performance increases for increasing total summer flows or, equivalently, for catchments with higher mean elevation. Future work will focus on regionalizing the model parameters and on extending the model framework to all four seasons for snow-influenced catchments.

Competing interests. The authors declare that they have no conflict of interest.

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References

- Addor, N. and Fischer, E. M.: The influence of natural variability and interpolation errors on bias characterization in RCM simulations, *Journal of Geophysical Research: Atmospheres*, 120, 2015.
- Aschwanden, A.: Caractéristiques physiographiques des bassins de recherches hydrologiques en Suisse, 1996.
- 5 Basso, S., Schirmer, M., and Botter, G.: On the emergence of heavy-tailed streamflow distributions, *Advances in Water Resources*, 82, 98–105, doi:10.1016/j.advwatres.2015.04.013, 2015.
- Biswal, B. and Marani, M.: Geomorphological origin of recession curves, *Geophysical Research Letters*, 37, n/a–n/a, doi:10.1029/2010gl045415, 2010.
- Biswal, B. and Marani, M.: 'Universal' recession curves and their geomorphological interpretation, *Advances in Water Resources*, 65, 34–42, doi:10.1016/j.advwatres.2014.01.004, 2014.
- 10 Botter, G., Peratoner, F., Porporato, A., Rodriguez-Iturbe, I., and Rinaldo, A.: Signatures of large-scale soil moisture dynamics on streamflow statistics across U.S. climate regimes, *Water Resources Research*, 43, doi:10.1029/2007wr006162, 2007a.
- Botter, G., Porporato, A., Daly, E., Rodriguez-Iturbe, I., and Rinaldo, A.: Probabilistic characterization of base flows in river basins: Roles of soil, vegetation, and geomorphology, *Water Resources Research*, 43, doi:10.1029/2006wr005397, 2007b.
- 15 Botter, G., Porporato, A., Rodriguez-Iturbe, I., and Rinaldo, A.: Basin-scale soil moisture dynamics and the probabilistic characterization of carrier hydrologic flows: Slow, leaching-prone components of the hydrologic response, *Water Resources Research*, 43, n/a–n/a, doi:10.1029/2006WR005043, w02417, 2007c.
- Botter, G., Zanardo, S., Porporato, A., Rodriguez-Iturbe, I., and Rinaldo, A.: Ecohydrological model of flow duration curves and annual minima, *Water Resources Research*, 44, doi:10.1029/2008wr006814, 2008.
- 20 Botter, G., Porporato, A., Rodriguez-Iturbe, I., and Rinaldo, A.: Nonlinear storage-discharge relations and catchment streamflow regimes, *Water Resources Research*, 45, doi:10.1029/2008wr007658, 2009.
- Botter, G., Basso, S., Rodriguez-Iturbe, I., and Rinaldo, A.: Resilience of river flow regimes, *Proceedings of the National Academy of Sciences*, 110, 12925–12930, doi:10.1073/pnas.1311920110, 2013.
- Brutsaert, W. and Nieber, J. L.: Regionalized drought flow hydrographs from a mature glaciated plateau, *Water Resources Research*, 13, 637–643, doi:10.1029/wr013i003p00637, 1977.
- 25 Burnham, K. P. and Anderson, D. R., eds.: *Model Selection and Multimodel Inference*, Springer New York, doi:10.1007/b97636, 2004.
- Castellarin, A., Galeati, G., Brandimarte, L., Montanari, A., and Brath, A.: Regional flow-duration curves: reliability for ungauged basins, *Advances in Water Resources*, 27, 953–965, doi:10.1016/j.advwatres.2004.08.005, 2004.
- Castellarin, A., Botter, G., Hughes, D. A., Liu, S., Ouarda, T. B. M. J., Parajka, J., Post, D. A., Sivapalan, M., Spence, C., Viglione, A., et al.: Prediction of flow duration curves in ungauged basins, *Runoff prediction in ungauged basins: Synthesis across processes, places and scales*, pp. 135–162, 2013.
- 30 Ceola, S., Botter, G., Bertuzzo, E., Porporato, A., Rodriguez-Iturbe, I., and Rinaldo, A.: Comparative study of ecohydrological streamflow probability distributions, *Water Resources Research*, 46, doi:10.1029/2010wr009102, 2010.
- Doulatyari, B., Betterle, A., Basso, S., Biswal, B., Schirmer, M., and Botter, G.: Predicting streamflow distributions and flow duration curves from landscape and climate, *Advances in Water Resources*, 83, 285–298, doi:10.1016/j.advwatres.2015.06.013, 2015.
- FOEN: Hydrological data and forecasts, <https://www.hydrodaten.admin.ch/en/stations-and-data.html>, 2017.
- FOS: Statistique de la superficie du sol selon nomenclature 2004, *Utilisation du sol (Land Use)*, 2015.



