

1 **CALIBRATING ELECTROMAGNETIC INDUCTION CONDUCTIVITIES WITH TIME-DOMAIN**

2 **REFLECTOMETRY MEASUREMENTS**

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15

16 **Abstract**

17 This paper deals with the issue of monitoring the spatial distribution of bulk electrical
18 conductivity σ_b , in the soil root zone by using Electromagnetic Induction (EMI) sensors under
19 different water and salinity conditions. To deduce the actual distribution of depth-specific σ_b
20 from EMI apparent electrical conductivity (EC_a) measurements, we inverted the data by using a
21 regularized 1D inversion procedure designed to manage nonlinear multiple EMI-depth
22 responses. The inversion technique is based on the coupling of the damped Gauss-Newton
23 method with truncated generalized singular value decomposition (TGSVD). The ill-posedness of
24 the EMI data inversion is addressed by using a sharp stabilizer term in the objective function.

25 This specific stabilizer promotes the reconstruction of blocky targets, thereby contributing to
26 enhance the spatial resolution of the EMI results in presence of sharp boundaries (otherwise
27 smeared out after the application of more standard, Occam-like regularization strategies
28 searching for smooth solutions). Time-Domain Reflectometry (TDR) data are used as ground-
29 truth data for calibration of the inversion results. An experimental field was divided into four
30 transects 30 m long and 2.8 m wide, cultivated with green bean and irrigated with water at two
31 different salinity levels and using two different irrigation volumes. Clearly, this induced
32 different salinity and water contents within the soil profiles. For each transect, 26 regularly
33 spaced monitoring soundings (1 m apart) were selected for the collection of, respectively: (i)
34 Geonics EM-38 and (ii) Tektronix Reflectometer data. Despite the original discrepancies in the
35 EMI and TDR data, we found a significant correlation of the means and standard deviations of
36 the two data series, in particular, after a low-pass spatial filtering of the TDR data. Based on
37 these findings, the paper introduces a novel methodology to calibrate EMI-based electrical
38 conductivities via TDR direct measurements. This calibration strategy consists in a linear
39 mapping of the original inversion results into a new conductivity spatial distribution with the
40 coefficients of the transformation uniquely based on the statistics of the two original
41 measurement datasets (EMI and TDR conductivities).

42

43 **Introduction**

44 Soil water content and salinity vary in space both vertically and horizontally. Their distribution
45 depends on management practices and on the complex nonlinear processes of soil water flow
46 and solute transport, resulting in variable storages of solutes and water (Coppola et al. 2015).
47 Monitoring the actual distribution of water and salts in the soil profile explored by roots is
48 crucial for managing irrigation with saline water, while still maintaining an acceptable crop

49 yield. For water and salts monitoring over large areas, there are now non-invasive techniques
50 based on electromagnetic sensors which allow the bulk electrical conductivity of soils σ_b to be
51 determined (Sheets and Hendrickx 1995, Corwin and Lesch 2005, Robinson et al. 2012,
52 Doolittle and Brevik 2014, Von Hebel et al. 2014, among many others).

53 σ_b depends on: (i) soil water content θ ; (ii) electrical conductivity of the soil solution (salinity)
54 σ_w ; (iii) tortuosity of the soil-pore system τ ; and (iv) other factors related to the solid phase such
55 as bulk density, clay content and mineralogy.

56 Electromagnetic induction (EMI) sensors provide measurements of the depth-weighted
57 apparent electrical conductivity EC_a accordingly to the specific distribution of the bulk electrical
58 conductivity σ_b as well as the depth response function of the sensor used (McNeill 1980). Thus,
59 the dependence on σ_b makes EC_a sensitive to soil salinity and water distributions. In principle,
60 specific procedures for estimating salinity and water content may be developed through
61 controlled laboratory experiments where σ_b , σ_w and θ are measured simultaneously (Rhoades
62 and Corwin 1981). That said, to monitor salinity and water content, it is crucial to correctly infer
63 the depth-distribution of σ_b from profile-integrated EC_a readings. To date, this issue has been
64 tackled by applying two different strategies: The first is to use empirical calibration relations
65 relating the depth-integrated EC_a readings to the σ_b values measured by alternative methods -
66 like Time-Domain Reflectometry (TDR) - within discrete depth intervals (Rhoades and Corwin,
67 1981; Lesch et al., 1992; Triantafilis et al., 2000; Amezketta, 2006; Yao and Yang, 2010; Coppola
68 et al. 2016); The second consists in the 1D inversion of the observations from the EMI sensor to
69 reconstruct the vertical conductivity profile (Borchers, et al., 1997; Hendrickx et al., 2002;
70 Santos et al., 2010; Lavoué et al., 2010; Mester et al., 2011; Minsley et al., 2012; Deidda et al.,
71 2014; Von Hebel et al., 2014).

72 With regard to EC_a inversion, a forward model still commonly used is the cumulative response
73 model or local-sensitivity model (LSM) (McNeill, 1980). McNeill's linear approach is well suited
74 to the cases characterized by an induction number B (defined as the ratio between the coil
75 distance and the skin depth) much smaller than 1. However, because of the increasing
76 computing power, improved forward modeling algorithms based on more accurate nonlinear
77 approaches are becoming increasingly common (Hendrickx et al., 2002; Deidda et al., 2014;
78 Deidda et al., 2003; Lavoué et al., 2010; Santos et al., 2010). For example, these more
79 sophisticated forward modeling codes can cope with a wider range of conductivities for which
80 the assumption $B \ll 1$ is not necessarily met.

81 To obtain reliable vertical distributions of electrical conductivity, the EC_a data used for the
82 inversion should consist of multi-configuration data. Hence, data collection should be
83 performed either with the simultaneous use of different sensors or with different acquisition
84 configurations with only one sensor (different configurations may consist, e.g., in different coil
85 orientations, varying intercoil separations and/or frequencies – see, for example Díaz de Alba
86 and Rodriguez, 2016). Multi-configuration data can be effectively used to invert for vertical
87 electrical conductivity profiling since the EC_a measures actually investigate different,
88 overlapping soil volumes. Devices specifically designed for the simultaneous acquisition of
89 multi-configuration data are currently available. Some of them consist of one transmitter and
90 several receivers with different coil separations and orientations (Santos et al., 2010). If,
91 instead, a sensor with single intercoil distance and frequency is available, a possible alternative
92 to having multi-configuration measurements could be to record the data at different heights
93 above the ground.

94 Unfortunately, like every other physical measurement, frequency-domain electromagnetic
95 measurements are sensitive to noise that is very hard to model effectively. Moreover as

96 discussed, for example, in Lavoué et al. (2010), Mester et al. (2011), and Von Hebel et al.
97 (2014), an instrumental shift in conductivity values could be observed due to system
98 miscalibration and the influence of surrounding conditions such as temperature, solar
99 radiation, power supply conditions, the presence of the operator, zero-leveling procedures,
100 cables close to the system and/or the field setup (see, amongst others, Sudduth et al., 2001;
101 Robinson et al., 2004; Abdu, et al., 2007; Gebbers et al., 2009; Nüscher et al., 2010). Hence, the
102 EC_a data from EMI measurements would generally require a proper calibration. One option
103 could be to use soil cores as ground-truth data. In this case, EC_a measurements at the sampling
104 locations can be compared against EC_a data predicted by the theoretical forward response
105 applied to the true electrical conductivity distribution measured directly on the soil cores
106 (Triantafyllidis et al., 2000; Moghadas et al., 2012). Clearly, this strategy is extremely time- (and
107 resource-) consuming. To avoid drilling, Lavoué et al. (2010) introduced a calibration method,
108 later also adopted by Mester et al. (2011) and Von Hebel et al. (2014), using the electrical
109 conductivity distribution obtained from Electrical Resistivity Tomography (ERT) data as input for
110 electromagnetic forward modeling. The EC_a values predicted on the basis of ERT data were
111 used to remove the observed instrumental shift and correct the measured conductivity values
112 by linear regression. However, in general, a prerequisite for such an approach concerns the
113 reliability of the inversion of the ERT result. This is not only due to the quality of the original
114 data, but also the adopted inversion procedure. Indeed, ERT inversion is an ill-posed problem:
115 its solutions are characterized by non-uniqueness and instability with respect to the input data
116 (Yu and Dougherty 2000; Zhdanov 2002; Günther 2011). In the Tikhonov regularization
117 framework, ill-posedness is addressed by including the available prior information. Such
118 information can be very general. For example, it can be geometrical (i.e., associated to the
119 presence of smooth or sharp boundaries between different lithologies). Obviously, the final

120 result largely reflects the initial guess formalized via the chosen regularization term (Pagliara
121 and Vignoli 2006; Günther 2011; Vignoli, Deiana, and Cassiani 2012; Fiandaca et al. 2015).
122 When relatively shallow depths have to be explored (1-2m), direct soil sampling and ERT can be
123 effectively replaced by TDR observations. TDR devices are designed to measure the dielectric
124 properties of soils. More precisely, they measure the apparent electrical permittivity, from
125 which, not only the dielectric constant, but also the effective electrical conductivity can be
126 deduced (e.g., Dalton et al., 1984; Topp et al., 1988; Weerts et al., 2001; Noborio, 2001; Jones
127 et al., 2002; Robinson et al., 2003; Lin et al., 2007; Thomsen et al., 2007; Huisman et al., 2008;
128 Lin et al., 2008; Koestel et al., 2008; Bechtold et al., 2010). In general, TDR measurements might
129 be difficult to be used to recover the electrical conductivity with the desired accuracy.
130 However, in the literature, many examples are reported in which, within the range 0.002 – 0.2
131 S/m (compatible with the examples investigated in the present research), and by properly using
132 the TDR device (e.g., by paying attention to minimize the effects of nonparallel device rods
133 inserted into the ground), the TDR conductivity can be measured with an uncertainty level
134 lower than 5% (e.g.: Huisman et al., 2008; Bechtold et al., 2010). Besides, since the TDR
135 measurements are commonly calibrated in saline solutions just before the field data
136 acquisitions, they could potentially provide a reliable, absolute estimation of the actual ground
137 conductivity (Ferré et al., 1998a). For this reason, in some cases, TDR observations have been
138 proposed as a valid tool for ground-truthing the ERT and, possibly, as ancillary information
139 source to constraint for the ERT inversions (Koestel et al., 2008). For additional studies dealing
140 with the use of ERT data for the validation of the EMI and TDR measurements for soil
141 characterization we refer the reader to, for example, Cassiani et al. (2012), and Ursino et al.
142 (2014).

