

A pore-size classification for peat bogs derived from unsaturated hydraulic properties

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Abstract. In ombrotrophic peatlands, the moisture content of the acrotelm (vadoze zone) controls oxygen diffusion rates, redox state, and the turnover of organic matter. Thus, variably saturated flow processes determine whether peatlands act as
10 sinks or sources of atmospheric carbon, and modelling these processes is crucial to assess effects of changed environmental conditions on the future development of these ecosystems. We show that the Richards equation can be used to accurately describe the moisture dynamics under evaporative conditions in variably saturated peat soil, encompassing the transition from the topmost living moss layer to the decomposed peat as part of the vadose zone. Soil hydraulic properties (SHP) were identified by inverse simulation of evaporation experiments on samples from the entire acrotelm. To obtain consistent
15 descriptions of the observations, the traditional van Genuchten-Mualem model was extended to account for non-capillary water storage and flow. We found that the SHP of the uppermost moss layer reflect a pore-size distribution (PSD) that combines three distinct pore systems of the *Sphagnum* moss. For deeper samples, acrotelm pedogenesis changes the shape of the SHP due to the collapse of inter-plant pores and an infill with smaller particles. This leads to gradually more homogeneous and bi-modal PSDs with increasing depth, which in turn can serve as a proxy for increasing state of pedogenesis in peatlands. From
20 this, we derive a nomenclature and size classification for the pore spaces of *Sphagnum* mosses and define inter-, intra-, and inner-plant pore spaces, with effective pore diameters of $>^{\circ}300^{\circ}\mu\text{m}$, $300\text{--}30^{\circ}\mu\text{m}$ and $30\text{--}10^{\circ}\mu\text{m}$, respectively.

1 Introduction

Sphagnum moss is a dominant and keystone species in temperate and boreal peat bog development (Kuhry and Vitt, 1996). As ecosystem engineer, *Sphagnum* moss (Jones et al., 1994) induces vertical growth of peat bogs and may lead to a manifestation
25 of the ombrotrophication process (Balyea, 2009; Rydin and Jeglum, 2016), and has led to considerable terrestrial carbon accumulation during the Holocene (Frolking and Roulet, 2007). The ability of *Sphagnum* spp. to photosynthesize critically depends on the water regime and is limited to the topmost centimetres of the bog profile where growth occurs (Clymo, 1973). Under field conditions, soil hydraulic properties (SHP) control the water regime in the topmost, growing part of the peat profile and are thus a critical factor for moss growth and survival (Hájek and Beckett, 2008). The importance of capillary, film and
30 vapour flow processes for upward water fluxes in moss and peat has been emphasized by Hayward and Clymo (1982) and

Price et al. (2009) while SHP accounting for these processes have only recently been identified by Weber et al. (2017a) for a limited number of samples.

In natural and undisturbed peat bog ecosystems there is a transition from living moss near the surface to heavily decomposed moss peat at greater depths (Clymo and Hayward, 1982, Limpens et al., 2008, Morris et al., 2011), with a concomitant change in SHP (e.g. Quinton et al., 2008; Price et al., 2008; McCarter and Price, 2012, 2014; Morris et al., 2015; Weber et al., 2017a). As *Sphagnum* decomposes, the fibrous material is biochemically broken up into smaller solid fragments (Rezanezhad et al., 2016). This change in physical structure reduces the pore sizes by a collapse of large pores and fine material filling the voids of the organic soil matrix. An increase in overburden leads to vertical shrinkage due to compression and a resulting increase in dry bulk density with depth (Clymo, 1978; Johnson et al., 1990; Price, 2003). The resulting strong decrease in saturated hydraulic conductivity, K_s ($L T^{-1}$) (Boelter, 1969; Ingram, 1978; Quinton et al., 2008) is positively correlated with the state of decomposition as shown by Ingram (1978), Clymo (1970, 1984), Clymo and Hayward (1982), Hayward and Clymo (1982), and Morris et al. (2015). Exceptions from this rule have been observed in cases where pipe flow (Holden, 2005), fire disturbances (Sherwood et al, 2013), and rapid climate change resulting in changes in vegetation and subsequent peat deposition history (Rydin and Jeglum; 2016, Hedwall et al., 2017) occur. In summary, the afore mentioned processes constitute the entire continuous pedogenesis shaping the soil profile as an ongoing process (Blume et al., 2016). It should be noted that this includes the actively growing *Sphagnum* mosses, as Weber et al. (2017a) define the actively growing and living part of the *Sphagnum* mosses as part of the vadose zone, i.e. as part of the soil profile.

In soil hydrology, the Richards equation is widely used as process model for simulating temporally and spatially variable water contents and fluxes in soils. Recently, Weber et al. (2017a) demonstrated that the Richards equation is an adequate process model for unsaturated water flow under evaporative conditions even for the uppermost layer of a bog, where the living *Sphagnum* moss can be treated as part of the soil. The solution of the Richards equation requires the parameterization of SHP. For systems with depth-dependent SHP like peat bogs, one can assume either a homogeneous system and identify effective SHP, or parametrize the SHP as depth-dependent functions (Durner et al., 2008, Vereecken, 2007). In peatland hydrology, the saturated hydraulic conductivity K_s is the most frequently measured hydraulic parameter for different depths. However, the saturated conductivity is not necessarily a good predictor for the unsaturated hydraulic conductivity curve, since the contribution of macro-porosity on preferential flow can be substantial in the saturated case. While the correlation of the saturated hydraulic properties, i.e. K_s and porosity with depth has been well established, corresponding changes of the SHP, namely the water retention characteristic (WRC) and particularly the unsaturated hydraulic conductivity curve (HCC) with depth have neither been extensively investigated nor been treated in numerical simulations.

In ecohydrological modelling of peatland mires containing *Sphagnum*, unimodal expressions of the WRC still dominate (e.g. Dimitrov et al., 2011, Sulman et al., 2012; Wu and Blodau, 2013; Mezbahuddin et al. 2016). However, the investigation of the WRC of organic soils has revealed bimodal pore size distributions which has been found for different, but limited pressure head ranges (Rezanezhad et al., 2009, Quinton et al. 2008, Quinton et al. 2009, Rezanezhad et al., 2010, Kettridge and Binley,

2011, and Rezanezhad et al., 2016), and have so far been rarely expressed in terms of effective SHP over the full pressure head range.

Weber et al. (2017a) applied the highly sensitive method of inverse modelling evaporation experiments performed on *Sphagnum* moss and peat over a wide moisture range to parameterise SHP. The WRCs over the pressure head range from -1500 to 0 cm revealed a trimodal pore-size distribution (PSD) and clearly showed the necessity to account for adsorbed water in drying soil. Samples from two depths of the acrotelm were analysed and the identified SHP differed systematically and in a complex manner for the two depths. The HCC could not be described by simply scaling the saturated hydraulic conductivity, and showed the relevance of capillary and film components for water flow in organic soils. The trimodal nature of the PSD of the sample with living *Sphagnum* moss was linked to three conceptual pore spaces: pores between plant individuals (inter-plant pores), pores between branches and leaves of individual plants (intra-plant pores), and plant-internal water stored in hyaline cells (inner-plant pores). The deeper sample with decomposed moss showed a bimodal PSD with pores associated to the organic soil matrix and pores to the hyaline cells and its skeletal remnants (Fig. 1).

From this we state three hypotheses for this study. First, we expect a gradual shift in the characteristic pore sizes of the inter-plant and inner-plant pores with depth, due to increasing compaction and decomposition of the living moss material. Second, we expect a gradual disappearance of the distinct modalities (particularly the one that indicates the inter-plant pores) and an associated narrowing of the effective pore-size distribution with depth. Finally, we hypothesize that the variability of replicate samples from the same depth decreases with increasing depth, which is associated with the disappearance of the inter-plant pores. The last hypothesis is based on the assumption that samples become more homogeneous due to pedogenic processes such as biochemical degradation and compaction, and that the typical representative elementary volume for the different pore-classes differ, being largest for the inter-plant pores.

