



1 **MULTI RADAR PERFORMANCE IN THE MIDWESTERN UNITED STATES AT LARGE RANGES**

2

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11

12 **Abstract.** Since the advent of dual-polarized technology, many studies have been conducted to determine  
13 the extent to which the differential reflectivity (ZDR) and specific differential phase shift (KDP) add  
14 benefits to estimating rain rates (R) to reflectivity (Z). It has been previously noted that this new  
15 technology provides significant improvement to rain rate estimation, but only for ranges within 125 km  
16 from the radar. Beyond this range, it is unclear as to whether the National Weather Service conventional  
17 R(Z)-Convective algorithm is superior, as little research has investigated radar precipitation estimate  
18 performance at large ranges. The current study investigates the performance of three radars, St. Louis  
19 (KLSX), Kansas City (KEAX), and Springfield (KSGF), MO, with respect to range, with 15 terrestrial-  
20 based tipping bucket gauges served as ground-truth to the radars. Over 1100 hours of precipitation data  
21 were analyzed for the current study. It was found that, in general, performance degraded with range  
22 beyond, approximately, 150 km from the radar. Probability of detection in addition to bias values  
23 decreased, while the false alarm ratios increased as range increased. Bright-band contamination was  
24 observed to play a potential role as large increases in the absolute bias and overall error values near 120  
25 km for the cool season, and 150 km in the warm season. The analyses found further our understanding in  
26 the strengths and limitations of the Next Generation Radar system overall, and from a seasonal  
27 perspective.



## 28 1 Introduction

29 In 2012, the National Weather Service (NWS) began upgrading the Next Generation Radar  
30 (NEXRAD) system from single- to dual-polarization. The potential benefits of this upgrade were  
31 investigated by the National Severe Storms Laboratory (NSSL) and the Cooperative Institute for  
32 Mesoscale Meteorological Studies. These advantages include, but are not limited to, (1) significant  
33 improvement in radar rainfall estimation (Ryzhkov et al., 2005; Gourley et al., 2010) through better  
34 representation of precipitation shape (Brandes et al., 2002; Gorgucci et al., 2000, 2006), (2)  
35 discrimination between solid and liquid precipitation (Zrnich and Ryzhkov, 1996), allowing for better  
36 distinction between areas of heavy rain and hail (Park et al., 2009; Giangrande and Ryzhkov, 2008;  
37 Cunha et al., 2013), (3) identifying the melting layer position in the radar field (Straka et al., 2000; Park  
38 et al., 2009), and (4) calculating drop-size distributions retrieved from measurements of reflectivity (Z),  
39 differential reflectivity (ZDR), and specific differential phase shift (KDP) as opposed to using ground-  
40 based point located disdrometers (Zhang et al., 2001; Brandes et al., 2004; Anagnostou et al., 2008).

41 Despite the advantages listed above, there are several sources of uncertainty and challenges that  
42 meteorologists and hydrometeorologists currently endure. For example, in order to ensure accuracy in  
43 rain-rate (R) estimates, Ryzhkov et al., (2005) stated the (mis)calibration effects should, approximately,  
44 be limited between  $\pm 1$  dBZ in reflectivity, and  $\pm 0.2$  dB for differential reflectivity. The specific  
45 differential phase has been shown to be unaffected by beam blockage and other absolute calibration  
46 issues (Zrnich and Ryzhkov, 1999), yet attenuation effects may be amplified at X-band radars where the  
47 wavelength of the radar signal is more affected by the size of the hydrometeors (Delrieu et al., 2000;  
48 Berne and Uijlenhoet, 2005).

49 Rain rate retrieval by weather radars is an estimation based upon the dielectric properties of the  
50 hydrometeors encountered in the atmosphere. Therefore, there is no direct measurement of rainfall, and  
51 this inherently introduces error. Although dual-polarized technology allows for the measurements of not



52 only Z, but also ZDR and KDP, conflicting studies have been conducted as to whether dual-polarized  
53 radar rain rate algorithms have improved estimates over single-polarized radar rain rate algorithms. For  
54 example, Gourley et al. (2010) and Cunha et al. (2015) reported that conventional R(Z) algorithms have  
55 significantly better bias than algorithms containing ZDR and/or KDP, while others (e.g., Ryzhkov et al.,  
56 2013; Simpson et al., 2016) report the opposite. This could be due, at least in part, to the fact that  
57 hydrometeor types (e.g., rain versus hail) vary on spatial scales that cannot be easily resolved by even  
58 densely gauged networks.

59 Multiple studies have found that, in general, the performance of radar rain rate estimates decrease  
60 as range increases (Smith et al., 1996; Ryzhkov et al., 2003) which is caused, primarily, by degradation of  
61 beam quality and broadening of the beam with range. Furthermore, the researchers also discuss how the  
62 probability of detection at larger ranges decreases, as the radar beam overshoots shallow, stratiform  
63 precipitation, including winter storms. Bright-banding can also play a crucial role in significantly  
64 increasing the amount of precipitation estimated by the radar.

65 Despite these overall disadvantages, studies have shown that radar rainrate algorithms seldom  
66 exceed absolute errors on the order of  $10 \text{ mm h}^{-1}$ . However, many of these studies have looked at a small  
67 sample of rain events (on the order of 10-50 hours) (Kitchen and Jackson, 1993; Smith et al., 1996;  
68 Ryzhkov et al., 2003; Gourley et al., 2010; Cunha et al., 2013). Additionally, few studies (e.g., Smith et  
69 al., 1996; Cunha et al., 2015; Simpson et al., 2016) quantified meteorologically significant statistical  
70 measures including the probability of detection and false alarm ratio. In order to get a better  
71 understanding of the performance of weather radars on rain rate estimates, more data must be collected  
72 over a broad range of precipitation regimes in addition to an overall broad region of interest.

73 The overarching objective of the current study was to assess the overall performance of three  
74 different radars within the state of Missouri at various ranges from the radar, using terrestrial-based  
75 tipping bucket gauges as ground-truth data. Radar rain rate estimation algorithms include 55 algorithms



76 encompassing standard R(Z) relations, in addition to algorithms containing dual-polarization variables  
77 including ZDR and KDP. A rain rate echo classification algorithm was also tested for performance in  
78 correctly identifying the suitable rain rate algorithm to choose based on the Z, ZDR, and KDP radar  
79 fields. The current work expands upon that of Simpson et al. (2016) such that a larger sample of data were  
80 analyzed (over 1000 hours of rainfall data from forty-six separate days in 2014) to encompass multiple  
81 different precipitation regimes for both summer and winter, with several ground-truth tipping buckets to  
82 analyze the performance of three separate radars at varying ranges, and further expanding upon the effects  
83 of erroneous precipitation estimates on the overall radar error. Objectives for this study included, (1)  
84 statistically analyze the performance of each radar at various ranges (compared against the terrestrial-  
85 based gauges), (2) compute (a) the amount of precipitation incorrectly estimated by the radar (quantifying  
86 the probability of false detection) and (b) the amount of precipitation incorrectly missed by the radar but  
87 measured by the rain gauge, (3) test the overall best radar rain rate algorithm, and (4) perform objectives  
88 (1), (2), and (3) while the data is separated into warm and cool seasons.

89

## 90 **2 Study area and methods**

### 91 **2.1 Study area**

92 National Weather Service radars from St. Louis (KLSX), Kansas City (KEAX), and Springfield  
93 (KSGF), MO are able to scan the majority of the state of Missouri. Because of this, the three  
94 aforementioned radars were used to assess overall performance in estimating precipitation for this study.  
95 Each radar covered a 200-km radius for which a different number of gauges were within the domain:  
96 KLSX, KEAX, and KSGF covered 9, 8, and 5 gauges, respectively (Figure 1).