143 In the present research, we focus on the use of TDR data to absolute calibrate the
144 conductivities obtained by inverting the EMI measurements. To do this, a dataset collected
145 during an experiment carried out along four transects under different salinity and water
146 content conditions (and monitored with both EMI and TDR sensors) is utilized. We first tackle
147 the problem of inferring the soil electrical conductivity distribution from multi-height EC_a
148 readings via the proper inversion strategy. Then we assess the quality of these reconstructions
149 by using TDR data as ground-truth. In this respect, in the following, we discuss how to
150 effectively compare the σ_b values generated by the EMI inversion with the associated TDR
151 values. In fact, as discussed by Coppola et al. (2016), because of their relatively smaller
152 observation volume, TDR data provide quasi-pointlike measurements and do not integrate the
153 small-scale variability (of soil water content, solute concentrations, etc.) induced by natural soil
154 heterogeneity. By contrast, EMI data necessarily overrule the small-scale heterogeneities seen
155 by TDR probes as they investigate a much larger volume. Accordingly, the paper provides a
156 methodology to calibrate EMI results by TDR readings. This procedure lies in conditioning the
157 original TDR data and in the statistical characteristics of the two EMI and TDR data series. On
158 the basis of the proposed analysis, we discuss the physical reasons for the differences between
159 EMI and TDR-based bulk electrical conductivity and identify a method to effectively migrate the
160 reliable TDR information across the larger volume investigated by EMI.

161

162 **Materials and Methods**

163 The experiment was carried out at the Mediterranean Agronomic Institute of Bari (MAIB) in
164 south-eastern Italy. The soil was pedologically classified as Colluvic Regosol, consisting of a
165 silty-loam layer of an average depth of 0.6 m on fractured calcarenite bedrock. The
166 experimental set-up (Fig. 1) consisted of four transects of 30 m length and 2.8 m width,

167 equipped with a drip irrigation system with five dripper lines placed 0.35 m apart and
168 characterized by an inter-dripper distance of 0.2 m. The dripper discharge was 2 l/h. Green
169 beans were grown in each transect. The irrigation volumes were calculated according to the
170 time-dynamics of water content in the first 0.25 m measured by a TDR probe inserted vertically
171 at the soil surface. TDR readings were taken: (i) just before and (ii) two hours after every
172 irrigation. Based on the difference between the water content at field capacity and that
173 measured just before irrigation, it was easy to assess the volumes needed to bring the soil
174 water content back to the field capacity.

175 The four transects were irrigated with water at two different salinity levels and with two
176 different water volumes. Transect 1: 100% of the irrigation water at 1 dSm⁻¹ (hereafter 100-
177 1dS); Transect 2: 50% of irrigation water at 1 dSm⁻¹ (50-1dS); Transect 3: 100% of the irrigation
178 water at 6 dSm⁻¹ (100-6dS); Transect 4: 50% of irrigation water at 6 dSm⁻¹ (50-6dS). Water
179 salinity was induced by adding calcium chloride (CaCl₂) to tap water. Irrigation volumes were
180 applied every two days.

181 EMI readings - in vertical magnetic dipoles configurations - were collected by using a Geonics
182 EM38 device (Geonics Limited, Ontario, Canada). The EM38 operates at a frequency of 14.6 kHz
183 with a coil spacing of 1 m, and with a nominal measurement depth of ~1.5 m (McNeill, 1980).
184 The lateral footprint of the EM38 measurement can be considered approximately equal to the
185 vertical one. Thus, the σ_b seen by the EMI, in a given depth-layer, necessarily differs from that
186 seen by a TDR probe at the same depth-layer, due to the very different spatial resolutions.

187 At the beginning of the measurement campaign, the EMI sensor was “nulled” according to the
188 manufacturer’s manual. Readings were taken just after each irrigation application at 1 m step,
189 along the central line of each transect, for an overall total of 26 soundings per transect. Multi-
190 height EM38 readings were acquired at heights of 0.0, 0.2, 0.4 and 0.6 m from the ground.

191 Taking measurements just after irrigation allowed relatively time-stable water contents to be
192 assumed at each site throughout the monitoring phases.

193 Just after the EM38 measurements, a TDR probe was inserted vertically at the soil surface in 26
194 locations, each corresponding to the central point of an EM38 reading. A Tektronix 1502C cable
195 tester (Tektronix Inc., Beaverton, OR) was used in this study. It enables simultaneous
196 measurement of water content θ and bulk electrical conductivity σ_b of the soil volume explored
197 by the probe (Heimovaara et al., 1995; Robinson and Friedman, 2003; Coppola et al., 2011;
198 Coppola et al., 2015). The TDR transmission line consisted of an antenna cable (RG58, 50 Ω
199 characteristic impedance, 2 m long and with 0.2 Ω connector impedance) and three-wire
200 probes, 0.25 m long, 0.07 m internal distance, and 0.005 m in diameter. The TDR probe was not
201 embedded permanently at fixed depths along the soil profile to avoid any potential disturbance
202 to the EMI acquisitions. The TDR readings were taken at three different depth intervals (0.0-
203 0.2, 0.2-0.4, 0.4-0.6 m). After the measurements at the surface (0.0-0.2 m), a trench was dug up
204 to 0.2 m depth. TDR probes were then inserted vertically for the additional collection of the
205 data in the interval 0.2-0.4 m, after which the trench was deepened up to 0.4 m and readings
206 were taken at 0.4-0.6 m. The $\sigma_{b,TDR}$ readings were used for the calibration of the EM38 inversion
207 results.

208

209 Data Handling

210 *Multi-height EMI readings inversion*

211 Nonlinear 1D forward modeling, which predicts multi-height EMI readings from a loop-loop
212 device, can be obtained by suitable simplification of Maxwell's equations that takes the
213 symmetry of the problem into account. This approach is described in detail in (Hendrickx et al.
214 2002), and is based on a classical approach extensively described in the literature (Wait 1982;

215 Ward and Hohmann 1988). The predicted data are functions of the electrical conductivity and
216 the magnetic permeability in a horizontally layered medium.

217 When the coils of the recording device are vertically oriented with respect to the ground
218 surface, the reading at height h can be expressed by using the integral:

$$-\rho^3 \int_0^{\infty} \lambda^2 e^{-2h\lambda} R_0(\lambda) J_0(\rho\lambda) d\lambda, \quad (1)$$

219 where ρ denotes the distance between the coils, $J_0(\lambda)$ is the Bessel function of the first kind
220 of order 0, and $R_0(\lambda)$ is a complex valued function which depends upon the electromagnetic
221 properties of the ground layers. A similar expression is valid also when the coils are horizontally
222 aligned. Hence the dependence of the measured data on the electrical conductivity σ_k , of the
223 (homogeneous) j -th layer is incorporated into the function $R_0(\lambda)$. We discretize the problem
224 with n layers whose characteristic parameters σ_j (with $j = 1, \dots, n$) are the unknowns we invert
225 for. In the present research, we neglect any dependence of the electromagnetic response on
226 magnetic permeability as we assume it is fixed and equal to the permeability of empty space. In
227 principle, it is possible to consider two measurements for each location: one for the horizontal
228 and one for the vertical configuration of the transmitting and receiving loops. In this case, the
229 data used as inputs for the inversion are $2 \cdot m$, with m representing the number of heights $h_1,$
230 h_2, \dots, h_m where the measurements are performed.

231 A least squares data fitting approach leads to the minimization of the function:

$$f(\sigma) = \frac{1}{2} \sum_{i=1}^{2m} r_i^2(\sigma), \quad (2)$$

232 where $\sigma = (\sigma_1, \dots, \sigma_n)^T$, and $r_i^2(\sigma)$ is the misfit between the i -th measurement and the
233 corresponding forward modeling prediction based on Eq. 1.