Correspondingly, the research aims of this study are i) to investigate in detail the gradual change of SHP with depth, encompassing the transition from living moss to peat, ii) to analyse and quantify the spatial variability in SHP with depth, and iii) to provide a unifying framework to distinguish between different pore systems in *Sphagnum* moss and peat which is based on the PSD and distinct pressure head ranges. To achieve these goals, a series of 28 laboratory evaporation experiments was conducted on undisturbed samples from the topmost 40 cm of a bog profile. The measured data were evaluated by inverse modelling using the Richards equation as process model with the objective to identify SHP for living moss and *Sphagnum*-derived peat. The results are presented in terms of average SHP for each depth, PSDs, and air entry pressure heads of the individual pore systems.

2 Materials and Methods

2.1 Sampling site and sample preparation

The samples were collected at an ombrotrophic peat bog, the Odersprungmoor, Harz Mountains, Central Germany (UTM 32U 608000 mE 5737000 mN; 800 to 821 m a.s.l.). The Odersprungmoor formed on a saddle with an average downslope of 3 %

in the SE-NW direction. In the SW-NE direction it is located in a gentle trough position (Fig. 2; Jensen, 1990). The long-term average temperature is 6.8°C and annual precipitation is 1270 mm with a high inter-annual variance. The open bog is almost elliptical in shape in plan with the longer axes oriented in SE-NW direction and has an area of 16.9 ha which is surrounded by spruce forest. The predominant bog vegetation consists of *Sphagnum magellanicum* Brid. and *Sphagnum rubellum* Wilson
5 with interdispersed *Eriophorum angustifolium* Honck. Further extensive vegetation mapping was carried out by Baumann (2009). Figure 2 provides a detailed spatial reference and an overview on the peat types in the bog. The Odersprungmoor shows features of a poor-fen in some small areas where it is slightly influenced by minerotrophic water which only occurs on a small strip on the North-Western flank (indicated by the arrows, Fig 1, bottom). Most of the incoming water from the shallow soils formed on granite in the North-East is diverted past the bog along the northern rim of the bog towards the North-West
10 (Border and Biester, 2015); thus our sampling location is situated in the ombrotrophic part of the bog. Broder and Biester (2015) provided information on the geochemical composition of the substrate and pore waters which supports this. Weber et al. (2017b) give a detailed account of the carbon, water and energy fluxes of the site during the vegetation period of 2013, a year with exceptionally dry summer time conditions in comparison to the 136 year long term record measured by the meteorological station of the German Weather Service (DWD) at nearby Braunlage.

15 In the acrotelm, a profile characterization with depth is possible as follows: the first 15 cm are composed of living moss, in 15-30 cm dead plant remnants dominate with some parts of the plants still visible, and the 30-40 cm samples contain the dark coloured decomposed moss peat. After the first 15 cm of living moss, a continuous increase in the state of decomposition is measurable (Broder and Biester, 2015). From the profile, 28 cylindrical samples of 250 cm³ volume and 5 cm height were obtained from frozen large sampling blocks using a drill rig (Quinton et al., 2009). We will refer to the samples by the
20 respective mid sampling depths, i.e. 2.5 (n=5), 7.5 (n=6), 12.5 (n=3), 17.5 (n=3), 22.5 (n=3), 32.5 (n=4), and 37.5 (n=4) cm (number of replicates in brackets). Freezing is considered to be a negligible source of error (Branham and Strack, 2014). A comprehensive description of sampling protocol, sample treatment, and methodology is provided by Weber et al. (2017a).

2.2 Identification of soil hydraulic properties

Initially, the samples were saturated using de-aired and de-ionized water over a period of 48 h. The saturated hydraulic
25 conductivity, K_s (cm d⁻¹) of all samples was determined by the falling head-method (KSAT device version 1.4; UMS GmbH, München, Germany). Subsequently, transient evaporation experiments were carried out (Wendroth et al., 1993; Schwärzel et al., 2006) on samples 5 cm i.h. and 8 cm i.d., starting with fully saturated samples that were exposed to free evaporation in the lab. Matric potentials were measured in two depths, and water fluxes were derived from weight changes with time. The measured data were evaluated by inverse modelling using the Hydrus-1D code to solve the Richards equation numerically
30 (Šimůnek et al., 2016). Model parameters were identified by minimizing a weighted least-squares objective function (OF), which contained the time series of pressure heads in two depths (1.25 and 3.75 cm) and the sample's average water content. Details are given by Weber et al. (2017a). Six different parameterizations of the SHP which can be categorized into two main groups were tested. The first model group is based on the widely used van Genuchten-Mualem model (van Genuchten, 1980),

which conceptualises all pore water to be contained and conducted in capillaries. We used unimodal (VGM1), bimodal (VGM2), and trimodal (VGM3) van Genuchten models to parametrize the SHP. The uni- and multimodal van Genuchten models are used widely in soil hydrology and the equations are therefore not repeated here in detail, but can be found, e.g., in Priesack and Durner (2006). The second model group consists of the Peters-Durner-Iden (PDI) model of the SHP. The model is physically more comprehensive in that it ensures zero water content at oven-dryness, and accounts for water flow in completely-filled capillaries, partly-filled capillaries, adsorbed water films, and isothermal vapour diffusion. We used the parameterization derived by Peters (2013), in the modified form published by Iden and Durner (2014) and Peters (2014). The PDI retention curve model has an identical number of free parameters as the VGM. For the conductivity curve, two additional parameters are required which express i) the relative contribution of a non-capillary conductivity to the total unsaturated conductivity, and ii) the steepness of the decrease of the non-capillary conductivity curve with increasing suction. Similar to the VGM models, the PDI models were applied in uni, bi- and trimodal form (PDI equations are given in the Annex).

The data from the evaporation experiments on the 28 samples were evaluated by inverse modelling using all six models of the SHP (VGM1, VGM2, VGM3, PDI1, PDI2, PDI3). In the parameter optimization, the saturated conductivity parameter, K_s , was fixed to the measured value for each individual sample. This resulted in six sets of estimated model parameters, corresponding SHP, and model performance criteria per sample. Model selection was based on model ranking using the Akaike information criterion corrected for small sample size, AICc, as defined in Ye et al. (2008).

2.3 Calculation of mean soil hydraulic properties

After identifying the best parameterization of the SHP for each sample depth based on the AICc, the SHP of the replicates were averaged to obtain representative, mean SHP for each depth. Due to the nonlinear dependence of the SHP on the model parameters, average SHP were not calculated by averaging parameters. The averaging was done by first generating 197 equidistant support points on the pF interval [-3, 6.8] (since the pressure head ranges across orders of magnitude in drying soil, we will use, for convenience, the pF unit in the remainder of this article. It is defined as the common logarithm of the negative pressure head $h(\text{cm})$, i.e., $\text{pF} = \log_{10}(-h)$ (-)). Subsequently, point values of the WRC and HCC were calculated at the support points for each replicate based on its respective best fitted model. The resulting datasets of the replicates were binned into one dataset and a new set of average PDI3 parameters was estimated by nonlinear least-squares fitting. Fitting was done sequentially, first the average WRC model parameters were estimated and in a second step, the retention parameters were kept constant and the parameters of the HCC were estimated using \log_{10} conductivity data in the objective function. The sequential parameter estimation circumvents the need to weight the data groups of $\theta(h)$ and $\log_{10} K(h)$, whereas if measured WRC and HCC data are used to estimate SHP model parameters simultaneously, it involves a weighted multi-objective problem. An example of the averaging method is illustrated in Fig. 3. The iterative least-squares minimization was done with the Differential Evolution algorithm (Price et al. 2006) as implemented in the R package DEoptim (Mullen et al., 2011).

