

Analytical flow duration curves for summer streamflow in Switzerland

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Abstract. This paper proposes a systematic assessment of the performance of an analytical modeling framework for streamflow probability distributions for a set of 25 Swiss catchments. These catchments show a wide range of hydroclimatic regimes, including namely snow-influenced streamflows. The model parameters are calculated from a spatially averaged gridded daily precipitation data set and from observed daily discharge time series, both in a forward estimation mode (direct parameter calculation from observed data) and in a inverse estimation mode (maximum likelihood estimation). The performance of the linear and the nonlinear model versions is assessed in terms of reproducing observed flow duration curves and their natural variability. Overall, the nonlinear model version outperforms the linear model for all regimes, but the linear model shows a notable performance increase with catchment elevation. More importantly, the obtained results demonstrate that the analytical model performs well for summer discharge for all analyzed streamflow regimes, ranging from rainfall-driven regimes with summer low flow to snow and glacier regimes with summer high flow. These results suggest that the model's encoding of discharge-generating events based on stochastic soil moisture dynamics is more flexible than previously thought. As shown in this paper, the presence of snow- or icemelt is accommodated by a relative increase of the discharge-generating frequency, a key parameter of the model. Explicit quantification of this frequency increase as a function of mean catchment meteorological conditions is left for future research.

15 1 Introduction

Knowledge of the availability and variability of daily discharges in a given stream section proves useful for many engineering applications (e.g. the design of hydro-power plants or water supply systems), as well as for studies about stream ecology alterations and sediment transport or about water quality and allocation (Basso et al., 2015; Ceola et al., 2010; Searcy, 1959; Vogel and Fennessey, 1995). For many such applications, knowledge of the probability distribution of daily discharges rather than of their exact temporal occurrence is sufficient.

In hydrology, the probability distribution of daily discharges is traditionally not represented as a probability density function (pdf) but in terms of flow duration curves (FDCs) that associate an exceedance probability to each discharge value (Vogel and Fennessey, 1994) and that correspond to the complement of the cumulative distribution function (cdf).

Different methods exist to estimate FDCs (ie. to estimate their shape), the most straightforward method being the assignment of empirical probabilities to observed ranked data (yielding empirical FDCs) (Vogel and Fennessey, 1994). FDCs can also be obtained from statistical methods that relate the FDC shape to catchment characteristics (Castellarin et al., 2013).

An important category of FDC models are process-based models that combine climate controls and catchment characteristics to estimate the shape of FDCs. Such models describe the shape of FDCs either based on long term simulations of the system behavior or based on a direct parameterization of the FDC shape as a function of key hydrological controls. One such model is the model developed by Botter et al. (2007c), who derived an analytical description of streamflow distributions as the result of subsurface flow pulses triggered by stochastic rainfall and censored by the soil moisture dynamics. The resulting streamflow distribution is characterized by only a few parameters: the mean rainfall depth and the frequency of rainfall events that produce discharge, the area of the catchment and the mean residence time of the catchment.

This modelling framework has been applied successfully for a range of case studies in Italy (Botter et al., 2007c, 2009; Ceola et al., 2010; Schaeffli et al., 2013), Switzerland (Basso et al., 2015; Doulatyari et al., 2017; Schaeffli et al., 2013) and the US (Botter et al., 2007a, 2013; Ceola et al., 2010). Müller et al. (2014) expanded the framework to seasonally dry climates with an application in Nepal. According to Müller and Thompson (2016), the benefits of such a process-based approach, as opposed to purely statistical or empirical methods, can be summarized as follows: i) it provides an explicit link between the FDC shape, rainfall characteristics and catchment recession characteristics rather than an empirical or statistical link to regional FDC shapes; ii) the method is applicable to periods characterized by different meteorological conditions, thanks to the explicit treatment of rainfall and evapotranspiration characteristics.

The original model framework was developed for rainfall-driven catchments that show a linear recession behavior. Besides the aforementioned extension to seasonally dry climates, the framework has namely been extended to nonlinear recessions (Botter et al., 2009) and to the description of winter low flow resulting from seasonal snow accumulation (Schaeffli et al., 2013).

In the previous applications of the model, the focus was generally on the study of signatures of discharge regimes under different climates and landscape conditions (Botter et al., 2007a, 2013), where the shape of the pdf was more important than the accuracy of the predicted discharge probabilities. Furthermore, all previous applications deliberately excluded all catchments or seasons that where snowmelt affected (Botter et al., 2007a, 2013; Ceola et al., 2010; Doulatyari et al., 2015).

The objective of this research is to assess and compare the performance of the model in its linear and nonlinear forms for summer streamflows for a range of Alpine discharge regimes. The selected set of case studies covers all Swiss catchments that have a natural (unperturbed) discharge regime and long term discharge monitoring. Compared to existing studies (eg. Basso et al., 2015; Ceola et al., 2010; Doulatyari et al., 2017), this paper provides a systematic analysis of all model parameters and of their seasonality, and a comprehensive analysis of a wide range of discharge regimes, including namely rainfall-driven and

snowfall-influenced regimes. This allows a first detailed view on the suitability of the modeling framework for Alpine summer discharges (influenced by rain and snow) and an assessment of the model performance as a function of the discharge regime.

The paper is organized as follows: Section 2 provides a description of the analytical model, together with the methods adopted in this paper to estimate the model parameters and to assess the model performance, followed by a presentation of the Swiss case studies (Section 3). The obtained results for the linear and nonlinear model versions (Section 4) are discussed in Section 5 with a particular focus on the model performance under different hydrological regimes. The conclusions are summarized in Section 6.

2 Methods

Hereafter, we first give a short overview over the used analytic modelling framework, followed by the two different methods adopted for parameter estimation and for model performance assessment. All methods are applied only to the summer season (June 1st to August 31st, see also Section 3). The model evaluation framework adopted here is synthesized in Figure 1, starting from the empirical cdfs as references for performance evaluation. Next, the precipitation frequency λ_p (Section 2.1) is estimated from precipitation and the discharge-producing frequency λ from observed discharge (Equation 7, Section 2.2). The recession parameters are obtained in forward mode (Section 2.2) or inverse mode (Section 2.3). Based on these parameters, the model cdf is calculated from the linear model (Equation 4) or from the nonlinear model (Equation 6). The model performance is evaluated based on two classical performance indicators and by comparison to the natural variability of the observed cdfs (Section 2.4).

2.1 Model framework

The analytical modelling framework of Botter et al. (2007c) for probabilistic characterization of rainfall-driven daily discharges is based on a soil moisture model originally proposed by Rodriguez-Iturbe et al. (1999). This point-scale model represents the dynamics of soil moisture as the result of a deterministic, state-dependent loss function, combined with stochastic increments triggered by rainfall events. Rodriguez-Iturbe et al. (1999) showed that the corresponding spatially averaged soil moisture $s(t)$ can be obtained from the water balance equation as follows:

$$\frac{ds(t)}{dt} = -\rho[s(t)] + \xi_t, \quad (1)$$

where $-\rho[s(t)]$ is the loss function, due to evapotranspiration, surface runoff and deep percolation, and where ξ_t represents the stochastic instantaneous increments due to infiltration from rainfall.

Botter et al. (2007c) proposed to describe the dynamics of daily streamflow with a similar stochastic differential equation, supposing that rainfall acts as a stochastic forcing for discharge production and that, at the catchment-scale, the water is released following a linear decay:

$$\frac{dQ(t)}{dt} = -kQ(t) + \xi_t'', \quad (2)$$

where Q is the daily streamflow, k is the inverse of the time constant associated with the loss function and ξ_t'' is the stochastic process associated to discharge-producing precipitation events (i.e. the sequence of events that trigger a flow response in the river).

It is assumed hereby that discharge Q is the result of a series of rainfall inputs (ξ_t'') that deliver enough water to fill the water deficit in the soil, i.e. that deliver enough water to raise the soil moisture level above its retention capacity. The excess of water is removed from the soil as subsurface runoff and becomes river discharge. This description of the streamflow response neglects any direct surface flow.