234 We solve the nonlinear minimization problem by the inversion procedure described in Deidda
235 et al. (2014). The algorithm is based on a damped regularized Gauss-Newton method. The
236 problem is linearized at each iteration by means of a first order Taylor expansion. The use of
237 the exact Jacobian (Deidda et al., 2014) makes the computation faster and more accurate than
238 using a finite difference approximation. The damping parameter is determined in order to
239 ensure both the convergence of the method and the positivity of the solution. The regularized
240 solution to each linear subproblem is computed by the truncated generalized singular value
241 decomposition (TGSVD - Díaz de Alba and Rodriguez, 2016) employing different regularization
242 operators. Besides the classical regularization matrices based on the discretization of the first
243 and second derivatives, to further improve the spatial resolution of EMI inversion results in all
244 the cases characterized by sharp interfaces, we tested a nonlinear regularization stabilizer
245 promoting the reconstruction of blocky features (Zhdanov, Vignoli, and Ueda 2006; Ley-Cooper
246 et al. 2015; Vignoli et al. 2015; Vignoli et al. 2017). The advantage of this relatively new
247 regularization is that, when appropriate prior knowledge about the medium to reconstruct is
248 available, it can mitigate the smearing and over-smoothing effects of the more standard
249 inversion strategies. This, in turn, can make the calibration of the EMI data against the TDR data
250 more effective. For this reason, in the following, the EMI results used for our assessments are
251 those inferred by means of this sharp inversion. The differences between the “standard”
252 smooth (based on the first derivative) reconstruction and the sharp one are clearly shown in
253 Fig.s 2 and 4. In all cases, the inversions are performed with a 100-layer homogeneous
254 discretization, down to 8 m, with fix interfaces. We opted for such a parameterization to be
255 able to: (i) control the inversion results by acting merely on the regularization parameters, and
256 (ii) remove the regularization effects possibly originated by the discretization choice (e.g., the
257 number of layers, interfaces locations). In this way, it was possible to use an automatic strategy

258 for the selection of the regularization parameters. In Fig.s 2 and 4, the sharp results (upper
259 panels) associated with the cases 100-6dS and 50-6dS are compared against the corresponding
260 smooth inversions (middle panels). Even if the data misfit levels largely match (lower panels in
261 Fig.s 2 and 4, but also Fig.s 3 and 5), the two inversion strategies produce reconstructions that
262 differ significantly. This is due to the inherent ill-posedness of the EMI inversion. By considering
263 solely the geophysical observations, it is impossible to decide which model is the best. In this
264 research, based on the fact that, just after the irrigation, the effect of the water is supposed to
265 remain localized in the shallowest portion of the soil section, the sharp inversion was found to
266 provide more reliable results. Moreover, to some extent, the general better agreement of the
267 data calculated from the sharp model supports the idea that the electrical properties
268 distributions are better inferred via the sharp regularization. In any case, since in this research
269 we calibrate the EMI-derived models (and not the data), the final calibrated result will reflect
270 the assumptions made in the first place, when the EMI data are inverted (specifically, the
271 regularization assumptions).

272 A possible alternative way to still effectively use the TDR data to calibrate the EMI
273 measurements (and not the associated conductivity model) could consist in performing the
274 calibration in the data-space (and not in the model-space). In the data-space calibration, the
275 measured TDR conductivity could be used as input model to calculate the EC_a response of the
276 EMI device actually used. In turn, this calculated EC_a response can be compared against the
277 measured EMI data and used for their calibration. However, eventually, also this latter data-
278 space calibration will have to deal with the inversion issues once the calibrated EMI data need
279 to be converted into conductivities σ_b . In this paper, we chose the model-space calibration
280 strategy as, in general, in the available EMI inversion codes, it is not always easy to decouple
281 the forward modelling routines from the overall inversion algorithm. Hence, the discussed

282 approach could be more directly applicable and beneficial for practitioners. On the other hand,
283 it is true that the data-space calibration naturally takes into account the scale-mismatch
284 between the TDR and the EMI measurements with no need for any statistical calculation.
285 It is worth noting that the constant magnetic permeability assumption is not always valid.
286 Inverting for the magnetic permeability is sometimes not only necessary, but it can also provide
287 an additional tool for soil characterization (e.g., Beard and Nyquist, 1998; Farquharson et al.,
288 2003; Sasaki et al., 2010; Guillemoteau et al. 2016; Noh et al. 2017; Deidda et al., 2017).
289 For the sake of clarity, hereafter, the σ_b values generated from the EMI data inversion will be
290 identified explicitly as $\sigma_{b,EMI}$.

291

292 *TDR-based water content and bulk electrical conductivity*

293 The Tektronix 1502C can measure the total resistance R_t of the transmission line by:

$$R_t = Z_c \frac{(1 + \rho_\infty)}{(1 - \rho_\infty)} = R_s + R_c \quad (3)$$

294 where: R_s is the soil's contribution to total resistance and R_c accounts for the contribution of
295 the series resistance from the cable; the connector Z_c is the characteristic impedance of the
296 transmission line; and ρ is a reflection coefficient at a very long time, when the waveform has
297 stabilized.

298 The σ_b value at 25°C can be calculated as (Rhoades and van Schilfgaarde 1976; Wraith et al.
299 1993):

$$\sigma_{b,25^\circ\text{C}} = \frac{K_c}{Z_c} f_T \quad (4)$$

300 where K_c is the geometric constant of the TDR probe and f_T is a temperature correction factor
301 to be used for values recorded at temperatures other than 25°C. Both Z_c and K_c can be

302 determined by measuring R_t with the TDR probe immersed in a solution with known
 303 conductivity σ_b . Hereafter, these σ_b measurements will be identified as $\sigma_{b,TDR}$.

304

305 *Evaluation of Concordance between $\sigma_{b,TDR}$ measurements and $\sigma_{b,EMI}$ estimates*

306 The agreement between $\sigma_{b,TDR}$ measurements and $\sigma_{b,EMI}$ estimations in the 0.0-0.6 m range was
 307 evaluated by the Concordance Correlation Coefficient, ρ_L :

$$\rho_L = \frac{2s_{xy}}{z_x^2 + z_y^2 + (m_x - m_y)^2} \quad (5)$$

308 where m_x , m_y , s_x , s_y , s_{xy} are means, standard deviations and covariances of the two data series
 309 ($x = \sigma_{b,EMI}$; $y = \sigma_{b,TDR}$), respectively.

310 Scatter plots of the $\sigma_{b,EMI}$ and $\sigma_{b,TDR}$ data series (both original and filtered) were evaluated by
 311 the line of perfect concordance (1:1 line) and the reduced major axis of the data (RMA)
 312 (Freedman et al., 1991). The method combines measurements of both precision and accuracy
 313 to determine how close the two data series are to the line of perfect concordance $\sigma_{b,EMI} = \sigma_{b,TDR}$.

314 Compared to the classical Pearson correlation coefficient, ρ_p :

$$\rho_p = \frac{s_{xy}}{s_x s_y}, \quad (6)$$

315 ρ_L not only measures the strength of linear relationship (how close the data in the scatter plot
 316 are to a line), but also the level of agreement (how close that line is to the line of perfect
 317 agreement, the 1:1 line). In this sense, ρ_L may also be calculated as (Cox, 2006):

$$\rho_L = \rho_p C_b,$$

$$C_b = \frac{2}{(v+1/v+u^2)}, \quad (7)$$

$$v = s_x / s_y,$$

318 and

$$u = (m_x - m_y) / \sqrt{s_x s_y},$$

319 where C_b is the bias correction factor measuring how far the best-fit line deviates from the 1:1
320 line. The maximum value of $C_b = 1$ ($0 < C_b < 1$) corresponds to no deviation from the line. The
321 smaller C_b is, the greater the deviation from the line. In other words, C_b is a measure of
322 accuracy (how much the average estimate differs from the average measurement value,
323 assumed to be the true value) and refers to the systematic error, whereas ρ_p is a measure of
324 precision (measures the variability of measurements around their own average) and refers to
325 the random error. The RMA line is given by:

$$y = (m_y - \beta m_x) + \beta x = \alpha + \beta x. \quad (8)$$

326 This line passes through the means of the x and y values and has slope given by the sign of
327 Pearson's correlation coefficient, ρ_p , and the ratio of the standard deviations, s , of the two
328 series (Freedman et al., 1991; Corwin and Lesch, 2005):

$$\beta = s_y / s_x. \quad (9)$$

329 ρ_L increases in value as (i) the RMA approaches the line of perfect concordance (a matter of
330 accuracy) and (ii) the data approach the RMA (a matter of precision). In the ideal case of
331 perfect concordance, the intercept of the RMA, α , should be 0 and β should be 1. Therefore, α
332 $\neq 0$ or $\beta \neq 1$ indicate additive and/or multiplicative biases (location and/or scale shifts). The
333 concordance was evaluated for the original TDR data, as well as for the filtered TDR data. For
334 the analysis described in detail later in the paper, it is worth noting that the coefficients α and β
335 depend only on the statistical characteristics (mean and standard deviation) of the two series,
336 as $\alpha = m_y - \beta m_x$ and $\beta = s_y / s_x$.

337

338 *Fourier filtering*

339 Because of their relatively small observation volume ($\sim 10^{-3} \text{ m}^3$), TDR sensors provide quasi-
340 pointlike measurements and are, thus, more effective in capturing small-scale variability (in
341 water content, solute concentrations) induced by natural soil heterogeneity. Thus, the
342 variability within a set of TDR readings is expected to originate from a combination of small and
343 large-scale heterogeneities (high and low spatial frequency components). By contrast, the EMI
344 measurements (because of the size and physics of the instrumentation) necessarily integrate
345 out the small-scale variability at the TDR scale of investigation.

346 Hence, in order to make the two datasets comparable, the original spatial TDR data series need
347 to be filtered to remove the variation from small-scale heterogeneities (recorded only by the
348 TDR probe). In this way, only the information at a spatial scale equal to or larger than the
349 observation volume of both sensors is preserved.

350 Thus, a simple filter based on the Fourier Transform (FT) is applied to the TDR series. So, a low-
351 pass frequency filtering is performed on the TDR data to remove all components related to the
352 small-scale heterogeneities and make it comparable with the EMI measurements. More
353 specifically, for each transect, we consider the $\sigma_{b,EMI}$ reconstruction and, for each of its 1D
354 models, calculate the average conductivity value within each depth interval for which the TDR
355 data are available (namely: 0.0-0.2 m, 0.2-0.4 m, 0.4-0.6 m). Hence, for each depth interval,
356 along the entire transect, we can calculate the mean and standard deviation of the conductivity
357 values retrieved from the EMI observations. Subsequently, this standard deviation (associated
358 with the EMI data) is compared with the standard deviation of the iteratively low-pass filtered
359 TDR data for the same depth interval. In this way, an optimal cut-off frequency can be selected
360 to make the scales of the two kinds of measurements compatible. Figure 6 shows the
361 comparison between the standard deviations of the EMI and filtered TDR data, for the 50-6dS

362 transect, at 0.2-0.4 m depth. In this specific case, the selected cut-off frequency to filter the
363 TDR data is 0.313 cycles/m, corresponding to a 3.2 m range. This is not surprising at this is of
364 the order of magnitude of the footprint of the EMI measurements.