- Franchini, M. and Suppo, M.: Regional analysis of flow duration curves for a limestone region, *Water Resources Management*, 10, 199–218, doi:10.1007/bf00424203, 1996.
- Ganora, D., Claps, P., Laio, F., and Viglione, A.: An approach to estimate nonparametric flow duration curves in ungauged basins, *Water Resources Research*, 45, doi:10.1029/2008wr007472, 2009.
- 5 Gerrits, A. M. J.: *The role of interception in the hydrological cycle*, TU Delft, Delft University of Technology, 2010.
- Gonseth, Y., Wohlgemuth, T., Sansonnens, B., and Buttler, A.: Les régions biogéographiques de la Suisse—explications et division standard, *Cahier de l’environnement*, 137, 1–48, 2001.
- Huss, M.: Present and future contribution of glacier storage change to runoff from macroscale drainage basins in Europe, *Water Resources Research*, 47, doi:10.1029/2010wr010299, 2011.
- 10 MeteoSwiss: Daily Precipitation (final analysis): RhiresD, 2014a.
- MeteoSwiss: Daily Temperature (final analysis): TabsD, 2014b.
- Müller, M. F., Dralle, D. N., and Thompson, S. E.: Analytical model for flow duration curves in seasonally dry climates, *Water Resources Research*, 50, 5510–5531, doi:10.1002/2014wr015301, 2014.
- Mutzner, R., Bertuzzo, E., Tarolli, P., Weijs, S. V., Nicotina, L., Ceola, S., Tomasic, N., Rodriguez-Iturbe, I., Parlange, M. B., and Rinaldo,
- 15 A.: Geomorphic signatures on Brutsaert base flow recession analysis, *Water Resources Research*, 49, 5462–5472, doi:10.1002/wrcr.20417, 2013.
- Naghetini, M.: Preliminary Analysis of Hydrologic Data, in: *Fundamentals of Statistical Hydrology*, pp. 21–56, Springer International Publishing, doi:10.1007/978-3-319-43561-9_2, 2016.
- Paschalis, A., Fatichi, S., Molnar, P., Rimkus, S., and Burlando, P.: On the effects of small scale space–time variability of rainfall on basin
- 20 flood response, *Journal of Hydrology*, 514, 313–327, doi:10.1016/j.jhydrol.2014.04.014, 2014.
- Pugliese, A., Castellarin, A., and Brath, A.: Geostatistical prediction of flow–duration curves in an index–flow framework, *Hydrology and Earth System Sciences*, 18, 3801–3816, doi:10.5194/hess-18-3801-2014, 2014.
- Rinaldo, A., Beven, K. J., Bertuzzo, E., Nicotina, L., Davies, J., Fiori, A., Russo, D., and Botter, G.: Catchment travel time distributions and water flow in soils, *Water Resour. Res.*, 47, W07 537, 2011.
- 25 Rinaldo, A., Benettin, P., Harman, C. J., Hrachowitz, M., McGuire, K. J., van der Velde, Y., Bertuzzo, E., and Botter, G.: Storage selection functions: A coherent framework for quantifying how catchments store and release water and solutes, *Water Resources Research*, 51, 4840–4847, rinaldo, Andrea Benettin, Paolo Harman, Ciaran J. Hrachowitz, Markus McGuire, Kevin J. van der Velde, Ype Bertuzzo, Enrico Botter, Gianluca, 2015.
- Rodriguez-Iturbe, I., Porporato, A., Ridolfi, L., Isham, V., and Coxi, D. R.: Probabilistic modelling of water balance at a point: the role of
- 30 climate, soil and vegetation, *Proceedings of the Royal Society A: Mathematical, Physical and Engineering Sciences*, 455, 3789–3805, doi:10.1098/rspa.1999.0477, 1999.
- Schaefli, B., Rinaldo, A., and Botter, G.: Analytic probability distributions for snow-dominated streamflow, *Water Resources Research*, 49, 2701–2713, doi:10.1002/wrcr.20234, 2013.
- Schwarb, M., Daly, C., Frei, C., and Schär, C.: Mean annual precipitation throughout the European Alps 1971–1990, *Hydrologic atlas of*
- 35 Switzerland, pp. 2–6, 2001.
- Searcy, J. K.: *Flow-duration curves*, US Government Printing Office, 1959.
- Spreafico, M. and Weingartner, R.: *The hydrology of Switzerland: selected aspects and results*, Bundesamt für Wasser und Geologie, 2005.



- Viviroli, D., Zappa, M., Gurtz, J., and Weingartner, R.: An introduction to the hydrological modelling system PREVAH and its pre- and post-processing-tools, *Environmental Modelling & Software*, 24, 1209–1222, doi:10.1016/j.envsoft.2009.04.001, 2009.
- Vogel, R. M. and Fennessey, N. M.: Flow-Duration Curves I: New Interpretation and Confidence Intervals, *Journal of Water Resources Planning and Management*, 120, 485–504, doi:10.1061/(asce)0733-9496(1994)120:4(485), 1994.
- 5 Vogel, R. M. and Fennessey, N. M.: Flow duration curves II: a review of the applications in water resources planning, *Journal of the American Water Resources Association*, 31, 1029–1039, doi:10.1111/j.1752-1688.1995.tb03419.x, 1995.
- Wagener, T., Sivapalan, M., Troch, P., and Woods, R.: Catchment Classification and Hydrologic Similarity, *Geography Compass*, 1, 901–931, doi:10.1111/j.1749-8198.2007.00039.x, 2007.
- Weingartner, R. and Aschwenden, H.: Discharge regime—the basis for the estimation of average flows, *Hydrological Atlas of Switzerland*, 10 Plate, 5, 26, 1992.