The rainfall forcing ξ_t'' is modeled as a marked Poisson process with frequency λ_p and exponentially distributed rainfall depths with average α (average rainfall on raindays). Not all the rainfall events trigger a streamflow response, i.e. the frequency of discharge-producing events corresponds to $\lambda < \lambda_p$, where λ is influenced by the soil storage capacity and soil drying time and can be written as (Botter et al., 2007a):

$$\lambda = \eta \frac{\exp(-\gamma) \gamma^{\frac{\lambda_p}{\eta}}}{\Gamma(\lambda_p/\eta, \gamma)}, \quad (3)$$

where $\Gamma(a, b)$ is a lower incomplete Gamma function with parameters a and b , $\eta = E/(nZ_r(s_1 - s_w))$, $\gamma = \gamma_p n Z_r (s_1 - s_w)$ and $\gamma_p = 1/\alpha$. E is the maximum evapotranspiration rate and $nZ_r(s_1 - s_w)$ synthesizes the soil volume liable to be filled by water before drainage starts; n is the porosity of the soil, Z_r is the effective soil depth, s_1 is the retention capacity and s_w the permanent wilting point.

As discussed in detail by Botter et al. (2007c), this framework results in the following probability distribution of daily discharges at the catchment-scale:

$$p(Q, t \rightarrow \infty) = \frac{1}{\Gamma(\frac{\lambda}{k})} \frac{1}{Q} \left(\frac{Q}{\alpha k A} \right)^{\frac{\lambda}{k}} \exp\left(-\frac{Q}{\alpha k A}\right), \quad (4)$$

where A is the catchment area. This corresponds to a Gamma distribution with shape parameter λ/k and a scale parameter $\alpha k A$. The corresponding expected mean discharge equals $\bar{Q} = \lambda \alpha$. The model is suitable for steady state conditions, at the annual or seasonal scale, depending on the temporal variability of the model parameters (Botter et al., 2007a).

Nonlinear storage-discharge relations at the catchment-scale are commonly observed (Botter et al., 2009; Brutsaert and Nieber, 1977; Mutzner et al., 2013). Accordingly, Botter et al. (2009) proposed an extension of the above modeling framework assuming that:

$$\frac{dQ(t)}{dt} = -k_n Q(t)^a + \xi_t'', \quad (5)$$

where k_n and a are the constants of the nonlinear recession. As for the linear model, it is possible to obtain an equation for the pdf of the daily discharges:

$$p(Q, t \rightarrow \infty) = C \left\{ \frac{1}{Q^a} \exp\left[-\frac{Q^{2-a}}{\alpha k_n (2-a)} + \frac{Q^{1-a} \lambda}{k_n (1-a)}\right] \right\}, \quad (6)$$

where C is a normalizing constant (Botter et al., 2009).

2.2 Parameter estimation 1: forward estimation

We use the term "forward parameter estimation" to emphasize that the parameters are estimated directly from observed data, without calibration. This method is generally used in the context of this modelling framework for the estimation of the parameters related to the stochastic inputs (λ_p , α , λ), and this method is always used for these parameters in the present paper. However, the recession parameters (k , k_n and a) are either estimated in a forward mode (Botter et al., 2007c, 2009; Ceola et al., 2010; Schaeffli et al., 2013) or in an inverse mode (Ceola et al., 2010) (see Section 2.3).

The computation of the precipitation parameters first involves the computation of a reference catchment-scale precipitation time series (here obtained from gridded data, see Section 3). Then interception losses (I) are subtracted from the observed daily precipitation depths. These losses are in fact evaporated (or sublimated in case of snow) before participating to soil moisture dynamics. Following Rodriguez-Iturbe et al. (1999), previous model applications generally assumed that these losses are accounted for when the frequency of precipitation events is corrected to the frequency of discharge-producing events. In view of understanding how the model parameters vary in space, it was decided here to treat interception losses explicitly with minimal assumptions about this process: different maximum interception depths are attributed to four different land covers: 4 mm for forests, 2 mm, for low vegetation, 1 mm for impervious areas, 0 mm for water bodies (Gerrits, 2010). The catchment-scale maximum interception depth is obtained as the land use-weighted average of these values, but a minimum interception depth of 1 mm is imposed. This catchment-scale interception depth is subtracted from daily precipitation depths, assuming that at a daily time step, all intercepted water re-evaporates during the same time step.

Instead of correcting the frequency of precipitation events λ_p according to Equation 3, the frequency of discharge-producing events λ is estimated directly from the theoretical relationship between the mean discharge and the precipitation parameters, $\bar{Q} = \lambda\alpha$ (see Equation 4). Replacing the mean modelled discharge \bar{Q} with the mean observed discharge \bar{Q} , it follows that

$$\lambda = \frac{\alpha}{\bar{Q}}. \quad (7)$$

Estimating λ from the above equation rather than directly from the soil properties as in Equation 3, has been shown by Ceola et al. (2010) to provide much better results, and this method was used by the majority of studies since then (e.g. Ceola et al., 2010; Botter et al., 2013; Basso et al., 2015).

The recession parameter for the linear model is calculated directly from observed daily discharge based on a classical Brutsaert-Nieber recession analysis (Brutsaert and Nieber, 1977; Biswal and Marani, 2010, 2014; Mutzner et al., 2013), considering, however, only discharges below a certain threshold, fixed to 95%. The nonlinear recession parameters, k_n and a are also obtained based from a recession analysis, using the same discharge threshold via linear regression of the logarithm of $(-dQ/dt)$ versus the logarithm of Q , where a is the slope and k_n the intercept.

2.3 Parameter estimation 2: inverse estimation

To objectively compare the potential of the linear and the nonlinear model formulations to capture observed flow-duration curves, the recession parameters for the linear model (k) and for the nonlinear model (k_n, a) are also estimated in a classical inverse estimation mode where the model parameters are obtained by maximizing the likelihood function formulated for the model. For the linear model, the likelihood function is obtained from the model as follows:

$$\mathcal{L}(k|\tilde{\mathbf{Q}}, \theta) = \prod_{j=1}^N p(\tilde{Q}_j|k, \theta), \quad (8)$$

where the probability $p(\cdot)$ is obtained from Equation 4 and $\theta = [\alpha, A, \lambda]$ is the parameter vector containing all parameters that are estimated directly from observed data (i.e. not maximized). For the nonlinear case, the likelihood is obtained analogously by replacing k with k_n and a and using $p(\cdot)$ from Equation 6.

10 2.4 Model evaluation criteria

To objectively compare different models, we propose to use the Kolmogorov-Smirnov distance between the cdfs corresponding to different models (Ceola et al., 2010; Schaepli et al., 2013), i.e. the maximum difference between the values of the empirical and the modeled cumulative distributions:

$$c^{\text{KS}} = \sup_x |F(\tilde{Q}) - F(Q)|, \quad (9)$$

15 where $F(\tilde{Q})$ corresponds to the empirical cumulative distribution of the discharges and $F(Q)$ to the modeled cumulative distribution of the discharges. A good model should have a low c^{KS} value.

This comparison of the cdfs overcomes an important limitation inherent in the comparison of analytic pdfs and empirical pdfs. In fact, the choice of the number of classes for the calculation of the empirical pdf from observed data (via a so-called frequency polygon, Naghettini, 2016) can change the shape of the empirical pdf. The problem does not arise for cdfs given their cumulative nature.

20 Since the nonlinear model formulation has an additional parameter, the linear and the nonlinear models are also compared based on the Akaike information criterion (Burnham and Anderson, 2004; Ceola et al., 2010; Laio et al., 2009):

$$c^{\text{AIC}} = 2n - \ln(\hat{\mathcal{L}}), \quad (10)$$

where n is the number of parameters of the model and $\ln(\hat{\mathcal{L}})$ is the logarithm of the maximum likelihood function obtained by maximizing Equation 8. As for c^{KS} , a good model should have a low c^{AIC} value.