365

366 **Results and Discussion**

367 Hereafter, the original and filtered data will be respectively labeled ORG and FLT. The graphs on
368 the top panels in Fig. 7 compare $\sigma_{b,TDR}$ measured by TDR against the corresponding conductivity
369 $\sigma_{b,EMI}$ retrieved by the EMI (sharp) inversion for the all the transects. From the left, the graphs
370 refer respectively to the transects identified as 100-6dS, 50-6dS, 100-1dS and 50-1dS. All plots
371 show the data for the entire investigated profile between 0.0 and 0.6 m, together with the line
372 of perfect concordance (1:1, black line), and the main regression axis (MRA, red line).

373 The general conclusion is that, in all four transects, and for all three considered depth-layers,
374 the $\sigma_{b,EMI}$ values underestimate the $\sigma_{b,TDR}$ measurements, such that the MRA line generally lies
375 above the 1:1 line. Not surprisingly, the EMI result seems quite insensitive to TDR variability.
376 Also, a considerable scatter around the MRA line may be observed for all transects.

377 Table 1 shows the MRA coefficients (C_b , α , β), as well as the Pearson, ρ_p , and the concordance
378 correlation, ρ_L , for the three depth-layers and for all four transects investigated. We recall that
379 the bias correction factor C_b , the slope β , and the intercept α should be respectively close to 1,
380 1 and 0, for the MRA to approximate the line of perfect concordance. For all the transects and
381 all the depth-layers considered, the parameters confirm the relatively loose relationship
382 between $\sigma_{b,EMI}$ and $\sigma_{b,TDR}$ already observed in the graphs, both in terms of accuracy (the distance
383 of the MRA line from the 1:1) and precision (the data scatter around the MRA line).

384 Von Hebel et al. (2014) found a similar behavior when comparing their EMI and ERT datasets. In
385 that case, the EC_a values measured by EMI systematically underestimated the EC_a generated by

386 applying EMI forward modeling to the σ_b distribution retrieved by ERT. To remove the bias, the
387 authors performed a linear regression between measured and predicted EC_a after applying a
388 ten-term moving average to the original data. By using the regression coefficients, all the
389 measured EC_a values were converted to ERT-calibrated EC_a values.

390 Here, we follow a different approach to calibrate the $\sigma_{b,EMI}$ values against the $\sigma_{b,TDR}$
391 measurements based on the MRA coefficients and, so, on the statistical parameters (mean and
392 standard deviation) of the two data series. Specifically, the present approach looks for a
393 systematic correction of the bias based on well-defined statistical sources of the discrepancies.
394 In short, the proposed method performs the calibration in the σ_b model-space, instead of the
395 EC_a data-space. Our model-space approach mostly relies on the statistical parameters of the
396 two series. Analyzing the role of these statistics in explaining the discrepancies between EMI
397 and TDR data observed in Fig. 7a may help to understand how they can be effectively used for
398 making EMI results directly comparable with the TDR values.

399 In nearly all of the graphs in the top panels in Fig. 7, the discrepancies between $\sigma_{b,EMI}$ and $\sigma_{b,TDR}$
400 values can be decomposed in the following components:

- 401 1. The distance along the $\sigma_{b,EMI}$ axis of the MRA line from the 1:1 line, that is the difference
402 between the $\sigma_{b,EMI}$ and the $\sigma_{b,TDR}$ means.
- 403 2. The difference in the slope of the MRA and of the 1:1 lines, which stems from the different
404 variability of $\sigma_{b,EMI}$ (its standard deviation) and that of $\sigma_{b,TDR}$. We recall here that the slope of
405 the MRA is just the ratio of the two standard deviations, $\hat{\beta} = s_y / s_x$.
- 406 3. The scatter of the data around the MRA line, which may come from different sensors' noise
407 and the influence of surrounding conditions (e.g., temperature).

408 Below, we analyze in detail the role of all these three points with the support of the measured
409 data.

410 1. The distance of the MRA from the 1:1 line is mostly due to the difference in the observed
411 means. The plot in Figure 8a compares the means for the two original series (squares-solid line
412 for TDR, circles-dashed line for EMI). Figure 8b reports the same comparison on a 1:1 plot
413 (triangles-solid regression line). The mean values confirm the general underestimation of TDR
414 by the EMI data. However, the trends are evidently similar, which is reflected in the high
415 correlation between the means of the two series, with a significantly high $R^2=0.81$. This high
416 correlation has very positive implications from an applicative point of view, since, after the
417 calibration in a specific site, it allows the EMI mean to be inferred given the mean of TDR
418 readings taken in that soil, and thus provides the possibility to migrate the more reliable TDR
419 information across the larger area that can be practically investigated during an EMI survey.

420 2. The different slope of the two lines has to be ascribed to the different variability of the two
421 series. Figure 9a compares the standard deviations for the two original series (squares-solid line
422 for TDR, circles-dashed line for EMI). Figure 9b reports the same comparison on a 1:1 plot
423 (triangles-solid regression line). Conceptually, the different variability of the two series can be
424 related to the different sensor observation volumes (originated from the different spatial
425 sensitivity of the sensors - Coppola et al. 2016). For TDR probes, most of the measurement
426 sensitivity is close to the rods (Ferré et al. 1998b). Conversely, the spatial resolution of inverted
427 EMI EC_a values may be much lower as the resolution of the EMI result depends on the physics
428 of the method, the specifications (and configuration) of the recording device, and the
429 regularization strategy applied during the inversion. Thus, the EMI is generally unable to
430 capture the small-scale variability seen by the TDR. For our calibration purposes, it is important
431 to make the variability of EMI and TDR conductivities actually comparable. As discussed by

432 Coppola et al. (2016), a possible method can consist in filtering out the high frequency
433 components (at small spatial scale) of the original TDR data, while retaining the lower
434 frequency information. This corresponds to keep the information at a spatial scale larger than
435 the observation volume of the TDR sensor and attuned with the resolution of the $\sigma_{b,EMI}$
436 distribution. From a practical point of view, this makes sense, as TDR readings are often “too
437 local” to actually represent the macroscopic physical characteristics of interest for applications
438 (water content, solute concentrations). The volume explored by a TDR probe may, or may not,
439 include preferential channels (Mallants et al., 1994; Oberdörster et al., 2010), stones (Coppola
440 et al., 2011; Coppola et al., 2013), small-scale changes in the texture and structure (Coppola et
441 al., 2011), which can make the interpretation of local measurements difficult for practical
442 applications. In this sense, EMI’s removal of these small-scale effects may be desirable from a
443 management perspective. Consistently, the original TDR data are conditioned via a low-pass
444 filtering, as described in the Data Handling section. The filtering results, in terms of standard
445 deviations, are reported in Fig. 9a (crosses-dashed line) and Fig. 9b (squares-dashed regression
446 line). As expected, the low-pass filter makes the standard deviations much closer (almost
447 overlapping) in all transects and all considered depth-layers. The regression improved
448 significantly from 0.25 for the original data to 0.78 after the TDR data filtering.

449 3. The scatter is consistently reduced by the spatial filtering (as similarly discussed in Von Hebel
450 et al., 2014).

451

452 Eventually, the calibrated $\sigma_{b,EMI}^{rg}$ distribution (superscript *rg* means: EMI data after regression)
453 can then be obtained from the original $\sigma_{b,EMI}$ via the linear mapping:

$$454 \quad \sigma_{b,EMI}^{rg} = \alpha + \beta \sigma_{b,EMI}, \quad (10)$$

455 where the coefficients α and β can be easily calculated from the means and standard
 456 deviations of the EMI results and the filtered TDR data. Thus, if m_{EMI} and $m_{TDR(FLT)}$, and s_{EMI} and
 457 $s_{TDR(FLT)}$ are, respectively, the means and the standard deviations of the original $\sigma_{b,EMI}$ EMI data
 458 and of the filtered $\sigma_{b,TDR(FLT)}$ TDR data, the MRA line coefficients can be expressed as
 459 $\alpha = m_{TDR(FLT)} - \beta m_{EMI}$ and $\beta = s_{TDR(FLT)} / s_{EMI}$.

460 The bottom panels in Fig. 7 show the results of the application of the linear mapping. In
 461 particular, they compare the calibrated EMI data (EMI rg) with the filtered TDR (TDR FLT)
 462 measurements. The MRA parameters and the concordance coefficients in the case of filtered
 463 TDR data are reported in Table 2. Clearly, considering the (calibrated) EMI and (filtered) TDR
 464 standard deviations turns the MRA line to be practically matching the 1:1 line, with the
 465 coefficient β approaching to 1. Moreover, from Table 2, the improvement of the bias C_b and the
 466 concordance ρ_L is generally significant. On the other hand, the Pearson's correlation ρ_P is not
 467 influenced by the recalibration as the proposed approach deals with the statistics of the data
 468 series rather than the single data. Thus, after the application of the low-pass filter to the TDR
 469 data, the coefficient β is close to 1, and the calibration turns out to be (almost) a simple shift of
 470 the inverted $\sigma_{b,EMI}$. The amount of this shift is equal to the difference between the mean values
 471 $m_{TDR(FLT)}$ and m_{EMI} . To summarize, the TDR filtering allows removing the outlier values generated
 472 by the small scale variability and preserving the information content necessary to properly
 473 calculate the shift required for the absolute calibration of the EMI inversion results.