2.4 Pore-size distributions and classification of pore sizes

According to the Young-Laplace equation (Jury and Horton, 2004) the pressure head at which a capillary tube drains is inversely proportional to the equivalent effective diameter, d_{eff} (L), of that capillary which is calculated by:

$$d_{eff} = \frac{4 \gamma \cos \beta}{|h| \rho_w g} \quad (1)$$

where γ is the surface tension (M T⁻²) of water at 20°C, h is pressure head (L), ρ_w is the density of water (M L⁻³), g is the gravitational acceleration (L T⁻²), and β (-) the contact angle between water and the solids which we here set to 0° (Valat et al., 1991), i.e. complete wettability is assumed during monotonic drying (Goetz and Price, 2015).

The PSD function, $f(h)$, was defined as change of capillary saturation with log pressure head (Durner, 1994):

$$f(h) = -\frac{dS_c}{d[\log(10) |h|]} = -\log(10) |h| \frac{dS_c}{dh} \quad (2)$$

where S_c is the capillary saturation function defined by Eqs. (A2) and (A3) in the appendix. In multimodal pore systems, this can be applied to the capillary saturation functions of each pore system $S_{c,i}$ (-), which define the individual pore systems that are superimposed in the effective PSD.

The analysis of the systematic changes in SHP with depth is based on Eq. (1) and Eq. (2). We characterise the depth evolution of d_{eff} by the evolution of the median pore diameter, d_{50} , and the ratio of the 75th to the 25th quantile, d_{75}/d_{25} of the pore size distributions (Eq. 2). This is in analogy to characterisations of particle size distributions.

A size classification of the individual pore domains was based on pressure heads at which air entry occurs to the different pore systems defining the multimodal PSD. In a first step, air-entry pressure heads, $h_{ae,i}$, were determined for each superimposed effective PSD of each depth. From the seven determined values each for the first, second, and third PSD of the depth averaged SHP, as described in section 2.3, a profile average for each modality was computed to determine the air entry.

In case of the van Genuchten saturation model used in the PDI models, the air entry pressure is usually approximated as the reciprocal of parameter α (Assouline et al., 1998). However, the steepness of the WRC is controlled by the shape parameter n and only for relatively large values of n is the air-entry pressure indeed approximately equal to α^{-1} . Therefore, we define the air-entry pressure of a pore system as the pressure head where $S_{c,i} = 0.95$. For the weighted saturation function of the van Genuchten model, the equation to calculate the approximate air-entry value pressure of the i th pore system is given by the equation

$$h_{ae,i} = \alpha_i^{-1} * (0.95^{-1/m_i} - 1)^{1/n_i} \quad (3)$$

. This equation can equally be used for the PDI model. Equation (3) shows that the air-entry pressure depends not only on shape parameter α but additionally on parameter n which characterizes the width of the PSD.

As mentioned above, three pressure heads are calculated delimiting the three pore domains, as averages over all depths.

3 Results and Discussion

3.1 Model performance

The statistical metrics for all 168 inverse simulations (28 samples times 6 models) are listed in Table S1, characterizing model performance by the AICc enabling model comparisons. The values for the best performing model for each sample are summarised in Table 1. According to the AICc, the PDI3 model performed best for 24 out of the 28 samples. For the remaining four samples, the VGM3 model performed best in three cases and the PDI2 in one. Thus, the PDI3 leads to the best model prediction in the majority of replicates regardless of sampling depths. We recall that this is achieved by estimating one additional conductivity curve parameter in the PDI compared to the VGM models with the same modality. This finding challenges the de facto standard usage of the VGM1 and VGM2 models for parametrizing the SHP of Sphagnum moss and peat and extends the theoretical considerations, results, and conclusions in Weber et al. (2017a) to multiple depths in the bog profile. It furthermore corroborates the fact that even model parameters of three-modal functions can be uniquely identified. Note that the use of an incorrect model, despite lower number of parameters, often leads to very high parameter uncertainties like in Dettman and Bechtold (2016). As a consequence, the averaging of the SHP among the replicates was based on the PDI3 model for all depths.

3.2 Soil hydraulic properties and pore-size distributions of all samples

Figure 4 presents the WRCs (left), HCCs (middle), and PSDs (right) of all measured samples, grouped for the seven sampling depths (denominated A to G, from top to bottom). A comparison of the SHP at the different depths reveals three main trends. First, the variability between the replicates decreases with increasing depth, i.e. SHP of the replicates become more similar. Second, for all depths a comparable modality of relatively small pores is discernible, which starts to drain at about $pF = 2$ (-100 cm). Superimposed to this pore system, there is a second and third modality indicating larger pore systems for the near-surface samples, with the third modality reflecting a pore domain close to water saturation. With increasing depth the variability in the two larger pore domains decreases considerably. Third, the HCCs for all depths appear very similar in the more unsaturated moisture range ($pF > 2$), but diverge towards saturation. One possible reason for the scatter for $pF < 2$ is the insensitivity of evaporation experiments to changes in the $K(h)$ function in wet soil. This insensitivity occurs if the evaporation rate is on the order of $K(h)$ or smaller, leading to small gradients in pressure head which cannot be resolved by tensiometers (Peters and Durner, 2008). A more reliable determination of the HCC close to water saturation could be obtained by the tension disk method (Klute and Dirckson, 1986; McCarter et al. 2017), multi-step outflow (Durner and Iden, 2011), or multi-step flux measurements (Weller et al., 2011). However, these methods have their own challenges when applied to organic soils and the latter two have, to the best of our knowledge, not been applied to obtain SHP for organic media so far, although Qi et al. (2011) used in multi-step outflow experiments to determine the WRC.

3.3 Change of pore-system characteristics with depth

To better identify the pore system changes with depth, we compare mean SHP for all depths in Fig 5. The trends with depth which have been observed for the individual samples, now become much clearer. The seven mean WRCs (Fig 5, left) show an increased water holding capacity with increasing depth across a wide pressure head range, from saturation up to $pF = 3.2$ (a pressure head of -1500 cm). This finding is supported by literature data for conditions near water-saturation (Price et al., 2008; Price and Whittington 2010; McCarter and Price, 2012; Goetz and Price; 2015). Concurrently, the HCCs show a pronounced decrease of the saturated conductivity and systematically higher unsaturated conductivities with increasing depth (Fig 5, right), with a crossing point of the conductivity functions at around $pF = 1$.

From an ecophysiological point of view, it is interesting to analyse the relationship between SHP and the resilience against desiccation. In fact, all samples have a high water capacity around $pF = 2$. During meteorological conditions favouring prolonged periods of drying, the decrease in pressure head is slowed down by the release of this water, and low pressure heads leading to desiccation and cessation of photosynthesis (Hájek and Beckett, 2008) are reached only slowly. Commensurate to the WRC, the slope of the HCC around $pF = 2$ decreases as water drains from hyaline cells and their skeleton material, and hydraulic conductivity remains at values of approximately $10^{-2} \text{ cm d}^{-1}$ until approx. $pF = 2.5$, where it drops at all depths rapidly below $10^{-4} \text{ cm d}^{-1}$. The relatively high hydraulic conductivity in the pressure head range until $pF = 2.5$ ensures an upward flow of water which contributes to the effective desiccation tolerance of the vegetation under field conditions.

We further observe that the WRCs shifts with depth from a trimodal pore-size distribution to a bimodal one with a distinct expression of the two remaining pore systems. This is nicely recognizable from the plots of the PSDs in Fig. 6. To calculate meaningful pore-size parameters, we separated the fine pore system, characterized by the capillary saturation function with the parameters w_3 , a_3 and n_3 , from the system of larger pores, defined by the superposition of the two saturation functions with parameters w_2 , a_2 , n_2 and w_1 , a_1 , and n_1 , and calculated the median diameters of the two pore systems for each depth as the characteristic pore size. These characteristic pore sizes are indicated in Fig. 6 by the dashed vertical lines. From visual inspection, and confirmed by the values of the fitted parameters of the third pore subsystem (Table 2), it becomes obvious that the fine pore system remains virtually unchanged with depth, encompassing about 15 to 20 % of the total pore space, $w_3(\theta_s - \theta_r)$. This pore system is characterized by a well-defined maximum of its pore size distribution at $pF = 2.3$, which does not change with depth (Fig. 6). Also, the width of this fine pore system shows no change with depth. In contrast, the median equivalent diameter, d_{50} (L), from the superimposed first and second modality drifts gradually from larger to finer pores (Fig. 6).