97 Missouri is characterized as a continental type of climate, marked by relatively strong seasonality.  
98 Furthermore, Missouri is subject to frequent changes in temperature, primarily due to its inland location  
99 and its lack of proximity to any large lakes. All of Missouri experiences below-freezing temperatures on a



100 yearly-basis. For example, the majority of the state experiences, on average, 110 days with temperatures  
101 below freezing, while the Bootheel (i.e., southeast region) registers, on average, 70 days of below  
102 freezing days. This elaborates upon the typical northwest to southeast warming pattern of temperatures  
103 observed in the state. Because of the large variability in temperature, the warm and cool seasons were  
104 defined from an agronomic perspective, primarily taking probabilities of freezing into account. Based on  
105 the climatological averages of Missouri, from 1983 to 2013, November through April registered average  
106 minimum temperatures below freezing, and was considered the cool season, while May through  
107 October's minimum average temperature were above freezing and constituted the warm season.

## 108 **2.2 Rainfall data**

109 Terrestrial-based (ground-truthed) precipitation gauge data were collected from 15 separate  
110 weather stations within the Missouri Mesonet, established by the Commercial Agriculture Program of  
111 University Extension (Table 1). All precipitation data were recorded in hourly intervals which, ultimately,  
112 were aggregated to daily totals from 0 to 0 CST for each day used in the study. Forty-six days for the year  
113 of 2014 were analyzed for a total of 1,104 hours for each radar which converts to, approximately, 33,000  
114 radar scans in all. The days were chosen based on availability of data from the National Climate Data  
115 Center's (NCDC) Hierarchical Data Storage System (HDSS) for all three radars, in addition to error-free  
116 performance notes from each of the gauges used. The dates analyzed were split near evenly between  
117 warm (May – October) and cool (November – April), therefore encompassing an overall performance of  
118 each of the radars throughout the year with no preferential bias towards rain or snow. Additionally, days  
119 were distributed evenly during the summer between convective and stratiform events with a threshold of  
120 38 dBZ (Gamache and Houze, 1982).

121 Observed precipitation data were collected using Campbell Scientific TE525 tipping buckets  
122 located at each of the locations for the study (Table 1). The precipitation gauges have a 15.4-cm orifice  
123 which funnels to a fulcrum which registers 0.01 mm of rainfall per tip. The performance of each gauge is



124 maximized between 0 and 50°C, for which each day of the study's temperature did not exceed. Accuracy  
125 in gauge measurements range between -1 to 1%, -3 to 0%, and -5 to 0% for precipitation up to 25.4 mm h<sup>-1</sup>,  
126 25.4 to 50.8 mm h<sup>-1</sup>, and 50.8 to 76.2 mm h<sup>-1</sup>, respectively, which are, primarily, associated with local  
127 random errors and errors in tip-counting schemes (Kitchen and Blackall, 1992; Habib et al., 2001). Each  
128 tipping bucket is located, approximately, 1 m above the ground in areas clear of buildings and properly  
129 maintained vegetation height to mitigate turbulence effects (Habib et al., 1999). These errors were  
130 assumed negligible and, therefore, allowed for the gauges to be representative of the true rainfall rate.

### 131 **2.3 Radar data and radar-rainfall algorithms**

132 Next Generation Radar (NEXRAD) level-II data were retrieved from the NCDC's HDSS. Files  
133 were analyzed using the Weather Decision Support System – Integrated Information (WDSS-II) program  
134 (Lakshmanan et al., 2007) to assess reflectivity (Z) in addition to dual-polarized radar variables including  
135 differential reflectivity (ZDR) and specific differential phase shift (KDP). Three other variables were also  
136 generated based on a KDP-based smoothing field (Ryzhkov et al., 2003) for reflectivity, differential  
137 reflectivity, and specific differential phase: DSMZ, DZDR, and DKDP, respectively. A rain rate echo  
138 classification variable (RREC) was also computed, which chooses whether an R(Z), R(KDP), R(Z,ZDR),  
139 or R(ZDR, KDP) algorithm is implemented in estimating rain rates based on the radar fields of Z, ZDR,  
140 and KDP (Kessinger et al., 2003).

141 All seven variables (Z, ZDR, KDP, DSMZ, DZDR, DKDP, and RREC) were converted from  
142 their native polar grid to 256 x 256 1-km Cartesian grids, where the lowest radar elevation scans (0.5°)  
143 were used to mitigate uncalculated effects from evaporation and wind drift. An average of 5-minute scans  
144 were used for each of the variables, which were aggregated to hourly totals to be compared to the hourly  
145 tipping-bucket accumulations. The latitude and longitude of each of the 15 gauges were matched with the  
146 radar pixel that corresponds to the Cartesian grid such that each quantitative value of the seven radar  
147 variables were able to be extracted and used in rain rate calculations. Post-processing `_rain-rate`



148 calculations were conducted using the equations presented by Ryzhkov et al. (2005) (Table 2), which  
149 were gathered from multiple studies using disdrometers to derive a relationship between reflectivity,  
150 differential reflectivity, and specific differential phase (Bringi and Chandrasekar, 2001; Brandes et al.,  
151 2002; Illingworth and Blackman, 2002; Ryzhkov et al., 2003). Standard R(Z) algorithms were also  
152 included to test whether the addition of dual-polarized technology to rainfall estimates produced  
153 improvement.

154 With the use of both Z, ZDR, KDP, and DSMZ, DZDR, and DKDP fields produced by WDSS-II,  
155 the number of algorithms tested was 55. This includes the three standard single-polarized algorithms  
156 (stratiform, convective, and tropical) which were calculated using reflectivity R(Z), and then calculated as  
157 R(DSMZ), while algorithms 1-6 (R(KDP)) were also calculated as R(DKDP). Algorithms 7-11 (R(Z,  
158 ZDR)) were additionally calculated as R(Z, DZDR), R(DSMZ, ZDR), and R(DSMZ, DZDR), while the  
159 same four combinations of non- and KDP-smoothed fields were applied to the R(KDP, ZDR) algorithms  
160 (12-15).

## 161 2.4 Statistical analyses

162 To test the performance of each algorithm, several statistical analyses were calculated. The  
163 average difference (Bias) was calculated as

$$164 \text{ Bias} = \frac{\sum (R_i - G_i)}{N} \quad (1)$$

165 where  $R_i$  is each hourly aggregated radar estimated rainfall amount calculated from one of the 55  
166 algorithms,  $G_i$  is the hourly aggregated gauge (observed) measurement, and  $N$  is the total number of  
167 observations which, for this study, was 1,104 hours. A second statistical parameter, the normalized mean  
168 bias (NMB), was calculated as



$$169 \quad NMB = \frac{1}{N} \frac{\sum (R_i - G_i)}{\sum G_i} \quad (2)$$

170 The normalized mean bias is included in the analyses due to the fact that overestimations (i.e., radar  
171 estimates larger than gauge measurements) and underestimations (i.e., radar estimates smaller than gauge  
172 measurements) are treated proportionately. This is directly analogous to choosing the mean absolute error  
173 (MAE) opposed to the standard deviation as the MAE does not penalize smaller or larger errors,  
174 obscuring the overall results (Chai and Draxler, 2014). Bias measurements (Bias and NMB) were  
175 calculated to determine whether radar derived rain rates were over- or under-estimated in comparison to  
176 the gauges. However, to calculate the overall magnitude of error associated with the performance of the  
177 radars, the absolute values of (1) and (2) were performed to yield the mean absolute error (MAE), and  
178 normalized standard error (NSE), respectively.