474 Figure 10 shows, on the left, the original $\sigma_{b,EMI}$ distribution to be compared against the $\sigma_{b,EMI}^{rg}$
 475 results (on the right) obtained through the application of the linear transformation in Eq. 10.
 476 The calibrated transects preserves the spatial variability of the original EMI inversions, but are
 477 now characterized by value ranges that are more realistic (as they are obviously closer to the

478 TDR measurements assumed to be more representative of the real soil conditions). The results
479 in Fig. 10 obviously reflect the experimental irrigation set-up. Hence, not surprisingly, the
480 conductivity of the 100-6dS case (irrigated with 100% of the water at 6 dSm^{-1}) is the most
481 effected (Fig. 10d), while the 50-1dS case (corresponding to an irrigation with 50% of the water
482 at 1 dSm^{-1}) is the example with the lowest conductivity range (Fig. 10g). The intermediate
483 irrigation tests 50-6dS (Fig. 10e) and 100-1dS (Fig. 10f) show very similar maximum and
484 minimum conductivity values over the two transects. However, there is a difference concerning
485 the spatial distributions. In particular, in the 100-1dS case, the highest $\sigma_{b,EMI}^{rg}$ values
486 characterize not only the shallower 0.0 - 0.1 m portion (Fig. 10f), but they appear to spread
487 almost homogeneously all over the section. On the contrary, in the 50-6dS test, the maximum
488 values are limited to the first soundings at the beginning of the transect and to the 0.2 - 0.4 m
489 depth interval. More important, if we compare the original 50-6dS (Fig. 10b) and 100-1dS (Fig.
490 10c) conductivity distributions against the corresponding calibrated results (Fig. 10e and Fig.
491 10f), the original $\sigma_{b,EMI}$ section, which used to be the generally most conductive one (50-6dS,
492 Fig. 10b), is now the most resistive (Fig. 10e) and vice versa. This, one more time, demonstrates
493 that the proper calibration may lead to significantly different conclusions.

494 As already discussed, the high correlation of the means and the standard deviations of the two
495 series are central for this procedure to be of practical interest. In short, the procedure can be
496 summarized as follows: (i) An area is monitored via EMI survey and a few TDR calibration
497 measurements are collected concurrently. (ii) The availability of the two different datasets
498 allows performing the regression for the mean and the standard deviation of the original EMI
499 inversion results and the filtered TDR data, like those shown in Figs 8b and 9b. (iv) These
500 statistical parameters can be promptly used for the calculation of the coefficients α and β to be

501 inserted into Eq. 10. (v) The original EMI inversion results are not always reliable when
502 compared with the direct measurements obtained by using a TDR probe. Rather, they only
503 contain the low-frequency information supplied by TDR (most likely, together with some shifts
504 connected with the poor absolute calibration of the EMI system and/or the working conditions,
505 e.g., the temperature). Thus, for quantitative analyses, it may be crucial to transform the
506 original EMI result $\sigma_{b,EMI}$ into a new, calibrated section $\sigma_{b,EMI}^{rg}$ by means of the linear mapping
507 in Eq. 10.

508 The proposed workflow enables us to translate the original non-calibrated $\sigma_{b,EMI}$ data into the
509 actual σ_b we would collect in ideal conditions, and which would perfectly match “low-
510 resolution” TRD measurements. $\sigma_{b,EMI}^{rg}$ is our best possible estimation of the true electrical
511 conductivity at the scale of investigation of the EMI survey: it is the original $\sigma_{b,EMI}$ after the
512 application of the appropriate rescaling and shifts deduced by the more reliable and absolutely
513 calibrated TDR measurements.

514

515 **Conclusions**

516 The objective of the paper is to infer the bulk electrical conductivity distribution in the root
517 zone from multi-height (potentially non-calibrated) EMI readings. TDR direct measurements are
518 used as ground-truth σ_b data to evaluate the correctness of the σ_b estimations generated by
519 EMI inversion. For all four transects and for all three depth-layers considered in this study, the
520 $\sigma_{b,EMI}$ values underestimate the $\sigma_{b,TDR}$ measurements, such that the MRA line generally lies
521 above the 1:1 line. Also, a considerable scatter around the MRA line was observed for all
522 transects.

523 The proposed analysis allows discussing the physical reasons for the differences between EMI-
524 and TDR-based electrical conductivity and developing an approach to calibrate the original
525 $\sigma_{b,EMI}$ by using the $\sigma_{b,TDR}$ measurements. Our approach is based on the MRA coefficients and,
526 hence, on the statistical parameters (mean and standard deviation) of the two series.
527 Specifically, the approach looks for a systematic correction of the bias based on well-defined
528 statistical sources of the discrepancies. A low-pass filtering has been carried out on the TDR
529 data to obtain a significantly high correlation between the standard deviations of the two data
530 series. After that, a simple linear transformation can be applied to the originally inverted EMI
531 section $\sigma_{b,EMI}$ to get a calibrated σ_b result.

532 The proposed strategy lies on the assumption that TDR direct measurements supply absolutely
533 calibrated observations of the electrical conductivity of the soil and can be effectively used to
534 calibrate the conductivity distributions inferred from EMI data. The availability of EMI
535 calibrated data paves the way to reliable reconstructions of the electrical conductivity
536 distribution over large areas (typical for EMI surveys, but not for TDR campaigns) unaffected by
537 the usual EMI miscalibrations. This, in turn, can result in the possibility of effective time-lapse
538 surveys and/or in consistent merging of subsequent surveys.

539 On the other hand, the proposed statistical workflow for making the TDR measurement
540 comparable with the associated EMI results provides a more sophisticated approach than
541 simple smoothing to upscale the TDR data. Thus, from the opposite perspective, the approach
542 in question can be used to tackle the problems connected with handling the TDR data
543 characterized by excessively high spatial resolution.