To further carve out the depth-dependency of key characteristics of the pore systems, we show the depth dependence of saturated conductivity and two characteristic pore-size parameters in Fig. 7. The near log-linear decrease in measured saturated hydraulic conductivity K_s (Fig.7, a) is in agreement with established trends in these ecosystems (Morris et al., 2015). The shift in the median pore size of the larger pore system indicates the strongest transition between 10 and 25 cm (Fig.7, b). The width

of the associated pore system, expressed by the ratio of the first and third quartile of the PSD, d_{75}/d_{25} (-), shows a distinct and continuous narrowing with depth (Fig.7, c).

As a side note, we like to comment on an interesting aspect of using the different parameterizations of the HCC. We found that the tortuosity/connectivity parameter τ in this study is positive for each individual sample parameterisation with the PDI3 (Table S1). The same is true for the calculated mean functions at all depths (Table 2). A positive value of τ is in agreement with its conceptual meaning (Mualem, 1976; Peters et al., 2011). This contrasts with reports from the literature (Price et al., 2008; Whittington and Price, 2010) and our findings with van Genuchten type functions, where τ is often negative (Table S1). Obviously, the use of a structurally more correct model of the SHP that accounts for partially filled capillaries, prevents parameter τ from becoming negative. Conversely, if an inadequate model of the SHP is applied, τ has a tendency to become increasingly small and even negative because it induces the HCC to be less steep in the in the medium to dry range. Although this effect may be welcome to describe measurements, it is obtained by a physically implausible value of the shape parameter (Hoffman-Riem et al., 1999). Another important feature of the identified values of τ is their relative small variation with depth. The gradual change of PSDs with depth summarized by Fig. 6 can be explained by the origin of the samples and the pedogenic processes they have undergone, i.e. biochemical degradation breaking up fibres into smaller pieces (e.g. Rezanezhad et al. 2016), compaction (Price and Schlotzhauer, 1999), the shrinkage and swelling of bog soils (Schlotzhauer and Price, 1999; Price et al., 2003; Price, 2003; Glaser et al., 2004) and freeze-thaw processes (Meiers et al., 2013). These findings are corroborated by a positive relationship between depth and advance in decomposition at this site (Broder and Biester, 2015). Obviously, these processes lead to a homogenisation of the organic material, a disappearance of the largest pores, and thus to a smaller spatial variability of the SHP in greater depths. While in the upper 15 cm the living moss reveals a large natural phenotypic variability over orders of centimetres, the dead plant remnants at 15-30 cm have already been subject to some compaction and the inter-plant pores are filled with smaller particles. The most decomposed samples from 30-40 cm, which lie beneath the water table most of the time, are the most homogeneous and have completely lost the distinct trimodality in the PSD, which was evident for the samples from near the surface. The deepest samples are also the most homogeneous in colour and solid particle sizes. It is worthwhile to note that the PSDs are basically bimodal but this does not contradict the superiority of using a trimodal parameterization (see section 3.1 and Table 1) as indicated by the AICc. The superposition of PSDs can improve the overall description, even if they do not represent two distinct pore systems with different characteristic pore sizes. This was also discussed for the bimodal van Genuchten model by Zurmühl and Durner (1998) and for organic soils by Weber et al. (2017a). Without contradiction to the presented model, we point out that preferential flow may be an important driver for saturated flow on the very large.

30 **4 Proposal of a pore size classification for *Sphagnum* moss and peat**

The results of our study suggest a pore-size classification that is based on the three different pore domains characterised by the air-entry pressures (Eq. 3; Table 3). This classification relates the PSD to different physical components of moss and peat and

hereby also directly links the SHP to pedogenesis. The resulting averaged air entry pressures for the first, second, and third pore domain are given as pF 0, 1, 2, respectively, and in the following we give a detailed description of the pore water domains and the residual water (Fig. 8, Table 4). I-III are based on capillary water storage and IV is based on non-capillary (adsorptive) water storage.

- 5 The **first domain (I)** reaches from saturation to a pressure head of approx. -10 cm (pF = 1), which is marked by the mean $\bar{h}_{ae,2}$, corresponding to effective pore diameters of > 300 μm . At this point the HCCs of different depths converge in the sense that for pF > 1 the scatter is significantly reduced and the individual curves run in parallel with a range of approximately one order of magnitude (Fig. 5). This pressure head corresponds to a state where the highly heterogeneous *inter-plant pores* (living and slightly decayed *Sphagnum*) have drained (Fig. 1).
- 10 The **second domain (II)** extends from pF = 1 to pF = 2 corresponding to effective pore diameters between 300 μm and 30 μm . It comprises the *intra-plant pore space* in the sampling depths 2.5 cm to 27.5 cm where macroscopic living and undecomposed moss fragments exist. In the remaining sampling depths decomposition is advanced but the skeletal structures containing the hyaline cells remains (Fig. 1). Correspondingly the water in the second domain is here stored in the outer skeletal spaces of the peat (Rezanezhad et al., 2016).
- 15 Finally, the **third pore domain (III)** is represented by intact and decayed hyaline cells with effective pore radii of 30 μm to 10 μm . As shown in Fig. 1, the hyaline cells can still have intact cell membranes, but appear to decay more rapidly than the structures bearing them. In fact, the distances between two structural elements (skeleton) making up the hyaline cells is, effectively, marginally larger than the hyaline cell opening.

Thus, in the absence of macropores, two size classes can be differentiated in decomposed *Sphagnum* peat; the *outer plant*
20 *matrix* pores > 30 μm , and the *inner plant matrix* pores with effective pore radii 30 to 10 μm (Table 4). The above mentioned hyaline cells and their skeletal structures are drained by pF = 2.5 which is the pressure head where the **fourth domain (IV)** starts. At these pressures of pF > 2.5 , the water conductance can no longer be described by capillary flow theory.

In our analysis we assume that shrinkage does not affect our key findings. Shrinkage was observed to be around 5-8% on
25 samples from the same depths and same bog, as referenced to the initial volume. Since the delimitations of our pore size classification span orders of magnitude in pressure head and related effective pore radii, we believe that shrinkage will not have a considerable influence on the derived soil hydraulic properties for the small scale.

In line with these definitions, a pressure head delimitation of pore water into an active (*inter- and intra-plant and inter-plant*
matrix pore space) and an inactive porosity (*inner-plant and inner plant matrix*) at a pressure head of $h = -100$ cm is suggested. Finally, a word of caution with respect to generalizing our findings: Michaelis (2011) describes 286 species of
30 *Sphagnum*, occurring globally; thus, our results might not be applicable to all species, since the phenology of decaying *Sphagnum* might be different between species.

5 Conclusions

Based on measured data from transient evaporation experiments and an evaluation by inverse modelling using the Richards equation as a process model, we identified SHP for 28 samples from an acrotelm of an ombrotrophic, *Sphagnum* moss dominated bog. To parameterize the SHP, we compared six different models. The successful description of the observed data was possible by a) considering three modalities representing the underlying PSD and b) including the contribution of non-capillary water in the SHP models. Combined, this results in an encompassing parameterization across the full moisture range. With the continuous information from fully parameterised models, available from the presented work, greatly extends the level of detail in comparison to previous works.