179 Several other meteorological parameters were calculated, including probability of detection  
180 (PoD) which was calculated as

$$181 \quad PoD = \frac{\sum |R_i \bullet G_i > 0 \& R_i > 0|}{\sum |G_i|} \quad (3)$$

182 where the bullet ( $\bullet$ ) indicates "if", to determine how accurate the radars were at correctly detecting  
183 precipitation. The probability of detection values range between 0.0 (radar did not detect any precipitation  
184 correctly) and 1.0 (radar detected the occurrence of all precipitation 100% correctly). The probability of  
185 false detection takes into account the amount of precipitation the radars incorrectly estimated when the  
186 gauges recorded zero values, and was calculated as

$$187 \quad PoFD = \frac{\sum R_i \bullet (G_i = 0 \& R_i > 0)}{\sum G_i} \quad (4)$$

188 Conversely, the missed precipitation amount (MPA) is the opposite of the PoFD, such that





189 
$$MPA = \sum R_i \bullet (G_i > 0 \ \& \ R_i = 0) \tag{5}$$

190 Equations 3, 4, and 5 are scaled by the amount of precipitation measured by the gauges. The total amount  
191 of rainfall missed and falsely detected (i.e., numerator) of (3), (4), and (5) were also quantified and  
192 reported.

193

### 194 **3 Results and discussion**

#### 195 **3.1 Individual radar performance: All data**

196 To test the overall performance of each radar, it was necessary to determine the overall best  
197 algorithm for each statistical measure. Furthermore, the algorithm that performed the best and worst for  
198 each gauge and for each radar was assessed.

199

##### 200 **3.1.1 KEAX**

201 The overall bias showed that there was a positive bias, peaking near  $5.5 \text{ mm hr}^{-1}$  at the second  
202 gauge for KEAX, approximately 115 km from the radar for both the best and worst performing  
203 algorithms (Figure 2). This could correspond to a bright-band signature which caused overestimation in  
204 precipitation from the algorithms. The overall worst algorithm, equation 13, an R(ZDR,KDP)  
205 relationship, revealed a decreasing trend in bias as the distance from the radar increased. This could be  
206 due, at least in part, to the algorithm's utilization of KDP which performs poorly in frozen precipitation  
207 (Zrnicek and Ryzhkov, 1996), causing the underestimation. Conversely, the algorithm with the lowest bias  
208 was an R(Z,ZDR) algorithm (equation 11). There was a maximum in the bias calculations while utilizing  
209 equation 11 near 120 km, similar to equation 13, however, there was a more pronounced minimum in the  
210 data near 150 km. Furthermore, it appears the data oscillates around a bias value of  $0 \text{ mm hr}^{-1}$  when using



211 equation 13. This could be due to ZDR's capability to respond to precipitation shape (Kumjian 2013a, b),  
212 which helps to scale the reflectivity portion of the rainfall estimation algorithm to a more accurate value.  
213 The normalized mean bias (NMB) reveals the same trend in values for bias but with a decrease in  
214 magnitude. It is important to note, however, that the algorithms that tend to perform the worst (e.g.,  
215 algorithms containing KDP) result in anomalous range responses which would be due, at least in part, to a  
216 stronger response to precipitation type.

217 The absolute bias and normalized standard error (NSE) shows the same maxima in the data at the  
218 second gauge (Brunswick) that was present in the bias data. However, a second maxima is located at the  
219 fifth gauge at, approximately, 150 km (Linneus), which could be a second bright-band present in the  
220 summer data, whereas the first maxima is a bright-band in the winter data. There was also a more  
221 pronounced minimum in the NSE results at the fourth gauge, indicating the effects of stratiform as  
222 opposed to convective precipitation.

223 The probability of detection (PoD) results show a large difference in algorithm choice for  
224 correctly detecting precipitation. The KDP-smoothed R(Z) convective algorithm, R(DSMZ) convective,  
225 performed the best in terms of correctly detecting precipitation, whereas algorithm 1 (KDP1) performed  
226 the worst, despite its advantages at large ranges (Zrníc and Ryzhkov, 1996). The increased PoD at the  
227 second gauge indicates the definite presence of a bright-band, while the low PoD at, approximately 150  
228 km, indicates overshooting of the beam. This is further aided by the MPA results, as about 225 mm of  
229 precipitation was missed by the radar at 150 km, whereas only 100 mm of precipitation was missed by the  
230 radar at the second gauge at 120 km. Although equation 11, an R(Z,ZDR) algorithm was superior in terms  
231 of the bias, the same algorithm with a KDP-smoothed reflectivity value, R(DSMZ,ZDR) revealed the  
232 overall least amount of falsely missed precipitation. However, the summation of the amount of  
233 precipitation falsely detected (PoFD) by KEAX showed a larger source of error than the MPA in terms of



234 magnitude. For example, at the second (fifth) gauge, only 100 (225) mm of precipitation was missed by  
235 the radar, but over 700 (725) mm of precipitation was incorrectly estimated by the radar.

236

### 237 **3.1.2 KLSX**

238 Unlike the KEAX data, the gauges used for analyses for the KLSX radar span between 90 – 150  
239 km. Furthermore, 5 out of the 8 gauges were located within 10 km of range from one-another, near 140  
240 km from the radar, limiting the data available for analyses between 100 and 140 km (Figure 3).

241 The bias and NMB show a relatively modest peak in values near the second gauge of 5 mm hr<sup>-1</sup>,  
242 which decreases to approximately 3.6 mm hr<sup>-1</sup> at the third gauge, 120 km from the radar. The worst  
243 performing algorithm, equation 13, was the same R(ZDR,KDP) relation as the worst KEAX bias and  
244 NMB data. Additionally, the overall trend of decreasing bias and NMB as distance from the radar  
245 increases was noted, presumably due to overshooting effects similar to the KEAX data. Furthermore, the  
246 overall negative bias displayed by the best-performing algorithm, equation 11, was similar to the KEAX  
247 data as well.

248 The double maxima in the absolute bias graph are present as with the KEAX data, but are not as  
249 pronounced. Additionally, the overall minima in the absolute bias for both KEAX and KLSX are at,  
250 approximately, 125 km from the radar. However, the relative distance from the radars are the same, where  
251 the two maxima for KEAX were at 115 and 150 km, while the maxima were at, approximately, 100 and  
252 140 km. The overall best and worst performing algorithms for the absolute bias and NSE were equations  
253 11 and 13, the R(Z,ZDR) and R(ZDR,KDP) algorithms, respectively.

254 One of the main differences between the KLSX and KEAX data was the decreased probability of  
255 detection at 120 km for KLSX, while there was an increased probability of detection for KEAX. In  
256 general, the PoD values were worse for KLSX when compared to KEAX. There was also a trend of



257 increasing PoD values as distance from the St. Louis radar increased and, at one point near 140 km, the  
258 best algorithm, R(DSMZ) convective and the worst algorithm, KDP1, were not significantly different  
259 (10% difference in detection). Additionally, the maxima in the PoD while utilizing KDP1 corresponds to  
260 a minima in the R(DSMZ) detection percentage, which is well correlated by the similarly valued MPA  
261 results.