Based on the above criterion, we measure the relative performance increase from the linear to the nonlinear model as follows:

$$r^{\text{AIC}} = -\left(\frac{c_n^{\text{AIC}} - c_l^{\text{AIC}}}{c_l^{\text{AIC}}}\right), \quad (11)$$

where c_n^{AIC} is the Akaike criterion for the nonlinear model and c_l^{AIC} for the linear model. Taking the opposite of the relative difference between the Akaike criteria ensures that a higher r^{AIC} value indicates a stronger performance increase (recall that the Akaike criterion is to be minimized).

In addition to assess the performance difference between different models, the obtained models are compared to the natural variability of the observed discharge cdfs. Therefore, an empirical long term cdf is constructed, obtained by ranking the observed data in ascending order and dividing the rank numbers by the total sample size. Furthermore, to assess the natural yearly variability, individual cdfs are constructed for each summer season of each civil year (Vogel and Fennessey, 1994). From this collection of annual cdfs, envelopes are obtained based on the maximum and minimum values of discharge for each probability class of the annual cdfs. A reliable model should yield a cdf contained between these curves and should be as close as possible to the long term cdf.

3 Case studies

In this paper, we analyze 25 Swiss catchments with areas ranging from 1.05 km² to 377 km² and with mean elevations ranging from 615 m asl. (meters above sea level) to 2945 m asl. (Table 1, Figure 3). These catchments correspond to all streamflow gauging stations run by the Swiss Federal Office for the Environment (FOEN) (FOEN, 2017) and that have unperturbed discharges (i.e. minimal anthropogenic influence).

The average precipitation at the country scale is around 1300 mm yr⁻¹ (Blanc and Schädler, 2013). The complex topography leads to a high diversity of hydrologic regimes (Weingartner and Aschwanden, 1992), which can be grouped into i) pluvial or rainfall-driven regimes, ii) snow-dominated regimes and iii) glacier regimes. Pluvial regimes are rainfall-dominated with sporadic snowfall events during winter; these regimes occur on the Swiss Plateau and in the Jura region (Figure 3). Snow-dominated regimes result from a seasonal snow cover, roughly at elevations above 900 m asl. In these catchments, solid precipitation accumulates during several weeks up to several months during the cold season (winter) and is entirely released in the following spring and early summer. Glacier regimes result from perennial snow and ice accumulation at elevations roughly beyond 3000 m asl. Most snow-dominated and glacier regimes are located in the Alps region (Figure 3), few of them are located in the South of Alps region, which overall has a warmer climate and presents higher precipitation than the other two regions.

Most Swiss discharge regimes show a strong seasonality (Weingartner and Aschwanden, 1992), illustrated in Figure 2 for typical examples of the three regime main types; air temperature is shown here as a proxy for snow and evapotranspiration processes. The pluvial Goldach river (GOL) shows the typical summer low flow resulting from evapotranspiration; the Dischmabach shows a snow regime with high summer flows resulting from the release of snowmelt stored in the subsurface during the main snowmelt period (spring) and from residual snowmelt during summer. The Rhône river (RHG) with its 50% glacier cover shows a glacier regime, with significant ice melt during summer, and with monthly discharge peaking for the same month as air temperature (July).

It is noteworthy that surface runoff processes can play a certain role for extreme events in all regions of Switzerland (Bernet et al., 2017), but all hydrologic regimes are dominated by subsurface runoff processes, a pre-condition for the application of the modelling framework developed by Botter et al. (2007c).

Besides observed daily discharge, the model requires catchment-scale daily precipitation as input. Most of the previous applications of the models used precipitation from one or several meteorological stations as input (Botter et al., 2007c, a, 2013; Ceola et al., 2010; Basso et al., 2015; Schaeffli et al., 2013). Here, we use the relatively new spatial precipitation data set of MeteoSwiss with a nominal resolution of 2.2 km and an effective resolution between 15 km and 20 km and extending back to 1961 (MeteoSwiss, 2014a). This data set can be assumed to give relatively good estimates of area-averaged precipitation (Paschalis et al., 2014; Addor and Fischer, 2015), even in mountainous areas where there are only few meteorological stations. Corresponding catchment-scale average precipitation time series per case study catchment are obtained by averaging the daily precipitation time series of all pixels contained in the catchment (a list of pixels per catchment is included in the Supplementary Material). In addition, we also used the corresponding gridded temperature data set (MeteoSwiss, 2014b) to support the analysis of parameter seasonality. As for precipitation, the catchment-scale average temperature data set is obtained by averaging the daily time series of all pixels.

Before estimating rainfall frequency (λ_p) and average rainfall depth on raindays (α), the catchment-scale precipitation time series are pre-processed to remove losses from interception. This step requires information about land use. Of the retained 25 case study catchments, 22 are part of what is called "hydrological study areas" and have an associated extended data set, including land use (Aschwanden, 1996). For the other catchments (i.e. the Areuse, Rhône-Gletsch and Venoge), land use is obtained from the Swiss land use database (for Statistics, 2001) Details about the land use estimation are available in the Supplementary Material accompanying this article).

4 Results

4.1 Discharge regimes and parameter seasonality

To gain further insights into the hydrological processes underlying the different regimes, Figure 4 shows the within-year variability of the model parameters obtained by estimating the parameters in forward mode for moving and overlapping 90-day windows. The precipitation parameters α and λ_p do not show strong seasonal patterns, except for a few catchments such as the Goldach river (Figure 4a). For snow and glacier regimes, the frequency of discharge-producing events, λ , increases strongly at the beginning of spring (Figure 4b and c), which indicates the release of water from snow- or icemelt.

The inverse of the linear recession coefficient $\tau = k^{-1}$ shows a coherent annual cycle for all catchments, independent of the underlying discharge regime (Figure 5). This seasonal pattern with consistently low τ values during summer for all catchments clearly justifies the choice of a common summer season (June, July, August) for all regimes. The amplitude of the annual cycle (the difference between high and low τ values) is stronger for snow or glacier regimes, which reflects the fact that in these regimes, parts of the catchment are effectively dormant during the winter (Schaeffli et al., 2013).

4.2 Linear model

All estimated parameters for both forward and inverse estimations are summarized in Table 2, together with the values of the performance indicator c^{KS} . It can be noted that for 11 catchments (i.e. Rein da Sumvitg, Dischmabach, Alpbach, Grosstalbach, Rhône à Gletsch, Massa, Verzasca, Riale di Calneggia, Krumbach, Poschiavino and Ova da Cluozza), λ exceeds λ_p , contradicting the original description of the model (Botter et al., 2007b), which states that the discharge-producing frequency λ is smaller than the precipitation frequency λ_p . Such an exceedance of λ over λ_p should only happen in catchments or seasons with an additional source of water (additional to rainfall), which in the present case is snow- or icemelt. The exceedance of λ over λ_p increases with mean catchment elevation (Figure 6), the limit of $\lambda = \lambda_p$ being at around 1500 m asl. This important result is further discussed in Section 5.

The cdfs obtained from all estimated parameters are presented in Figure 7 for the three example case studies. For the catchment with rainfall-driven discharges (GOL), it can be seen that the probabilities of occurrence of low flows are largely overestimated with forward estimation (Figure 7a). This is a typical indication that the recession time scale is underestimated. The model values even exceed the envelopes that represent the natural variability of the discharges. In the presence of snow, the linear model in forward estimation mode tends to underestimate low flows, with satisfactory results for some cases, such as the Dischmabach (Figure 7b).

Overall, there is a strong increasing trend of the linear model performance with mean catchment elevation (Figure 9a). Despite of this, the results of the linear model are not satisfactory for the forward estimation method for any of the regimes.

The inverse estimation of the model parameters improves the results significantly, but the c^{KS} performance indicator shows relatively high values and the curves are visually not accurate, especially for pluvial regimes. This suggests that the model with a linear discharge decay is overall not suitable for the studied catchments.