We averaged the SHP for each of the seven sampled depths and found, compared to insights from biological studies, that these mean hydraulic properties reflect the physiological nature of the pore size domains in the living moss carpets of peatbogs. Larger heterogeneities in identified SHP between depth replicates could be shown for samples from the living moss; however, this effect reduced considerably with increasing depth and a concomitant reduction of PSDs from tri- to bimodal. Both effects, the homogenisation and reduction in modality, can be explained by pedogenic processes.

A unifying nomenclature to describe and report results from research on the vadose zone of ombrotrophic peatlands is proposed. With this, the pore spaces in *Sphagnum* moss and peat can be classified according to size ranges of the effective pore diameters. These size ranges are derived from an analysis of the shape of SHP and underlying PSDs from the uppermost 40 cm of the acrotelm. In living *Sphagnum* moss, the three pore spaces are thus proposed to be referred to as *inter-*, *intra-*, and *inner-plant pore spaces*, with effective pore diameters of $>300\mu\text{m}$, 300 to $30\mu\text{m}$ and 30 to $10\mu\text{m}$, respectively. For deeper samples, the pedogenesis of the acrotelm has had a considerable impact on the shape of the SHP. First, the collapse of the inter-plant pores and their filling with smaller particles led to more homogeneous and to gradually bi-modal PSDs with increasing depth. Much of the hyaline cell structure and skeleton remains less affected by compaction and is resilient to decomposition. These remaining larger pores with effective pore diameters of $>300\mu\text{m}$ and fine pores 30 to $10\mu\text{m}$ correspond more to the plant matrix than the fully visible plant and were thus described as *outer plant matrix* pores and the *inner plant matrix*, respectively.

Following these delimitations and with depth continuous differentiation between the larger pores and inner-plant pores, we conclude that, based on this soil hydrological perspective, the water storage domain suggests a partitioning into an active and inactive porosity when considering solute transport and is delimited at a pressure head of $h = -100$ cm. The proposed domain classification was inferred from a soil hydrological modelling approach and with the discussion of the physiological meaning, we associate them to measurements and reflections in the seminal biological studies by Hayward and Clymo (1982), Lewis (1988), and van Breemen (1995).

Future research should include testing the Richards equation under various boundary conditions to verify that the identified SHP can be used for predictive purposes. Additionally, the research should be conducted to establish if proxies such as bulk

density, C/N ratios, and/or vegetation structure can be used to predict SHP accurately. Lastly, scaling approaches are expected to help to describe in numerical simulations the gradual and continuous change of SHP with depth .

Code and Data availability

Codes can be made available upon request. Measured data (pressure heads at two depths and evaporation rates) are available
5 in form of the HYDRUS 1D input files in the online Supplementary Information.

Supplement

Table S 1: Model performance criteria and parameters for all models and all depths.

28 HYDRUS 1D projects containing the observed matric potential measurements and evaporation rates of each sample.

Appendix A: PDI Model Equations

10 The WRC of the PDI model family (Peters, 2013, Iden and Durner, 2014, Peters, 2014) is given by the equation

$$\theta(h) = (\theta_s - \theta_r) S_c(h) + \theta_r S_{nc}(h) \quad (A1)$$

where θ (-) is volumetric water content, h (cm) is pressure head, and $S_c(h)$ (-) and $S_{nc}(h)$ (-) are the saturation functions for capillary and non-capillary water, respectively. $S_c(h)$ (-) is defined as:

$$S_c(h) = \frac{\Gamma(h) - \Gamma_0}{1 - \Gamma_0} \quad (A2)$$

where $\Gamma_0 = \Gamma(h_0)$, h_0 (cm) is the pressure head at oven-dryness, and $\Gamma(h)$ is the multimodal van Genuchten saturation function (Durner, 1994)

$$\Gamma(h) = \sum_{i=1}^k \Gamma_i(h) = \sum_{i=1}^k w_i [1 + (-\alpha_i h)^{n_i}]^{-m_i} \quad (A3)$$

15 with shape parameters α_i (cm⁻¹) and n_i , the constraint $m_i = 1 - 1/n_i$, the number of modes or pore systems, k (-), and weights w_i which sum to unity. The non-capillary saturation function is given as

$$S_{nc}(h) = 1 + \frac{1}{x_a + x_0} \left\{ x - x_a + \ln \left[1 + \exp \left(\frac{x_a - x}{b} \right) \right] \right\} \quad (A4)$$

where $x = \log_{10}(-h)$, $x_a = \log_{10}(-h_a)$, $x_0 = \log_{10}(-h_0)$, and $h_a = 1/\alpha_1$. Parameter b is a smoothing parameter for which empirical equations are given in Iden and Durner (2014). The HCC is defined as

$$K(h) = (1 - \omega) K_s K_{rc}(S_c) + \omega K_s K_{rnc}(S_{nc}) + K_v(h) \quad (A5)$$

20 where ω (-) is the relative proportion of water flow in films and corners, $K_{rc}(h)$ (-) is relative hydraulic conductivity caused by flow in completely-filled capillaries, $K_{rnc}(h)$ (-) is relative hydraulic conductivity caused by flow in films and corners

(incompletely filled capillaries), and $K_v(h)$ is the effective hydraulic conductivity for isothermal vapour diffusion. The equation for $K_v(h)$ can be found in Saito et al., (2006) and the closed-form equations for the two liquid conductivities are (Peters, 2013; Peters, 2014)

$$K_{rc}(S_c) = S_c^\tau \left[1 - \left(\frac{\sum_{i=1}^k w_i \alpha_i (1 - \Gamma_i^{1/m_i})^{m_i}}{\sum_{i=1}^k w_i \alpha_i (1 - \Gamma_{i,0}^{1/m_i})^{m_i}} \right)^{m-2} \right] \quad (\text{A6})$$

and

$$K_{rnc}(S_{nc}) = \left(\frac{h_0}{h_a} \right)^{a(1-S_{nc})} \quad (\text{A7})$$

5 where $\Gamma_{i,0} = \Gamma_i(h_0)$ and $a = 1.5$ is an empirical parameter for film flow (Tokunaga, 2009).

Author contributions

TW designed the study, the experiments and carried them out. SI developed the model code and jointly performed the simulations with TW. TW prepared the manuscript with contributions from all co-authors. WD oversaw the formal analysis, acquired the funds, and provided all the necessary resources for this research.

10 Competing interests

The authors declare that they have no conflict of interest.

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Figures



Figure 1: Sphagnum moss structures and soil pore sizes. a) Sphagnum lawn with visible bleaching due to desiccation of the capitula (in German language Sphagnum is also referred to as ‘Bleichmoos’, which translates to ‘bleaching moss’), a-b) images of *Sphagnum cuspidatum* H.Klinggr. to exemplify the b) sampled and slightly spread out individuals with visible interconnectedness of branches, c) close up of the capitulum with pending branches and leaves, d) scanning electron microscope image of Sphagnum leaves on a branch with visible dark circles as the opening to the hyaline cells (by courtesy of Reuven Simhayov). Right: drawing of *Sphagnum magellanicum* (by courtesy of Bent Johnsen. © Department of Biology, University of Copenhagen) with, e) individual plant, f) branch surface with skeletal structure in green, g) branch with leaves, h) cross section of a leaf with large hyaline cells, and i) individual leaf.