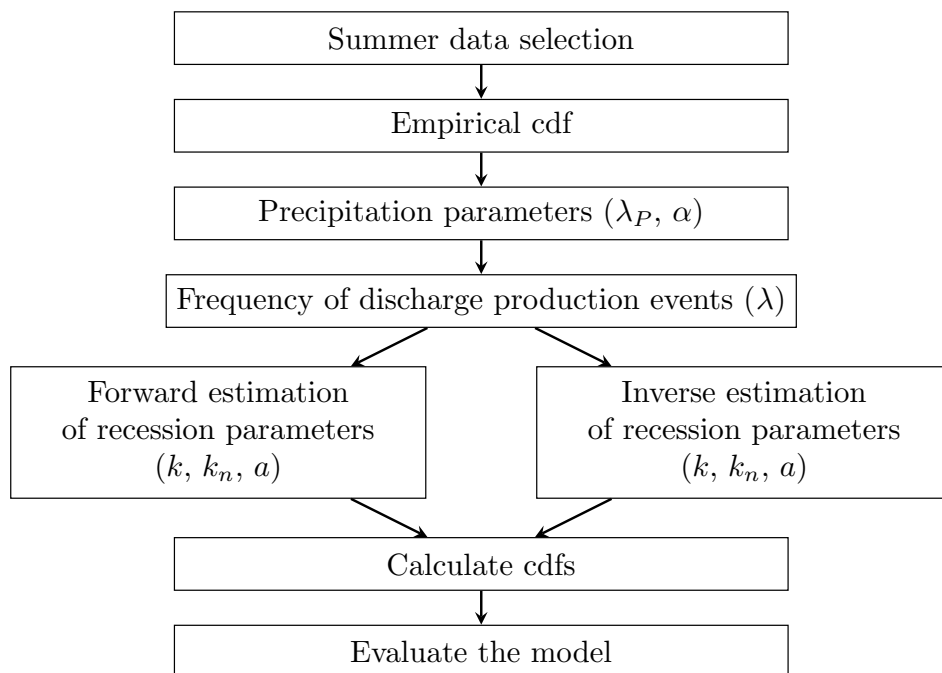


Figure 1. Parameter estimation and model evaluation.

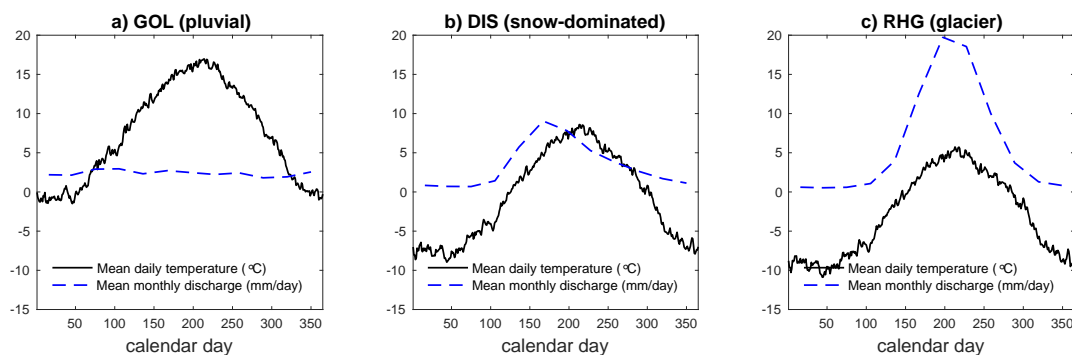


Figure 2. Examples of the behavior of discharge and temperature for catchments under different regimes