4.3 Nonlinear models

The results obtained from inverse parameter estimation for the nonlinear model are very good (Figure 8, Table 2), and the nonlinear model outperforms the linear model for all catchments, both in terms of the KS performance and in terms of the Akaike criterion (Table 2). The relative model performance increase (as measured by r^{AIC}) shows furthermore a strong inverse trend with mean catchment elevation (Figure 10), which results from the increasing performance of the linear model with increasing elevation (Figure 9b). It is noteworthy that the two catchments for which the performance increase of the nonlinear model over the linear models exceeds 20% are the two catchments that have a strongly karst-influenced regime (Scheulte at Vicques and Venoge at Ecublens).

As for the linear model, the forward estimation mode gives less good results than the inverse estimation mode. For some catchments (i.e. Murg-Wängi, Gürbe, Sense, Ilfis, and Grosstalbach), the forward estimation mode gives nevertheless very good results with c^{KS} below 0.1. In general, for the catchments where the discrepancies between modeled and observed cdfs are due to an underestimation of τ , the nonlinear model yields a significant improvement. For catchments where the recession time scale is overestimated with the linear model, the nonlinear model in forward model leads to a performance decrease.

5 Discussion

Our results show that analytical modelling framework for streamflow distributions proposed by Botter et al. (2007c) performs well for the 25 Swiss catchments across all studied discharge regimes. A detailed comparison between the performance of the linear and the nonlinear models considering the optimized parameters obtained from the inverse approach shows that the results for the nonlinear model are always better than for the linear model. This underlines that the nonlinear recession suits better the hydrological conditions of all studied catchments, which is inline with previous results (Basso et al., 2015; Ceola et al., 2010).

In forward estimation mode, the linear model outperforms the nonlinear model for catchments with summer high flows; the nonlinear model outperforms the linear model for catchments with rainfall-driven regimes (i.e. summer low flows). This results from the fact that for regimes with summer high flow, the linear model overestimates the recession time scale (resulting in an underestimation of the discharge variance). For regimes with summer low flow, the linear model in exchange underestimates the recession time scale. Given that the nonlinear model yields longer recessions, the nonlinear model shows accordingly a better performance for regimes with summer low flow.

The comparison between the forward and inverse estimation methods shows a clear underestimation of k_n for most of the catchments, which was already discussed by Dralle et al. (2015) and which is inline with previous work that tried to improve the results of the model in forward estimation mode, for the linear and the nonlinear formulation (Basso et al., 2015; Ceola et al., 2010). There is clearly a need to further improve the methods to estimate the recession parameters. Our results pinpoint that a key hereby might be the detailed investigation of recession analysis methods along elevational gradients and related hydrologic regimes.

Overall, the good model performance in many different catchments with different regimes indicates that the modelling framework is suitable for the prediction of FDCs in Switzerland. A more detailed model temporal model validation (e.g. with a split sample test, Klemeš, 1986) is not possible for this framework since the model parameters are obtained directly from observed data for each time period (i.e. they vary from period to period). The obtained model performances are comparable to the results obtained in previous studies, e.g. in the work of Ceola et al. (2010). They obtained for different case studies in Italy and the US c^{KS} values varying between 0.030 and 0.409 for the nonlinear model using different methods of forward estimation, and c^{KS} values between 0.021 to 0.051 for inverse estimation. For the linear model, Ceola et al. (2010) obtained c^{KS} values between 0.054 and 0.567. Basso et al. (2015) and Doulatyari et al. (2017) studied some case studies that are included in the present paper (Sitter at Appenzell and Murg at Wängi). Recomputing their results with their model parameters yields slightly different c^{KS} values for the nonlinear model for the Sitter (0.12 compared to our 0.19) and for the Murg (0.05 to 0.06 compared to our 0.06). These differences are small and can be explained by different data periods and by the methodological choices in the calculation of parameters.

The most remarkable result of the presented analysis is the fact that the modelling framework is applicable in its original formulation to catchments where summer flow is influenced by snow processes. The additional source of water from snow or icemelt is accommodated by increasing the frequency λ of discharge-producing events. This is inline with a common

assumption in catchment-scale precipitation-runoff modeling (e.g. Schaeffli et al., 2005), which is that runoff from snowmelt can be modeled with exactly the same functional relationships as for rainfall, by simply feeding so-called equivalent precipitation (sum of rainfall and simulated snowmelt) into the runoff generation module.

The increase of the discharge-producing frequency to account for snow or icemelt is furthermore also coherent with the original description of the analytic modelling framework, which incorporates losses as a decrease of the discharge-producing frequency. This type of behavior can be identified in previous studies. Basso et al. (2015) obtained for the Sitter at Appenzell λ values that are close to the precipitation frequency λ_p during spring; for the Thur at Jonschwil they obtain $\lambda = \lambda_p$ for spring. Both catchments have a mean elevation above 1000 m asl., which suggests the presence of snow processes. Later on, Doulatyari et al. (2017) discussed that snow accumulation and melt could be affecting the streamflow pdf estimation for the Sitter at Appenzell, without, however, exploring the issue further.

As can be seen in Figure 6, the switch from $\lambda < \lambda_p$ to λ_p to $\lambda > \lambda_p$ is located at around 1500 m asl. This corresponds to a relatively low mean catchment elevation; for this mean elevation, it can a priori not be assumed that significant snowmelt continues throughout the summer. In fact, for most snow-influenced catchments, the majority of snowmelt happens during spring. Summer flows are nevertheless directly influenced by spring snowmelt since the summer discharge results from a continuous release of melt water stored in the catchment during the preceding snowmelt period. For high elevation catchments, the exceedance of λ over λ_p is directly related to significant snow- and icemelt inputs throughout the summer.

It should be kept in mind here, that for the present study, λ is estimated directly from the relation between discharge and precipitation (see section 2.2 and Equation 7). The question of how to estimate this parameter directly from catchment characteristics based on long term snow cover statistics and data on glacier cover remains to be answered in future work.

Besides the important result that the model is applicable to snow-influenced catchments, additional insights can be obtained from the highlighted model performance trends with mean catchment elevation (Figure 9 and 10). These performance trends are explained by the evolution of the regimes with mean catchment elevation, from rainfall-dominated (pluvial) regimes with summer low flow to snowfall-influenced (nival and glacier) regimes with summer high flow. This result suggests that mean catchment elevation is a good proxy for regime shifts, despite the fact that many other catchment characteristics vary strongly across the set of studied catchments (area, hypsometric curve, land use etc.). Given the strong link between mean catchment elevation, mean catchment air temperature and snow accumulation, this opens interesting perspectives for parameter regionalization.

6 Conclusions

This application of the analytic framework of Botter et al. (2007c) to estimate summer streamflow probability distributions for 25 Swiss catchments shows that this framework performs well without any further methodological adjustments across a wide range of discharge regimes, including rainfall-driven regimes with summer low flows, but also regimes with snow- and glacier melt influenced summer high flows. Given that the original framework was developed for purely rainfall-driven regimes, this result is unexpected. For snow-influenced catchments, the model has been shown here to accommodate the additional source

of water from snowmelt by a relative increase of the discharge-producing frequency, which is coherent with the underlying analytic framework.

5 The detailed comparison between the performance of the linear and the nonlinear model formulation shows that the description of Swiss summer flows strongly benefits from using a nonlinear storage-discharge relationship, in particular for catchments with summer low flow and for the karst catchments. In general, the linear model performance increases for increasing total summer flows or, equivalently, for catchments with higher mean elevation. Future work will focus on improving the model parameter estimation directly from observed data (without parameter optimization), which is a pre-condition for parameter regionalization. Better insights into the physical grounds of the different parameters will also open new perspectives for the extension of the model framework to all four seasons for all Swiss streamflow regimes.

10 *Data availability.* The used meteorological data is currently not freely available but requires a license from MeteoSwiss. The discharge data is available upon request from the Swiss Federal Office for the Environment at <https://www.hydrodaten.admin.ch/en/> (last accessed on 15 December 2017). The used basin boundaries, obtained from the Swiss Federal Office for the Environment, are available in the Supplementary Material of this paper as vector files.