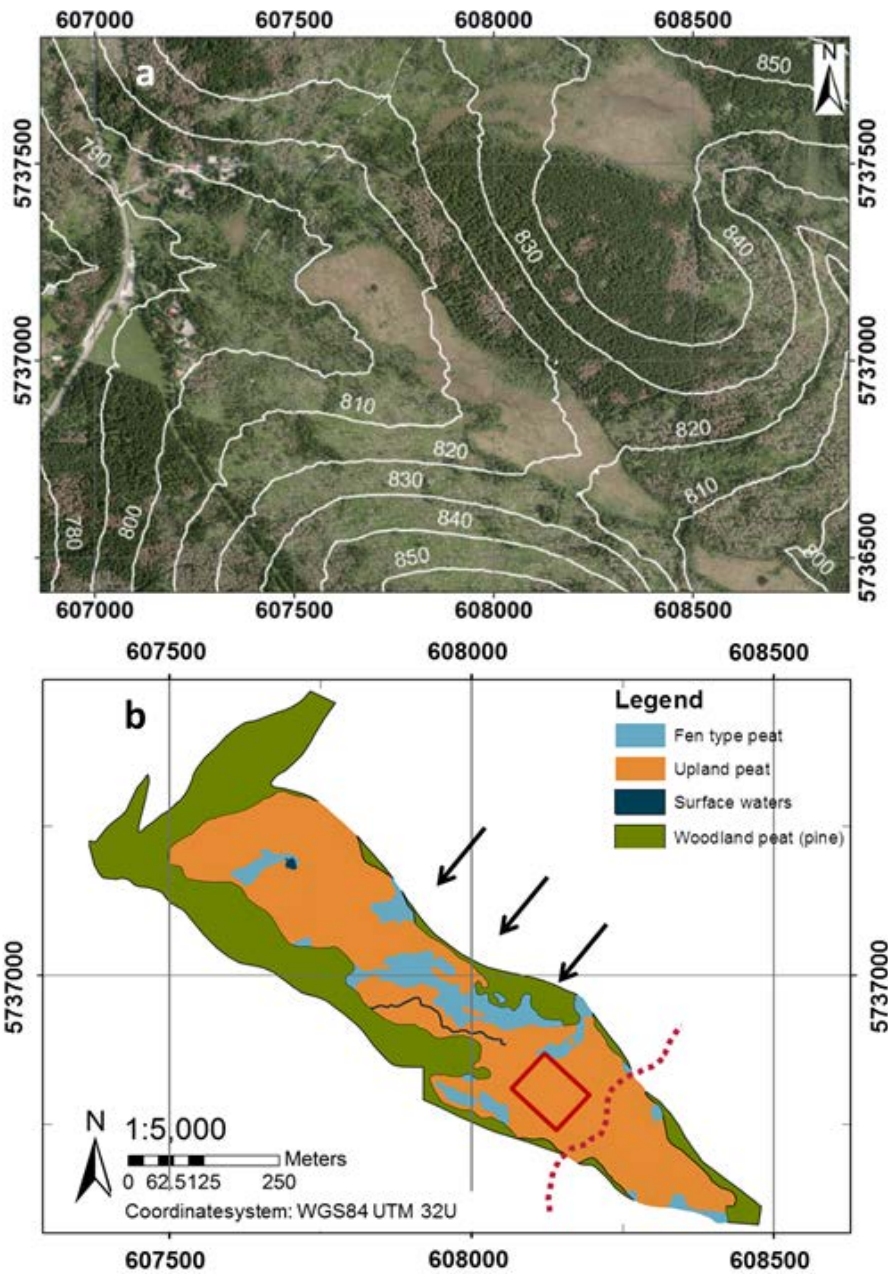


Figure 2: a) Satellite image and elevation contours (m.a.s.l.) of the Odersprungmoor, b) vegetation mapping and characterisation of the peatland, black arrows indicate minerotrophic water influx into the peatland resulting in higher proportion of fen type vegetation, the red dashed line is the approximate watershed divide, and the red box marks the sampling area.

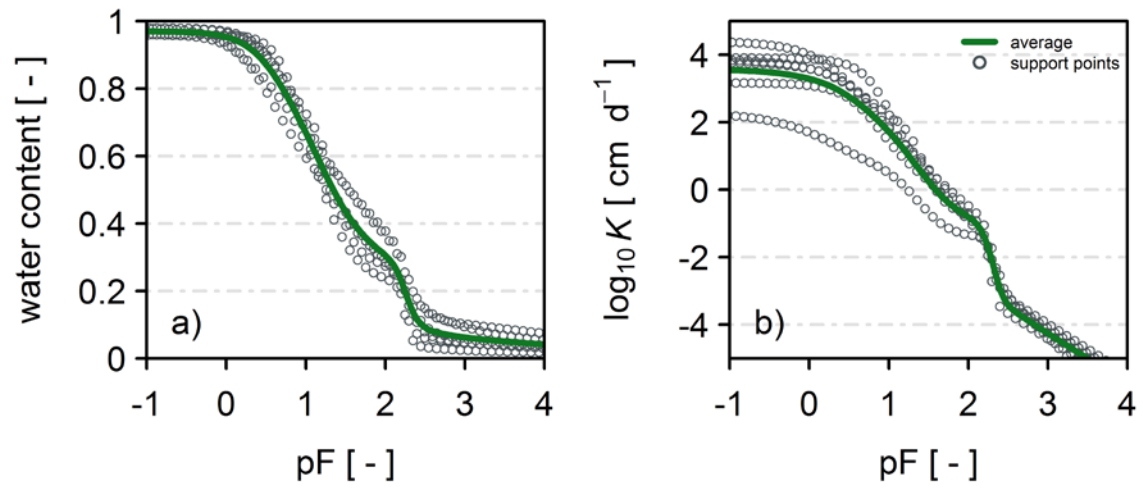


Figure 3: Example of the averaging process for (a) water retention curve and (b) hydraulic conductivity curves, shown for depth 7.5 cm (five replicates). Despite the variability of the individual curves, the key structural features are conserved.