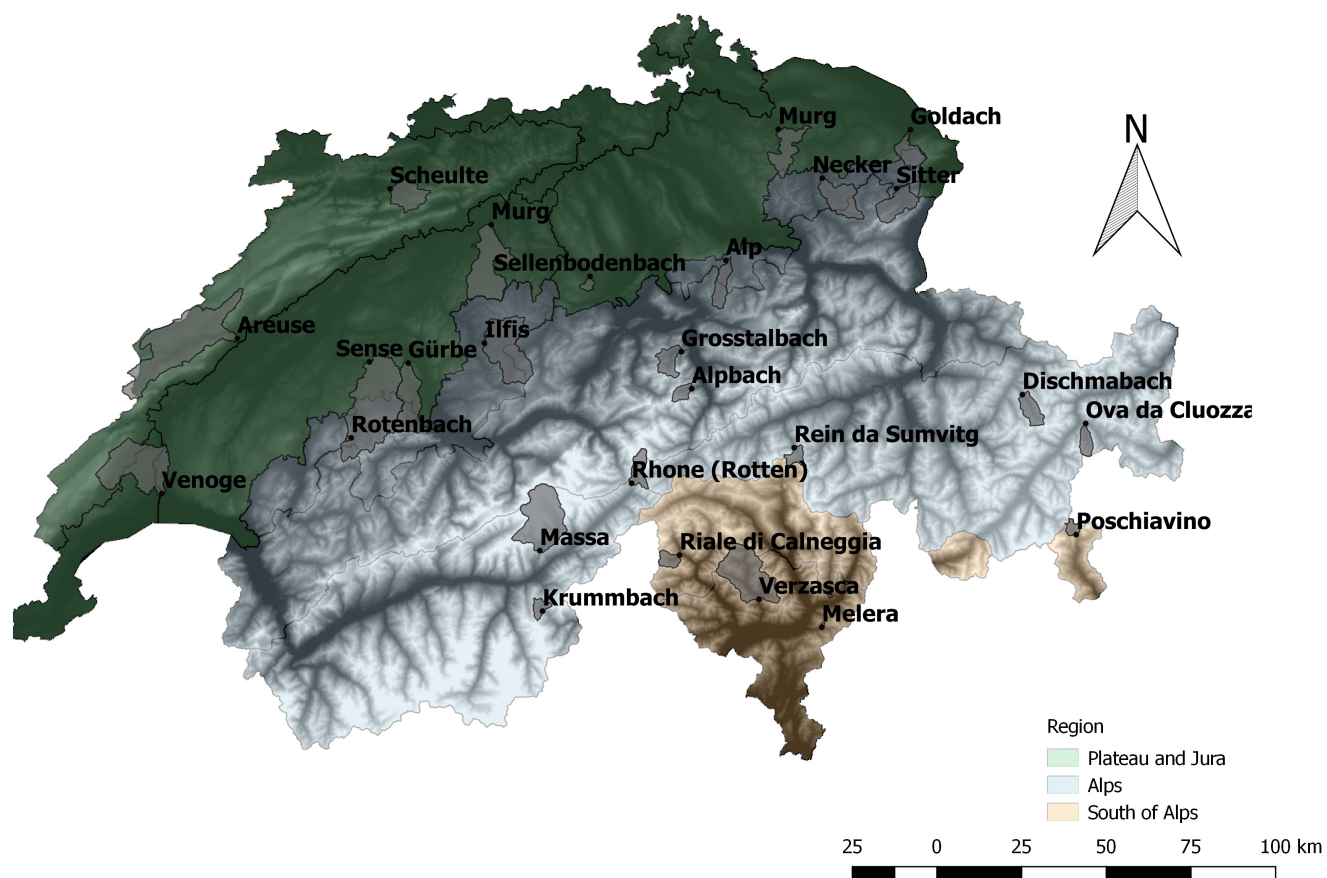


Figure 3. Location of the case studies in Switzerland.

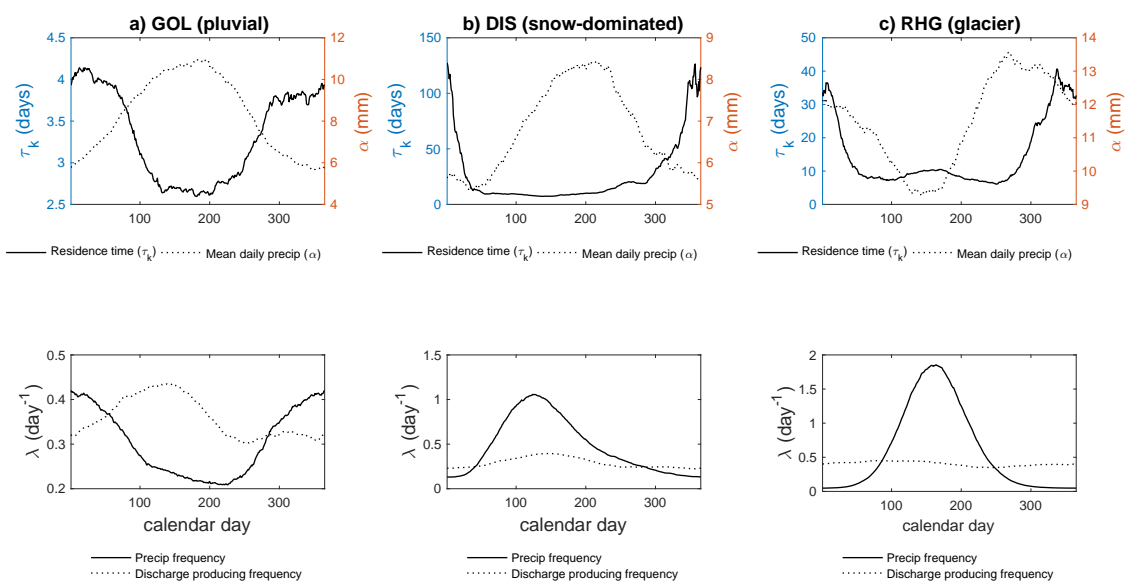


Figure 4. Examples of the annual variation of the model parameters. The parameters are calculated for 90 days intervals beginning at the calendar day for which the value is plotted. Top row: residence time τ_k and mean daily precipitation depth α ; bottom row: precipitation frequency λ_p and discharge-producing frequency λ .