Competing interests. The authors declare that they have no conflict of interest.

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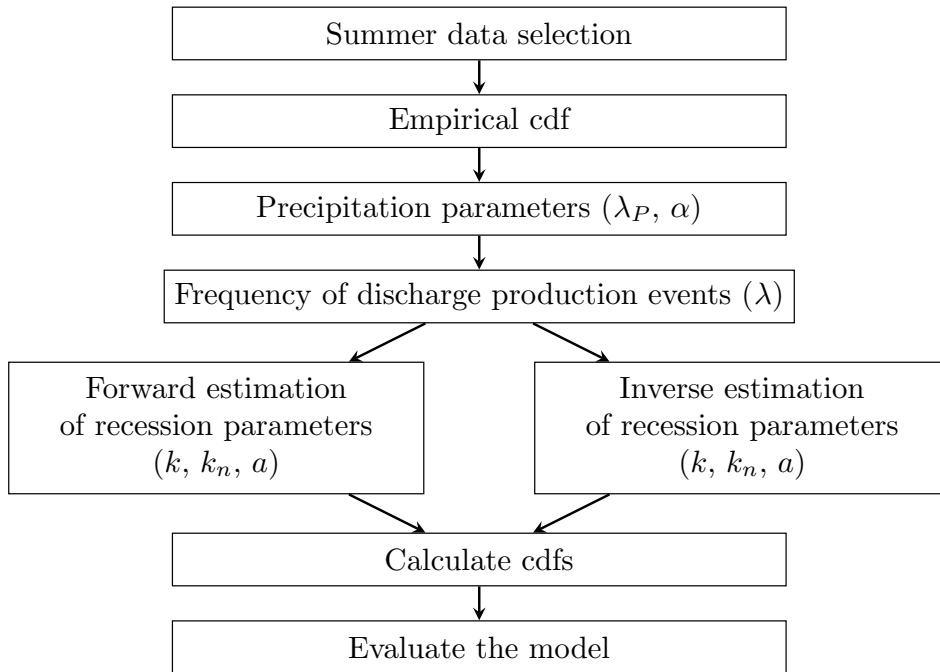


Figure 1. Sketch of the adopted workflow for model parameter estimation and performance assessment.

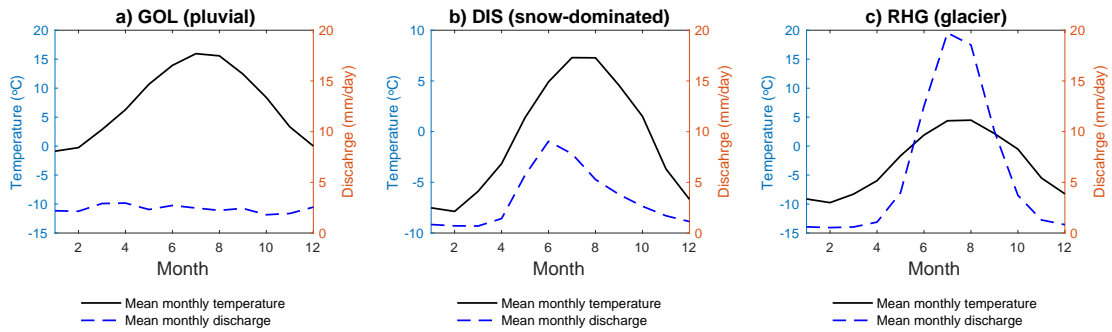


Figure 2. Annual cycle of discharge and air temperature for three selected catchments representing three different hydrologic regimes (pluvial, snow-dominated and glacier regime). Shown are the mean monthly values computed over the entire observation period for each catchment (see Table 1).

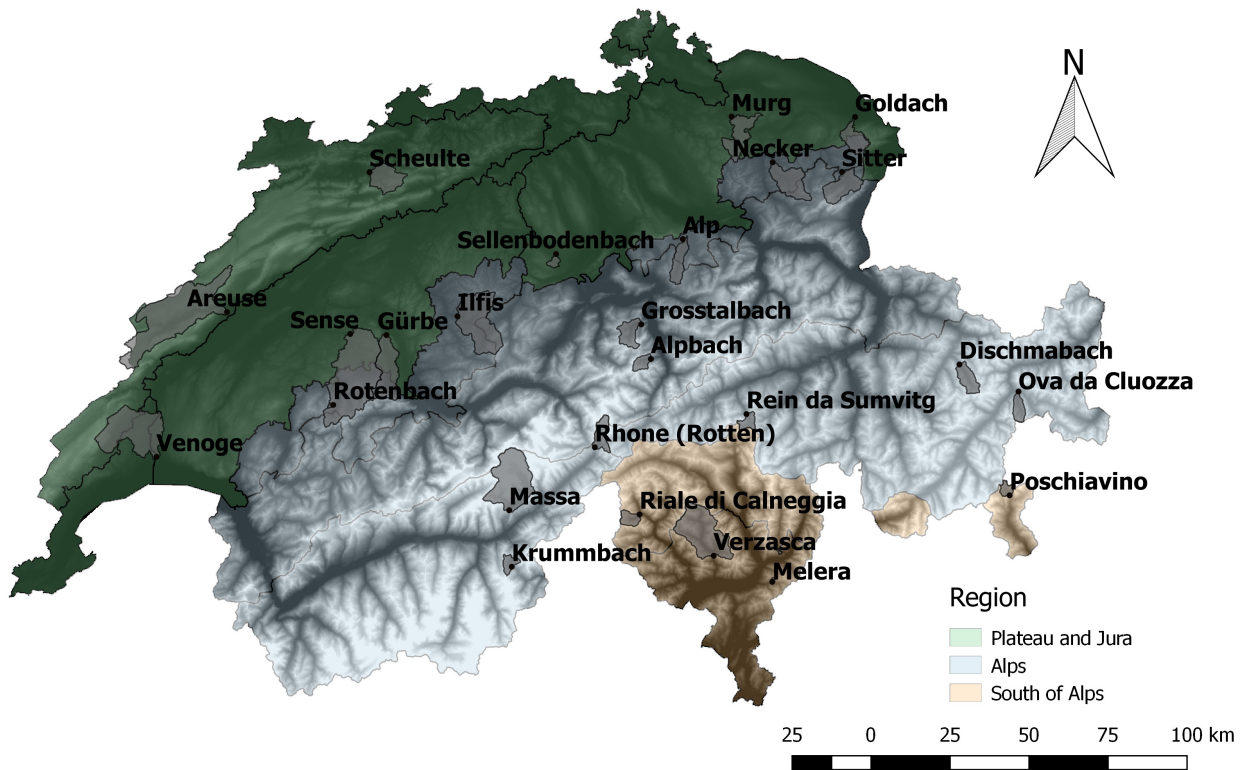


Figure 3. Location of the case study catchments in Switzerland. The six biogeographical regions of Switzerland (for the Environment, 2004) are summarized here into three main regions. Data source: Digital elevation model (SwissTopo, 2005), catchments: (Helbling, 2016).