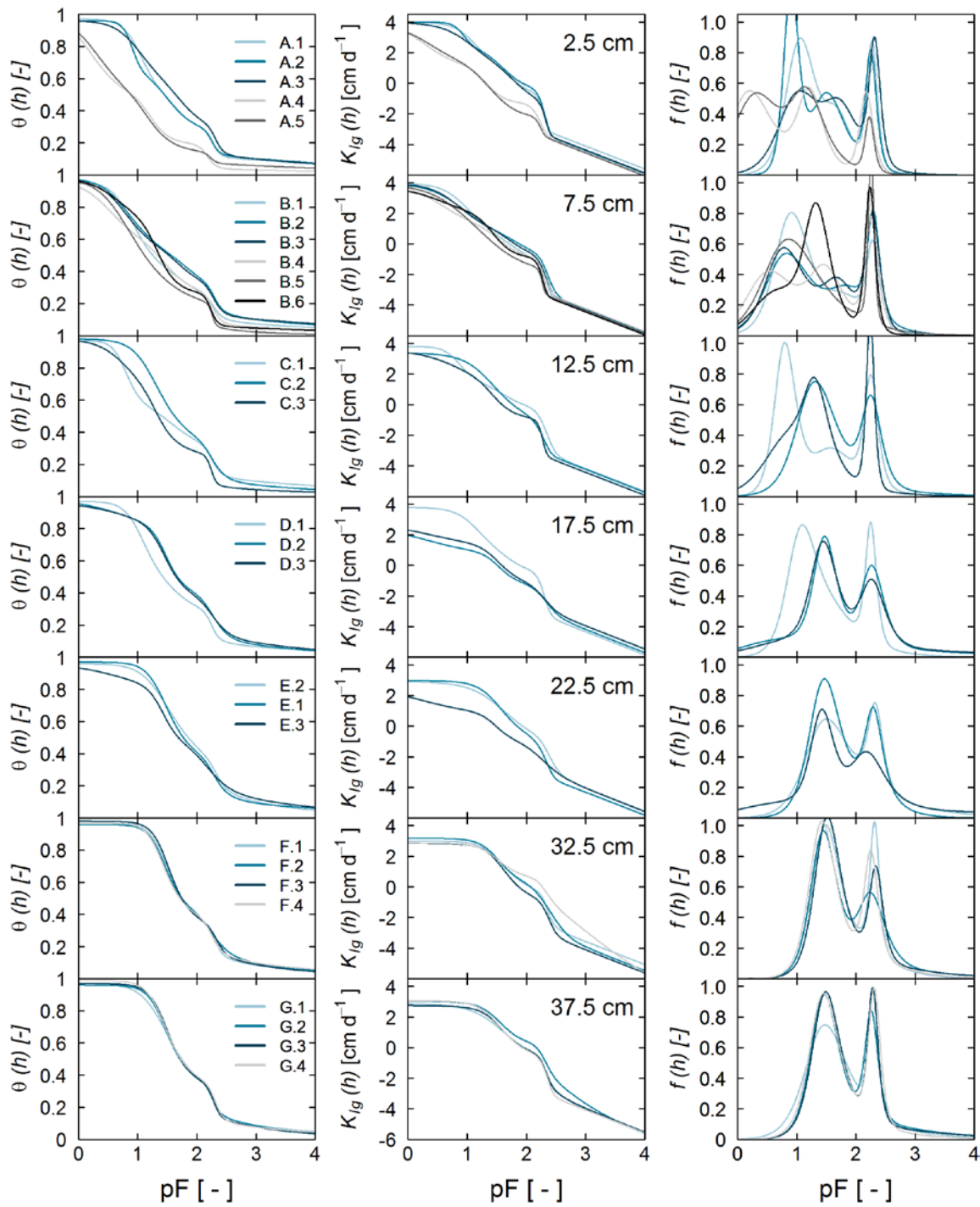


Figure 4: Left: Water retention curves, center: hydraulic conductivity curves, and right: Pore-size distributions (of all 28 samples, K_{lg} refers to the common logarithm of the conductivity value).

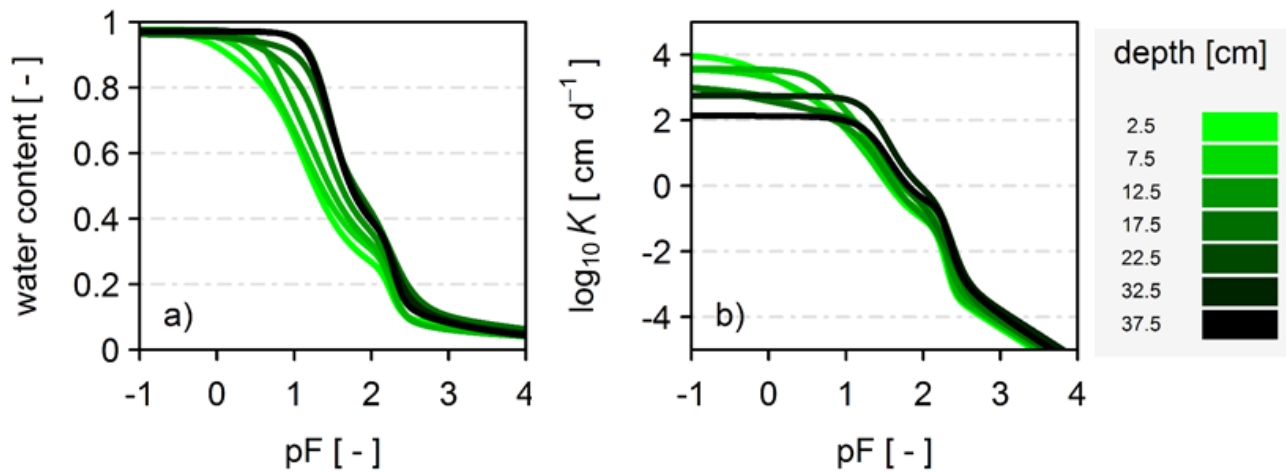


Figure 5: Mean (a) retention and (b) conductivity curves for the depths 2.5 to 37.5 cm in 5 cm increments.

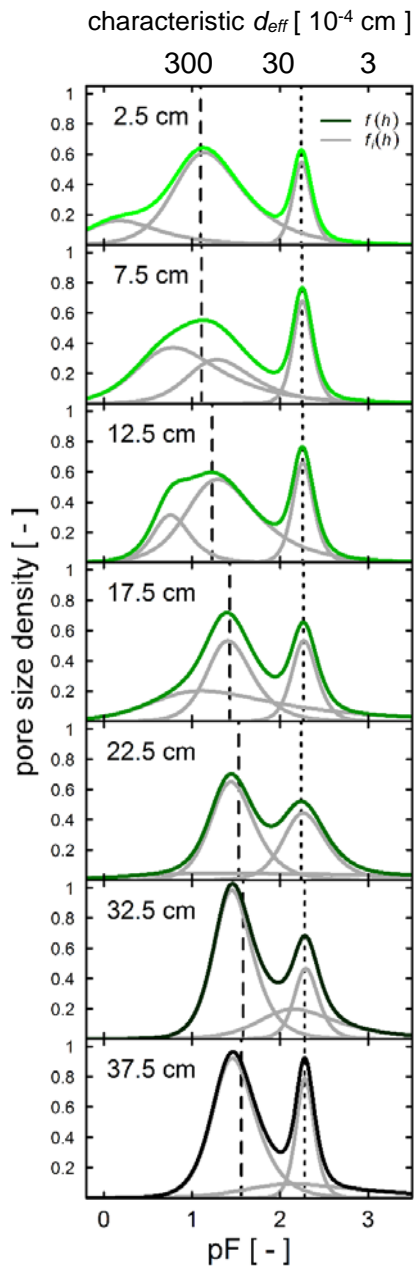


Figure 6: Continuous pore size distributions calculated from Eq. 4 per depth showing the overlap of the three pore spaces. The dashed lines represent the median (d_{50}) of the first and second pore domain the increase of which positively correlates with increasing depth. The dotted lines mark the modus of the third modality which remains constant regardless of depth.

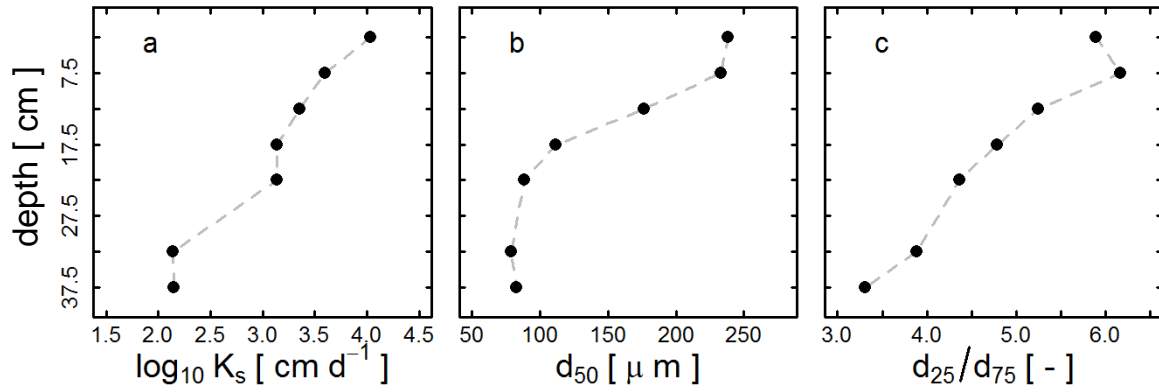
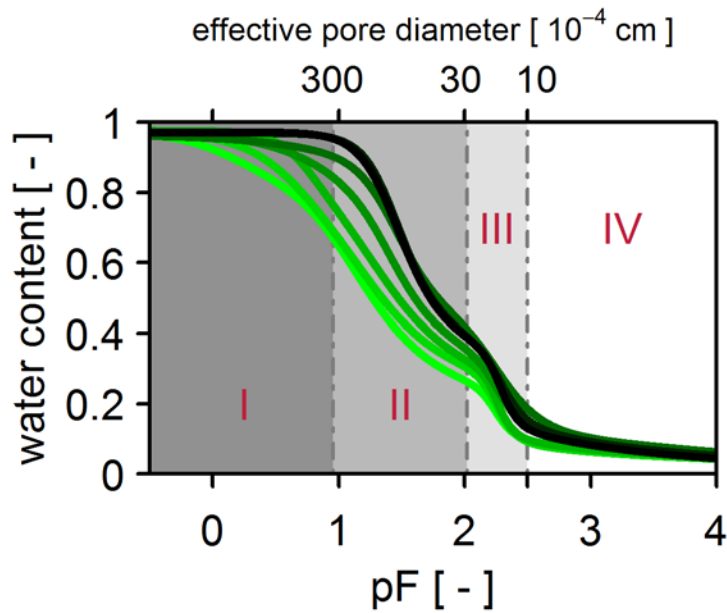


Figure 7: (a) Trends of key pore systems characteristics with depth: (a) near exponential decrease in K_s with depth, (b) decrease of characteristic pore diameter with depth, expressed as median pore diameter d_{50} of the second modality (c) reduction of the width of the pores-size distribution with depth, expressed by d_{75}/d_{25} .