262 Another difference between the KEAX and KLSX data was the overall decrease in the PoFD as  
263 distance from the radar increased. Because of this, the maxima in the amount of falsely identified  
264 precipitation is only 100 km from the radar, which may be effects from bright-banding. Furthermore, this  
265 resulted in the overall error in precipitation for algorithm 13 to be in excess of 1,500 mm, while algorithm  
266 11 did not exceed 500 mm for the 1,104-hour dataset for KLSX.

267

### 268 **3.1.3 KSGF**

269 Although the KLSX and KEAX data strongly suggests bright-banding signatures near  
270 approximately 100 km and 150 km from the radar, the KSGF results reveal an overall increase of error  
271 with range (Figure 4). One of the main reasons for this could be due to the fact that the gauge furthest  
272 from any radar analyzed is Cook Station, 185 km from KSGF, which is the range where Ryzhkov et al.  
273 (2003, 2005) reported significant fallout in radar performance in rainfall estimation.

274 Overall, the absolute bias values for KLSX, KEAX, and KSGF were within  $\pm 2$  from 6 mm hr<sup>-1</sup>  
275 for the worst performing algorithm, equation 13. However, the radar at Springfield, MO revealed the  
276 maximum absolute bias was the furthest gauge at, approximately, 185 km (Cook Station). Although a  
277 slight bright-band effect is evident at the second gauge, 100 km from KSGF, the first bright-band is not as  
278 evident when compared to the KEAX and KLSX data. However, the overshooting of the beam is more  
279 pronounced between 140- and 160-km from KSGF. For example, there is a sharp decrease in the  
280 probability of detection within this range, correlating with a decrease in the bias and NMB. Furthermore,



281 there is an increase in the magnitude of the FAR, indicating a large portion of precipitation was no  
282 captured by the radar beam.

283

### 284 **3.2 Individual radar performance: Seasonal data**

285 In order to achieve a better understanding of the minimum and maximum values portrayed by the  
286 data, all of the radar scans and gauge data were divided into summer (May – October) and winter  
287 (November – April) months based on the average climatology of Missouri. This resulted in 652 hours of  
288 data for summer, and 452 hours for winter (59 and 41% of the entire data, respectively). Because of this,  
289 the overall error is more weighted towards the summer data than the winter data.

290 The Kansas City bias and absolute bias summer data (Figure 5) shows a similarity to the overall  
291 data (Figure 2) in terms of both trend and magnitude. Also, the best performing algorithm for the  
292 probability of detection (equation 11) was the same for the summer and overall data. However, the R(Z)  
293 Tropical algorithm showed the least reliability in correctly detecting precipitation for the summer,  
294 resulting in a more pronounced decrease in the PoD percentage overall. For the NMB and NSE data, the  
295 same algorithms that performed best and worse for the overall data (equations 11 and 13) were the best  
296 and worst for summer, respectively, and showed similar magnitudes and trends. Conversely, the winter  
297 data (Figure 6) showed a pronounced overestimation in the NMB and NSE at the third gauge (125 km)  
298 from the radar, with values exceeding 30 mm hr<sup>-1</sup> compared to values below 6 mm hr<sup>-1</sup> for the combined  
299 seasonal data. This could be due, at least in part, to the large amount of precipitation overestimated by the  
300 radar relative to the total amount of precipitation. For example, winter precipitation amounts are  
301 significantly lower than convective summertime amounts and, thus, result in a small denominator in (2),  
302 leading to an increase in bias. These trends in the KEAX higher NMB and NSE values can be observed  
303 for the KLSX and KSGF data as well (Figures 7 and 8, respectively). However, the magnitudes of NMB  
304 and NSE were smaller for KSGF in comparison to KLSX and KEAX.



305           Summing the amount of precipitation not recorded by the radar but recorded by the gauge (MPA)  
306 showed similar results when compared between summer and the overall data, but also revealed little  
307 contribution of the overall amount from the winter data. Additionally, the best and worst algorithms for  
308 the MPA (equations 10 and 14, respectively) were not significantly different ( $p = 0.05$ ). Furthermore, the  
309 relatively small contribution from the winter data to the amount of precipitation not estimated by the  
310 gauge but estimated by the radar (30 and 40 mm for KLSX and KSGF, respectively) was similar to the  
311 KEAX data. The contributions of winter MPA to the overall MPA for all three radars were,  
312 approximately, 20%. Conversely, the total amount of precipitation recorded by the radar but not recorded  
313 by the gauge (PoFD) showed a relatively large portion from the winter data as opposed to the summer  
314 data, with the noticeable exception of the bright-banding effects at the second and fifth gauges (120 and  
315 150 km, respectively) for KEAX. Overall, the winter contribution to the overall PoFD was about 50%.

316           Overall, the summation of all errors from the radar, including MPA, PoFD, and the absolute bias  
317 reveals that, approximately, 20-30% of the error was due to the winter data while comprising 41% of the  
318 entire dataset for all three radars. Conversely, the bulk of the error (80%) was due to the 59% total  
319 summer results, primarily due to the overall larger magnitudes in rainfall from convective storms. This is  
320 further exemplified via Figure 9, showing a scatterplot of all gauge versus radar comparisons. With the  
321 exception of a few data points for KEAX, seldom does the winter radar estimated precipitation exceed 10  
322  $\text{mm hr}^{-1}$ , while no gauge recorded precipitation exceeded 10  $\text{mm hr}^{-1}$ . It is interesting to note that, with the  
323 exception of the KLSX data, the winter correlation coefficient values exceed the summer. This could be  
324 due, at least in part, to local random errors (Ciach and Krajewski, 1999a) and the excessive (i.e.,  
325 convective) rainfall that the tipping buckets are unable to accurately measure (Ciach and Krajewski,  
326 1999b; Ciach 2002). Furthermore, because the magnitude of precipitation in the winter is less than the  
327 summer, smaller variance and absolute error values are common, causing the correlation coefficient  
328 values to be larger than the frequent summertime showers where precipitation values can range from 0  
329  $\text{mm hr}^{-1}$  to, in extreme cases, 100  $\text{mm hr}^{-1}$ .



330

331 **3.3 Radar performance: Hits only**

332 From the results presented thus far, the majority of the error has resulted from either the PoFD or  
333 MPA. Therefore, an analysis into how accurate each algorithm was in comparison to a one-to-one ratio  
334 for a correct hit (i.e., gauge and radar recorded precipitation) is presented. This will, in turn, determine  
335 whether algorithm 11, an R(Z,ZDR) equation, is still most accurate and whether algorithm 13, an  
336 R(ZDR,KDP) equation, is least accurate.

337 From the 55 algorithms possible, the first gauge from each of the three radars (Greenridge,  
338 Williamsburg, and Lamar for KEAX, KLSX, and KSGF, respectively), all within 100 km from the radar,  
339 showed that either an R(Z) or R(DSMZ) convective algorithm was most accurate with correlation  
340 coefficient values around 0.70 (Figures 10-12). Additionally, the second gauge from KEAX (Brunswick)  
341 also revealed that an R(Z) convective  $R^2$  value was superior to all other algorithms. For the intermediate  
342 gauges from each radar, the rain rate echo classification (RREC) algorithm had the highest correlation  
343 coefficient value. For example, for KEAX, St. Joseph (115 km) and Versailles (129 km) had some of the  
344 highest  $R^2$  values of 0.62 and 0.88, respectively. For KLSX, the fourth gauge (Bradford, at 135 km from  
345 the radar), the RREC correlation coefficient value was 0.55. Beyond, approximately, 140 km from the  
346 radar, the KDP3 equation was superior. In fact, the furthest two gauges from each radar showed KDP3  $R^2$   
347 values exceeding 0.40. This could be due, at least in part, to the fact that the specific differential phase  
348 does not degrade quality with range, resulting in more accurate results at larger distances (Zrnich and  
349 Ryzhkov, 1999; Ryzhkov et al., 2003).