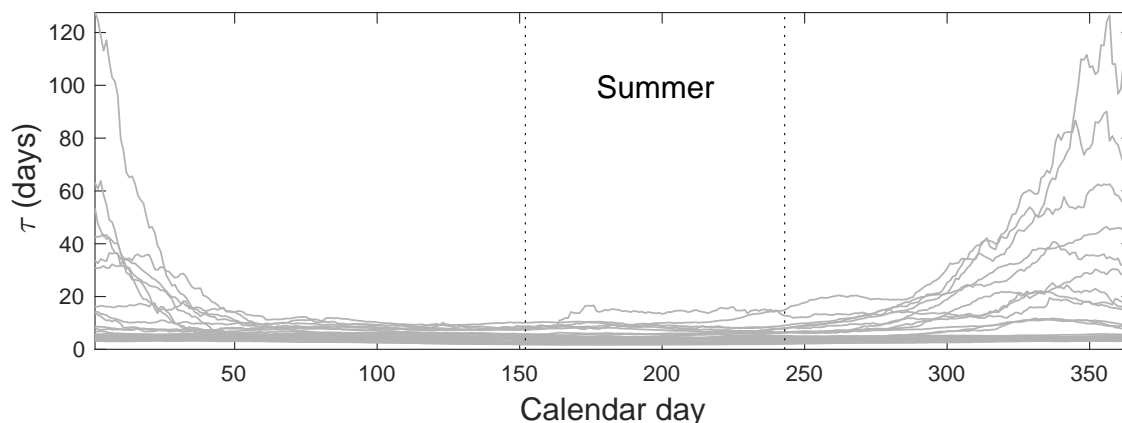


Figure 5. Annual variation of the residence time (τ_k) for the 26 catchments.

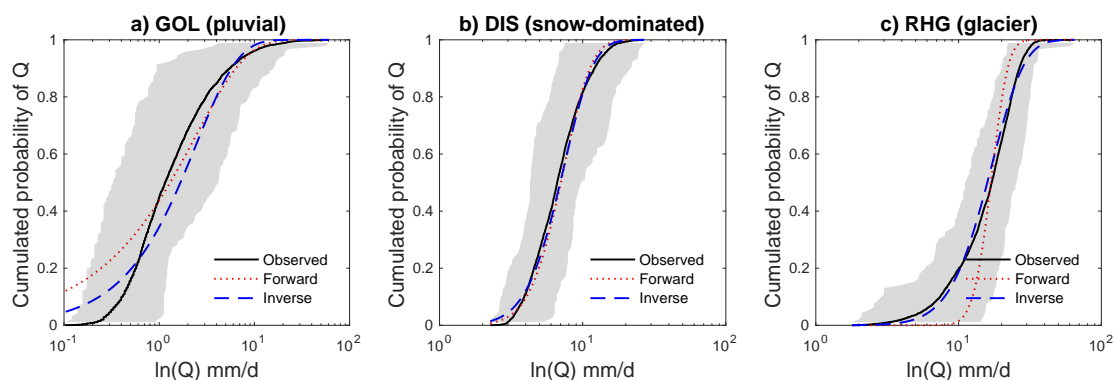


Figure 6. Linear model results for summer in the three selected catchments. The area comprehended between the cdf envelopes that represents the natural variability of the discharges is shaded.

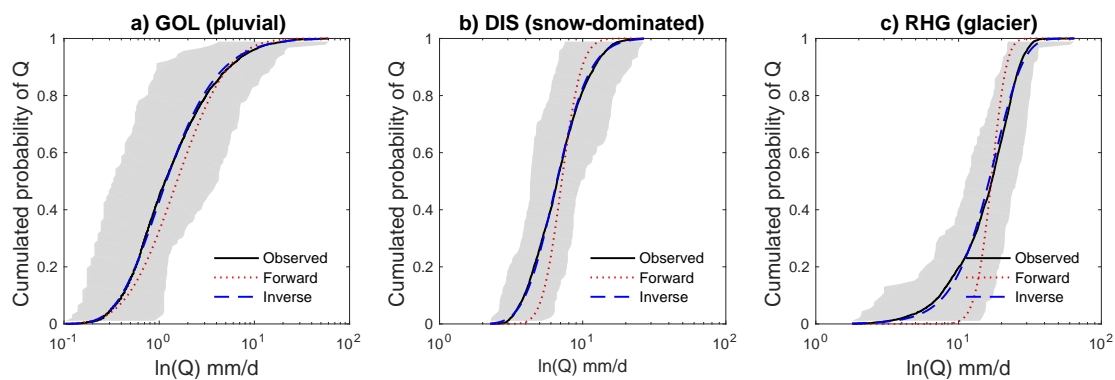


Figure 7. Nonlinear model results for summer in selected catchments. The area comprehended between the cdf envelopes that represents the natural variability of the discharges is shaded.

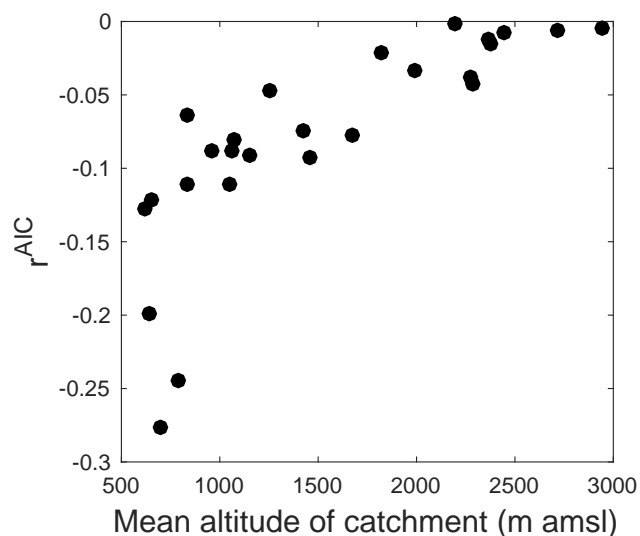


Figure 8. Performance of the relative performance increase of the nonlinear with respect to the linear model as a function of mean catchment elevation.