5 Figure 8: Four pore domains represented in the soil water retention curve. The roman letters I-III denote different capillary water domains for which a detailed explanation is given in the text and values are presented in Table 4. The region denoted by IV is non-capillary (residual) water.

Tables

Table 1: Statistical evaluation results of the inverse parameter estimation for 31 samples of eight mid sampling depths.

Sample Name	Mid sampling depth	OF Value ¹	RMSE _w ² 0.75	RMSE _w ³ 0.25	AICc ⁴	Δ AICc ⁵	Best Model ⁶
[-]	[cm]	(x 10 ⁴)	[cm]	[cm]	[-]	[-]	[-]
A.1	2.5	0.82	5.1	2.4	2348	417	PDI3
A.2	2.5	1.60	7.1	2.7	2734	795	PDI3
A.3	2.5	0.58	6.5	2.1	2688	394	PDI3
A.4	2.5	1.03	8.2	5.1	3518	321	PDI3
A.5	2.5	0.78	6.8	4.5	3051	432	PDI3
B.1	7.5	2.03	3.8	2.9	1766	806	PDI3
B.2	7.5	1.51	4.9	2.3	2156	954	PDI3
B.3	7.5	1.05	6.6	3.0	2600	413	PDI3
B.4	7.5	0.91	7.4	4.2	2595	782	PDI3
B.5	7.5	0.61	8.4	3.9	3692	350	PDI3
B.6	7.5	1.41	4.3	3.7	3408	1566	VGM3
C.1	12.5	1.17	4.6	2.3	1856	642	PDI3
C.2	12.5	1.29	8.6	8.0	5562	27	PDI2
C.3	12.5	1.12	5.0	4.6	3594	797	PDI3
D.1	17.5	0.95	2.6	4.9	2362	185	PDI3
D.2	17.5	2.31	3.5	3.8	3209	1727	PDI3
D.3	17.5	2.06	1.9	2.4	1727	2788	PDI3
E.1	22.5	1.81	2.2	2.3	1724	1182	PDI3
E.2	22.5	2.45	4.1	2.1	2418	957	PDI3
E.3	22.5	3.99	2.6	3.7	2684	1654	PDI3
F.1	32.5	3.69	3.0	2.9	1966	958	VGM3
F.2	32.5	2.52	2.1	3.9	2347	186	PDI3
F.3	32.5	1.26	4.3	1.5	2102	447	PDI3
F.4	32.5	0.95	4.8	3.5	2166	94	VGM3
G.1	37.5	2.79	3.8	4.3	2640	653	PDI3
G.2	37.5	1.90	3.0	3.2	2162	470	PDI3
G.3	37.5	0.54	2.6	2.7	1724	1424	PDI3
G.4	37.5	0.38	4.6	2.1	2445	156	PDI3

¹ Objective function value (Eq. 20 in Weber et al., 2017a).

² Root mean square weighted error of the matric potential measurements at a height of 3.75 cm. The a median RMSE_w value over all depths is 3.0 cm.

- ³ Root mean square weighted error of the matric potential measurements at a height of 1.25 cm. The a median $RMSE_w$ value over all depths is 4.3 cm.
- ⁴ Corrected Akaike Information criterion.
- ⁵ Difference in AICc between best and second best model.
- 5 ⁶ Trimodal van Genuchten-Mualem model (VGM3) and trimodal PDI variant (PDI3).

Table 2: PDI3-model parameter* values of the depth averaged effective soil hydraulic properties

Depth (cm)	θ_r (-)	θ_s (-)	α_1 (cm ⁻¹)	n_1 (-)	w_1 (-)	α_2 (cm ⁻¹)	n_2 (-)	w_2 (-)	α_3 (cm ⁻¹)	n_3 (-)	$\lg K_s$ (cm d ⁻¹)	τ (-)	$\lg \omega$ (-)
2.5	0.12	0.97	0.96	2.0	0.18	0.1	2.1	0.66	0.006	6.4	4.0	0.6	-5.9
7.5	0.09	0.97	0.26	1.8	0.50	0.07	2.1	0.30	0.006	6.2	3.6	0.6	-4.2
12.5	0.10	0.98	0.19	3.3	0.20	0.07	2.0	0.60	0.006	7.5	3.4	1	-4.2
17.5	0.06	0.97	0.18	1.4	0.42	0.05	2.9	0.37	0.006	4.9	3.1	1.0	-5.9
22.5	0.04	0.96	0.44	1.1	0.24	0.04	2.9	0.46	0.006	3.1	2.8	1.7	-6.0
32.5	0.09	0.97	0.04	3.4	0.55	0.02	1.7	0.25	0.005	5.3	2.1	0.2	-5.6
37.5	0.06	0.97	0.04	3.0	0.61	0.02	1.5	0.17	0.005	6.6	2.1	0.3	-5.7

* θ_r : residual water content, θ_s : saturated water content, α_i and n_i : shape parameters of the three superimposed capillary bundles, respectively, w_i : weighting coefficient of the capillary bundles, K_s : saturated hydraulic conductivity, ω : non-capillary conductivity, τ : tortuosity parameter. The common logarithm to the base 10 is denoted by lg . The parameters of all individual samples can be found in the Supplementary Information.

Table 3: Air entry pressures of the three pore systems of the effective SHP for all sampling depths (left column) and arithmetic means to delimit the individual pore domains.

Depth	$h_{ae,1}$	$h_{ae,2}$	$h_{ae,3}$
[cm]	[cm]	[cm]	[cm]
2.5	-0.3	-3.4	-108
7.5	-1.2	-4.9	-107
12.5	-2.4	-4.7	-104
17.5	-1.7	-9.3	-96
22.5	-1.8	-10.5	-72
32.5	-11.8*	-31.8	-117
37.5	-10.8*	-20.2	-132
Mean	-1.5	-8.0	-105
SD	-0.7	-3.2	-17.1

* As previously established, the depths 32.5 and 37.5 show no macro porosity and are excluded from calculating the mean and standard deviation for the average $\bar{h}_{ae,1}$ -value. The mean $\bar{h}_{ae,2}$ -value is calculated from the the $h_{ae,2}$ -values of the sampling depths 2.5-27.5 cm, and the two $h_{ae,1}$ -values at depths 32.5 and 37.5 cm. The mean $\bar{h}_{ae,3}$ - value is calculated based on all depths.

Table 4: Overview for proposed pore domain nomenclature with corresponding pressure head delimitations and effective pore diameters.

Name of pore domain	Pore domain Number	Effective pore diameter [μm]	Pressure head [cm]	pF [-]
Inter-plant pores	I	> 300	> -10	1
Intra-plant and outer plant matrix* pores	II	300 to 30	-10 to -100	1 - 2
Inner-plant and plant matrix* pores	III	30 to 10	-100 to -300	2 - 2.5
non-capillary, cytoplasmic and apoplastic water	IV	na**	<-1000	> pF 3

* The plant matrix refers to the skeleton of the *Sphagnum* which in its living form contains intact hyaline cells and the decomposition of cell walls results in the remaining more persistent plant skeleton (Figure 1).

**it is not applicable to calculate an effective radius for water which is not contained in capillaries.