350 For the vast majority of scenarios, DZDRDKDP2 or the R(Z) Tropical algorithms were the worst  
351 performing equations. Because the R(Z) Tropical equation was designed for maritime precipitation while  
352 this study was conducted in the Midwest, it was not surprising that it was one of the poorest performing  
353 algorithms. From the scatterplots of gauge versus radar precipitation (Figures 10-12), when the R(Z)



354 Tropical equation was the worst correlation correlation-valued algorithm, there was, generally,  
355 underestimation of precipitation estimated by the radar. Conversely, for the DZDRDKDP algorithm,  
356 overestimation of radar estimated precipitation was observed. This could be due to over-smoothing of the  
357 ZDR and KDP fields, causing overestimation in rain estimates (Simpson et al., 2016).

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#### 361 **4 Conclusions**

362 Dual-polarization technology was implemented to the National Weather Service Next Generation  
363 Radar network in the Spring of 2012 to, primarily, improve precipitation estimation and hydrometeor  
364 classification. Since this time, a number of studies have been conducted to determine whether this  
365 upgrade has improved radar performance in a meteorological, and hydrometeorological sense. Many  
366 studies have observed an improvement of radar-based precipitation estimation compared to terrestrial-  
367 based precipitation monitors (e.g., Ryzhkov et al., 2003, 2005; Simpson et al., 2016), while other studies  
368 show ambiguity between whether there is improvement (e.g., Gourley et al., 2010; Cunha et al., 2015).  
369 This study observed over 1,100 hours of precipitation data with three separate radars in Missouri using 55  
370 algorithms including the three conventional R(Z) radar rain-rate estimation algorithms (stratiform,  
371 convective, and tropical) along with a myriad of R(KDP), R(Z,ZDR), and R(ZDR,KDP) algorithms  
372 which can be found in Ryzhkov et al. (2005). Additionally, a KDP-smoothing field of reflectivity,  
373 differential reflectivity, and the specific differential phase shift (DSMZ, DZDR, and DKDP, respectively)  
374 were measured and used for analyses. Unlike previous studies, the current work emphasizes the amount  
375 of precipitation correctly and incorrectly estimated by the radar in comparison to the terrestrial based  
376 precipitation gauges through measurements of the probability of detection, probability of false detection,  
377 and missed precipitation amount.





378 For all three radars, Kansas City, St. Louis, and Springfield, MO (KEAX, KLSX, and KSGF,  
379 respectively), the vast majority of precipitation error (over 60%) was contributed by the amount of  
380 precipitation falsely detection by the radar (up to 725 mm), while 20% was due to the radar missing the  
381 precipitation (up to 225 mm) for KEAX. Similar magnitudes of error were reported for KLSX and KSGF,  
382 with an overall error in precipitation for each radar ranging between 250 mm for the best performing of  
383 the 55 algorithms, equation 11 (an R(Z,ZDR) algorithm), and up to 2000 mm for the worst performing  
384 algorithms, R(ZDR,KDP) equation 13.

385 Radar performance in different seasons has been shown to be significantly different, therefore,  
386 the data was divided into summer (May – October) and winter (November – April) months resulting in  
387 652 hours for summer, and 452 hours for winter (59 and 41% of the entire data, respectively). Despite the  
388 winter data contributing less than the summertime data, it accounted for 20% of the overall MPA, and  
389 40% to the overall PoFD. The best and worst performing algorithms were the same for the summer and  
390 winter data as the overall data, R(Z,ZDR) equation 11 and R(ZDR,KDP) equation 13, respectively.

391 The overall data was further subdivided into correct radar hits (radar correctly estimated  
392 precipitation to be present while the terrestrial based gauge recorded precipitation) for the 1,100-hour  
393 dataset. It was found that within 100 km from each of the three radars, the R(Z) or R(DSMZ) convective  
394 algorithm revealed the best correlation coefficient values of, approximately, 0.70. Further from the radar,  
395 beyond 135 km, RKDP3 generally performed the best due to the algorithms non-degrading capabilities  
396 and immunity to beam blockage, whereas at intermediate distances (between 100 and 135 km from the  
397 radars), the rain rate echo classification algorithm performed the best. Overall, the worst performing  
398 equations were either the R(Z) tropical, or DZDRDKDP2.

399 These results help our understanding in the possibilities for hydrometeorological studies.  
400 Although a mixture of R(Z) convective and R(KDP) algorithms performed the best when precipitation  
401 was correctly estimated by the radar, nearly 50% of the 1,100 hours analyzed for the study consisted of



402 either falsely estimated precipitation by the radar, or missed by the radar. Furthermore, these errors  
403 accumulate between 500 to 2,000 mm of precipitation depending on the algorithms chosen. Because of  
404 this, a significant source of error and uncertainty must be overcome before radar data can be fully  
405 implemented into hydrologic models, especially on a continuous, operational basis.

406

407 **Author Contribution.** N. Fox designed the experiment and provided feedback while M. Simpson carried  
408 out the calculations and wrote the manuscript.

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413

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518 Table 1. Terrestrial-based precipitation gauge locations used for the study in addition to the National  
519 Weather Service Radars Springfield, MO (KSGF), Kansas City, MO (KEAX), and St. Louis, MO  
520 (KLSX) used in conjunction with each gauge.

| Gauge Location | Latitude (°N) | Longitude (°W) | Radar(s) Used |
|----------------|---------------|----------------|---------------|
| Bradford       | 38.897236     | -92.218070     | KLSX, KEAX    |
| Brunswick      | 39.412667     | -93.196500     | KEAX          |
| Capen Park     | 38.929237     | -92.321297     | KLSX, KEAX    |
| Cook Station   | 37.797945     | -91.429645     | KLSX, KSGF    |
| Green Ridge    | 38.621147     | -93.416652     | KEAX, KSGF    |
| Jefferson Farm | 38.906992     | -92.269976     | KLSX, KEAX    |
| Lamar          | 37.493366     | -94.318185     | KSGF          |



|                |           |            |            |
|----------------|-----------|------------|------------|
| Linneus        | 39.856919 | -93.149726 | KEAX       |
| Monroe City    | 39.635314 | -91.725370 | KLSX       |
| Mountain Grove | 37.153865 | -92.268831 | KSGF       |
| Sanborn Field  | 38.942301 | -92.320395 | KLSX, KEAX |
| St. Joseph     | 39.757821 | -94.794567 | KEAX       |
| Vandalia       | 39.302300 | -91.513000 | KLSX       |
| Versailles     | 38.434700 | -92.853733 | KEAX, KSGF |
| Williamsburg   | 38.907350 | -91.734210 | KLSX       |

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526 Table 2. List of single- and dual-polarimetric algorithms used for radar rainfall estimates.