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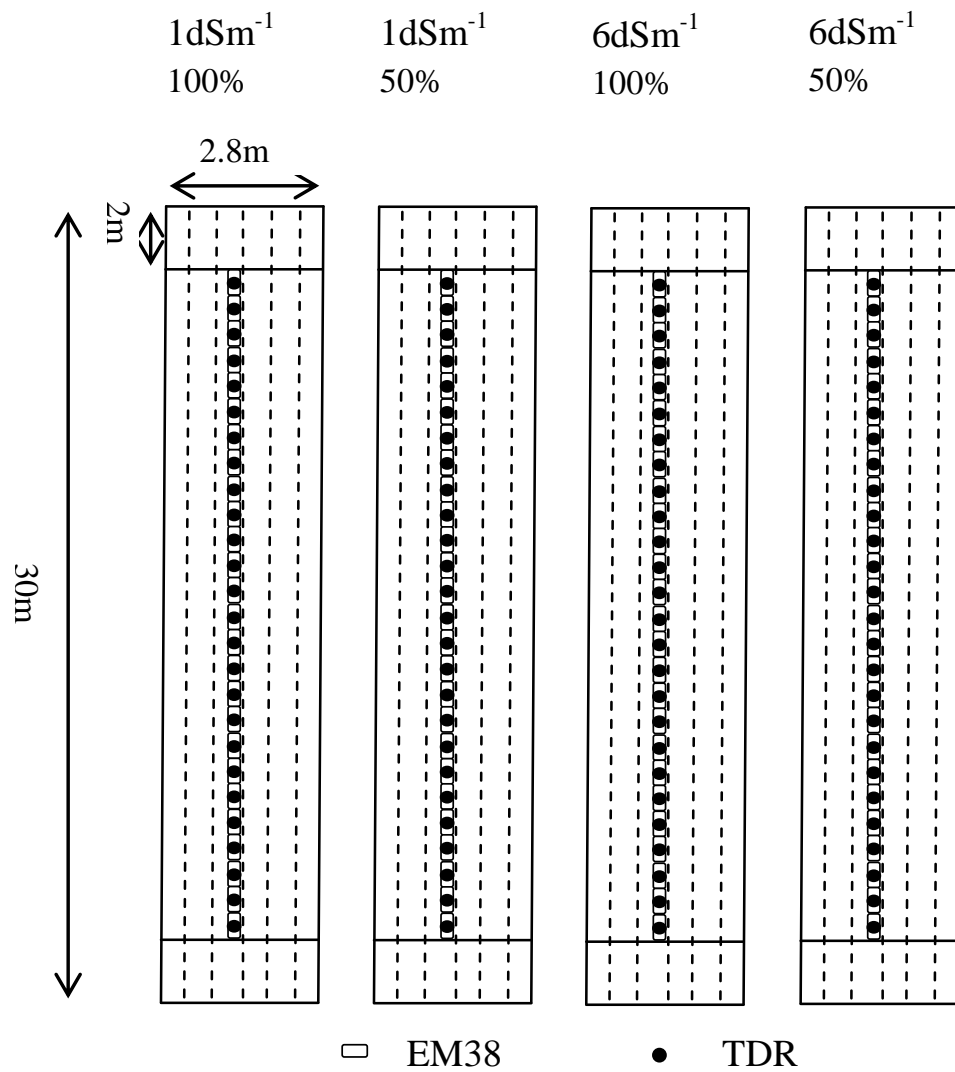
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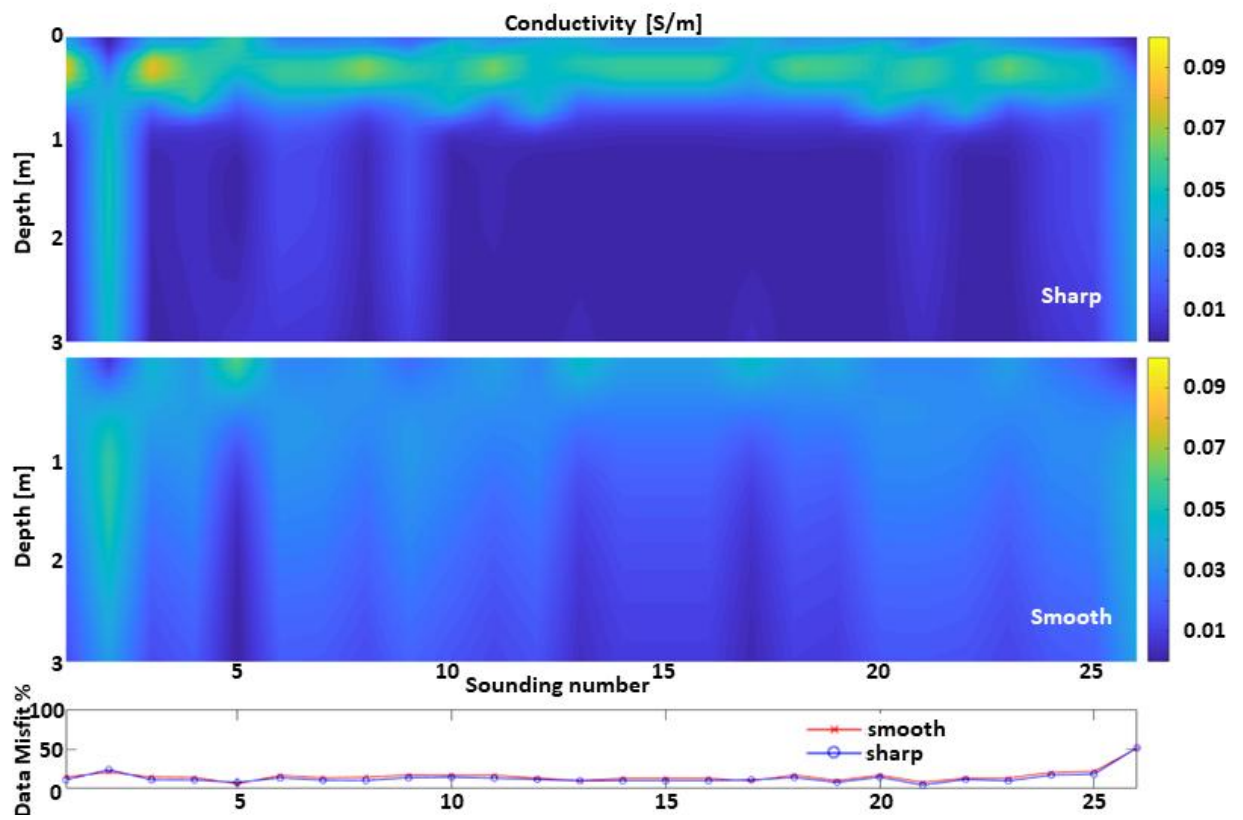
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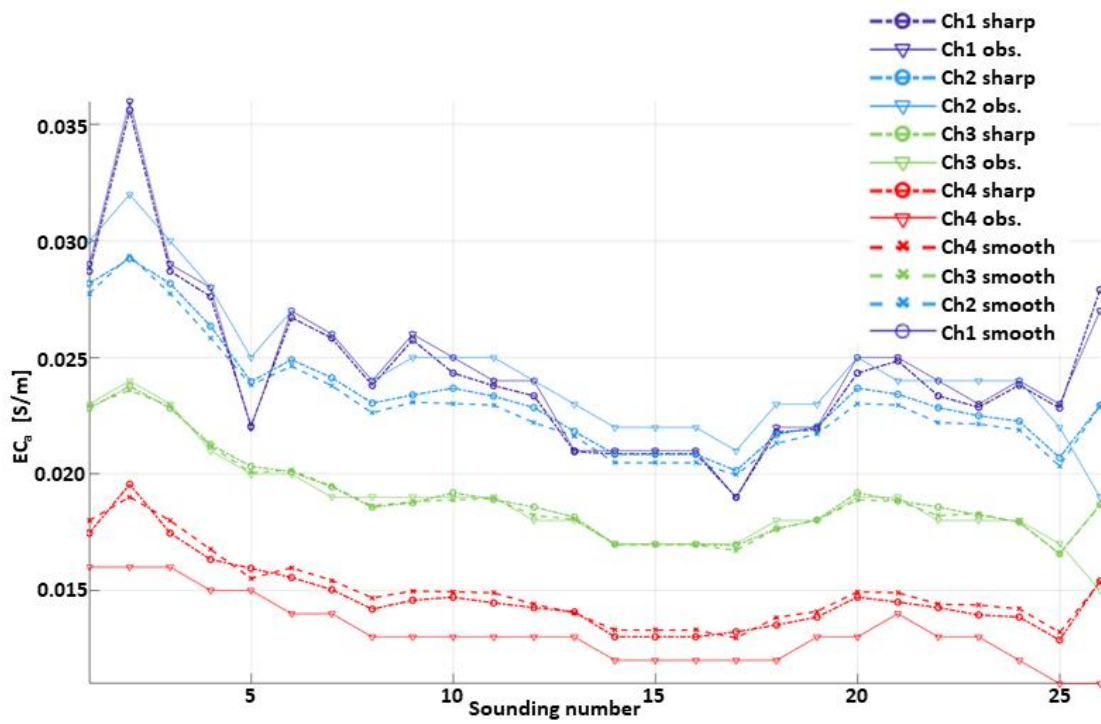
812 Figure 1. Schematic view of the experimental field



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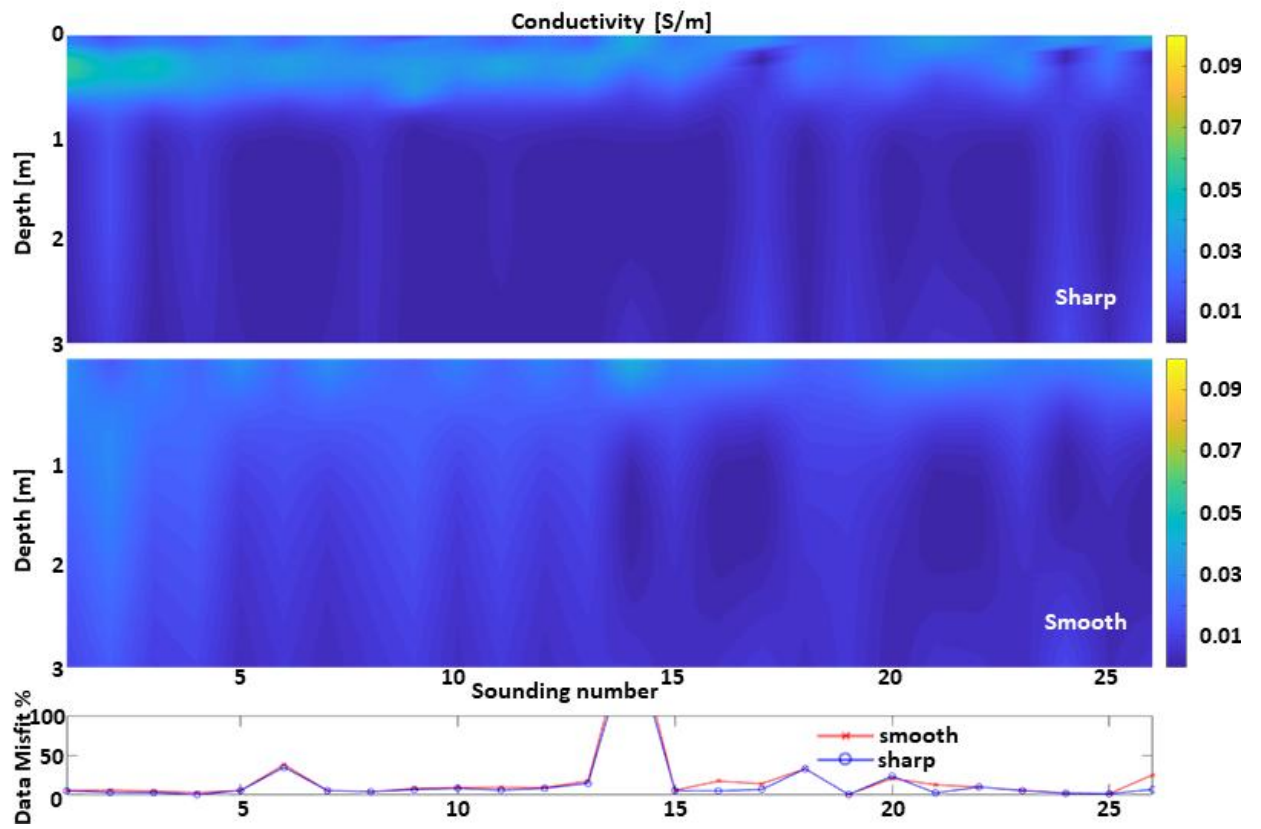
814 Figure 2. Examples of sharp and smooth inversions applied to the dataset 100-6dS. The results

815 are shown together with their corresponding data misfit.