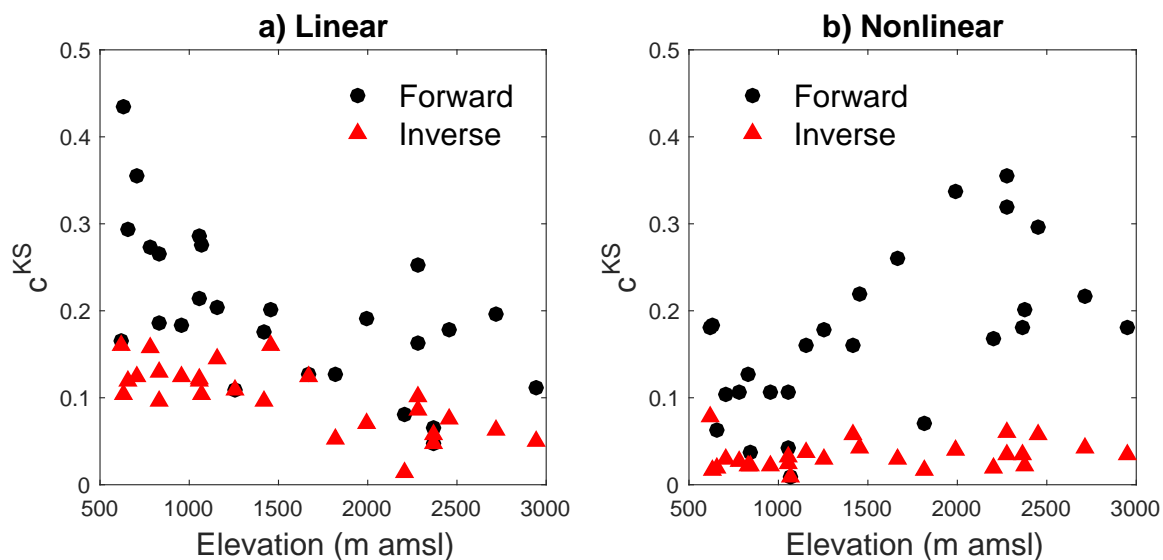


Figure 9. Performance of the linear and nonlinear models as a function of mean catchment elevation.



Table 1. Characteristics of case studies in Switzerland as given in the FOEN database, including i) the period for which discharge and gridded precipitation are available; ii) regime classification according to the sixteen Swiss regimes and to the simplified three classes used here. P stands for the mean annual precipitation and \bar{T} is the mean annual temperature