| $R(Z) = aZ^b$                         |      |      |   |
|---------------------------------------|------|------|---|
| Precipitation type                    | a    | b    | c |
| Stratiform                            | 200  | 1.6  | - |
| Convective                            | 300  | 1.4  | - |
| Tropical                              | 250  | 1.2  | - |
| $R(KDP) = a  KDP ^b \text{sign}(KDP)$ |      |      |   |
| Algorithm number                      |      |      |   |
| 1                                     | 50.7 | 0.85 | - |





|  |                       |       |       |
|--|-----------------------|-------|-------|
| 2  | 54.3                  | 0.81  | -     |
| 3  | 51.6                  | 0.71  | -     |
| 4  | 44.0                  | 0.82  | -     |
| 5  | 50.3                  | 0.81  | -     |
| 6  | 47.3                  | 0.79  | -     |
| <hr/>  |                       |       |       |
| $R(Z, ZDR) = aZ^b ZDR^c$                         |                       |       |       |
| <hr/>  |                       |       |       |
| Algorithm number                                 |                       |       |       |
| 7  | $6.70 \times 10^{-3}$ | 0.927 | -3.43 |
| 8  | $7.46 \times 10^{-3}$ | 0.945 | -4.76 |
| 9  | $1.42 \times 10^{-2}$ | 0.770 | -1.67 |
| 10   | $1.59 \times 10^{-2}$ | 0.737 | -1.03 |
| 11   | $1.44 \times 10^{-2}$ | 0.761 | -1.51 |
| <hr/>  |                       |       |       |
| $R(ZDR, KDP) = a  KDP ^b ZDR^c \text{sign}(KDP)$ |                       |       |       |
| <hr/>  |                       |       |       |
| Algorithm number                                 |                       |       |       |
| 12   | 90.8                  | 0.930 | -1.69 |
| 13   | 136                   | 0.968 | -2.86 |
| 14   | 52.9                  | 0.852 | -0.53 |
| 15   | 63.3                  | 0.851 | -0.72 |

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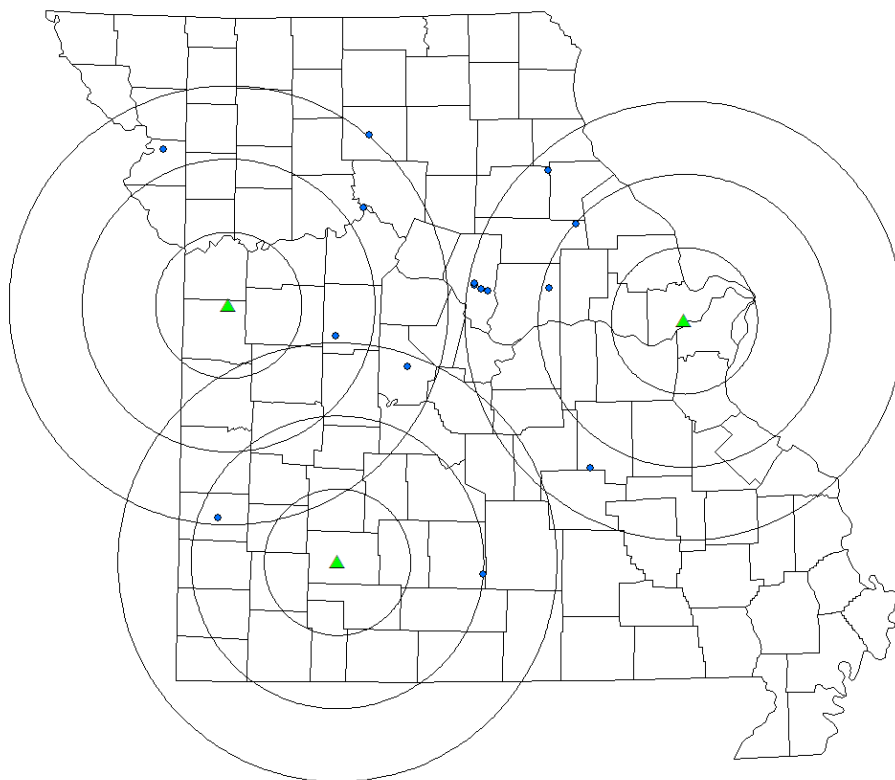
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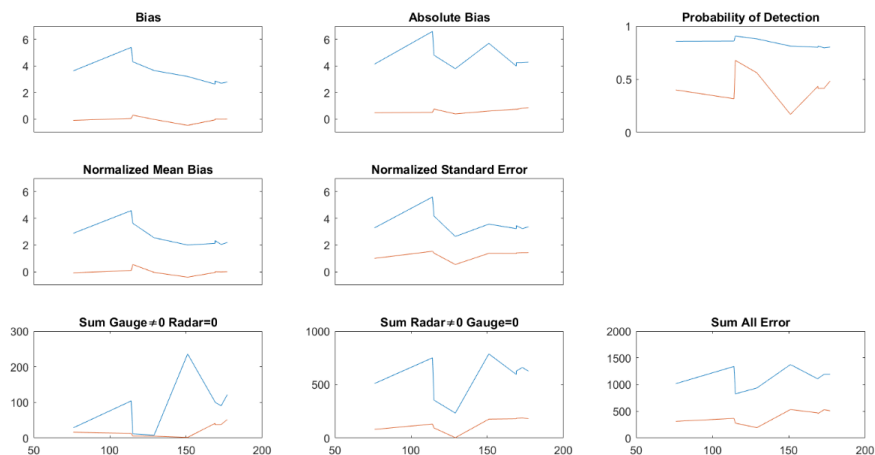
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544 **Figures**



545

546 Figure 1. Study location (Missouri) with St. Louis (KLSX), Kansas City (KEAX), and Springfield  
547 (KSGF), MO radars (triangles) overlaid with 50-, 100-, and 150-km range rings in addition to the 15  
548 terrestrial-based precipitation gauges utilized as ground-truthed data.



549

550 Figure 2. Overall statistical analyses for the nine gauges used for Kansas City, MO. The blue line  
551 represents the weakest performing rain rate estimation algorithm, while the red line represents the overall  
552 best performing algorithm for all graphs, with the exception of the probability of detection. All units are  
553 in  $\text{mm hr}^{-1}$  with the exclusion of the probability of detection (unitless).

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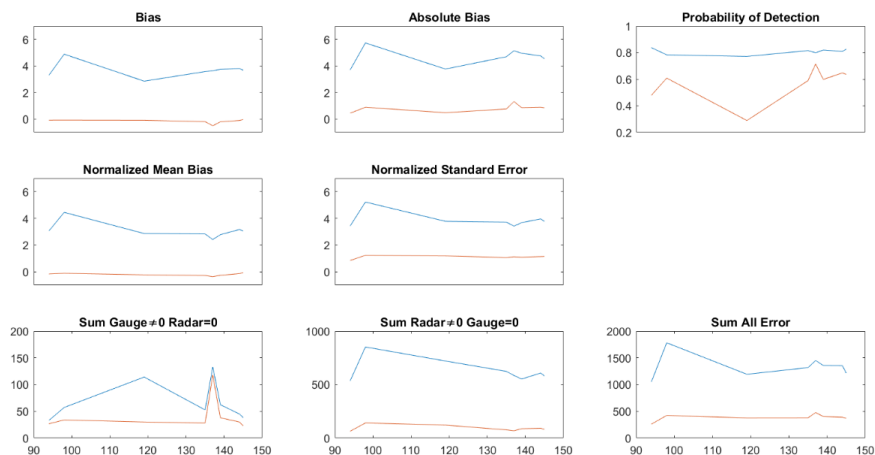
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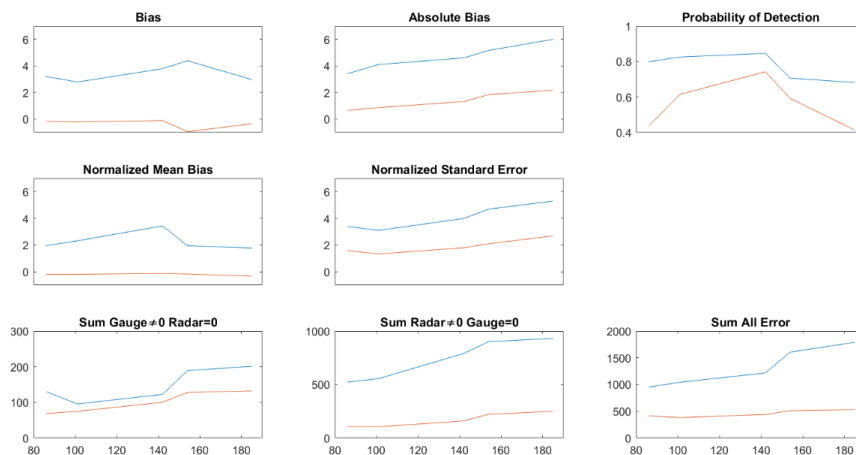
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561 Figure 3. Overall statistical analyses for the nine gauges used for St. Louis, MO. The blue line represents  
562 the weakest performing rain rate estimation algorithm, while the red line represents the overall best  
563 performing algorithm for all graphs, with the exception of the probability of detection. All units are in  
564  $\text{mm hr}^{-1}$  with the exclusion of the probability of detection (unitless).