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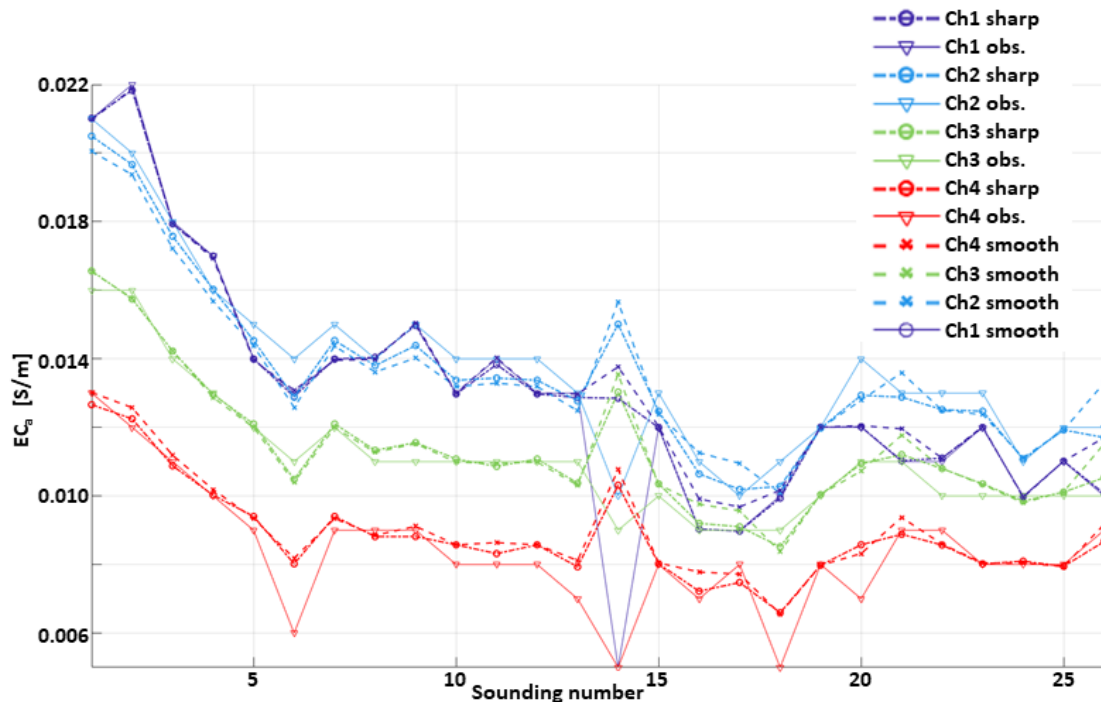
817 Figure 3. Comparison of the data fitting associated with the sharp and smooth inversions
 818 applied to the dataset 100-6dS (Fig. 2). The calculated data corresponding to the sharp and
 819 smooth results are shown together with the observations for each of the four measured
 820 channels (heights).



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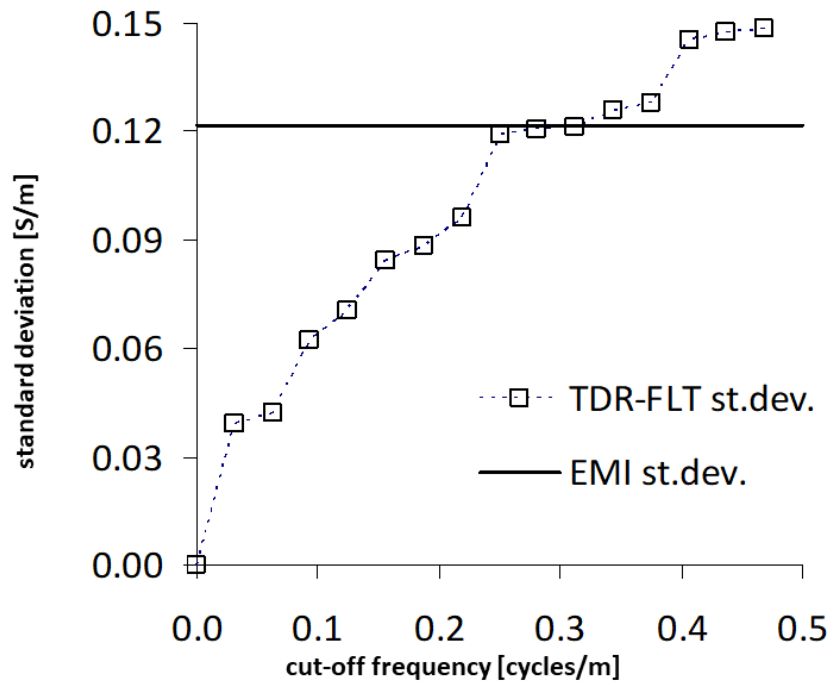
822 Figure 4. Examples of sharp and smooth inversions applied to the dataset 50-6dS. The results

823 are shown together with their corresponding data misfit.



824

825 Figure 5. Comparison of the data fitting associated with the sharp and smooth inversions
 826 applied to the dataset 50-6dS (Fig. 4). The calculated data corresponding to the sharp and
 827 smooth results are shown together with the observations for each of the four measured
 828 channels (heights).



829

830 Figure 6. Standard deviation of the EMI series (horizontal black line) for the 50-6dS transect at
 831 0.2-0.4 m depth. The squares show the corresponding standard deviations for the TDR series
 832 for different level of filtering. The intersection of the EMI line with the TDR curve allows
 833 identifying the optimal cut-off frequency range (~0.313 cycles/m) to make the two standard
 834 deviations similar.

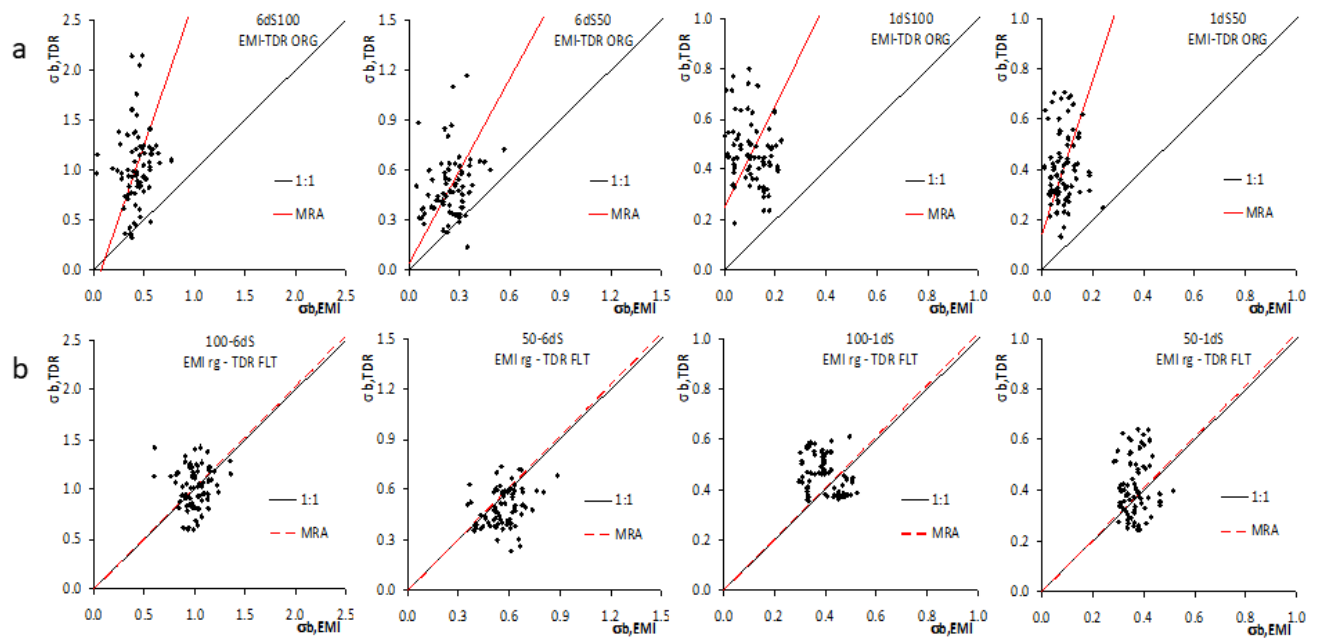


Figure 7. Comparison between $\sigma_{b,TDR}$ and $\sigma_{b,EMI}$ for all four transects for the depth range 0.0-0.6 m. The graphs in the top panels (a) show the original TDR and EMI data, while those in the bottom panels (b) the Filtered (FLT) TDR and EMI data after the regression based on MRA parameters (rg).

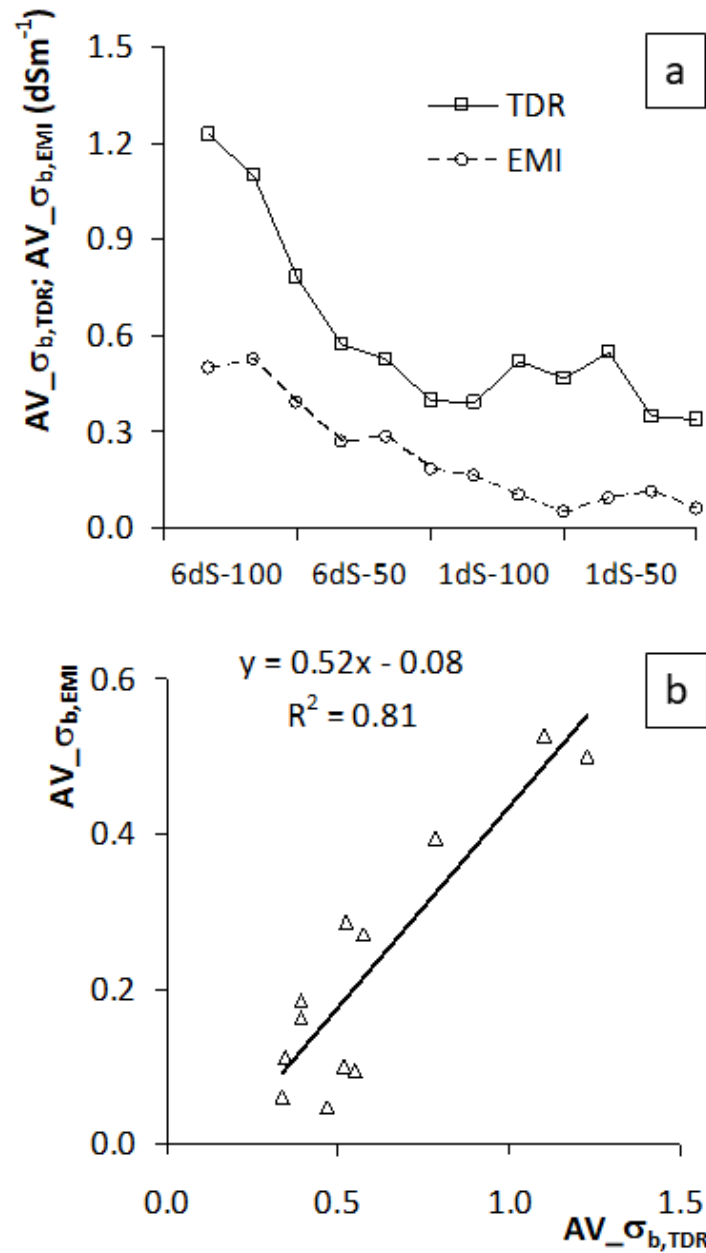


Figure 8. (a) Comparison of the means for the two original series (squares-solid line for TDR, dcircles-dashed line for EMI); (b) The same comparison on a 1:1 plot (triangles-solid regression line). In the panel (a), the four cases are shown in sequence. For each case, the three values are for the three depth intervals 0.0-0.2, 0.2-0.4, and 0.4-0.6 m.