ID	Name	Coordinates	Area (km ²)	Mean elevation (m asl.)	Station elevation (m asl.)	Glaciation (%)	P (mm)	\bar{T} (°C)	Data period	Regime 16 classes	Regime 3 classes
2430	Rein da Sunvigt - Sumvigt, Encardens	718810 / 167690	21.8	2450	1490	6.7	1707	-1,19	15-09-1977 to 31-12-2014	b-glacio nival	glacier
2327	Dischmabach - Davos, Kriegsmatte	786220 / 183370	43.3	2372	1668	2.1	1021	-0,62	24-07-1961 to 31-12-2014	b-glacio nival	glacier
2308	Goldach - Goldach, Bleiche	753190 / 261590	49.8	833	399	0	1446	7,39	01-01-1974 to 31-12-2014	pluvial supérieur	pluvial
2374	Necker - Mogelsberg, Aachsäge	727110 / 247290	88.2	959	606	0	1777	6,47	01-01-1972 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
2112	Sitter - Appenzell	749040 / 244220	74.2	1252	769	0,08	1904	5,10	01-01-1961 to 31-12-2014	nival de transition	snow-dominated
2126	Murg - Wängi	714105 / 261720	78.9	650	466	0	1357	7,90	01-01-1961 to 31-12-2014	pluvial inférieur	pluvial
2610	Scheulte - Vicques	599485 / 244150	72.8	785	463	0	1325	7,27	01-01-1992 to 31-12-2014	nivo-pluvial jurassien	snow-dominated
2159	Gürbe - Belp, Mülimatt	604810 / 192680	117	837	522	0	1295	7,21	01-01-1961 to 31-12-2014	pluvial supérieur	pluvial
2251	Rotenbach - Plaffeien, Schwyberg	587980 / 170590	1.65	1454	1275	0	1910	5,81	01-09-1961 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
2179	Sense - Thörishaus, Sense matt	593350 / 193020	352	1068	553	0	1479	6,29	01-01-1961 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
2480	Areuse - Boudry	554350 / 199940	377	1060	444	0	1531	5,41	01-01-1961 to 31-12-2014	pluvial jurassien	pluvial
2603	Ilfis - Langnau	627320 / 198600	188	1051	685	0	1719	6,22	01-04-1989 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
2471	Murg - Murgenthal, Walliswil	629340 / 233555	207	637	419	0	1252	7,84	26-06-1980 to 31-12-2014	pluvial inférieur	pluvial
2608	Sellenbodenbach - Neuenkirch	658530 / 218290	10.5	615	515	0	1230	8,72	12-09-1980 to 31-12-2014	pluvial inférieur	pluvial
2299	Alpbach - Erstfeld, Bodenberg	688560 / 185120	20.6	2200	1022	27,7	1645	0,68	01-01-1961 to 31-12-2014	b-glaciaire	glacier
2276	Grosstalbach - Isenthal	685500 / 196050	43.9	1820	767	9,3	1801	2,22	01-01-1961 to 31-12-2014	nival alpin	snow-dominated
2609	Alp - Einsiedeln	698640 / 223020	46.4	1155	840	0	2005	5,43	27-02-1991 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
2268	Rhone - Gletsch	670810 / 157200	38.9	2719	1761	52,2	2066	-2,98	01-01-1961 to 31-12-2014	a-glaciaire	glacier
2161	Massa - Blatten bei Naters	643700 / 137290	195	2945	1446	65,9	2423	-3,18	01-01-1961 to 31-12-2014	a-glaciaire	glacier
2432	Venoge - Ecublens, Les Bois	532040 / 154160	231	700	383	0	1181	9,29	01-01-1979 to 31-12-2014	pluvial jurassien	pluvial
2206	Melera - Melera (Valle Morobbia)	726988 / 114670	1.05	1419	944	0	1716	4,74	01-01-2005 to 31-12-2014	nivo-pluvial méridional	snow-dominated
2605	Verzasca - Lavertezzo, Campiòi	708420 / 122920	186	1672	490	0	2051	4,37	01-09-1989 to 31-12-2014	nivo-pluvial méridional	snow-dominated
2356	Riale di Calneggia - Caveragno, Pontit	684970 / 135960	24	1996	890	0	1918	2,54	01-01-1967 to 31-12-2014	nival méridional	snow-dominated
2244	Krummbach - Klusmatten	644500 / 119420	19.8	2276	1795	3	1475	1,92	01-01-1995 to 31-12-2014	nival méridional	snow-dominated
2366	Poschiavino - La Rösa	802120 / 142010	14.1	2283	1860	0,35	1512	0,02	01-01-1970 to 31-12-2014	nival méridional	snow-dominated
2319	Ova da Cluozza - Zerne	804930 / 174830	26.9	2368	1509	2,2	963	-1,36	24-07-1961 to 31-12-2014	nivo-glaciaire	snow-dominated



Table 2. Parameter values and performance indicators for all the catchments for summer with linear model and forward estimation, summer linear model and inverse estimation, summer nonlinear model and forward estimation, winter nonlinear model and inverse estimation, winter linear model and forward estimation. \bar{Q} stands for the mean observed discharge, P_s the mean total precipitation during summer, \bar{T}_s the mean temperature during summer, I for interception depth, c^{KS} for the Kolmogorov-Smirnov distance. The indices stand for: f forward estimation, i inverse estimation, l linear model, n nonlinear model.