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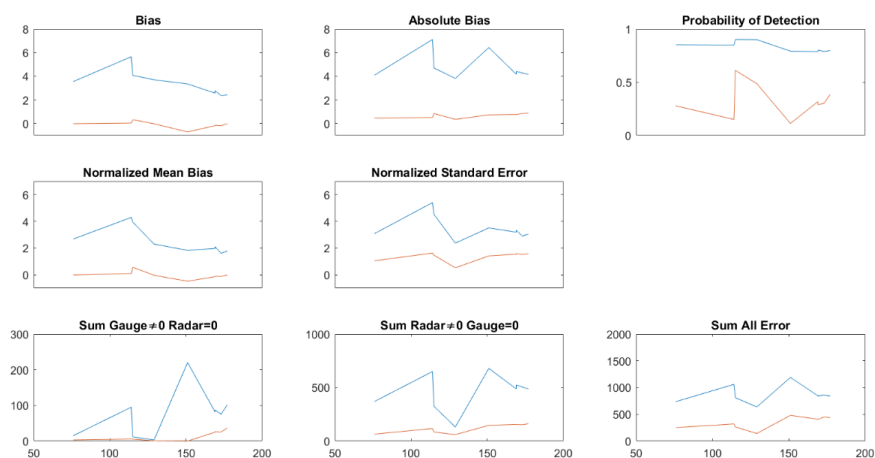
569 Figure 4. Overall statistical analyses for the nine gauges used for Springfield, MO. The blue line  
570 represents the weakest performing rain rate estimation algorithm, while the red line represents the overall  
571 best performing algorithm for all graphs, with the exception of the probability of detection. All units are  
572 in  $\text{mm hr}^{-1}$  with the exclusion of the probability of detection (unitless).

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578 Figure 5. Statistical analyses for the nine gauges used for Kansas City, MO for warm season data, only.

579 The blue line represents the weakest performing rain rate estimation algorithm, while the red line

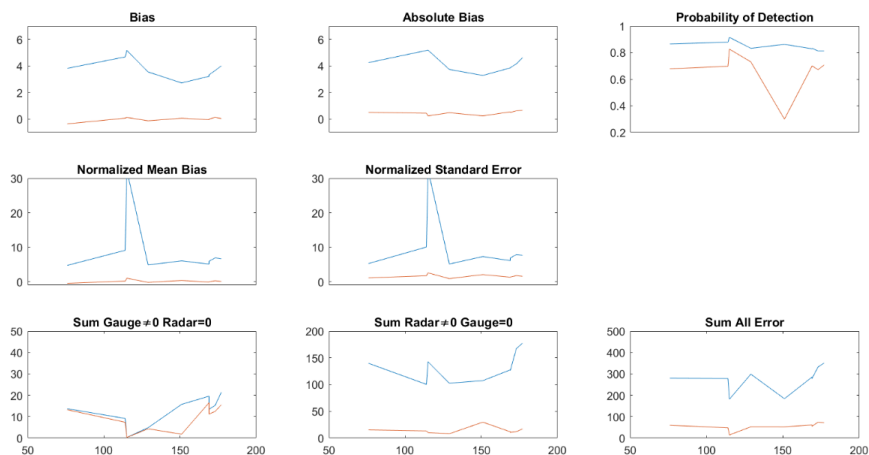
580 represents the overall best performing algorithm for all graphs, with the exception of the probability of

581 detection. All units are in  $\text{mm hr}^{-1}$  with the exclusion of the probability of detection (unitless).

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586 Figure 6. Statistical analyses for the nine gauges used for Kansas City, MO for cool season analyses, only.

587 The blue line represents the weakest performing rain rate estimation algorithm, while the red line

588 represents the overall best performing algorithm for all graphs, with the exception of the probability of

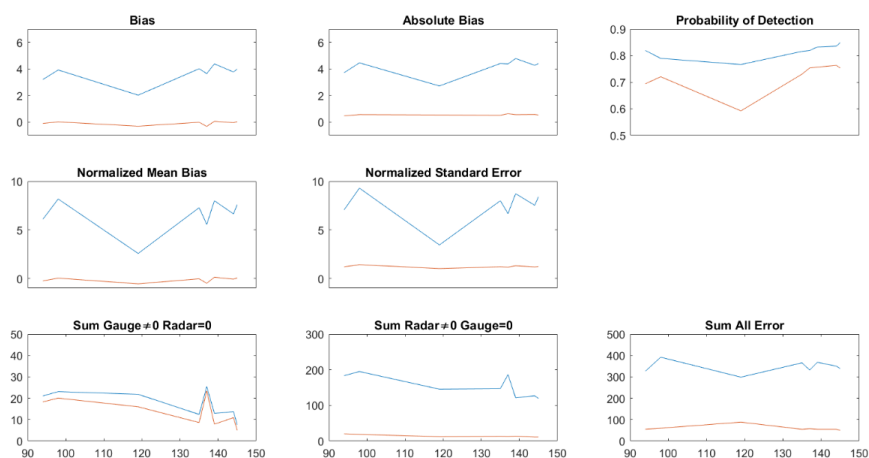
589 detection. All units are in  $\text{mm hr}^{-1}$  with the exclusion of the probability of detection (unitless).