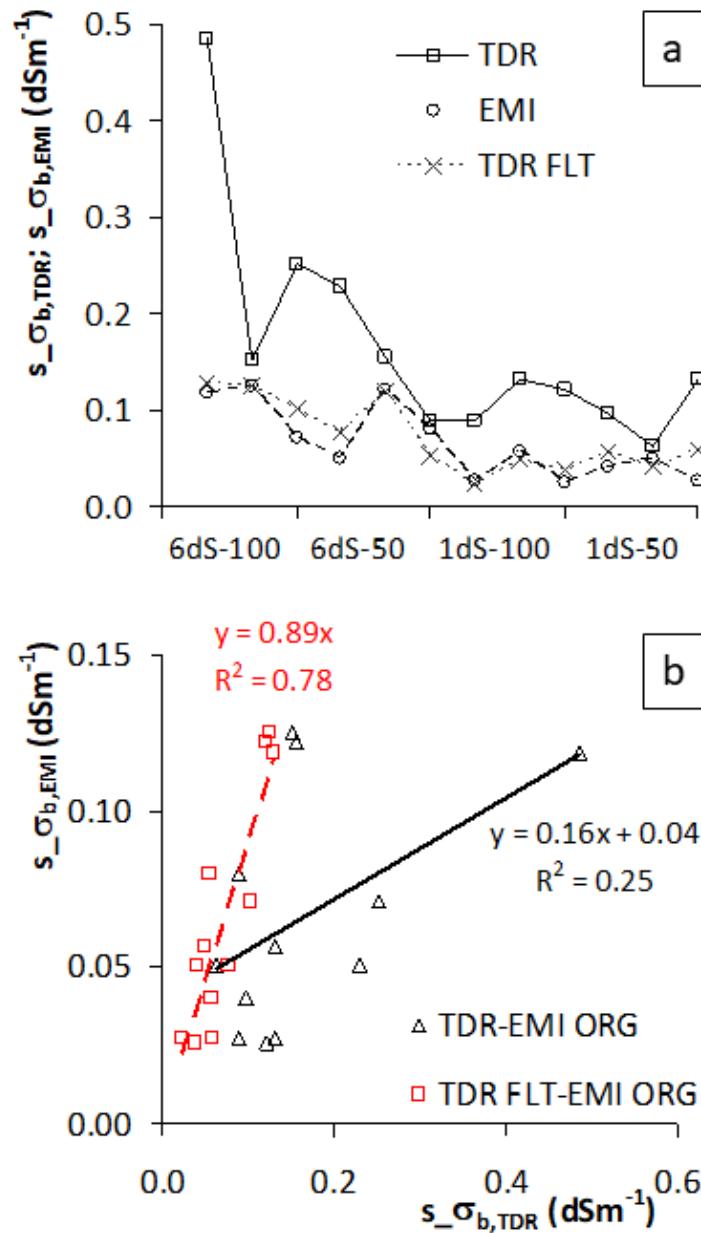


Figure 9. (a) Comparison of the standard deviations of the TDR original series (squares-solid line), of the EMI original series (circles-dashed line), and of the filtered (FLT) TDR series (crosses-dashed line); (b) The same comparison on a 1:1 plot: the original TDR and EMI data (triangles-solid regression line); filtered (FLT) TDR and original EMI data (squares-dashed regression line). In the panel (a), the four cases are shown in sequence. For each case, the three values are for the three depth intervals 0.0-0.2, 0.2-0.4, and 0.4-0.6 m.

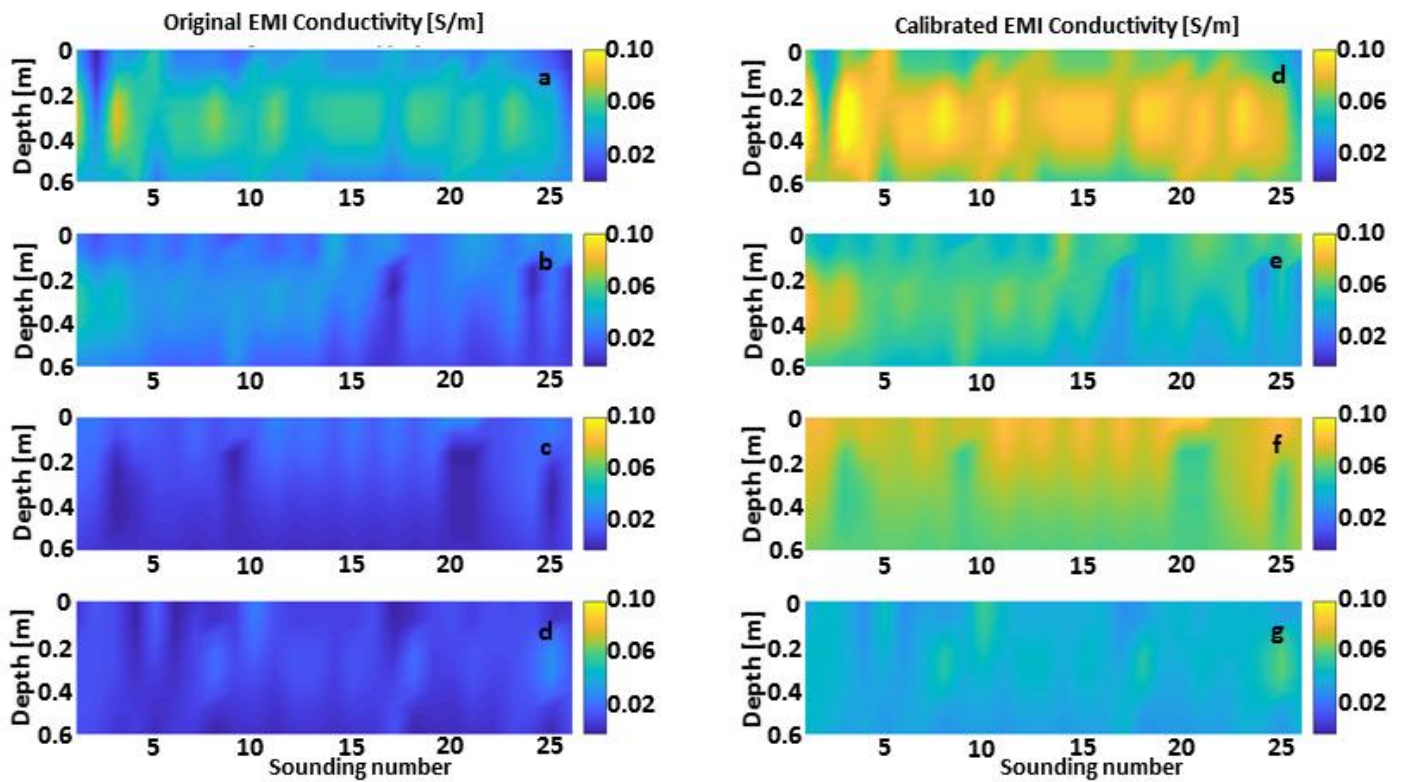


Figure 10. Maps of bulk electrical conductivity for the: (a) 100-6dS, (b) 50-6dS, (c) 100-1dS, (d) 50-1dS transects showing the original $\sigma_{b,EMI}$ resulting from the inversion of the observed EMI data. Panels (d) to (g) show instead the corresponding results after the calibration via the TDR measurements (i.e., by applying Eq. 10).

Transect	C_b	ρ_L	ρ_P	β	α
100-1dS	0.10	0.02	0.33	2.04	0.25
50-1dS	0.10	0.00	0.08	3.06	0.14
100-6dS	0.18	0.02	0.07	2.92	-0.21
50-6dS	0.34	0.08	0.32	1.84	0.04

Table 1. Concordance parameters for the four transects for the TDR_ORG and EMI_ORG data. The table reports the Concordance, ρ_L , and the Pearson, ρ_P , correlation, as well as parameters α and β of the MRA line. The bias factor, C_b , is also shown.

Transect	C_b	ρ_L	ρ_P	β	α
100-1dS	0.74	0.24	0.33	1.02	0.29
50-1dS	0.62	0.05	0.08	1.02	0.27
100-6dS	0.87	0.06	0.07	1.02	0.57
50-6dS	0.79	0.25	0.32	1.02	0.31

Table 2. Concordance parameters for the four transects for the TDR_FLT and EMI_ORG data. The table reports the Concordance, ρ_L , and the Pearson, ρ_P , correlation, as well as parameters α and β of the MRA line. The bias factor, C_b , is also shown.