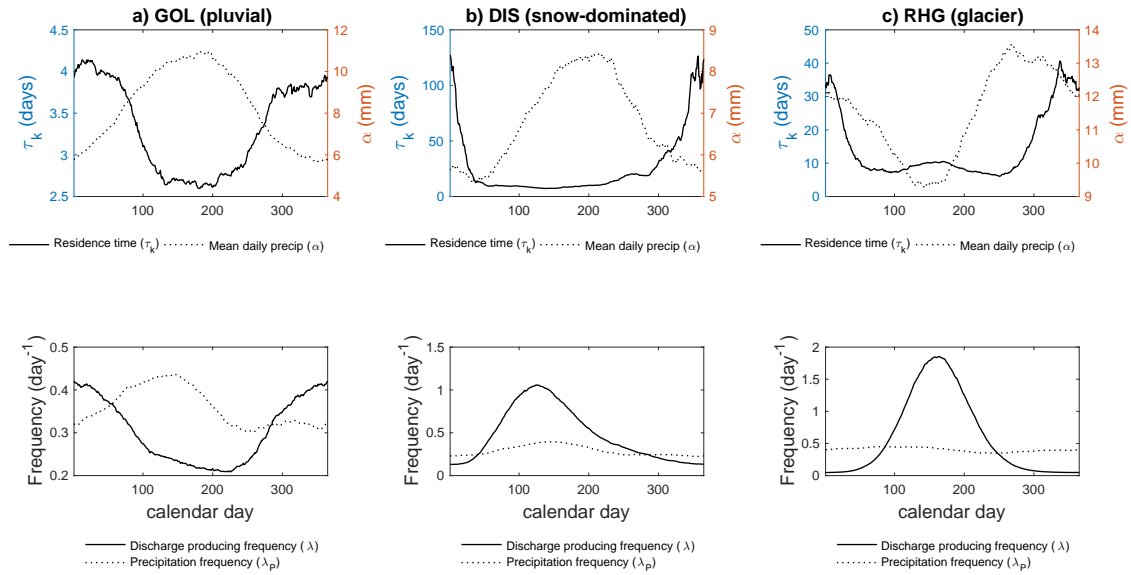


Figure 4. Examples of the temporal variation of the model parameters over the course of a year. The parameters are calculated for 90 days intervals beginning at the calendar day for which the value is plotted; for a given time window, the data points corresponding to this window in all available civil years are pooled together. Top row: residence time τ_k and mean daily precipitation depth α ; bottom row: precipitation frequency λ_p and discharge-producing frequency λ .

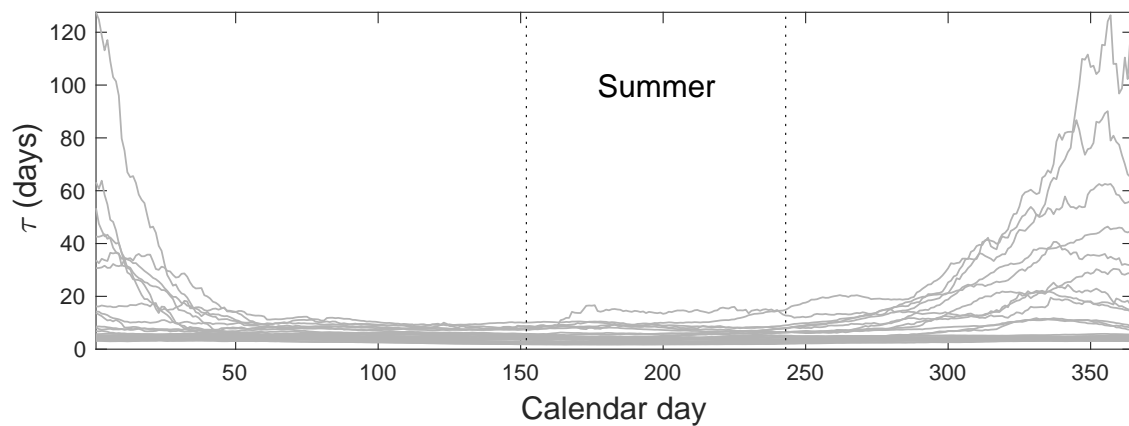


Figure 5. Temporal variation of the residence time ($\tau_k = k^{-1}$) for the 25 catchments. The temporal variation is obtained as in Figure 4.

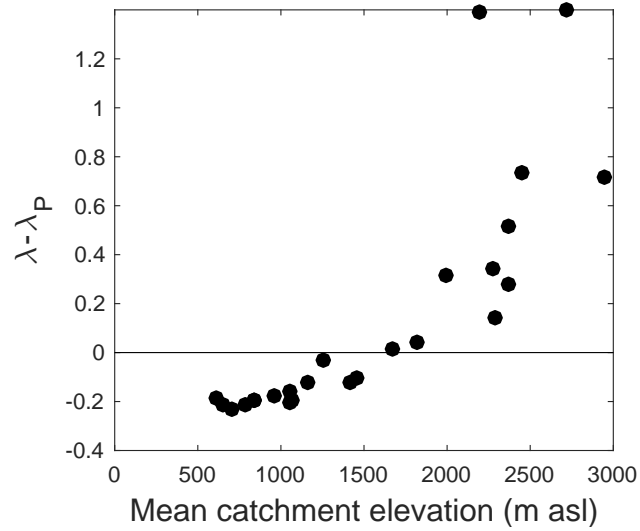


Figure 6. Difference between λ and λ_p as a function of mean catchment elevation.

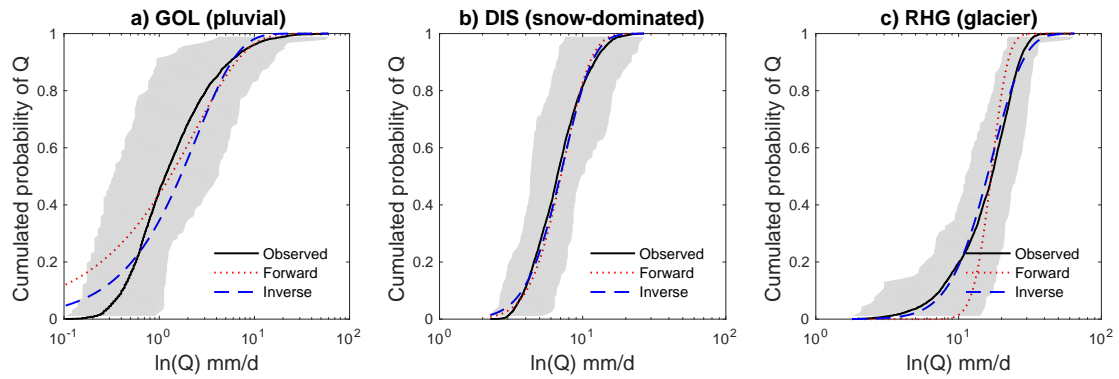


Figure 7. Modelled cdfs with forward and inverse parameter estimation for the three selected catchments. The shaded area is located between the cdf envelopes and represents the natural variability of the daily discharges.

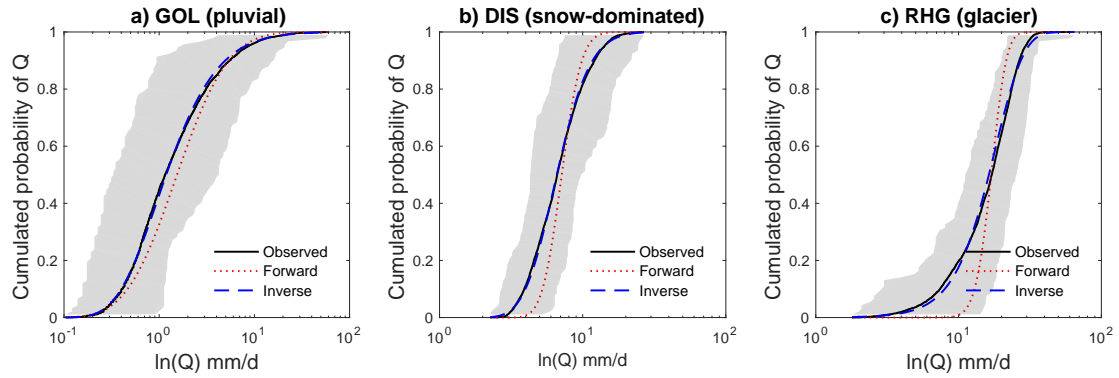


Figure 8. As Figure 7 but for the nonlinear model.