Name	\bar{Q} (mm/d)	P_s (mm)	\bar{T}_s (°C)	α (mm/d)	λ_P mm	I (l/d)	λ (mm)	k_f (l/d)	c_{lf}^{KS}	k_i (l/d)	c_{li}^{KS}	c_{li}^{AIC}
Rein da Sumvitg - Sumvitg, Encardens	13,8	532	5,62	12,4	0,410	1,83	1,115	0,201	0,179	0,383	0,075	21550
Dischmabach - Davos, Kriegsmatte	7,4	378	6,49	8,2	0,377	2,29	0,906	0,136	0,065	0,163	0,048	22300
Goldach - Goldach, Bleiche	2,5	513	15,15	11,0	0,376	3,13	0,224	0,370	0,187	0,236	0,130	13494
Necker - Mogelsberg, Aachsäge	3,3	600	14,22	12,2	0,393	3,30	0,273	0,435	0,183	0,275	0,125	16467
Sitter - Appenzell	5,4	648	12,30	12,5	0,433	3,06	0,427	0,393	0,109	0,308	0,108	25067
Murg - Wängi	1,7	432	16,07	9,6	0,348	3,13	0,174	0,282	0,293	0,105	0,120	13636
Scheulte - Vicques	1,5	388	15,10	9,1	0,312	3,46	0,162	0,264	0,274	0,133	0,158	5262
Gürbe - Belp, Mülimatt	2,1	450	15,15	9,9	0,355	3,06	0,210	0,271	0,266	0,096	0,095	15070
Rotenbach - Plaffeien, Schwyberg	4,3	616	13,29	14,0	0,378	3,16	0,309	0,550	0,202	0,339	0,161	22856
Sense - Thörishaus, Sense matt	2,2	483	13,98	10,7	0,356	3,22	0,208	0,344	0,275	0,127	0,105	16401
Areuse - Boudry	1,7	383	13,10	8,8	0,316	3,37	0,191	0,261	0,214	0,132	0,120	14013
Ifis - Langnau	2,7	567	13,79	12,4	0,373	3,40	0,220	0,362	0,287	0,149	0,123	8210
Murg - Murgenthal, Walliswil	1,2	389	15,99	9,0	0,323	3,12	0,135	0,230	0,435	0,033	0,105	4779
Sellenbodenbach - Neuenkirch	2,0	431	16,86	9,7	0,357	2,99	0,207	0,381	0,165	0,285	0,161	6617
Alpbach - Erstfeld, Bodenber	16,5	457	7,29	8,9	0,477	1,28	1,858	0,171	0,081	0,276	0,014	30444
Grosstalbach - Isenthal	6,0	598	8,97	11,8	0,444	2,35	0,504	0,195	0,128	0,106	0,053	22256
Alp - Einsiedeln	4,7	687	13,03	14,1	0,415	3,40	0,335	0,521	0,204	0,318	0,144	9763
Rhone - Gletsch	17,1	473	3,58	9,0	0,505	1,00	1,905	0,092	0,197	0,419	0,064	32412
Massa - Blatten bei Naters	17,1	739	3,48	13,9	0,533	1,00	1,228	0,130	0,112	0,272	0,049	32418
Venoge - Ecublens, Les Bois	0,7	298	17,39	7,9	0,268	3,14	0,090	0,194	0,355	0,056	0,124	3737
Melera - Melera (Valle Morobbia)	3,1	562	12,64	18,1	0,273	3,87	0,174	0,142	0,176	0,079	0,096	2918
Verzasca - Lavertezzo, Campiòi	6,0	581	12,03	17,9	0,313	3,00	0,333	0,287	0,127	0,294	0,125	11649
Riale di Calneggia - Caveragno, Pontit	8,9	482	9,96	13,5	0,332	2,04	0,655	0,173	0,192	0,352	0,071	25838
Krummbach - Klusmatten	6,0	317	9,30	9,2	0,294	2,35	0,656	0,117	0,253	0,297	0,102	8673
Poschiavino - La Rösa	5,4	424	7,83	11,1	0,323	2,49	0,490	0,125	0,162	0,199	0,087	19679
Ova da Cluozza - Zerne	5,2	329	6,58	8,4	0,342	1,77	0,619	0,215	0,047	0,192	0,058	21954

Name	$k_{n,f}$	a_f	$c_{n,f}^{KS}$	$k_{n,i}$	a_i	$c_{n,i}^{KS}$	$c_{n,i}^{AIC}$
Rein da Sumvitg - Sumvitg, Encardens	0,029	1,46	0,296	0,110	1,52	0,057	21387
Dischmabach - Davos, Kriegsmatte	0,013	1,73	0,201	0,031	1,86	0,022	21972
Goldach - Goldach, Bleiche	0,145	1,50	0,126	0,174	1,81	0,023	11990
Necker - Mogelsberg, Aachsäge	0,125	1,63	0,107	0,156	1,81	0,023	15015
Sitter - Appenzell	0,066	1,69	0,179	0,115	1,76	0,029	23888
Murg - Wängi	0,099	1,70	0,062	0,081	1,98	0,019	11978
Scheulte - Vicques	0,099	1,72	0,106	0,117	2,20	0,027	3978
Gürbe - Belp, Mülimatt	0,068	1,76	0,036	0,063	1,76	0,023	14108
Rotenbach - Plaffeien, Schwyberg	0,080	1,81	0,218	0,154	1,87	0,043	20753
Sense - Thörishaus, Sense matt	0,084	1,85	0,010	0,082	1,86	0,009	15069
Areuse - Boudry	0,078	1,85	0,106	0,116	1,77	0,032	12785
Ifis - Langnau	0,068	1,96	0,042	0,069	2,04	0,025	7303
Murg - Murgenthal, Walliswil	0,056	2,29	0,183	0,026	2,51	0,016	3831
Sellenbodenbach - Neuenkirch	0,184	1,38	0,181	0,271	1,49	0,077	5776
Alpbach - Erstfeld, Bodenber	0,057	1,17	0,168	0,156	1,21	0,020	30420
Grosstalbach - Isenthal	0,017	1,88	0,070	0,025	1,86	0,016	21768
Alp - Einsiedeln	0,089	1,76	0,160	0,110	1,97	0,036	8870
Rhone - Gletsch	0,107	0,87	0,216	0,897	0,70	0,043	32234
Massa - Blatten bei Naters	0,052	1,13	0,181	0,585	0,70	0,034	32274
Venoge - Ecublens, Les Bois	0,119	1,65	0,103	0,104	2,00	0,030	2706
Melera - Melera (Valle Morobbia)	0,054	0,92	0,161	0,031	1,94	0,057	2702
Verzasca - Lavertezzo, Campiòi	0,041	1,70	0,261	0,081	1,94	0,030	10738
Riale di Calneggia - Caveragno, Pontit	0,014	1,79	0,336	0,077	1,79	0,039	24958
Krummbach - Klusmatten	0,032	1,37	0,354	0,064	1,99	0,060	8345
Poschiavino - La Rösa	0,014	1,75	0,318	0,042	2,05	0,035	18837
Ova da Cluozza - Zerne	0,030	1,70	0,180	0,083	1,58	0,034	21673