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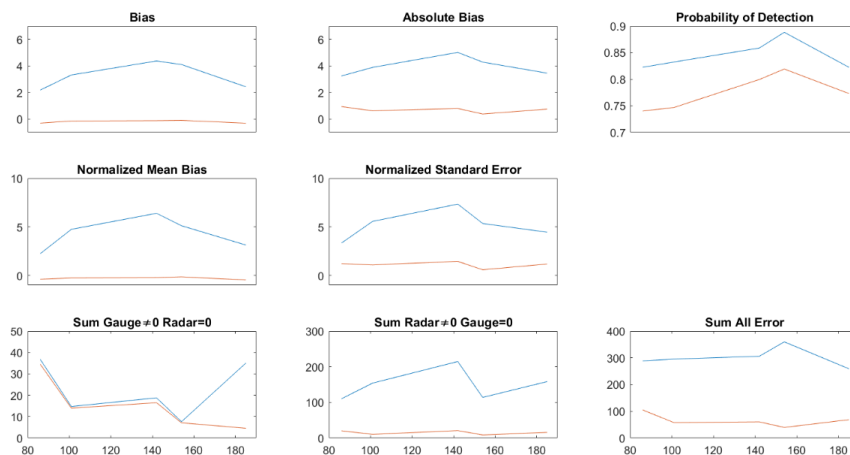


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594 Figure 7. statistical analyses for the nine gauges used for St. Louis, MO for cool season analyses,  
595 only. The blue line represents the weakest performing rain rate estimation algorithm, while the red  
596 line represents the overall best performing algorithm for all graphs, with the exception of the  
597 probability of detection. All units are in  $\text{mm hr}^{-1}$  with the exclusion of the probability of detection  
598 (unitless).

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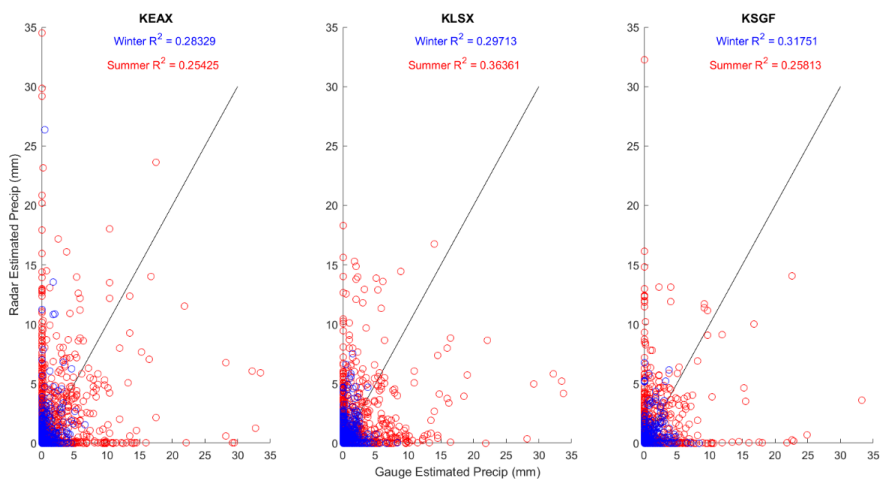
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602 Figure 8. Statistical analyses for the nine gauges used for Springfield, MO for cool season analyses,  
603 only. The blue line represents the weakest performing rain rate estimation algorithm, while the red  
604 line represents the overall best performing algorithm for all graphs, with the exception of the  
605 probability of detection. All units are in  $\text{mm hr}^{-1}$  with the exclusion of the probability of detection  
606 (unitless).

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611 Figure 9. Scatterplot of gauge estimation precipitation versus radar estimated precipitation with their  
612 respective correlation coefficient values for warm and cool seasons.

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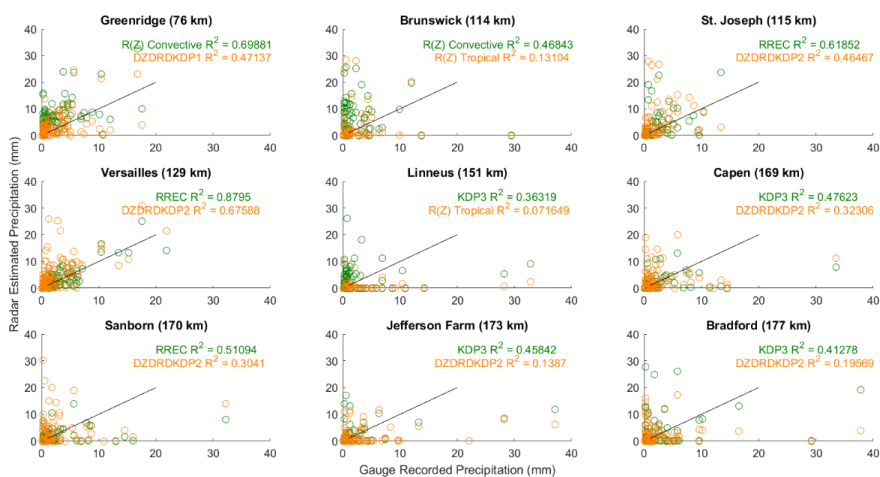
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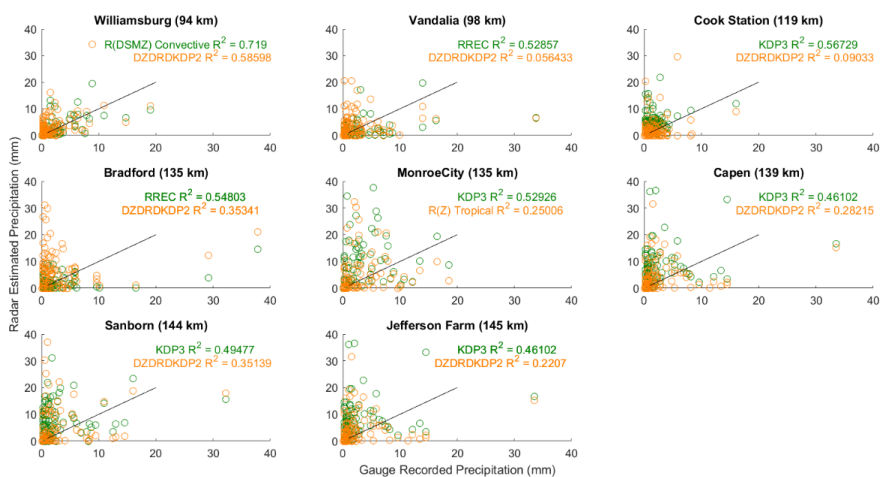
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620 Figure 10. Scatterplots of the best (green) and worst (orange) performing radar rain rate estimation  
621 algorithms at each terrestrial based gauge location. Distance from the Kansas City (KEAX) radar is  
622 labeled in parenthesis next to the gauge name.

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627 Figure 11. Scatterplots of the best (green) and worst (orange) performing radar rain rate estimation  
628 algorithms at each terrestrial based gauge location. Distance from the St. Louis (KLSX) radar is  
629 labeled in parenthesis next to the gauge name.

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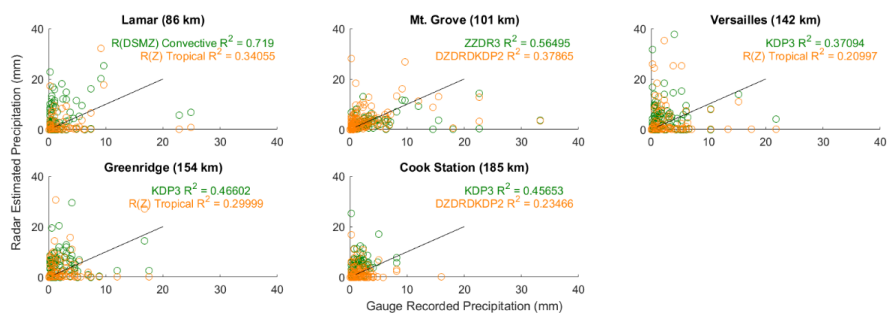
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637 Figure 12. Scatterplots of the best (green) and worst (orange) performing radar rain rate estimation  
638 algorithms at each terrestrial based gauge location. Distance from the Springfield (KSGF) radar is  
639 labeled in parenthesis next to the gauge name.