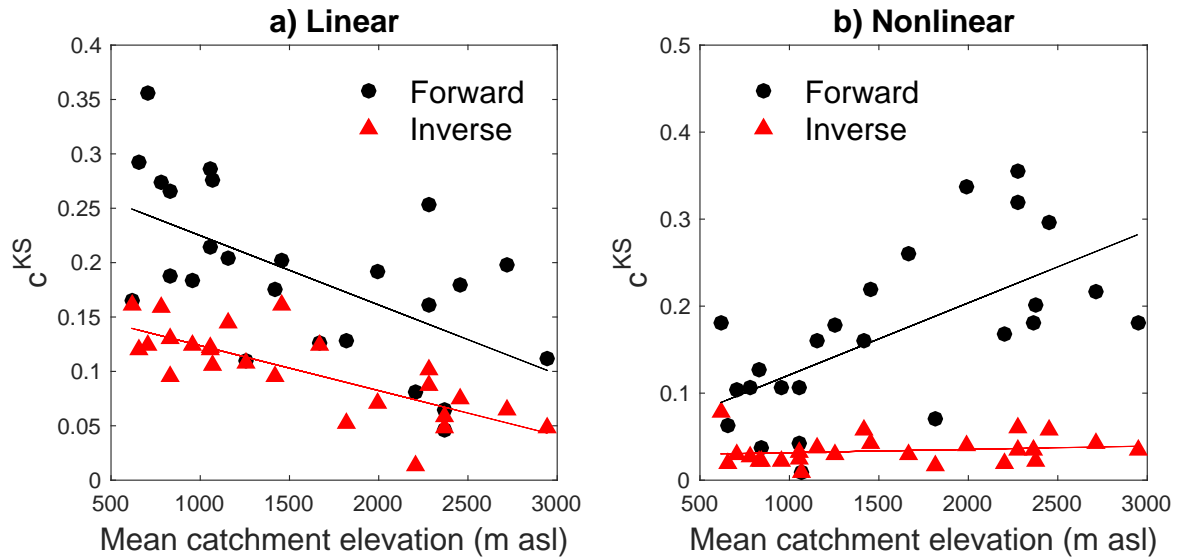


Figure 9. Performance of the linear model and nonlinear model as a function of mean catchment elevation. The shown performance measure, c^{KS} is zero for a perfect model.

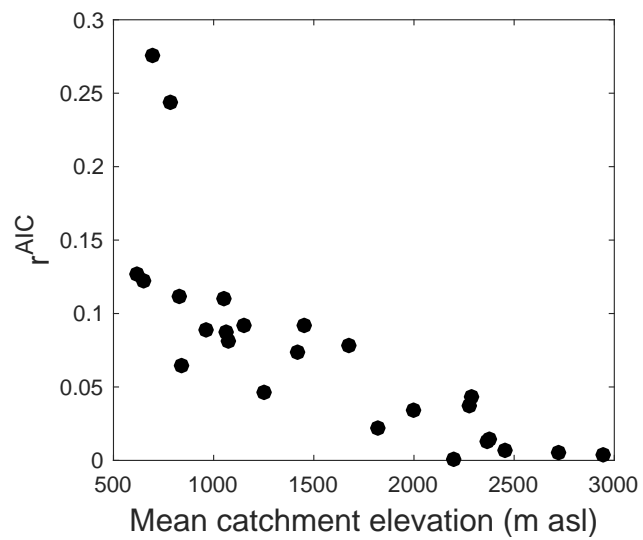


Figure 10. Relative increase of the performance of the nonlinear model with respect to the linear model (as measured by r^{AIC}) as a function of mean catchment elevation. All model parameters are estimated in inverse mode.

Table 1. Characteristics of Swiss case study catchments as given in the FOEN database, including: the FOEN identification code (ID), the catchment name, the Swiss coordinates of the gauging station, the drainage area, the mean elevation of the catchment and the gauging station elevation, the percentage of glacier-cover of the catchment, the mean annual precipitation, the mean annual temperature, the period of data acquisition. The 16 regime classes of Weingartner and Aschwanden (1992) are regrouped here into three classes (details are available in the Supplementary Material).

ID	Name	Coordinates (CH1903)	Area (km ²)	Mean elevation (m asl.)	Station elevation (m asl.)	Glaciation (%)	P (mm)	\bar{T} (°C)	Data period	Regime 16 classes	Regime 3 classes	
1	2430	Rein da Sumvitg - Sumvitg, Encardens	718810 / 167690	21.8	2450	1490	6.7	1707	-1,19	15-09-1977 to 31-12-2014	b-glacio nival	glacier
2	2327	Dischmabach - Davos, Kriegsmatte	786220 / 183370	43.3	2372	1668	2.1	1021	-0,62	24-07-1961 to 31-12-2014	b-glacio nival	glacier
3	2308	Goldach - Goldach, Bleiche	753190 / 261590	49.8	833	399	0	1446	7,39	01-01-1974 to 31-12-2014	pluvial supérieur	pluvial
4	2374	Necker - Mogelsberg, Aachsäge	727110 / 247290	88.2	959	606	0	1777	6,47	01-01-1972 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
5	2112	Sitter - Appenzell	749040 / 244220	74.2	1252	769	0.08	1904	5,10	01-01-1961 to 31-12-2014	nival de transition	snow-dominated
6	2126	Murg - Wängi	714105 / 261720	78.9	650	466	0	1357	7,90	01-01-1961 to 31-12-2014	pluvial inférieur	pluvial
7	2610	Scheulte - Vicques	599485 / 244150	72.8	785	463	0	1325	7,27	01-01-1992 to 31-12-2014	nivo-pluvial jurassien	snow-dominated
8	2159	Gürbe - Belp, Mülimatt	604810 / 192680	117	837	522	0	1295	7,21	01-01-1961 to 31-12-2014	pluvial supérieur	pluvial
9	2251	Rotenbach - Plaffeien, Schwyberg	587980 / 170590	1.65	1454	1275	0	1910	5,81	01-09-1961 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
10	2179	Sense - Thörishaus, Sense matt	593350 / 193020	352	1068	553	0	1479	6,29	01-01-1961 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
11	2480	Areuse - Boudry	554350 / 199940	377	1060	444	0	1531	5,41	01-01-1961 to 31-12-2014	pluvial jurassien	pluvial
12	2603	Ifis - Langnau	627320 / 198600	188	1051	685	0	1719	6,22	01-04-1989 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
13	2608	Sellenbodenbach - Neuenkirch	658530 / 218290	10.5	615	515	0	1230	8,72	12-09-1980 to 31-12-2014	pluvial inférieur	pluvial
14	2299	Alpbach - Erstfeld, Bodenberg	688560 / 185120	20.6	2200	1022	27.7	1645	0,68	01-01-1961 to 31-12-2014	b-glaciaire	glacier
15	2276	Grosstalbach - Isenthal	685500 / 196050	43.9	1820	767	9.3	1801	2,22	01-01-1961 to 31-12-2014	nival alpin	snow-dominated
16	2609	Alp - Einsiedeln	698640 / 223020	46.4	1155	840	0	2005	5,43	27-02-1991 to 31-12-2014	nivo-pluvial préalpin	snow-dominated
17	2268	Rhone - Gletsch	670810 / 157200	38.9	2719	1761	52.2	2066	-2,98	01-01-1961 to 31-12-2014	a-glaciaire	glacier
18	2161	Massa - Blatten bei Naters	643700 / 137290	195	2945	1446	65.9	2423	-3,18	01-01-1961 to 31-12-2014	a-glaciaire	glacier
19	2432	Venoge - Ecublens, Les Bois	532040 / 154160	231	700	383	0	1181	9,29	01-01-1979 to 31-12-2014	pluvial jurassien	pluvial
20	2206	Melera - Melera (Valle Morobbia)	726988 / 114670	1.05	1419	944	0	1716	4,74	01-01-2005 to 31-12-2014	nivo-pluvial méridional	snow-dominated
21	2605	Verzasca - Lavertezzo, Campiòi	708420 / 122920	186	1672	490	0	2051	4,37	01-09-1989 to 31-12-2014	nivo-pluvial méridional	snow-dominated
22	2356	Riale di Calneggia - Caveragno, Pontit	684970 / 135960	24	1996	890	0	1918	2,54	01-01-1967 to 31-12-2014	nival méridional	snow-dominated
23	2244	Krummbach - Klusmatten	644500 / 119420	19.8	2276	1795	3	1475	1,92	01-01-1995 to 31-12-2014	nival méridional	snow-dominated
24	2366	Poschiavino - La Rôsa	802120 / 142010	14.1	2283	1860	0.35	1512	0,02	01-01-1970 to 31-12-2014	nival méridional	snow-dominated
25	2319	Ova da Cluozza - Zernez	804930 / 174830	26.9	2368	1509	2.2	963	-1,36	24-07-1961 to 31-12-2014	nivo glaciaire	snow-dominated

Table 2. Parameter values and performance indicators for all the catchments for summer with linear model and forward estimation, summer linear model and inverse estimation, summer nonlinear model and forward estimation, winter nonlinear model and inverse estimation, winter linear model and forward estimation. \bar{Q} stands for the mean observed discharge, P_s the mean total precipitation during summer, \bar{T}_s the mean temperature during summer, I for interception depth, c^{KS} for the Kolmogorov-Smirnov distance. The indices stand for: f forward estimation, i inverse estimation, l linear model, n nonlinear model.

Name	\bar{Q} (mm/d)	P_s (mm)	\bar{T}_s ($^{\circ}C$)	α (mm/d)	λ_p mm	I (1/d)	λ (mm)	k_f (1/d)	c_{lf}^{KS}	k_i (1/d)	c_{li}^{KS}	c_{li}^{AIC}
Rein da Sumvitg - Sumvitg, Encardens	13,8	532	5,62	12,4	0,410	1,83	1,115	0,201	0,179	0,383	0,075	21550
Dischmabach - Davos, Kriegsmatte	7,4	378	6,49	8,2	0,377	2,29	0,906	0,136	0,065	0,163	0,048	22300
Goldach - Goldach, Bleiche	2,5	513	15,15	11,0	0,376	3,13	0,224	0,370	0,187	0,236	0,130	13494
Necker - Mogelsberg, Aachsäge	3,3	600	14,22	12,2	0,393	3,30	0,273	0,435	0,183	0,275	0,125	16467
Sitter - Appenzell	5,4	648	12,30	12,5	0,433	3,06	0,427	0,393	0,109	0,308	0,108	25067
Murg - Wängi	1,7	432	16,07	9,6	0,348	3,13	0,174	0,282	0,293	0,105	0,120	13636
Scheulte - Vicques	1,5	388	15,10	9,1	0,312	3,46	0,162	0,264	0,274	0,133	0,158	5262
Gürbe - Belp, Mülimatt	2,1	450	15,15	9,9	0,355	3,06	0,210	0,271	0,266	0,096	0,095	15070
Rotenbach - Plaffeien, Schwyberg	4,3	616	13,29	14,0	0,378	3,16	0,309	0,550	0,202	0,339	0,161	22856
Sense - Thörishaus, Sense matt	2,2	483	13,98	10,7	0,356	3,22	0,208	0,344	0,275	0,127	0,105	16401
Areuse - Boudry	1,7	383	13,10	8,8	0,316	3,37	0,191	0,261	0,214	0,132	0,120	14013
Ilfis - Langnau	2,7	567	13,79	12,4	0,373	3,40	0,220	0,362	0,287	0,149	0,123	8210
Sellenbodenbach - Neuenkirch	2,0	431	16,86	9,7	0,357	2,99	0,207	0,381	0,165	0,285	0,161	6617
Alpbach - Erstfeld, Bodenber	16,5	457	7,29	8,9	0,477	1,28	1,858	0,171	0,081	0,276	0,014	30444
Grosstalbach - Isenthal	6,0	598	8,97	11,8	0,444	2,35	0,504	0,195	0,128	0,106	0,053	22256
Alp - Einsiedeln	4,7	687	13,03	14,1	0,415	3,40	0,335	0,521	0,204	0,318	0,144	9763
Rhone - Gletsch	17,1	473	3,58	9,0	0,505	1,00	1,905	0,092	0,197	0,419	0,064	32412
Massa - Blatten bei Naters	17,1	739	3,48	13,9	0,533	1,00	1,228	0,130	0,112	0,272	0,049	32418
Venoge - Ecublens, Les Bois	0,7	298	17,39	7,9	0,268	3,14	0,090	0,194	0,355	0,056	0,124	3737
Melera - Melera (Valle Morobbia)	3,1	562	12,64	18,1	0,273	3,87	0,174	0,142	0,176	0,079	0,096	2918
Verzasca - Lavertezzo, Campiöi	6,0	581	12,03	17,9	0,313	3,00	0,333	0,287	0,127	0,294	0,125	11649
Riale di Calneggia - Cavereno, Pontit	8,9	482	9,96	13,5	0,332	2,04	0,655	0,173	0,192	0,352	0,071	25838
Krummbach - Klusmatten	6,0	317	9,30	9,2	0,294	2,35	0,656	0,117	0,253	0,297	0,102	8673
Poschiavino - La Rösa	5,4	424	7,83	11,1	0,323	2,49	0,490	0,125	0,162	0,199	0,087	19679
Ova da Cluozza - Zerne	5,2	329	6,58	8,4	0,342	1,77	0,619	0,215	0,047	0,192	0,058	21954

Name	k_{nf}	a_f	c_{nf}^{KS}	k_{ni}	a_i	c_{ni}^{KS}	c_{ni}^{AIC}
Rein da Sumvitg - Sumvitg, Encardens	0,029	1,46	0,296	0,110	1,52	0,057	21387
Dischmabach - Davos, Kriegsmatte	0,013	1,73	0,201	0,031	1,86	0,022	21972
Goldach - Goldach, Bleiche	0,145	1,50	0,126	0,174	1,81	0,023	11990
Necker - Mogelsberg, Aachsäge	0,125	1,63	0,107	0,156	1,81	0,023	15015
Sitter - Appenzell	0,066	1,69	0,179	0,115	1,76	0,029	23888
Murg - Wängi	0,099	1,70	0,062	0,081	1,98	0,019	11978
Scheulte - Vicques	0,099	1,72	0,106	0,117	2,20	0,027	3978
Gürbe - Belp, Mülimatt	0,068	1,76	0,036	0,063	1,76	0,023	14108
Rotenbach - Plaffeien, Schwyberg	0,080	1,81	0,218	0,154	1,87	0,043	20753
Sense - Thörishaus, Sense matt	0,084	1,85	0,010	0,082	1,86	0,009	15069
Areuse - Boudry	0,078	1,85	0,106	0,116	1,77	0,032	12785
Ilfis - Langnau	0,068	1,96	0,042	0,069	2,04	0,025	7303
Sellenbodenbach - Neuenkirch	0,184	1,38	0,181	0,271	1,49	0,077	5776
Alpbach - Erstfeld, Bodenber	0,057	1,17	0,168	0,156	1,21	0,020	30420
Grosstalbach - Isenthal	0,017	1,88	0,070	0,025	1,86	0,016	21768
Alp - Einsiedeln	0,089	1,76	0,160	0,110	1,97	0,036	8870
Rhone - Gletsch	0,107	0,87	0,216	0,897	0,70	0,043	32234
Massa - Blatten bei Naters	0,052	1,13	0,181	0,585	0,70	0,034	32274
Venoge - Ecublens, Les Bois	0,119	1,65	0,103	0,104	2,00	0,030	2706
Melera - Melera (Valle Morobbia)	0,054	0,92	0,161	0,031	1,94	0,057	2702
Verzasca - Lavertezzo, Campiöi	0,041	1,70	0,261	0,081	1,94	0,030	10738
Riale di Calneggia - Cavereno, Pontit	0,014	1,79	0,336	0,077	1,79	0,039	24958
Krummbach - Klusmatten	0,032	1,37	0,354	0,064	1,99	0,060	8345
Poschiavino - La Rösa	0,014	1,75	0,318	0,042	2,05	0,035	18837
Ova da Cluozza - Zerne	0,030	1,70	0,180	0,083	1,58	0,034	21673